Course 9

LR(k) Parsing (cont.)

LR(k) parsing: LR(0), SLR, LR(1), LALR

- Define item
- Construct set of states
- Construct table

Executed 1 time

Parse sequence based on moves between configurations

Algorithm *ColCan_LR(0)*

```
INPUT: G'- gramatica îmbogățită
OUTPUT: C - colecția canonică de stări
\mathcal{C} := \emptyset;
s_0 := closure(\{[S' 
ightarrow .S]\}) // state corresponding to prod. of S' = initial state
\mathcal{C} := \mathcal{C} \cup \{s_0\};
                                       //initialize collection with s<sub>0</sub>
repeat
   for \forall s \in \mathcal{C} do
      for \forall X \in N \cup \Sigma \ \mathbf{do}
         if goto(s, X) \neq \emptyset and goto(s, X) \notin \mathcal{C} then
                                          //add new state
            C = C \cup goto(s, X)
         end if
      end for
   end for
until \mathcal{C} nu se mai modifică
```

Algorithm *Closure*

```
INPUT: I-element de analiză; G'- gramatica îmbogățită
OUTPUT: C = closure(I);
C := \{I\};
                     //initialize Closure with the LR(0) item
repeat
   for \forall [A \to \alpha.B\beta] \in C do
                                        //search productions with dot in front of nonterminal
      for \forall B \rightarrow \gamma \in P do
                                       //search productions of that nonterminal
         if [B \rightarrow .\gamma] \notin C then
            C = C \cup [B \rightarrow .\gamma]
                                        //adds item formed from production with dot in
         end if
                                         //front of right hand side of the production
      end for
   end for
until C nu se mai modifică
```

Function *goto*

```
goto : P(\mathcal{E}_0) \times (N \cup \Sigma) \rightarrow P(\mathcal{E}_0) //creates new states where \mathcal{E}_0 = set of LR(0) items
```

goto(s, X) = closure(
$$\{[A \rightarrow \alpha X.\beta] | [A \rightarrow \alpha.X\beta] \in s\}$$
)

goto(s,X): in state s, search LR(0) item that has dot in front of symbol X. Move the dot after symbol X and call closure for this new item.

SLR Parser

• SLR = Simple LR

Prediction = next symbols on input sequence

Remark:

LR(0) – lots of conflicts – solved if considering prediction

=>

- 1. LR(0) canonical collection of states—prediction of length 0
- 2. Table and parsing sequence prediction of length 1

SLR Parsing:

- define item
- Construct set of states
- Construct table
- Parse sequence based on moves between configurations



Construct SLR table

Remarks:

- 1. Prediction = next symbol from input sequence => FOLLOW
 - see LL(1)
- 2. Structure LR(k):
 - Lines states
 - action + goto

action – a column for each prediction $\in \Sigma$ goto – a column for each symbol $X \in \mathbb{N} \cup \Sigma$ Optimize table structure: merge *action* and *goto* columns for Σ

Remark (LR(0) table):

- if s is accept state then goto(s, X) = \emptyset , \forall X \in N \cup Σ .
- If in state s action is reduce then goto(s, X) = \emptyset , \forall X \in N \cup Σ .

SLR table



	Action			GOTO		
	a ₁	•••	a _n	B ₁	•••	B _m
s_0						
s ₀						
•••						
S _k						

$$a_1,...,a_n \in \Sigma$$
 $B_1,...,B_m \in \mathbb{N}$
 $s_0,...,s_k$ - states

Rules for SLR table

- 1. If $[A \rightarrow \alpha.\beta] \in s_i$ and $goto(s_i,a) = s_j$ then $action(s_i,a) = shift s_j$ // dot is not at the end
- 2. if $[A \rightarrow \beta] \in s_i$ and $A \neq S'$ then **action(s_i,u)**=reduce I, where I number of production $A \rightarrow \beta$, $\forall u \in FOLLOW(A)$

//dot is at the end, but not for S'

- 3. if $[S' \rightarrow S.] \in s_i$ then **action**(s_i , \$)=acc // dot is at the end, prod. of S'
- 4. if goto(s_i , X) = s_j then goto(s_i , X) = s_j , $\forall X \in N$
- 5. otherwise **error**

Remarks

1. Similarity with LR(0)

2. A grammar is SLR if the SLR table does not contain conflicts (more than one value in a cell)

Parsing sequences

• INPUT:

- Grammar G' = (NU{S'}, Σ, P U {S'->S},S')
- SLR table
- Input sequence $w = a_1 ... a_n$

• OUTPUT:

```
if (w ∈L(G)) then string of productions
else error & location of error
```

SLR = LR(0) configurations

 (α, β, π)

Initial configuration: $(\$s_0, w\$, \varepsilon)$

where:

- α = working stack
- β = input stack
- π = output (result)

Final configuration: $(\$s_{acc}, \$, \pi)$

1. Shift

if
$$action(s_m,a_i) = shift s_j$$
 then
 $(\$s_0x_1 ...x_ms_m,a_i ...a_n\$, \pi) \vdash (\$s_0x_1 ...x_ms_ma_is_i,a_{i+1} ...a_n\$, \pi)$

2. Reduce

if $action(s_m, a_i) = reduce t AND (t) A \rightarrow x_{m-p+1} ... x_m AND goto(s_{m-p}, A) = s_j$ then

$$(\$s_0 ... x_m s_m, a_i ... a_n \$, \pi) \vdash (\$s_0 ... x_{m-p} s_{m-p} A s_j, a_i ... a_n \$, t \pi)$$

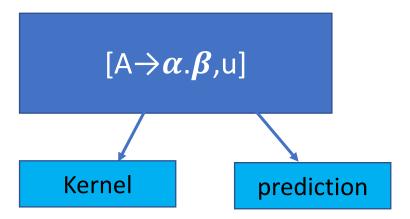
3. Accept

if $action(s_m,\$) = accept then (\$s_m,\$, \pi) = acc$

4. Error - otherwise

LR(1) Parser

- 1. Define item
- 2. Construct set of states
- 3. Construct table
- 4. Parse sequence based on moves between configurations



Construct LR(1) set of states

- Alg ColCan_LR1
- Function goto_LR1
- Alg Closure_LR1

Algorithm ColCan_LR1

```
INPUT: G' – enhanced grammar
OUTPUT: C_1 – cannonical collection of states
C_1 = \emptyset
S0 = Closure\_LR1([S' \rightarrow .S, \$])
C_1 := C_1 \cup \{s_0\}
Repeat
   for \forall s \in C_1 do
      for \forall X \in \mathbb{N} \cup \Sigma do
           T = goto_LR1(s,X)
           if T \neq \emptyset and T \notin C_1 then
                       C_1 = C_1 \cup T
           endif
      endfor
   endfor
Until C<sub>1</sub> unchanged
```

Function *goto_LR1*

Goto_LR1 : $P(\mathcal{E}_1) \times (N \cup \Sigma) \rightarrow P(\mathcal{E}_1)$ where \mathcal{E}_1 = set ofLR(1) items

$$Goto_{LR1}(s, X) = Closure_{LR1}(\{A \rightarrow \alpha X.\beta, u\} | [A \rightarrow \alpha.X\beta, u] \in s\})$$

Algorithm *Closure_LR1*

• [A $\rightarrow \alpha$.B β ,u] valid for live prefix $\gamma \alpha =>$

$$S \stackrel{*}{\Rightarrow}_{dr} \gamma Aw \Rightarrow_{dr} \gamma \alpha B\beta w$$
$$u = FIRST_k(w)$$

• [B
$$\rightarrow$$
 .8, smth] \in P => $S \stackrel{*}{\Rightarrow} \gamma Aw \Rightarrow_{dr} \gamma \alpha B\beta w \Rightarrow_{dr} \gamma \alpha \delta \beta w$.

Algorithm *Closure_LR1*

```
INPUT: I-element de analiză; G'- gramatica îmbogățită;
             FIRST(X), \forall X \in N \cup \Sigma;
OUTPUT: C_1 = \text{closure}(I);
C_1 := \{I\};
repeat
   for \forall [A \to \alpha.B\beta, a] \in C_1 do
      for \forall B \rightarrow \gamma \in P do
       for \forall b \in FIRST(\beta a) do
            if [B \to .\gamma, b] \not\in C_1 then C_1 = C_1 \cup [B \to .\gamma, b]
            end if
         end for
      end for
   end for
until C_1 nu se mai modifică
```

Construct LR(1) table

- Structure SLR
- Rules:
- 1. if $[A \rightarrow \alpha.\beta,u] \in s_i$ and $goto(s_i,a) = s_j$ then $action(s_i,a) = shift s_j$
- 2. if $[A \rightarrow \beta, u] \in s_i$ and $A \neq S'$ then **action(s_i, u)**=reduce I, where I number of production $A \rightarrow \beta$
- 3. if $[S' \rightarrow S., \$] \in s_i$ then $action(s_i, \$) = acc$
- 4. if goto(s_i , X) = s_j then goto(s_i , X) = s_j , $\forall X \in \mathbb{N}$
- 5. otherwise = **error**

Remarks

1. A grammar is LR(1) if the LR(1) table does not contain conflicts

2. Number of states – significantly increase

4. Define configurations and moves

• INPUT:

- Grammar G' = (NU{S'}, Σ, P U {S'->S},S')
- LR(1) table
- Input sequence $w = a_1 ... a_n$

• OUTPUT:

```
if (w ∈L(G)) then string of productions
else error & location of error
```

LR(1) configurations

 (α, β, π)

where:

- α = working stack
- β = input stack
- π = output (result)

Initial configuration: $(\$s_0, w\$, \varepsilon)$

Final configuration: $(\$s_{acc}, \$, \pi)$

1. Shift

if
$$action(s_m, a_i) = shift s_j$$
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2. Reduce

if $action(s_m, a_i) = reduce t AND (t) A \rightarrow x_{m-p+1} ... x_m AND goto(s_{m-p}, A) = s_j$ then

$$(\$s_0 ... x_m s_m, a_i ... a_n \$, \pi) \vdash (\$s_0 ... x_{m-p} s_{m-p} A s_j, a_i ... a_n \$, t \pi)$$

3. Accept

if $action(s_m,\$) = accept then (\$s_m,\$, \pi) = acc$

4. Error - otherwise

LALR Parser

• LALR = Look Ahead LR(1)

• why?

LALR principle

$$[A \rightarrow \alpha \beta., u] \in s_i$$
 apply reduce (k) then goto(s_i , A) = s_m $[A \rightarrow \alpha \beta., v] \in s_j$ apply reduce (k) then goto(s_j , A) = s_n

$$[A \rightarrow \alpha.\beta,u] \in s_i$$

$$=> [A \rightarrow \alpha.\beta,u | v] \in s_{i,j}$$

$$[A \rightarrow \alpha.\beta,v] \in s_j$$

Merge states with the same kernel, conserving all predictions, if no conflict is created

LALR Parsing

- Same as LR(1)
- Number of LALR states = number of SLR / LR(0) states

• How? - LR(1) states

LR(k) Parsers

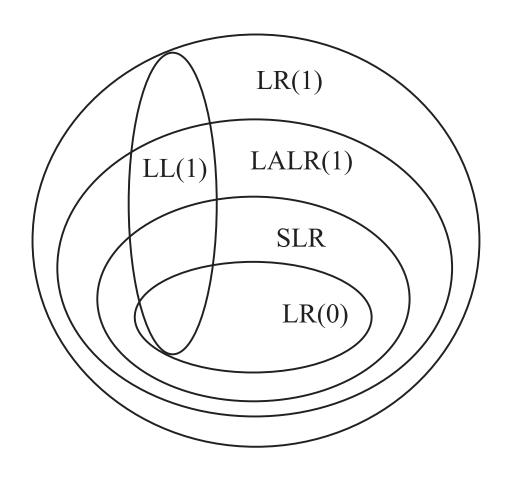
- LR(0):
 - Items ignore prediction
 - Reduce can be applied only in singular states (contain one item)
 - Lot of conflicts
- SLR:
 - Use same items as LR(0)
 - When reduce consider prediction
 - Eliminate several LR(0) conflicts (not all)
- LR(1):
 - Performant algorithm for set of states
 - Generate few conflicts
 - Generate lot of states
- LALR:
 - Merge LR(1) states corresponding to same kernel
 - Most used algorithm (most performant)

Quiz time

Parsing - recap

	Descendent	Ascendent
Recursive	Descendent recursive	Ascendent recursive parser
	parser	
Linear	LL(1)	LR(0), SLR, LR(1), LALR

Parsing - recap



Structure of compiler

