FINC-672 – WORKSHOP IN FINANCE: EMPIRICAL RESEARCH

JULIA DATA STRUCTURES

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GOALS

Broadcasting Operators and Functions
String
Tuple, NamedTuple
UnitRange,
Array
Pair, Dict

BROADCASTING

- \bullet For mathematical operations, like * (multiplication) or + (addition), we can broadcast it using the dot operator .
- For example, broadcasted addition would imply in changing the + to .+

```
julia> [1, 2, 3] .+ 1
3-element Vector{Int64}:
2
3
4
```

BROADCASTING

- It also works with functions automatically.
- Let's use the logarithm function.

```
julia> log.([1, 2, 3])
3-element Vector{Float64}:
0.0
0.6931471805599453
1.0986122886681098
```

COMPREHENSIONS

- It is often useful to use a *comprehension* as a basic programming construct.
- A typical form of a comprehension is.

```
[f(x) \text{ for } x \text{ in } A]
```

• For example

```
julia> [(2n+1)^2 for n in 1:5]
5-element Vector{Int64}:
    9
    25
    49
    81
121
```

STRINGS

• Strings are represented delimited by double quotes.

```
julia> typeof("This is a string")
String
```

STRINGS

• We can also write a multiline string.

```
julia> text = "
This is a big multiline string.
As you can see.
It is still a String to Julia.
";
julia> println(text)
This is a big multiline string.
As you can see.
It is still a String to Julia.
```

STRINGS

• But, it is, typically, more clear to use triple quotation marks.¹

```
julia> s = """
    This is a big multiline string with a nested "quotation".
    As you can see.
    It is still a String to Julia.
    """;

julia> println(s)
This is a big multiline string with a nested "quotation".
As you can see.
It is still a String to Julia.
```

¹When using triple-backticks, the indentation and newline at the start is ignored by Julia. This improves code readability because you can indent the block in your source code without those spaces ending up in your string.

STRING CONCATENATION

- A common string operation is **string concatenation**.
- Suppose that you want to construct a new string that is the concatenation of two or more strings.
- This is accomplished in julia either with the * operator or the join function.

```
julia> hello = "Hello";
julia> goodbye = "Goodbye";
julia>
hello * goodbye
"HelloGoodbye"
```

STRING CONCATENATION (CONT'D)

- As you can see, we are missing a space between hello and goodbye.
- We could concatenate an additional " " string with the *, but that would be cumbersome for more than two strings.
- That's when the join function is useful.
- We just pass as arguments the strings inside the brackets [] and the separator.

```
julia> join([hello, goodbye], " ")
"Hello Goodbye"
```

STRING INTERPOLATION

- Concatenating strings can be convoluted.
- We can be much more expressive with **string interpolation**.
- It works like this: you specify whatever you want to be included in your string with the dollar sign \$.
- Here's the example before but now using interpolation.

```
julia> s = "$hello $goodbye"
"Hello Goodbye"
```

STRING INTERPOLATION (CONT'D)

• It works even inside functions. Let's create a function to illustrate the idea.

```
julia> function test_interpolated(a, b)
   if a < b
        "$a is less than $b"
    elseif a > b
        "$a is greater than $b"
    else
        "$a is equal to $b"
    end
end:
iulia>
test interpolated (3.14, 3.14)
"3.14 is equal to 3.14"
```

STRING MANIPULATIONS

- There are several functions to manipulate strings in Julia. We will demonstrate the most common ones.
- Also, note that most of these functions accepts a Regular Expression (RegEx) as arguments.
- We won't cover RegEx in this course, but you are encouraged to learn about them, especially if most of your work uses textual data.
- First, let us define a string for us to work with.

julia> julia_string = "Julia is an amazing opensource programming language"
"Julia is an amazing opensource programming language"

STRING MANIPULATIONS (CONT'D)

- 1. occursin, startswith and endswith: A conditional (returns either true or false) if the first argument is a.
 - substring of the second argument
 - **prefix** of the second argument
 - suffix of the second argument

```
julia> occursin("Julia", julia_string)
true

julia> startswith("Julia", julia_string)
false

julia> endswith("Julia", julia_string)
false
```

STRING MANIPULATIONS (CONT'D)

• 2. lowercase, uppercase, titlecase and lowercasefirst.

```
julia> lowercase(julia string)
"julia is an amazing opensource programming language"
julia> uppercase(julia string)
"III TA TS AN AMAZING OPENSOURCE PROGRAMMING LANGUAGE"
iulia> titlecase(julia string)
"Julia Is An Amazing Opensource Programming Language"
iulia> lowercasefirst(iulia string)
"julia is an amazing opensource programming language"
```

STRING MANIPULATIONS (CONT'D)

- 3. replace: introduces a new syntax, called the Pair
- 4. split: breaks up a string by a delimiter.

```
julia> replace(julia string, "amazing" => "awesome")
"Julia is an awesome opensource programming language"
julia> split(julia string, " ")
7-element Vector{SubString{String}}:
 "Julia"
"is"
"an"
"amazing"
"opensource"
"programming"
 "language"
```

STRING CONVERSIONS

- Often, we need to convert between types in Julia.
- We can use the string function.

```
julia> my_number = 123;
julia> typeof(string(my_number))
String
```

- Sometimes, we want the opposite: convert a string to a number.
- Julia has a handy function for that: parse

```
julia> typeof(parse(Int64, "123"))
Int64
```

STRING CONVERSIONS (CONT'D)

- Sometimes, we want to play safe with these convertions.
- That's when tryparse function steps in.
- It has the same functionality as parse but returns either a value of the requested type, or nothing.
- That makes tryparse handy when we want to avoid errors.
- Of course, you would need to deal with all those nothing values afterwards.

julia> tryparse(Int64, "A very non-numeric string")

TUPLES

- Julia has a data structure called **tuple**. They are really *special* in Julia because they are often used in relation to functions.
- A tuple is a fixed-length container that can hold multiple different types.
- A tuple is an **imutable object**, meaning that it cannot be modified after instantiation.
- To construct a tuple, use parentheses () to delimitate the beginning and end, along with commas , as value's delimiters.

TUPLES (CONT'D)

```
julia> my_tuple = (1, 3.14, "Julia")
(1, 3.14, "Julia")
```

- Here, we are creating a tuple with three values.
- Each one of the values is a different type. We can access them via indexing.

```
julia> my_tuple[2]
3.14
```

- We can also loop over tuples with the **for** keyword. And even apply functions to tuples.
- But we can **never change any value of a tuple** since they are **immutable**.

TUPLES (CONT'D)

- Recall that functions can return multiple values.
- Let's inspect what our add_multiply function returns.

```
julia> function add multiplv(x, y)
    addition = x + y
    multiplication = x * v
    return addition, multiplication
end;
iulia>
return_multiple = add multiply(1, 2)
(3, 2)
julia> typeof(return multiple)
Tuple{Int64, Int64}
  • This is because return a, b is the same as return (a, b).
```

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TUPLES (CONT'D)

- One more thing about tuples.
- When you want to pass more than one variable to an anonymous function, what would you need to use?
- Answer: tuples

```
julia> map((x, y) -> x^y, 2, 3)
8
```

• Or, even more than two arguments.

```
julia> map((x, y, z) -> x^y + z, 2, 3, 1)
```

NAMED TUPLE

- Sometimes, you want to name the values in tuples. That's when **named tuples** comes in.
- Their functionality is pretty much same the same as tuples. they are **immutable** and can hold **any type of value**.
- Named tuple's construction are slightly different from tuples.
- You have the familiar parentheses () and comma , value separator.
- But now you name the values.

```
julia> my_namedtuple = (i=1, f=3.14, s="Julia")
(i = 1, f = 3.14, s = "Julia")
```

NAMED TUPLE (CONT'D)

• We can access a named tuple's values via indexing like regular tuples or, alternatively, **access by their names** with .

```
julia> my_namedtuple.s
"Julia"
```

NAMED TUPLE (CONT'D)

- Often Julia users create a named tuple by using the familiar parenthesis () and commas ,, but without naming the values.
- To do so you begin the named tuple construction by specifying first a semicolon; before the values.
- This is especially useful when the values that would compose the named tuple are already defined in variables or when you want to avoid long lines.

```
julia> i = 1;
julia> f = 3.14;
julia> s = "Julia";
julia>
my_quick_namedtuple = (; i, f, s)
(i = 1, f = 3.14, s = "Julia")
```

RANGES

- A range in Julia represents an interval between a start and stop boundaries.
- The syntax is start:stop

```
julia> 1:10
1:10
```

• As you can see, our instantiated range is of type <code>UnitRange{T}</code> where <code>T</code> is the type inside the <code>UnitRange</code>.

```
julia> typeof(1:10)
UnitRange{Int64}
```

RANGES (CONT'D)

• And, if we gather all the values, we get.

```
julia> [x for x in 1:10]
10-element Vector{Int64}:
 10
```

RANGES (CONT'D)

• We can construct ranges also for other types:

```
julia> typeof(1.0:10.0)
StepRangeLen{Float64, Base.TwicePrecision{Float64}, Base.TwicePrecision{Float64}}
```

- Sometimes, we want to change the default interval stepsize behavior.
- We can do that by adding a stepsize in the range syntax start:step:stop.
- For example, suppose we want a range of Float64 from 0 to 1 with steps of size 0.2.

```
julia> 0.0:0.2:1.0
0.0:0.2:1.0
```

- If you want to "materialize" a **UnitRange** into a collection, you can use the function **collect**.
- We have an array of the type specified in the **UnitRange** between the boundaries that we've set.

ARRAYS

- Arrays are a **systematic arrangement of similar objects**, usually in *rows* and *columns*.
- Let's start with arrays types. There are several, but we will focus on two.
 - Vector{T}: one-dimensional array. Alias for Array{T, 1}.
 - Matrix{T}: two-dimensional array. Alias for Array{T, 2}.
- For example, Vector{Int64} is a Vector which all elements are Int64s and Matrix{AbstractFloat} is a Matrix which all elements are subtypes of AbstractFloat.
- Most of the time, especially when dealing with tabular data, we are using either one- or two-dimensional arrays.
- We can use the aliases **Vector** and **Matrix** for clear and concise syntax.

²Note here that T is the type of the underlying array.

ARRAY CONSTRUCTION

- How do we construct an array? The simplest answer is to use the *default* constructor.
- It accepts the element type as the type parameter inside the {} brackets and inside the constructor you pass the element type followed by the dimensions.
- It is common to initialize vector and matrices with undefined elements by using the undef argument for type.

• For example, a vector of 10 undef Float64 elements can be constructed as.

```
julia> my vector = Vector{Float64}(undef, 10)
10-element Vector{Float64}:
2.379519675e-315
2.37951999e-315
1.675265855e-315
2.379520307e-315
2.379520465e-315
2.37952078e-315
2.37952094e-315
2.3795211e-315
2.33538167e-315
0.0
```

- For matrices, we need to pass two dimensions arguments inside the constructor: one for **rows** and another for **columns**.
- For example, a matrix with 10 rows, 2 columns is instantiated as.

```
iulia> my matrix = Matrix{Float64}(undef, 10, 2)
10×2 Matrix{Float64}:
2.29504e-315 1.19738e-315
2.29504e-315 2.29505e-315
2.29504e-315 1.19739e-315
2.29504e-315 1.19738e-315
2.29504e-315 1.19739e-315
2.29504e-315 1.19739e-315
2.29504e-315 2.29505e-315
2.29504e-315 2.29505e-315
2.29504e-315 2.29505e-315
 1.19739e-315 1.1974e-315
```

- We also have some **syntax aliases** for the most common elements in array construction.
- zeros for all elements being initialized to value zero.

```
julia> my vector zeros = zeros(10)
10-element Vector{Float64}:
0.0
0.0
0.0
0.0
0.0
0.0
0.0
0.0
0.0
 \Theta. \Theta
```

```
julia> my_matrix_zeros = zeros(Int64, 10, 2)
10×2 Matrix{Int64}:
0    0
0    0
0    0
0    0
0    0
0    0
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0    0
0    0
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0    0
0
```

• ones for all elements being initialized to value one.

```
julia> my matrix ones = ones(10, 2)
10×2 Matrix{Float64}:
1.0 1.0
1.0 1.0
1.0 1.0
1.0 1.0
1.0 1.0
1.0 1.0
1.0 1.0
1.0 1.0
1.0 1.0
1.0 1.0
```

- For other elements we can first intantiate an array with undef elements and use the fill! function to fill all elements of an array with the desired element.
- Here's an example with 3.14 (π) .

```
julia> my_matrix_π = Matrix{Float64}(undef, 2, 2);
julia> fill!(my_matrix_π, 3.14)
2×2 Matrix{Float64}:
3.14 3.14
3.14 3.14
```

- We can also create arrays with arrays literals.
- For example a 2x2 matrix of integers.

```
julia> [[1 2]
[3 4]]
2×2 Matrix{Int64}:
    1    2
    3    4
```

- Array literals also accept a type specification before the [] brackets.
- So, if we want the same 2x2 array as before but now as floats, we can do so.

```
julia> Float64[[1 2]
        [3 4]]
2×2 Matrix{Float64}:
1.0 2.0
3.0 4.0
```

• It also works for vectors.

```
julia> Bool[0, 1, 0, 1]
4-element Vector{Bool}:
0
1
0
1
```

• You can even **mix and match** array literals with the constructors.

```
julia> [ones(Int, 2, 2) zeros(Int, 2, 2)]
2×4 Matrix{Int64}:
julia> [zeros(Int, 2, 2)
ones(Int, 2, 2)1
4×2 Matrix{Int64}:
   0
```

ARRAY COMPREHENSIONS

- Another powerful way to create arrays are **array comprehensions**.
- You specify what you want to do inside the [] brackets.
- For example, say we want to create a vector of squares from 1 to 100.

```
julia> [x^2 \text{ for } x \text{ in } 1:10]
10-element Vector{Int64}:
  16
  25
  36
  49
  64
  81
 100
```

ARRAY COMPREHENSIONS (CONT'D)

• They also support multiple inputs.

```
julia> [x*y for x in 1:7 for y in 1:2]
14-element Vector{Int64}:
 10
```

ARRAY COMPREHENSIONS (CONT'D)

• And conditionals.

```
julia> [x^2 for x in 1:10 if isodd(x)]
5-element Vector{Int64}:
    1
    9
25
49
81
```

ARRAY COMPREHENSIONS (CONT'D)

• As with array literals you can specify your desired type before the [] brackets.

```
julia> Float64[x^2 for x in 1:10 if isodd(x)]
5-element Vector{Float64}:
    1.0
    9.0
25.0
49.0
81.0
```

ARRAY CONCATENATION

- Finally, we can also create arrays with **concatenation functions**.
- cat: concatenate input arrays along a specific dimension dims

```
julia> cat(ones(2), zeros(2), dims=1)
4-element Vector{Float64}:
1.0
1.0
0.0
0.0

julia> cat(ones(2), zeros(2), dims=2)
2×2 Matrix{Float64}:
1.0 0.0
1.0 0.0
```

ARRAY CONCATENATION (CONT'D)

• vcat: vertical concatenation, a shorthand for cat(...; dims=1)

```
julia> vcat(ones(2), zeros(2))
4-element Vector{Float64}:
1.0
1.0
0.0
0.0
```

ARRAY CONCATENATION (CONT'D)

• hcat: horizontal concatenation, a shorthand for cat(...; dims=2)

```
julia> hcat(ones(2), zeros(2))
2×2 Matrix{Float64}:
1.0  0.0
1.0  0.0
```

ARRAY INSPECTION

- Once we have arrays, the next logical step is to inspect them.
- There are a lot of handy functions that allows the user to have an inner insight into any array.
- It is most useful to know what *type of elements* are inside an array.
- We can do this with eltype:

```
julia> eltype(my_matrix_π)
Float64
```

ARRAY INSPECTION (CONT'D)

- size is a little tricky.
- By default it will return a tuple containing the array's dimensions.

```
julia> size(my_matrix_π)
(2, 2)
```

You can get a specific dimension with a second argument to size

```
julia> size(my_matrix_π, 2) # columns
```

ARRAY INDEXING AND SLICING

- Sometimes we want to only inspect certain parts of an array.
- This is called **indexing** and **slicing**.
- If you want a particular observation of a vector, or a row or column of a matrix; you'll probably need to *index an array*.
- First, let's create an example vector and matrix.

- Let's see first an example with vectors.
- Suppose you want the second element of a vector.
- You append [] brackets with the desired **index** inside.

```
julia> my_example_vector[2]
2
```

- The same syntax follows with matrices.
- But, since matrices are 2-dimensional arrays, we have to specify **both** rows and columns.
- Let's retrieve the element from the second row (first dimension) and first column (second dimension).

```
julia> my_example_matrix[2, 1]
4
```

- Julia also have conventional keywords for the first and last elements of an array: begin and end.
- For example, the second to last element of a vector can be retrieved as.

```
julia> my_example_vector[end-1]
```

- It also works for matrices.
- Let's retrieve the element of the last row and second column.

```
julia> my_example_matrix[end, begin+1]
8
```

- Often, we are not only interested in just one array element, but in a whole subset of array elements.
- We can accomplish this by **slicing** an array.
- It uses the same index syntax, but with the added colon: to denote the boundaries that we are slicing through the array.
- For example, suppose we want to get the 2nd to 4th element of a vector.

```
julia> my_example_vector[2:4]
3-element Vector{Int64}:
2
3
4
```

- We could do the same with matrices.
- Particularly with matrices if we want to select all elements in a following dimension we can do so with just a colon:
- For example, all elements in the second row.

```
julia> my_example_matrix[2, :]
3-element Vector{Int64}:
4
5
6
```

- You can interpret this with something like "take 2nd row and all columns".
- It also supports begin and end.

```
julia> my_example_matrix[begin+1:end, end]
2-element Vector{Int64}:
6
9
```

ARRAY MANIPULATION

- There are several ways we could manipulate an array.
- The first would be to manipulate a **singular element** of the array.
- We just index the array by the element and proceed with an assignment =

ARRAY MANIPULATION

- Or you can manipulate a certain **subset** of elements of the array.
- In this case, we need to slice the array and then assign with =

```
julia> my_example_matrix[3, :] = [17, 16, 15];
julia> my_example_matrix
3×3 Matrix{Int64}:
    1    2    3
    4    42    6
    17    16    15
```

• Note that we had to assign a vector because we our sliced array is of type **Vector**.

```
julia> typeof(my_example_matrix[3, :])
Vector{Int64} (alias for Array{Int64, 1})
```

- The second way we could manipulate an array is to alter its shape.
- Suppose you have a 6-element vector and you want to make it a 3x2 matrix.
- You can do so with reshape, by using the array as first argument and a tuple of dimensions as second argument.

```
julia> six_vector = [1, 2, 3, 4, 5, 6];
julia> tree_two_matrix = reshape(six_vector, (3, 2));
julia> tree_two_matrix
3×2 Matrix{Int64}:
    1     4
    2     5
    3     6
```

• You can do the reverse, convert it back to a vector, by specifying a tuple with only one dimension as second argument.

```
julia> reshape(tree_two_matrix, (6, ))
6-element Vector{Int64}:
    1
    2
    3
    4
    5
    6
```

- The third way we could manipulate an array is to apply a function over every array element.
- This is where the familiar broadcasting "dot" operator . comes in.

```
julia> log.(my_example_matrix)
3×3 Matrix{Float64}:
0.0     0.693147   1.09861
1.38629   3.73767   1.79176
2.83321   2.77259   2.70805
```

• We can broadcast operators.

```
julia> my_example_matrix .+ 100
3×3 Matrix{Int64}:
    101    102    103
    104    142    106
    117    116    115
```

• We can use also map to apply a function to every element of an array.

```
julia> map(log, my_example_matrix)
3×3 Matrix{Float64}:
0.0     0.693147    1.09861
1.38629    3.73767    1.79176
2.83321    2.77259    2.70805
```

• It also accepts an anonymous function.

```
julia> map(x -> x*3, my_example_matrix)
3×3 Matrix{Int64}:
3    6    9
12    126    18
51    48    45
```

• It also works with slicing.

```
julia> map(x -> x + 100, my_example_matrix[:, 3])
3-element Vector{Int64}:
103
106
115
```

- Finally, sometimes, and specially when dealing with tabular data, we want to apply a function over all elements in a specific array dimension.
- This can be done with the mapslices function.
- Similar to map, the first argument is the function and the second argument is the array.
- The only change is that we need to specify the dims argument to flag what dimension we want to transform the elements.
- For example let's use mapslice with the sum function on both rows (dims=1) and columns (dims=2).

```
julia> mapslices(sum, my_example_matrix; dims=1)
1×3 Matrix{Int64}:
22 60 24

julia> mapslices(sum, my_example_matrix; dims=2)
3×1 Matrix{Int64}:
6
52
48
```

ARRAY ITERATION

- One common operation is to iterate over an array with a **for** loop.
- The regular for loop over an array returns each element.

```
julia> simple vector = [1, 2, 3];
julia> empty vector = Int64[];
iulia>
for i in simple vector
    push!(empty vector, i + 1);
end
iulia>
empty vector
3-element Vector{Int64}:
```

ARRAY ITERATION (CONT'D)

- Sometimes you don't want to loop over each element, but actually over each array index.
- We can the eachindex function combined with a for loop to iterate over each array index.
- Let's look at an example on the next slide.

ARRAY ITERATION (CONT'D)

```
julia> forty two vector = [42, 42, 42];
julia> empty vector = Int64[];
julia>
for i in eachindex(forty_two_vector)
    push!(empty vector, i)
end
iulia>
empty vector
3-element Vector{Int64}:
```

• In the last example the eachindex(forty_two_vector) iterator inside the for loop returns not forty_two_vector's values but its indices: [1, 2, 3].

- Iterating over matrices involves more details.
- The standard for loop goes first over columns then over rows.
- It will first traverse all elements in column 1, from the first row to the last row, then it will move to column 2 in a similar fashion until it has covered all columns.³
- Let's show this in an example.

³Those familiar with other programming languages, Julia, like most scientific programming languages, is "column-major". This means that arrays are stored contiguously using a column orientation.

• Example continues on next slide.

```
julia> for i in column_major
    push!(empty_vector, i)
end;

julia>
empty_vector
4-element Vector{Int64}:
    1
    3
    2
    4
```

```
julia> empty vector = Int64[];
julia>
for i in row major
    push!(empty vector, i)
end;
julia>
empty vector
4-element Vector{Int64}:
```

- There are some handy functions to iterate over matrices.
- eachcol: iterates over an array column first
- eachrow: iterates over an array row first

```
julia> first(eachcol(column_major))
2-element view(::Matrix{Int64}, :, 1) with eltype Int64:
    1
    3

julia> first(eachrow(column_major))
2-element view(::Matrix{Int64}, 1, :) with eltype Int64:
    1
    2
```

PAIRS

- Pair is a data structure that holds two types.
- How we construct a pair in Julia is using the following syntax.

```
julia> my_pair = Pair("Julia", 42)
"Julia" => 42
```

• Alternatively, we can create a pair by specifying both values and in between we use the pair '=>' operator.

```
julia> my_pair = "Julia" => 42
"Julia" => 42
```

PAIRS (CONT'D)

• The elements are stored in the fields first and second.

```
julia> my_pair.first
"Julia"

julia> my_pair.second
42
```

DICT

- Dict in Julia is just a "hash table" with pairs of key and value.
- keys and values can be of any type, but generally you'll see keys as strings.
- There are two ways to construct **Dict**s in Julia.
- The first is using the default constructor **Dict** and passing a vector of tuples composed of (key, value).

```
julia> my_dict = Dict([("one", 1), ("two", 2)])
Dict{String, Int64} with 2 entries:
    "two" => 2
    "one" => 1
```

- The second way of constructing **Dicts** is more elegant because it has a more expressive syntax.
- You use the same default constructor **Dict**, but now you pass pairs of key and value.

```
julia> my_dict = Dict("one" => 1, "two" => 2)
Dict{String, Int64} with 2 entries:
  "two" => 2
  "one" => 1
```

• You can retrieve a **Dicts** value by indexing it by the corresponding key.

```
julia> my_dict["one"]
1
```

• Similarly, to add a new entry you index the **Dict** by the desired **key** and assign a **value** with the assignment = operator.

```
julia> my_dict["three"] = 3
3
```

• If you want to check if a **Dict** has a certain key you can use the haskey function.

```
julia> haskey(my_dict, "two")
true
```

• To delete a key you can use either the delete! function.

```
julia> delete!(my_dict, "three")
Dict{String, Int64} with 2 entries:
   "two" => 2
   "one" => 1
```

• Or to delete a key while retuning its value you can use the pop! function.

```
julia> popped_value = pop!(my_dict, "two")
2
```

• Now our my_dict has only one key.

```
julia> length(my_dict)
1
julia> my_dict
Dict{String, Int64} with 1 entry:
   "one" => 1
```

- There is one useful **Dict** constructor that we use a lot.
- Suppose you have two vectors and you want to construct a Dict with one of them as keys and the other as values.
- You can do that with the zip function which "glues" together two objects just like a zipper.

```
julia> A = ["one", "two", "three"];
julia> B = [1, 2, 3];
julia>
dic = Dict(zip(A, B))
Dict{String, Int64} with 3 entries:
    "two" => 2
    "one" => 1
    "three" => 3
```

• For instance, we can now get the number 3 via.

```
julia> dic["three"]
3
```

SPLAT OPERATOR

- In Julia we have the "splat" operator ... which is mainly used in function calls as a **sequence of arguments**.
- The most intuitive way to learn about splatting is with an example.
- The add_elements function below takes three arguments to be adeed together.

```
julia> add_elements(a, b, c) = a + b + c;
```

SPLAT OPERATOR (CONT'D)

- Now suppose that I have a collection with three elements.
- The naïve way to this would be to supply the function with all three elements as function arguments like this.

```
julia> my_collection = [1, 2, 3];
julia>
add_elements(my_collection[1], my_collection[2], my_collection[3])
6
```

SPLAT OPERATOR (CONT'D)

• Here is where we use the "splat" operator . . . which takes a collection (often an array, vector, tuple or range) and converts into a sequence of arguments.

```
julia> add_elements(my_collection...) # and splat!
```

- The ... is included after the collection that we want to "splat" into a sequence of arguments.
- In the example above, syntactically speaking, the following are the same.

```
collection = [x, y, z]
function(collection...) = function(x, y, z)
```

SPLAT OPERATOR (CONT'D)

- Anytime Julia sees a splatting operator inside a function call, it will be converted on a sequence of arguments for all elements of the collection separated by commas.
- It also works for ranges.

```
julia> add_elements(1:3...) # and splat!
6
```

WRAP-UP

- ✓ Broadcasting Operators and Functions
- **String**
- ✓ Tuple, NamedTuple
- ✓ UnitRange,
- **✓** Array
- **✓** Pair, Dict