

present

UD/ISCTE-IUL Trading and Bloomberg Program

Fixed Income Securities

U.S. Treasury Securities Market

Summer 2022

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Table of Contents

Overview

The U.S. Treasury Market

Types of Treasury Securities

Treasury Bill (T-bill)

Treasury Note (T-Note)

Treasury Bond (T-Bond)

Example of Treasury Note Cash Flows

Treasury Floating Rate Note (FRN)

Treasury STRIPS

Treasury Inflation Protected Securities (TIPS)

Indexing Bonds to Inflation

U.S. Consumer Price Index

TIPS Inflation Adjustment Details

Deflation Protection

Inflation-Adjusted Coupon Interest

Inflation-Adjusted Coupon Interest Example

Inflation Derivatives

Inflation Swap Basics

Inflation Swap Cash Flows

Inflation Swap Example

Reading

Overview

Our goals for today

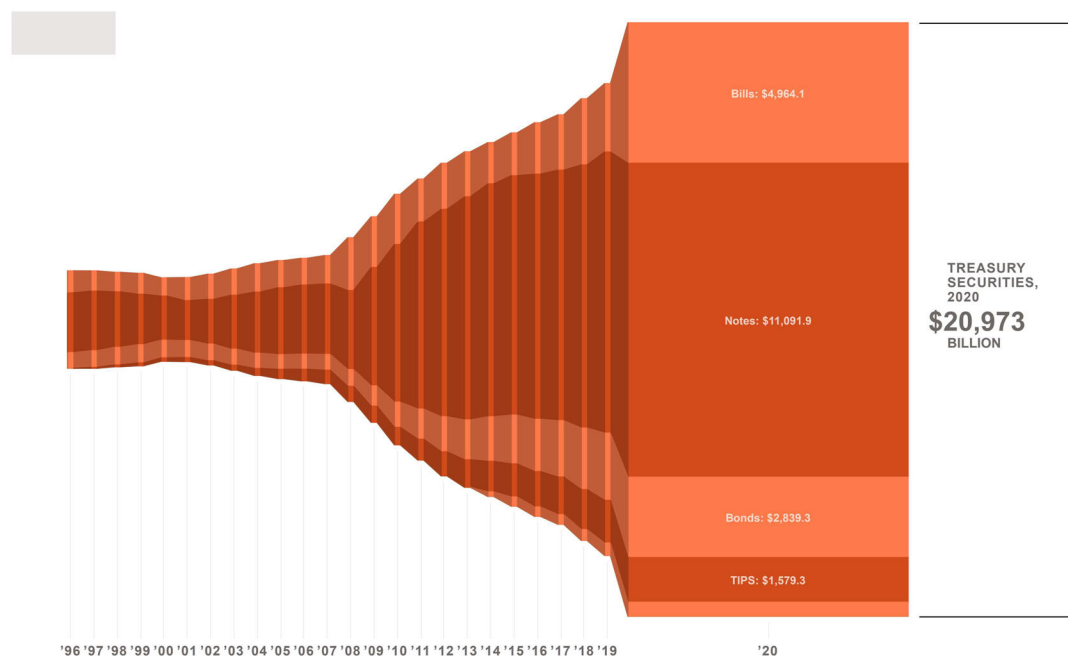
- ☐ Introduction to the U.S. Treasury Securities Market
- ☐ Treasury Bills
- ☐ Treasury Notes and Bonds
- ☐ Treasury STRIPS
- ☐ Treasury TIPS
- ☐ Inflation Swaps

The U.S. Treasury Market

- The Department of the Treasury is the largest single issuer of debt in the world.
- The large volume of total debt and the large size of any single issue have contributed to making the Treasury market the most active and hence the most liquid market in the world

[SIFMA Fixed Income Statistics](#)

U.S. Treasury Debt Amount Outstanding



[Link to SIFMA](#)

Types of Treasury Securities

- Where to get information about U.S. Treasury securities?
- Go to webpage of the [U.S. Treasury](#).
- In the middle panel, click on Treasury securities Overview.

1099 Questions? WE HAVE ANSWERS

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- ▶ [Interest rates for Series EE](#)
- ▶ [Interest rates for Series I](#)
- ▶ [How to buy Series EE](#)
- ▶ [How to buy Series I](#)
- ▶ [Gift savings bonds](#)
- ▶ [More ...](#)

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- ▶ [Treasury securities Overview](#)
- ▶ [How Treasury auctions work](#)
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- ▶ [Auction Announcements and Results](#)
- ▶ [Record-setting auction data](#)
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Try Treasury Hunt to search for matured bonds and held interest payments. Also, see the [Matured Unredeemed Debt \(MUD\) Report](#).

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[Home](#) > [Institutional](#) > [Treasury Marketable Securities](#)

Financial Institutions

Treasury Marketable Securities

- ▶ [Treasury Bills](#)
- ▶ [Treasury Notes](#)
- ▶ [Treasury Bonds](#)
- ▶ [FRNs](#)
- ▶ [TIPS](#)
- ▶ [STRIPS](#)
- ▶ [BECCS & CUBES](#)

Announcements, Data & Results

Auction Fundamentals

Statutes, Regulations & Guidelines

Research Center

Savings Bonds

Forms for Institutions

Treasury Marketable Securities

U.S. Treasury marketable securities are debt instruments issued to raise money needed to operate the federal government and pay off maturing obligations. These liquid securities can be sold for cash in the secondary market.

U.S. Treasury marketable securities can be stripped into interest and principal components within the secondary market or can be converted from bearer securities into those that can be held in commercial book-entry accounts.

Find out more by selecting from the left navigation.

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Treasury Bill (T-bill)

- Short-term securities with maturities of 4, 13, 26, and 52 weeks.
- Treasury bills do not pay interest before maturity.
 - This is often referred to as a *discount security* or *zero-coupon security*.
- Instead, Treasury bills are issued at a price less than their par value and at maturity, Treasury bills pay back their par value.
 - Intuitively, the “interest” to the investor is the difference between par value and the purchase price.
 - Example: a 52-week T-bill with par value of \$100 has a price of \$98.

Example of 52-week Treasury Bill

B 0 01/26/23

↑ 0.8450

--

0.8550 / 0.8450

0.872 / 0.862

At 10:35

-- x --

Source BGN

B 0 01/26/23 Govt

Actions ▾

Settings ▾

Page 1/11

Security Description: Bond

95 Buy

96 Sell

25 Bond Description

26 Issuer Description

Pages

11 Bond Info

12 Addtl Info

13 Covenants

14 Guarantors

15 Bond Ratings

16 Identifiers

17 Exchanges

18 Inv Parties

19 Fees, Restrict

20 Schedules

21 Coupons

Issuer Information

NameTREASURY BILL

IndustryTreasury (BCLASS)

Security Information

Issue Date01/27/2022

Interest Accrues

1st Coupon Date

Maturity Date01/26/2023

Floater FormulaN.A.

Workout Date

Security TypeUSD

Cpn Frequency

Mty/Refund TypeNORMAL

Calc TypeDISCOUNT

Day CountACT/360

Market SectorUS GOVT

Country/RegionUS

CurrencyUSD

TENDERS ACCEPTED: \$34000MM

Identifiers

ID Number912796S34

CUSIP912796S34

ISINUS912796S348

SEDOL 1BN95VN6

FIGIBBG014QWGLP0

Issuance & Trading

Disc @ Issue.630000

Risk Factor.952

Amount Issued38137 (MM)

Amount Outstanding38137 (MM)

Minimum Piece100

Minimum Increment100

SOMA Holdings10.85

Quick Links

32 ALLQ Pricing

33 QRD Quote Recap

34 CACS Corp Action

35 CN Sec News

36 HDS Holders

66 Send Bond

- How to get there on the Bloomberg terminal?
- Open a terminal and on the keyboard type T Bill.
- In the popup window, select B Govt - United States Treasury Bill (Multiple Matches).
- Next, click on one of the different Treasury bills in the list.
- Then, click on DES on the top-right, or type DES on the keyboard and press enter.

Treasury Note (T-Note)

- Medium-term securities with maturities of 2, 3, 5, 7, and 10 years.
- Treasury notes pay interest every six months up to and including the maturity date.
 - Example: A 2-year T-note has its last interest payment in two years, and it pays interest after 6 months, 12 months, and 18 months.
- At maturity, Treasury notes pay back their par value.

Example of 10-year Treasury Note

T 1 3/8 11/15/31	↓ 95-02+ - 06	95-02 / 95-02+ -- X --	1.932 / 1.930
	At 10:52		Source BGN
T 1 3/8 11/15/31 Govt	Actions ▾	Settings ▾	Page 1/11 Security Description: Bond
			95 Buy 90 Sell
25 Bond Description	20 Issuer Description		
Pages	Issuer Information	Identifiers	
11 Bond Info	Name US TREASURY N/B	ID Number 91282CDJ7	
12 Addtl Info	Industry Treasury (BCLASS)	CUSIP 91282CDJ7	
13 Covenants	Security Information	ISIN US91282CDJ71	
14 Guarantors	Issue Date 11/15/2021	SEDOL 1 BMF0Q22	
15 Bond Ratings	Interest Accrues 11/15/2021	FIGI BBG013BNT3Y4	
16 Identifiers	1st Coupon Date 05/15/2022	Issuance & Trading	
17 Exchanges	Maturity Date 11/15/2031	Issue Price 96.866042	
18 Inv Parties	Floater Formula N.A.	Risk Factor 8.617	
19 Fees, Restrict	Workout Date 11/15/2031	Amount Issued 144644 (M...	
20 Schedules	Coupon 1.375	Amount Outstanding 144644 (M...	
21 Coupons	Cpn Frequency S/A	Minimum Piece 100	
Quick Links	Mty/Refund Type NORMAL	Minimum Increment 100	
32 ALLQ Pricing	Calc Type STREET CONVENTION	SOMA Holdings 23.26	
33 QRD Quote Recap	Day Count ACT/ACT		
34 CACS Corp Action	Market Sector US GOVT		
35 CN Sec News	Country/Region US	Currency USD	
36 HDS Holders			
60 Send Bond			
	TENDERS ACCEPTED: \$39000MM \$36000MM ISS'D AS A REOPENING EFF 12/15/21. \$36000MM ISS'D AS A REOPENING EFF 01/18/22.		

- How to get there on the Bloomberg terminal?
 - Open a terminal and on the keyboard type T Note.
 - In the popup window, select T Govt - United States Treasury Note/Bond (Multiple Matches).
 - Next, click on one of the different Treasury notes in the list.
 - Then, click on DES on the top-right, or type DES on the keyboard and press enter.
-
- Let's look at price quotes for this Treasury note.
 - If you were to purchase this Treasury note, would you pay \$95.02?
 - The answer is *no*. Prices for Treasury notes are quoted in a specific way, which we will discuss in the next lecture.



- How to get there on the Bloomberg terminal?
- From the Description page where you are currently at, type GP and press enter.

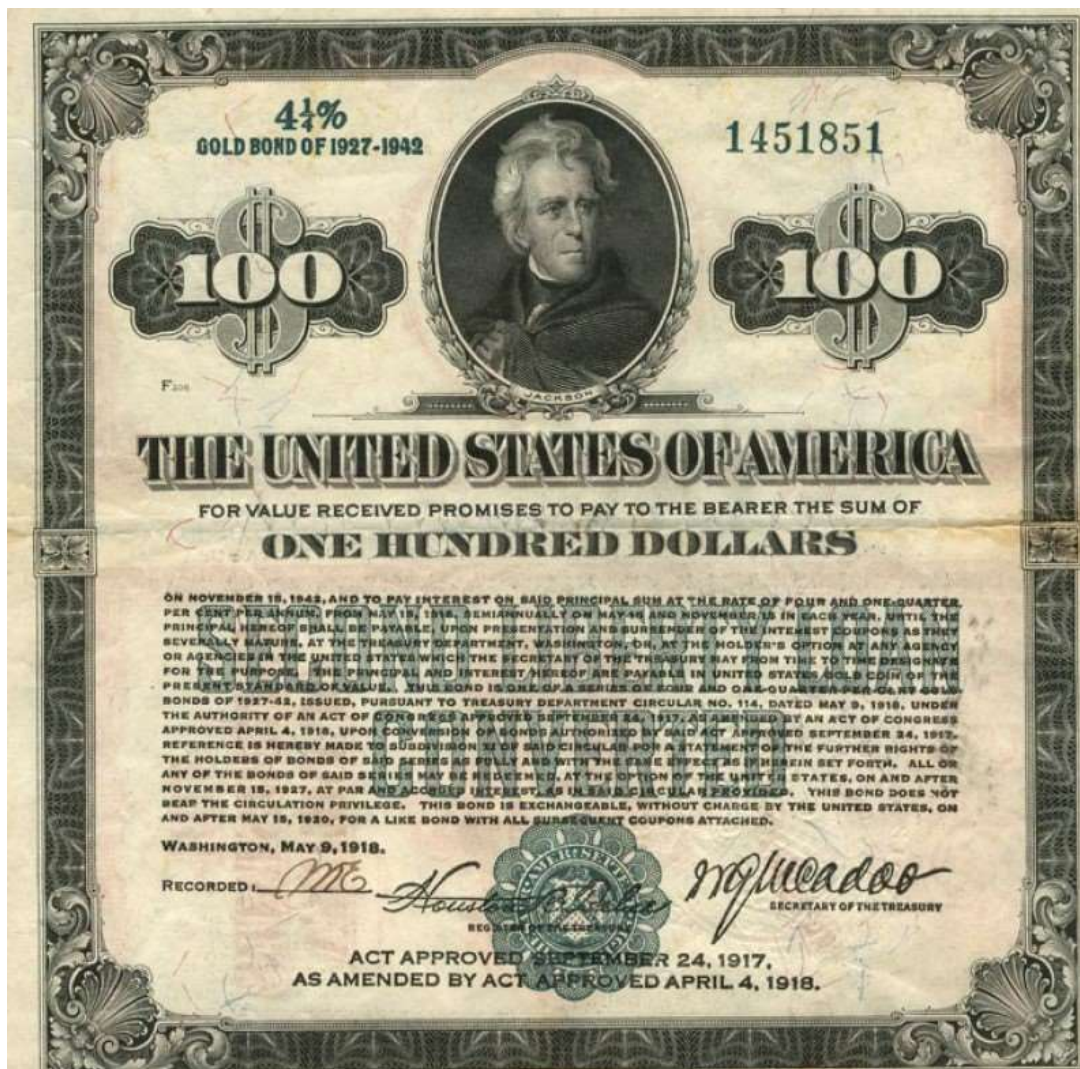
Treasury Bond (T-Bond)

- Long-term securities with maturities of 20 and 30 years.
 - Currently, the Treasury does not issue 15-year Treasury bonds.
- Treasury bonds notes pay interest every six months up to and including the maturity date. At maturity, Treasury notes pay back their par value.
 - Similar to Treasury notes.

Treasury Marketable Securities

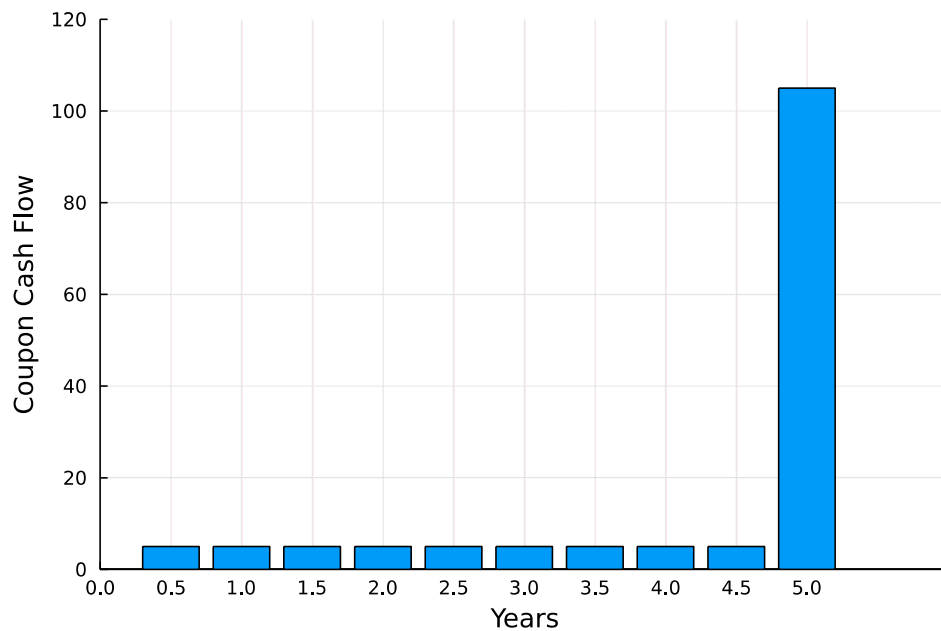
Coupon bonds

- Treasury notes and bonds are referred to as **coupon** securities.
- Why?



Example of Treasury Note Cash Flows

- Par Value $F = \$100$.
- Coupon Rate c [% p.a.]:
- Time to maturity T [years]:



Treasury Floating Rate Note (FRN)

- First issued in 2014 by the U.S. Treasury.
- Maturity of 2 years.
- Pay interest every three months up to and including the maturity date.
 - At maturity, FRNs pay back their par value.
- The interest on an FRN varies with interest rate on 13-week Treasury bills.

Treasury STRIPS

- The Treasury does not issue zero-coupon notes or bonds.
- However, because of the demand for zero-coupon instruments with no credit risk, the private sector has created such securities.
- The process of separating the interest on a bond from the underlying principal is called coupon stripping
- Zero-coupon Treasury securities were first created in August 1982 by large Wall-Street firms.
 - The problem with these securities was that they were identified with particular dealers and therefore reduced liquidity.
 - Moreover, the process involved legal and insurance costs.
 - Today, all Treasury notes and bonds (fixed-principal and inflation-indexed) are eligible for stripping.
- The zero-coupon Treasury securities created under the STRIPS program are direct obligations of the U.S. government

Treasury STRIPS in Bloomberg

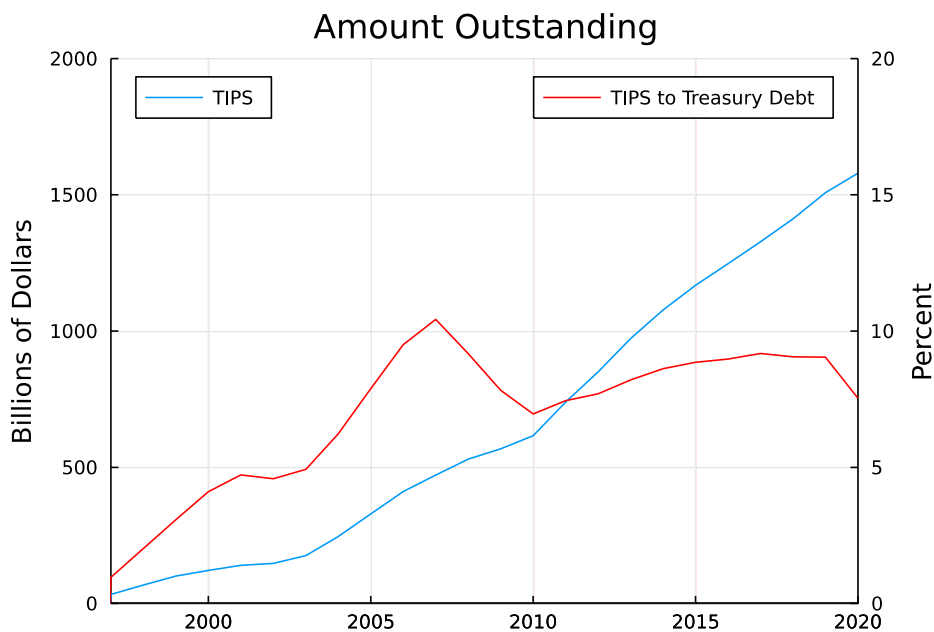
Name	Tic...	Coupon	Maturity	Mty Type	Ctry/Reg	Curr	Identifier
STRIP*	S				US	USD	
United States Treasury Strip Coupon	S	0.000	08/15/2051	NORMAL	US	USD	912834XG8
United States Treasury Strip Coupon	S	0.000	05/15/2051	NORMAL	US	USD	912834WZ7
United States Treasury Strip Coupon	S	0.000	02/15/2051	NORMAL	US	USD	912834WR5
United States Treasury Strip Coupon	S	0.000	11/15/2050	NORMAL	US	USD	912834WJ3
United States Treasury Strip Coupon	S	0.000	08/15/2050	NORMAL	US	USD	912834WC8
United States Treasury Strip Coupon	S	0.000	05/15/2050	NORMAL	US	USD	912834VV7
United States Treasury Strip Coupon	S	0.000	02/15/2050	NORMAL	US	USD	912834VM7
United States Treasury Strip Coupon	S	0.000	11/15/2049	NORMAL	US	USD	912834VE5
United States Treasury Strip Coupon	S	0.000	08/15/2049	NORMAL	US	USD	912834UY2
United States Treasury Strip Coupon	S	0.000	05/15/2049	NORMAL	US	USD	912834UR7
United States Treasury Strip Coupon	S	0.000	02/15/2049	NORMAL	US	USD	912834UH9
United States Treasury Strip Coupon	S	0.000	11/15/2048	NORMAL	US	USD	912834UB2
United States Treasury Strip Coupon	S	0.000	08/15/2048	NORMAL	US	USD	912834TV0
United States Treasury Strip Coupon	S	0.000	05/15/2048	NORMAL	US	USD	912834TP3
United States Treasury Strip Coupon	S	0.000	02/15/2048	NORMAL	US	USD	912834TF5
United States Treasury Strip Coupon	S	0.000	11/15/2047	NORMAL	US	USD	912834SZ2
United States Treasury Strip Coupon	S	0.000	08/15/2047	NORMAL	US	USD	912834RR1
United States Treasury Strip Coupon	S	0.000	05/15/2047	NORMAL	US	USD	912834RK6
United States Treasury Strip Coupon	S	0.000	02/15/2047	NORMAL	US	USD	912834RB6
United States Treasury Strip Coupon	S	0.000	11/15/2046	NORMAL	US	USD	912834QV3

- How to get there on the Bloomberg terminal?
- Open a terminal and on the keyboard type Treasury STRIP.
- In the popup window, select S Govt - United States Treasury Strip Coupon (Multiple Matches).
- Next, click on one of the different Treasury bills in the list.
- Then, click on DES on the top-right, or type DES on the keyboard and press enter.

S 0 02/15/25		↑1.485	+ .011	1.552 / 1.485	95.440 / 95.632
		At 11:08	-- X --	Source BGN	
S 0 02/15/25 Govt		Actions ▾	Settings ▾	Page 1/11	Security Description: Bond
				95 Buy	96 Sell
25 Bond Description		20 Issuer Description			
Pages		Issuer Information		Identifiers	
11 Bond Info	Name STRIPS		ID Number	912833LU2	
12 Addtl Info	Industry Treasury (BCLASS)		CUSIP	912833LU2	
13 Covenants	Security Information		ISIN	US912833LU26	
14 Guarantors	Issue Date 02/15/1995		SEDOL 1	2894870	
15 Bond Ratings	Interest Accrues		FIGI	BBG000DPKMR9	
16 Identifiers	1st Coupon Date		Issuance & Trading		
17 Exchanges	Maturity Date 02/15/2025		Issue Price		
18 Inv Parties	Floater Formula N.A.		Risk Factor	2.859	
19 Fees, Restrict	Workout Date 02/15/2025		Amount Unstripped	0 (MM)	
20 Schedules	Coupon		Security Type USW	Amount Stripped 0 (MM)	
21 Coupons	Cpn Frequency		Type ZERO	Minimum Piece .01	
Quick Links		Mty/Refund Type NORMAL Series		Minimum Increment .01	
32 ALLQ Pricing	Calc Type STREET CONVENTION		SOMA Holdings		N.A.
33 QRD Quote Recap	Day Count ACT/ACT				
34 CACS Corp Action	Market Sector US GOVT				
35 CN Sec News	Country/Region US		Currency	USD	
36 HDS Holders	LISTED: AMEX.				
66 Send Bond					

Treasury Inflation Protected Securities (TIPS)

- First issued in 1997 by the U.S. Treasury.
 - Maturities of 5, 10, and 30 years.
 - TIPS pay interest every six months up to and including the maturity date. At maturity, Treasury notes pay back their par value.
 - Similar to Treasury notes and bonds.
 - Key difference is that both par value and interest go up with the rate of inflation.
-
- Why inflation matters ...
 - [WSJ, June 10, 2022: U.S. Inflation Hit 8.6% in May. Energy, groceries, shelter costs drive fastest rise in consumer-price index since December 1981](#)
 - [WSJ, January 12, 2022: U.S. Inflation Hit 7% in December, Fastest Pace Since 1982](#)
 - [WSJ, February 10, 2022: U.S. Inflation Rate Accelerates to a 40-Year High of 7.5%](#)
 - [WSJ, February 6, 2022: What Investors Should Know About TIPS](#)



Example of a Treasury TIPS

TII 0 1₈ 01/15/32 ↑ 105-27+ - 18¹/₄ 105-25 / 105-27+ -0.444 / -0.451
At 11:02 -- X -- Source BGN

TII 0 1₈ 01/15/32 Govt Actions Settings Page 1/11 Security Description: Bond

95 Buy 90 Sell

25 Bond Description20 Issuer Description

Pages

11) Bond Info12) Addtl Info13) Covenants14) Guarantors15) Bond Ratings16) Identifiers17) Exchanges18) Inv Parties19) Fees, Restrict20) Schedules21) Coupons

Quick Links

32) ALLQ Pricing33) QRD Quote Recap34) CACS Corp Action35) CN Sec News36) HDS Holders

60 Send Bond

Issuer Information

NameTSY INFL IX N/BIndustryTreasury (BCLASS)Security Information

Issue Date01/31/2022Interest Accrues01/15/20221st Coupon Date07/15/2022Maturity Date01/15/2032Floater FormulaN.A.Workout Date01/15/2032Coupon.125Cpn FrequencyS/ASecurity TypeUSN

Mty/Refund TypeNORMALCalc TypeU.S. I/L REAL YLDDay CountACT/ACTMarket SectorUS GOVTCountry/RegionUSCurrencyUSD

Identifiers

ID Number91282CDX6CUSIP91282CDX6ISINUS91282CDX65SEDOL 1BPLFCC4FIGIBBG014KBX792

Issuance & Trading

Issue Price106.811231Risk Factor5.253Amount Issued18391 (MM)Amount Outstanding18391 (MM)Minimum Piece100Minimum Increment100SOMA Holdings17.45

TENDERS ACCEPTED: \$16000MM. SEE CPIRJN22 <Index> FOR INDEX RATIO.
CALCULATIONS OF PRINCIPAL VALUE AND INTEREST PAYMENTS ARE NOT ADJUSTED IF
PREVIOUSLY REPORTED CPI FIGURES ARE REVISED.

- How to get there on the Bloomberg terminal?
- Open a terminal and on the keyboard type Treasury TIPS.
- In the popup window, select TII Govt - United States Treasury Inflation Indexed Bonds (Multiple Matches).
- Next, click on one of the different Treasury bills in the list.
- Then, click on DES on the top-right, or type DES on the keyboard and press enter.

- Let's look at price quotes for this Treasury TIPS.
- If you were to purchase this Treasury TIPS, would you pay \$105.28?
- The answer is *no*. Prices for Treasury TIPS are quoted in a specific way, which we will discuss in the next lecture.

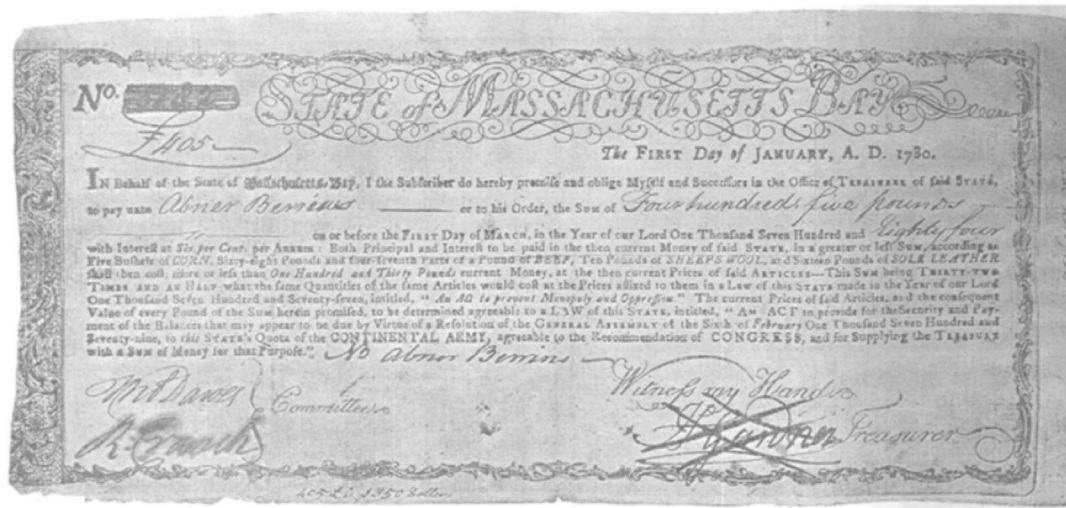


- How to get there on the Bloomberg terminal?
- From the Description page where you are currently at, type GP and press enter.

Inflation-Linked notes date back centuries

Both Principal and Interest to be paid in the then current Money of said State, in a greater or less Sum, according as Five Bushels of Corn, Sixty-eight Pounds and four-seventh Parts of a Pound of Beef, Ten Pounds of Sheeps Wool, and Sixteen Pounds of Sole Leather shall then cost more or less than One Hundred and Thirty Pounds current Money, at the then current Prices of said Articles.

Source: "Inflation-indexed Securities: Bonds, Swaps and Other Derivatives", 2nd Edition, M. Deacon, A. Derry, D. Mirfendereski, Wiley.



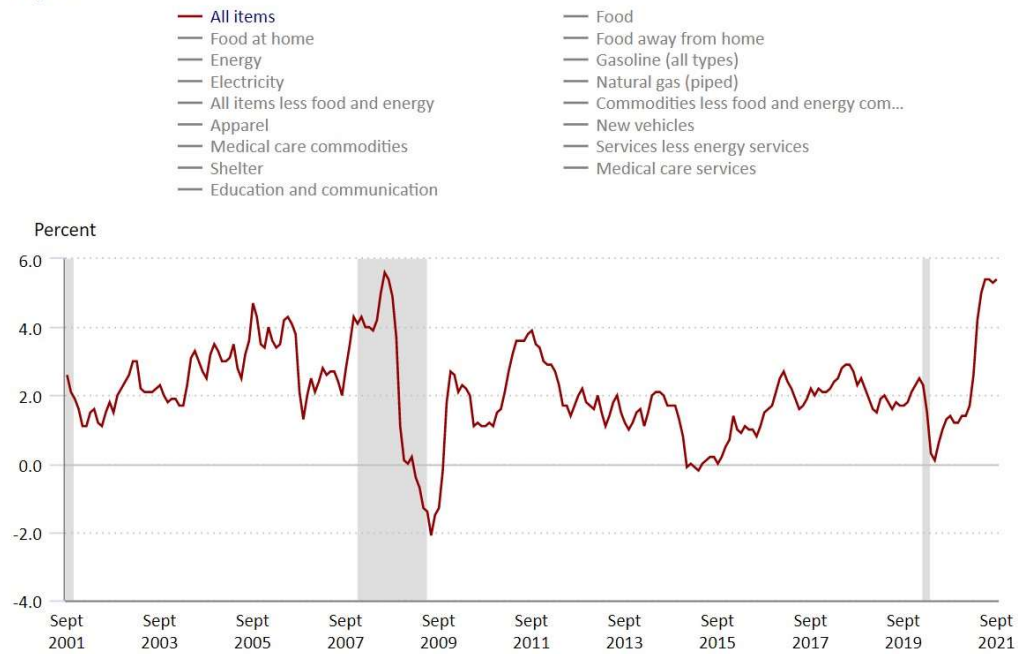
Indexing Bonds to Inflation

- Treasury Inflation-Protected Securities (TIPS) are *index-linked* bonds.
 - An index-linked bond is one whose *cash flows* are linked to movements in a specific price index.
- The *principal amount* of a TIPS is indexed to the price level.
 - Since a fixed coupon rate is applied to the principal that varies with the price level, the actual coupon cash flows vary in response to the realized rate of inflation.
- Index-linked bonds are usually indexed to a broad measure of prices, typically a domestic *Consumer Price Index (CPI)*.

U.S. Consumer Price Index

- In the U.S. this price index is the Consumer Price Index for All Urban Consumers (*CPI-U*).
- The CPI-U measures the level of prices paid by consumers for goods and services.
- This index is published by the Bureau of Labor Statistics (BLS) every month.
- Bureau of Labor Statistics; Bureau of Labor Statistics Release

12-month percentage change, Consumer Price Index, selected categories, not seasonally adjusted



Hover over chart to view data.

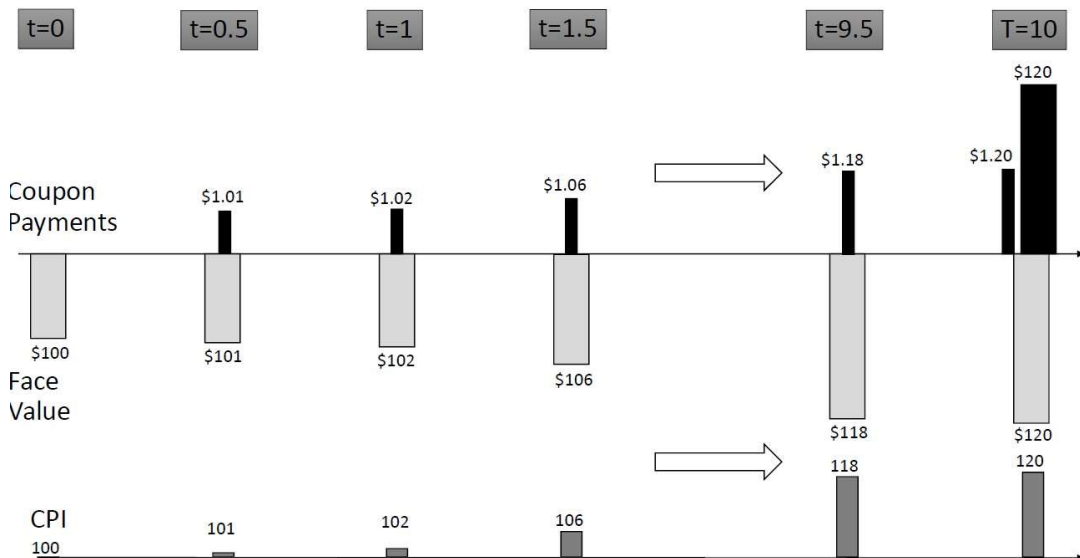
Note: Shaded area represents recession, as determined by the National Bureau of Economic Research.

Source: U.S. Bureau of Labor Statistics.



Source: [BLS.gov](https://www.bls.gov)

TIPS Inflation-Adjustment

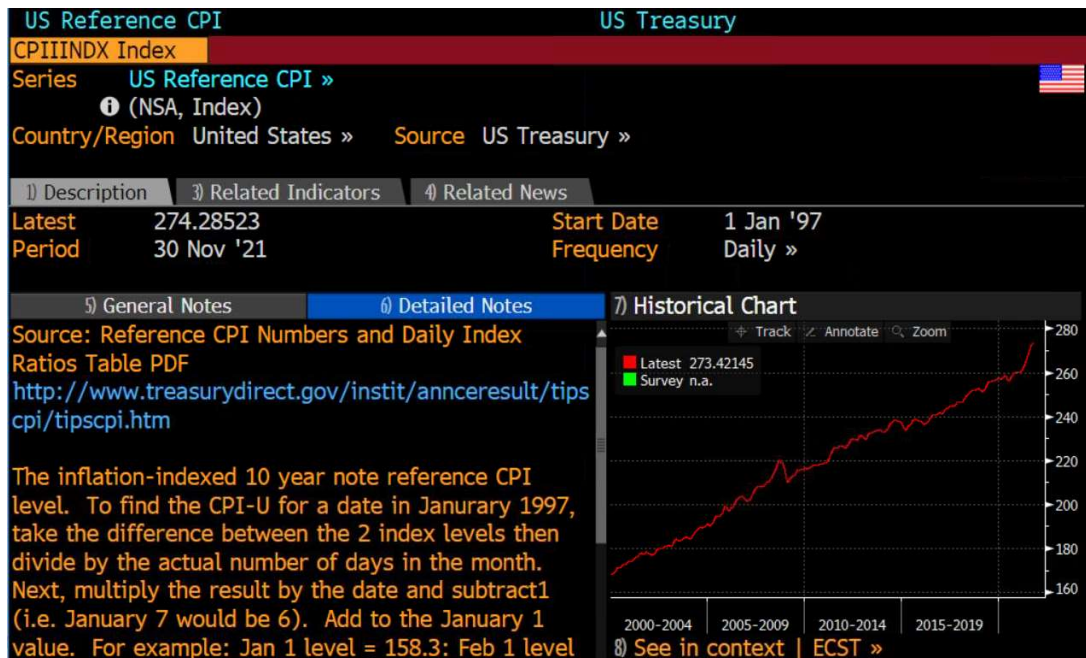


TIPS Inflation Adjustment Details

- The principal amount of a TIPS (assume 100 at issuance) is adjusted daily based on the CPI-U.
- The inflation adjustment I_t is computed as the ratio of the **Reference CPI** at the time t divided by the reference CPI when the TIPS was first issued ($t = 0$).

$$I_t = \frac{\text{Reference CPI at time } t}{\text{Reference CPI at TIPS issue date}}$$

- The **Reference CPI** for a particular date t during a month is linearly interpolated from the **Reference CPI** for the beginning of that month and the **Reference CPI** for the beginning of the subsequent month.
 - The **Reference CPI** for the first day of *any* calendar month is the CPI-U index for the third preceding calendar month.
- *Example 1:* the **Reference CPI** for *April 1* is the CPI-U index for the month of *January* (which is reported by the BLS during February).
- *Example 2:* the **Reference CPI** for *April 15* is roughly the average of the CPI-U index for the month of *January* and the CPI-U index for the month of February.



Deflation Protection

- TIPS have an embedded option that protects against deflation.
- The Treasury guarantees that the *final redemption value is no less than \$100 per \$100 nominal* amount, irrespective of the movements in the CPI over the life of the bond.
- Let F be the TIPS principal amount and T the time to maturity of the TIPS.
- The principal cash flow at maturity T is

$$F \times \max[I_T, 1]$$

- This deflation protection does not apply to coupon cash flows.





Inflation-Adjusted Coupon Interest

Security: Description: CUSIP Number: Dated Date: Original Issue Date: Additional Issue Date: Maturity Date: Ref CPI on Dated Date:	3-3/8% 10-Year Notes Series A-2007 9128272M3 January 15, 1997 February 6, 1997 April 15, 1997 January 15, 2007 158.43548
---	---

- The Reference CPI is then turned into a ratio to calculate the inflation adjustment by taking the Reference CPI on the date and dividing by the Reference CPI at issue.
 - For example, the Reference CPI for January 15, the official issue date of the inaugural TIPS bond is 158.43548. Assume \$100 par value at issuance.
 - Suppose we are on July 15 and the first coupon cash flow is about to be paid. Suppose that the reference CPI on July 15 turns out to be 168.53226.
 - Then, the inflation adjustment factor is $168.53226/158.43458 = 1.063734$
 - This means coupon rate is paid on par value of $\$100 \times 1.063734 = \106.3734 .

Inflation-Adjusted Coupon Interest Example

- Let F be the TIPS principal value.
- Let c denote the (fixed) *real* coupon rate on the TIPS.
- Let T denote the time to maturity of the TIPS (in years).

- Principal F [\$]:  100
- Real Coupon Rate c [%]:  3.0
- Time to Maturity T [years]:  5
- Reference CPI at issue date:  100

- Suppose, $c = 3.0\%$ and $F = 100$.
- In real terms, the coupon cash flows at each coupon date are

$$\frac{c}{2} F = \frac{0.03}{2} 100 = 1.5$$

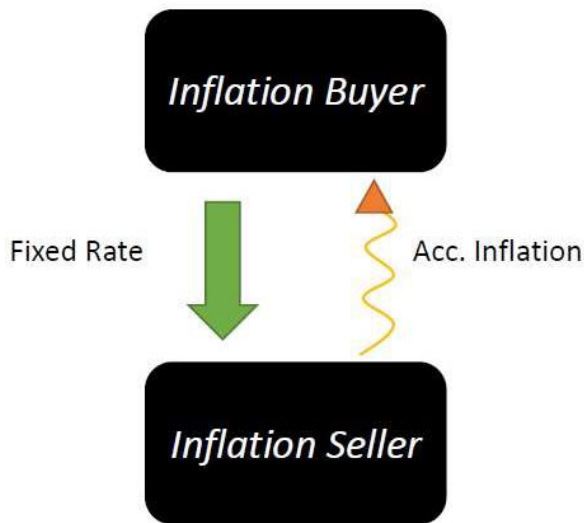
- Suppose there is inflation (or deflation).
- The actual cash flows (in nominal terms) of the TIPS are:

	Time	Reference_CPI	I_t	Adjusted_Principal	Cashflows
1	0.5	101.209	1.01209	101.209	1.51814
2	1.0	100.344	1.00344	100.344	1.50515
3	1.5	102.195	1.02195	102.195	1.53293
4	2.0	103.319	1.03319	103.319	1.54979
5	2.5	104.589	1.04589	104.589	1.56884
6	3.0	103.968	1.03968	103.968	1.55952
7	3.5	103.605	1.03605	103.605	1.55408
8	4.0	104.347	1.04347	104.347	1.5652
9	4.5	104.563	1.04563	104.563	1.56844
10	5.0	105.198	1.05198	105.198	106.776

Inflation Derivatives

- In addition to the cash inflation market, there is an active derivatives market that consists mainly of inflation swap contracts and inflation options.

Inflation Swap Basics



USSWIT1 CMPN Currency

Properties	Related Instruments	Related Curves
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USD Inflation Swap Zero Coupon

FIGI BBG009K9TV35

A derivative used to transfer inflation risk from one party to another through an exchange of cash flows. In a zero coupon inflation swap, only one payment is done at maturity where one party pays a fixed rate on a notional principal amount, while the other party pays a floating rate linked to an inflation index.

Overview	Fixed Leg	Inflation Leg			
Currency	USD	Day Count	1/1		
Settlement	T+2 Days 26-OCT-2021	Bus Adj	ModifiedFollowing	Index	CPURNSA Index
Term	1 Year 26-OCT-2022	Adjust	Pay Dates	Bus Adj	ModifiedFollowing
Discounting	OIS	Roll Conv	Backward (EOM)	Adjust	Pay Dates
Lag	3 Month	Calc Cal	FD, EN	Roll Conv	Backward (EOM)
Interpolation	Daily	Pay Delay	0 Business Days	Calc Cal	FD, EN
Compound Freq	Annual			Pay Delay	0 Business Days
Quote	3.8700 %			Reset Position	In Advance

USSWIT1		3.8700	As of 22 Oct		Source CMPN	
USSWIT1 CMPN Curncy			Export	Settings		
USD INFL SWAP ZC 1Y				High	2.1300 on	09/29/06
Range	09/29/2006	- 10/31/2006	Period	Daily	Low	1.7300 on 10/18/06
Market	Last Price		Currency	USD	Average	1.8417
View	Price Table		Source	CMPN	Net Chg	-.3400 -15.96%
Date		Last Price		Date		Last Price
Fr	11/03/06			Fr	10/13/06	1.8100
Th	11/02/06			Th	10/12/06	1.8400
We	11/01/06			We	10/11/06	1.8600
Tu	10/31/06	1.7900		Tu	10/10/06	1.8500
Mo	10/30/06	1.8300		Mo	10/09/06	1.9900
Fr	10/27/06	1.8800		Fr	10/06/06	1.8100
Th	10/26/06	1.9000		Th	10/05/06	1.8500
We	10/25/06	1.8900		We	10/04/06	1.7900
Tu	10/24/06	1.7800		Tu	10/03/06	1.8600
Mo	10/23/06	1.7500		Mo	10/02/06	1.9000



Inflation Swap Cash Flows

- The swap is executed between two counterparties at time $t = 0$ and has only one cash flow that occurs at maturity in T years.
- For example, imagine that at time $t = 0$, the five-year zero-coupon inflation swap rate is 200 basis points and that the inflation swap has a notional of \$1.
- There are no cash flows at time $t = 0$ when the swap is executed.
- At the maturity of the swap in $T = 5$ years, suppose that realized inflation is I_T , then the counterparties to the inflation swap exchange a cash flow of

$$[(1 + 0.0200)^5 - 1] - [I_T - 1],$$





- Thus, if the realized inflation rate was 1.50% per year over the five-year horizon of the swap,

$$I_T = 1.015^5 = 1.077284$$

- In this case, the net cash flow per \$1 notional of the swap from the swap would be

$$[(1 + 0.0200)^5 - 1] - [1.077284 - 1] = 0.026797$$

Inflation Swap Example

- Notional N [\$]:  100
- Inflation Swap Rate f [%]:  3.0
- Time to Maturity T [years]:  5
- Annual Inflation Rate I [%]:  2.0

- Cash flow on the fixed leg of the inflation swap:

$$N \times [(1 + f)^T - 1] = 100 \times [(1 + 0.03)^5 - 1] = 15.9274$$

- Cash flow on the floating leg of the swap:

$$N \times [(1 + I)^T - 1] = 100 \times [(1 + 0.02)^5 - 1] = 10.4081$$

- Net cash flow of inflation buyer: -5.5193

Wrap-Up

Our goals for today

- ☒ Introduction to the U.S. Treasury Securities Market
- ☒ Treasury Bills
- ☒ Treasury Notes and Bonds
- ☒ Treasury STRIPS
- ☒ Treasury TIPS
- ☒ Inflation Swaps

Reading

Fabozzi, Fabozzi, 2021, Bond Markets, Analysis, and Strategies, 10th Edition
Chapter 7

