galois

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Exercise 1:
 ffs_imp.c:
   #include <stdio.h>
  #include <stdlib.h>
   typedef unsigned int uint32_t;
   uint32_t ffs_imp(uint32_t word) {
      char n = 1;
      if (!(word & 0xffff)) { n += 16; word >>= 16; }
      if (!(word & 0x00ff)) { n += 8; word >>= 8; }
      if (!(word & 0x000f)) { n += 4; word >>= 4; }
      if (!(word & 0x0003)) { n += 2; word >>= 2; }
      return (word) ? (n+((word+1) \& 0x01)) : 0;
  }
   int main (int argc, char **argv) {
      if (argc != 2) {
         printf("Usage: %s <number>\n", argv[0]);
         exit(0);
      }
      uint32_t n = atol(argv[1]);
      printf("ffs_imp: first 1 at %d\n", ffs_imp(n));
   }
Exercise 2:
 ffs ref.bc:
   clang-12 -g -00 -c -emit-llvm ffs_ref.c -o ffs_ref.bc
 ffs imp.bc:
   clang-12 -g -00 -c -emit-llvm ffs_imp.c -o ffs_imp.bc
 ffs imp.saw:
   m1 <- llvm_load_module "ffs_ref.bc";</pre>
   ffs_ref <- llvm_extract m1 "ffs_ref";
  m2 <- llvm_load_module "ffs_imp.bc";</pre>
  ffs_imp <- llvm_extract m2 "ffs_imp";
   let thm1 = \{\{ \x -> ffs\_ref x == ffs\_imp x \}\};
   result <- prove z3 thm1;
   print result;
running ffs imp.saw:
   saw ffs_imp.saw
   [19:05:02.280] Loading file "<path-to-ffs_imp.saw>/ffs_imp.saw"
   [19:05:02.439] Valid
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Exercise 3:
 ffs mus.c:
   uint32_t ffs_mus (uint32_t word) {
     static const char debruijn32[32] = {
       0, 1, 23, 2, 29, 24, 19, 3, 30, 27, 25, 11, 20, 8, 4, 13,
      31, 22, 28, 18, 26, 10, 7, 12, 21, 17, 9, 6, 16, 5, 15, 14
     return word ? debruijn32[(word & -word)*0x076be629 >> 27]+1 : 0;
   }
   int main (int argc, char **argv) {
      if (argc != 2) {
         printf("Usage: %s <number>\n", argv[0]);
         exit(0);
      }
      uint32_t n = atol(argv[1]);
      printf("ffs_mus: first 1 at %d\n", ffs_mus(n));
   }
 ffs mus.bc:
   clang-12 -g -00 -c -emit-llvm ffs_mus.c -o ffs_mus.bc
 ffs imp.saw:
  m1 <- llvm_load_module "ffs_ref.bc";</pre>
   ffs_ref <- llvm_extract m1 "ffs_ref";
  m2 <- llvm_load_module "ffs_mus.bc";</pre>
  ffs_mus <- llvm_extract m2 "ffs_mus";
   let thm2 = \{\{ \x -> ffs\_ref x == ffs\_mus x \}\};
   result <- prove z3 thm2;
  print result;
 running ffs imp.saw:
   saw ffs_mus.saw
   [17:40:08.109] Loading file
   "<path-to-ffs_mus.saw>/ffs_mus.saw"
   [17:40:08.280] Valid
Exercise 4:
 ffs bug.c:
   uint32_t ffs_bug(uint32_t word) {
      int i = 0;
      int cnt = 0;
      if (!word) return 0;
      /* injected bug: */
      if (word == 1052688) return 4; /* instead of 5 (in hex: 0x101010) */
      for (cnt = 0; cnt < 32; cnt++)
        if (((1 << i++) \& word) != 0) return i;
      return 0;
   }
```

```
int main (int argc, char **argv) {
    if (argc != 2) {
        printf("Usage: %s <number>\n", argv[0]);
        exit(0);
    }
    uint32_t n = atol(argv[1]);
    printf("ffs_bug: first 1 at %d\n", ffs_bug(n));
 }
ffs bug.bc:
 clang-12 -g -00 -c -emit-llvm ffs_bug.c -o ffs_bug.bc
ffs_bug.saw:
 m1 <- llvm_load_module "ffs_ref.bc";</pre>
 ffs_ref <- llvm_extract m1 "ffs_ref";
 m2 <- llvm_load_module "ffs_bug.bc";</pre>
 ffs_bug <- llvm_extract m2 "ffs_bug";
 let thm3 = \{\{ \x -> ffs\_ref x == ffs\_bug x \}\};
 result <- prove z3 thm3;
 print result;
running ffs bug.saw:
 saw ffs_bug.saw
 [17:57:41.672] Loading file
 "<path-to-ffs_bug.saw>/ffs_bug.saw"
 [17:57:41.835] Sat: [x = 1052688]
```