# Multivariate Statistics Assignment 1

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#### Question 1: Describing individual variables

a) Describe the 7 variables with mean values, standard deviations etc.

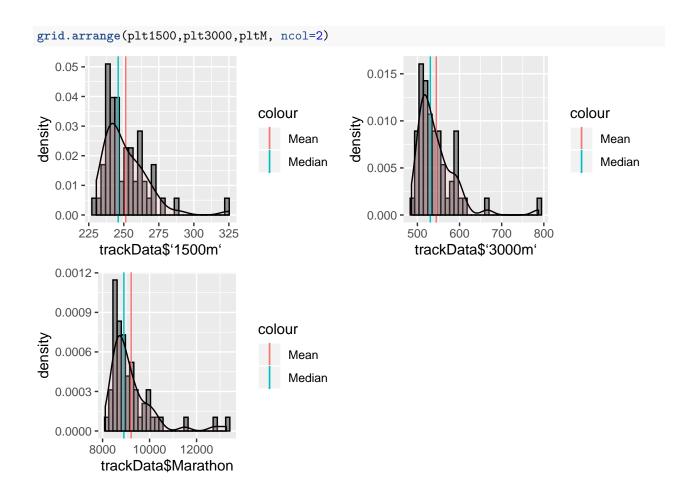
```
trackData = read.table("T1-9.dat")
colnames(trackData) = c("Countries", "100m", "200m", "400m", "800m", "1500m", "3000m", "Marathon")
samplesnames = c("100m", "200m", "400m", "800m", "1500m", "3000m", "Marathon")
trackData[,5:8] = trackData[,5:8]*60
trackData_Mean = colMeans(trackData[,2:8])
trackData_SD = apply(trackData[,2:8], 2, sd)
trackData_Median = apply(trackData[,2:8], 2, median)
```

#### b) Illustrate the variables with different graphs

\*\* Illustrate the variables with different graphs (explore what plotting possibilities R has). Make sure that the graphs look attractive (it is absolutely necessary to look at the labels, font sizes, point types). Are there any apparent extreme values? Do the variables seem normally distributed? Plot the best fitting (match the mean and standard deviation, i.e. method of moments) Gaussian density curve on the data's histogram. For the last part you may be interested in the hist() and density() functions \*\*

```
plt100 = ggplot()+
  geom_histogram(aes(x=trackData$^100m^, y=..density..), color = "black", fill = "#343434",alpha=0.5,bi
  geom_vline(aes(xintercept = trackData_Mean[1],color="Mean"))+
  geom_vline(aes(xintercept = trackData_Median[1],color="Median"))+
  geom_density(aes(x=trackData$`100m`, y=..density..), fill="lightpink", alpha=0.2)+
  theme()
plt200 = ggplot()+
  geom_histogram(aes(x=trackData$`200m`, y= ..density..), color = "black", fill = "#343434",alpha=0.5,b
  geom_vline(aes(xintercept = trackData_Mean[2],color="Mean"))+
  geom_vline(aes(xintercept = trackData_Median[2],color="Median"))+
  geom density(aes(x=trackData$^200m`, y=..density..), fill="lightpink", alpha=0.2)+
  theme()
plt400 = ggplot() +
  geom_histogram(aes(x=trackData$^400m`, y= ..density..), color = "black", fill = "#343434",alpha=0.5,b
  geom_vline(aes(xintercept = trackData_Mean[3],color="Mean"))+
  geom_vline(aes(xintercept = trackData_Median[3],color="Median"))+
  geom_density(aes(x=trackData$`400m`, y=..density..), fill="lightpink", alpha=0.2)+
  theme()
plt800 = ggplot()+
  geom_histogram(aes(x=trackData$`800m`, y= ..density..), color = "black", fill = "#343434",alpha=0.5,b
```

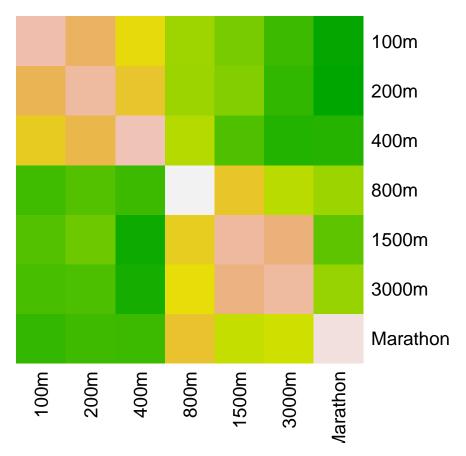
```
geom_vline(aes(xintercept = trackData_Mean[4],color="Mean"))+
  geom_vline(aes(xintercept = trackData_Median[4],color="Median"))+
  geom_density(aes(x=trackData$`800m`, y=..density..), fill="lightpink", alpha=0.2)+
  theme()
plt1500 = ggplot() +
  geom_histogram(aes(x=trackData$`1500m`, y= ..density..), color = "black", fill = "#343434",alpha=0.5,
  geom_vline(aes(xintercept = trackData_Mean[5],color="Mean"))+
  geom_vline(aes(xintercept = trackData_Median[5],color="Median"))+
  geom_density(aes(x=trackData$`1500m`, y=..density..), fill="lightpink", alpha=0.2)+
  theme()
plt3000 = ggplot() +
  geom_histogram(aes(x=trackData$`3000m`, y= ..density..), color = "black", fill = "#343434",alpha=0.5,
  geom_vline(aes(xintercept = trackData_Mean[6],color="Mean"))+
  geom_vline(aes(xintercept = trackData_Median[6],color="Median"))+
  geom_density(aes(x=trackData$`3000m`, y=..density..), fill="lightpink", alpha=0.2)+
  theme()
pltM = ggplot()+
  geom_histogram(aes(x=trackData$`Marathon`, y= ..density..), color = "black", fill = "#343434",alpha=0
  geom_vline(aes(xintercept = trackData_Mean[7],color="Mean"))+
  geom_vline(aes(xintercept = trackData_Median[7],color="Median"))+
  geom_density(aes(x=trackData$`Marathon`, y=..density..), fill="lightpink", alpha=0.2)+
  theme()
grid.arrange(plt100,plt200,plt400,plt800, ncol=2)
                                                  0.8 -
   1.5 -
                                                  0.6
                                  colour
                                                                                 colour
                                               density
density
   1.0
                                      Mean
                                                                                     Mean
                                                  0.4
                                      Median
                                                                                     Median
   0.5
                                                  0.2
                                                  0.0
   0.0
      10.5 11.0 11.5 12.0 12.5
                                                                       25
                                                     21
                                                              23
                                                                  24
         trackData$'100m'
                                                         trackData$'200m'
   0.20 -
                                                  0.10
density
0.10
                                 colour
                                                                                 colour
                                               density
                                      Mean
                                                                                     Mean
                                                  0.05 -
                                      Median
                                                                                     Median
   0.05
   0.00 -
                                                  0.00 -
                  .
55
                          60
                                                            120
                                                                    130
           50
                                                         trackData$'800m'
          trackData$'400m'
```



### Question 2: Relationships between the variables

a) Compute the covariance and correlation matrices

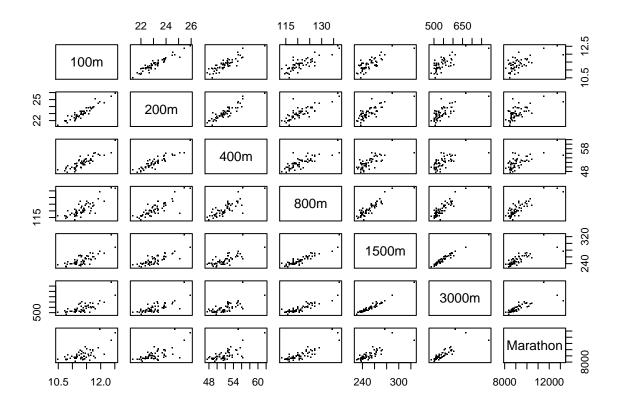
```
trackData_Cov = cov(trackData[,2:8])
trackData_Cor = cor(trackData[,2:8])
heatmap(trackData_Cor, col = terrain.colors(256), Rowv=NA,Colv=NA, revC=T)
```



Each square shows the correlation between the variables on each axis. Correlation ranges from -1 to +1. Values closer to zero means there is no linear trend between the two variables. The close to 1 the correlation is the more positively correlated they are; that is as one increases so does the other and the closer to 1 the stronger this relationship is. A correlation closer to -1 is similar, but instead of both increasing one variable will decrease as the other increases. The diagonals are all 1/dark green because those squares are correlating each variable to itself (so it's a perfect correlation). For the rest the larger the number and darker the color the higher the correlation between the two variables. The plot is also symmetrical about the diagonal since the same two variables are being paired together in those squares.

#### b) Scatterplots between each pair of variables

```
pairs(trackData[,2:8], pch = ".", cex = 1.5)
```



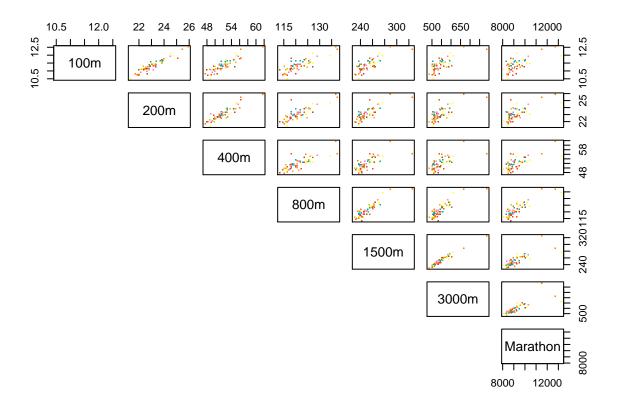
 $\mathbf{c})$ 

```
### Chernoff faces.
ncolors=c("pink","blue","red","yellow","green","purple","orange","magenta")
faces(trackData[,2:8],face.type=1, col.face =rainbow(50)) ## with colour
```

```
9
17
25
33
41
          10
          18
                   19
                             20
                                                          31
39
                                                 <u>30</u>
          26
                   27
                                       29
                                                 <u>38</u>
                                       37
                                                 46
                             44
                                       45
          42
          50
                             <u>52</u>
                                                 54
                   51
```

```
## "smiling
                     " "3000m"
## "height of eyes
                    " "Marathon"
                     " "100m"
## "width of eyes
## "height of hair
                    " "200m"
## "width of hair " "400m"
## "style of hair
                    " "800m"
## "height of nose " "1500m"
## "width of nose
                    " "3000m"
                    " "Marathon"
## "width of ear
## "height of ear
                    " "100m"
stars(trackData[,2:8], key.loc = c(14, 2), main = "Meters : stars(*, full = F)", full = FALSE)
    Meters : stars(*, full = F)
\triangle
\Delta
                                    \triangle
      \triangle
                                     1500m 400m
3000m 200m
Marathon 100m
A
            \triangle
my_cols <- c("#00AFBB", "#E7B800", "#FC4E07", "#ff7f00", "#ffff33", "#a65628", "#f781bf")
pairs(trackData[,2:8], pch = ".", cex = 1.5,
      col = my_cols,
```

lower.panel=NULL)



### Question 3: Examining for extreme values

## Appendix

```
knitr::opts_chunk$set(echo = TRUE)
library(ggplot2)
library(aplpack) # for Chernoff faces
library(gridExtra)

trackData = read.table("T1-9.dat")
colnames(trackData) = c("Countries", "100m", "200m", "400m", "800m", "1500m", "3000m", "Marathon")
samplesnames = c("100m", "200m", "400m", "800m", "1500m", "3000m", "Marathon")
trackData[,5:8] = trackData[,5:8]*60
trackData_Mean = colMeans(trackData[,2:8])
trackData_SD = apply(trackData[,2:8], 2, sd)
trackData_Median = apply(trackData[,2:8], 2, median)

plt100 = ggplot()+
    geom_histogram(aes(x=trackData$`100m`, y=..density..), color = "black", fill = "#343434",alpha=0.5,bir
geom_vline(aes(xintercept = trackData_Mean[1],color="Mean"))+
geom_vline(aes(xintercept = trackData_Median[1],color="Median"))+
```

```
geom_density(aes(x=trackData$`100m`, y=..density..), fill="lightpink", alpha=0.2)+
  theme()
plt200 = ggplot() +
  geom_histogram(aes(x=trackData$^200m`, y= ..density..), color = "black", fill = "#343434",alpha=0.5,b
  geom_vline(aes(xintercept = trackData_Mean[2],color="Mean"))+
  geom_vline(aes(xintercept = trackData_Median[2],color="Median"))+
  geom_density(aes(x=trackData$^200m^, y=..density..), fill="lightpink", alpha=0.2)+
  theme()
plt400 = ggplot()+
  geom_histogram(aes(x=trackData$^400m`, y= ..density..), color = "black", fill = "#343434",alpha=0.5,b
  geom_vline(aes(xintercept = trackData_Mean[3],color="Mean"))+
  geom_vline(aes(xintercept = trackData_Median[3],color="Median"))+
  geom_density(aes(x=trackData$`400m`, y=..density..), fill="lightpink", alpha=0.2)+
  theme()
plt800 = ggplot()+
  geom_histogram(aes(x=trackData$`800m`, y= ..density..), color = "black", fill = "#343434",alpha=0.5,b
  geom_vline(aes(xintercept = trackData_Mean[4],color="Mean"))+
  geom_vline(aes(xintercept = trackData_Median[4],color="Median"))+
  geom_density(aes(x=trackData$`800m`, y=..density..), fill="lightpink", alpha=0.2)+
  theme()
plt1500 = ggplot()+
  geom_histogram(aes(x=trackData$\cdot 1500m\cdot, y= ..density..), color = "black", fill = "#343434",alpha=0.5,
  geom_vline(aes(xintercept = trackData_Mean[5],color="Mean"))+
  geom_vline(aes(xintercept = trackData_Median[5],color="Median"))+
  geom_density(aes(x=trackData$`1500m`, y=..density..), fill="lightpink", alpha=0.2)+
  theme()
plt3000 = ggplot() +
  geom_histogram(aes(x=trackData$`3000m`, y= ..density..), color = "black", fill = "#343434",alpha=0.5,
  geom_vline(aes(xintercept = trackData_Mean[6],color="Mean"))+
  geom_vline(aes(xintercept = trackData_Median[6],color="Median"))+
  geom_density(aes(x=trackData$`3000m`, y=..density..), fill="lightpink", alpha=0.2)+
  theme()
pltM = ggplot()+
  geom_histogram(aes(x=trackData$`Marathon`, y= ..density..), color = "black", fill = "#343434",alpha=0
  geom_vline(aes(xintercept = trackData_Mean[7],color="Mean"))+
  geom_vline(aes(xintercept = trackData_Median[7],color="Median"))+
  geom_density(aes(x=trackData$`Marathon`, y=..density..), fill="lightpink", alpha=0.2)+
  theme()
grid.arrange(plt100,plt200,plt400,plt800, ncol=2)
grid.arrange(plt1500,plt3000,pltM, ncol=2)
trackData_Cov = cov(trackData[,2:8])
trackData_Cor = cor(trackData[,2:8])
heatmap(trackData_Cor, col = terrain.colors(256), Rowv=NA, Colv=NA, revC=T)
pairs(trackData[,2:8], pch = ".", cex = 1.5)
### Chernoff faces.
ncolors=c("pink","blue","red","yellow","green","purple","orange","magenta")
```