

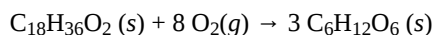
3.9.3: Foods- Fat vs. Sugar Metabolism

One of the most useful features of thermochemical equations is that they can be combined to determine ΔH_m values for other chemical reactions which have never been observed. We might want to see what ΔH_m would be if we could carry out a reaction that has never been done, or it might be interesting for theoretical reasons.

For example, we have noted that the body would have to store up to 67.5 lb of sugar complexes for the energy equivalent of 10 lb of fat.^[1]



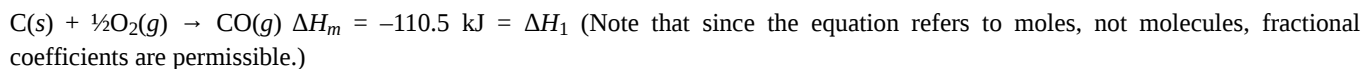
In Example 1 below, we calculate the energy for the *hypothetical reaction* in which a fat is converted to sugar:



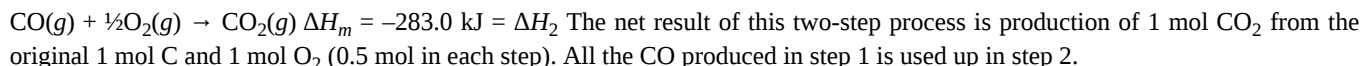
ΔH_m for this reaction is the extra energy our body can get from a fat.

A Simple Case

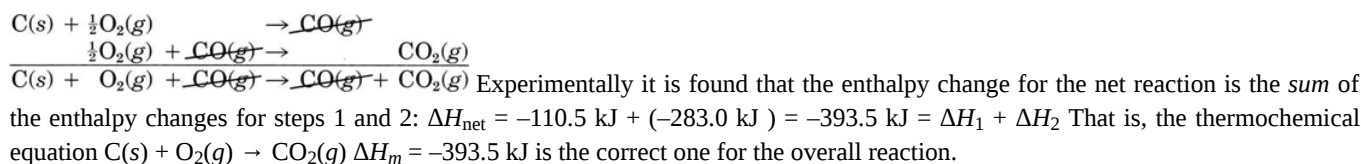
But first, a simpler example may help to make the method clear. Instead of the oxidation of a complicated fat molecule, we'll consider the simplest possible oxidation, a sequence in which carbon itself is oxidized. Step 1 is the oxidation of 1 mol C(s) and 0.5 mol $\text{O}_2(\text{g})$ to form 1 mol $\text{CO}(\text{g})$:



In step 2 the some of the mole of CO reacts with an additional 0.5 mol O_2 yielding 1 mol CO_2 :



On paper this net result can be obtained by *adding* the two chemical equations as though they were algebraic equations. The CO produced is canceled by the CO consumed since it is both a reactant and a product of the overall reaction



Hess' Law

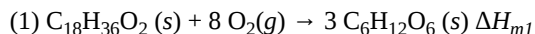
In the general case it is always true that *whenever two or more chemical equations can be added algebraically to give a net reaction, their enthalpy changes may also be added to give the enthalpy change of the net reaction.*

This principle is known as **Hess' law**. If it were not true, it would be possible to think up a series of reactions in which energy would be created but which would end up with exactly the same substances we started with. This would contradict the law of conservation of energy. Hess' law enables us to obtain ΔH_m values for reactions which cannot be carried out experimentally, as the next example shows.

Example 1: Fat vs. Sugar Metabolism

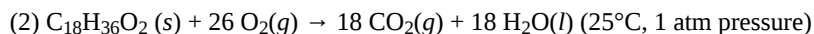
EXAMPLE 1

Although fat metabolism is a complicated process (called "beta oxidation") which yields the ATP that releases energy to muscle, we could imagine a reaction that helps us understand why fats store so much energy compared to sugar. We could imagine the combustion of stearic acid to the sugar, glucose, according to the equation

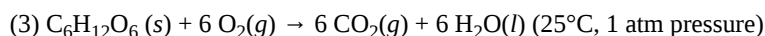


This would represent the "extra" energy that fats provide, over the energy that metabolism of a sugar like glucose provides.

Calculate ΔH_{m1} for this reaction from the following thermochemical equations, (which are heats of combustion that are easily determined experimentally):



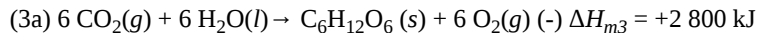
$$\Delta H_{m2} = -11\,407 \text{ kJ} \quad [2]$$



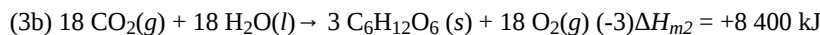
$$\Delta H_{m3} = -2\,800 \text{ kJ} \quad [3]$$

Solution

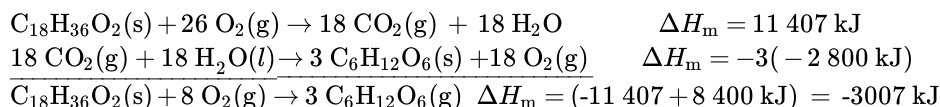
We see that reaction (3) has glucose ($\text{C}_6\text{H}_{12}\text{O}_6$) on the left, but the target reaction (1) has it on the right. We'll need to reverse equation (3), and then combine it with equation (2) to get the target equation (1). If we reverse (3), we change the sign on ΔH_{m3} :



But we also might notice that the target equation contains no $\text{CO}_2(\text{g})$ or $\text{H}_2\text{O}(\text{l})$, so we'll need to multiply equation (3) by 3, so that there will be an equal amount of $\text{CO}_2(\text{g})$ or $\text{H}_2\text{O}(\text{l})$ on the left and right, and they will cancel. Multiplying equation (3a) by 3:



When we combine this equation, and its associated ΔH_m with Equation (2), we get the target reaction, (1):



$$\Delta H_{m1} = \Delta H_{m2} + (-3)\Delta H_{m3} = -11\,407 + 8400 \text{ kJ}$$

$$\Delta H_{m1} = -3\,007 \text{ kJ}$$

So one mole (284.48 g) of stearic acid releases 3 007 kJ when it's oxidized to 3 mol of glucose. This is 10.57 kJ/g, or 2.5 Cal/g that we get from fat but not from sugar.

Additionally, for every gram of stearic acid, we get the energy from 1.900 g of glucose (see the stoichiometry summary table below), which provides 4 Cal per gram. This is 1.90 g x 4 Cal/g = 7.59 Cal, so the total energy from 1 g of fat is 2.5 + 7.6 = 10.1 Cal in this case (similar to the 9 Cal/g estimate for typical fats).

Solution to Example 1

	$\text{C}_{18}\text{H}_{36}\text{O}_2$	+ 8 O_2	$\rightarrow 3 \text{C}_6\text{H}_{12}\text{O}_6$
m (g)	1.00	0.900	1.90
M (g/mol)	284.4	32.0	180
n (mol)	0.00352	0.281	0.0106

References

1. Energy from Fats and Sugars
2. home.fuse.net/clymer/rq/hocatable.html
3. home.fuse.net/clymer/rq/hocatable.html

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