

## 17.13: Galvanic Cells and Free Energy

We see in the section on the Electromotive Force of Galvanic Cells that the emf of a galvanic cell can tell us whether the cell reaction is spontaneous. In other sections we show that the free-energy change  $\Delta G$  of a chemical process also indicates whether that process is spontaneous. It is quite reasonable, then, to expect some relationship between  $\Delta G$  and E, and indeed one exists.

In the section on Free Energy we stated that the free-energy change corresponds to the maximum quantity of useful work which can be obtained when a chemical reaction occurs. In other words,

$$\triangle G = -w_{max}$$

where the minus sign is necessary because the free energy decreases as the chemical system does useful work on its surroundings. If we are referring to a redox reaction, that work can be obtained in electrical form by means of an appropriate galvanic cell. It can be measured readily, because when a quantity of charge Q moves through a potential difference  $\Delta V$ , the work done is given by

$$w = Q \triangle V$$

Thus if one coulomb passes through a potential difference of one volt, the work done is

$$w = 1 \text{ C} \times 1 \text{ V} = 1 \text{ As} \times 1 \text{ J A}^{-1} \text{ s}^{-1} = 1 \text{ J}$$

Now suppose we construct a Zn-Cu cell of the type described earlier:

$$Zn|Zn^{2+}(1 M) \parallel Cu^{2+}(1 M)|Cu$$

and suppose we make the cell large enough that the concentrations of  $Cu^{2+}$  and  $Zn^{2+}$  will not change significantly even though 1 mol Zn is oxidized to 1 mol  $Zn^{2+}$  according to the cell reaction

$$\operatorname{Zn}(s) + \operatorname{Cu}^{2+}(\operatorname{aq}) \longrightarrow \operatorname{Zn}^{2+}(\operatorname{aq}) + \operatorname{Cu}(s)$$
 (17.13.1)

If this cell is discharged through a large enough resistance, the potential difference will have its maximum value, namely, the cell emf,  $E^{\circ}$ ; so if we know how much charge is transferred, we can calculate the electrical work done. For the oxidation of 1 mol Zn [that is, for the occurrence of 1 mol of reaction 17.13.1], there must be 2 mol  $e^{-}$  transferred according to the half-equation

$$\operatorname{Zn}(s) \longrightarrow \operatorname{Zn}^{2+}(\operatorname{ag}) + 2e^{-}$$

Therefore the quantity of electrical charge transferred per mole of reaction is

$$Q_{m} = 2 \cdot \mathrm{F} {=} 2 \cdot 9 \cdot 649 \, \times 10^{\,4} \mathrm{Cmol}^{-1} {=} 1 \cdot 930 \cdot 10^{\,5} \mathrm{Cmol}^{-1}$$

(The Faraday constant, F, is the quantity of charge per mole of electrons. It has the value 96,485 C/mol.) The maximum useful work per mole of reaction which the cell can perform while discharging is thus

$$w_{max} = Q_m E^o = 2 \text{ FE}^o = 2 \cdot 9 \cdot 649 \cdot 10^4 \text{Cmol}^{-1} \cdot 1 \cdot 10 \text{ V} = 212 \frac{\text{kJ}}{\text{mol}}$$

The standard molar free energy change for the cell reaction is thus

$$\Delta G_m^o = -w_{max} = -2FE^o = -212 \frac{\mathrm{kJ}}{\mathrm{mol}}$$

A similar argument can be applied to any cell in which the reactants and products are all at their standard concentrations or pressures. If the standard emf of such a cell is  $E^{\circ}$ , while  $\Delta G_m^{\circ}$  is the standard molar free energy change for the cell reaction, these two quantities are related by the equation

$$\Delta G_m^o = -\,zFE^\circ$$

where *z* (a dimensionless number) corresponds to the number of moles of electrons transferred per mole of cell reaction. A similar relationship holds even when reactants and products are not at standard concentrations and pressure:

$$\Delta G_m = -zFE$$



This connection between cell emf and free-energy change provides a means of measuring  $\Delta G_m$ , directly, rather than by determining  $\Delta H_m$ , and  $\Delta S_m$ , and then combining them.

## $\checkmark$ Example 17.13.1: The emf of a Cell

$$\mathrm{Pt}, \mathrm{H}_2(1\,\mathrm{atm}) \mid \mathrm{H}^+(1\,\mathrm{M}) \mid \mathrm{O}_2(1\,\mathrm{atm}), \mathrm{Pt}$$

is 1.229 V at 298.15 K. Calculate  $\Delta G_f^{\, \circ}$  for liquid water at this temperature.

Solution: The half-equations for the cell are

$$2\,\mathrm{H_2(g)} \longrightarrow 4\,\mathrm{H^+(aq)} + 4e^-$$

$$\begin{split} &2\,\mathrm{H}_2(\mathrm{g}) \longrightarrow 4\,\mathrm{H}^+(\mathrm{aq}) + 4e^- \\ &4e^- + 4\,\mathrm{H}^+(\mathrm{aq}) + \mathrm{O}_2(\mathrm{g}) \longrightarrow 2\,\mathrm{H}_2\mathrm{O}(\mathrm{l}) \end{split}$$

so that the cell reaction is

$$2\,\mathrm{H_2(g)} + \mathrm{O_2(g)} \longrightarrow 2\,\mathrm{H_2O(l)} \quad 1\;\mathrm{atm},\,298.15\;\mathrm{K}$$

Since there are 4 mol  $e^-$  transferred per mol cell reaction, z = 4 and

$$\Delta G_m = -zFE = -4 imesrac{9.649*10^4\mathrm{C}}{1\mathrm{\ mol}} imes1.229\mathrm{V} = -474.3rac{\mathrm{kJ}}{\mathrm{mol}}$$

The reaction produces liquid water at standard pressure and the desired temperature, but 1 mol reaction produces 1 mol  $2H_2O(l)$ , that is, 2 mol  $H_2O$ . Therefore

$$riangle G_f^o[ ext{H}_2 ext{O}(l), 298 ext{ K}] = rac{1}{2} riangle G_m = -237.2rac{ ext{kJ}}{ ext{mol}}$$

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