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1 import numpy as np
2 from FixedVariables import gamma
3 from TimeIntegration import make_mesh
4 from FixedVariables import xmax, xmin
5 from InputVariables import var
6
7 G = gamma
8 Ms = 1.44061
9
10 # compute the pressure, density, velocity and the speed of sound
    from an 3-dimensional array of primitive variables.
11 def p_(w):
12     return w[-1]
13
14 def rho_(w):
15     return w[0]
16
17 def v_(w):
18     return w[1]
19
20 def a_(w):
21     return np.sqrt(G*p_(w)/rho_(w))
22
23 # computes the values of density, velocity and pressure in the five
    different regions
24 def RegionR():
25     return [1, 0, 1]
26
27 def RegionL():
28     return [8, 0, 8/G]
29
30 def Region1():
31     R = RegionR()
32     one = [0, 0, 0]
33     one[0] = rho_(R)/(2/((G+1)*np.square(Ms)) + (G-1)/(G+1))
34     one[1] = (2/(G+1)*(Ms - 1/Ms))
35     one[2] = ((2*G*np.square(Ms))/(G+1) - (G-1)/(G+1))*p_(R)
36     return one
37
38 def Region2():
39     one = Region1()
40     L = RegionL()
41     two = [0, 0, 0]
42     two[1] = v_(one)
43     two[2] = p_(one)
44     two[0] = np.power(p_(two)/p_(L), 1/G)*rho_(L)
45     return two

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46
47 def RegionE(i, t):
48     L = RegionL()
49     E = [0, 0, 0]
50     E[1] = (2/(G+1))*(a_(L) + i/t)
51     a = a_(L) - (G-1)*v_(E)/2
52     E[2] = p_(L)*np.power(a/a_(L), 2*G/(G-1))
53     E[0] = (G*p_(E))/(np.square(a_(L) - (G-1)*v_(E)/2))
54     return E
55
56 # computes for time t the analytic solution as a (nx, 3)-dimensional
    array
57 def analytic_solution(nx, t):
58     x = make_mesh(xmin, xmax, nx)
59     x.pop(0)
60     x.pop(-1)
61     a_sol = []
62     R = RegionR()
63     L = RegionL()
64     one = Region1()
65     two = Region2()
66     for i in range(nx):
67         if x[i] < -a_(L)*t:
68             a_sol.append(L)
69         elif x[i] >= -a_(L)*t and x[i] <= (v_(two)-a_(two))*t:
70             a_sol.append(RegionE(x[i], t))
71         elif x[i] > (v_(two)-a_(two))*t and x[i] < v_(two)*t:
72             a_sol.append(two)
73         elif x[i] >= v_(two)*t and x[i] <= Ms*t:
74             a_sol.append(one)
75         else:
76             a_sol.append(R)
77     return a_sol
78
79 # computes from the analytic solution the values for density,
    velocity and pressure
80 def analytic_solver(nx, t):
81     A = analytic_solution(nx, t)
82     if var == 'mass density':
83         a = [A[i][0] for i in range(nx)]
84     elif var == 'velocity':
85         a = [A[i][1] for i in range(nx)]
86     elif var == 'pressure':
87         a = [A[i][2] for i in range(nx)]
88     return a
89
90

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