

# **A Connection Between Star Formation Rate and Dark Matter Halos at $Z \sim 6$ In 2013 Planck Cosmology.**

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## ABSTRACT

This work relates baryonic matter and dark matter at redshift  $z = 5.9$  using observational data from CFHTLS (Willott et al. 2013), HST Legacy Survey (Bouwens et al. 2014; Finkelstein et al. 2014), UKIDSS and SDXS (McLure et al. 2009), and results of the Multidark Simulation (Klypin et al. 2014) in a cubic box of  $1000\text{Mpc h}^{-1}$  length with 2013 Planck Cosmology (Planck Collaboration et al 2014). The Luminosity Function (LF) is fitted via four parameters with the Markov Chain Monte Carlo method. The relationship between the Dark Matter Halos Mass and Star Formation Rate is obtained using the relationship between the UV continuum (from the fitted LF) and Star Formation Rate (SFR) by Kennicutt (1998). Cosmic variance effects are studied on smaller boxes of  $250\text{Mpc h}^{-1}$  length.

*Subject headings:* Dark Matter, UV Luminosity Function, Star Formation Rate, High Redshift Galaxies, Reionization

## 1. Observations

This paper is based on four main observational data sets from the Hubble Space Telescope and three ground-based telescopes. All  $z \sim 6$  LBG candidates were discovered using the drop-out technique (Steidel et al. 2003). All magnitudes are in AB system.

The data from the Hubble Space Telescope Legacy (HSTL) (Bouwens et al. 2014) is a compilation of observations since the installation of the Advanced Camera for Surveys (ACS) in 2002, through the near-infrared Wide Field Camera 3 (WFC3/IR) installed in 2009, up to 2012. The HST fields of view are: XDF, HUDF09-1, HUDF09-2, CANDELS-S/Deep, CANDELS-S/Wide, ERS, CANDELS-N/Deep, CANDELS-N/Wide, CANDELS-UDS, CANDELS-COSMOS and CANDELS-EGS, with areas of 4.7, 4.7, 4.7, 64.5, 34.2, 40.5, 62.9, 60.9, 151.2, 151.9 and 150.7 arcmin<sup>2</sup> respectively. The total area corresponds to  $\sim 0.7 \text{ deg}^2$  over five different lines of sight, reducing cosmic variance effects. Two cameras performed the observations: ACS and WFC3/IR, using  $B_{435}$ ,  $V_{606}$ ,  $i_{814}$ ,  $z_{850}$ ,  $I_{814}$ ,  $Y_{098}$ ,  $Y_{105}$ ,  $J_{125}$ ,  $JH_{140}$  and  $H_{160}$  filters. The limit magnitude is between  $\sim 27.5 \text{ mag}$  in CANDELS-EGS and  $\sim 30 \text{ mag}$  in the deepest field (XDF). Total number of  $z=6$  LBG candidates is 940, most of them in the faint end of the LF, magnitudes in the rest frame are in the range  $-22.52 \leq M_{1600} \leq -16.77$  ? calculated LF using a stepwise maximum-likelihood (SWML) based on Efstathiou et al. (1988). The Schechter parameters derived are:  $\phi^* = (0.33^{+0.15}_{-0.10}) \times 10^{-3} / \text{Mpc}^{-3}$ ,  $M_{1600}^* = -21.16 \pm 0.20$  and  $\alpha = -1.91 \pm 0.09$ . Bouwens et al. (2014) reported that using just few fields of view, UVLF has a slightly non-Schechter-like form.

Finkelstein et al. (2014) worked also with HST, using the HUDF, CANDELS and GOODS fields, along with two of the Hubble Frontier Fields (HFF): deep parallel observations (unlensed fields) near the Abell 2744 and MACS J0416.1-2403 clusters. The HFF uses the ACS and the WFC3/IR with the same filters aforementioned but  $z_{850}$ .

Willott et al. (2013) presented the sixth release of the Canada-France-Hawaii Telescope Legacy Survey CFHTLS. The observations were performed over four separated fields covering a total area  $\sim 4 \text{ deg}^2$  (a large area), it gives this survey great robustness. Optical observations used MegaCam with  $u^*g'r'i'z'$  filters. The main selection criteria: all the objects must be brighter than magnitude  $z' = 25.3$ . The final number of LBGs founded was 40. Moreover, they get spectroscopic confirmation for 7 candidates using GMOS spectrograph on the Gemini Telescopes, which has a  $\ll 5.5$ -square arcmin field of view. They show incompleteness in the sample due to foreground contamination and the detection algorithm; there is no warranty to have every object brighter than the limit magnitude on the faint limit. The full galaxy LF at  $z = 6$  cannot be obtained as in other studies. Nevertheless, this survey was focussed on the highly luminous LBGs. LF is calculated using the stepwise maximum likelihood method of Efstathiou et al. (1988), within magnitudes from  $M_{1350} = -22.5$  up to  $-20.5$ . The luminosity function of  $z = 5.9$  shows an exponential decline at the bright end, where feedback processes and inefficient last cooling limit star forming in bright galaxies hosted in the most massive halos.

McLure et al. (2009) build the luminosity function for  $z = 5$  and  $z = 6$  using data from two ground-based telescopes: the United Kingdom Infrared Telescope in the near-IR imaging and Subaru Telescope for the optical imaging. They use the first data release of the UKIRT Infrared DeepSky Survey Ultra Deep Survey (UDS), together with the Subaru XMM-Newton Survey (SXDS). Total observed area is  $0.63 \text{ deg}^2$  uniformly covered by both catalogues. The UKIRT was equipped with the WFCAM using  $JK$  filters. The Subaru was equipped with the Suprime-Cam with the  $BVRi'z'$  filters. All candidates were brighter than  $z' = 26$ . The UV rest frame magnitude range is  $-22.4 \leq M_{1500} \leq -20.6$ . The LF was calculated using the maximum likelihood estimator of Schmidt (1968). Their analysis gave a total number of 104 LBG candidates in the redshift range  $5.7 \leq z \leq 6.3$ . LF was parameterized according to the Schechter function with  $\phi^*/\text{Mpc}^{-3} = (1.8 \pm 0.5) \times 10^{-3}$ ,

$M_{1500}^* = -20.04 \pm 0.12$  and  $\alpha = -1.71 \pm 0.11$ .

The dataset was retrieved from McLure et al. (2009) graph using GAVO-DEXTER<sup>1</sup>.

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<sup>1</sup><http://dc.zah.uni-heidelberg.de/dexter/ui/ui/custom>

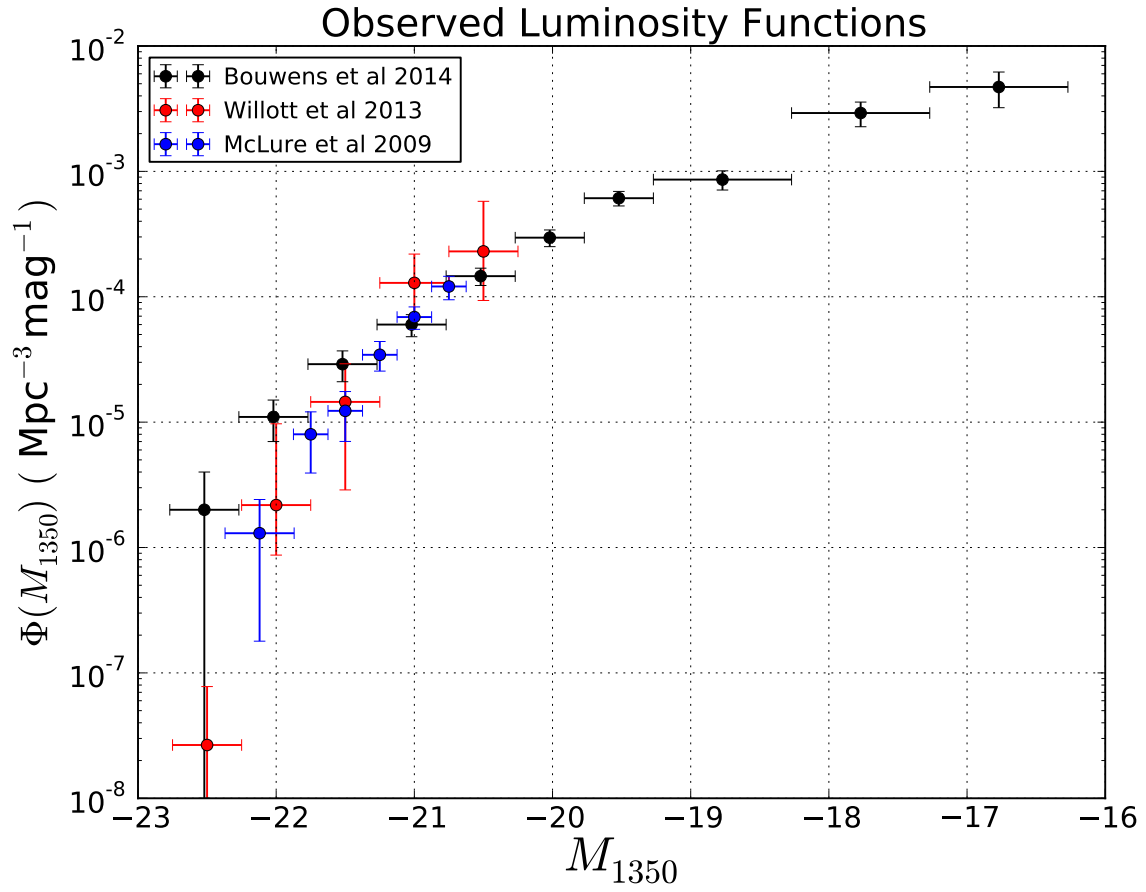


Fig. 1.— Observational data from Bouwens et al. (2014); McLure et al. (2009) and Willott et al. (2013).

## 2. Methodology

The key element to connect SFR with halo mass from simulations is the observed UVLF. If there exist a function whom gives to each halo a UV luminosity then is posible to reproduce UVLF from DMH catalogs. The fitting parameters can be explored using a Markov Chain Monte-Carlo (MCMC) implementation. Once the parameters are found, the SFR-Halo Mass relation have been found.

We use the dark matter halo catalog from the Big MultiDark Plank 1 (MDPL) Simulation (Klypin et al. 2014) with 2013 Planck cosmology (Planck Collaboration et al 2014). MDPL is quite similar to the Big Bolshoi ( $1\text{Gpc h}^{-1}$ ) (Prada et al. 2012) and its predecesor Bolshoi (Klypin et al. 2011) ( $250\text{Mpc h}^{-1}$ ), booth of them with WMAP5 cosmology, but MDPL has bigger mass resolution. Those halo catalogs are available at the MultiDark Database<sup>2</sup> (Riebe et al. 2013).

The MDPL run is a N-body dark matter only simulation based on the L-Gadget2 code. The simulated volume is a cubic box of  $1\text{Gpc h}^{-1}$  side length. It has  $3840^3$  dark matter particles of  $1.51 \times 9\text{M}_{\odot}\text{h}^{-1}$  mass each one. The 2013 Planck cosmology is defined by the following parameters:  $\Omega_M = 0.307$ ,  $\Omega_B = 0.048$ ,  $\Omega_{\Lambda} = 0.730$ ,  $\sigma_8 = 0.829$ ,  $n_s = 0.96$  and  $H_0 = 67.8$ . The DMH Catalog at  $z = 6$  contains  $\sim 10.9 \times 10^7$  halos, to avoid incompleteness in the low mass end, halos with mass below  $10^{10.3}\text{M}_{\odot}\text{h}^{-1}$  are rejected. In order to study how cosmic variance can affect measurements, the original catalog is divided into 64 small cubic boxes, with a similar volume to the observations.

The following treatment is applied to every one small box.

The halo abundance matching technique has been widely used (Colín et al. 1999; Kravtsov et al. 2004) resulting in good reproduction of the observed galaxy clustering.

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<sup>2</sup><http://www.multidark.org>

(Conroy et al. 2006; Lee et al. 2009). Here we use the simplest case with few premises:

1. Each halo in the catalog hosts one galaxy. There are not empty halos, also none of halos has two or more galaxies.
2. The UV luminosity of each galaxy is function of one variable; the mass of the DMH in which is located. This function must be monotone, this guarantees that most massive halos will host the most luminous galaxies in the same volume.

## 2.1. Fitting Model

The observed UV Luminosity Function has two slopes. To reproduce it we decide to use the four parameter model:

$$L_{\text{UV}}(M) = L_0 M \left[ \left( \frac{M}{M_0} \right)^{-\beta} + \left( \frac{M}{M_0} \right)^{\gamma} \right]^{-1} \quad (1)$$

where  $M$  is the hosting DMH mass,  $L_0$  is a normalization constant,  $M_0$  is the critical mass where the luminosity function has a slope change,  $\beta$  and  $\gamma$  are the slopes. This equation has a similar fashion to the mass to light relation (van den Bosch et al. 2003) and the mean relation between stellar mass of a galaxy and the mass of its halo used by Moster et al. (2010).

## 2.2. Dust Attenuation

Dust in galaxies absorbs part of the UV radiation and reemits on IR. The more massive is the galaxy then more dust contains and dust attenuation will be bigger.

The UV Spectral Slope  $\beta$  was introduced by Meurer et al. (1999) as a color index to study dust attenuation in high redshift galaxies calibrating with local galaxies. This index



is becomes from a power law fitting, with the flux  $f$  as function of the wavelength  $\lambda$ ,

$$f \propto \lambda^\beta$$

, The relation they found is:

$$A = 4.43 + 1.99\beta \quad (2)$$

.

Bouwens et al. (2012b) found a linear relation between  $\beta$  and the UV magnitude.

$$\langle\beta\rangle = \frac{d\beta}{dM_{UV}} (M_{UV,AB} + 19.5) + \beta_{M_{UV}=-19.5} \quad (3)$$

We use a similar dust attenuation model as the used by Smit et al. (2012) with  $\beta_{M_{UV}=-19.5} = -2.20$  and  $d\beta/dM_{UV} = -0.21$  at  $z = 5.9$  according (?)bouwens12b), imposing also the condition:

$$A \geq 0$$

### 2.3. MCMC

We used a Markov Chain Monte Carlo method to find the best parameters and its uncertainties over each one of the boxes and each observational dataset.

Observational data set to fit is selected. A halo catalog of a cubic box of length 250 Mpc h-1 is selected. Initial parameters are introduced.

An UV luminosity is given to each halo as function of his mass according to equation 1. Luminosity is converted to magnitude using:

$$M_U = 51.82 - 2.5 \log_{10}(L_U).$$

The luminosity function is constructed as an histogram of the magnitudes normalized by the volume of the catalog. Each observed luminosity function has a different bin range.

Once having the LF, we compare our LF against observed LF. Our likelihood estimator is the sum of the square difference over each bin, divided by the number of degrees of freedom. We worked on the logarithmic space of luminosities to have a good fitting on six decades.

$$\chi^2 = \sum_{i=0}^n (x_{i,obs} - x_{i,fit})^2$$

$$\mathcal{L} \propto \exp\left(\frac{\chi^2}{n}\right)$$

Then we have a small variation on the parameters, it gives us a new LF and a new likelihood estimator  $\chi^2$ .

We compare the new fitting versus the old fitting.

Some restrictions were imposed over two parameters to guarantee convergence in the MCMC method:  $0 \leq \alpha \leq 1.8$  and  $\gamma \geq 0$ .

Finally, the UV luminosity for each galaxy can be directly related with SFR according to Madau et al. (1998). This model is accurate within the range of  $10^8 - 10^9 \text{yr}$  (Kennicutt 1998). The relation between UV luminosity and Star Formation Rate (Madau et al. 1998; Kennicutt 1998) is given by:

$$\text{SFR} (M_{\odot} \text{yr}^{-1}) = 1.4 \times 10^{-28} L_{\nu} (\text{erg s}^{-1} \text{Hz}^{-1}) \quad (4)$$

### 3. Discussion

(Lundgren et al. 2014(@) SFR evolution from  $z = 1$  to 6

(Bouwens et al. 2014) HST Legacy

(Jiang et al. 2011) Keck spectroscopy

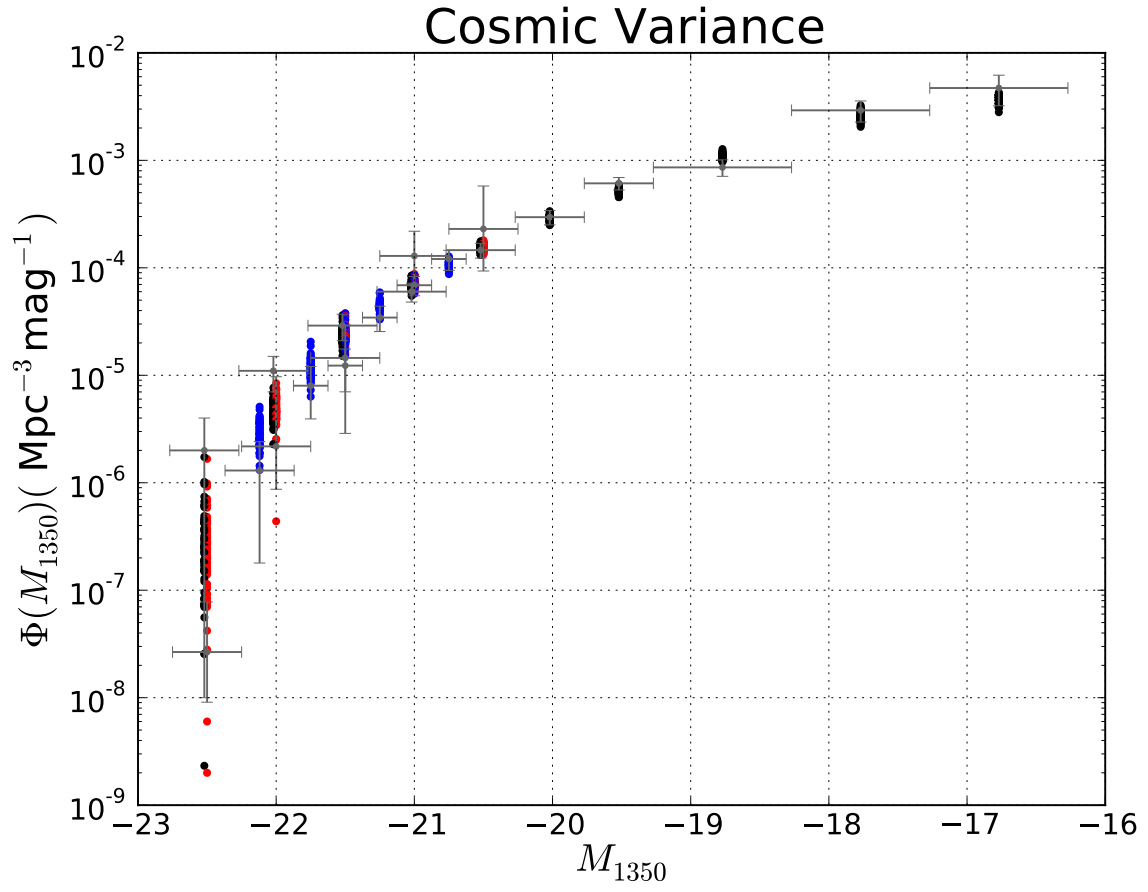


Fig. 2.— Cosmic Variance: The Luminosity Function is made using the DMH catalog from the full box and the set of parameters from the small boxes.

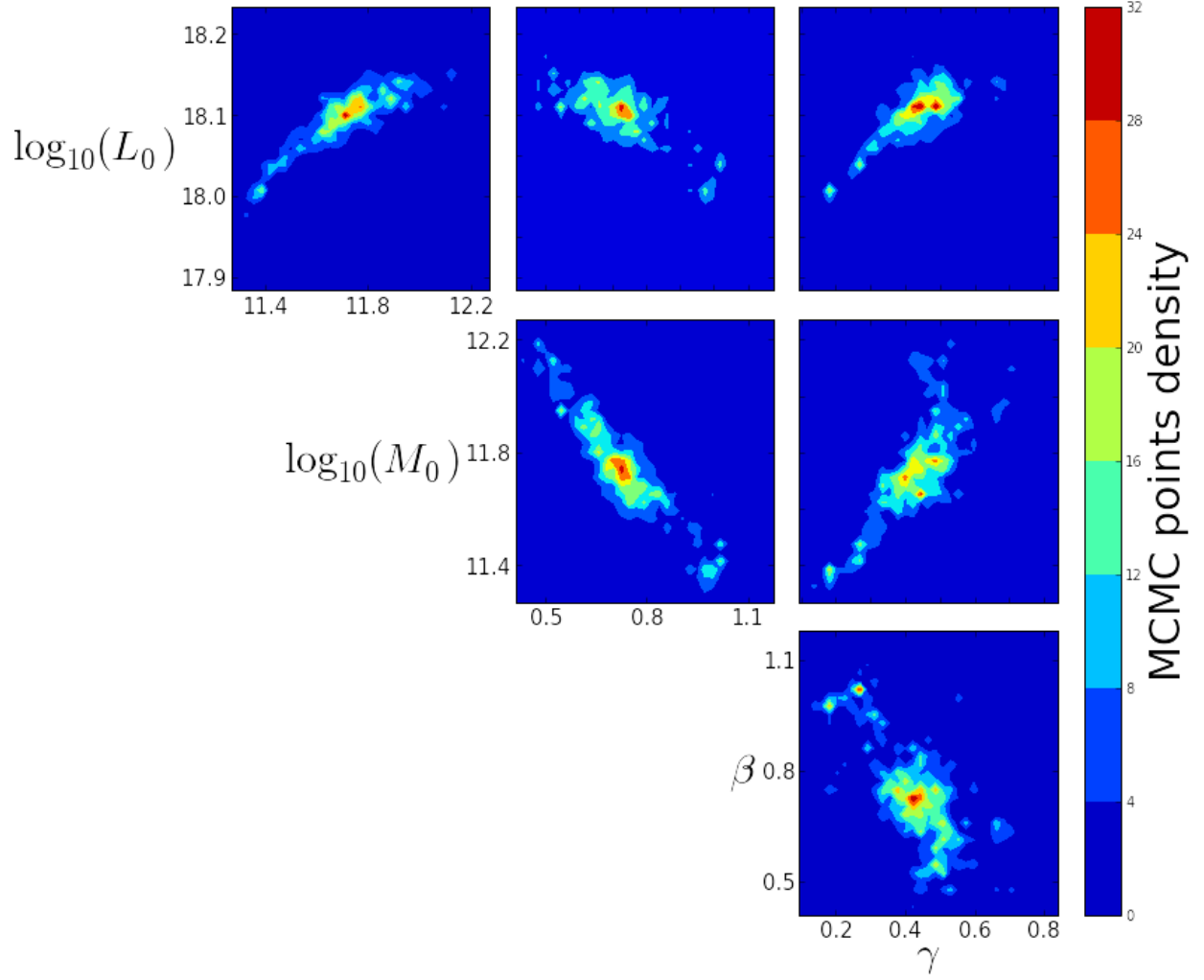


Fig. 3.— Covariance of parameters for one small box

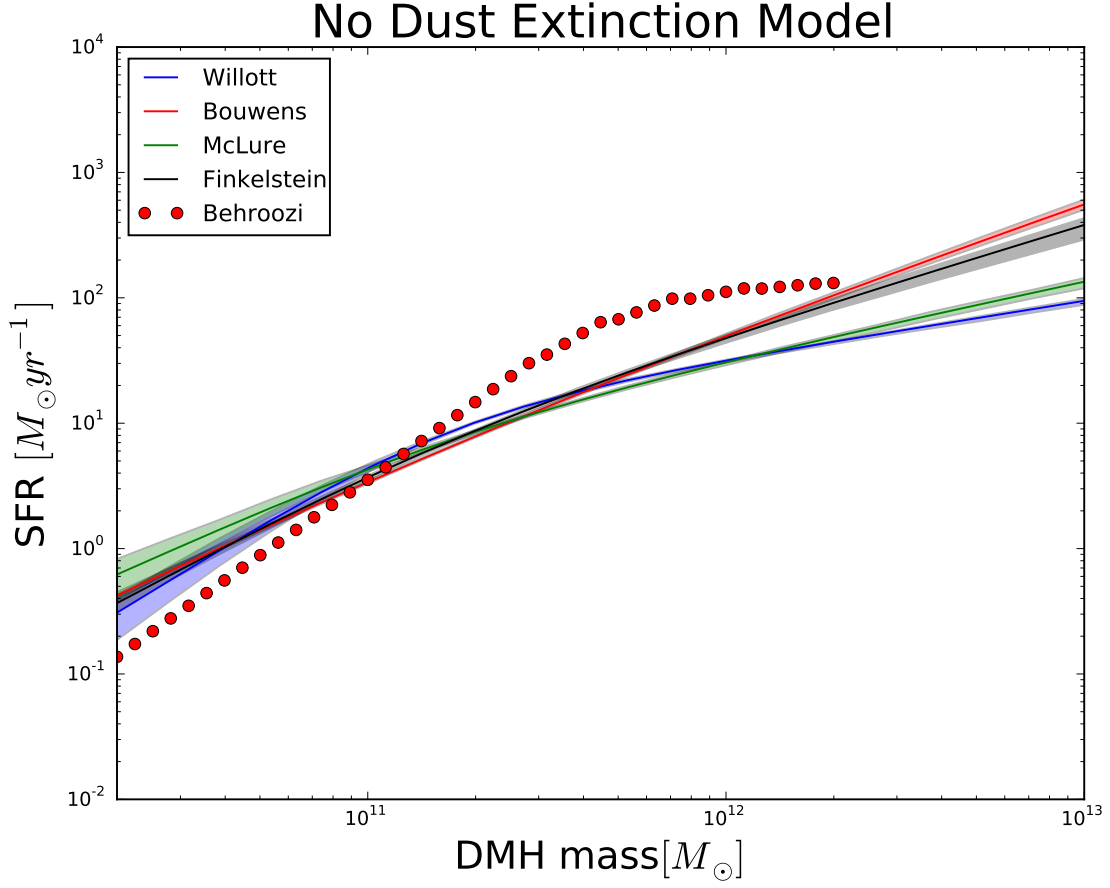


Fig. 4.— Star formation rate as function of the dark matter halo mass without dust attenuation. Solid lines represents the mean SFR value over the small boxes within 50% shaded region.

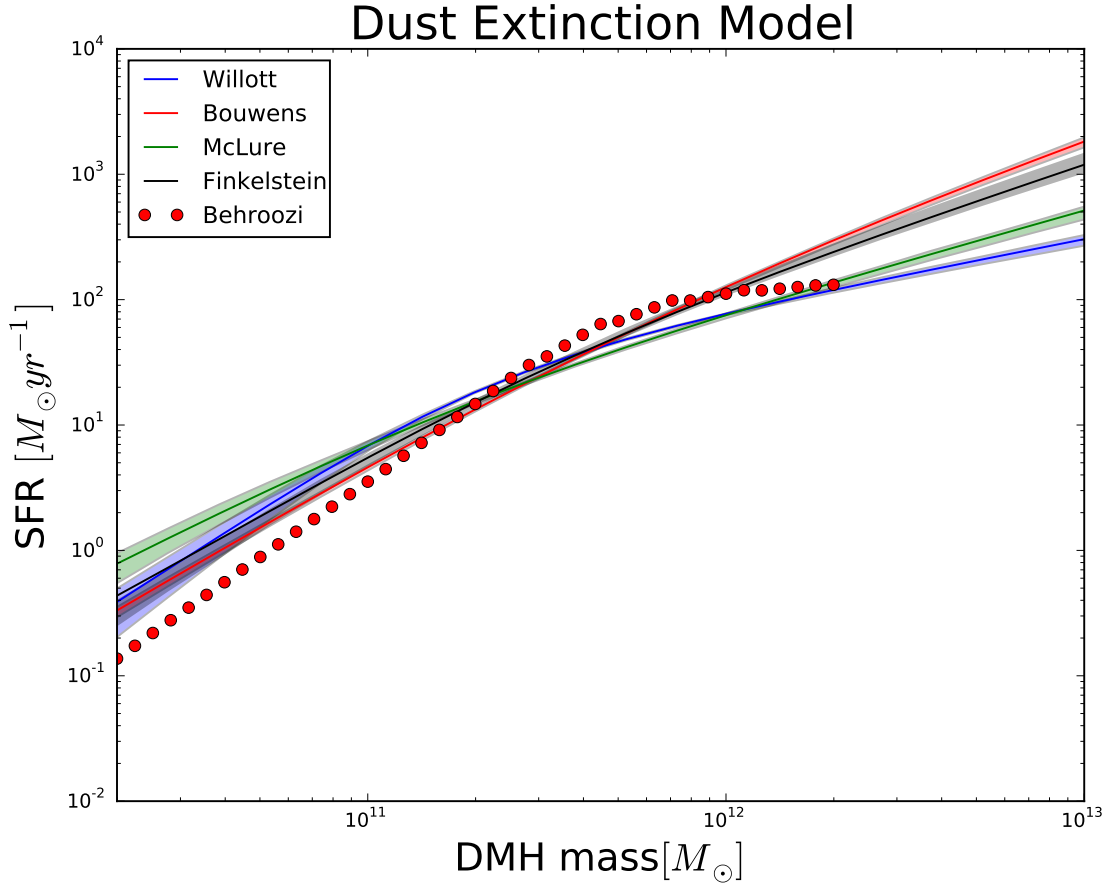


Fig. 5.— Star formation rate as function of the dark matter halo mass with dust attenuation. Solid lines represents the mean SFR value over the small boxes within 50% shaded region.

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