

12/12/2021

String Matching

Find substring in main string

↓
Pattern - m.↓
Text (length $\rightarrow n$)

1) $T = a b c d a b f a b e g$
 $P = a b e$

Sol: $T = \overset{0}{a} \overset{1}{b} \overset{2}{c} \overset{3}{d} \overset{4}{a} \overset{5}{b} \overset{6}{f} \overset{7}{a} \overset{8}{b} \overset{9}{e} \overset{10}{g}$
 $P = \overset{\downarrow}{a} \overset{\downarrow}{b} \overset{\times \downarrow}{e}$

$T = \overset{0}{a} \overset{1}{b} \overset{2}{c} \overset{3}{d} \overset{4}{a} \overset{5}{b} \overset{6}{f} \overset{7}{a} \overset{8}{b} \overset{9}{e} \overset{10}{g}$
 $P = \overset{\times \downarrow}{a} \overset{\times \downarrow}{b} e$

$T = \overset{0}{a} \overset{1}{b} \overset{2}{c} \overset{3}{d} \overset{4}{a} \overset{5}{b} \overset{6}{f} \overset{7}{a} \overset{8}{b} \overset{9}{e} \overset{10}{g}$
 $P = \overset{\times \downarrow}{a} b e$

$T = \overset{0}{a} \overset{1}{b} \overset{2}{c} \overset{3}{d} \overset{4}{a} \overset{5}{b} \overset{6}{f} \overset{7}{a} \overset{8}{b} \overset{9}{e} \overset{10}{g}$
 $P = \overset{\times \downarrow}{a} b e$

$T = \overset{0}{a} \overset{1}{b} \overset{2}{c} \overset{3}{d} \overset{4}{a} \overset{5}{b} \overset{6}{f} \overset{7}{a} \overset{8}{b} \overset{9}{e} \overset{10}{g}$
 $P = \overset{\downarrow}{a} \overset{\downarrow}{b} \overset{\times \downarrow}{e}$

$T = \overset{0}{a} \overset{1}{b} \overset{2}{c} \overset{3}{d} \overset{4}{a} \overset{5}{b} \overset{6}{f} \overset{7}{a} \overset{8}{b} \overset{9}{e} \overset{10}{g}$
 $P = \overset{\downarrow}{a} b e$

$T =$

	0	1	2	3	4	5	6	7	8	9	10
T	a	b	c	d	a	b	f	a	b	e	g
P									x	a	b

T =

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
P	0	0	0	0	1	0	0	0	1	0	1	0	0	0	1

$T =$

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
	0	0	0	0	1	0	0	0	1	0	1	0	0	0	1
			↓	↓	x ↓	↓									
$P =$			0	0	0	1									

$T = 000010001010001$
 $P = \quad \quad \quad \downarrow \downarrow \downarrow \downarrow$
 $\quad \quad \quad 0001$

$T =$

0	0	0	0	1	0	0	0	1	0	1	0	0	0	1
				X										
				↓	↓	↓	↓							
				0	0	0	1							

T =

0	0	0	0	1	0	0	0	1	0	1	0	0	0	1
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

P =

					↓	↓	↓	↓						
					0	0	0	1						

$$T = \begin{matrix} & 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12 & 13 & 14 \\ \begin{matrix} 0 \\ 1 \end{matrix} & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 1 & 0 & 1 & 0 & 0 & 0 & 1 \end{matrix}$$

$T = 000010001010001$
 $\quad \quad \quad \quad \quad \quad \quad \downarrow \downarrow \downarrow \downarrow$
 $\quad \quad \quad \quad \quad \quad \quad 0010$

$T =$

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
0	0	0	0	1	0	0	0	1	0	1	0	0	0	1
								x	↓	↓	↓	↓		
								0	0	0	1			

$T =$

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
0	0	0	0	1	0	0	0	1	0	1	0	0	0	1

$P =$

0	0	0	0	1	0	0	0	1	0	1	0	0	0	1
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

$T =$

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
0	0	0	0	1	0	0	0	1	0	1	0	0	0	1

$P =$

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
0	0	0	0	1	0	0	0	1	0	1	0	0	0	1

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		0	1	2	3	4	5	6	7	8	9	10
T		a	b	c	d	a	b	a	b	c		
P							a	b	c			

		0	1	2	3	4	5	6	7	8	9	10
T		a	b	c	d	a	b	a	b	c		
P							a	b	c			

		0	1	2	3	4	5	6	7	8	9	10
T		a	b	c	d	a	b	a	b	c		
P								a	b	c		

Sliding Window Matches (T, P)

1. n = T.length
 2. m = P.length
 for s = 0 to n-m
 {
 4. if P[1..m] == T[s+1..s+m]
 5. print "Pattern occurs with shift s"
 }

2) T = 000010001010001
 P = 0001

Set 1: T = 000010001010001
 P = 0001

T = 000010001010001
 P = 0001

0 1 2 3 4 5 6 7 8 9 10 11 12 13 14
 T = 0 0 0 0 1 0 0 0 1 0 1 0 0 0 1
 ↓ ↓ ↓ ↓
 P = 0 0 0 1

0 1 2 3 4 5 6 7 8 9 10 11 12 13 14
 T = 0 0 0 0 1 0 0 0 1 0 1 0 0 0 1
 ↓ ↓
 P = 0 0 0 1

0 1 2 3 4 5 6 7 8 9 10 11 12 13 14
 T = 0 0 0 0 1 0 0 0 1 0 1 0 0 0 1
 × ↓ ↓ ↓ ↓
 0 0 0 1

0 1 2 3 4 5 6 7 8 9 10 11 12 13 14
 T = 0 0 0 0 1 0 0 0 1 0 1 0 0 0 1
 ↓ ↓ ↓ ↓
 P = 0 0 0 1

0 1 2 3 4 5 6 7 8 9 10 11 12 13 14
 T = 0 0 0 0 1 0 0 0 1 0 1 0 0 0 1
 ↓ ↓ ↓ × ↓
 0 0 0 1

0 1 2 3 4 5 6 7 8 9 10 11 12 13 14
 T = 0 0 0 0 1 0 0 0 1 0 1 0 0 0 1
 × ↓ ↓ ↓ ↓
 0 0 0 1 0

0 1 2 3 4 5 6 7 8 9 10 11 12 13 14
 T = 0 0 0 0 1 0 0 0 1 0 1 0 0 0 1
 × ↓ ↓ ↓ ↓
 0 0 0 1

0 1 2 3 4 5 6 7 8 9 10 11 12 13 14
 T = 0 0 0 0 1 0 0 0 1 0 1 0 0 0 1
 ↓ ↓ ↓ ↓
 P = 0 0 0 1

0 1 2 3 4 5 6 7 8 9 10 11 12 13 14
 T = 0 0 0 0 1 0 0 0 1 0 1 0 0 0 1
 × ↓ ↓ ↓
 0 0 0 1

0 1 2 3 4 5 6 7 8 9 10 11 12 13 14

T: 0 0 0 0 1 0 0 0 1 0 1 0 0 0 1

P: 0 0 0 1

$$S = 1$$

$$S = 5$$

$$S = 11$$

Boyer Moore

T: BESS - KNEW - ABOUT - BAOBABS.

P: B A O B A B

Bad symbol table

c	A	B	S	O	_	*	m - l - j.
t(c)	1	2	6	3	6	6	m → no. of letter j → index no

→ We have to consider rightmost letter

Good shift table

K	Pattern	d ₂
1	B A O B A B	2
2	B A O B A B	5
3	B A O B A B	5
4	B A O B A B	5
5	B A O B A B	5
6	B A O B A B	5

T: BESS - KNEW - ABOUT - BA OBAB S

P: ~~BA OBAB~~ S

P: BA OBAB

$$d_1 = t(c) - k$$

$$= 6 - 0$$

$$= 6$$

T: BESS - KNEW - ABOUT - BA OBAB S

P: BA O ^xBA ¹B

$$d_1 = 6 - 2$$

$$= 4$$

$$d_2 = 5$$

$$= \max\{d_1, d_2\}$$

$$= \max\{4, 5\}$$

$$= 5$$

T: BESS - KNEW - ABOUT - BA OBAB S.

P: BA OBA ^xA ¹B

$$d_1 = 6 - 1$$

$$= 5$$

$$d_2 = 2$$

$$= \max\{d_1, d_2\}$$

$$= \max\{5, 2\}$$

$$= 5$$

T: BESS - KNEW - ABOUT - BA0BABS
P: BA0BABS

String is matched.

h.w

T: JIM - SAW - ME - IN - A - BARBERSHOP
P: BARBER

Bad symbol table

C	A	B	E	R	*
h(i)	4	2	1	3	6

Good shift table

k	Pattern	d ₂
1	^{5 4 3 2 1 0} BARBER	3
2	^{4 3 2 1 0} BARBER	3
3	^{3 2 1 0} BARBER	3
4	^{2 1 0} BARBER	3
5	^{1 0} BARBER	3

T: JIM - SAW - ME - IN - A - BARBERSHOP
P: BARBER

$$\begin{aligned}
 d_1 &= \max(h(c)_i - k) \\
 &= \max(4, 0) \\
 &= 4.
 \end{aligned}$$

T: JIM - SAW - ME - IN - A - BARBER SHOP

P: ~~BARBER~~ BARBER

$$d_1 = \max(t(c), k)$$

$$= \max(1, 0)$$

$$= 1$$

T: JIM - SAW - ME - IN - A - BARBERSHOP

P: BARBER

$$= \max(t(k) - k_1)$$

$$= \max(6 - 0, 3)$$

$$= 6$$

T: JIM - SAW - ME - IN - A - BARBERSHOP

P: BARBER

$$= \max(t(c) - k, d_2)$$

$$= \max(2, 3)$$

$$= 3$$

T: JIM - SAW - ME - IN - A - BARBERSHOP

P: BARBER

$$= \max(t(c) - k, d_2)$$

$$= \max(t(c) - k, d_2)$$

$$= \max(4 - 0, 0)$$

$$= 4$$

T. JIM - SAW - ME - IN - A - BARBERSHOP
P. BARBER

String is matched.

g W O W K O W

Good shift table.

K	Pattern	d ₂	#- when there is first match don't select last one
1	^{5 4 3 2 1 0} W O W K O W	2 2	
2	^{5 4 3 2 1 0} W O W K O W	5	
3	^{5 4 3 2 1 0} W O W K O W	5	
4	^{5 4 3 2 1 0} W O W K O W	5	
5	^{5 4 3 2 1 0} W O W K O W	5	

g K U Y U L A Y U

Good shift table

K	Pattern	d ₂
1	^{7 6 5 4 3 2 1 0} K U Y U L A Y U	6
2	^{7 6 5 4 3 2 1 0} K U Y U L A Y U	4 4
3	^{7 6 5 4 3 2 1 0} K U Y U L A Y U	4 4
4	^{7 6 5 4 3 2 1 0} K U Y U L A Y U	4 4
5	^{7 6 5 4 3 2 1 0} K U Y U L A Y U	4 4
6	^{7 6 5 4 3 2 1 0} K U Y U L A Y U	4 4

Hashing

Date: / /

Valid list
~~21~~ → spurious list

$$21 = 8 \times$$

$$15 = 2 \times$$

$$56 = 4 \times$$

$$67 = 2 \times$$

$$78 = 0 \quad \checkmark$$

$$82 = 4$$

$$26 = 0$$

T :

21	56	78	26	4
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P : 78