1. (k points) How big is the parabolic segment between the parabola $f(x) = 2x^2$ and the line $g(x) = 4 + 2x$?

   Sketch a graph to visualize the desired area.

Solution: The functions intersect at $P_1(-1, 2)^T$ and at $P_2(2, 8)^T$. Thus, the area is

$$A = \int_{-1}^{2} g(x) - f(x)\,\mathrm{d}x = \int_{-1}^{2} 4 + 2x - 2x^2\,\mathrm{d}x = \left[4 + 2x - 2x^2\right]_{-1}^{2} = 9.0$$