

1. Find all eigenvalues and eigenvectors of the matrix

$$A = \begin{bmatrix} -4 & 2 \\ 24 & -6 \end{bmatrix}.$$

**Solution:**

Calculate  $A - \lambda I_2$ :

$$A - \lambda I_2 = \begin{bmatrix} -4 & 2 \\ 24 & -6 \end{bmatrix} - \lambda \begin{bmatrix} 1.0 & 0.0 \\ 0.0 & 1.0 \end{bmatrix} = \begin{bmatrix} -4 - 1.0\lambda & 2.0 \\ 24.0 & -6 - 1.0\lambda \end{bmatrix}.$$

Then, calculate  $\det(A - \lambda I_2)$ .

$$\det(A - \lambda I_2) = -48.0 + (-6 - 1.0\lambda)(-4 - 1.0\lambda)$$

Now, we solve  $\det(A - \lambda I_2) = 0$ .

The matrix  $A$  has the eigenvalues  $\lambda_1 = -12$  and  $\lambda_2 = 2$ .