

1. How big is the parabolic segment between the parabola  $f(x) = \frac{x^2}{2}$  and the line  $g(x) = 4 + x$ ? Sketch a graph to visualize the desired area.

**Solution:** The functions intersect at  $P_1(-2, 2)^T$  and at  $P_2(4, 8)^T$ . Thus, the area is

$$A = \int_{-2}^4 g(x) - f(x) \, dx = \int_{-2}^4 4 + x + \left(\frac{-1}{2}\right) x^2 \, dx = \left[ \frac{1}{6} x (24 + 3x - x^2) \right]_{-2}^4 = -16 + 3x^2 - 0.5x^3$$

