Universidade do Minho
Escola de Engenharia
Departamento de Informática

Knowledge Representation

Prolog

MESTRADO INTEGRADO EM ENGENHARIA INFORMÁTICA
Sistemas de Representação de Conhecimento e Raciocínio

Fevereiro 2020

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Synthetic Intelligence Lab

Summary

- Theory:
  - Unification;
  - Unification in Prolog;
  - Proof search.

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Unification

- When Prolog unifies:
  - **mulher(X)**
- with
  - **mulher(ana)**
- It is instantiating the variable **X** with the atom **ana**.

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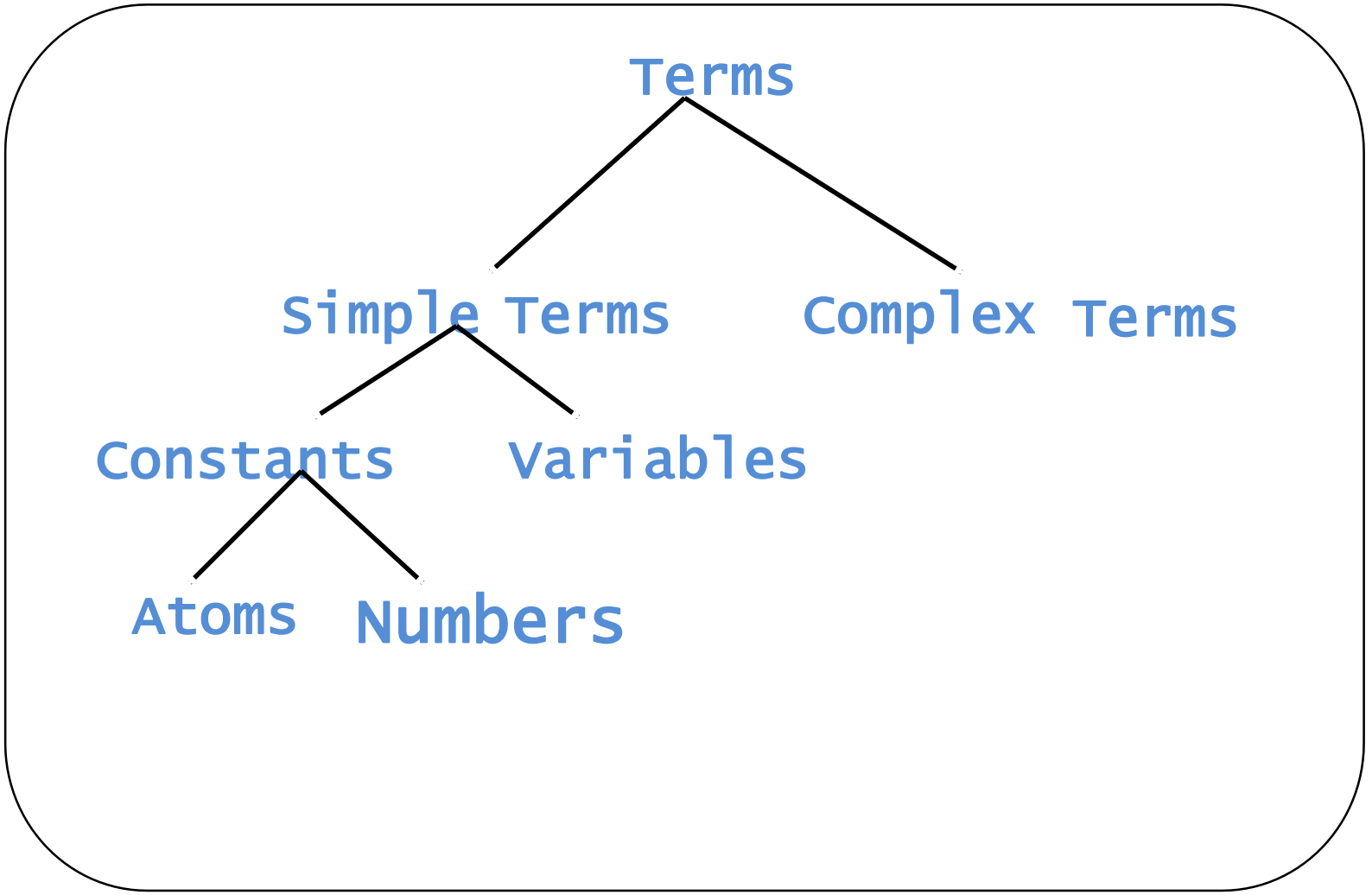
Recall Prolog Terms



Unification

- **Two terms unify**:
  - if they are the same term,

  or
  - if they contain variables that can be uniformly instantiated with terms in such a way that the resulting terms are equal.

Unification

- This means that:
  - **ana** and **ana** unify;
  - **42** and **42** unify;
  - **mulher(ana)** and **mulher(ana)** unify.

- This also means that:
  - **bruno** and **ana** do not unify;
  - **mulher(ana)** and **mulher(berta)** do not unify.

Unification

- What about the terms:
  - **ana** and **X;**
  - **mulher(Z)** and **mulher(ana);**
  - **gosta(ana,X)** and **gosta(Y,miguel)**

  - **They unify!**
    - **X is instantiated to ana;**
    - **Z is instantiated to ana;**
    - **X is instantiated to Miguel, ana to Y.**

Instantiations

- When Prolog unifies two terms, it performs all the necessary instantiations, so that the terms are equal afterwards;

- This makes unification a powerful programming mechanism.

Unification

- If C_1 and C_2 are constants, then C_1 and C_2 unify if they are the same atom, or the same number;
- If C_1 is a variable and C_2 is any type of term, then C_1 and C_2 unify, and C_1 is instantiated to C_2 (and vice versa);

Unification

- If C_1 and C_2 are complex terms then they unify if:
  - They have the same functor and arity, and all their corresponding arguments unify, and the variable instantiations are compatible.

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How will Prolog respond?

```
?- X=ana, X=bruno.

 no

?-
```

Why? After working through the first goal, Prolog has instantiated X with **ana**, so that it cannot unify it with **bruno** anymore. Hence the second goal fails.

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Example with complex terms

```
?- k(s(g),Y) = k(X,t(k)).
X=s(g)
Y=t(k)
 yes
?-
```

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Prolog and unification

- Prolog does not use a standard unification algorithm;
- Consider the following query:

  ?- pai(X) = X.

- Do these terms unify or not?

Infinite terms

```
?- pai(X) = X.
X=pai(pai(pai(pai(pai(pai(pai(pai(pai(pai(...)))))))))?
;
no
```

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Occurs Check

- A standard unification algorithm carries out an **occurs check:**
  - If it is asked to unify a variable with another term it checks whether the variable occurs in this term;
  - In Prolog (ISO standard):

```
?- unify_with_occurs_check(pai(X), X).
no
```

Programming with Unification

```
vertical(line(point(X,Y), point(X,Z))).

horizontal(line(point(X,Y), point(Z,Y))).
```

```
?- vertical(line(point(1,1),point(1,3))).
 yes
?- vertical(line(point(1,1),point(3,2))).
no
?-
```

Programming with Unification

```
vertical(line(point(X,Y), point(X,Z))).

horizontal(line(point(X,Y), point(Z,Y))).

?-horizontal(line(point(1,1),point(1,Y))).
Y = 1;
Yes
?-
```

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Which of the following pairs unify?

1. pao = pao
2. ’Pao’ = pao
3. ’pao’ = pao
4. Pao = pao
5. pao = molho
6. comida(pao) = pao
7. comida(pao) = X
8. comida(X) = comida(pao)
9. comida(pao,X) = comida(Y,molho)
10. comida(pao,X,cerveja) = comida(Y,molho,X)
11. comida(pao,X,cerveja) = comida(Y,big_mac)
12. refeicao(comida(pao),bebida(cerveja)) = refeicao(X,Y)
13. refeicao(comida(pao),X) = refeicao(X,bebida(cerveja))

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Which of the following pairs unify?

1. pao = pao yes
2. 'Pao' = pao No
3. 'pao' = pao Yes
4. Pao = pao Yes, Pao=pao
5. pao = molho No
6. comida(pao) = pao No
7. comida(pao) = X Yes, X=comida(pao)
8. comida(X) = comida(pao) Yes, X=pao
9. comida(pao,X) = comida(Y,molho) Yes, X=molho, Y=pao
10. comida(pao,X,cerveja) = comida(Y,molho,X) No
11. comida(pao,X,cerveja) = comida(Y,big_mac) No
12. refeicao(comida(pao),bebida(cerveja)) = refeicao(X,Y) Yes, X=comida(pao), Y=bebida(cerveja)
13. refeicao(comida(pao),X) = refeicao(X,bebida(cerveja)) No

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Which queries are satisfied?

```
elfo(diogo).
bruxa(herminia).
bruxa('Maria').
bruxa(rita).
magico(X):- elfo(X).
magico(X):- feiticeiro(X).
magico(X):- bruxa(X).
```

```
?- magic(elfo).
?- feiticeiro(andre).
?- magico(feiticeiro).
?- magico('Maria').
?- magico(Herminia).
```

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Which queries are satisfied?

```
elfo(diogo).
bruxa(herminia).
bruxa('Maria').
bruxa(rita).
magico(X):- elfo(X).
magico(X):- feiticeiro(X).
magico(X):- bruxa(X).
```

?- magico(elfo). No
?- feiticeiro(harry). No
?- magico(feiticeiro). No
?- magico('Maria'). No
?- magico(Herminia). Yes, Herminia = diogo ;

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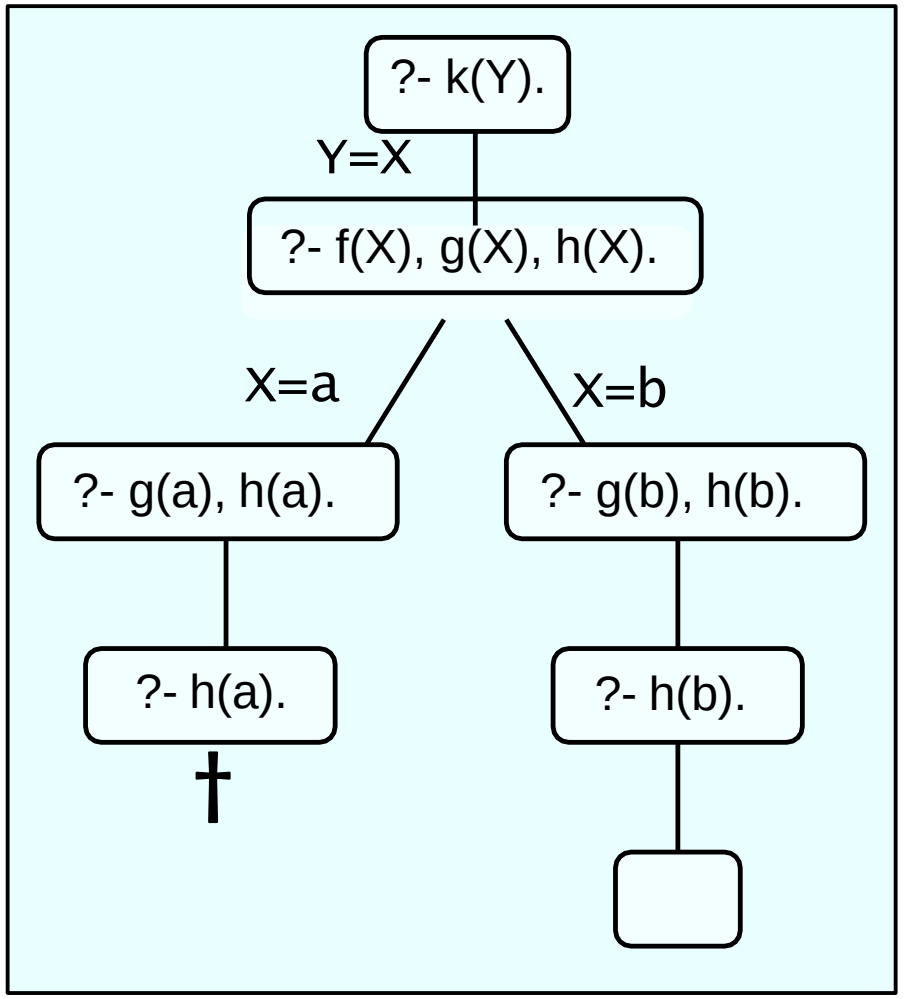
Example: search tree

```
f(a).
f(b).
g(a).
g(b).
h(b).
k(X):- f(X), g(X), h(X).

?- k(Y).
Y=b;
true
?-
```



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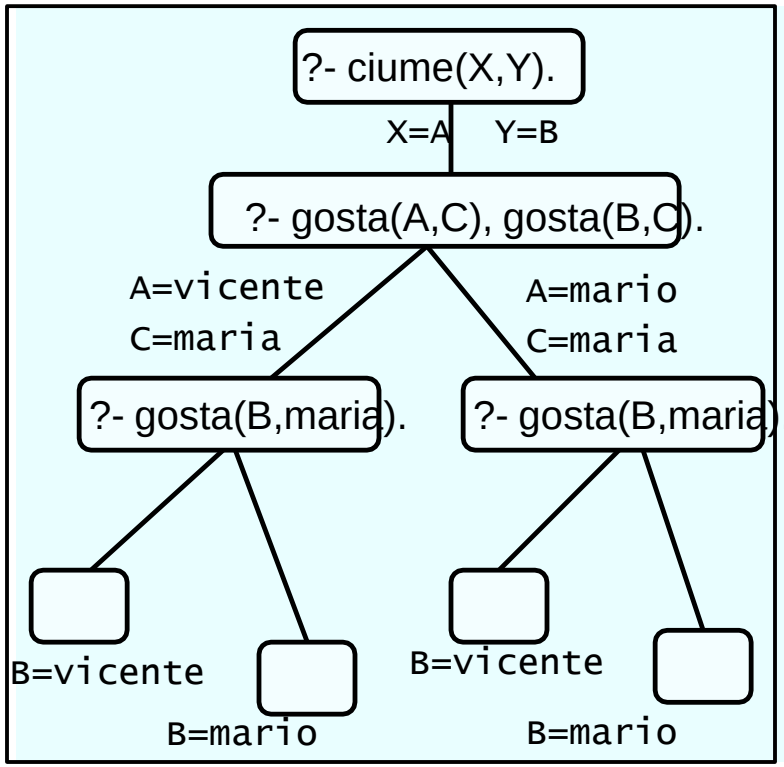
Another example

```
gosta(vicente,maria).
gosta(mario,maria).

ciume(A,B):-gosta(A,C),gosta(B,C).
```

```
?- ciume(X,Y).
X=vicente
Y=vicente;
X=vicente
Y=mario;
X=mario
Y=vicente;
X=mario
Y=mario;
no
```



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Exercise

```
elfo(diogo).
bruxa(herminia).
bruxa('Maria').
bruxa(rita).
magico(X):- elfo(X).
magico(X):- feiticeiro(X).
magico(X):- feiticeiro(X).

?- magico(Herminia).
```

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