Regras de inferência de DNP

$$\frac{\varphi \quad \psi}{\varphi \wedge \psi} \wedge I$$

$$\frac{\varphi \wedge \psi}{\varphi} \wedge_1 E \qquad \frac{\varphi \wedge \psi}{\psi} \wedge_2 E$$

$$\begin{array}{c} \varphi \\ \vdots \\ \frac{\psi}{\varphi \to \psi} \to I \end{array}$$

$$\frac{\varphi \quad \varphi \to \psi}{\psi} \to E$$

$$\begin{array}{c} \varphi \\ \vdots \\ \frac{\perp}{\neg \varphi} \neg I \end{array}$$

$$\frac{\varphi \quad \neg \varphi}{\bot} \ \neg E$$

$$\frac{\varphi}{\varphi \vee \psi} \vee_1 I \qquad \frac{\psi}{\varphi \vee \psi} \vee_2 I$$

$$\begin{array}{ccc}
\varphi & \psi \\
\vdots & \vdots \\
\psi & \varphi \\
\hline
\varphi \leftrightarrow \psi & \leftrightarrow I
\end{array}$$

$$\frac{\varphi \quad \varphi \leftrightarrow \psi}{\psi} \leftrightarrow_1 E \quad \frac{\psi \quad \varphi \leftrightarrow \psi}{\varphi} \leftrightarrow_2 E$$

$$\frac{\perp}{\varphi}$$
 (\perp)