

P165: Introduction to Particle Physics

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Abstract

This is a 10 week course on the theory of the Standard Model geared towards undergraduates who have taken at least the first of a three-quarter sequence in quantum mechanics. Last Compiled: March 29, 2022

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1 Introduction

To be filled in.

2 Units and Natural Units

Imagine that you have three apples. This is a number (three) and a unit (apple). The meaning of the unit depends on what you're using it to measure. For example, if apples are \$1 each, then you could use an apple as a unit of currency. The way to do this is to simply *multiply by one*:

$$(3 \text{ apples}) \times \left(\frac{\$1}{\text{apple}} \right) = \$3 . \quad (2.1)$$

We have used the fact that the exchange rate is simply the statement that

$$1 \text{ apple} = \$1 \quad \Rightarrow \quad 1 = \frac{\$1}{1 \text{ apple}} . \quad (2.2)$$

Exercise 2.1. *An apple is also roughly 100 dietary calories. If a friend buys me a coffee for \$2, does this mean that I can pay that friend back in 200 dietary calories? Comment on the relative merits of using apples as an exchange between monetary value and dietary energy.*

Exercise 2.2. *At the time of this writing, one dollar is worth three-fourths of a British pound sterling: $\$1 = 0.75$. Write an expression that is equal to one that is a ratio of pound sterling to dollars. Use this ratio to convert the cost of two apples in the UK. Is the exchange rate a good conversion factor? What if a friend of mine bought me coffee in Riverside, and I promised to pay them back in pound sterling in two years?*

All that matters is that the conversion is constant. Indeed, the constants of nature make very good ‘exchange rates.’ For example, in particle physics we like to use **natural units**. This is the curious statement that

$$\hbar = c = 1 . \quad (2.3)$$

At face value, this doesn’t make sense. \hbar has units of action, c is a speed, and 1 is dimensionless. However, because nature gives us a *fundamental* unit of action and a *fundamental* unit of speed, we may use them as conversion factors (exchange rates),

$$c = 3 \times 10^{10} \text{ cm/s} . \quad (2.4)$$

If $c = 1$, then this means

$$1 \text{ s} = 3 \times 10^{10} \text{ cm} . \quad (2.5)$$

This, in turn, connects a unit of time to a unit of distance. By measuring time, the constant c automatically gives us an associated distance. The physical relevance of the distance is tied to the nature of the fundamental constant: one second (or ‘light-second’) is the distance that a photon travels in one second. Observe that this only works because c is a constant.

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