



Modelling Multi-dimensional Opinions and Polarization Formation

The Opinioners

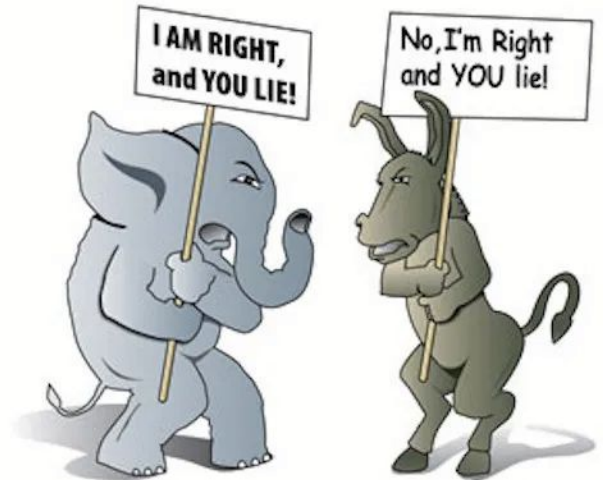
Michael Andres, Florian Dorner, Gian Luca Gehwolf, Fabian Hafner, David Metzger

Complex Social Systems

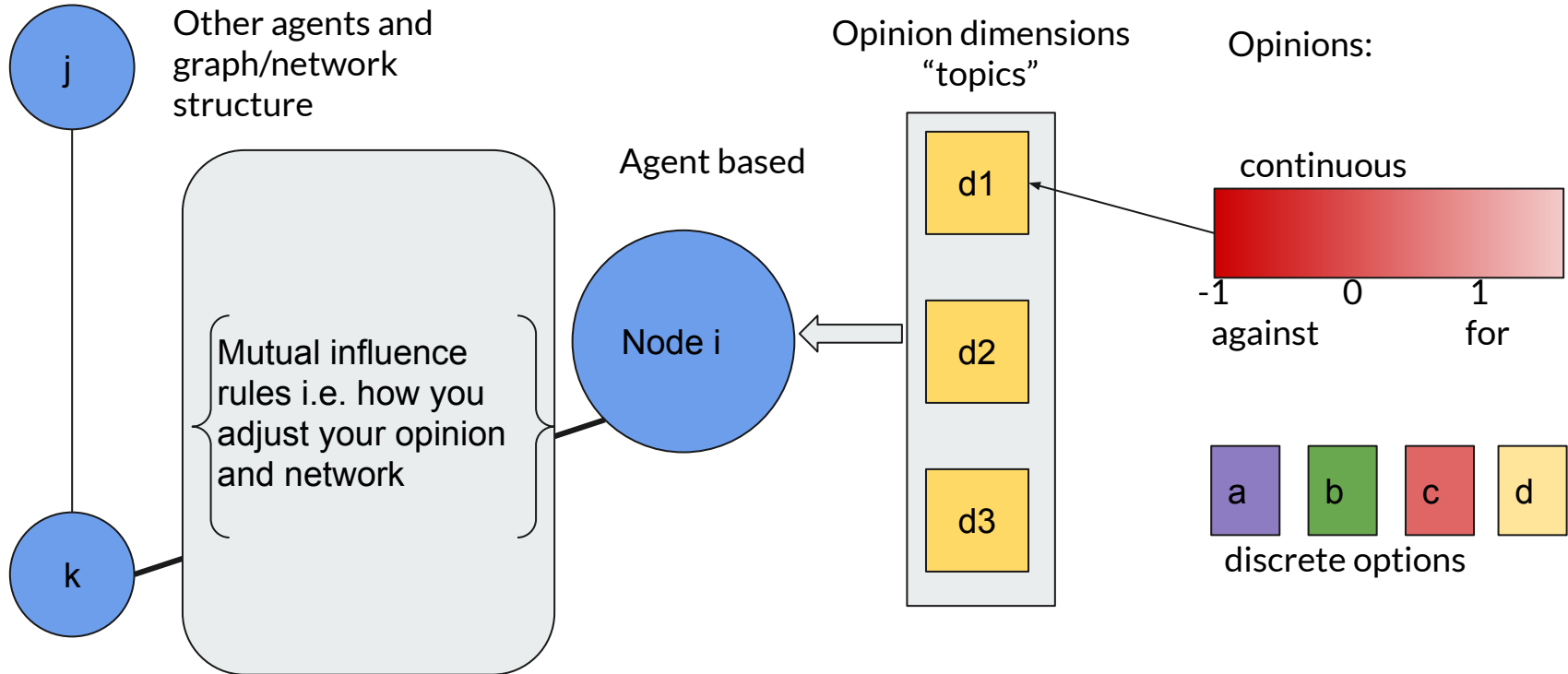
7 December 2020

Motivation

1. Political polarization is a threat to political stability
2. How can opinion polarization be simulated?
 - Weighted Balance Theory Model by Schweighofer et al. (2020)
3. How can opinion polarization dynamics be influenced by...
 - Network structures
 - Coevolution of networks and opinions model developed by Holme and Newman (2006)
 - Bots



How do opinion formation models work?

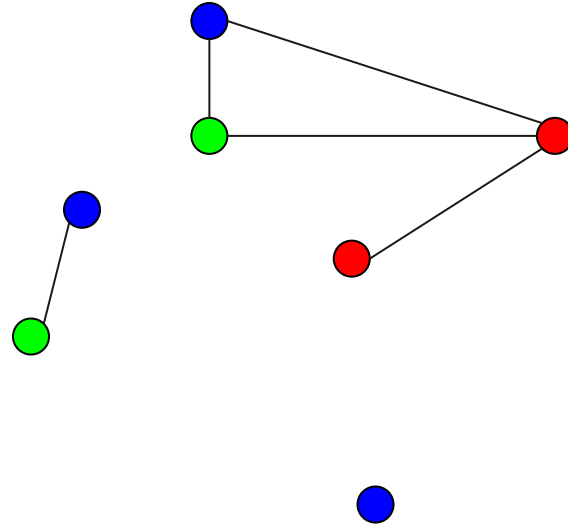


Model 1: coevolution of opinions and networks

Holme et al. 2006

Discrete, 1D opinions
Randomly initialized network

Example: 30 students need to choose
where to go for lunch

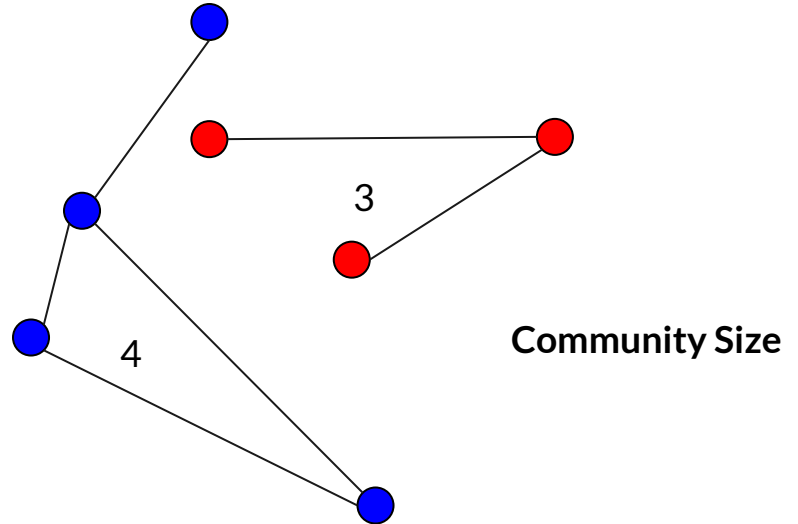


Model 1: coevolution of opinions and networks

Holme et al. 2006

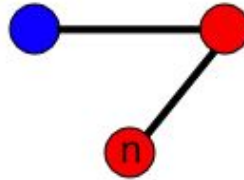
Discrete, 1D opinions
Randomly initialized network

Convergence when communities
have consensus



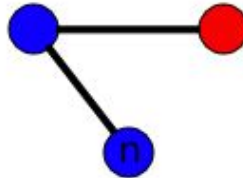
Coevolution Model - influence rules

with probability Φ



connect to like-minded

with probability $1-\Phi$

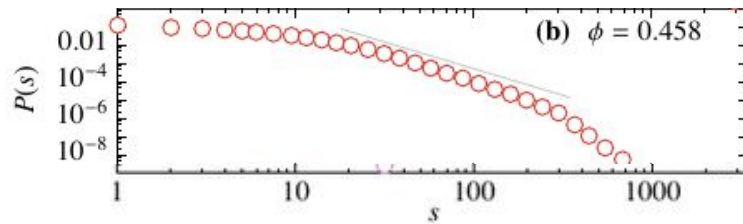


adjust my opinion

Comparison of Results

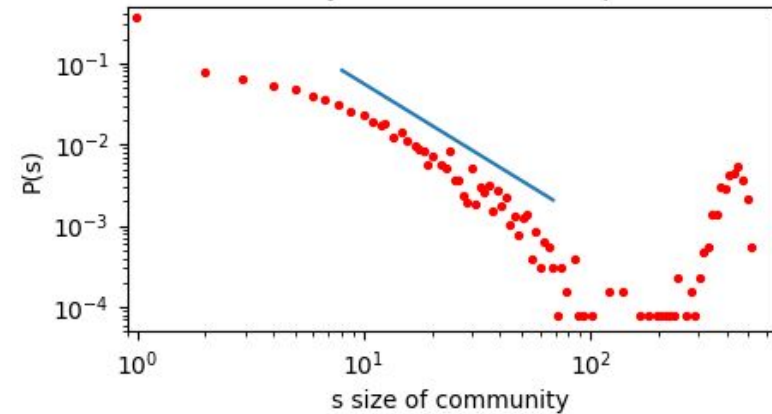
Holme 2006

Histograms of community sizes (avg)



Reproduced by us

community size distribution. $\phi=0.458$





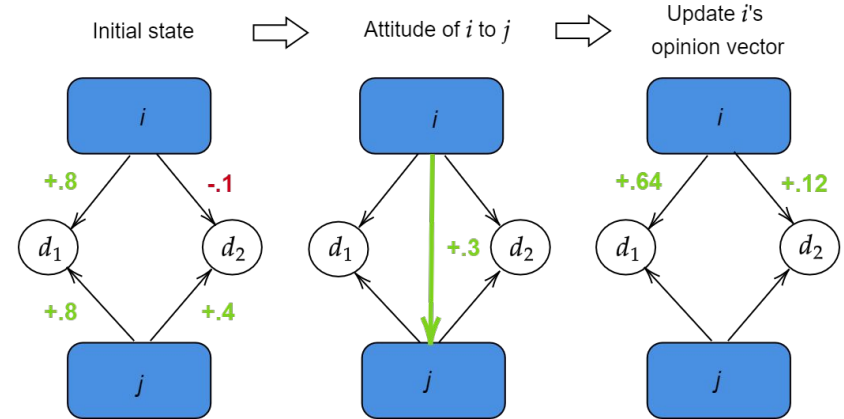
Model 2: Weighted Balance Theory

Schweighofer et al. 2020

- Multidimensional, continuous opinions $[-1, +1]$, no network. Political topics.
 - How opinions **change** depends on **overall opinion similarness**
- **Hyperpolarization:** extreme and clustered opinions
- Two-party system

Model 2: Weighted Balance Theory

- Interpersonal **attitude** A_{ij} as measure of closeness
 - within $[-1, +1]$ based on signed geometric mean and sigmoid evaluative extremeness
 - Equilibrium / fixed points
 $\mathbf{o}(i)_{eq} \simeq \pm \mathbf{o}(j)$



$$A_{ij} := f \left(\frac{1}{D} \sum_{d=1}^D \text{SGM}(o_d(i), o_d(j)) \right)$$

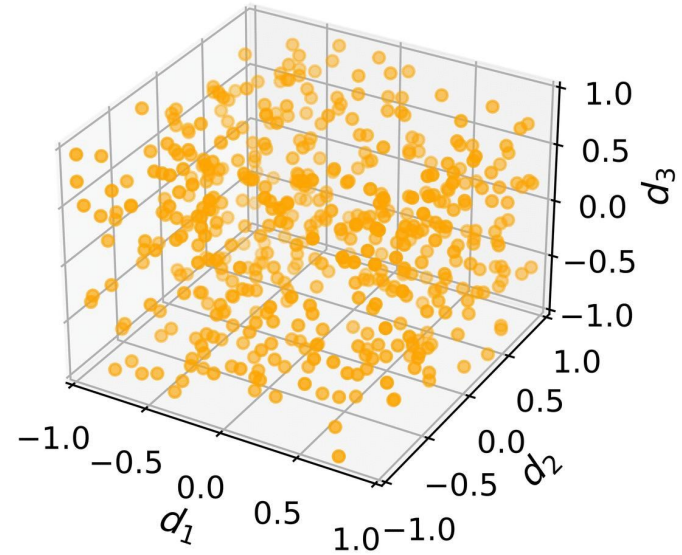
$$f(x) = \text{sign}(x) |x|^{1-e}$$

$$\mathbf{o}(i) \leftarrow \mathbf{o}(i) + \alpha [\mathbf{b}^{ij} - \mathbf{o}(i)] + \xi(0, z)$$

$$\mathbf{b}^{ij} := \begin{pmatrix} b_1^{ij} \\ \vdots \\ b_D^{ij} \end{pmatrix} := \begin{pmatrix} \text{SGM}(o_1(j), A_{ij}) \\ \vdots \\ \text{SGM}(o_D(j), A_{ij}) \end{pmatrix}$$

Model 2: Weighted Balance Theory

Hyperpolarisation



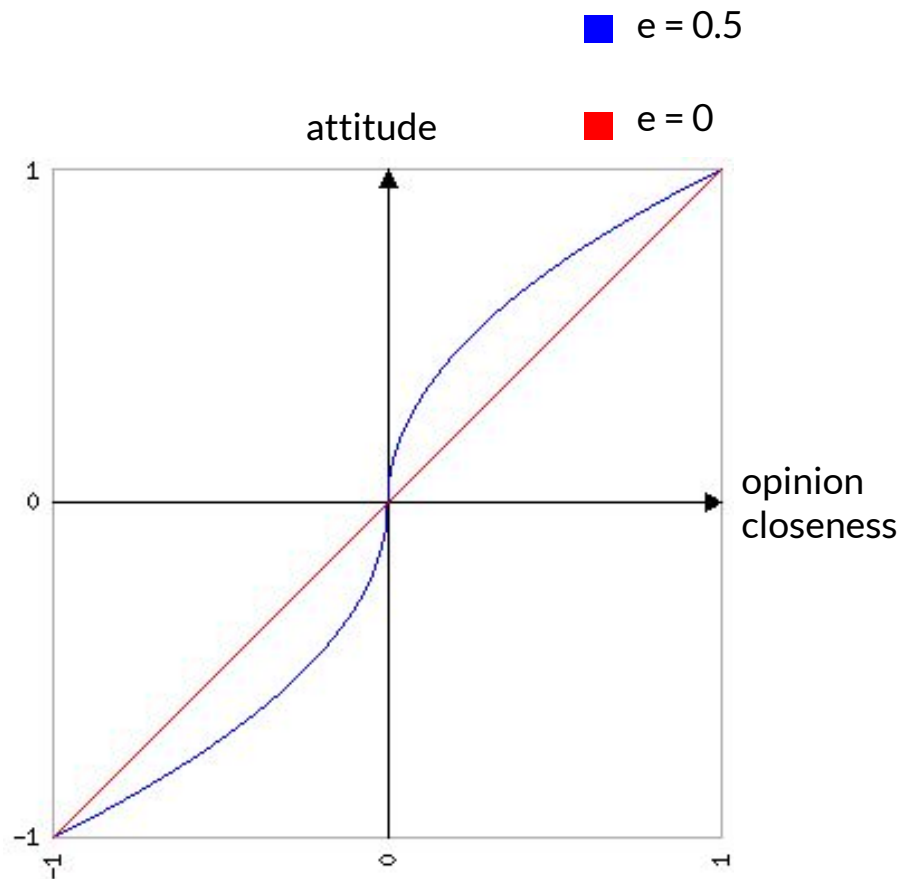


Evaluative extremeness

$$f(x) = \text{sign}(x)|x|^{1-e}$$

slightly agree
on average → like person a lot

slightly
disagree on
average → dislike a lot





Evaluative extremeness

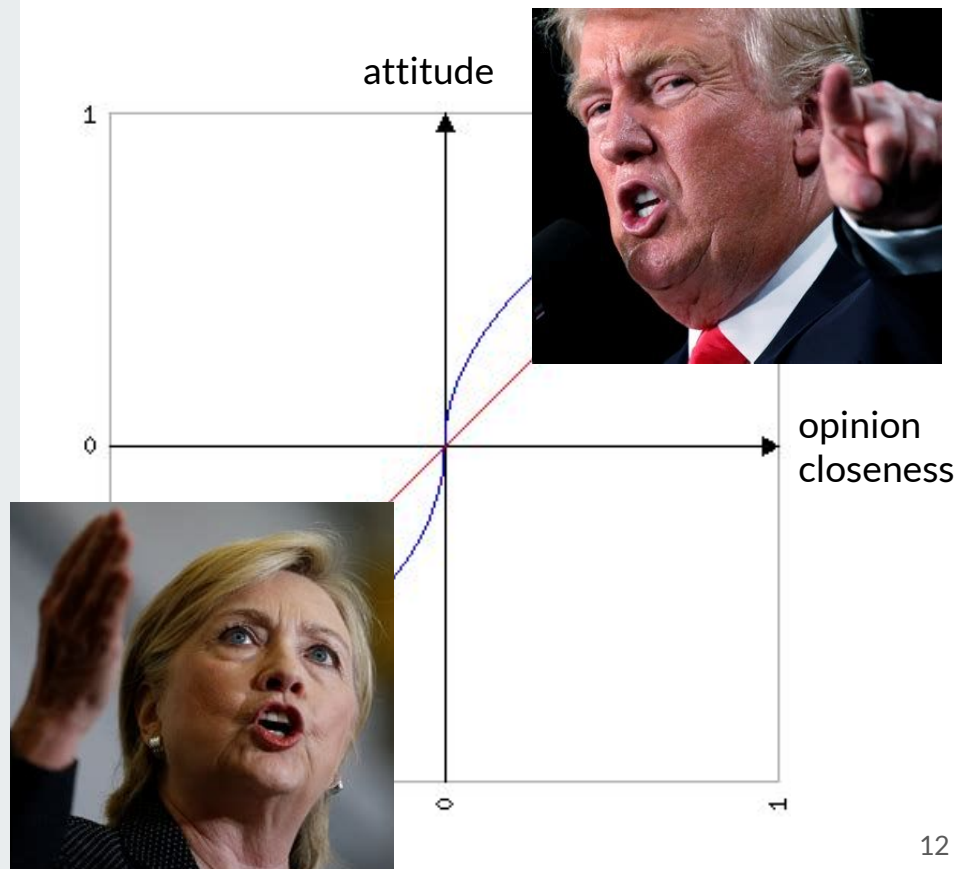
$$f(x) = \text{sign}(x)|x|^{1-e}$$

slightly agree
on average \longrightarrow like person a lot

slightly
disagree on
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Images: Carlo Allegri / Reuters, Chris Keane / Reuters

■ $e = 0.5$



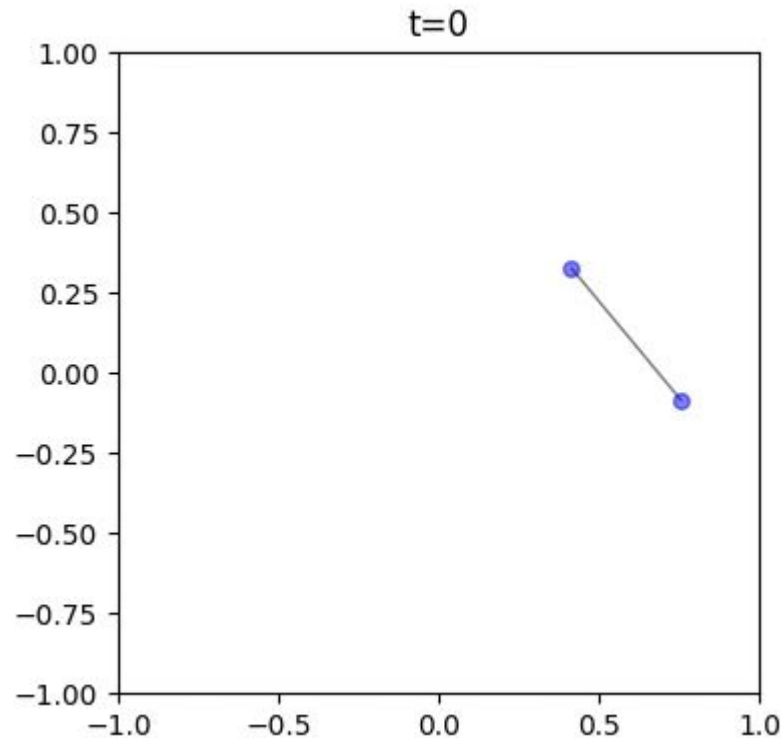


Evaluative extremeness

$$f(x) = \text{sign}(x)|x|^{1-e}$$

$e > 0$ creates drift to corners

→ not entirely unrealistic, but still surprising





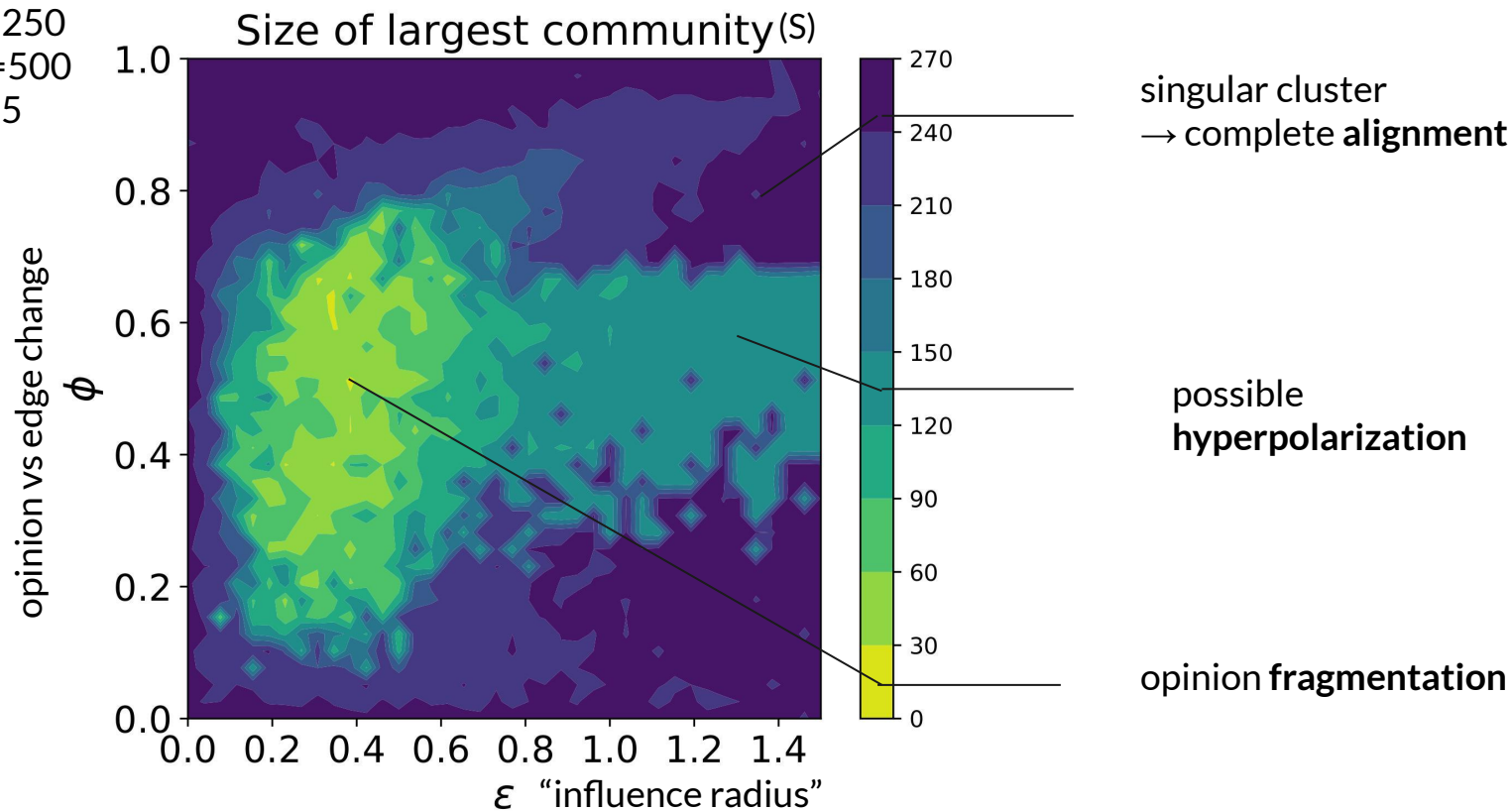
Model 3: Generalized WBT Model

- WBT Model implemented into network structure
- With probability Φ :
$$\text{connect}(\mathbf{o}(i), \mathbf{o}(j)) = \begin{cases} 1 & \text{if } |\mathbf{o}(i) - \mathbf{o}(j)| < \varepsilon(N, D, z) \\ 0 & \text{else} \end{cases}$$
- With probability $1-\Phi$:

$$\text{update}(\mathbf{o}(i), \mathbf{o}(j)) = \mathbf{o}(i) + \alpha [\mathbf{b}^{ij} - \mathbf{o}(i)] + \xi(0, z)$$

→ **New behavior:** clusters, phase transitions

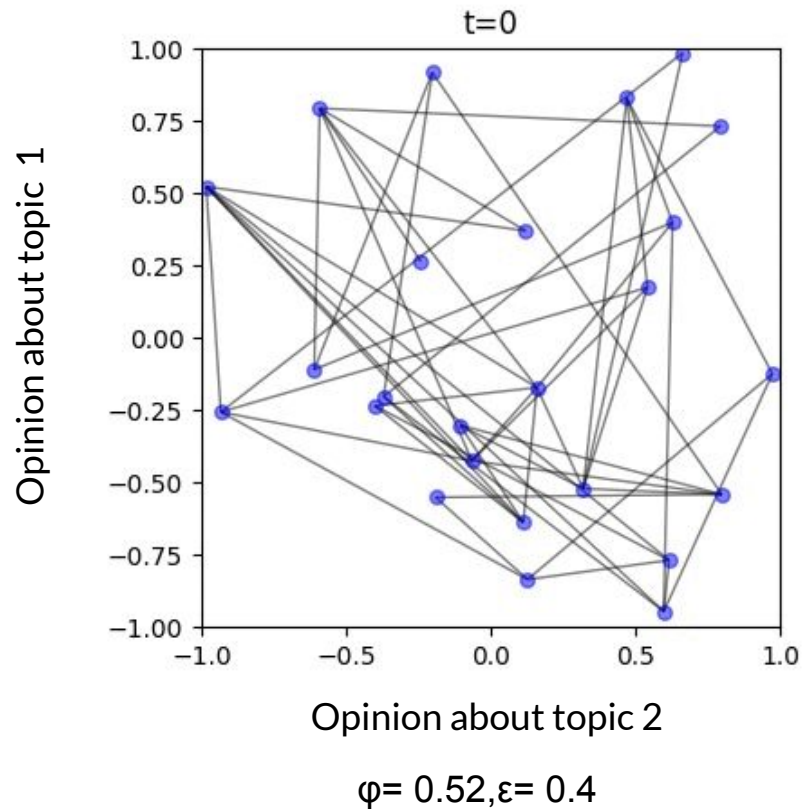
N=250
M=500
D=5



Observation: convergence into $\sim S/N$ similarly sized clusters

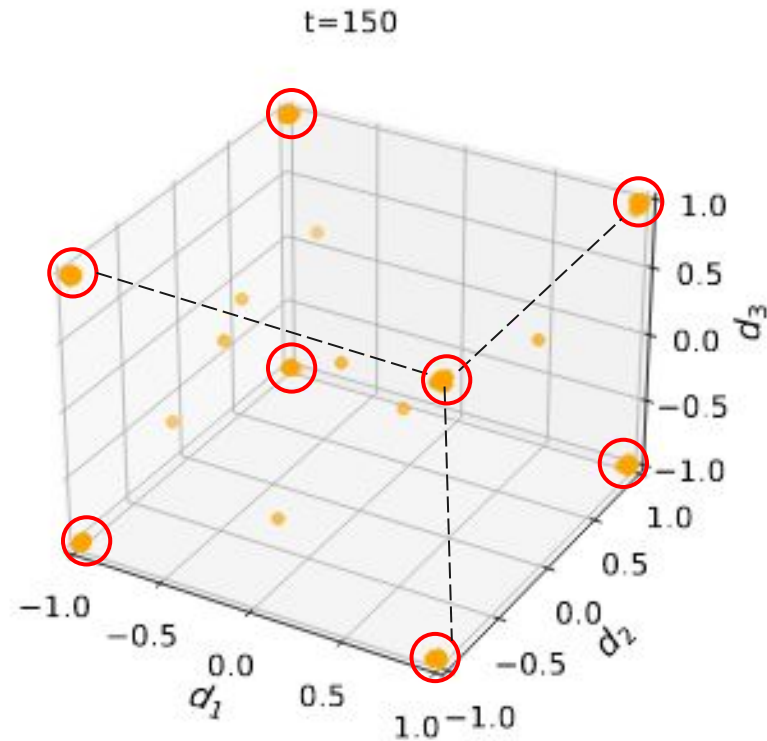
Graph evolution

from random to polarized



In some cases no hyperpolarization, just polarization & fragmentation

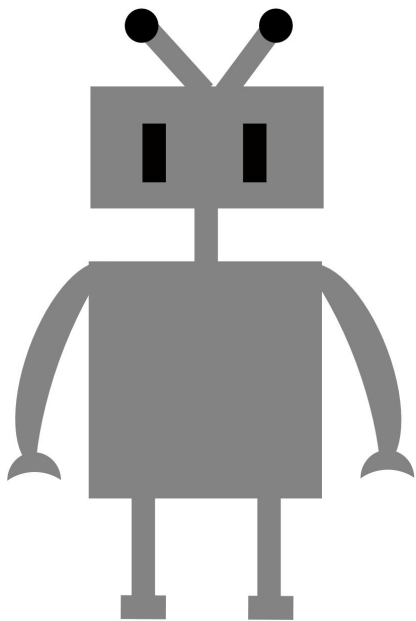
Clusters in the corners + some disconnected nodes



$\phi = 0.45, \epsilon = 0.3$



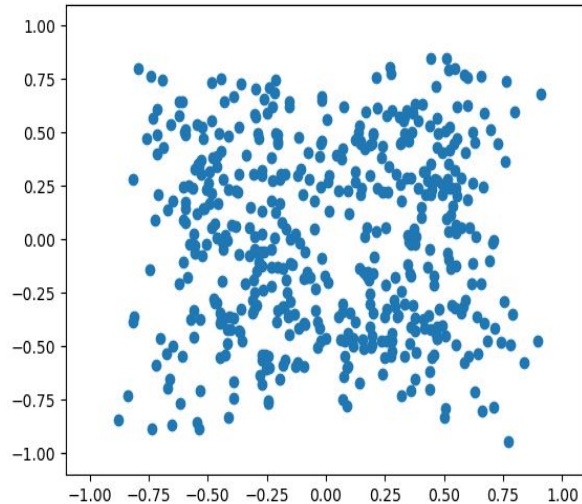
Bots



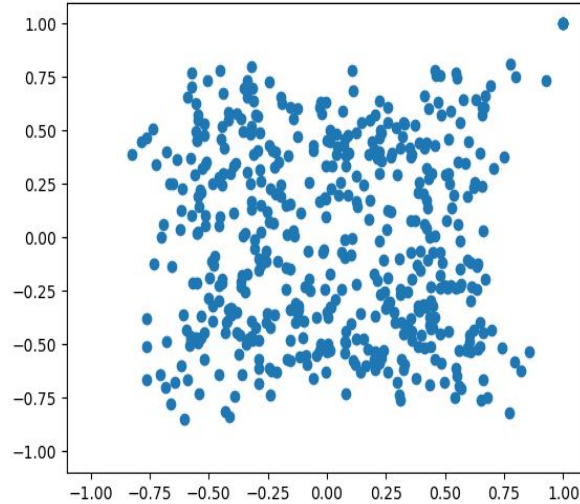
- Like normal nodes but don't change their opinion
- This presentation:
 - Bots all have same extreme opinion in all dimensions

Bots (e=0, fully connected network)

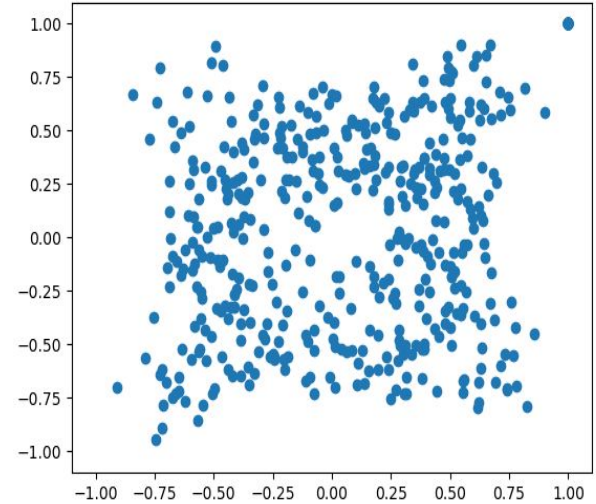
0/500 nodes are bots



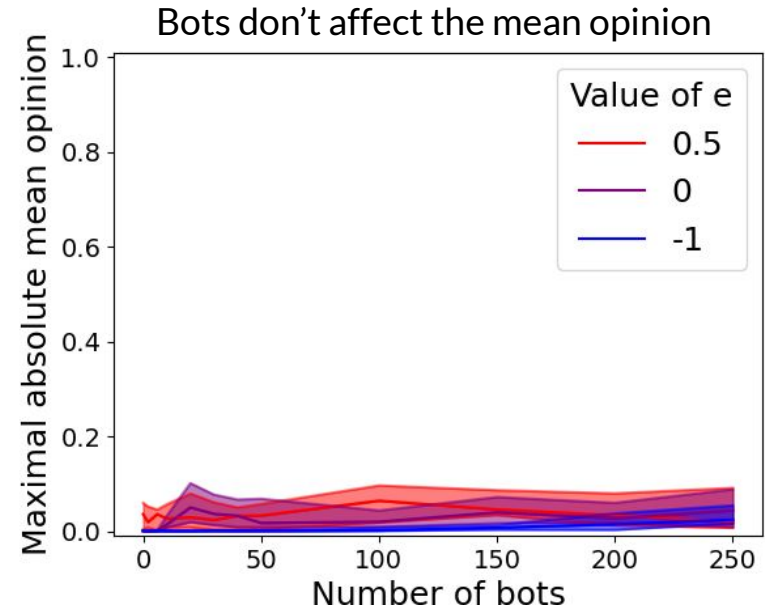
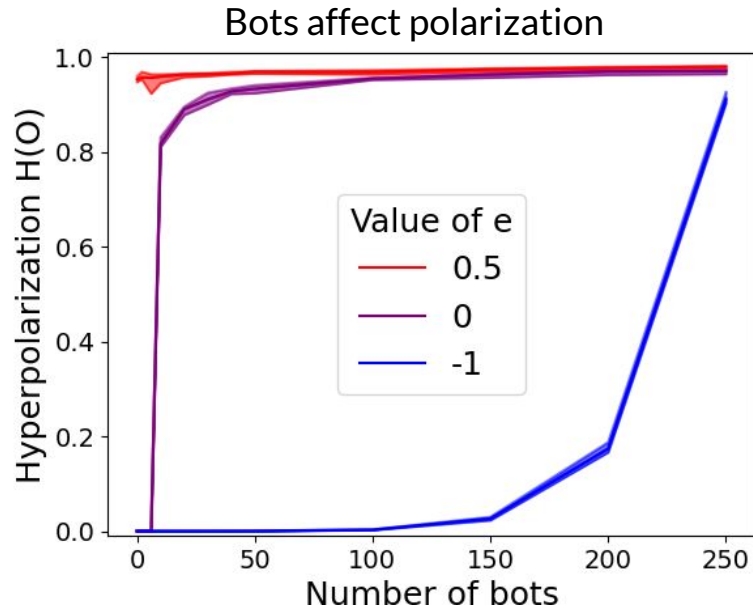
5/500 nodes are bots



50/500 nodes are bots

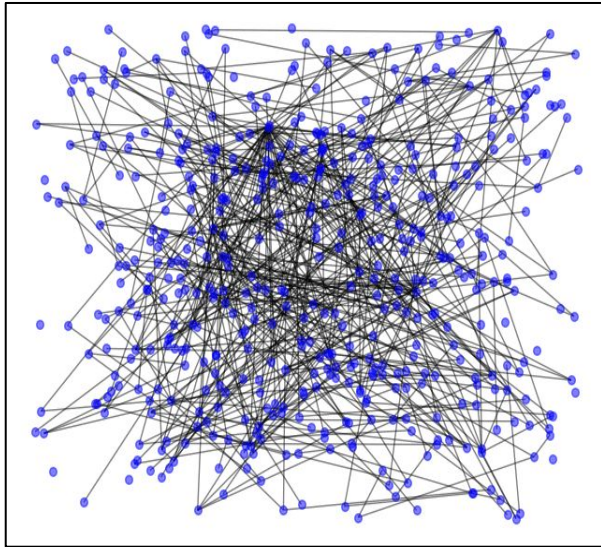


Bots (e=0, fully connected network)

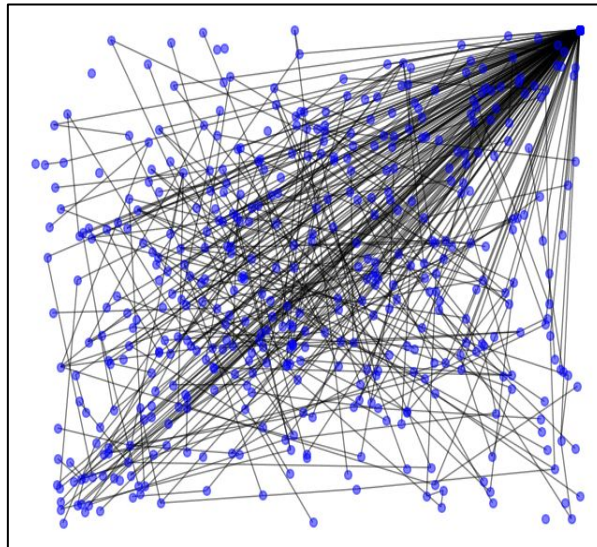


Bots in dynamic BA graph ($e=0, \phi=0.5, \epsilon=1$)

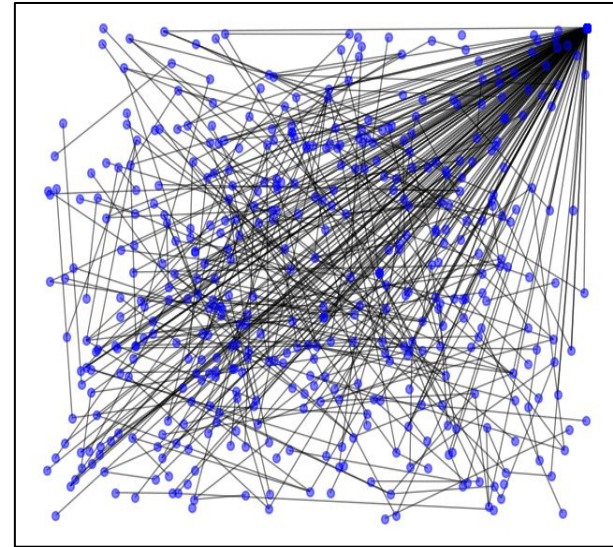
No bots



50 bots

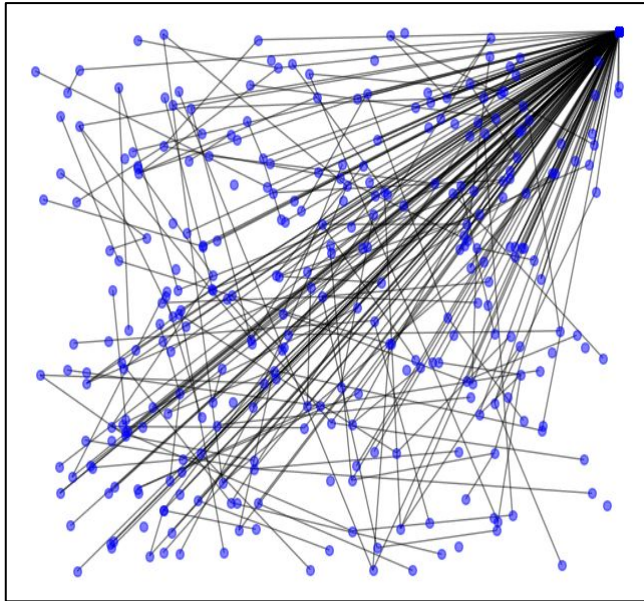


50 bots, bots can connect to all

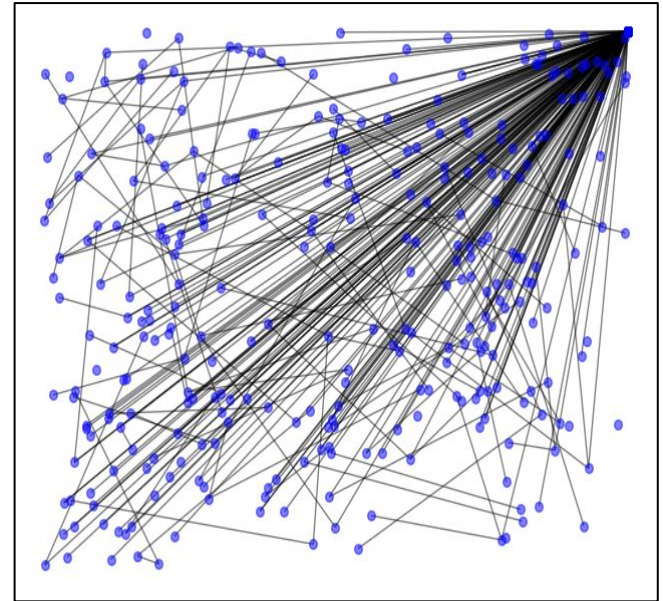


Bots in dynamic BA graph ($e=0, \phi=0.5, \epsilon=1$)

200 bots

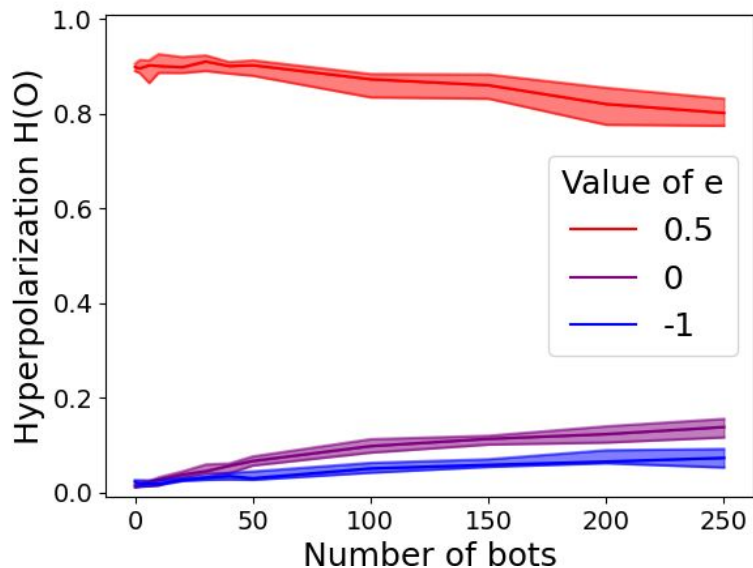


200 bots, bots can connect to all

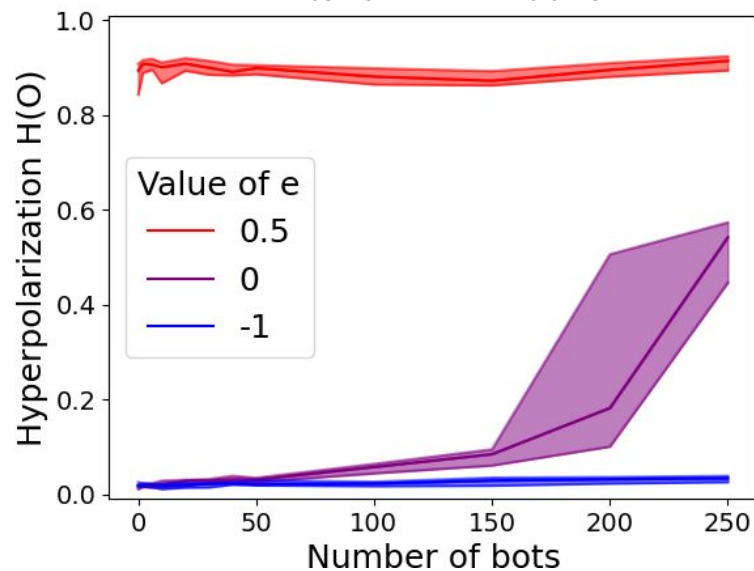


Bots in dynamic BA graph ($e=0, \phi=0.5, \epsilon=1$)

Bots connect like all other nodes



Bots can connect to all





Conclusion

Reproduction of Models

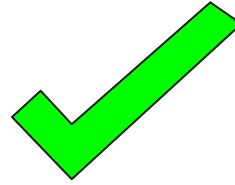
Extensions

Critique



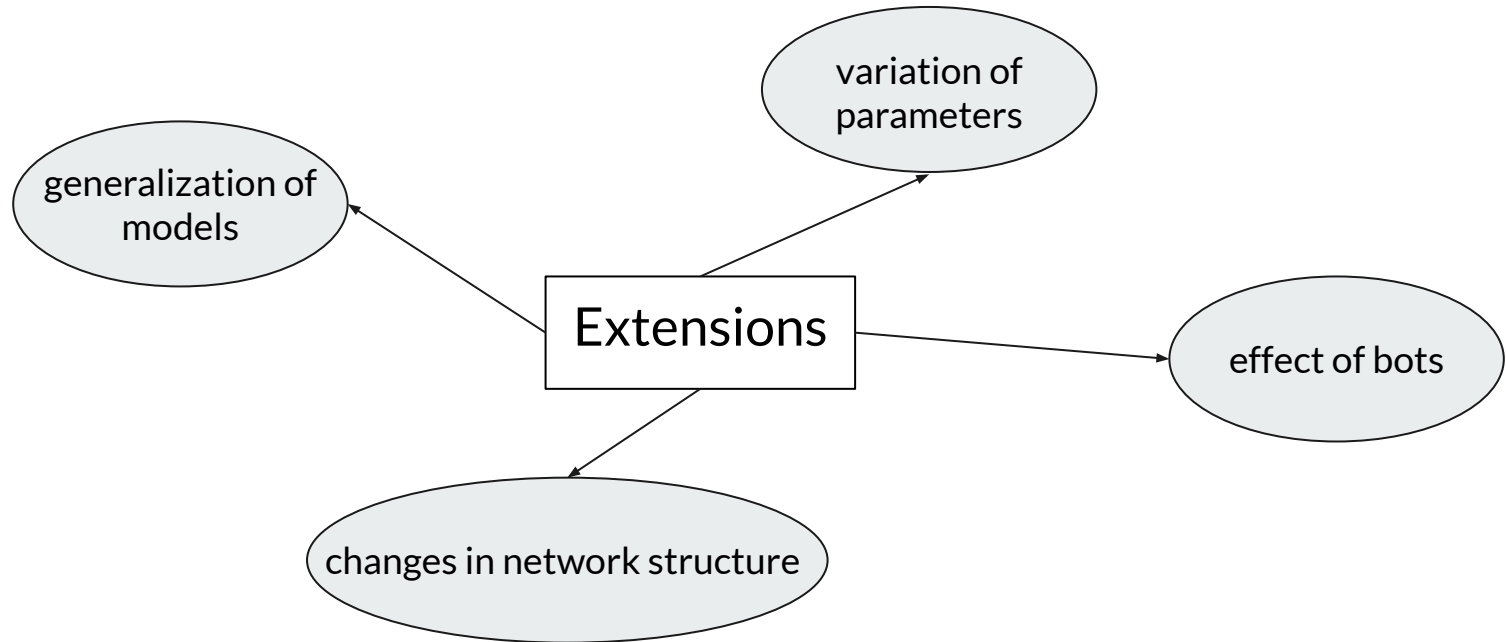
Conclusion

Reproduction of Models



- very similar findings for reproduced experiments and parameters
- only minor deviations due to smaller networks
- indicates other results also likely valid for larger networks

Conclusion





Conclusion

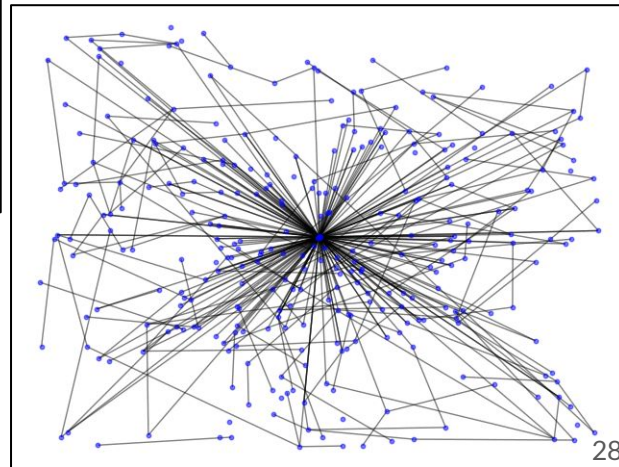
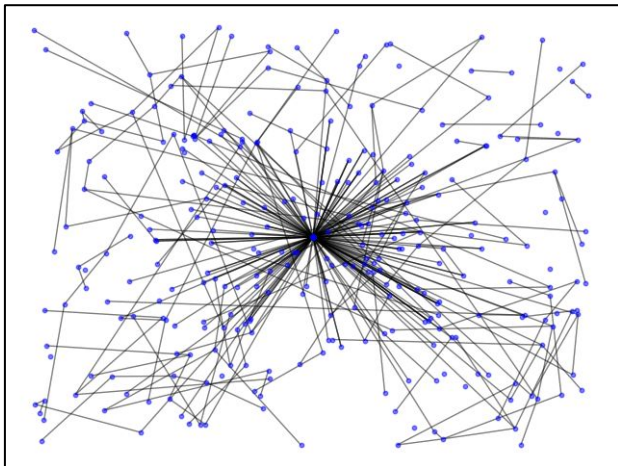
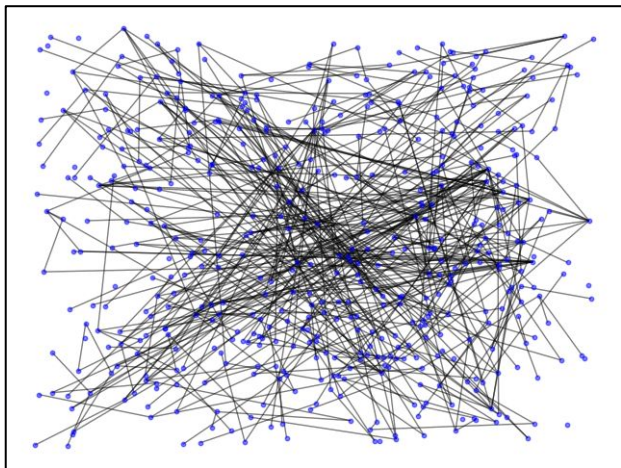
Critical assumption on
evaluative extremeness
& attitude as function of
opinions only

(Hyper)polarization only
allows (one) extreme
opinion on every topic
within one group

Critique

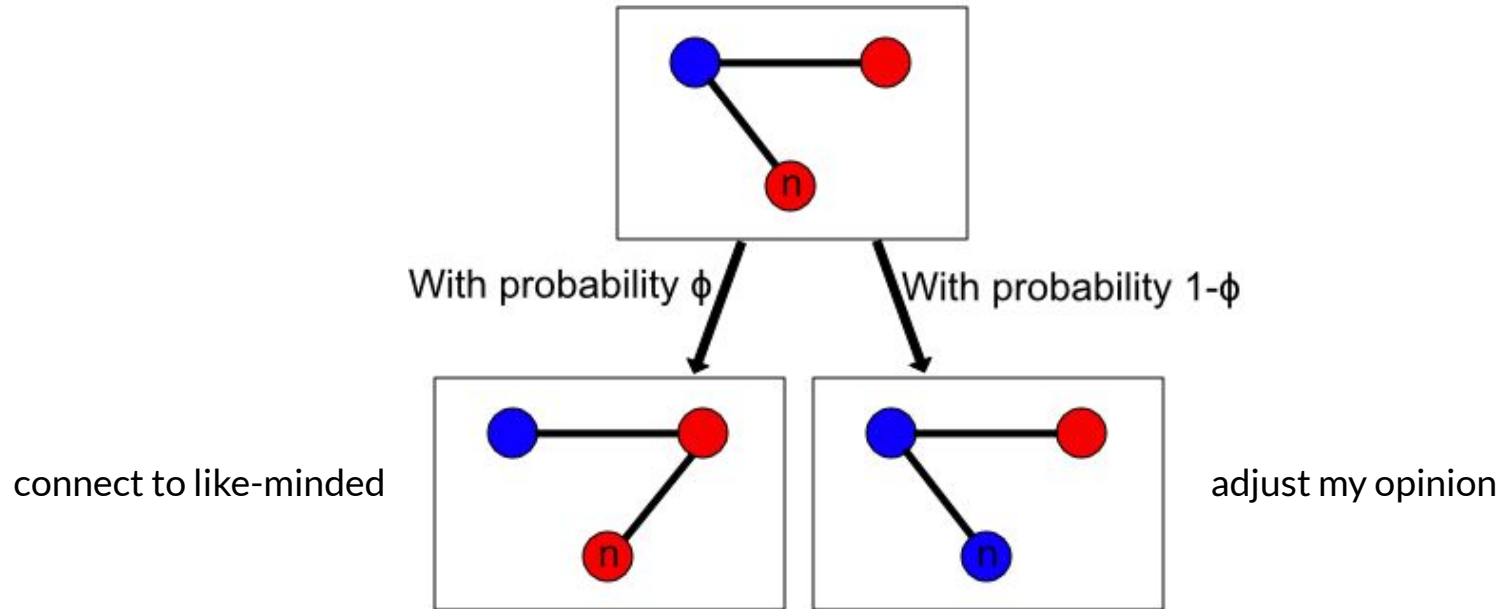
In general: different models can have
very different outcomes

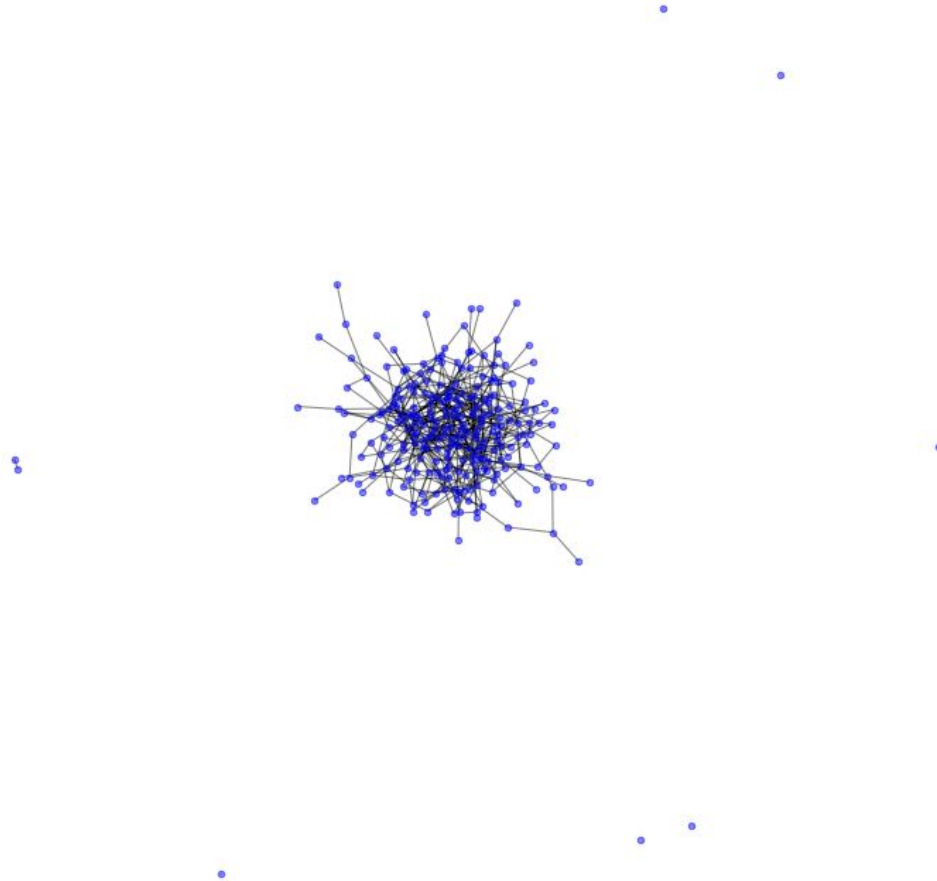
Thank you for your attention



Questions?

Coevolution Model







Implementation

1. Implement our own coevolution model
 - compare it to the coevolution model of Holme and Newman (2006)
2. Implement our own WBT model
 - compare to WBT model of Schweighofer et al. (2020)
3. Combine these two models to a generalized model

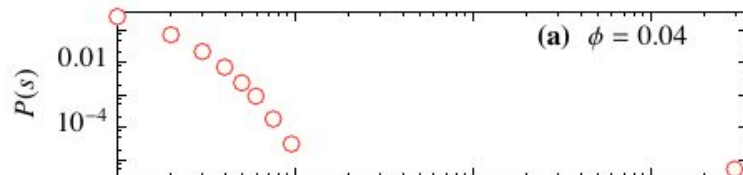


Model 2: Weighted Balance Theory

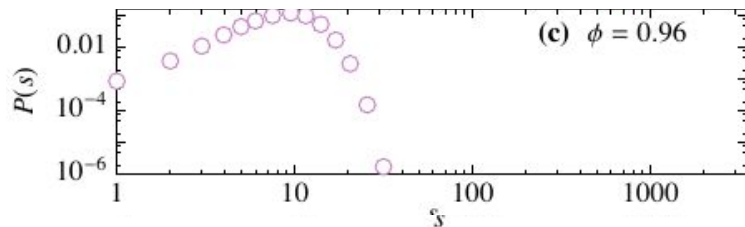
- simultaneous emergence of opinion extremeness and issue constraint (**Hyperpolarization**)
 - Two-party system, where all opinions are diametrically opposed

Comparison of Results

Holme 2006

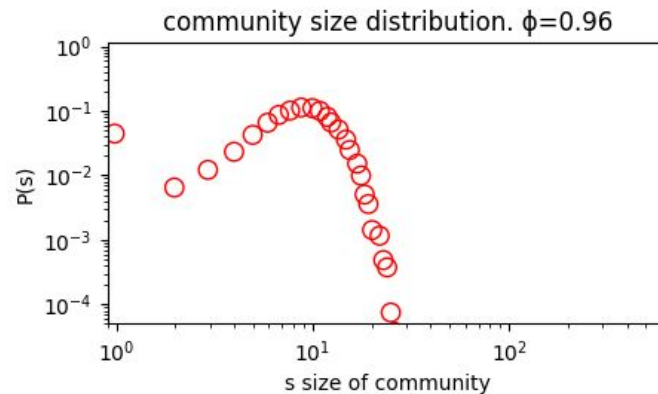
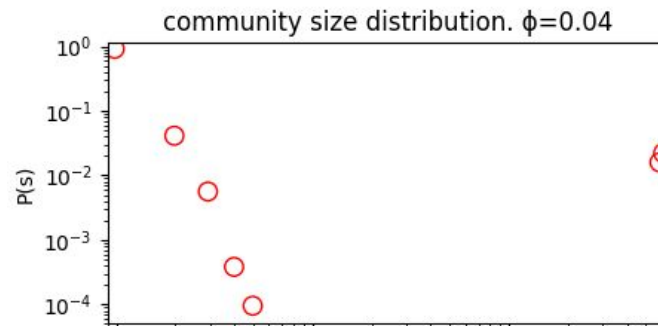


Histograms of community sizes (avg)



Reproduced by us.

$N=320$



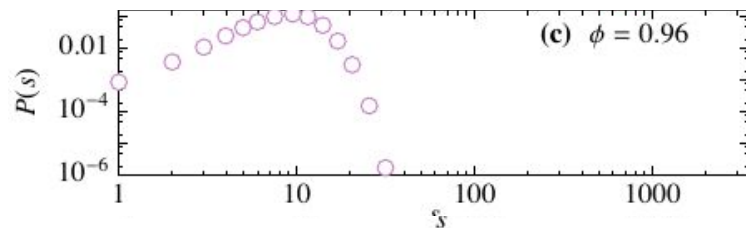


Reproduced by us

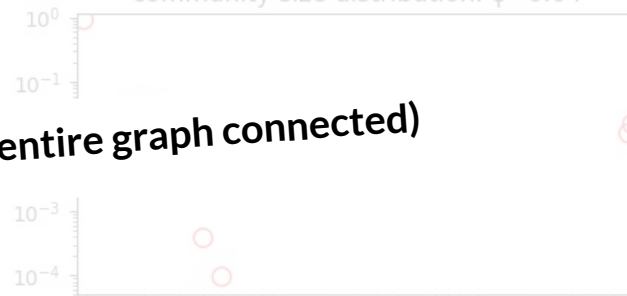
Holme 2006



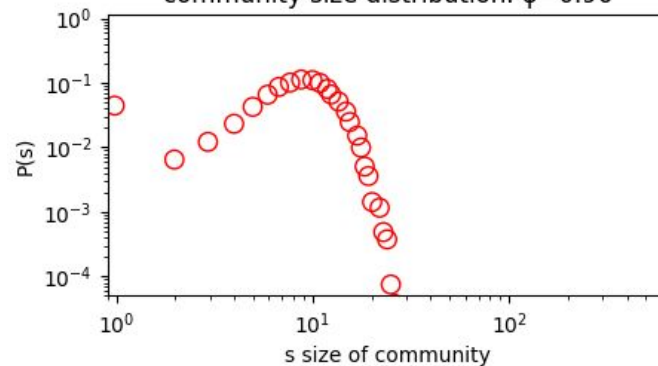
Random graph with giant component (almost entire graph connected)



community size distribution. $\phi=0.04$



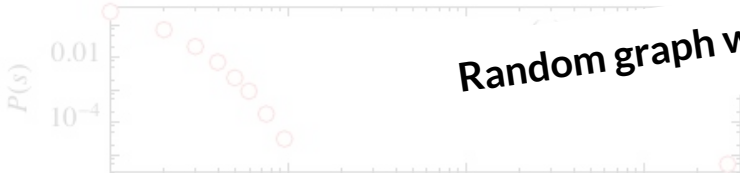
community size distribution. $\phi=0.96$



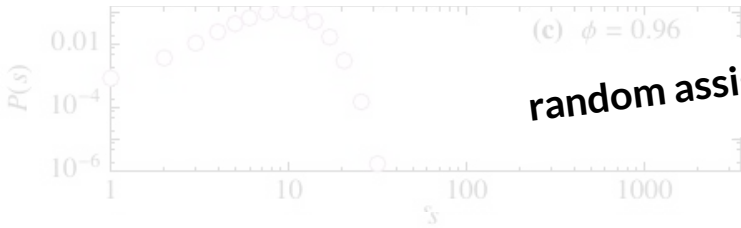


Reproduced by us

Holme 2006



Random graph with giant component

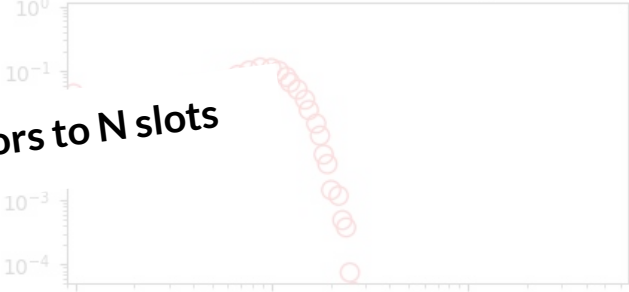


random assignment on K colors to N slots

community size distribution. $\phi=0.04$



community size distribution. $\phi=0.96$



s size of community



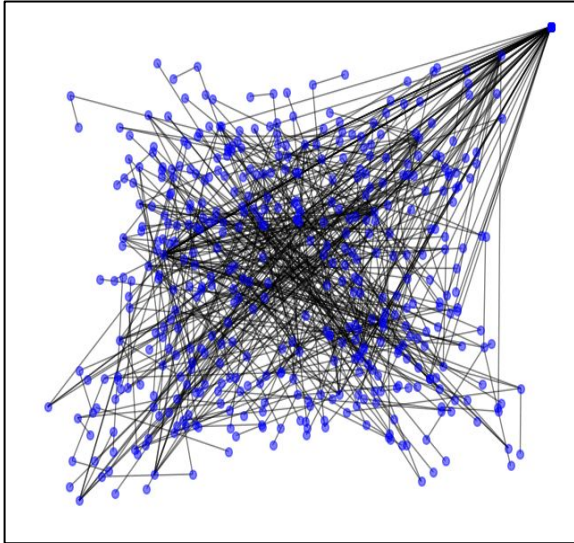
Model 2: Weighted Balance Theory

- simultaneous emergence of opinion extremeness and issue constraint (**Hyperpolarization**)
→ Two-party system
- Multi-dimensional opinion vectors with values within $[-1, +1]$
- Interpersonal attitudes within $[-1, +1]$ weighted with sigmoid-function and parameter e
→ **evaluative extremeness** (Backfire-Effect, convergence of like-minded agents)

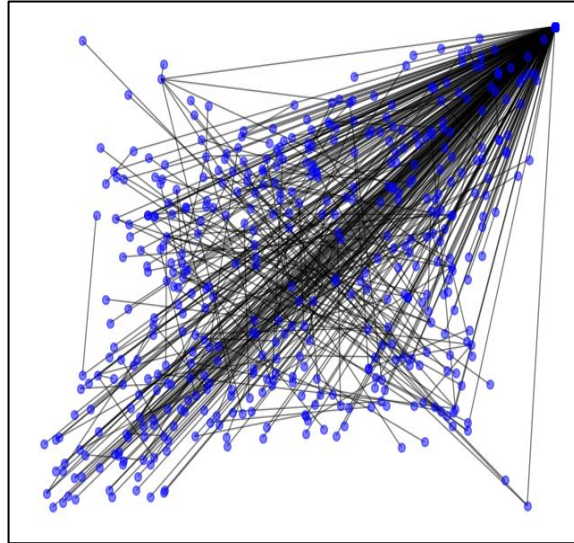


Bots in static Barabási–Albert graph ($e=0$)

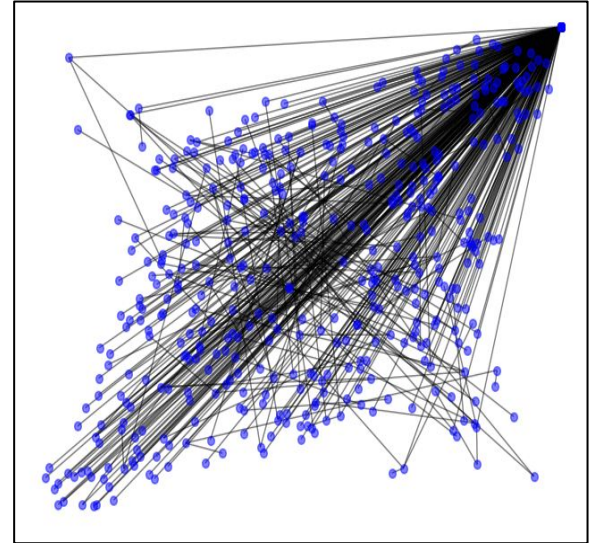
50 bots in least connected nodes



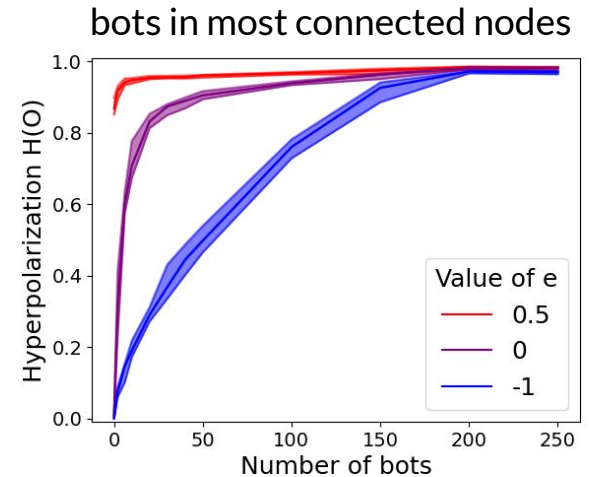
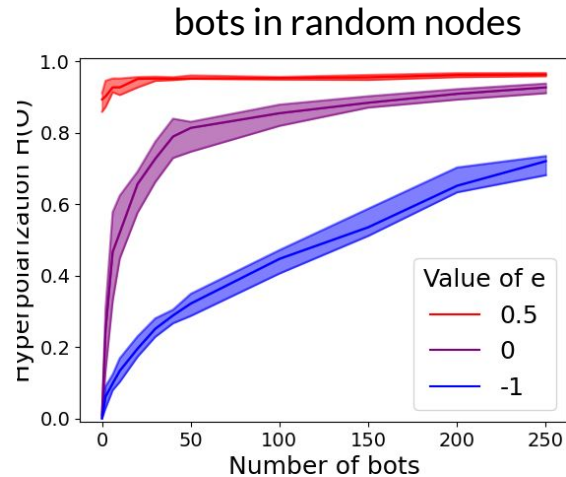
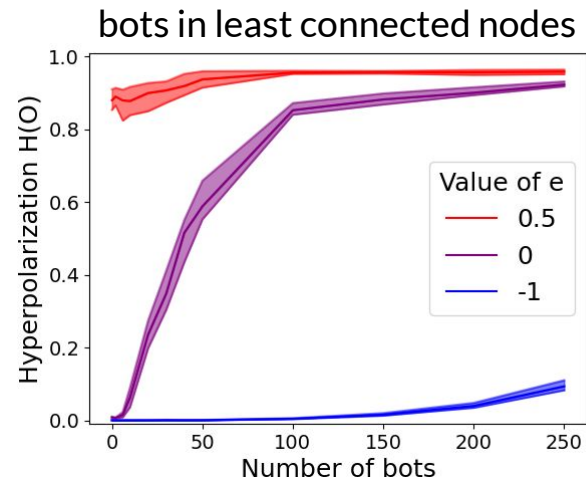
50 bots in random nodes



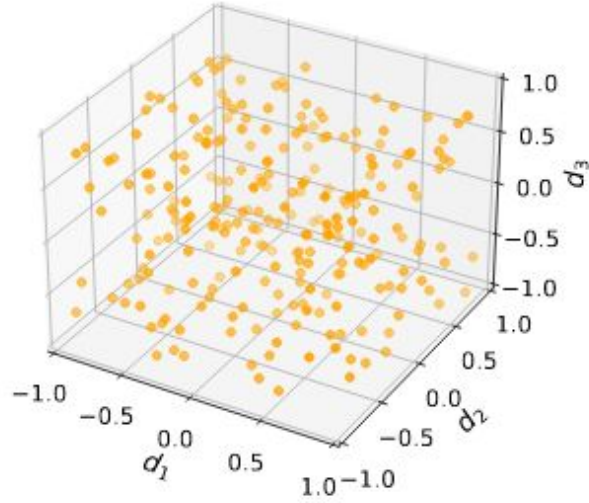
50 bots in most connected nodes



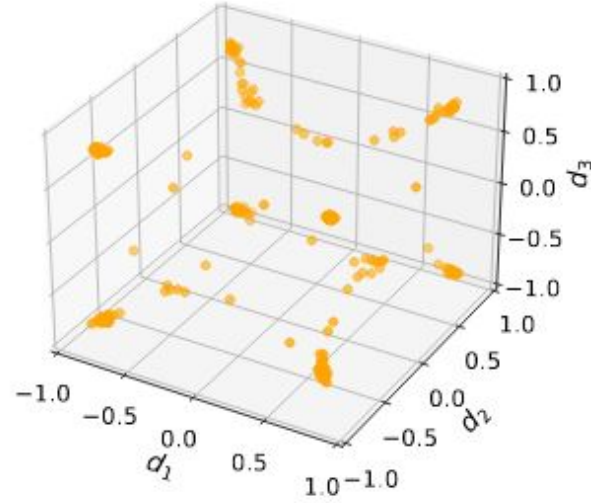
Bots in static Barabási–Albert graph ($e=0$)



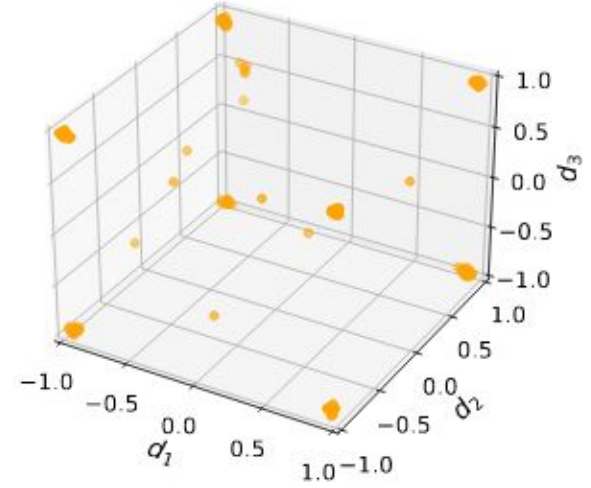
t=0



t=50



t=100



General Model, $N=250, D=3, e=0.3, \alpha=0.3, \varphi=0.45, \varepsilon(N,D,z)=0.3$.