

Strings & Software Model Checking

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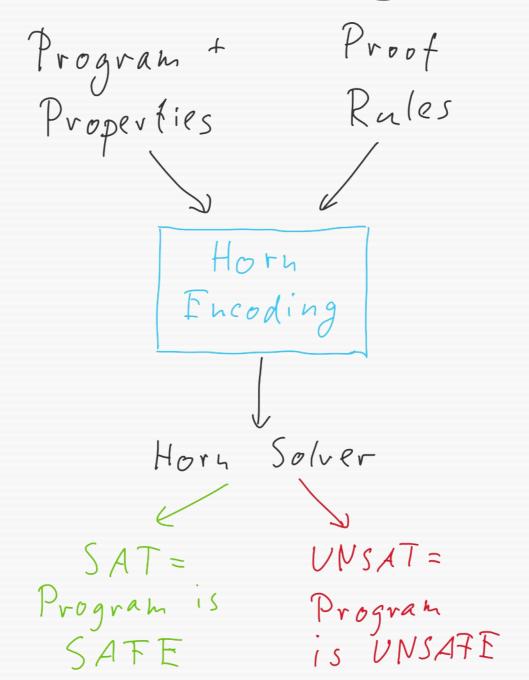
30 August 2019 Taipei, Taiwan

Outline

- Constrained Horn Clauses
- JayHorn Architecture
- JayHorn Approach to Handling Heap
- Demos & Examples

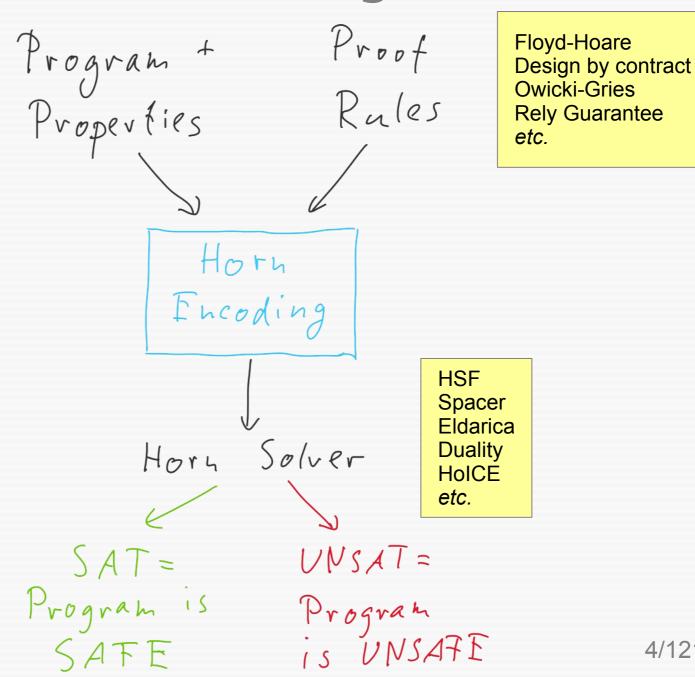
- Decision Procedures for Strings
- Strings in Software Model Checking

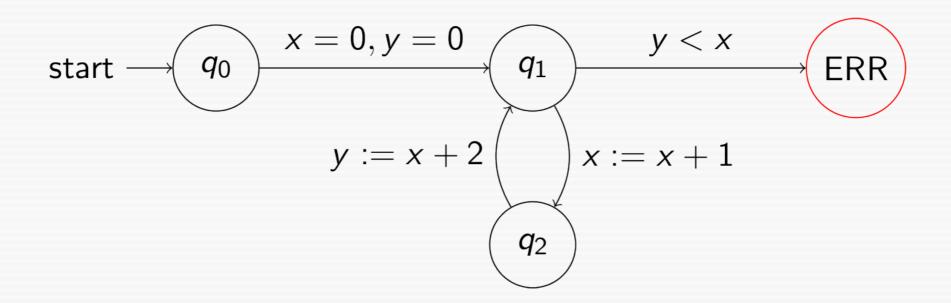
Verification Engines

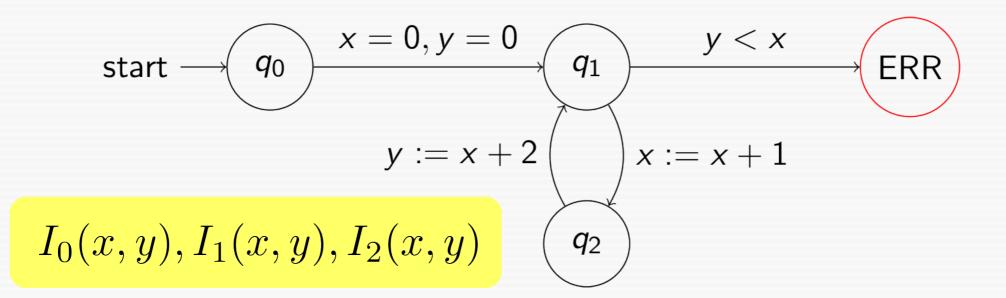


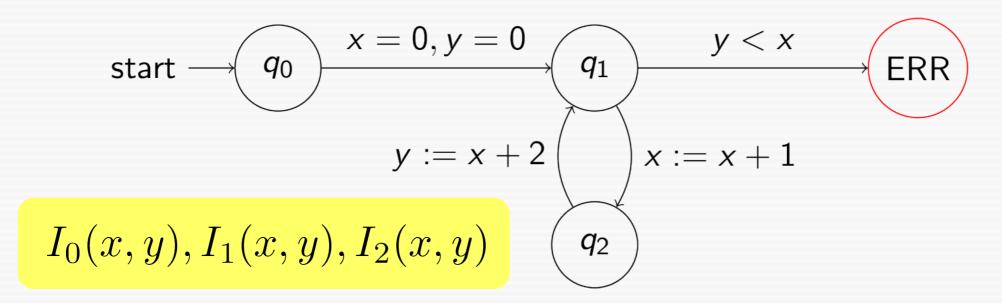
Verification Engines

Software programs Networks of timed automata **BIP** models etc.

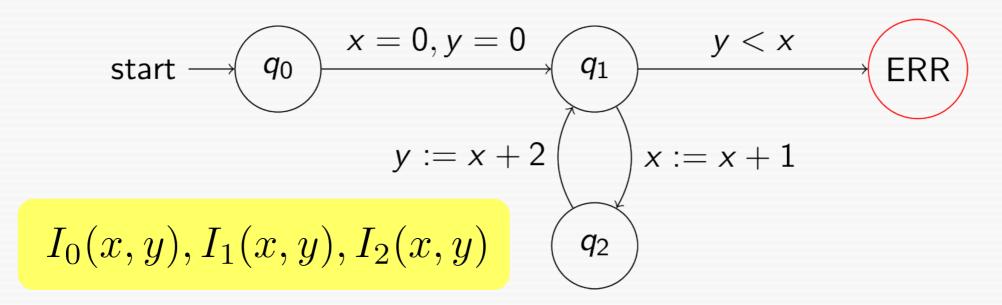




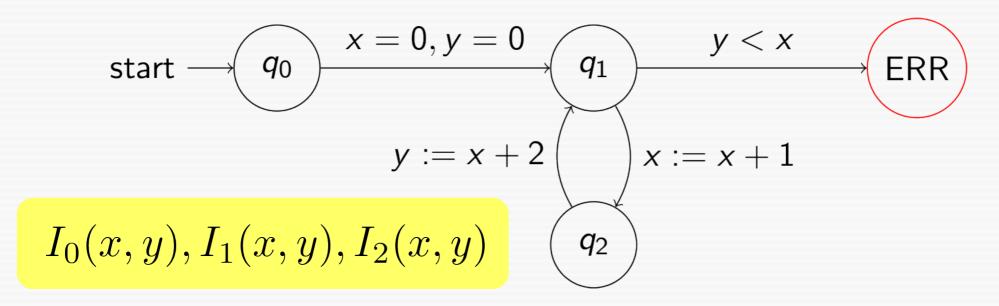




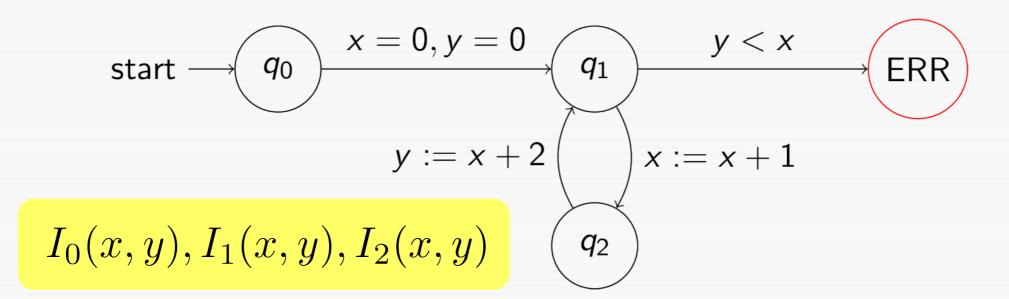
• When the program is in q_0 , $I_0(x,y)$ holds



- When the program is in q_0 , $I_0(x,y)$ holds
- When the program is in q_0 and $I_0(x,y)$ holds, then after transition to q_1 the formula $I_1(x,y)$ holds



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- When the program is in q_0 and $I_0(x,y)$ holds, then after transition to q_1 the formula $I_1(x,y)$ holds
- etc.



- When the
- When the holds, the formula
- etc.

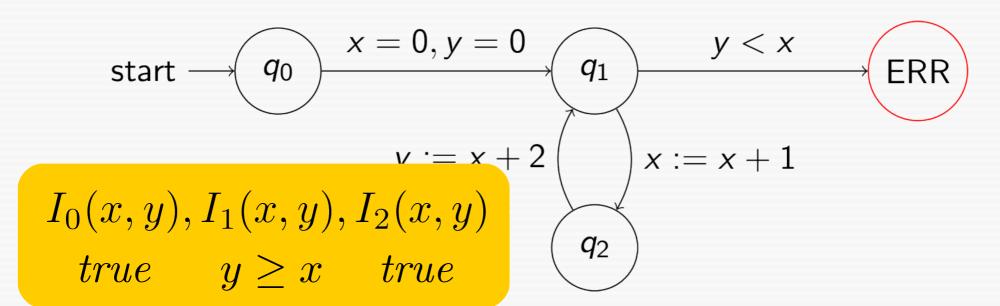
Constraints:

$$\forall x, y. \ true \rightarrow I_0(x, y)$$

 $\forall x, y. \ I_0(x, y) \rightarrow I_1(0, 0)$
 $\forall x, y. \ I_1(x, y) \rightarrow I_2(x + 1, y)$
 $\forall x, y. \ I_2(x, y) \rightarrow I_1(x, x + 2)$
 $\forall x, y. \ I_1(x, y) \land y < x \rightarrow false$

y) holds

 $I_0(x,y)$ the



- When the
- When the holds, the formula
- etc.

Constraints:

$$\forall x, y. \ true \rightarrow I_0(x, y)$$

 $\forall x, y. \ I_0(x, y) \rightarrow I_1(0, 0)$
 $\forall x, y. \ I_1(x, y) \rightarrow I_2(x + 1, y)$
 $\forall x, y. \ I_2(x, y) \rightarrow I_1(x, x + 2)$
 $\forall x, y. \ I_1(x, y) \land y < x \rightarrow false$

y) holds

 $I_0(x,y)$ the

In Machine-Readable Format

```
(set-logic HORN)
(declare-fun IO (Int Int) Bool)
(declare-fun I1 (Int Int) Bool)
(declare-fun I2 (Int Int) Bool)
(assert (forall ((x Int) (y Int)) (I0 x y)))
(assert (forall ((x Int) (y Int)) (\Rightarrow (I0 x y) (I1 0 0))))
(assert (forall ((x Int) (y Int)) (=> (I1 x y) (I2 (+ x 1) y))))
(assert (forall ((x Int) (y Int)) (=> (I2 x y) (I1 x (+ x 2)))))
(assert (forall ((x Int) (y Int)) (\Rightarrow (and (I1 x y) (< y x)) false)))
(check-sat)
(get-model)
```

In Machine-Readable Format

```
(set-logic HORN)
(declare-fun IO (Int Int) Bool)
(declare-fun I1 (Int Int) Bool)
(declare-fun I2 (Int Int) Bool)
(assert (forall ((x Int) (y Int)) (I0 x y)))
(assert (forall ((x Int) (y Int)) (\Rightarrow (I0 x y) (I1 0 0))))
(assert (forall ((x Int) (y Int)) (=> (I1 \times y) (I2 (+ \times 1) y)))
(assert (forall ((x Int) (y Int)) (=> (I2 \times y) (I1 \times (+ \times 2))))
(assert (forall ((x Int) (y Int)) (\Rightarrow (and (I1 x y) (< y x)) false)))
(check-sat)
(get-model)
                          i0(X, Y) :- 1=1.
                          i1(X', Y') :- i0(X, Y), X'=0, Y'=0.
                          i2(X', Y) :- i1(X, Y), X'=X+1.
                          i1(X, Y') :- i2(X, Y), Y'=X+2.
                          false :- i1(X, Y), Y < X.
                                                                    13/121
```

More formally ...

Definition

Suppose

- L is some constraint language (e.g., integers);
- \mathcal{R} is a set of relation symbols;
- \mathcal{X} is a set of first-order variables.

Then a *Horn clause* is a formula $C \wedge B_1, \dots, B_n \rightarrow H$ where

- C is a constraint in \mathcal{L} (without symbols from \mathcal{R});
- each B_i is a literal of the form $r(t_1, \ldots, t_m)$;
- H is either false, or of the same form as the B_i .

More formally ...

Definition

Suppose

- L is some constraint language (e.g., integers);
- \mathcal{R} is a set of relation symbols;
- \mathcal{X} is a set of first-order variables.

Then a *Horn clause* is a formula $C \wedge B_1, \dots, B_n \rightarrow H$ where

- Definition
- A set C of Horn clauses is (syntactically)
- solvable if the \mathcal{R} -symbols can be replaced with formulae such that all clauses become valid.

General Encoding Strategy

Choose a set of relation symbols representing

Inductive invariants

- for instance
 - one per control location
 - one per process
 - one per module
 - one per class/class instance
- Add constraints on inductive invariants: initiation, consecution
- Add safety constraints: invariants exclude error states

General Encoding Strategy

Choose a set of relation symbols representing

Program is correct (safe)

Constraints are solvable

- Add constraints on inductive invariants: initiation, consecution
- Add safety constraints: invariants exclude error states

$$f(x) = \begin{cases} x - 10, & \text{if } x > 100\\ f(f(x+11)), & \text{if } x \le 100 \end{cases}$$

$$f(x) = \begin{cases} x - 10, & \text{if } x > 100\\ f(f(x+11)), & \text{if } x \le 100 \end{cases}$$

Verify
$$x \le 100 \to f(x) = 91$$

$$f(x) = \begin{cases} x - 10, & \text{if } x > 100\\ f(f(x+11)), & \text{if } x \le 100 \end{cases}$$

Verify
$$x \le 100 \rightarrow f(x) = 91$$

Partial correctness

```
f(x) = \begin{cases} x - 10, & \text{if } x > 100\\ f(f(x+11)), & \text{if } x \le 100 \end{cases}
```

```
Verify x \le 100 \to f(x) = 91
```

```
int f(int x) {
   if (x > 100) {
     int t0 = x - 10;
     return t0;
   } else {
   int t0 = x + 11;
   int t1 = f(t0);
   int t2 = f(t1);
   return t2;
  }
}
```

Partial correctness

Full Encoding

```
i0(X0, X) : - X0=X.
                                        % int f(int x) {
i1(X0, X) :- i0(X0, X), X > 100. % if (X > 100) {
i2(X0, T0) :- i1(X0, X), T0=X-10.
                                    % int t0 = x - 10;
                                      % return t0;
post_f(X0, T0) :- i2(X0, T0).
i3(X0, X) :- i0(X0, X), X = < 100. % } else {
i4(X0, T0) :- i3(X0, X), T0=X+11.
                                              int t0 = x + 11;
i5(X0, T1) :- i4(X0, T0), post_f(T0, T1). %
                                              int t1 = f(t0);
i6(X0, T2) :- i5(X0, T1), post_f(T1, T2). % int t2 = f(t1);
post f(X0, T2) := i6(X0, T2).
                                         % return t2;
                                         % }
false :- post_f(X, R), X = < 100, \backslash + (R = 91). % Assertion
```

```
int N;
int i = 0, x = 1;
assume (N > 0);
while (i < N) {</pre>
 x *= 2;
  ++i;
assert (x > 1);
```

int N;

```
int i = 0, x = 1;
assume (N > 0);
while (i < N) {
 x *= 2;
  ++i;
assert (x > 1);
```

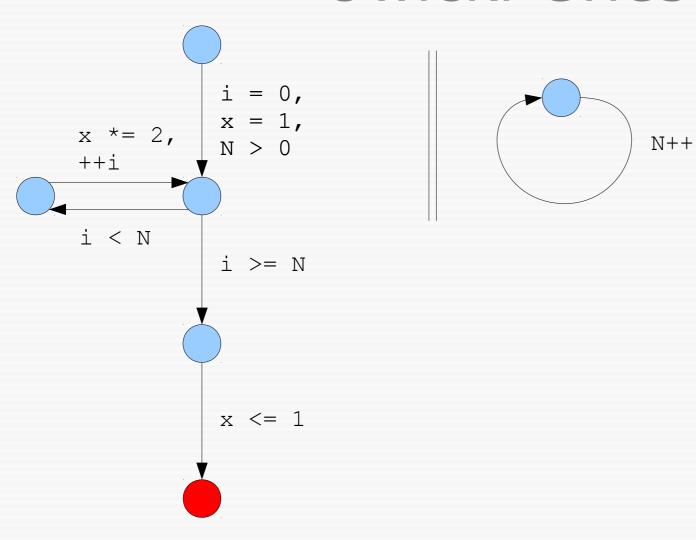
Loop invariant:

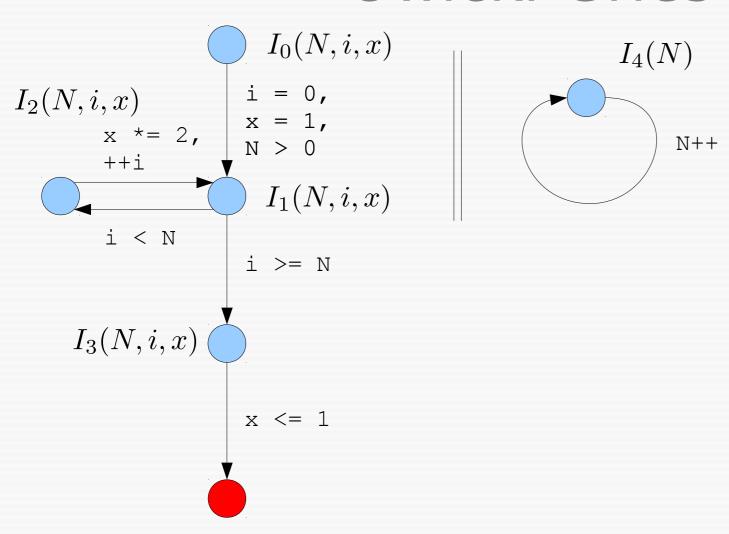
```
x >= 2 | (x = 1 \& i < N)
```

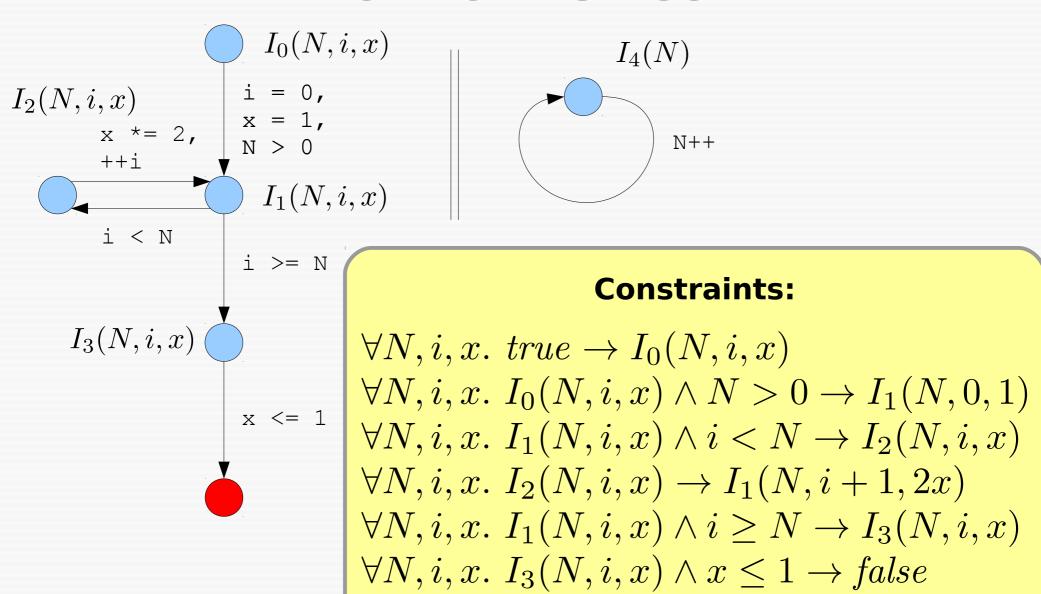
```
int N;
int i = 0, x = 1;
assume (N > 0);
                            Loop invariant:
                       x >= 2 | (x = 1 \& i < N)
while (i < N) {
 x *= 2;
  ++i;
                               while (1) {
                                 N++;
assert (x > 1);
```

```
int N;
int i = 0, x = 1;
assume (N > 0);
                            Loop invariant:
                       x >= 2 | (x = 1 \& i < N)
while (i < N) {
  x *= 2;
  ++i;
                               while (1) {
                                 N++;
assert (x > 1);
```

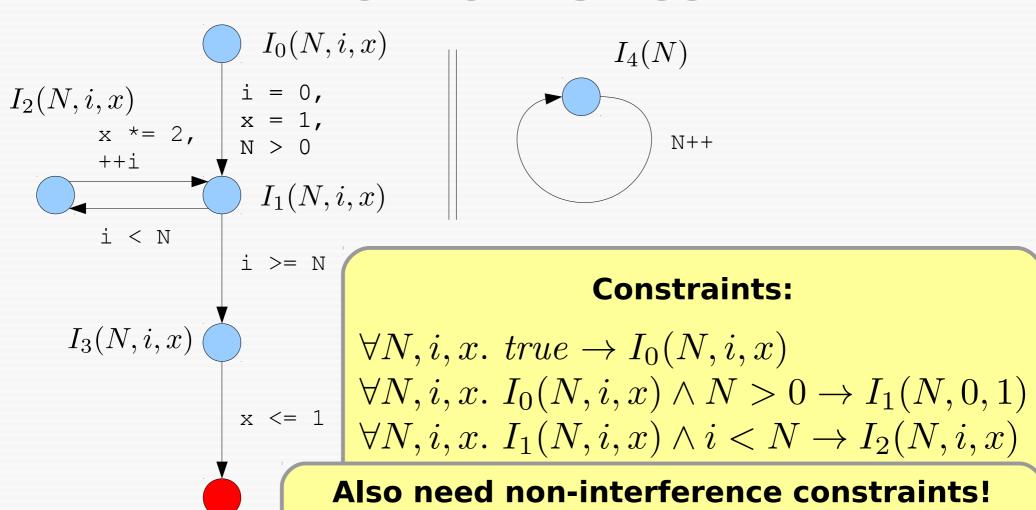
Can invariant still be used?





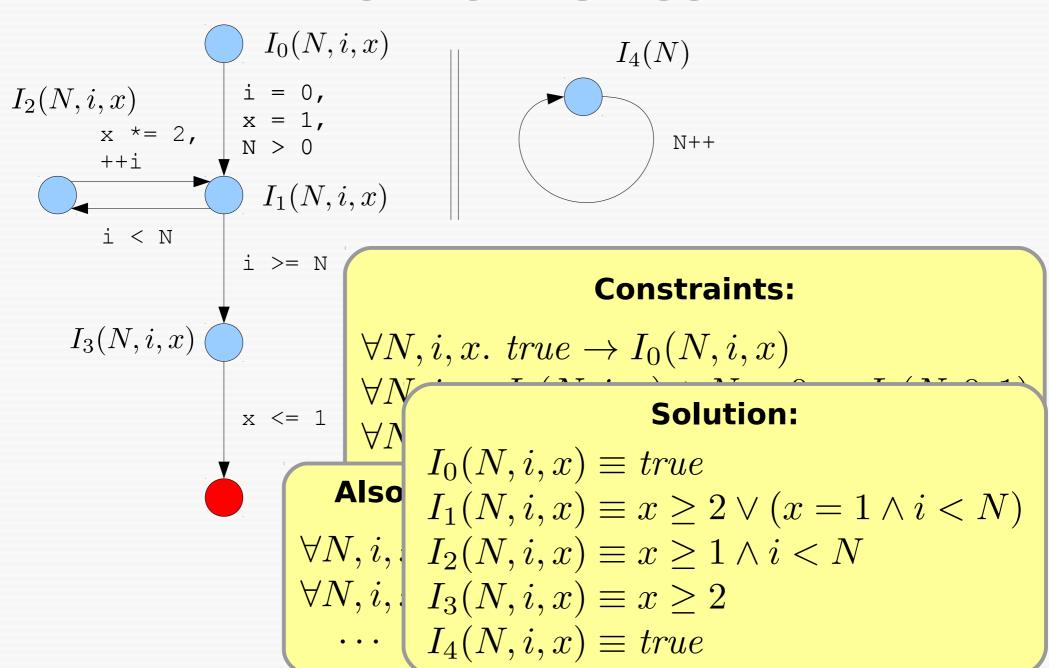


 $\forall N. \ I_4(N) \rightarrow I_4(N+1)$



$$\forall N, i, x. \ I_0(N, i, x) \land I_4(N) \to I_0(N+1, i, x)$$

 $\forall N, i, x. \ I_1(N, i, x) \land I_4(N) \to I_1(N+1, i, x)$



Other Horn Encodings

- Owicki-Gries
- Rely-guarantee
- Various forms of thread communication
- Parameterised systems
- Synchronous programs
- Timed systems
- Regression verification
- Games
- Networks, SDN

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CHC-COMP 2018

Arie Gurfinkel

Philipp Ruemmer, Grigory Fedyukovich, Adrien Champion

1st Competition on Solving Constrained Horn Clauses





Report on the Second Edition of the CHC Competition

Grigory Fedyukovich

Results: LIA-Nonlin



Solver	Score	#SAT	#UNSAT	Avg time
Spacer	270	153	117	5.04
Eldarica	234	131	103	15.93
Ultimate Unihorn Automizer	177	96	81	36.94
Hoice	176	110	66	9.85
PCSat	123	81	42	24.69
Ultimate Tree Automizer	73	29	44	4.85

^{* 283} instances total

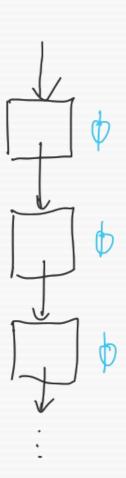
Data Structures and Heap?

Data Structures and Heap?

- Encoding using McCarthy Arrays
 - Precise, relatively complete
 - Hard to infer invariants automatically
- Refinement types, etc.
 - Incomplete
 - Easier to automate
- (Separation logic, ownership systems, dynamic frames, etc.)

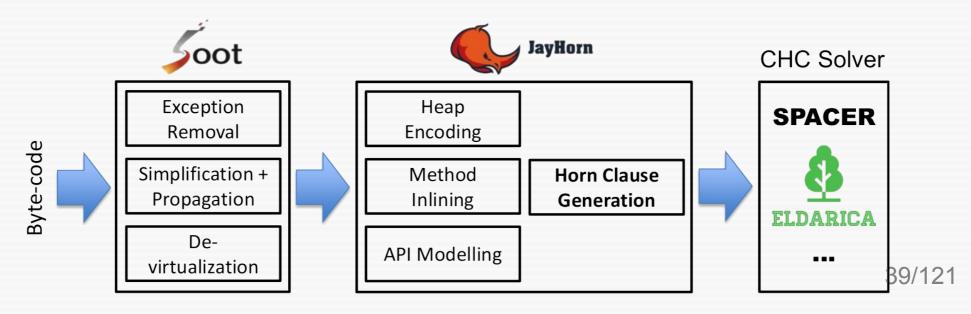
Data Structures and Heap?

- Encoding using McCarthy Arrays
 - Precise, relatively complete
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 - Incomplete
 - Easier to automate
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- A Horn-based verification tool for Java
- Fully implemented in Java
- Fully automatic
- Open source, MIT licence



Demo

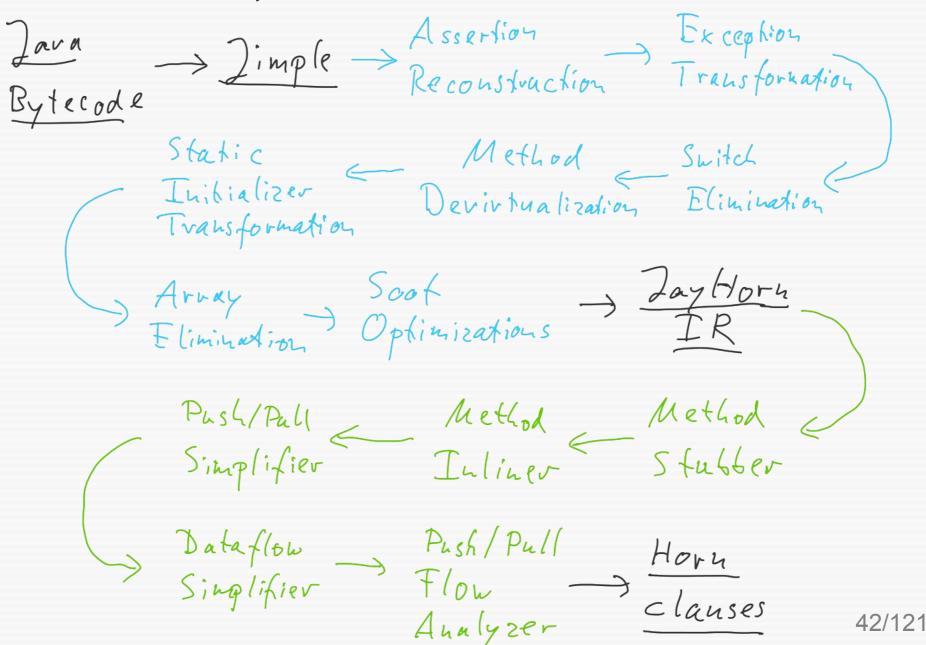
```
import org.sosy lab.sv benchmarks.Verifier;
public class McCarthy91 {
    private static int f(int n) {
        if (n > 100)
            return n - 10;
        else
            return f(f(n + 11));
    }
    public static void main(String[] args) {
        int x = Verifier.nondetInt();
        int y = f(x);
        assert(x > 101 \mid | y == 91);
```

Demo

```
import org.sosy lab.sv benchmarks.Verifier;
public class McCarthy91 {
     private static int f(int n) {
           if (n > 100)
                                                    https://github.com/sos
y-lab/sv-benchmarks/bl
ob/master/java/commo
n/org/sosy_lab/sv_benc
hmarks/Verifier.java
                return n - 10;
           else
                return f(f(n + 11));
     }
     public static void main(String[] args) {
           int x = Verifier.nondetInt();
           int y = f(x);
           assert(x > 101 \mid y == 91);
```

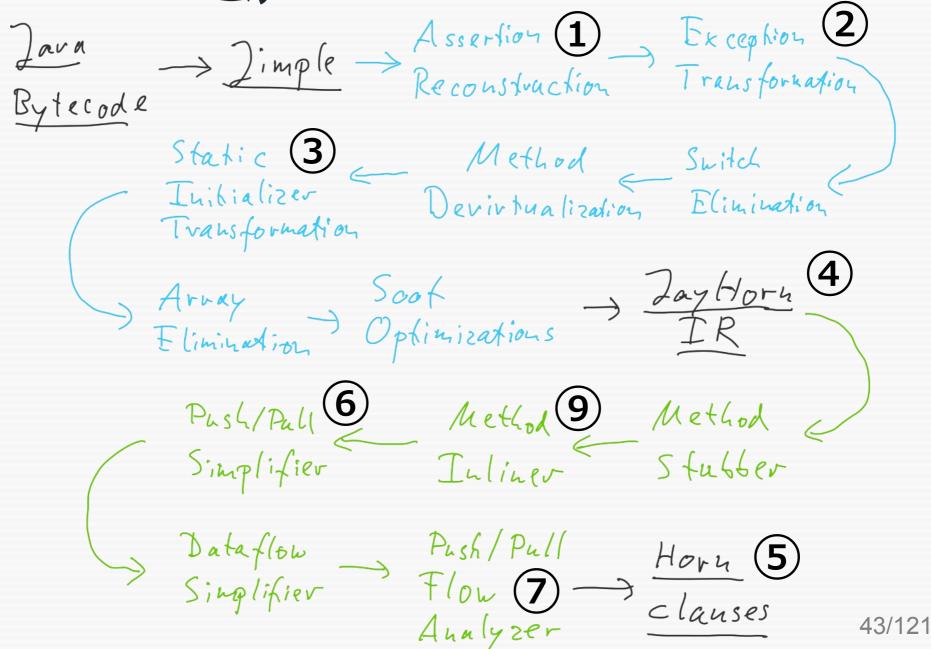


Data-Flow





Data-Flow



From Java to Jimple

```
public class Test {
   int x, y;
  public static void main(String[] args) {
     Test t = new Test();
     while (t.x < 10)
        t.x++;
     assert(t.x == 10);
  }
}</pre>
```

```
<Test: void main(java.lang.String[])>
                                                     public class Test {
public static void main(java.lang.String[])
                                                          int x, y;
                                                          public static void main(...) {
    java.lang.String[] r0;
                                                              Test t = new Test();
    Test r1, $r2;
                                                              while (t.x < 10)
    int $i0, $i1, $i2, $i3;
                                                                  t.x++;
    boolean $z0;
                                                              assert(t.x == 10);
    java.lang.AssertionError $r3;
    r0 := @parameter0: java.lang.String[];
    r2 = new Test;
    specialinvoke $r2.<Test: void <init>()>();
    r1 = r2;
 label1:
    \sin = r1.<\text{Test: int }x>
    if $i0 \ge 10 goto label2;
    $i2 = r1.<Test: int x>;
    $i3 = $i2 + 1;
    r1.<Test: int x> = $i3;
    goto label1;
 label2:
    $z0 = <Test: boolean $assertionsDisabled>;
    if z0 != 0 goto label3;
    $i1 = r1.<Test: int x>;
    if $i1 == 10 \text{ qoto label3};
    $r3 = new java.lang.AssertionError;
    specialinvoke $r3.<java.lang.AssertionError: void <init>()>();
    throw $r3;
label3:
    return;
                                                                                 45/121
```

```
<Test: void main(java.lang.String[])>
                                                    public class Test {
public static void main(java.lang.String[])
                                                        int x, y;
                                                        public static void main(...) {
    java.lang.String[] r0;
                                                            Test t = new Test();
    Test r1, $r2;
                                                            while (t.x < 10)
    int $i0, $i1, $i2, $i3;
                                                                t.x++;
    boolean $z0;
                                                            assert(t.x == 10);
    java.lang.AssertionError $r3;
    r0 := @parameter0: java.lang.String[];
    r2 = new Test;
    specialinvoke $r2.<Test: void <init>()>();
    r1 = r2;
 label1:
                                        + Several further
    $i0 = r1.<Test: int x>:
    if $i0 \ge 10 goto label2;
                                              methods
    $i2 = r1.<Test: int x>;
    $i3 = $i2 + 1;
    r1.<Test: int x> = $i3;
    goto label1;
 label2:
    $z0 = <Test: boolean $assertionsDisabled>;
    if z0 != 0 goto label3;
    $i1 = r1.<Test: int x>;
    if $i1 == 10 \text{ qoto label3};
    $r3 = new java.lang.AssertionError;
    specialinvoke $r3.<java.lang.AssertionError: void <init>()>();
    throw $r3;
label3:
    return;
```

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```
<Test: void main(java.lang.String[])>
                                                    public class Test {
public static void main(java.lang.String[])
                                                         int x, y;
                                                         public static void main(...) {
    java.lang.String[] r0;
                                                             Test t = new Test();
    Test r1, $r2;
                                                             while (t.x < 10)
    int $i0, $i1, $i2, $i3;
                                                                 t.x++;
    boolean $z0;
                                                             assert(t.x == 10);
    java.lang.AssertionError $r3;
    r0 := @parameter0: java.lang.String[];
    r2 = new Test;
    specialinvoke $r2.<Test: void <init>()>();
    r1 = r2;
                                    Load instruction
 label1:
    \sin = r1.<\text{Test: int }x>
    if $i0 \ge 10 goto label2;
    $i2 = r1.<Test: int x>;
    $i3 = $i2 + 1;
                                    Store instruction
    r1.<Test: int x> = $i3;
    goto label1;
 label2:
    $z0 = <Test: boolean $assertionsDisabled>;
    if z0 != 0 goto label3;
    $i1 = r1.<Test: int x>;
    if $i1 == 10 \text{ qoto label3};
    $r3 = new java.lang.AssertionError;
    specialinvoke $r3.<java.lang.AssertionError: void <init>()>();
    throw $r3;
label3:
    return;
                                                                               47/121
```

```
<Test: void main(java.lang.String[])>
                                                     public class Test {
public static void main(java.lang.String[])
                                                         int x, y;
                                                         public static void main(...) {
    java.lang.String[] r0;
                                                             Test t = new Test();
    Test r1, $r2;
                                                             while (t.x < 10)
    int $i0, $i1, $i2, $i3;
                                                                 t.x++;
    boolean $z0;
                                                             assert(t.x == 10);
    java.lang.AssertionError $r3;
    r0 := @parameter0: java.lang.String[];
    r2 = new Test;
    specialinvoke $r2.<Test: void <init>()>();
    r1 = r2;
 label1:
    \sin = r1.<\text{Test: int }x>
    if $i0 \ge 10 goto label2;
    $i2 = r1.<Test: int x>;
    $i3 = $i2 + 1;
    r1.<Test: int x> = $i3;
    goto label1;
 label2:
    $z0 = <Test: boolean $assertionsDisabled>;
    if $z0 != 0 goto label3;
    $i1 = r1.<Test: int x>;
    if $i1 == 10 goto label3;
    $r3 = new java.lang.AssertionError;
    specialinvoke $r3.<java.lang.AssertionError: void <init>()>();
    throw $r3;
label3:
```

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```
<Test: void main(java.lang.String[])>
public static void main(java.lang.String[])
    java.lang.String[] r0;
    Test r1, $r2;
    int $i0, $i1, $i2, $i3;
    boolean $z0;
    java.lang.AssertionError $r3;
    r0 := @parameter0: java.lang.String[];
    r2 = new Test;
    specialinvoke $r2.<Test: void <init>()>();
    r1 = r2;
 label1:
    \sin = r1.<\text{Test: int }x>
    if $i0 \ge 10 goto label2;
    $i2 = r1.<Test: int x>;
    $i3 = $i2 + 1;
    r1.<Test: int x> = $i3;
    goto label1;
```

label2:

Reconstructed assertion

```
$i1 = r1.<Test: int x>;
if $i1 == 10 goto label3;
$assert_9 = 0;
staticinvoke <JayHornAssertions: void assertion(boolean)>($assert_9);
```

```
label3:
return;
```

```
<Test: void main(java.lang.String[])>
                                                      public class Test {
public static void main(java.lang.String[])
                                                          int x, y;
                                                          public static void main(...) {
    java.lang.String[] r0;
                                                              Test t = new Test();
    Test r1, $r2;
                                                              while (t.x < 10)
    int $i0, $i1, $i2, $i3;
                                                                  t.x++;
    boolean $z0;
                                                              assert(t.x == 10);
    java.lang.AssertionError $r3;
    r0 := @parameter0: java.lang.String[];
    r2 = new Test;
    specialinvoke $r2.<Test: void <init>()>();
    r1 = r2;
 label1:
    \sin = r1.<\text{Test: int }x>
    if $i0 \ge 10 goto label2;
    $i2 = r1.<Test: int x>;
    $i3 = $i2 + 1;
    r1.<Test: int x> = $i3;
    goto label1;
label2:
    $i1 = r1.<Test: int x>;
    if $i1 == 10 \text{ qoto label3};
    sassert 9 = 0;
    staticinvoke <JayHornAssertions: void assertion(boolean)>($assert 9);
label3:
    return;
                                                                                 50/121
```

```
<Test: void main(java.lang.String[])>
                                                                                                                                                                public class Test {
public static void main(java.lang.String[])
                                                                                                                                                                            int x, y;
                                                                                                                                                                            public static void main(...) {
            java.lang.String[] r0;
                                                                                                                                                                                        Test t = new Test();
            Test r1, $r2;
                                                                                                                                                                                         while (t.x < 10)
            int $i0, $i1, $i2, $i3;
                                                                                                                                                                                                     t.x++;
            boolean $z0;
                                                                                                                                                                                         assert(t.x == 10);
            java.lang.AssertionError $r3;
            r0 := @parameter0: java.lang.String[];
            r2 = new Test;
            specialinvoke $r2.<Test: void <init>()>();
            $helper1 = <JayHornAssertions: java.lang.Throwable lastExceptionThrown>;
            $assert 11 = $helper1 == null;
            staticinvoke <JayHornAssertions: void assertion(boolean)>($assert 11);
            r1 = r2;
                                                                                                            Exception passing through variables;
   label1:
                                                                                                            assert absence of exceptions
            $i0 = r1.<Test: int x>;
            if $i0 \ge 10 goto label2;
            $i2 = r1.<Test: int x>;
            $i3 = $i2 + 1;
            r1.<Test: int x> = $i3;
            goto label1;
   label2:
            $i1 = r1.<Test: int x>;
            if $i1 == 10 goto label3;
            accepte{accepted} accepted accepted} accepted 
            staticinvoke <JayHornAssertions: void assertion(boolean)>($assert 9);
  label3:
            return;
                                                                                                                                                                                                                                                 51/121
```

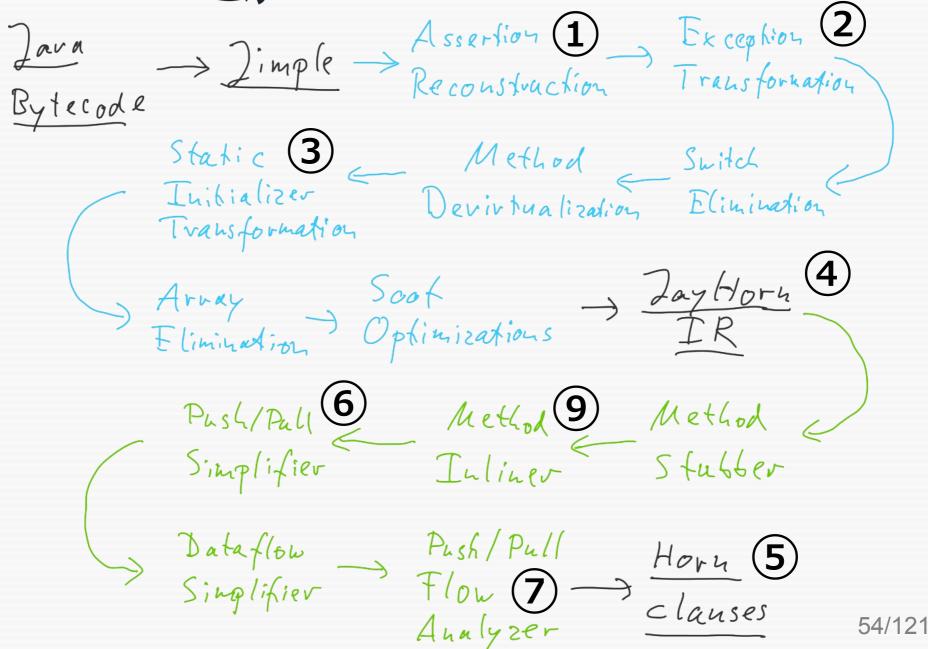
```
<Test: void main(java.lang.String[])>
                                                                                                                                                                            public class Test {
public static void main(java.lang.String[])
                                                                                                                                                                                          int x, y;
                                                                                                                                                                                          public static void main(...) {
             java.lang.String[] r0;
                                                                                                                                                                                                      Test t = new Test();
             Test r1, $r2;
                                                                                                                                                                                                       while (t.x < 10)
             int $i0, $i1, $i2, $i3;
                                                                                                                                                                                                                    t.x++;
             boolean $z0;
                                                                                                                                                                                                       assert(t.x == 10);
             java.lang.AssertionError $r3;
             r0 := @parameter0: java.lang.String[];
             r2 = new Test;
             specialinvoke $r2.<Test: void <init>()>();
             $helper1 = <JayHornAssertions: java.lang.Throwable lastExceptionThrown>;
             $assert 11 = $helper1 == null;
             staticinvoke <JayHornAssertions: void assertion(boolean)>($assert 11);
             r1 = r2;
   label1:
             $i0 = r1.<Test: int x>;
             if $i0 \ge 10 goto label2;
             $i2 = r1.<Test: int x>;
             $i3 = $i2 + 1;
             r1.<Test: int x> = $i3;
             goto label1;
   label2:
             $i1 = r1.<Test: int x>;
             if $i1 == 10 goto label3;
             accepte{accepted} accepted accepted} accepted 
             staticinvoke <JayHornAssertions: void assertion(boolean)>($assert 9);
  label3:
             return;
                                                                                                                                                                                                                                                                    52/121
```

```
<Test: void main(java.lang.String[])>
                                                    public class Test {
public static void main(java.lang.String[])
                                                         int x, y;
                                                         public static void main(...) {
    java.lang.String[] r0;
                                                             Test t = new Test();
    Test r1, $r2;
                                                             while (t.x < 10)
    int $i0, $i1, $i2, $i3;
                                                                 t.x++;
    boolean $z0;
                                                             assert(t.x == 10);
    java.lang.AssertionError $r3:
    r0 := @parameter0: java.lang.String[];
    staticinvoke <Test: void <clinit>()>();
                                                            Static initialisers
    staticinvoke <JayHornAssertions: void <clinit>()>();
    r2 = new Test;
                                                            as normal methods
    specialinvoke $r2.<Test: void <init>()>();
    $helper1 = <JayHornAssertions: java.lang.Throwable lastExceptionThrown>;
    $assert 11 = $helper1 == null;
    staticinvoke <JayHornAssertions: void assertion(boolean)>($assert 11);
    r1 = r2;
 label1:
    $i0 = r1.<Test: int x>;
    if $i0 \ge 10 goto label2;
    $i2 = r1.<Test: int x>;
    $i3 = $i2 + 1;
    r1.<Test: int x> = $i3;
    goto label1;
 label2:
    $i1 = r1.<Test: int x>;
    if $i1 == 10 \text{ qoto label3};
    arcspace $assert 9 = 0;
    staticinvoke <JayHornAssertions: void assertion(boolean)>($assert 9);
                                                                               53/121
 label3:
```

raturn



Data-Flow



4 From Jimple to JayHorn IR

- Intermediate representation similar to Jimple
- But simpler, e.g.:
 - Methods become C-like functions
 - No exceptions

4 From Jimple to JayHorn IR

- Intermediate representation similar to Jimple
- But simpler, e.g.:
 - Methods become C-like functions
 - No exceptions

Main difference:

```
load → pull
store → push
```

```
<Test: void main(java.lang.String[])>
                                                     public class Test {
public static void main(java.lang.String[])
                                                         int x, y;
                                                         public static void main(...) {
    java.lang.String[] r0;
                                                             Test t = new Test();
    Test r1, $r2;
                                                             while (t.x < 10)
    int $i0, $i1, $i2, $i3;
                                                                 t.x++;
    boolean $z0;
                                                             assert(t.x == 10);
    java.lang.AssertionError $r3;
    r0 := @parameter0: java.lang.String[];
    staticinvoke <Test: void <clinit>()>();
    staticinvoke <JayHornAssertions: void <clinit>()>();
    r2 = new Test;
    specialinvoke $r2.<Test: void <init>()>();
    $helper1 = <JayHornAssertions: java.lang.Throwable lastExceptionThrown>;
    $assert 11 = $helper1 == null;
    staticinvoke <JayHornAssertions: void assertion(boolean)>($assert 11);
    r1 = r2;
 label1:
    $i0 = r1.<Test: int x>;
    if $i0 >= 10 \text{ qoto label2};
    $i2 = r1.<Test: int x>;
    $i3 = $i2 + 1;
    r1.<Test: int x> = $i3;
    goto label1;
 label2:
    $i1 = r1.<Test: int x>;
    if $i1 == 10 goto label3;
    arcspace $assert 9 = 0;
    staticinvoke <JayHornAssertions: void assertion(boolean)>($assert_9);
                                                                                57/121
 label3:
```

```
<Test: void main(java.lang.String[])>
                                                     public class Test {
public static void main(java.lang.String[])
                                                          int x, y;
                                                          public static void main(...) {
    java.lang.String[] r0;
                                                              Test t = new Test();
    Test r1, $r2;
                                                              while (t.x < 10)
    int $i0, $i1, $i2, $i3;
                                                                  t.x++;
    boolean $z0;
                                                              assert(t.x == 10);
    java.lang.AssertionError $r3;
    r0 := @parameter0: java.lang.String[];
    staticinvoke <Test: void <clinit>()>();
    staticinvoke <JayHornAssertions: void <clinit>()>();
    r2 = new Test;
    specialinvoke $r2.<Test: void <init>()>();
    $helper1 = <JayHornAssertions: java.lang.Throwable lastExceptionThrown>;
    $assert 11 = $helper1 == null;
    staticinvoke <JayHornAssertions: void assertion(boolean)>($assert 11);
    r1 = r2;
 label1:
    $i0 = r1.<Test: int x>;
    if $i0 >= 10 \text{ goto label2};
    $i2 = r1.<Test: int x>;
    $i3 = $i2 + 1;
    r1.<Test: int x> = $i3;
    goto label1;
 label2:
    $i1 = r1.<Test: int x>;
    if $i1 == 10 \text{ goto label3};
    arcspace $assert 9 = 0;
    staticinvoke <JayHornAssertions: void assertion(boolean)>($assert_9);
                                                                                 58/121
 label3:
```

```
<Test: void main(java.lang.String[])>
                                                     public class Test {
public static void main(java.lang.String[])
                                                         int x, y;
                                                         public static void main(...) {
    java.lang.String[] r0;
                                                             Test t = new Test();
    Test r1, $r2;
                                                             while (t.x < 10)
    int $i0, $i1, $i2, $i3;
                                                                 t.x++;
    boolean $z0;
                                                             assert(t.x == 10);
    java.lang.AssertionError $r3;
    r0 := @parameter0: java.lang.String[];
    staticinvoke <Test: void <clinit>()>();
    staticinvoke <JayHornAssertions: void <clinit>()>();
    r2 = new Test;
    specialinvoke $r2.<Test: void <init>()>();
    $helper1 = <JayHornAssertions: java.lang.Throwable lastExceptionThrown>;
    $assert 11 = $helper1 == null;
    staticinvoke <JayHornAssertions: void assertion(boolean)>($assert 11);
    r1 = r2;
 label1:
                                        r1 x, r1 y := pull(Test, r1)
    $i0 = r1.<Test: int x>;
                                        $i0 := r1 x
    if $i0 >= 10 \text{ goto label2};
    $i2 = r1.<Test: int x>;
    $i3 = $i2 + 1;
    r1.<Test: int x> = $i3;
    goto label1;
 label2:
    $i1 = r1.<Test: int x>;
    if $i1 == 10 \text{ goto label3};
    arcspace $assert 9 = 0;
    staticinvoke <JayHornAssertions: void assertion(boolean)>($assert_9);
                                                                                59/121
 label3:
```

```
<Test: void main(java.lang.String[])>
                                                    public class Test {
public static void main(java.lang.String[])
                                                        int x, y;
                                                        public static void main(...) {
    java.lang.String[] r0;
                                                            Test t = new Test();
    Test r1, $r2;
                                                            while (t.x < 10)
    int $i0, $i1, $i2, $i3;
                                                                t.x++;
    boolean $z0;
                                                            assert(t.x == 10);
    java.lang.AssertionError $r3;
    r0 := @parameter0: java.lang.String[];
    staticinvoke <Test: void <clinit>()>();
    staticinvoke <JayHornAssertions: void <clinit>()>();
    r2 = new Test;
    specialinvoke $r2.<Test: void <init>()>();
    $helper1 = <JayHornAssertions: java.lang.Throwable lastExceptionThrown>;
    $assert 11 = $helper1 == null;
    staticinvoke <JayHornAssertions: void assertion(boolean)>($assert 11);
    r1 = r2;
 label1:
                                       r1_x, r1_y := pull(Test, r1)
    $i0 = r1.<Test: int x>;
                                       $i0 := r1 x
    if $i0 >= 10  goto label2;
    $i2 = r1.<Test: int x>;
                                       r1_x, r1_y := pull(Test, r1)
    $i3 = $i2 + 1;
                                       r1 x := $i3
    r1.<Test: int x> = $i3;
    goto label1;
                                       push(Test, r1, [r1_x, r1_y])
 label2:
    $i1 = r1.<Test: int x>;
    if $i1 == 10 \text{ goto label3};
    arcspace $assert 9 = 0;
    staticinvoke <JayHornAssertions: void assertion(boolean)>($assert_9);
                                                                               60/121
 label3:
```

```
<Test: void main(java.lang.String[])>
                                                     public class Test {
public static void main(java.lang.String[])
                                                         int x, y;
                                                         public static void main(...) {
    java.lang.String[] r0;
                                                             Test t = new Test();
    Test r1, $r2;
                                                              while (t.x < 10)
    int $i0, $i1, $i2, $i3;
                                                                  t.x++;
    boolean $z0;
                                                              assert(t.x == 10);
    java.lang.AssertionError $r3;
    r0 := @parameter0: java.lang.String[];
    staticinvoke <Test: void <clinit>()>();
    staticinvoke <JayHornAssertions: void <clinit>()>();
    r2 = new Test;
    specialinvoke $r2.<Test: void <ini havoc(r1 x, r1 y)</pre>
    $helper1 = <JayHornAssertions: javassume inv_Test(r1, r1_x, r1_y)</pre>
    $assert 11 = $helper1 == null;
    staticinvoke <JayHornAssertions: \[\begin{align*}
\text{----}
\]
    r1 = r2;
 label1:
                                        r1_x, r1_y := pull(Test, r1)
    $i0 = r1.<Test: int x>;
                                        $i0 := r1 x
    if $i0 >= 10 \text{ goto label2};
    $i2 = r1.<Test: int x>;
                                        r1_x, r1_y := pull(Test, r1)
    $i3 = $i2 + 1;
                                        r1 x := $i3
    r1.<Test: int x> = $i3;
    goto label1;
                                        push(Test, r1, [r1_x, r1_y])
 label2:
    $i1 = r1.<Test: int x>;
    if $i1 == 10 goto label3;
    arcspace $assert 9 = 0;
    staticinvoke <JayHornAssertions: void assertion(boolean)>($assert_9);
                                                                                61/121
 label3:
```

```
<Test: void main(java.lang.String[])>
                                                       public class Test {
public static void main(java.lang.String[])
                                                           int x, y;
                                                           public static void main(...) {
    java.lang.String[] r0;
                                                               Test t = new Test();
    Test r1, $r2;
                                                               while (t.x < 10)
    int $i0, $i1, $i2, $i3;
                                                                   t.x++;
    boolean $z0;
                                                               assert(t.x == 10);
    java.lang.AssertionError $r3;
    r0 := @parameter0: java.lang.String[];
    staticinvoke <Test: void <clinit>()>();
    staticinvoke <JayHornAssertions: void <clinit>()>();
    r2 = new Test;
    specialinvoke $r2.<Test: void <ini havoc(r1 x, r1_y)</pre>
    $helper1 = <JayHornAssertions: javassume inv_Test(r1, r1_x, r1_y)</pre>
    $assert 11 = $helper1 == null;
    staticinvoke <JayHornAssertions: \[\begin{align*}
\text{----}
\]
    r1 = r2;
 label1:
                                         r1_x, r1_y := pull(Test, r1)
    $i0 = r1.<Test: int x>;
                                         $i0 := r1 x
    if $i0 >= 10 \text{ goto label2};
    $i2 = r1.<Test: int x>;
                                         r1_x, r1_y := pull(Test, r1)
    $i3 = $i2 + 1;
                                         r1 x := $i3
    r1.<Test: int x> = $i3;
    goto label1;
                                         push(Test, r1, [r1_x, r1_y])
 label2:
    $i1 = r1.<Test: int x>;
    if $i1 == 10 goto label3;
                                         [...]
    arcspace $assert 9 = 0;
                                         assert inv Test(r1, r1 x, r1 y)
    staticinvoke <JayHornAssertions: <a href="mailto:void assertion">void assertion(bootean)>($assert_9);</a>
 label3:
```

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(5) JayHorn IR to Horn Clauses

Three kinds of predicates:

- State invariants loc_l
 for every control location l
 → like in Ex 1
- Pre-/post-conditions pre_m, post_m for every method m
 → like in Ex 2
- Class/instance invariants inv_C for every class C

JayHorn IR Instructions

• assert phi

$$loc_l(\ldots,x,\ldots) \to loc_{l'}(\ldots,t,\ldots)$$

$$\phi \wedge loc_l(\ldots) \rightarrow loc_{l'}(\ldots)$$

$$loc_l(\ldots) \to loc_{l'}(\ldots)$$
$$\neg \phi \land loc_l(\ldots) \to false$$

JayHorn IR Instructions

$$loc_l(\ldots,x,\ldots) \to loc_{l'}(\ldots,t,\ldots)$$

assume phi

$$\phi \wedge loc_l(\ldots) \rightarrow loc_{l'}(\ldots)$$

• assert phi

$$loc_l(\ldots) \to loc_{l'}(\ldots)$$
$$\neg \phi \land loc_l(\ldots) \to false$$

$$loc_l(\ldots) \wedge inv_C(\ldots) \rightarrow loc_{l'}(\ldots)$$

$$loc_l(\ldots) \to loc_{l'}(\ldots)$$

 $loc_l(\ldots) \to inv_C(\ldots)$

JayHorn IR Instructions

$$loc_l(\ldots,x,\ldots) \to loc_{l'}(\ldots,t,\ldots)$$

$$\phi \wedge loc_l(\ldots) \rightarrow loc_{l'}(\ldots)$$

$$loc_{l}(\ldots) \to loc_{l'}(\ldots)$$
$$\neg \phi \land loc_{l}(\ldots) \to false$$

$$loc_l(\ldots) \wedge inv_C(\ldots) \rightarrow loc_{l'}(\ldots)$$

$$loc_l(\ldots) \to loc_{l'}(\ldots)$$

 $loc_l(\ldots) \to inv_C(\ldots)$

In the Example

```
public class Test {
   int x, y;
   public static void main(String[] args) {
       Test t = new Test();
       while (t.x < 10)
            t.x++;
       assert(t.x == 10);
   }
}</pre>
```

```
public class Test {
    int x, y;
    public static void main(String[] args) {
        Test t = new Test();
        while (t.x < 10)
            t.x++;
        assert(t.x == 10);
```

```
public class Test {
    int x, y;
    public static void main(String[] args) {
         Test t = new Test();
         while (t.x < 10)
                                  x \subseteq [0, 10] \Longrightarrow
             t.x++;
                                   inv Test(t, x, y)
         assert(t.x == 10);
```

```
public class Test {
    int x, y;
    public static void main(String[] args) {
         Test t = new Test();
         while (t.x < 10)
                                  x \subseteq [0, 10] \Longrightarrow
             t.x++;
                                   inv Test(t, x, y)
         assert(t.x == 10);
```

inv Test(t, x, y) will be too weak to prove the assertion

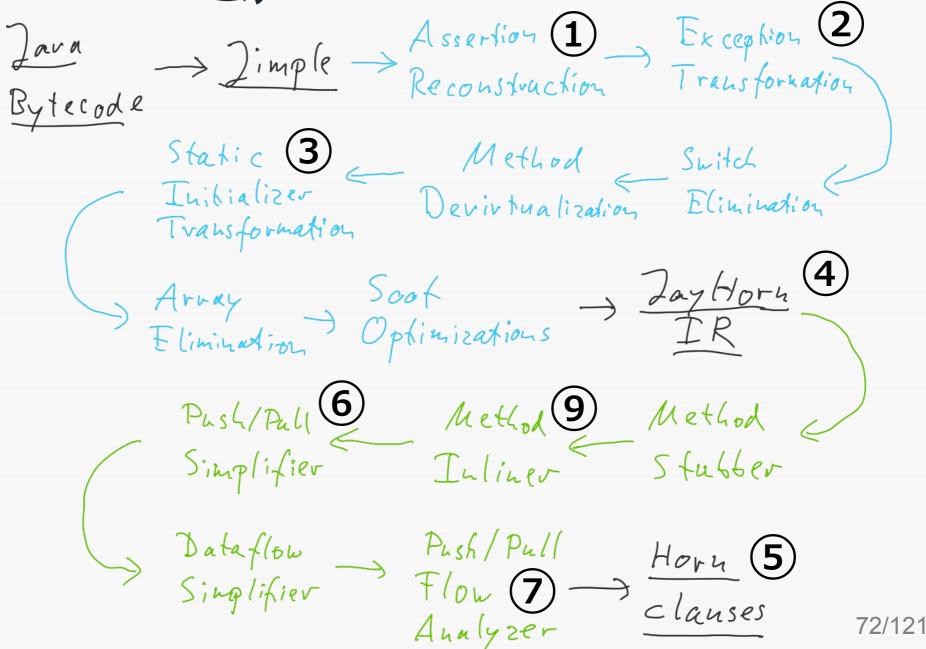
```
public class Test {
    int x, y;
    public static void main(String[] args) {
        Test t = new Test();
        while (t.x < 10)
                                  x \subseteq [0, 10] \Longrightarrow
             t.x++;
                                  inv Test(t, x, y)
        assert(x) = (x);
```

NB: loop condition does not help, since state invariants only see local variables

inv Test(t, x, y) will be too weak to prove the assertion



Data-Flow



```
<Test: void main(java.lang.String[])>
                                                    public class Test {
public static void main(java.lang.String[])
                                                        int x, y;
                                                        public static void main(...) {
    java.lang.String[] r0;
                                                            Test t = new Test();
    Test r1, $r2;
                                                            while (t.x < 10)
    int $i0, $i1, $i2, $i3;
                                                                t.x++;
    boolean $z0;
                                                            assert(t.x == 10);
    java.lang.AssertionError $r3;
    r0 := @parameter0: java.lang.String[];
    staticinvoke <Test: void <clinit>()>();
    staticinvoke <JayHornAssertions: void <clinit>()>();
    r2 = new Test;
    specialinvoke $r2.<Test: void <init>()>();
    $helper1 = <JayHornAssertions: java.lang.Throwable lastExceptionThrown>;
    $assert 11 = $helper1 == null;
    staticinvoke <JayHornAssertions: void assertion(boolean)>($assert 11);
    r1 = r2;
 label1:
    r1_x, r1_y := pull(Test, r1)
    $i0 := r1 x
    if $i0 \ge 10 goto label2;
    r1 x, r1 y := pull(Test, r1)
    $i2 := r1 x
    $i3 = $i2 + 1;
    r1 x, r1 y := pull(Test, r1)
    r1 x := $i3
    push(Test, r1, [r1_x, r1_y])
    goto label1;
 label2:
```

 $[\ldots]$

```
<Test: void main(java.lang.String[])>
                                                   public class Test {
public static void main(java.lang.String[])
                                                       int x, y;
                                                       public static void main(...) {
    java.lang.String[] r0;
                                                           Test t = new Test();
    Test r1, $r2;
                                                           while (t.x < 10)
    int $i0, $i1, $i2, $i3;
                                                               t.x++;
    boolean $z0;
                                                           assert(t.x == 10);
    java.lang.AssertionError $r3;
    r0 := @parameter0: java.lang.String[];
    staticinvoke <Test: void <clinit>()>();
    staticinvoke <JayHornAssertions: void <clinit>()>();
    r2 = new Test;
    specialinvoke $r2.<Test: void <init>()>();
    $helper1 = <JayHornAssertions: java.lang.Throwable lastExceptionThrown>;
    $assert 11 = $helper1 == null;
    staticinvoke <JayHornAssertions: void assertion(boolean)>($assert 11);
    r1 = r2;
 label1:
    r1_x, r1_y := pull(Test, r1)
    si0 := r1 x
    if $i0 >= 10 goto label2;
                                        Move pulls upward
    r1 x, r1 y := pull(Test, r1)
                                        and pushes downward (6)
    $i2 := r1 x
    $i3 = $i2 + 1;
                                        in the program
    r1 x, r1 y := pull(Test, r1)
    r1 x := $i3
    push(Test, r1, [r1_x, r1_y])
    goto label1;
 label2:
    [\ldots]
```

```
<Test: void main(java.lang.String[])>
                                                    public class Test {
public static void main(java.lang.String[])
                                                        int x, y;
                                                        public static void main(...) {
    java.lang.String[] r0;
                                                            Test t = new Test();
    Test r1, $r2;
                                                            while (t.x < 10)
    int $i0, $i1, $i2, $i3;
                                                                t.x++;
    boolean $z0;
                                                            assert(t.x == 10);
    java.lang.AssertionError $r3;
    r0 := @parameter0: java.lang.String[];
    staticinvoke <Test: void <clinit>()>();
    staticinvoke <JayHornAssertions: void <clinit>()>();
    r2 = new Test;
    specialinvoke $r2.<Test: void <init>()>();
    $helper1 = <JayHornAssertions: java.lang.Throwable lastExceptionThrown>;
    $assert 11 = $helper1 == null;
    staticinvoke <JayHornAssertions: void assertion(boolean)>($assert 11);
    r1 = r2;
                                        label1:
 label1:
    r1_x, r1_y := pull(Test, r1)
                                          r1 x, r1 y := pull(Test, r1)
                                          $i0 := r1 x
    $i0 := r1 x
    if $i0 >= 10 goto label2;
                                          if $i0 >= 10 goto label2;
    r1 x, r1 y := pull(Test, r1)
                                          r1 x, r1 y := pull(Test, r1)
                                          i2 := r1 x
    $i2 := r1 x
                                          $i3 = $i2 + 1;
    $i3 = $i2 + 1;
                                          r1_x, r1_y := pull(Test, r1)
    r1 x, r1 y := pull(Test, r1)
                                          r1 x := $i3
    r1 x := $i3
                                          push(Test, r1, [r1 x, r1 y])
    push(Test, r1, [r1_x, r1_y])
                                          goto label1;
    goto label1;
 label2:
```

 $[\ldots]$

```
<Test: void main(java.lang.String[])>
                                                    public class Test {
public static void main(java.lang.String[])
                                                        int x, y;
                                                        public static void main(...) {
    java.lang.String[] r0;
                                                            Test t = new Test();
    Test r1, $r2;
                                                            while (t.x < 10)
    int $i0, $i1, $i2, $i3;
                                                                t.x++;
    boolean $z0;
                                                            assert(t.x == 10);
    java.lang.AssertionError $r3;
    r0 := @parameter0: java.lang.String[];
    staticinvoke <Test: void <clinit>()>();
    staticinvoke <JayHornAssertions: void <clinit>()>();
    r2 = new Test;
    specialinvoke $r2.<Test: void <init>()>();
    $helper1 = <JayHornAssertions: java.lang.Throwable lastExceptionThrown>;
    $assert 11 = $helper1 == null;
    staticinvoke <JayHornAssertions: void assertion(boolean)>($assert 11);
    r1 = r2;
 label1:
                                        label1:
    r1_x, r1_y := pull(Test, r1)
                                          r1 x, r1 y := pull(Test, r1)
    $i0 := r1 x
                                          $i0 := r1 x
    if $i0 >= 10 goto label2;
                                          if $i0 >= 10 goto label2;
    r1 x, r1 y := pull(Test, r1)
                                          r1 x, r1 y := pull(Test, r1)
                                          i2 := r1 x
    $i2 := r1 x
                                          r1_x, r1_y := pull(Test, r1)
    $i3 = $i2 + 1;
    r1 x, r1 y := pull(Test, r1)
                                          $i3 = $i2 + 1;
                                          r1 x := $i3
    r1 x := $i3
                                          push(Test, r1, [r1 x, r1 y])
    push(Test, r1, [r1_x, r1_y])
                                          goto label1;
    goto label1;
```

label2:

```
<Test: void main(java.lang.String[])>
                                                    public class Test {
public static void main(java.lang.String[])
                                                        int x, y;
                                                        public static void main(...) {
    java.lang.String[] r0;
                                                            Test t = new Test();
    Test r1, $r2;
                                                            while (t.x < 10)
    int $i0, $i1, $i2, $i3;
                                                                t.x++;
    boolean $z0;
                                                            assert(t.x == 10);
    java.lang.AssertionError $r3;
    r0 := @parameter0: java.lang.String[];
    staticinvoke <Test: void <clinit>()>();
    staticinvoke <JayHornAssertions: void <clinit>()>();
    r2 = new Test;
    specialinvoke $r2.<Test: void <init>()>();
    $helper1 = <JayHornAssertions: java.lang.Throwable lastExceptionThrown>;
    $assert 11 = $helper1 == null;
    staticinvoke <JayHornAssertions: void assertion(boolean)>($assert 11);
    r1 = r2;
                                        label1:
 label1:
    r1_x, r1_y := pull(Test, r1)
                                          r1 x, r1 y := pull(Test, r1)
                                          $i0 := r1_x
    $i0 := r1 x
    if $i0 >= 10 goto label2;
                                          if $i0 >= 10 goto label2;
    r1 x, r1 y := pull(Test, r1)
                                          r1 x, r1 y := pull(Test, r1)
                                          r1 x', r1 y := pull(Test, r1)
    $i2 := r1 x
                                          $i2 := r1 x
    $i3 = $i2 + 1;
    r1_x, r1_y := pull(Test, r1)
                                          $i3 = $i2 + 1;
                                          r1 x := $i3
    r1 x := $i3
                                          push(Test, r1, [r1 x, r1 y])
    push(Test, r1, [r1_x, r1_y])
                                          goto label1;
    goto label1;
 label2:
```

 $[\ldots]$

```
<Test: void main(java.lang.String[])>
                                                    public class Test {
public static void main(java.lang.String[])
                                                        int x, y;
                                                        public static void main(...) {
    java.lang.String[] r0;
                                                            Test t = new Test();
    Test r1, $r2;
                                                            while (t.x < 10)
    int $i0, $i1, $i2, $i3;
                                                                t.x++;
    boolean $z0;
                                                            assert(t.x == 10);
    java.lang.AssertionError $r3;
    r0 := @parameter0: java.lang.String[];
    staticinvoke <Test: void <clinit>()>();
    staticinvoke <JayHornAssertions: void <clinit>()>();
    r2 = new Test;
    specialinvoke $r2.<Test: void <init>()>();
    $helper1 = <JayHornAssertions: java.lang.Throwable lastExceptionThrown>;
    $assert 11 = $helper1 == null;
    staticinvoke <JayHornAssertions: void assertion(boolean)>($assert 11);
    r1 = r2;
 label1:
                                        label1:
    r1_x, r1_y := pull(Test, r1)
                                          r1 x, r1 y := pull(Test, r1)
                                          $i0 := r1_x
    $i0 := r1 x
    if $i0 >= 10 goto label2;
                                          if $i0 >= 10 goto label2;
    r1 x, r1 y := pull(Test, r1)
                                          r1 x, r1 y := pull(Test, r1)
                                          r1 x' := r1 x; r1 y := r1 y
    $i2 := r1 x
                                          $i2 := r1 x
    $i3 = $i2 + 1;
    r1 x, r1 y := pull(Test, r1)
                                          $i3 = $i2 + 1;
                                          r1 x := $i3
    r1 x := $i3
                                          push(Test, r1, [r1 x, r1 y])
    push(Test, r1, [r1_x, r1_y])
                                          goto label1;
    goto label1;
 label2:
```

 $[\ldots]$

```
<Test: void main(java.lang.String[])>
                                                    public class Test {
public static void main(java.lang.String[])
                                                        int x, y;
                                                        public static void main(...) {
    java.lang.String[] r0;
                                                            Test t = new Test();
    Test r1, $r2;
                                                            while (t.x < 10)
    int $i0, $i1, $i2, $i3;
                                                                t.x++;
    boolean $z0;
                                                            assert(t.x == 10);
    java.lang.AssertionError $r3;
    r0 := @parameter0: java.lang.String[];
    staticinvoke <Test: void <clinit>()>();
    staticinvoke <JayHornAssertions: void <clinit>()>();
    r2 = new Test;
    specialinvoke $r2.<Test: void <init>()>();
    $helper1 = <JayHornAssertions: java.lang.Throwable lastExceptionThrown>;
    $assert 11 = $helper1 == null;
    staticinvoke <JayHornAssertions: void assertion(boolean)>($assert 11);
    r1 = r2;
 label1:
                                        label1:
    r1_x, r1_y := pull(Test, r1)
                                          r1 x, r1 y := pull(Test, r1)
                                          $i0 := r1 x
    $i0 := r1 x
    if $i0 >= 10 goto label2;
                                          if $i0 >= 10 goto label2;
    r1 x, r1 y := pull(Test, r1)
                                          r1 x, r1 y := pull(Test, r1)
    $i2 := r1 x
    $i3 = $i2 + 1;
                                          $i2 := r1 x
    r1 x, r1 y := pull(Test, r1)
                                          $i3 = $i2 + 1;
                                          r1 x := $i3
    r1 x := $i3
                                          push(Test, r1, [r1 x, r1 y])
    push(Test, r1, [r1_x, r1_y])
                                          goto label1;
    goto label1;
```

label2:

```
<Test: void main(java.lang.String[])>
                                                    public class Test {
public static void main(java.lang.String[])
                                                        int x, y;
                                                        public static void main(...) {
    java.lang.String[] r0;
                                                            Test t = new Test();
    Test r1, $r2;
                                                            while (t.x < 10)
    int $i0, $i1, $i2, $i3;
                                                                t.x++;
    boolean $z0;
                                                            assert(t.x == 10);
    java.lang.AssertionError $r3;
    r0 := @parameter0: java.lang.String[];
    staticinvoke <Test: void <clinit>()>();
    staticinvoke <JayHornAssertions: void <clinit>()>();
    r2 = new Test;
    specialinvoke $r2.<Test: void <init>()>();
    $helper1 = <JayHornAssertions: java.lang.Throwable lastExceptionThrown>;
    $assert 11 = $helper1 == null;
    staticinvoke <JayHornAssertions: void assertion(boolean)>($assert 11);
    r1 = r2;
 label1:
                                        label1:
    r1_x, r1_y := pull(Test, r1)
                                          r1 x, r1 y := pull(Test, r1)
                                          $i0 := r1 x
    $i0 := r1 x
    if $i0 >= 10 goto label2;
                                          if $i0 >= 10 goto label2;
    r1 x, r1 y := pull(Test, r1)
                                          r1 x, r1 y := pull(Test, r1)
    $i2 := r1 x
    $i3 = $i2 + 1;
                                          $i2 := r1 x
    r1 x, r1 y := pull(Test, r1)
                                          $i3 = $i2 + 1;
                                          r1 x := $i3
    r1 x := $i3
                                          push(Test, r1, [r1 x, r1 y])
    push(Test, r1, [r1_x, r1_y])
                                          goto label1;
    goto label1;
```

label2:

```
<Test: void main(java.lang.String[])>
                                                    public class Test {
public static void main(java.lang.String[])
                                                         int x, y;
                                                         public static void main(...) {
    java.lang.String[] r0;
                                                            Test t = new Test();
    Test r1, $r2;
                                                            while (t.x < 10)
    int $i0, $i1, $i2, $i3;
                                                                t.x++;
    boolean $z0;
                                                            assert(t.x == 10);
    java.lang.AssertionError $r3;
    r0 := @parameter0: java.lang.String[];
    staticinvoke <Test: void <clinit>()>();
    staticinvoke <JayHornAssertions: void <clinit>()>();
    r2 = new Test;
    specialinvoke $r2.<Test: void <init>()>();
    $helper1 = <JayHornAssertions: java.lang.Throwable lastExceptionThrown>;
    $assert 11 = $helper1 == null;
    staticinvoke <JayHornAssertions: void assertion(boolean)>($assert 11);
    r1 = r2;
                                        label1:
 label1:
    r1_x, r1_y := pull(Test, r1)
                                          r1 x, r1 y := pull(Test, r1)
    $i0 := r1 x
                                          $i0 := r1 x
    if $i0 >= 10 goto label2;
                                          r1 x, r1 y := pull(Test, r1)
    r1 x, r1 y := pull(Test, r1)
                                          if $i0 \ge 10 goto label2;
    $i2 := r1 x
    $i3 = $i2 + 1;
                                          $i2 := r1 x
                                          $i3 = $i2 + 1;
    r1 x, r1 y := pull(Test, r1)
                                          r1 x := $i3
    r1 x := $i3
    push(Test, r1, [r1_x, r1_y])
                                          push(Test, r1, [r1 x, r1 y])
                                          goto label1;
    goto label1;
 label2:
```

 $[\ldots]$

```
<Test: void main(java.lang.String[])>
                                                    public class Test {
public static void main(java.lang.String[])
                                                         int x, y;
                                                         public static void main(...) {
    java.lang.String[] r0;
                                                            Test t = new Test();
    Test r1, $r2;
                                                            while (t.x < 10)
    int $i0, $i1, $i2, $i3;
                                                                t.x++;
    boolean $z0;
                                                            assert(t.x == 10);
    java.lang.AssertionError $r3;
    r0 := @parameter0: java.lang.String[];
    staticinvoke <Test: void <clinit>()>();
    staticinvoke <JayHornAssertions: void <clinit>()>();
    r2 = new Test;
    specialinvoke $r2.<Test: void <init>()>();
    $helper1 = <JayHornAssertions: java.lang.Throwable lastExceptionThrown>;
    $assert 11 = $helper1 == null;
    staticinvoke <JayHornAssertions: void assertion(boolean)>($assert 11);
    r1 = r2;
                                        label1:
 label1:
    r1_x, r1_y := pull(Test, r1)
                                          r1 x, r1 y := pull(Test, r1)
    si0 := r1 x
                                          $i0 := r1 x
    if $i0 >= 10 goto label2;
                                          r1 x, r1 y := pull(Test, r1)
    r1 x, r1 y := pull(Test, r1)
                                          if $i0 \ge 10 goto label2;
    $i2 := r1 x
    $i3 = $i2 + 1;
                                          $i2 := r1 x
                                          $i3 = $i2 + 1;
    r1 x, r1 y := pull(Test, r1)
                                          r1 x := $i3
    r1 x := $i3
    push(Test, r1, [r1_x, r1_y])
                                          push(Test, r1, [r1 x, r1 y])
                                          goto label1;
    goto label1;
 label2:
```

 $[\ldots]$

```
<Test: void main(java.lang.String[])>
                                                    public class Test {
public static void main(java.lang.String[])
                                                        int x, y;
                                                        public static void main(...) {
    java.lang.String[] r0;
                                                            Test t = new Test();
    Test r1, $r2;
                                                            while (t.x < 10)
    int $i0, $i1, $i2, $i3;
                                                                t.x++;
    boolean $z0;
                                                            assert(t.x == 10);
    java.lang.AssertionError $r3;
    r0 := @parameter0: java.lang.String[];
    staticinvoke <Test: void <clinit>()>();
    staticinvoke <JayHornAssertions: void <clinit>()>();
    r2 = new Test;
    specialinvoke $r2.<Test: void <init>()>();
    $helper1 = <JayHornAssertions: java.lang.Throwable lastExceptionThrown>;
    $assert 11 = $helper1 == null;
    staticinvoke <JayHornAssertions: void assertion(boolean)>($assert 11);
    r1 = r2;
    r1 x, r1 y := pull(Test, r1)
                                     Finally, complete
 label1:
    $i0 := r1 x
                                     computation
    if $i0 >= 10 \text{ qoto label2};
                                     happening on local
    $i2 := r1 x
    $i3 = $i2 + 1;
                                     variables!
    r1 x := $i3
    push(Test, r1, [r1_x, r1_y])
    goto label1;
 label2:
    [\ldots]
```

Push/Pull Simplification Rules

$$(I) \ \, \frac{\operatorname{pull}_{c}(x_{1}, \ldots, x_{n}, p) \ \, \operatorname{pull}_{c}(y_{1}, \ldots, y_{n}, p)}{\operatorname{pull}_{c}(x_{1}, \ldots, x_{n}, p) \ \, y_{1} := x_{1}; \ldots; y_{n} := x_{n}}$$

$$(II) \ \, \frac{\operatorname{push}_{c}(p, t_{1}, \ldots, t_{n}) \ \, \operatorname{push}_{c}(p, s_{1}, \ldots, s_{n})}{\operatorname{push}_{c}(p, s_{1}, \ldots, s_{n})}$$

$$(III) \ \, \frac{\operatorname{push}_{c}(p, t_{1}, \ldots, t_{n}) \ \, \operatorname{pull}_{c}(x_{1}, \ldots, x_{n}, p)}{\operatorname{push}_{c}(p, t_{1}, \ldots, t_{n}) \ \, x_{1} := t_{1}; \ldots x_{n} := t_{n}}$$

$$(IV) \ \, \frac{\operatorname{pull}_{c}(x_{1}, \ldots, x_{n}, p) \ \, \operatorname{push}_{c}(p, x_{1}, \ldots, x_{n})}{\operatorname{pull}_{c}(x_{1}, \ldots, x_{n}, p)}$$

$$(V) \ \, \frac{x := t \ \, \operatorname{pull}_{c}(y_{1}, \ldots, y_{n}, p)}{\operatorname{pull}_{c}(y_{1}, \ldots, y_{n}, p) \ \, x := t} \ \, (VI) \ \, \frac{\operatorname{push}_{c}(p, t_{1}, \ldots, t_{n}) \ \, x := t}{x := t \ \, \operatorname{push}_{c}(p, t_{1}, \ldots, t_{n})}$$

$$(VII) \ \, \frac{\operatorname{push}_{c}(p, t_{1}, \ldots, t_{n}) \ \, \operatorname{pull}_{c}(x_{1}, \ldots, x_{n}, r)}{\operatorname{assert}(p \neq r) \ \, \operatorname{pull}_{c}(x_{1}, \ldots, x_{n}, r) \ \, \operatorname{push}_{c}(p, t_{1}, \ldots, t_{n})}$$

Push/Pull Simplification Rules

(I)
$$\frac{\text{pull}_{c}(x_{1},\ldots,x_{n},p) \text{ pull}_{c}(y_{1},\ldots,y_{n},p)}{\text{pull}_{c}(x_{1},\ldots,x_{n},p) y_{1} := x_{1};\ldots;y_{n} := x_{n}}$$

Assuming distinct sets of variables

(II)
$$\frac{\operatorname{push}_{\mathcal{C}}(p, t_1, \ldots, t_n) \operatorname{push}_{\mathcal{C}}(p, s_1, \ldots, s_n)}{\operatorname{push}_{\mathcal{C}}(p, s_1, \ldots, s_n)}$$

(III)
$$\frac{\operatorname{push}_{\mathcal{C}}(p, t_1, \ldots, t_n); \operatorname{pull}_{\mathcal{C}}(x_1, \ldots, x_n, p)}{\operatorname{push}_{\mathcal{C}}(p, t_1, \ldots, t_n) \ x_1 := t_1; \ldots x_n := t_n}$$

(IV)
$$\frac{\operatorname{pull}_{c}(x_{1},\ldots,x_{n},p) \operatorname{push}_{c}(p,x_{1},\ldots,x_{n})}{\operatorname{pull}_{c}(x_{1},\ldots,x_{n},p)}$$

x not occurring in p, t1, ...

$$(V) \frac{x := t \, \operatorname{pull}_{\mathcal{C}}(y_1, \dots, y_n, p)}{\operatorname{pull}_{\mathcal{C}}(y_1, \dots, y_n, p) \, x := t} \quad (VI) \frac{\operatorname{push}_{\mathcal{C}}(p, t_1, \dots, t_n) \, x := t}{x := t \, \operatorname{push}_{\mathcal{C}}(p, t_1, \dots, t_n)}$$

(VII)
$$\frac{\operatorname{push}_{c}(p, t_{1}, \ldots, t_{n}) \operatorname{pull}_{c}(x_{1}, \ldots, x_{n}, r)}{\operatorname{assert}(p \neq r) \operatorname{pull}_{c}(x_{1}, \ldots, x_{n}, r) \operatorname{push}_{c}(p, t_{1}, \ldots, t_{n})}$$

```
public class FlowSens {
    int x;
    public static void main(String[] args) {
        FlowSens t = new FlowSens();
        t.x = 1;
        if (args.length > 5)
            t.x += 10;
        else
          t.x += 20;
        f(t);
    public static void f(FlowSens t) {
        assert t.x > 1;
```

```
public class FlowSens {
    int x;
    public static void main(String[] args) {
        FlowSens t = new FlowSens(); push(t, 0)
        t.x = 1;
        if (args.length > 5)
            t.x += 10;
        else
          t.x += 20;
        f(t);
    public static void f(FlowSens t) {
        assert t.x > 1;
```

```
public class FlowSens {
    int x;
    public static void main(String[] args) {
        FlowSens t = new FlowSens(); push(t, 0)
        t.x = 1;
                                      push(t, 1)
        if (args.length > 5)
            t.x += 10;
        else
          t.x += 20;
        f(t);
    public static void f(FlowSens t) {
        assert t.x > 1;
```

```
public class FlowSens {
    int x;
    public static void main(String[] args) {
        FlowSens t = new FlowSens(); push(t, 0)
        t.x = 1;
                                       push(t, 1)
        if (args.length > 5)
                                       push(t, 11)
            t.x += 10;
        else
                                       push(t, 21)
          t.x += 20;
        f(t);
    public static void f(FlowSens t) {
        assert t.x > 1;
```

```
public class FlowSens {
    int x;
    public static void main(String[] args) {
        FlowSens t = new FlowSens();
                                      push(t, 0)
        t.x = 1;
                                       push(t, 1)
        if (args.length > 5)
                                       push(t, 11)
            t.x += 10;
        else
                                       push(t, 21)
          t.x += 20;
        f(t);
    public static void f(FlowSens t) {
        assert t.x > 1;
                                       x := pull(t)
```

```
public class FlowSens {
    int x;
    public static void main(String[] args) {
        FlowSens t = new FlowSens();
                                      push 0(t, 0)
                                       push 1(t, 1)
        t.x = 1;
        if (args.length > 5)
                                       push 2(t, 11)
            t.x += 10;
        else
                                       push_3(t, 21)
          t.x += 20;
        f(t);
    public static void f(FlowSens t) {
        assert t.x > 1;
                                       x := pull(t)
```

```
public class FlowSens {
    int x;
    public static void main(String[] args) {
        FlowSens t = new FlowSens();
                                      push 0(t, 0)
                                       push 1(t, 1)
        t.x = 1;
        if (args.length > 5)
                                       push 2(t, 11)
            t.x += 10;
        else
                                       push_3(t, 21)
          t.x += 20;
        f(t);
    public static void f(FlowSens t) {
        assert t.x > 1;
                                     x := pull(t)[2,3]
```

Definition

Statement

$$S = push(p, x)$$

is a (data-)dependency of statement

$$L = x := pull(q)$$

if there is a path from S to L such that

- p and q may alias (on that path);
- there is no further statement push(p', x') on the path such that p and p' must alias.

```
public class FlowSens {
    int x;
    public static void main(String[] args) {
        FlowSens t = new FlowSens();
                                      push 0(t, 0)
                                       push 1(t, 1)
        t.x = 1;
        if (args.length > 5)
                                       push 2(t, 11)
            t.x += 10;
        else
                                       push_3(t, 21)
         t.x += 20;
        f(t);
    public static void f(FlowSens t) {
        assert t.x > 1;
                                     x := pull(t)[2,3]
```

Ghost field to the last push

store the ID of g Flow-Sensitivity (3)

```
public class FlowSens {
    int x; int pushID;
    public static void main(String[] args) {
        FlowSens t = new FlowSens();
                                      push 0(t, 0)
                                       push 1(t, 1)
        t.x = 1;
        if (args.length > 5)
                                       push 2(t, 11)
            t.x += 10;
        else
                                       push_3(t, 21)
          t.x += 20;
        f(t);
    public static void f(FlowSens t) {
        assert t.x > 1;
                                     x := pull(t)[2,3]
```

Ghost field to store the ID of the last push

store the ID of g Flow-Sensitivity (3)

Assign to the ghost field

```
public class FlowSens {
    int x; int pushID;
    public static void main(String[] args) {
        FlowSens t = new FlowSens();
                                      push(t, 0, 0)
        t.x = 1;
                                       push(t, 1, 1)
        if (args.length > 5)
                                       push(t, 11, 2)
            t.x += 10;
        else
                                       push(t, 21, 3)
          t.x += 20;
        f(t);
    public static void f(FlowSens t) {
        assert t.x > 1;
                                     x := pull(t)[2,3]
```

Ghost field to store the ID of the last push

store the ID of g Flow-Sensitivity (3)

Assign to the ghost field

```
public class FlowSens {
    int x; int pushID;
    public static void main(String[] args) {
        FlowSens t = new FlowSens();
                                      push(t, 0, 0)
        t.x = 1;
                                       push(t, 1, 1)
        if (args.length > 5)
                                       push(t, 11, 2)
            t.x += 10;
        else
                                       push(t, 21, 3)
          t.x += 20;
        f(t);
    public static void f(FlowSens t) {
        assert t.x > 1;
                                   x, i := pull(t)
                                   assume i==2
            Check that we
            read right version
```

Ghost field to store the ID of the last push

store the ID of g Flow-Sensitivity (3)

Assign to the ghost field

```
public class FlowSens {
    int x; int pushID;
                                 .ng[] args) {
     Possible class invariant:
                                 is(); push(t, 0, 0)
     pushID == 0 \&\& x == 0
                                       push(t, 1, 1)
     pushID == 1 \&\& x == 1
     pushID == 2 \&\& x > 1
                                       push(t, 11, 2)
     pushID == 3 \&\& x > 1
                                       push(t, 21, 3)
       LIX TH ZU,
        f(t);
    public static void f(FlowSens t) {
        assert t.x > 1;
                                   x, i := pull(t)
                                   assume i==2
            Check that we
            read right version
```

```
01 public static class Node {
02
     final Node next;
     final int data;
03
04
05
     public Node(Node next, int data) {
06
       this.next = next;
07
       this.data = data;
80
     }
09
10
   public static void main(String[] args) {
12
     final int size = 10;
13
     final int[] table = new int[size];
14
     Node l1 = null;
15
     Node 12 = null;
     for (int i=0; i<args.length; i++) {</pre>
16
17
         int d = Integer.parseInt(args[i]);
18
         if (d \ge 0 \&\& d < size) {
19
           l1 = new Node(l1, d);
20
         } else {
21
           12 = \text{new Node}(12, d);
22
23
     }
24
     while (l1 != null) {
25
       table[l1.data] = table[l1.data] + 1;
26
       l1 = l1.next;
27
     }
28 }
```

8 Tupled References

```
01 public static class Node {
02
     final Node next;
     final int data;
03
04
05
     public Node(Node next, int data) {
06
       this.next = next;
07
       this.data = data;
80
09
10
   public static void main(String[] args) {
12
     final int size = 10;
13
     final int[] table = new int[size];
14
     Node l1 = null;
15
     Node 12 = null;
     for (int i=0; i<args.length; i++) {</pre>
16
         int d = Integer.parseInt(args[i]);
17
18
         if (d \ge 0 \&\& d < size) {
19
           l1 = new Node(l1, d);
20
         } else {
21
           12 = \text{new Node}(12, d);
22
23
     }
     while (l1 != null) {
24
25
       table[l1.data] = table[l1.data] + 1;
26
       l1 = l1.next;
27
     }
28 }
```



Need to show absence of ArrayIndexOutOfBoundsE.

```
01 public static class Node {
02
     final Node next;
     final int data;
03
04
05
     public Node(Node next, int data) {
06
       this.next = next;
07
       this.data = data;
80
09
10
   public static void main(String[] args) {
12
     final int size = 10;
13
     final int[] table = new int[size] ;
14
     Node 11 = null;
15
     Node 12 = null;
     for (int i=0; i<args.length; i++) {</pre>
16
         int d = Integer.parseInt(args[i]);
17
18
         if (d \ge 0 \&\& d < size) {
19
           l1 = new Node(l1, d);
20
         } else {
21
           l2 = new Node(l2, d);
22
23
     }
     while (l1 != null) {
24
25
       table[l1.data] = table[l1.data] + 1;
26
       l1 = l1.next;
27
     }
28 }
```



For this, we need an invariant about objects in the l1 list

Need to show absence of ArrayIndexOutOfBoundsE.

```
01 public static class Node {
02
     final Node next;
     final int data;
03
04
05
     public Node(Node next,
                             Idea: we can
06
       this.next = next;
                             distinguish
       this.data = data;
07
80
                             ll and l2
09
                             based on the
10
                             allocation site
   public static void main(
     final int size = 10;
12
                                  [size];
13
     final int[] table = new
14
     Node 11 = null;
15
     Node 12 = null;
16
     for (int i=0; i<args.l_rgth; i++) {
         int d = Integer.parseInt(args[i]);
17
18
         if (d \ge 0 \&\& d \lessdot size) {
19
           l1 = new Node(l1, d);
20
         } else {
21
           l2 = new Node(l2, d);
22
23
24
     while (l1 != null) {
25
       table[l1.data] = table[l1.data] + 1;
26
       l1 = l1.next;
27
     }
28 }
```

8 Tupled References

For this, we need an invariant about objects in the l1 list

Need to show absence of ArrayIndexOutOfBoundsE.

Partitioning of Classes

Redefine references to be tuples of immutable data about objects, e.g.:

- Memory address
- (Dynamic) type
- Allocation site
- Values of immutable fields
- Constructor arguments

Partitioning of Classes

Redefine references to be **tuples of immutable data** about objects, e.g.:

- Memory address
- (Dynamic) type
- Allocation site
- Values of immutable fields
- Constructor arguments

This data becomes visible in state invariants, method contracts, and class invariants!

```
01 public static class Node {
02
     final Node next;
     final int data;
03
04
05
     public Node(Node next, int data) {
06
       this.next = next;
07
       this.data = data;
80
     }
09
10
   public static void main(String[] args) {
12
     final int size = 10;
13
     final int[] table = new int[size];
14
     Node l1 = null;
15
     Node 12 = null;
     for (int i=0; i<args.length; i++) {</pre>
16
17
         int d = Integer.parseInt(args[i]);
18
         if (d \ge 0 \&\& d < size) {
19
           l1 = new Node(l1, d);
20
         } else {
21
           12 = \text{new Node}(12, d);
22
23
     }
24
     while (l1 != null) {
25
       table[l1.data] = table[l1.data] + 1;
26
       l1 = l1.next;
27
     }
28 }
```

8 Tupled References

```
01 public static class Node {
                                                    8) Tupled
02
     final Node next;
     final int data;
03
04
                                                References
05
     public Node(Node next, int data) {
06
       this.next = next;
07
       this.data = data;
80
    }
09
10
  public static void main(String[] args) {
12
     final int size = 10;
13
    final int[] table = new int[size];
14
    Node l1 = null;
15
     Node 12 = null;
    for (int i=0; i<args.length; i++) {</pre>
16
         int d = Integer.parseInt(args[i]);
17
18
         if (d >= 0 \&\& d < size) {
19
          l1 = new Node(l1, d);
20
         } else {
           l2 = new Node(l2, d);
21
22
                           Possible state/loop invariant:
23
     }
                           l1 == null || l1.allocSite == 19
     while (l1 != null) {
24
25
       table[l1.data] = table[l1.data] + 1;
26
      l1 = l1.next;
27
     }
                                                                107/121
28 }
```

```
01 public static class Node {
                                                       Tupled
02
    final Node next;
    final int data;
03
04
    public Node(No Possible class invariant:
05
      this.next = this.allocSite == 19 ==>
06
      this.data = (next == null || next.allocSite == 19) &&
07
80
    }
                   (0 <= data && data < 10)
09
10
  public static void main(String[] args) {
12
    final int size = 10;
13
    final int[] table = new int[size];
14
    Node l1 = null;
15
    Node 12 = null;
    for (int i=0; i<args.length; i++) {</pre>
16
17
         int d = Integer.parseInt(args[i]);
18
         if (d >= 0 \&\& d < size) {
19
          l1 = new Node(l1, d);
20
         } else {
          l2 = new Node(l2, d);
21
22
                           Possible state/loop invariant:
23
    }
                           l1 == null || l1.allocSite == 19
    while (l1 != null) {
24
25
       table[l1.data] = table[l1.data] + 1;
26
      l1 = l1.next;
27
    }
                                                               108/121
28 }
```

```
01 public static class Node {
02
     final Node next;
     final int data;
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     public Node(Node next, int data) {
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       this.next = next;
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       this.data = data;
80
     }
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10
   public static void main(String[] args) {
12
     final int size = 10;
13
     final int[] table = new int[size] ;
14
     Node l1 = null;
15
     Node 12 = null;
     for (int i=0; i<args.length; i++) {</pre>
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         int d = Integer.parseInt(args[i]);
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         } else {
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22
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     while (l1 != null) {
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       table[l1.data] = table[l1.data] + 1;
26
       l1 = l1.next;
27
     }
28 }
```

(8) Tupled References

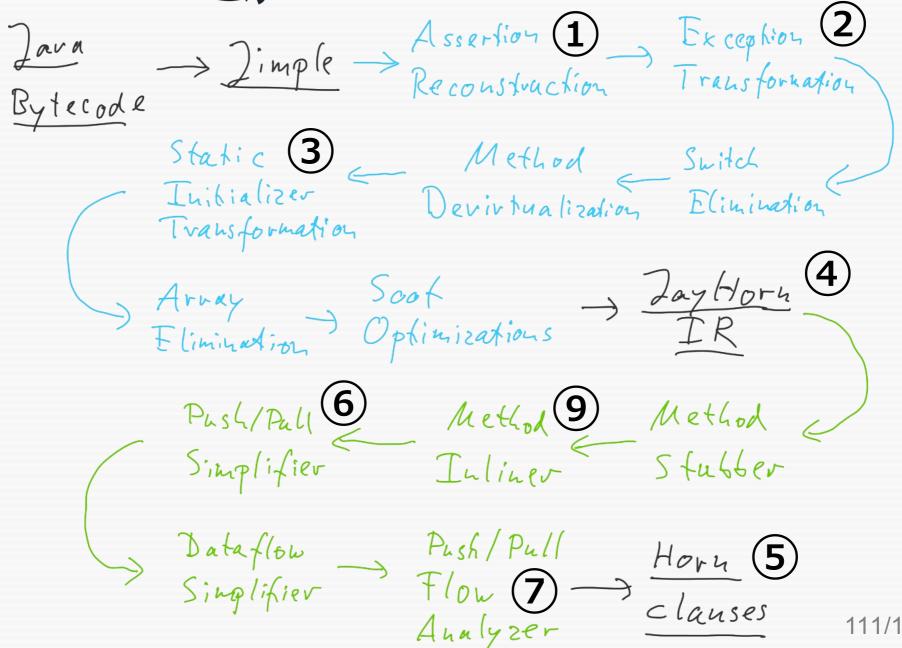
This example at the moment also needs option -inline-size 50

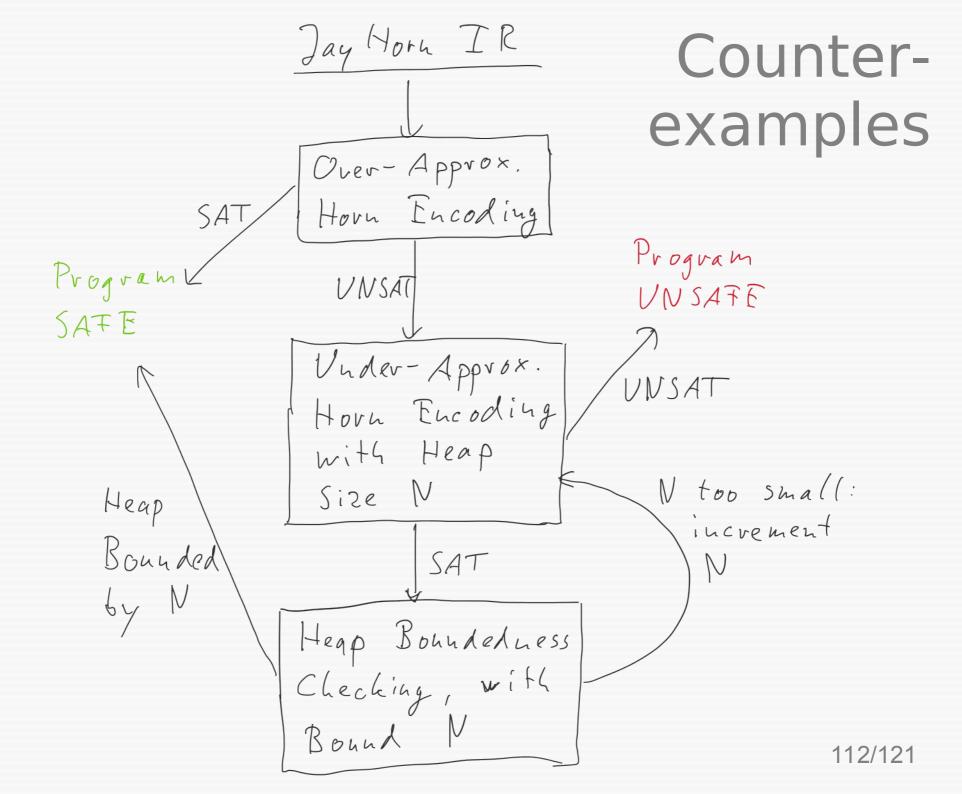
9 Method Inlining

- Simple, but extremely useful
 - Enables more effective push/pull movement (which is intra-proc.)
 - Reduces # of method contracts
- -inline-size <*n*>
 - Inline methods with at most <n>
 statements
- -inline-count <*n*>
 - Inline methods called at most <n> times



Data-Flow







- Sturm und Drang: 2015 2017
 - Intensive implementation period
 - Loads of news ideas

SV-COMP 2018

- Renewed activity: 2018 now
 - Making JayHorn useful ... (ongoing)

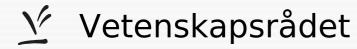
The original JayHorn crowd:

- Core team: Temesghen Kahsai, Rody Kersten, PR, Huascar Sanchez, Martin Schäf
- Contributors:
 Daniel Dietsch, Valentin Wüstholz

Current team (since 2018):

- Main developers:
 Temesghen Kahsai, PR, Martin Schäf
- Contributors: Hossein Hojjat, Ali Shamakhi

Funding













The Next Steps ...

Java Features

- Full support for enums
- Improved array handing
- Sound machine arithmetic handling

Java API modelling

Concurrency

Support for Strings (ongoing)

- Need native Horn solver support:
 - Strings directly, or
 - Algebraic data-types

- Tupled references can be used to get effective value semantics
 - Same for boxed data-types (Integer, etc.)

Reworking the Heap Encoding

- There is also TriCera: the C version of JayHorn
- Idea: Make the heap encoding independent of JayHorn

 Long-term goal: an SMT-LIB theory of heap

Certificates

- JayHorn is a complicated system
 - → to be trusted?

· Idea:

Output JML annotations that can be checked by an independent tool

Case Studies ...



- Constrained Horn Clauses:
 A paradigm to build verifiers
- JayHorn:
 An automatic verifier for Java

- Download and try!
- We are also looking for further contributors!
- https://github.com/jayhorn/jayhorn