

Simulation of Radar Profiles for Satellites Using Mercury Method of Moments

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Abstract

A brief survey of characterizing the three dimensional radar cross section of satellites.

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1 Precís

1.1 Models of Radar Cross Section

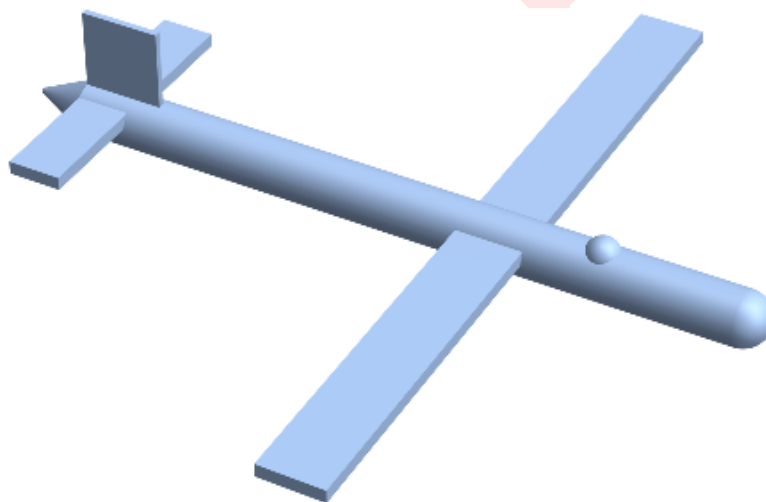


Figure 1: Toy model

Look angle

$$\sigma_{\nu}(\alpha) \approx \frac{a_0}{2} + \sum_{k=1}^d a_k \cos k\alpha + b_k \sin k\alpha \quad (1)$$

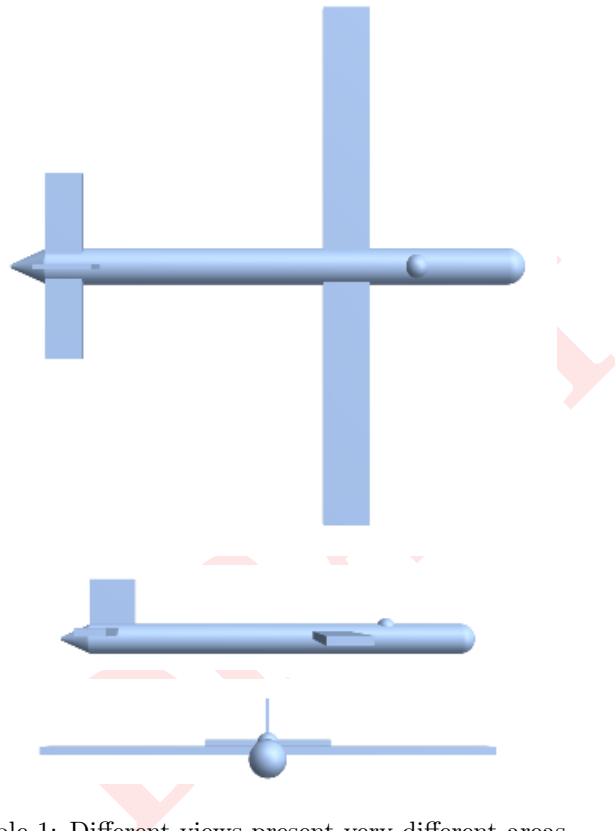
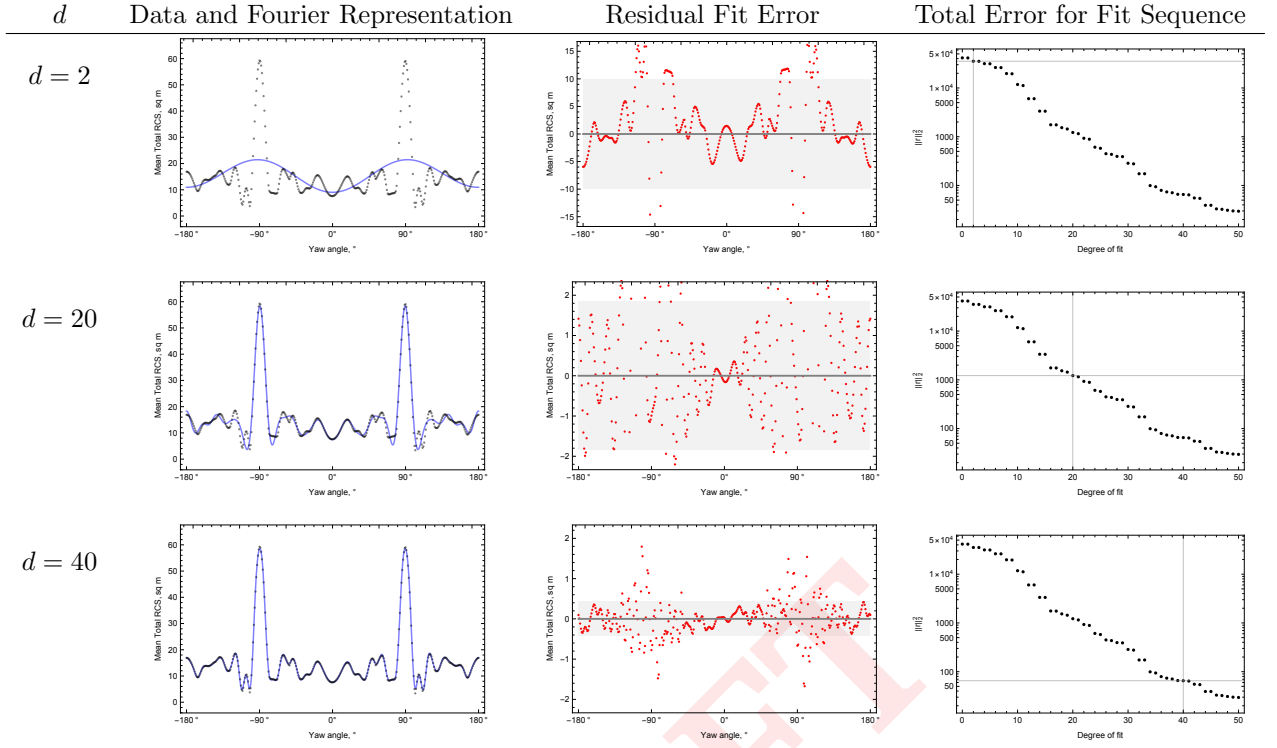


Table 1: Different views present very different areas.



Amplitudes and Errors for $\nu = 3$ MHz and $d = 7$:

$$\sigma_3(\theta) = a_0 + a_1 \cos \theta + a_2 \cos 2\theta + a_3 \cos 3\theta + a_4 \cos 4\theta + a_5 \cos 5\theta + a_6 \cos 6\theta + a_7 \cos 7\theta$$

$$\sigma_3(\theta) = 35.237 \pm 0.012 + (1.675 \pm 0.018) \cos \theta + (-3.434 \pm 0.018) \cos 2\theta + (-0.866 \pm 0.018) \cos 3\theta + (5.386 \pm 0.018) \cos 4\theta + (-1.280 \pm 0.018) \cos 5\theta + (1.379 \pm 0.018) \cos 6\theta + (-0.675 \pm 0.018) \cos 7\theta$$

1.2 Models of Increasing Fidelity

1.3 Running the Code

./MMoM_4.1.12 sample.geo

1.4 Radar

[Topa 2020c] [Topa 2020c] Working with CAF files, producing output, compressing data. Topa 2020d Topa (2020d)

1	Create CAD model	CAD software
2	Convert CAD to *.obj	CAD software
3	Convert *.obj to *.facet	Mathematica, Fortran
4	Input properties to materials.lib	VIM
5	Set radar frequencies	VIM
6	Simulate radar irradiation	Mercury MoM
7	Harvest reflection values from output	Mathematica, Fortran, Python
8	Describe RCS as a series of amplitudes	Not written

Table 2: Start with a CAD model and construct a Radar Cross Section model

1.5 Process

2 Overview: Modeling Radar Cross Section

2.1 Radar

Wave speed equation

$$\lambda\nu = c \quad (2)$$

band	ν	λ
HF	3 – 30 MHz	10 – 1 m
UHF	30 – 300 MHz	0.1 – 0.01 m
VHF	300 – 1000 MHz	0.01 – 0.03 m
L	1 – 2 GHz	30 – 15 mm
S	2 – 4 GHz	15 – 7.5 mm
C	4 – 8 GHz	7.5 – 3.7 mm
X	8 – 12 GHz	3.7 – 2.5 mm
Ku	12 – 18 GHz	2.5 – 1.7 mm
K	18 – 27 GHz	1.7 – 1.1 mm
Ka	27 – 40 GHz	1.1 – 0.75 mm
V	40 – 75 GHz	0.75 – 0.4 mm
W	75 – 110 GHz	0.4 – 0.27 mm
mm	110 – 300 GHz	0.27 – 0.1 mm

Table 3: IEEE Standard Designations for Radar Bands (Bruder et al. 2003).

- (A) Build a CAD model of the satellite (*.cad)
- (B) Seal the CAD mesh
- (C) Create geometry file (*.geo)
- (D) Irradiate object with Mercury MoM
- (E) Harvest backscatter
- (F) Construct RCS
- (G) Resolve RCS measurements into spherical harmonics

2.2 About

- (A) Build a CAD model of the satellite (*.cad)

- (B) Seal the CAD mesh
- (C) Create geometry file (*.geo)
- (D) Irradiate object with Mercury MoM
- (E) Harvest backscatter
- (F) Construct RCS
- (G) Resolve RCS measurements into spherical harmonics

3 File Types

Standard file types

1. *.obj

2. *.txt

Intrinsic file types

1. *.geo

2. *.facet

3.1 Geometry Files *.obj

The geometry files are the primary input to Hg MoM.

- 1. Mathematica: Import/Export format OBJ
- 2. Wikipedia: Wavefront .obj file
- 3. All3DP: The OBJ File Format – Simply Explained

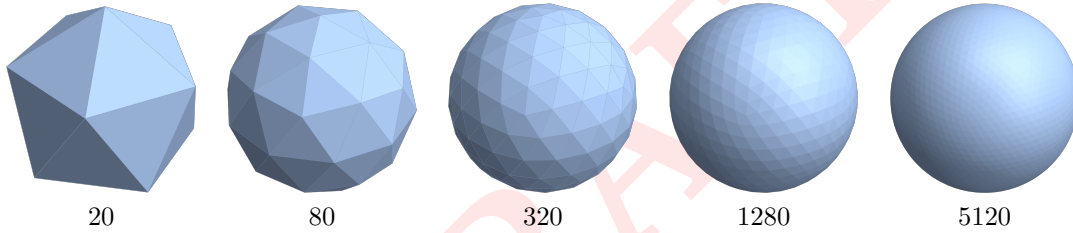


Table 4: A sphere resolved into facets in an *.obj file. The application irradiates each facet and aggregates the output.

Listing 1: The *.obj file for the sphere with 20 facets.

```

1 # Created with the Wolfram Language : www.wolfram.com
2 mtlllib sphere-d050-01.mtl
3
4 # 12 vertex positions
5 v 13.81966018676758 42.53253936767578 22.36067962646484
6 v -13.81966018676758 42.53253936767578 -22.36067962646484
7 v -36.18033981323242 26.28655624389648 22.36067962646484
8 v -36.18033981323242 -26.28655624389648 22.36067962646484
9 v -13.81966018676758 -42.53253936767578 -22.36067962646484
10 v 13.81966018676758 -42.53253936767578 22.36067962646484
11 v 36.18033981323242 26.28655624389648 -22.36067962646484
12 v -44.72135925292969 0 -22.36067962646484
13 v 44.72135925292969 0 22.36067962646484
14 v 36.18033981323242 -26.28655624389648 -22.36067962646484
15 v 0 0 50
16 v 0 0 -50
17
18 # 0 UV coordinates

```

```

19
20 # 0 vertex normals
21
22 # Mesh '' with 20 faces
23 usemtl DefaultMaterial
24 f 1/ 2/ 3/
25 f 4/ 5/ 6/
26 f 2/ 1/ 7/
27 f 4/ 3/ 8/
28 f 9/ 6/ 10/
29 f 3/ 4/ 11/
30 f 2/ 7/ 12/
31 f 3/ 2/ 8/
32 f 2/ 12/ 8/
33 f 12/ 5/ 8/
34 f 7/ 1/ 9/
35 f 5/ 4/ 8/
36 f 6/ 5/ 10/
37 f 5/ 12/ 10/
38 f 12/ 7/ 10/
39 f 7/ 9/ 10/
40 f 4/ 6/ 11/
41 f 6/ 9/ 11/
42 f 9/ 1/ 11/
43 f 1/ 3/ 11/

```

Listing 2: The *.facet file for the sphere with 20 facets.

```

1 facimusFacet.f08 2020-06-25 11:34:36
2
3 <partName>
4 0
5     12
6     13.819660      42.532539      22.360680
7     -13.819660      42.532539     -22.360680
8     -36.180340      26.286556      22.360680
9     -36.180340     -26.286556      22.360680
10    -13.819660     -42.532539     -22.360680
11     13.819660     -42.532539      22.360680
12     36.180340      26.286556     -22.360680
13    -44.721359       0.000000     -22.360680
14     44.721359       0.000000      22.360680
15     36.180340     -26.286556     -22.360680
16     0.000000       0.000000      50.000000
17     0.000000       0.000000     -50.000000
18     1
19 <partName>
20     3      20      0      0      0      0      0
21     1      2      3      0
22     4      5      6      0
23     2      1      7      0
24     4      3      8      0
25     9      6     10      0
26     3      4     11      0
27     2      7     12      0
28     3      2      8      0
29     2     12      8      0
30     12      5      8      0
31     7      1      9      0
32     5      4      8      0
33     6      5     10      0
34     5     12     10      0
35     12      7     10      0
36     7      9     10      0
37     4      6     11      0
38     6      9     11      0
39     9      1     11      0
40     1      3     11      0

```

3.2 New Efforts

4 Running Mercury Method of Moments

4.1 Inputs

Consider an example with the sphere.

Listing 3: “tabula-rasa.geo”

```
1  ego
2
3  !Mercury MoM input file, VIE/SIE Version 4.x compatible (VIE/Dual Sided SIE)
4
5  &MM_MOM
6    bUseACA = .TRUE.,
7    bSolve_ACA = .TRUE.,
8    bOutOfCore = .TRUE.,
9    bNormalizeToWaveLength = .FALSE.,
10   bNormalize = .FALSE.,
11   dCloseLambda = 0.100000,
12   ACA_Factor_Tol = 0.000010,
13   ACA_RHS_Tol = 0.000100,
14   Point_Tolerance = 0.001000,
15   nLargestBlockSize = 400,
16   MemorySize_GB = -1.000000,
17   stackSize_GB = -1.000000,
18   nFillThreads = -1,
19   nFillMKLThreads = 1,
20   nLUThreads = -1,
21   nLUMKLThreads = 1,
22   nRHSThreads = 1,
23   nRHSMKLThreads = 1,
24   bOutputACAGrouping = .FALSE.,
25   bOutputRankFraction = .FALSE.,
26   bLimitLUColumns = .FALSE.,
27   Lop_Admissibility = WEAK,
28   Kop_Admissibility = CLOSE
29 /
30
31 &Scratch_Memory
32   Scratch_RankFraction_Z = 0.300000,
33   Scratch_RankFraction_LU = 0.600000,
34   Scratch_RankFraction_RHS = 0.500000,
35   Scratch_RankFraction_Solve = 1.000000,
36   MemoryFraction_Z = 0.950000,
37   MemoryFraction_Scratch_LU = 0.500000,
38   MemoryFraction_LU = 1.000000,
39   MemoryFraction_RHS = 0.500000,
40   MemoryFraction_Solve = 0.900000,
41 /
42
43 &QUADRATURE
44   NTRISELF = 7,
45   NTRINEAR = 3,
46   NTRIFAR = 3,
47   NTETSELF = 11,
48   NTETNEAR = 4,
49   NTETFAR = 4,
50   NQGAUSS = 4,
51 /
52
53 FREQUENCY
54   mhz
55   nu-mhz nu-mhz 1 !Freq Start, Freq Stop, Number of Frequencies
56
57 Excitation
```



```

58  MONOSTATIC
59
60  Angle Cut
61  1
62  0.000000  359.000000  360
63  AZIMUTH
64  90.000000
65
66  Boundary Conditions
67  PEC-Materials.lib
68  4
69  V_FREE_SPACE => Free_Space
70  V_PEC => PEC
71  V_PMC => PMC
72  V_NULL => NULL
73  1
74  0 BC_PEC V_FREE_SPACE
75
76  SIE
77  myFacet.facet
78  m
79
80  Geometry_End
81
82  ! Fiducial run

```

Listing 4: A simple *.facet file

```

1  facimusFacet.f08  2020-06-25 11:34:36
2
3  <partName>
4  0
5      12
6      13.819660      42.532539      22.360680
7      -13.819660      42.532539      -22.360680
8      -36.180340      26.286556      22.360680
9      -36.180340      -26.286556      22.360680
10     -13.819660      -42.532539      -22.360680
11     13.819660      -42.532539      22.360680
12     36.180340      26.286556      -22.360680
13     -44.721359      0.000000      -22.360680
14     44.721359      0.000000      22.360680
15     36.180340      -26.286556      -22.360680
16     0.000000      0.000000      50.000000
17     0.000000      0.000000      -50.000000
18     1
19  <partName>
20     3      20      0      0      0      0      0
21     1      2      3      0
22     4      5      6      0
23     2      1      7      0
24     4      3      8      0
25     9      6      10     0
26     3      4      11     0
27     2      7      12     0
28     3      2      8      0
29     2      12     8      0
30     12     5      8      0
31     7      1      9      0
32     5      4      8      0
33     6      5      10     0
34     5      12     10     0
35     12     7      10     0
36     7      9      10     0
37     4      6      11     0
38     6      9      11     0
39     9      1      11     0
40     1      3      11     0

```

5 Additional Information

5.1 YouTube Videos

YouTube offers useful didactic presentations and simulations.

1. The Radar cross-section of backscattering objects
2. Basic Concepts of Radar Cross Section (RCS)
3. Mie scattering
4. Mie theory (BME51 Lecture 5)
5. Mie Scattering

5.2 Further Reading

Radar rudiments

1. D. K. Barton and H.R. Ward (1969). *Handbook of Radar Measurement*. New York, NY: Penguin Random House
2. Andrei A. Kolosov (1987). *Over the Horizon Radar*. Artech House. ISBN: 9780890062333. URL: <https://us.artechhouse.com/Over-the-Horizon-Radar-P254.aspx>
3. Peyton Z Peebles (2007). *Radar principles*. John Wiley & Sons

Radar cross section

1. JW Jr Crispin (2013). *Methods of radar cross-section analysis*. Elsevier
2. Allen E Fuhs (1982). *Radar cross section lectures*. Monterey, California, Naval Postgraduate School. URL: <https://calhoun.nps.edu/server/api/core/bitstreams/9e69ec48-4628-4243-9f9b-7e879521f7f8/content>
3. Eugene F Knott, John F Schaeffer, and Michael T Tulley (2004). *Radar cross section*. SciTech Publishing
4. M Madheswaran and P Suresh Kumar (2012). “Estimation of wide band radar cross section (RCS) of regular shaped objects using method of moments (MOM)”. in: *Ictact Journal on Communication Technology* 3.2, pp. 536–541

Method of Moments

1. Walton C Gibson (2021). *The method of moments in electromagnetics*. Chapman and Hall/CRC
2. Roger F Harrington (1987). “The method of moments in electromagnetics”. In: *Journal of Electromagnetic waves and Applications* 1.3, pp. 181–200
3. Cai-Cheng Lu and Chong Luo (2003). “Comparison of iteration convergences of SIE and VSIE for solving electromagnetic scattering problems for coated objects”. In: *Radio Science* 38.2, pp. 11–1
4. Jiade Yuan, Changqing Gu, and Guodong Han (2009). “Efficient generation of method of moments matrices using equivalent dipole-moment method”. In: *IEEE Antennas and Wireless Propagation Letters* 8, pp. 716–719

Using Mercury MoM and post-processing

1. Daniel Topa (Mar. 2020c). *Radar Cross Section Models for AFCAP Dashboard: Rapid Report 2020-02: Corrected*. Briefing
2. Daniel Topa (Apr. 2020a). *Mercury Method of Moments Adjunct Visualization Tool: Trials and Tribulations*. Tech. rep. ARFL/RVB
3. Daniel Topa (Apr. 2020d). *Radar Cross Section: Phase 1 Summary Report*. Tech. rep. ARFL/RVB
4. Daniel Topa (2020b). *Mercury Method of Moments: AFRL Quick Start Guide*. Tech. rep. AFRL

A Mercury Method of Moments: Data Formats

A.1 Numeric Results

The MoM RCS data is delivered in a matrix with m rows and n columns (standard matrix addressing).

$1 \leq m \leq 28$ MHz (integer steps)
 $1 \leq n \leq 90$ degrees (integer steps)

The matrix is WIDE (more columns than rows)

Frequency partition: row 1: 3 MHz row 2: 4 MHz . . . row 28: 30 Mhz

Let r index the rows. Then frequency ν is in row $= \nu - 2$

Angular partition col 1: 0 col 2: 1 . . . col 181: 180

col 1 col 2 col 3 col 181 0 1 2 . . . 180

Let c be the column index. The measurement for angle α is in column $c = \alpha + 1$

The test asset is symmetric: $\sigma(\alpha) = \sigma(-\alpha)$

But the matrix can easily be delivered in other forms, such as the transpose (interchange rows and columns), or packed into a linear array.

Sample:

4.16411, 4.14247, 4.07319, 3.95637, 3.79263, 3.58287, 3.32827, 3.0303, . . .
18.2776, 18.2369, 18.1199, 17.9248, 17.6523, 17.3041, 16.8817, 16.3876, . . .
25.6306, 25.5886, 25.463, 25.2538, 24.9618, 24.5882, 24.1346, 23.6028, . . .
...

B Mercury Method of Moments: Software Toolkit

Mercury MoM produces thousands of lines of output to a `*.4112.txt` file, a mix of numbers and strings. Once the data portions are located, they can be harvested straightaway. However, the text messages include debug information and the text patterns are varied.

Data analysis on data sets with a large number of facets can take several hours.

B.1 rcsharvester.f08

```
! harvest the electric field values from the ASCII file *.4112.txt mixed text and numeric
lines
! compute the mean total RCS and write these values
```

B.1.1 Class Electric Fields: m-class-electric-fields.f08

B.1.2 m-class-electric-fields.f08

The primary output of the simulation are the electric fields. Lines 17-24 define the class; the remainder of the codes is for methods. The input electric field is resolved into two polarization axes: horizontal and vertical. Each of these fields are resolved into horizontal and vertical components creating four complex vectors (line 21) whose length matches the angular sample size.

The class `m-class-electric-fields.f08` reads the text file and harvests the electric fields eventually passing back a composite value (lines 65-66) for all four components of the scattering return.

```

1  ! Parses alphanumeric line from MoM *.4112.txt and extracts electric field values
2  module mClassElectricFields
3
4      use mFormatDescriptors,          only : fmt_stat, fmt_iomsg
5      use mLibraryOfConstants,         only : cZero, MoMlineLength, messageLength
6      use mPrecisionDefinitions,       only : ip, rp
7
8      implicit none
9
10     integer ( ip ) :: left = 0, right = 0
11     integer :: io_stat = 0
12     character ( len = messageLength ) :: io_msg = ""
13     character ( len = 15 ) :: number = ""
14
15     ! theta = azimuth
16     ! phi = elevation (North Pole = 0, equator = 90)
17     type :: electricFields
18         real ( rp ) :: meanTotalRCS = 0.0_rp
19         real ( rp ) :: dBsm = 0.0_rp
20         real ( rp ) :: theta = 0.0_rp, phi = 0.0_rp
21         complex ( rp ) :: thetaTheta = cZero, thetaPhi = cZero, phiTheta = cZero, phiPhi = cZero
22     contains
23         procedure, public :: gather_mean_total_rcs => gather_mean_total_rcs_sub
24     end type electricFields
25
26     private :: gather_mean_total_rcs_sub
27     private :: compute_mean_total_rcs_sub, compute_dbsm_sub, extract_electric_fields_sub
28     private :: gather_complex_field_sub, gather_real_field_sub
29
30     ! parameters
31     integer ( ip ), parameter :: mll = MoMlineLength
32     ! finger print of data line: start and stop positions for each numerical field
33     ! load matrix as columns
34     ! sample data line:
35     ! 90.0000, 0.0000, (-0.4572920E+05, 0.8350829E+05), (0.2034567E+06, -0.9493007E+05), (0.2034813E+06, -0.9492184E+05), (-0.1727375E+06, 0.3787291E+05)
36     integer, parameter :: endpoints ( 1 : 10, 1 : 2 ) = &
37         reshape ( [ [ 1, 14, 28, 44, 62, 78, 96, 112, 130, 146 ], &
38             [ 12, 25, 42, 58, 76, 92, 110, 126, 144, 160 ] ], [ 10, 2 ] ) &
39     ! constructor
40     type ( electricFields ), parameter :: electricFields0 = &
41         electricFields ( meanTotalRCS = 0.0, theta = 0.0, phi = 0.0, &
42             thetaTheta = cZero, thetaPhi = cZero, phiTheta = cZero, phiPhi = cZero )
43     contains
44
45     ! master routine: only exposed procedure
46     subroutine gather_mean_total_rcs_sub ( me, textLine )
47         class ( electricFields ), target :: me
48         character ( len = mll ), intent ( in ) :: textLine
49         call extract_electric_fields_sub ( me, textLine )
50         call compute_mean_total_rcs_sub ( me )
51         call compute_dbsm_sub ( me )
52         return
53     end subroutine gather_mean_total_rcs_sub
54
55     ! Sciacca prescription
56     subroutine compute_dbsm_sub ( me )
57         class ( electricFields ), target :: me
58         me % dBsm = 10.0_rp * log10 ( me % meanTotalRCS )
59         return
60     end subroutine compute_dbsm_sub
61
62     ! Sciacca prescription
63     subroutine compute_mean_total_rcs_sub ( me )
64         class ( electricFields ), target :: me
65         me % meanTotalRCS = abs ( me % thetaTheta ) + abs ( me % thetaPhi ) &
66             + abs ( me % phiTheta ) + abs ( me % phiPhi )
67         me % meanTotalRCS = me % meanTotalRCS / real ( 2, kind = rp )
68         return
69     end subroutine compute_mean_total_rcs_sub
70
71     subroutine extract_electric_fields_sub ( me, textLine )
72         class ( electricFields ), target :: me
73         character ( len = mll ), intent ( in ) :: textLine
74         integer ( ip ) :: position = 0
75         ! move across text line gathering numeric values
76         position = 1
77         call gather_real_field_sub &
78             ( position = position, real_value = me % theta, textLine = textLine, fmt = "( f12.4 )" )
79         call gather_real_field_sub &
80             ( position = position, real_value = me % phi, textLine = textLine, fmt = "( f12.4 )" )
81         call gather_complex_field_sub &
82             ( position = position, complex_value = me % thetaTheta, textLine = textLine )
83         call gather_complex_field_sub &
84             ( position = position, complex_value = me % thetaPhi, textLine = textLine )
85         call gather_complex_field_sub &
86             ( position = position, complex_value = me % phiTheta, textLine = textLine )
87         call gather_complex_field_sub &
88             ( position = position, complex_value = me % phiPhi, textLine = textLine )

```

```

89     return
90 end subroutine extract_electric_fields_sub
91
92 subroutine gather_real_field_sub ( position, real_value, textLine, fmt )
93     real ( rp ),          intent ( out ) :: real_value
94     integer ( ip ),       intent ( inout ) :: position
95     character ( len = mll ), intent ( in ) :: textLine
96     character ( len = 9 ), intent ( in ) :: fmt
97     left = endpoints ( position, 1 )
98     right = endpoints ( position, 2 )
99     write ( number, fmt = 100 ) textLine ( left : right )
100     if ( io_stat /= 0 ) then
101         write ( *, fmt = '( 3g0 )' ) "Failure to WRITE string value '", trim ( textLine ( left : right ) ) , "'."
102         write ( *, fmt = fmt_stat ) io_stat
103         write ( *, fmt = fmt_iomsg ) trim ( io_msg )
104         stop "Error occurred in module 'mClassElectricFields', subroutine 'gather_real_field_sub'."
105     end if
106     read ( number, fmt = fmt ) real_value
107     if ( io_stat /= 0 ) then
108         write ( *, fmt = '( 5g0 )' ) "Failure to READ string value '", trim ( textLine ( left : right ) ) , &
109             "' as a REAL number using format descriptor ", fmt, "."
110         write ( *, fmt = fmt_stat ) io_stat
111         write ( *, fmt = fmt_iomsg ) trim ( io_msg )
112         stop "Error occurred in module 'mClassElectricFields', subroutine 'gather_real_field_sub'."
113     end if
114     position = position + 1
115     return
116     100 format ( g0 )
117 end subroutine gather_real_field_sub
118
119 subroutine gather_complex_field_sub ( position, complex_value, textLine )
120     complex ( rp ),          intent ( out ) :: complex_value
121     integer ( ip ),          intent ( inout ) :: position
122     character ( len = mll ), intent ( in ) :: textLine
123     real ( rp ) :: x = 0.0_rp, y = 0.0_rp
124     call gather_real_field_sub ( position = position, real_value = x, textLine = textLine, fmt = "( e15.7 )" )
125     call gather_real_field_sub ( position = position, real_value = y, textLine = textLine, fmt = "( e15.7 )" )
126     complex_value = cmplx ( x, y )
127     return
128 end subroutine gather_complex_field_sub
129
130 end module mClassElectricFields

```

B.1.3 Class Data File: m-class-data-file.f08

```

1 module mClassDataFile
2
3     use, intrinsic :: iso_fortran_env, only : iostat_end
4     ! classes
5     use mClassAverages,          only : average, average0
6     use mClassElectricFields,    only : electricFields, electricFields0
7     use mClassMesh,              only : meshReal
8     use mAllocations,            only : allocationToolkit, allocationToolkit0
9     use mAllocationsSpecial,     only : allocate_rank_one_averages_sub
10    ! utilities
11    use mLibraryOfConstants,      only : fileNameLength, messageLength, MoMlineLength
12    ! use mBulkRCS,                only : BulkRCS, BulkRCS0
13    use mFileHandling,            only : safeopen_readonly, safeopen_writereplace
14    use mFormatDescriptors,       only : fmt_one, fmt_stat, fmt_iomsg, fmt_shape2
15    use mPrecisionDefinitions,    only : ip, rp
16    use mTextFileUtilities,       only : count_lines_sub, mark_frequencies_sub, read_text_lines_sub, file_closer_sub, &
17        iostat_check_sub
18    ! use mTextFileUtilities,      only : count_lines_sub, file_closer_sub, iostat_check_sub, mark_frequencies_sub, &
19    ! parse_name_sub, read_text_lines_sub
20    implicit none
21
22    ! parameters
23    integer ( ip ), parameter :: fml = fileNameLength, msgl = messageLength, mll = MoMlineLength
24    character ( len = 9 ), parameter :: strAzimuth = "azimuth "
25    character ( len = 9 ), parameter :: strElevation = "elevation"
26    character ( len = * ), parameter :: moduleCrash = "Program crashed in module 'mClassDataFile', "
27
28    integer :: io_stat = 0
29    character ( len = msgl ) :: io_msg = ""
30
31    type :: dataFile4112
32        ! rank 2
33        real ( rp ),          allocatable :: rcs_table ( : , : ) ! angle mesh length x nu mesh length
34        real ( rp ),          allocatable :: dbsm_table ( : , : ) ! angle mesh length x nu mesh length
35        ! ! rank 1
36        integer ( ip ),       allocatable :: lineNumbersFrequency ( : )!, &
37        ! lineNumbersFinished ( : )
38        type ( average ),     allocatable :: perFrequencyAverage ( : ) ! nu mesh length
39        type ( average )      :: globalAverage
40        character ( len = mll ), allocatable :: lines4112Text ( : ) ! length numlines4112Text
41        ! rank 0
42        type ( electricFields ) :: eFields = electricFields0
43        type ( meshReal ) :: meshFrequency, &

```

```

44         meshFreeAngle
45     integer ( ip ) :: numFrequencies = 0, &
46         numFixedAngles = 0, &
47         numFreeAngles = 0, &
48         numMeasurements = 0, &
49         numLines4112Text = 0
50     integer ( ip ) :: io_unit = 0
51     character ( len = 9 ) :: angleFixedType = "", angleFreeType = ""
52     character ( len = fml ) :: file4112Name = "", fileRCStxtName = "", fileRCSbinaryName = "", &
53         fileBsmTxtName = "", fileBsmBinaryName = ""
54     ! allocation tools
55     type ( allocationToolkit ) :: myKit = allocationToolkit0
56 contains
57     procedure, public :: allocate_rcs_tables => allocate_rcs_tables_sub, &
58         allocate_rcsAverages => allocate_rcsAverages_sub, &
59         characterize_rcs_by_frequency => characterize_rcs_by_frequency_sub, &
60         check_rcs_table_structure => check_rcs_table_structure_sub, &
61         establish_free_angle_mesh => establish_free_angle_mesh_sub, &
62         establish_frequency_mesh => establish_frequency_mesh_sub, &
63         extract_rcs_from_4112_file => extract_rcs_from_4112_file_sub, &
64         harvest_frequencies => harvest_frequencies_sub, &
65         set_file_names => set_file_names_sub, &
66         set_free_angle_azimuth => set_free_angle_azimuth_sub, &
67         set_free_angle_elevation => set_free_angle_elevation_sub, &
68         write_rcs_file_set => write_rcs_file_set_sub, &
69         write_rcs_binary => write_rcs_binary_sub, &
70         write_rcs_csv => write_rcs_csv_sub, &
71         write_dBsm_binary => write_dBsm_binary_sub, &
72         write_dBsm_csv => write_dBsm_csv_sub, &
73         write_summary_by_frequency => write_summary_by_frequency_sub, &
74         write_summary_for_all_frequencies => write_summary_for_all_frequencies_sub
75 end type dataFile4112
76
77 private :: allocate_rcs_tables_sub, allocate_rcsAverages_sub, &
78     establish_free_angle_mesh_sub, establish_frequency_mesh_sub, extract_rcs_from_4112_file_sub, &
79     harvest_frequencies_sub, &
80     set_file_names_sub, set_free_angle_azimuth_sub, set_free_angle_elevation_sub, &
81     write_summary_by_frequency_sub, write_summary_for_all_frequencies_sub
82
83 contains
84
85     subroutine characterize_rcs_by_frequency_sub ( me )
86     class ( dataFile4112 ), target :: me
87     type ( average ), pointer :: p => null ( )
88     integer ( ip ) :: kFrequency = 0
89
90     sweep_frequencies: do kFrequency = 1, me % numFrequencies
91     p => me % perFrequencyAverage ( kFrequency )
92     call p % find_max_and_min ( vector = me % rcs_table ( 1 : me % numFreeAngles, kFrequency ) )
93     call p % compute_mean_and_variance ( vector = me % rcs_table ( 1 : me % numFreeAngles, kFrequency ), &
94         one = me % meshFreeAngle % one )
95     p => null ( )
96     end do sweep_frequencies
97
98     return
99 end subroutine characterize_rcs_by_frequency_sub
100
101 module subroutine write_summary_for_all_frequencies_sub ( me )
102 class ( dataFile4112 ), target :: me
103 integer ( ip ) :: kFrequency = 0, first = 0, last = 0, numConvolution = 0
104 real ( rp ), allocatable :: global_rcs ( : ), one ( : )
105 ! allocate memory for all RCS measurements
106 numConvolution = me % numFrequencies * me % numFreeAngles
107 call me % myKit % allocate_rank_one_reals ( real_array = global_rcs, index_min = 1, index_max = numConvolution )
108 call me % myKit % allocate_rank_one_reals ( real_array = one, index_min = 1, index_max = numConvolution )
109 ! load data vector
110 sweep_frequencies: do kFrequency = 1, me % meshFrequency % numMeshElements
111     first = ( kFrequency - 1 ) * me % numFreeAngles + 1
112     last = first + me % numFreeAngles - 1
113     global_rcs ( first : last ) = me % rcs_table ( 1 : me % numFreeAngles, kFrequency )
114 end do sweep_frequencies
115 ! compute extrema
116 one ( : ) = global_rcs ( : ) - global_rcs ( : ) + 1.0_rp
117 call me % globalAverage % find_max_and_min ( vector = global_rcs ( 1 : numConvolution ) )
118 call me % globalAverage % compute_mean_and_variance ( vector = global_rcs ( 1 : numConvolution ), one = one )
119 write ( *, * )
120 write ( *, fml = 100 ) me % globalAverage % mean, &
121     me % globalAverage % standardDeviation, &
122     me % globalAverage % extrema % minVal, &
123     me % globalAverage % extrema % maxVal
124 return
125 100 format ( "Aggregate for all RCS measurements: mean = ", g0, " +/- ", g0, " ", min = " ", g0, " ", max = " ", g0 )
126 end subroutine write_summary_for_all_frequencies_sub
127
128 module subroutine write_summary_by_frequency_sub ( me )
129 class ( dataFile4112 ), target :: me
130 integer ( ip ) :: kFrequency = 0
131 write ( *, * )
132 sweep_frequencies: do kFrequency = 1, me % meshFrequency % numMeshElements
133     write ( *, fml = 100 ) kFrequency, me % meshFrequency % meshValues ( kFrequency ), &
134         me % perFrequencyAverage ( kFrequency ) % mean, &
135         me % perFrequencyAverage ( kFrequency ) % standardDeviation, &

```

```

136                                     me % perFrequencyAverage ( kFrequency ) % extrema % minValue, &
137                                     me % perFrequencyAverage ( kFrequency ) % extrema % maxValue
138     end do sweep_frequencies
139     return
140     100 format ( I3.3, ". nu = ", g0, ", mean RCS = ", g0, " +/- ", g0, ", min = ", g0, ", max = ", g0 )
141 end subroutine write_summary_by_frequency_sub
142
143 module subroutine write_rcs_file_set_sub ( me )
144     class ( dataFile4112 ), target :: me
145     call me % write_rcs_csv ( )
146     call me % write_rcs_binary ( )
147     call me % write_dBsm_csv ( )
148     call me % write_dBsm_binary ( )
149     return
150 end subroutine write_rcs_file_set_sub
151
152 module subroutine write_rcs_binary_sub ( me )
153     class ( dataFile4112 ), target :: me
154     integer ( ip ) :: io_rcs = 0
155     character ( len = msgl ) :: crashChain = ""
156
157     crashChain = moduleCrash // "subroutine 'write_rcs_binary_sub'."
158
159     open ( newunit = io_rcs, file = me % fileRCSBinaryName, action = 'WRITE', status = 'REPLACE', form = 'UNFORMATTED', &
160           iostat = io_stat, iomsg = io_msg )
161     call iostat_check_sub ( action = "UNFORMATTED OPENING", fileName = me % fileRCSBinaryName, crashChain = crashChain, &
162           iostat = io_stat, iomsg = io_msg )
163
164     write ( io_rcs, iostat = io_stat, iomsg = io_msg ) me % rcs_table ( 1 : me % meshFreeAngle % numMeshElements, &
165           1 : me % meshFrequency % numMeshElements )
166     call iostat_check_sub ( action = "UNFORMATTED WRITE to", fileName = me % fileRCSBinaryName, crashChain = crashChain, &
167           iostat = io_stat, iomsg = io_msg )
168     call file_closer_sub ( io_unit = io_rcs, fileName = me % fileRCSBinaryName, crashChain = crashChain )
169
170     return
171 end subroutine write_rcs_binary_sub
172
173 module subroutine write_rcs_csv_sub ( me )
174     class ( dataFile4112 ), target :: me
175     integer ( ip ) :: kFrequency = 0, kFreeAngle = 0, &
176           io_out = 0
177     character ( len = msgl ) :: crashChain = ""
178
179     crashChain = moduleCrash // "subroutine 'write_rcs_csv_sub'."
180     io_out = safeopen_writereplace ( me % fileRCStxtName )
181     ! write RCS values one row (frequency) at a time
182     sweep_frequencies: do kFrequency = 1, me % meshFrequency % numMeshElements
183         write ( io_out, fmt = me % meshFreeAngle % valuesFormatDescriptor ) ( me % rcs_table ( kFreeAngle, kFrequency ), &
184               kFreeAngle = 1, me % meshFreeAngle % numMeshElements )
185         call iostat_check_sub ( action = "WRITE to", fileName = me % fileRCStxtName, crashChain = crashChain, &
186               iostat = io_stat, iomsg = io_msg )
187     end do sweep_frequencies
188     ! close io handle
189     call file_closer_sub ( io_unit = io_out, fileName = me % fileRCStxtName, crashChain = crashChain )
190
191     return
192 end subroutine write_rcs_csv_sub
193
194 module subroutine write_dBsm_binary_sub ( me )
195     class ( dataFile4112 ), target :: me
196     integer ( ip ) :: io_rcs = 0
197     character ( len = msgl ) :: crashChain = ""
198
199     crashChain = moduleCrash // "subroutine 'write_dBsm_binary_sub'."
200
201     open ( newunit = io_rcs, file = me % filedBsmBinaryName, action = 'WRITE', status = 'REPLACE', form = 'UNFORMATTED', &
202           iostat = io_stat, iomsg = io_msg )
203     call iostat_check_sub ( action = "UNFORMATTED OPENING", fileName = me % fileRCSBinaryName, crashChain = crashChain, &
204           iostat = io_stat, iomsg = io_msg )
205
206     write ( io_rcs, iostat = io_stat, iomsg = io_msg ) me % dBsm_table ( 1 : me % meshFreeAngle % numMeshElements, &
207           1 : me % meshFrequency % numMeshElements )
208     call iostat_check_sub ( action = "UNFORMATTED WRITE to", fileName = me % fileRCSBinaryName, crashChain = crashChain, &
209           iostat = io_stat, iomsg = io_msg )
210     call file_closer_sub ( io_unit = io_rcs, fileName = me % filedBsmBinaryName, crashChain = crashChain )
211
212     return
213 end subroutine write_dBsm_binary_sub
214
215 module subroutine write_dBsm_csv_sub ( me )
216     class ( dataFile4112 ), target :: me
217     integer ( ip ) :: kFrequency = 0, kFreeAngle = 0, &
218           io_out = 0
219     character ( len = msgl ) :: crashChain = ""
220
221     crashChain = moduleCrash // "subroutine 'write_dBsm_csv_sub'."
222     io_out = safeopen_writereplace ( me % filedBsmTxtName )
223     ! write RCS values one row (frequency) at a time
224     sweep_frequencies: do kFrequency = 1, me % meshFrequency % numMeshElements
225         write ( io_out, fmt = me % meshFreeAngle % valuesFormatDescriptor ) ( me % dBsm_table ( kFreeAngle, kFrequency ), &
226               kFreeAngle = 1, me % meshFreeAngle % numMeshElements )
227         call iostat_check_sub ( action = "WRITE to", fileName = me % filedBsmTxtName, crashChain = crashChain, &

```

```

228                                     iostat = io_stat, iomsg = io_msg )
229     end do sweep_frequencies
230     ! close io handle
231     call file_closer_sub ( io_unit = io_out, fileName = me % fileRCStxtName, crashChain = crashChain )
232
233     return
234 end subroutine write_dBsm_csv_sub
235
236 subroutine set_file_names_sub ( me, file4112Name )
237     class ( dataFile4112 ), target :: me
238     character ( len = fnl ), intent ( in ) :: file4112Name
239     integer ( ip ) :: nameLength = 0
240
241     nameLength = len ( trim ( file4112Name ) )
242     me % file4112Name = trim ( file4112Name )
243     me % fileRCStxtName = trim ( file4112Name ( 1 : nameLength - 4 ) ) // ".rcs.txt"
244     me % fileRCsBinaryName = trim ( file4112Name ( 1 : nameLength - 4 ) ) // ".rcs.r32"
245     me % filedBsmTxtName = trim ( file4112Name ( 1 : nameLength - 4 ) ) // ".dBsm.txt"
246     me % filedBsmBinaryName = trim ( file4112Name ( 1 : nameLength - 4 ) ) // ".dBsm.r32"
247
248     return
249 end subroutine set_file_names_sub
250
251 subroutine allocate_rcsAverages_sub ( me )
252     class ( dataFile4112 ), target :: me
253     call allocate_rank_one_averages_sub ( rank_1_average = me % perFrequencyAverage, &
254                                         index_min = 1, index_max = me % numFrequencies )
255     return
256 end subroutine allocate_rcsAverages_sub
257
258 subroutine allocate_rcs_tables_sub ( me )
259     class ( dataFile4112 ), target :: me
260     call me % myKit % allocate_rank_two_reals ( rank_2_real_array = me % rcs_table, &
261                                               dim1_index_min = 1, dim1_index_max = me % numFreeAngles, &
262                                               dim2_index_min = 1, dim2_index_max = me % numFrequencies )
263     call me % myKit % allocate_rank_two_reals ( rank_2_real_array = me % dBsm_table, &
264                                               dim1_index_min = 1, dim1_index_max = me % numFreeAngles, &
265                                               dim2_index_min = 1, dim2_index_max = me % numFrequencies )
266     return
267 end subroutine allocate_rcs_tables_sub
268
269 subroutine establish_frequency_mesh_sub ( me )
270     class ( dataFile4112 ), target :: me
271     ! count lines in MoM file (e.g. 14844)
272     call count_lines_sub ( fullFileName = me % file4112Name, numLines = me % numLines4112Text )
273     ! allocate object to hold text of MoM file as a collection of text lines
274     call me % myKit % allocate_rank_one_characters ( character_array = me % lines4112Text, &
275                                                    index_min = 1, index_max = me % numLines4112Text )
276     ! load MoM text into memory to count frequencies and angles
277     call read_text_lines_sub ( fileName = me % file4112Name, linesText = me % Lines4112Text )
278     ! sift through text lines for " Freq ="
279     call me % harvest_frequencies ( )
280     return
281 end subroutine establish_frequency_mesh_sub
282
283 ! sweep through character array looking for " Freq"
284 ! store these values in a temporary array until numMesh is allocated
285 subroutine harvest_frequencies_sub ( me )
286     class ( dataFile4112 ), target :: me
287     ! pointers
288     !character ( len = mll ), pointer :: p => null ( )
289     type ( meshReal ), pointer :: q => null ( )
290     type ( allocationToolKit ), pointer :: s => null ( )
291     ! temp arrays
292     real ( ip ) :: tempFrequencyValues ( 1 : 500 )
293     integer ( ip ) :: tempLineNumsFrequency ( 1 : 500 )
294     ! scalars
295     integer ( ip ) :: numFrequencies = 0, kFrequency = 0
296
297     ! find lines containing " Freq ="
298     call mark_frequencies_sub ( lines4112Text = me % lines4112Text, &
299                               numLines4112Text = me % numLines4112Text, &
300                               tempFrequencyValues = tempFrequencyValues, &
301                               tempLineNumsFrequency = tempLineNumsFrequency, &
302                               numFrequencies = numFrequencies )
303
304     ! record what we have learned about the mesh
305     q => me % meshFrequency
306     q % numMeshElements = numFrequencies
307     ! allocate data objects
308     call q % allocate_mesh_real ( )
309     s => me % myKit
310     call s % allocate_rank_one_integers ( integer_array = me % lineNumbersFrequency, index_min = 1, &
311                                         index_max = q % numMeshElements )
312     s => null ( )
313     ! move temporary array data into data object
314     do kFrequency = 1, q % numMeshElements
315         q % meshValues ( kFrequency ) = tempFrequencyValues ( kFrequency )
316         me % lineNumbersFrequency ( kFrequency ) = tempLineNumsFrequency ( kFrequency )
317     end do
318     me % numFrequencies = q % numMeshElements
319     call q % analyze_mesh_values ( )

```



```

320         q => null ( )
321     return
322 end subroutine harvest_frequencies_sub
323
324 subroutine extract_rcs_from_4112_file_sub ( me )
325     class ( dataFile4112 ), target :: me
326     ! locals
327     !real ( rp ) :: sigma = 0.0_rp
328     integer ( ip ) :: kFrequency = 0, kFreeAngle = 0, linePosition = 0
329     character ( len = mll ) :: textLine
330
331     ! open *.4112.txt file, read text lines into memory
332     call read_text_lines_sub ( fileName = me % file4112Name, linesText = me % lines4112Text )
333     ! sweep and harvest RCS value
334     sweep_frequencies: do kFrequency = 1, me % numFrequencies
335         linePosition = me % lineNumbersFrequency ( kFrequency ) + 8
336         sweep_free_angles: do kFreeAngle = 1, me % numFreeAngles
337             textLine = me % lines4112Text ( linePosition )
338             call me % eFields % gather_mean_total_rcs ( textLine = textLine )
339             me % rcs_table ( kFreeAngle, kFrequency ) = me % eFields % meanTotalRCS
340             me % dBsm_table ( kFreeAngle, kFrequency ) = me % eFields % dBsm
341             linePosition = linePosition + 1
342         end do sweep_free_angles
343     end do sweep_frequencies
344
345     return
346 end subroutine extract_rcs_from_4112_file_sub
347
348 subroutine set_free_angle_elevation_sub ( me )
349     class ( dataFile4112 ), target :: me
350     me % angleFreeType = strElevation
351     me % angleFixedType = strAzimuth
352     return
353 end subroutine set_free_angle_elevation_sub
354
355 subroutine set_free_angle_azimuth_sub ( me )
356     class ( dataFile4112 ), target :: me
357     me % angleFreeType = strAzimuth
358     me % angleFixedType = strElevation
359     return
360 end subroutine set_free_angle_azimuth_sub
361
362 subroutine establish_free_angle_mesh_sub ( me, angle_min, angle_max, angle_count )
363     class ( dataFile4112 ), target :: me
364     real ( rp ), intent ( in ) :: angle_min, angle_max
365     integer ( ip ), intent ( in ) :: angle_count
366
367     me % meshFreeAngle % meshAverage % extrema % minVal = angle_min
368     me % meshFreeAngle % meshAverage % extrema % maxVal = angle_max
369     me % meshFreeAngle % numMeshElements = angle_count
370     me % numFreeAngles = angle_count
371
372     call me % meshFreeAngle % allocate_mesh_real ( )
373     call me % meshFreeAngle % compute_real_mesh_length ( )
374     call me % meshFreeAngle % compute_real_mesh_interval ( )
375     call me % meshFreeAngle % populate_real_mesh ( )
376     call me % meshFreeAngle % populate_integer_mesh ( )
377
378     return
379 end subroutine establish_free_angle_mesh_sub
380
381 subroutine check_rcs_table_structure_sub ( me )
382     class ( dataFile4112 ), target :: me
383     write ( *, * )
384     write ( *, fmt = '( g0 )' ) "# # Dimensions for RCS data container # #"
385     write ( *, * )
386     write ( *, fmt = '( g0 )' ) "# Expected dimensions:"
387     write ( *, fmt = '( 2g0 )' ) "# Number of radar frequencies scanned by MoM: ", me % numFrequencies
388     write ( *, fmt = '( 4g0 )' ) "# Number of ", me % angleFreeType, " angles scanned by MoM: ", me % numFreeAngles
389     write ( *, * )
390     write ( *, fmt = '( 2g0 )' ) "# Container MoM 4112.txt file: rcs_table"
391     write ( *, fmt = '( 6g0 )' ) "# Free angle dimension = ", size ( me % rcs_table, 1 ), &
392         " indices run from ", lbound ( me % rcs_table, 1 ), &
393         " to ", ubound ( me % rcs_table, 1 )
394     write ( *, fmt = '( 6g0 )' ) "# Frequency dimension = ", size ( me % rcs_table, 2 ), &
395         " indices run from ", lbound ( me % rcs_table, 2 ), &
396         " to ", ubound ( me % rcs_table, 2 )
397     write ( *, * )
398     return
399 end subroutine check_rcs_table_structure_sub
400
401 end module mClassDataFile

```

C Mercury Method of Moments: Distribution and Rights

C.1 Distribution Letter for Software

The subsequent distribution letter was signed by Randy J. Petyak of the NASA Software Release Authority and describes terms for distribution, Government rights, and the ITAR status of the software.

DRAFT

December 11, 2019

Air Force Research Laboratory
RVB
3550 Aberdeen Ave SE
Kirtland Air Force Base, NM 87117-5776
Attn: Mr. Nelson Bonito

Subject: Transmittal of Mercury MoM version 4.1.12, MM_Viz Code.

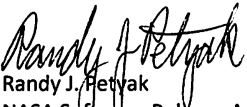
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Randy J. Petyak
NASA Software Release Authority
(202) 358-4387

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=====

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C.4 Obtaining Software and Documentation

For more information regarding this document contact the following:

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Figure 2: Contact information to request Mercury MoM Software and Documentations

C.5 Distribution Contents

C.5.1 Executables

1. Linux 64-bit
2. Windows 64-bit

C.5.2 Documentation

The distribution includes four documents in PDF which are marked as CUI:

1. User's Guide
2. Pill Tutorial
3. Code Validation Report
4. Benchmark Tests

D Using Python to Create Spreadsheets

D.1 Inputs

D.1.1 Main

Main module:

```
1 #! /usr/bin/python3
2
3 # # Daniel Topa
4
5 # # Excel tools
```

```

6 # xl_new_workbook( workbook_title )
7 # xl_sheet_requirements( this_workbook )
8 # xl_sheet_generate( this_workbook, title_sheet )
9 # xl_s( this_workbook )
10 # xl_sheet_header_footer( this_worksheet )
11
12 ## imports
13 import os # probe, change directories
14 import sys # python version
15 import datetime # https://stackoverflow.com/questions/415511/how-to-get-the-current-time-in-python
16 import numpy as np
17 import pandas as pd
18 import xlswriter # API for Excel
19 from xlswriter.utility import xl_rowcol_to_cell
20 import numpy as np
21 import pandas as pd
22
23 import cls_TestObject
24
25 ## modules
26 def xl_new_workbook( testObject ):
27
28     MoMResults = xlswriter.Workbook( testObject.outputFile )
29     print( "output file %s" % testObject.outputFile )
30     print( "source file %s" % testObject.sourceFile )
31
32     xl_sheet_master( MoMResults, testObject ) # MoM summary
33     xl_add_data_sheets( MoMResults, testObject ) # MoM summary
34     xl_sheet_provenance( MoMResults ) # provenance sheet
35
36     return MoMResults;
37
38 # == == == == == == == == == == == == == == == #
39
40 def xl_add_data_sheets( this_workbook, testObject ):
41
42     format_MoM_title = this_workbook.add_format( )
43     format_MoM_title.set_bold( )
44     format_MoM_title.set_font_color( "red" )
45
46     format_MoM_head = this_workbook.add_format( )
47     format_MoM_head.set_bold( )
48
49     format_MoM_polarization = this_workbook.add_format( )
50     format_MoM_polarization.set_bold( )
51
52     number_format = this_workbook.add_format({'num_format': '#,##0.000'})
53
54     # https://xlsxwriter.readthedocs.io/format.html#set_center_across
55     cell_format = this_workbook.add_format()
56     cell_format.set_center_across()
57
58     for index in range( 1, 29 ):
59         # add sheet and tag header and footer
60         title = str( index + 2 ) + ' MHz'
61         print ( 'adding sheet %s' % title )
62         s = xl_sheet_generate( this_workbook, title )
63         xl_sheet_header_footer( s )
64         s.write( "A1", "MoM 4.1.12 output (*.dat)", format_MoM_title )
65         #
66         s.write( "A3", "azimuth, ", format_MoM_head )
67         s.write( "B3", "HH, dBsm", format_MoM_head )
68         s.write( "C3", "VV, dBsm", format_MoM_head )
69         s.write( "D3", "HV, dBsm", format_MoM_head )
70         s.write( "E3", "VH, dBsm", format_MoM_head )
71         #
72         s.write( "H3", "mean", format_MoM_head )
73         s.write( "J3", "standard deviation", format_MoM_head )
74         #
75         s.write( "G4", "HH", format_MoM_polarization )
76         s.write( "G5", "VV", format_MoM_polarization )
77         #
78         # AttributeError: 'str' object has no attribute '_get_xf_index'
79         # s.write( "I4", "HH", u"\u00B1" )
80         s.write( "I4", '', cell_format )
81         s.write( "I5", '', cell_format )
82         s.set_column( "I:I", 3 )
83
84         # = AVERAGE( B5:B364 )
85         # = STDEV( B5:B364 )
86         s.write( "H4", '= AVERAGE( B5:B364)', number_format )
87         s.write( "H5", '= AVERAGE( C5:C364)', number_format )
88         s.write( "J4", '= STDEV( B5:B364 )', number_format )
89         s.write( "J5", '= STDEV( B5:B364 )', number_format )
90
91     # read in data file
92     filename = './data/sphere-005-' + testObject.resolution + '-' + str( index + 2 ).zfill(2) + '.4112.dat.txt'
93     s.write_string( "D1", filename )
94     data = pd.read_csv( filename, delimiter=r"\s+", header = None )
95     data_np = data.values
96     row = 3
97     col = 0

```


[illegible]

```

282     format_title = wbook.add_format( )
283     format_title.set_bold( )
284     format_title.set_font_color( "blue" )
285
286     format_label = wbook.add_format( )
287     format_label.set_bold( )
288
289     # https://xlsxwriter.readthedocs.io/example_defined_name.html
290     # https://docs.python.org/2.0/ref/strings.html
291     wbook.define_name( 'c_', '=299792458' )
292     #string = '\'+ str( testObject.sizeValue / 2 ) + \''
293     #print( 'string = %s' % string )
294     wbook.define_name( 'radius', '=5' )
295     wbook.define_name( 'size_optical_sq_m', '=\' + testObject.masterSheet + \'!$B$6\' )
296     wbook.define_name( 'size_optical_dbm', '=\' + testObject.masterSheet + \'!$B$7\' )
297
298     # sheet operations
299     s = xl_sheet_generate( wbook, testObject.masterSheet )
300     s.set_first_sheet( )
301
302     # widen first columns
303     s.set_column( "A:A", 17 )
304     s.set_column( "B:B", 10 )
305
306     # column of labels
307     s.write_string( row, col, 'INPUT', format_title ); row += 2
308
309     s.write( row, col, 'MoM output:', format_label )
310     s.write( row, col + 1, testObject.sourceFile ); row += 2
311
312     s.write( row, col, testObject.sizeName, format_label );
313     s.write( row, col + 1, testObject.sizeValue )
314     s.write( row, col + 2, 'm' ); row += 1
315
316     s.write( row, col, 'optical size', format_label )
317     s.write( row, col + 1, '= pi() * radius^2' )
318     s.write_string( row, col + 2, testObject.areaUnits ); row += 1
319     s.write_formula( row, col + 1, '= 10 * LOG10( size_optical_sq_m )' );
320     s.write( row, col + 2, 'dB area' ); row += 2
321
322     s.write( row, col, 'frequency (MHz)', format_label ); row += 1
323     s.write( row, col, 'wavelength (m)', format_label ); row += 1
324     s.write( row, col, 'radius / lambda', format_label ); row += 2
325
326     s.write( row, col, 'MoM average (dBm)', format_label ); row += 1
327     s.write( row, col, 'rel error (dBm)', format_label ); row += 2
328
329     s.write( row, col, 'rcs, sq m', format_label ); row += 1
330     s.write( row, col, 'rel error (sq m)', format_label )
331
332     xl_sheet_header_footer( s )
333
334
335     return
336
337 # root@f21d93a5a2e9:sphere $ python tools_xl.py
338 #
339 # root@f21d93a5a2e9:sphere $ date
340 # Wed Jun 24 01:19:38 MDT 2020
341 #
342 # root@f21d93a5a2e9:sphere $ pwd
343 # /Tlaloc/python/sphere
344

```

D.1.2 Class Test Object

Radar return data.

```

1  #!/usr/bin/python3
2
3  # # Daniel Topa
4
5  # imports
6  import math                # pi
7  import uuid                # Universal Unique Identifier
8  #from pathlib import Path  # rename file
9
10 class TestObject( object ):
11     def __init__( self ):
12
13         self._descriptor    = None    # sphere
14         self._sizeName      = None    # diameter
15         self._sizeValue     = None    # 10
16         self._sizeUnits     = None    # m
17         self._areaValue     = None    # pi r^2
18         self._areaUnits     = None    # m^2
19         self._resolution    = None    # 04
20         self._mastersheet   = None    # sphere, d = 10 m
21         self._sourceFile    = None    # *.dat

```

```

22     self._sourcePath      = None      # absolute path to *.dat
23     self._sourcePathFile  = None      # path + source file name
24     self._outputFile       = None      # *.xlsx
25     self._outputPath       = None      # absolute path to *.xlsx
26     self._outputPathFile   = None      # path + *.xlsx
27     self._uuid              = uuid.uuid4( ) # de facto time stamp
28
29 # P R O P E R T I E S #
30
31 @property
32 def descriptor( self ):
33     """Descriptor (sphere, cube, etc.)"""
34     return self._descriptor
35
36 @property
37 def sizeName( self ):
38     """Name of size parameter (edge, radius, etc.)"""
39     return self._sizeName
40
41 @property
42 def sizeValue( self ):
43     """Length parameter"""
44     return self._sizeValue
45
46 @property
47 def sizeUnits( self ):
48     """Units (m, mm, etc.)"""
49     return self._sizeUnits
50
51 @property
52 def areaValue( self ):
53     """Area"""
54     return self._areaValue
55
56 @property
57 def areaUnits( self ):
58     """Area units (m2, mm, etc.)"""
59     return self._areaUnits
60
61 @property
62 def masterSheet( self ):
63     """Name of master sheet"""
64     return self._masterSheet
65
66 @property
67 def sourcePath( self ):
68     """Path (absolute) to source file"""
69     return self._sourcePath
70
71 @property
72 def sourceFile( self ):
73     """Path + Name for input file"""
74     return self._sourceFile
75
76 @property
77 def outputFile( self ):
78     """Name of output file"""
79     return self._outputFile
80
81 @property
82 def outputPath( self ):
83     """Path (absolute) to output file"""
84     return self._outputPath
85
86 @property
87 def outputPathFile( self ):
88     """Path + Name for output file"""
89     return self._outputPathFile
90
91 @property
92 def uuid( self ):
93     """Universal unique identifier: connects requirements to source document"""
94     return self._uuid
95
96 # S E T T E R S #
97
98 @descriptor.setter
99 def descriptor( self, value ):
100     self._descriptor = value
101
102 @sizeName.setter
103 def sizeName( self, value ):
104     self._sizeName = value
105
106 @sizeValue.setter
107 def sizeValue( self, value ):
108     self._sizeValue = value
109
110 @sizeUnits.setter
111 def sizeUnits( self, value ):
112     self._sizeUnits = value
113

```

```

114 @areaValue.setter
115 def areaValue( self, value ):
116     self._areaValue = value
117
118 @areaUnits.setter
119 def areaUnits( self, value ):
120     self._areaUnits = value
121
122 @masterSheet.setter
123 def masterSheet( self, value ):
124     self._masterSheet = value
125
126 @sourcePath.setter
127 def sourcePath( self, value ):
128     self._sourcePath = value
129
130 @sourceFile.setter
131 def sourceFile( self, value ):
132     self._sourceFile = value
133
134 @outputFile.setter
135 def outputFile( self, value ):
136     self._outputFile = value
137
138 @outputPath.setter
139 def outputPath( self, value ):
140     self._outputPath = value
141
142 @outputPathFile.setter
143 def outputPathFile( self, value ):
144     self._outputPathFile = value
145
146 # D E L E T E R S #
147
148 @descriptor.deleter
149 def descriptor( self ):
150     del self._descriptor
151
152 @sizeName.deleter
153 def sizeName( self ):
154     del self._sizeName
155
156 @sizeValue.deleter
157 def sizeValue( self ):
158     del self._sizeValue
159
160 @sizeUnits.deleter
161 def sizeUnits( self ):
162     del self._sizeUnits
163
164 @areaValue.deleter
165 def areaValue( self ):
166     del self._areaValue
167
168 @areaUnits.deleter
169 def areaUnits( self ):
170     del self._areaUnits
171
172 @masterSheet.deleter
173 def masterSheet( self ):
174     del self._masterSheet
175
176 @sourcePath.deleter
177 def sourcePath( self ):
178     del self._sourcePath
179
180 @sourceFile.deleter
181 def sourceFile( self ):
182     del self._sourceFile
183
184 @outputFile.deleter
185 def outputFile( self ):
186     del self._outputFile
187
188 @outputPath.deleter
189 def outputPath( self ):
190     del self._outputPath
191
192 @outputPathFile.deleter
193 def outputPathFile( self ):
194     del self._outputPathFile
195
196 @uuid.deleter
197 def uuid( self ):
198     del self._uuid
199
200 # M E T H O D S #
201
202 def print_attributes( self ):
203     print( '\nSource attributes:' )
204     print( 'descriptor      = %s' % self.descriptor )
205     print( 'sizeName          = %s' % self.sizeName )

```



```

37
38 # == == == == == == == == == == == == #
39
40 def xl_add_data_sheets( this_workbook, testObject ):
41
42     format_MoM_title = this_workbook.add_format( )
43     format_MoM_title.set_bold( )
44     format_MoM_title.set_font_color( "red" )
45
46     format_MoM_head = this_workbook.add_format( )
47     format_MoM_head.set_bold( )
48
49     format_MoM_polarization = this_workbook.add_format( )
50     format_MoM_polarization.set_bold( )
51
52     number_format = this_workbook.add_format({'num_format': '#,##0.000'})
53
54     # https://xlsxwriter.readthedocs.io/format.html#set_center_across
55     cell_format = this_workbook.add_format()
56     cell_format.set_center_across()
57
58     for index in range( 1, 29 ):
59         # add sheet and tag header and footer
60         title = str( index + 2 ) + ' MHz'
61         print ( 'adding sheet %s' % title )
62         s = xl_sheet_generate( this_workbook, title )
63         xl_sheet_header_footer( s )
64         s.write( "A1", "MoM 4.1.12 output (*.dat)", format_MoM_title )
65         #
66         s.write( "A3", "azimuth, ", format_MoM_head )
67         s.write( "B3", "HH, dBsm", format_MoM_head )
68         s.write( "C3", "VV, dBsm", format_MoM_head )
69         s.write( "D3", "HV, dBsm", format_MoM_head )
70         s.write( "E3", "VH, dBsm", format_MoM_head )
71         #
72         s.write( "H3", "mean", format_MoM_head )
73         s.write( "J3", "standard deviation", format_MoM_head )
74         #
75         s.write( "G4", "HH", format_MoM_polarization )
76         s.write( "G5", "VV", format_MoM_polarization )
77         #
78         # AttributeError: 'str' object has no attribute '_get_xf_index'
79         # s.write( "I4", "HH", u"\u00Bi" )
80         s.write( "I4", "", cell_format )
81         s.write( "I5", "", cell_format )
82         s.set_column( "I:I", 3 )
83
84         # = AVERAGE( B5:B364 )
85         # = STDEV( B5:B364 )
86         s.write( "H4", "= AVERAGE( B5:B364)", number_format )
87         s.write( "H5", "= AVERAGE( C5:C364)", number_format )
88         s.write( "J4", "= STDEV( B5:B364 )", number_format )
89         s.write( "J5", "= STDEV( C5:C364 )", number_format )
90
91         # read in data file
92         filename = './data/sphere-005-' + testObject.resolution + '-' + str( index + 2 ).zfill(2) + '.4112.dat.txt'
93         s.write_string( "D1", filename )
94         data = pd.read_csv( filename, delimiter=r"\s+", header = None )
95         data_np = data.values
96         row = 3
97         col = 0
98         for line in range( 0, len ( data_np ) ):
99             cell = xl_rowcol_to_cell ( row, col )
100             s.write( row, col, data_np[ line ][ 0 ], number_format )
101             s.write( row, col + 1, data_np[ line ][ 1 ], number_format )
102             s.write( row, col + 2, data_np[ line ][ 2 ], number_format )
103             s.write( row, col + 3, data_np[ line ][ 3 ], number_format )
104             s.write( row, col + 4, data_np[ line ][ 4 ], number_format )
105             row += 1
106
107     return
108
109 # == == == == == == == == == == == == #
110
111 def xl_sheet_generate( this_workbook, title_sheet ):
112
113     # insure every worksheet has a header and footer
114     mySheet = this_workbook.add_worksheet( title_sheet )
115     xl_sheet_header_footer( mySheet )
116
117     return mySheet;
118
119 # == == == == == == == == == == == == #
120
121 def xl_sheet_provenance( this_workbook ):
122
123     # Define some global names.
124     this_workbook.define_name( 'c_', '=299792458' )
125     # forensic info
126     s = xl_sheet_generate( this_workbook, "provenance" )
127     # # special formats
128     # https://xlsxwriter.readthedocs.io/format.html#highlight=bold

```

```

130 # method 1
131 # setting the property as a dictionary of key/value pairs in the constructor
132 format_title = this_workbook.add_format( )
133 format_title.set_bold( )
134 format_title.set_font_color( "blue" )
135
136 # method 2
137 # passing a dictionary of properties to the add_format() constructor
138 format_time = this_workbook.add_format( {'num_format': 'yy/mm/dd hh:mm'} ) # https://xlsxwriter.readthedocs.io/working_with_dates_and_time.html
139
140 # widen first columns
141 s.set_column( "A:A", 15 )
142 s.set_column( "B:B", 13 )
143
144 # https://xlsxwriter.readthedocs.io/worksheet.html
145 s.write_url( "A1", "https://en.wikipedia.org/wiki/Computational_electromagnetics", string = "Radar Cross Section Measurements" )
146
147 # # provencance
148 s.write( "A3", "Workbook created by", format_title )
149 s.write( "A1", tip, "boo" )
150
151 # python notebook which creates workbook
152 s.write( "A4", "python source" )
153 s.write( "B4", os.path.basename( __file__ ) ) # charlie.py
154
155 # current working directory
156 s.write( "A5", "directory" )
157 s.write( "B5", os.getcwd( ) ) # /Volumes/Tlaitecutli/repos/GitHub/topa-development/python/xlsx
158
159 # python version
160 s.write( "A6", "python version" )
161 s.write( "B6", sys.version ) # "3.7.0 (default, Jun 28 2018, 07:39:16) [Clang 4.0.1 (tags/RELEASE_401/final)]"
162
163 # # environment variables
164 # practise row, col notation
165 col = 0 # starting column
166 row = 7 # starting row
167 s.write( row, col, "Environment variables", format_title ); row += 1
168
169 s.write( row, col, "SUSER" ) # 1127914
170 s.write( row, col + 1, os.environ[ "USER" ] ); row += 1
171
172 s.write( row, col, "SHOSTNAME" ) # Cauchy.Schwarz
173 s.write( row, col + 1, os.environ[ "HOSTNAME" ] ); row += 1
174
175 s.write( row, col, "SHOME" ) # /Users/1127914
176 s.write( row, col + 1, os.environ[ "HOME" ] ); row += 1
177
178 s.write( row, col, "timestamp" ) # 11/21/18 16:18
179 s.write( row, col + 1, datetime.datetime.now( ), format_time ); row += 1
180
181 # # Excel info routines
182 # https://xlsxwriter.readthedocs.io/working_with_formulas.html
183
184 row += 1 # jump
185 s.write( row, col, "XL info function", format_title ); row += 1
186
187 s.write( row, col, "platform" ) # mac
188 s.write_formula( row, col + 1, '= INFO( "system" )' ); row += 1
189
190 s.write( row, col, "recalculation mode" ) # Automatic
191 s.write_formula( row, col + 1, '= INFO( "recalc" )' ); row += 1
192
193 s.write( row, col, "active sheets" ) # 1
194 s.write_formula( row, col + 1, '= INFO( "numfile" )' ); row += 1
195
196 s.write( row, col, "cursor" ) # $A:$A$1
197 s.write_formula( row, col + 1, '= INFO( "origin" )' ); row += 1
198
199 s.write( row, col, "XL release" ) # 16.16
200 s.write_formula( row, col + 1, '= INFO( "release" )' ); row += 1
201
202 s.write( row, col, "application directory" ) # /Users/dantopa/Library/Containers/com.microsoft.Excel/Data/Documents/
203 s.write_formula( row, col + 1, '= INFO( "directory" )' ); row += 1
204
205 s.write( row, col, "operating systems" ) # Macintosh (Intel) Version 10.13.3 (Build 17D47)
206 s.write_formula( row, col + 1, '= INFO( "osversion" )' ); row += 1
207
208 return
209
210 # == == == == == == == == == == == == #
211
212 def xl_sheet_header_footer( this_worksheet ):
213
214     # header: sheet name (center)
215     # footer: date/time, page number, path/file
216
217     myheader = "&C&12&A" # fontsize 12
218     myfooter = "&L&8&T\n&8&D" + "&C &P / &N" + "&R&8&Z\n&8&F" # fontsize 8
219
220     this_worksheet.set_header( myheader )

```

[illegible]


```

313     s.write( row, col + 1, testObject.sizeValue )
314     s.write( row, col + 2, 'm' ); row += 1
315
316     s.write( row, col, 'optical size', format_label )
317     s.write( row, col + 1, 'pi() * radius^2' )
318     s.write_string( row, col + 2, testObject.areaUnits ); row += 1
319     s.write_formula( row, col + 1, '10 * LOG10( size_optical_sq_m )' );
320     s.write( row, col + 2, 'dB area' ); row += 2
321
322     s.write( row, col, 'frequency (MHz)', format_label ); row += 1
323     s.write( row, col, 'wavelength (m)', format_label ); row += 1
324     s.write( row, col, 'radius / lambda', format_label ); row += 2
325
326     s.write( row, col, 'MoM average (dBsm)', format_label ); row += 1
327     s.write( row, col, 'rel error (dBsm)', format_label ); row += 2
328
329     s.write( row, col, 'RCS, sq m', format_label ); row += 1
330     s.write( row, col, 'rel error (sq m)', format_label )
331
332     xl_sheet_header_footer( s )
333
334
335     return
336
337 # root@f21d93a5a2e9:sphere $ python tools_xl.py
338 #
339 # root@f21d93a5a2e9:sphere $ date
340 # Wed Jun 24 01:19:38 MDT 2020
341 #
342 # root@f21d93a5a2e9:sphere $ pwd
343 # /Tlaloc/python/sphere
344
345

```

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