

```

In[140]:= Manipulate[
  meanRCS = Import["rsc-values.dat"];
  (* pointer to data file *)
  index =  $\nu$  - 2;
  (* wavelegnth in meters *)
   $\lambda$  = Round[ $\frac{c}{\nu \cdot 1000000}$ ];
  (* grab rcs at specific wavelength *)
  rcs = meanRCS[[index]];
  (* number of data points *)
   $\theta$  = Table[
    k  $\frac{\pi}{180}$ 
    , {k, -180, 180}];
  m = Length[ $\theta$ ];
  (* center on nose (yaw angle  $\alpha = 90$ ) *)
   $\sigma$  = RotateLeft[rcs, 180];
  (* characterize variation for plot range *)
  mx = Max[ $\sigma$ ];
  mn = Min[ $\sigma$ ];
   $\Delta$  = 1.1;
  {top, bot} = {1.1 mx, 0.9 mn};
  (* plot subtitles *)
  subtitle = " $\nu$  = " <> ToString[ $\nu$ ] <> " MHz";
  subtitle = subtitle <> ",  $\lambda$  = " <> ToString[ $\lambda$ ] <> " m";
  (* scatter plot of data points *)
  z = { $\theta$ ,  $\sigma$ }T;
  g000 = ListPlot[z, PlotStyle -> {Purple, Opacity[0.5], PointSize[0.005]}];
  (* assemble linear system *)
  avector = Table[Cos[j  $\theta$ ], {j,  $\theta$ , d}];
  A = Table[
    Simplify[avector /.  $\theta \rightarrow \theta[[k]]$ ]
    , {k, m}];
  (* compute Fourier-Bessel coefficients *)
  c = LeastSquares[A,  $\sigma$ ];
  (* approximation function *)
  Clear[f];
  f[ $\theta$ _] = c.avector;
  (* approximation vector *)
  F = f[ $\theta$ ] /.  $\theta \rightarrow \theta$ ;
  (* residual error *)
  r =  $\sigma$  - F;
  R = { $\theta$ , r}T;

```

```

(* total error *)
r2 = r.r;
(* uncertainty propagation *)

$$\epsilon = \sqrt{\frac{r2}{m - (d + 1)} \text{Diagonal}[\text{Inverse}[A^H.A // N]]}$$
;
(* signal to noise *)

$$\gamma = \frac{\text{Last}[c]}{\text{Last}[\epsilon]}$$
;
(* function *)
g001 = Plot[f[θ], {θ, -π, π},
  Frame → True,
  FrameTicks → fticks,
  PlotStyle → {Opacity[0.25], Blue}];
(* bar chart *)
gbars = BarChart[c,
  Frame → True,
  PlotLabel → "Amplitudes for d = "<>ToString[d]<>lf<>subtitle,
  ChartStyle → {{Blue}, {Opacity[0.1]}},
  FrameTicks → {{Automatic, Automatic}, {Table[
    {k + 1, Subscript["a", k]}
    , {k, 0, d}], Automatic}},
  ipad, isize];
(* compare data to fit *)
dsubtitle = subtitle<>" , d = "<>ToString[d];
ga = Show[{g001, g000},
  PlotLabel → sty["MoM RCS vs Fourier Cosine Expansion"<>lf<>dsubtitle],
  FrameLabel → {sty["Yaw angle, α"], sty["Mean total RCS, <σT>"]},
  FrameTicks → fticks,
  PlotRange → {bot, top},
  isize, ipad];
(* residual error *)
gb = ListPlot[R,
  Frame → True,
  FrameTicks → fticks,
  FrameLabel → {sty["Yaw angle, α"], sty["Residual error"]},
  (* PlotRange → {-1, 1}, *)
  PlotStyle → {Red, PointSize[0.005]},
  PlotLabel → sty["Fourier Approximation Error"<>lf<>dsubtitle],
  isize, ipad];
(* bar chart *)
gbars = BarChart[c,
  Frame → True,

```

```

PlotLabel → "Amplitudes for  $d =$ " <> ToString[d] <> lf <> subtitle,
ChartStyle → {{Blue}, {Opacity[0.1]}}},
FrameTicks → {{Automatic, Automatic}, {Table[
    {k + 1, Subscript["a", k]}
    , {k, 0, d}], Automatic}}},
    ipad, isize];
(* amplitudes with errors *)
ebars = Table[
    {k - 1, Around[c[[k]], e[[k]]]}
    , {k, Length[c]}}];
gebars = ListPlot[ebars,
    isize,
    Frame → True,
    FrameTicks → {{Automatic, Automatic},
        {Table[{k, Subscript["a", k]}, {k, 0, Length[ebars]}], Automatic}},
    PlotLabel → "Amplitudes with errors for  $d =$ " <> ToString[d] <> lf <> subtitle,
    PlotStyle → Blue,
    PlotRange → {{-0.5, d + 0.5}, Full},
    isize, ipad];
(* group plots *)
gout = GraphicsGrid[{{ga, gb}, {gbars, gebars}},
    ImageSize → 12 × 72]
, {v, 3, 30, 1}, {d, 0, 25, 1}]

```

