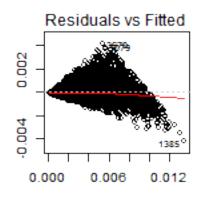
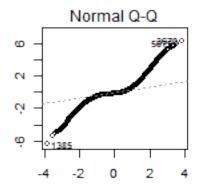
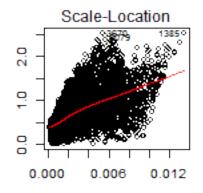
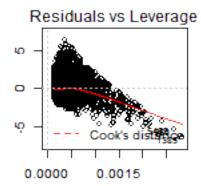
## 1 Risk $\sim \log(\text{Parameters})$

```
## Number of independent variables= 1
## lm(formula = data$Risk ~ as.matrix(data_temp))
## Residuals:
        Min
                   1Q
                         Median
                                       3Q
## -0.004124 -0.000192 -0.000109 0.000102 0.004112
##
## Coefficients:
                       Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                       1.35e-04
                                 1.03e-05
                                                13
## as.matrix(data_temp) 3.89e-09
                                 1.18e-11
                                               328
                                                     <2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.000644 on 7075 degrees of freedom
## Multiple R-squared: 0.938, Adjusted R-squared: 0.938
## F-statistic: 1.08e+05 on 1 and 7075 DF, p-value: <2e-16
##
        R2 Adj_R2
                       RSS
                               ESS
## 3 0.9385 0.9385 0.002937 0.04479
```

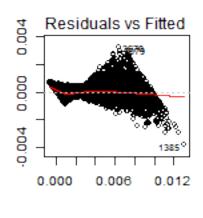


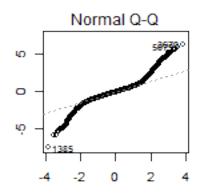


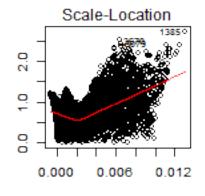


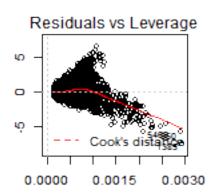


```
## Number of independent variables= 2
## Call:
## lm(formula = data$Risk ~ as.matrix(data_temp))
## Residuals:
##
        Min
                   1Q
                         Median
                                       3Q
## -0.003747 -0.000254 -0.000021 0.000222 0.003198
## Coefficients:
                                Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                                1.79e-03
                                          2.57e-05
                                                       69.6 <2e-16 ***
## as.matrix(data_temp)rho
                               -8.49e-07
                                           1.25e-08
                                                      -67.8
## as.matrix(data_temp)Mass.utf 3.97e-09
                                           9.29e-12
                                                      427.1
                                                              <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.000502 on 7074 degrees of freedom
## Multiple R-squared: 0.963, Adjusted R-squared: 0.963
## F-statistic: 9.13e+04 on 2 and 7074 DF, p-value: <2e-16
##
        R2 Adj_R2
                      RSS
                              ESS
## 2 0.9627 0.9627 0.00178 0.04595
```



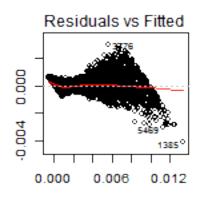


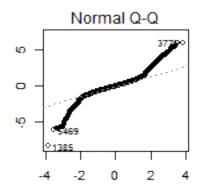


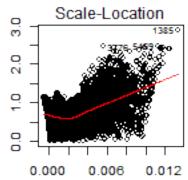


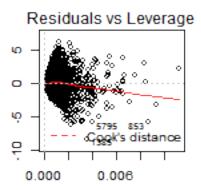
```
## Number of independent variables= 3
## Call:
## lm(formula = data$Risk ~ as.matrix(data_temp))
```

```
## Residuals:
                          Median
         Min
                    1Q
                                        3Q
## -0.004025 -0.000242 -0.000014 0.000217 0.002910
## Coefficients:
##
                                 Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                 1.54e-03
                                            2.67e-05
                                                        57.7
                                                                <2e-16 ***
                                            1.30e-08
## as.matrix(data_temp)rho
                                -7.31e-07
                                                       -56.2
                                                                <2e-16 ***
## as.matrix(data_temp)Mass.utf 3.48e-09
                                            2.25e-11
                                                        154.7
                                                                <2e-16 ***
## as.matrix(data_temp)Mass.w
                                 3.73e-07
                                            1.56e-08
                                                        24.0
                                                               <2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.000482 on 7073 degrees of freedom
## Multiple R-squared: 0.966, Adjusted R-squared: 0.966
## F-statistic: 6.6e+04 on 3 and 7073 DF, p-value: <2e-16
##
                        RSS
                                ESS
         R2 Adj_R2
## 5 0.9655 0.9655 0.001646 0.04608
```



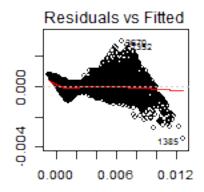


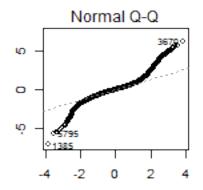


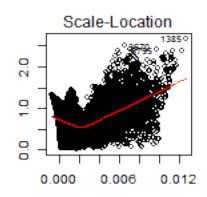


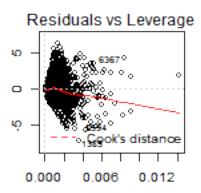
```
## Number of independent variables= 4
## Call:
## lm(formula = data$Risk ~ as.matrix(data_temp))
##
## Residuals:
```

```
Min 1Q Median
  -0.003397 -0.000235 -0.000010 0.000200 0.002975
##
## Coefficients:
##
                               Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                               1.99e-03
                                          2.73e-05
                                                      73.1
                                                             <2e-16 ***
## as.matrix(data_temp)rho
                              -7.79e-07
                                          1.21e-08
                                                     -64.2
                                                            <2e-16 ***
## as.matrix(data_temp)Mass.f
                               4.30e-10
                                          1.72e-11
                                                     25.0 <2e-16 ***
## as.matrix(data_temp)Mass.utf 3.73e-09
                                          1.31e-11
                                                     284.2
                                                           <2e-16 ***
## as.matrix(data_temp)ach
                              -2.25e-04
                                          8.83e-06
                                                     -25.4
                                                            <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.000472 on 7072 degrees of freedom
## Multiple R-squared: 0.967, Adjusted R-squared: 0.967
## F-statistic: 5.17e+04 on 4 and 7072 DF, p-value: <2e-16
##
##
        R2 Adj_R2
                       RSS
## 2 0.9669 0.9669 0.001578 0.04615
```



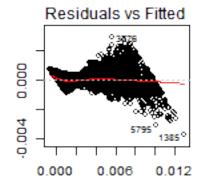


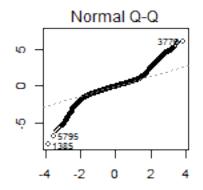


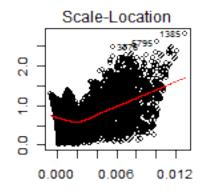


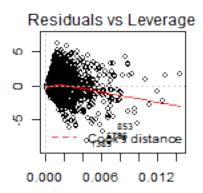
```
## Number of independent variables= 5
## Call:
## lm(formula = data$Risk ~ as.matrix(data_temp))
##
## Residuals:
## Min 1Q Median 3Q Max
```

```
## -0.003661 -0.000231 -0.000009 0.000201 0.002839
##
## Coefficients:
##
                                Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                1.77e-03
                                           2.88e-05
                                                       61.3
                                                             <2e-16 ***
                                                             <2e-16 ***
## as.matrix(data_temp)rho
                               -6.93e-07
                                           1.26e-08
                                                      -55.0
## as.matrix(data_temp)Mass.f
                                3.79e-10
                                           1.69e-11
                                                       22.4
                                                             <2e-16 ***
## as.matrix(data_temp)Mass.utf 3.36e-09
                                          2.25e-11
                                                      149.2
                                                             <2e-16 ***
## as.matrix(data_temp)Mass.w
                                2.98e-07
                                           1.51e-08
                                                      19.7
                                                              <2e-16 ***
## as.matrix(data_temp)ach
                                                      -22.5
                               -1.96e-04
                                           8.72e-06
                                                              <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.00046 on 7071 degrees of freedom
## Multiple R-squared: 0.969, Adjusted R-squared: 0.969
## F-statistic: 4.37e+04 on 5 and 7071 DF, p-value: <2e-16
##
##
        R2 Adj_R2
                       RSS
## 1 0.9687 0.9686 0.001496 0.04623
```



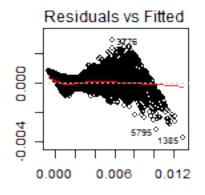


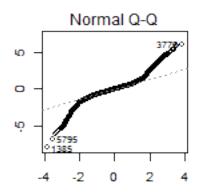


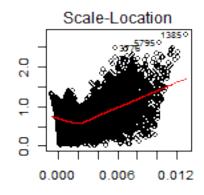


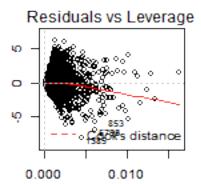
```
## Number of independent variables= 6
## Call:
## lm(formula = data$Risk ~ as.matrix(data_temp))
##
## Residuals:
## Min 1Q Median 3Q Max
```

```
## -0.003654 -0.000231 -0.000009 0.000201 0.002817
##
## Coefficients:
##
                                Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                1.84e-03
                                          3.18e-05
                                                     57.88 < 2e-16 ***
## as.matrix(data_temp)rho
                               -6.84e-07
                                           1.27e-08 -54.01 < 2e-16 ***
## as.matrix(data_temp)Mass.f
                                4.33e-10
                                           1.96e-11
                                                      22.13 < 2e-16 ***
## as.matrix(data_temp)Mass.utf 3.33e-09
                                          2.33e-11 143.17 < 2e-16 ***
## as.matrix(data_temp)Mass.w
                                2.99e-07
                                           1.51e-08
                                                     19.84 < 2e-16 ***
## as.matrix(data_temp)ach
                               -2.08e-04
                                           8.98e-06 -23.21
                                                            < 2e-16 ***
## as.matrix(data_temp)p
                               -1.44e-04
                                          2.65e-05
                                                      -5.44 5.7e-08 ***
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.000459 on 7070 degrees of freedom
## Multiple R-squared: 0.969, Adjusted R-squared: 0.969
## F-statistic: 3.66e+04 on 6 and 7070 DF, p-value: <2e-16
##
                      RSS
                              ESS
        R2 Adj_R2
## 1 0.9688 0.9688 0.00149 0.04624
```









ggplot