# robo rally

May 25, 2020

## 1 Robo Rally

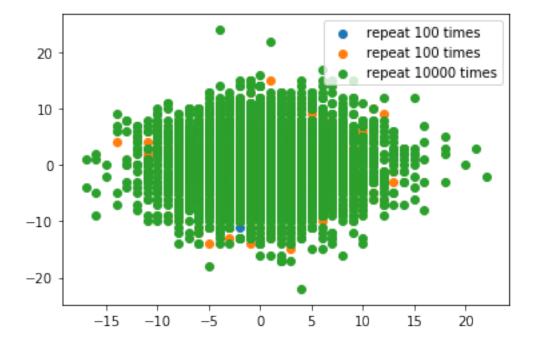
```
[1]: import random as rd
import numpy aas np
import math
import matplotlib.pyplot as plt
%matplotlib inline
```

## 2 Original game

```
[2]: def roborally(x=0,y=0,limit=100):
         Move=['G','R','L']
         #G move 1 ,R turn right ,L turn left
         K=rd.randrange(5,limit,1)
         #k instructions ranging farom 5 to 100
         N,E,S,W=0,1,2,3
         dir= E
         #initial direction East
         seq=[]
         for i in range(K):
             seq.append(rd.choice(Move))
         #print(seq)
         for m in seq:
             if m == 'R':
                 dir = (dir + 1)\%4
             elif m == 'L':
                 dir = (4 + dir - 1)\%4
             else:
                     # if move == 'G'
                     if dir == N:
                         y += 1
                     elif dir == E:
                         x += 1
```

#### 2.1 Visualize the spread of robot's ending position

```
[39]: test=[100,1000,10000]
    rest=np.array([roborally() for i in range(test[0])])
    x,y=rest.T
    rest1=np.array([roborally() for i in range(test[1])])
    x1,y1=rest1.T
    rest2=np.array([roborally() for i in range(test[2])])
    x2,y2=rest2.T
    plt.scatter(x, y,label='repeat 100 times')
    plt.scatter(x1, y1,label='repeat 100 times')
    plt.scatter(x2, y2,label='repeat 10000 times')
    plt.legend()
    plt.show()
```



```
[42]: rest=np.array([roborally() for i in range(100000)])
x,y=rest.T
print(max(abs(x)),max(abs(y)))
```

```
[43]: #repeat 1000000 times
rest=np.array([roborally() for i in range(1000000)])
x,y=rest.T
print(max(abs(x)),max(abs(y)))
```

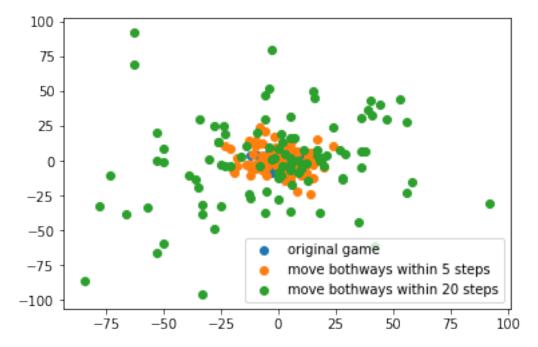
30 28

If we repeat the game 1000000 times, the range may extend to above 24-30 range. Thus the probability of the robot falling off the board does depend on the size of the board.

## 3 Extended project 1: move more than 1 step is allowed

```
[3]: def roborally1(x=0,y=0,limit=100,step=5):
         Move=['G','R','L']
         #G move 1 ,R turn right ,L turn left
         K=rd.randrange(5,limit,1)
         #k instructions ranging from 5 to 100
         N,E,S,W=0,1,2,3
         dir= E
         #initial direction East
         seq=[]
         for i in range(K):
             seq.append(rd.choice(Move))
         #print(seq)
         for m in seq:
             s=rd.randrange(-step, step, 1)
             #move forward or backward more than one
             if m == 'R':
                 dir = (dir + 1)\%4
             elif m == 'L':
                 dir = (4 + dir - 1)\%4
                     # if move == 'G'
             else:
                     if dir == N:
                         y += s
                     elif dir == E:
                         x += s
                     elif dir == S:
                         y -= s
                     else:
                         x -= s
         return [x,y]
```

```
[15]: test=100
    rest=np.array([roborally() for i in range(test)])
    x,y=rest.T
    rest1=np.array([roborally1() for i in range(test)])
    x1,y1=rest1.T
    rest2=np.array([roborally1(step=20) for i in range(test)])
    x2,y2=rest2.T
    plt.scatter(x, y,label='original game')
    plt.scatter(x1, y1,label='move bothways within 5 steps')
    plt.scatter(x2, y2,label='move bothways within 20 steps')
    plt.legend()
    plt.show()
```



Obviously larger the step size, wider the range.

# 4 Extended project 2: rotation less than a quarter is allowed

```
[23]: def roborally2(x=0,y=0,limit=100,step=5):

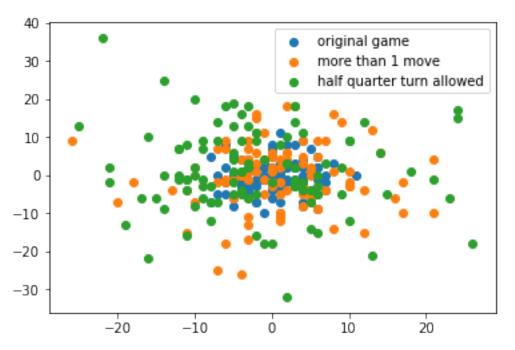
Move=['G','R','L']
#G move 1 ,R turn right ,L turn left
K=rd.randrange(5,limit,1)
#k instructions ranging from 5 to 100
N,NE,E,SE,S,SW,W,NW=0,1,2,3,4,5,6,7
```

```
dir= E
#initial direction East
seq=[]
for i in range(K):
    seq.append(rd.choice(Move))
#print(seq)
for m in seq:
    s=rd.randrange(-step,step,1)
    #move both ways more than 1
    if m == 'R':
        dir = (dir + 1)\%8
    elif m == 'L':
        dir = (8 + dir - 1)\%8
            # if move == 'G'
    else:
            if dir == N:
                y += s
            elif dir == E:
                x += s
            elif dir == S:
                y -= s
            elif dir == W:
                x -= s
            elif dir == NE:
                y += s
                x += s
            elif dir == SE:
                y -=s
                x +=s
            elif dir == SW:
                y-=s
                x-=s
            else :
                y += s
                x-=s
return [x,y]
```

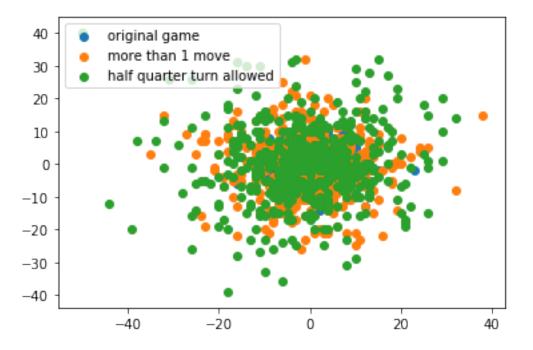
## 4.1 Visualize the spread of ending positions of three scenarios

```
[24]: test=100
    rest=np.array([roborally() for i in range(test)])
    x,y=rest.T
    rest1=np.array([roborally1() for i in range(test)])
    x1,y1=rest1.T
    rest2=np.array([roborally2() for i in range(test)])
```

```
x2,y2=rest2.T
plt.scatter(x, y,label='original game')
plt.scatter(x1, y1,label='more than 1 move')
plt.scatter(x2, y2,label='half quarter turn allowed')
plt.legend()
plt.show()
```



```
[25]: test=500
    rest=np.array([roborally() for i in range(test)])
    x,y=rest.T
    rest1=np.array([roborally1() for i in range(test)])
    x1,y1=rest1.T
    rest2=np.array([roborally2() for i in range(test)])
    x2,y2=rest2.T
    plt.scatter(x, y,label='original game')
    plt.scatter(x1, y1,label='more than 1 move')
    plt.scatter(x2, y2,label='half quarter turn allowed')
    plt.legend()
    plt.show()
```



With the same step size, smaller the rotation angle ,wider the move range.

# 5 Extended project 3: See the probability of hitting the hazard/taget

#### 5.0.1 Set random target within chosen range

```
[109]: def roborally_process(x=0,y=0,limit=100,step=5,r=15):
    #r stands for target/hazard range
    a,b=rd.randrange(-r,r,1),rd.randrange(-r,r,1)
    Move=['G','R','L']
    #G move 1 ,R turn right ,L turn left
    K=rd.randrange(5,limit,1)
    #k instructions ranging from 5 to 100
    N,E,S,W=0,1,2,3
    dir= E
    #initial direction East
    seq=[]

for i in range(K):
    seq.append(rd.choice(Move))
    #print(seq)

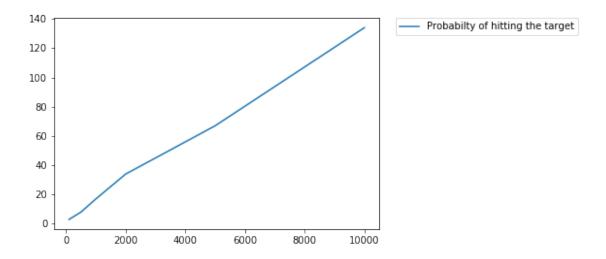
for m in seq:
```

```
s=rd.randrange(-step,step,1)
               #move forward or backward more than one
               if m == 'R':
                   dir = (dir + 1)\%4
               elif m == 'L':
                   dir = (4 + dir - 1)\%4
               else:
                       # if move == 'G'
                       if dir == N:
                           y += s
                       elif dir == E:
                           x += s
                       elif dir == S:
                           y -= s
                       else:
                           x -= s
               if x==a and y==b:
                   return 1
           return 0
[135]: repeat=[100,500,1000,2000,5000,10000]
       ans=[]
       for i in range(len(repeat)):
           sum=0
           for i in range(repeat[i]):
               sum+=roborally_process(limit=100)
           ans.append(sum)
       prob=[]
       for i in range(len(repeat)):
           prob.append(ans[i]/repeat[i])
```

```
[135]: 0.0178
```

np.mean(prob)

```
[136]: plt.plot(repeat,ans,label='Probabilty of hitting the target')
plt.legend(bbox_to_anchor=(1.05, 1), loc='upper left', borderaxespad=0.)
plt.show()
```

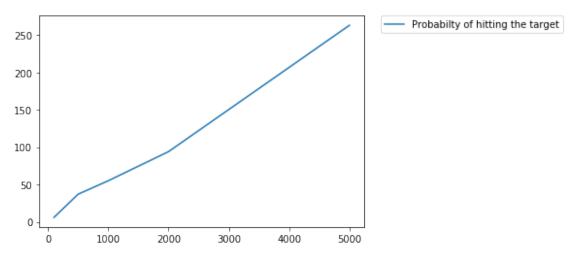


## 5.0.2 If each game with 100 sequence of moves, the probabilty of hitting the target is 0.0178

```
[126]: repeat=[100,500,1000,2000,5000]
    ans=[]
    for i in range(len(repeat)):
        sum=0
        for i in range(repeat[i]):
            sum+=roborally_process(limit=1000)
        ans.append(sum)

plt.plot(repeat,ans,label='Probabilty of hitting the target')
    plt.legend(bbox_to_anchor=(1.05, 1), loc='upper left', borderaxespad=0.)

plt.show()
```



```
[134]: prob=[]
for i in range(len(repeat)):
    prob.append(ans[i]/repeat[i])
np.mean(prob)
```

[134]: 0.05771999999999994

If each game with 1000 sequence of moves, the probabilty of hitting the target is 0.05771

We can see more frequent the moves, higer the chance of hitting target or hazard

[]: