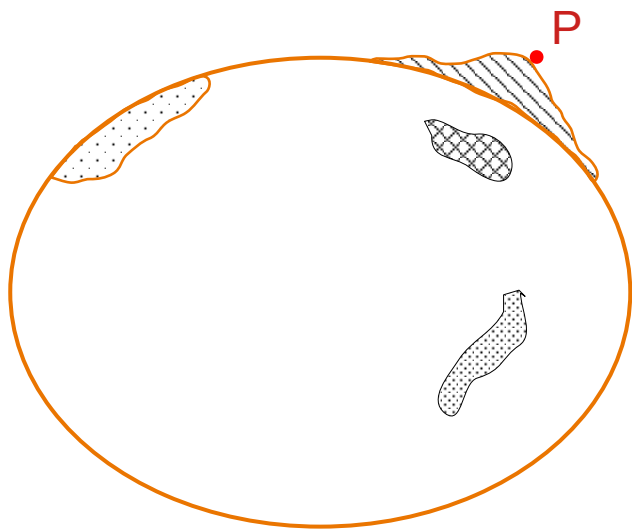


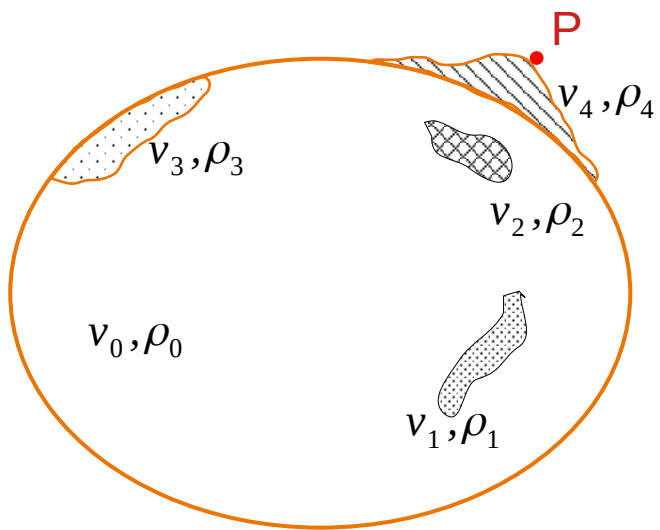
Integração de Métodos Geofísicos

Gravimetria – Parte 2

Terra Verdadeira



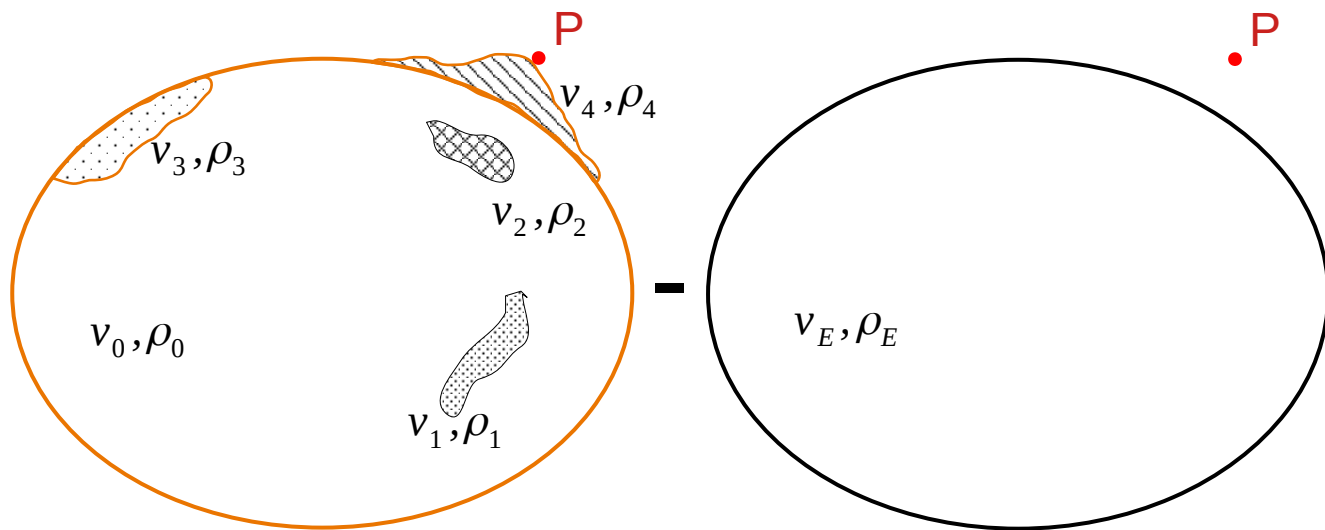
Terra Verdadeira



$$P = (x, y, z)$$

Terra Verdadeira

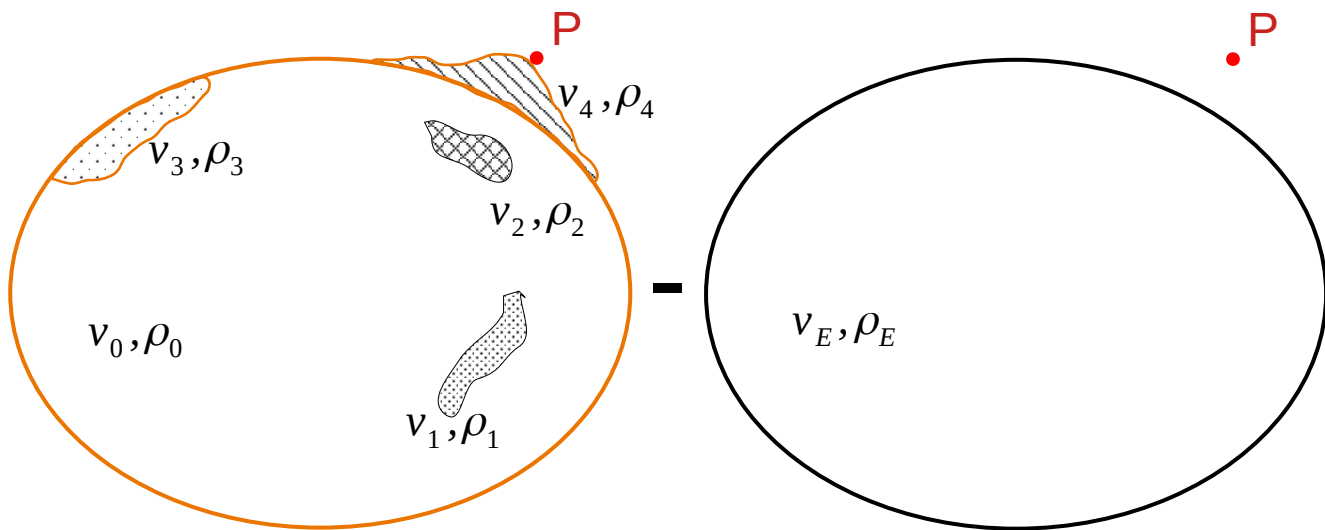
Terra Normal



$$P = (x, y, z)$$

Terra Verdadeira

Terra Normal

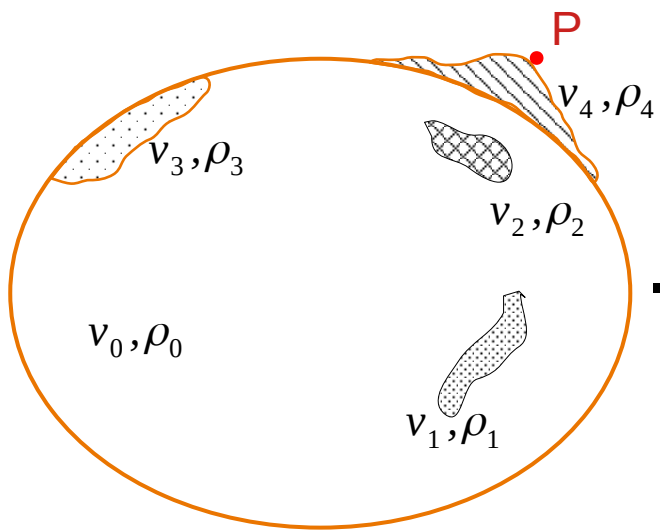


$$v_E = v_0 \cup v_1 \cup v_2 \cup v_3 \cup v_4$$

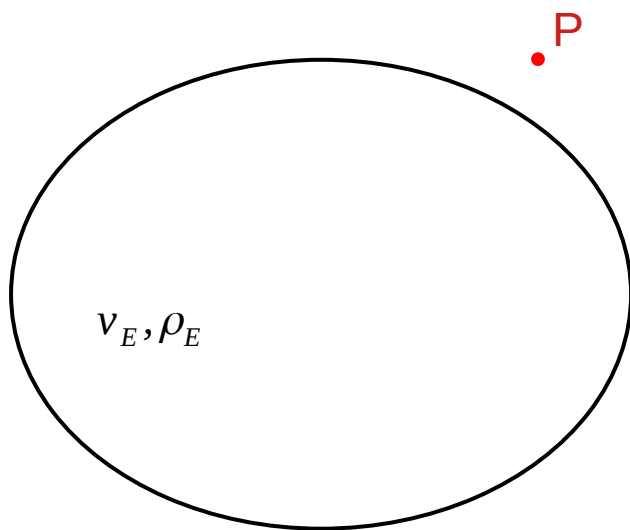
$P = (x, y, z)$



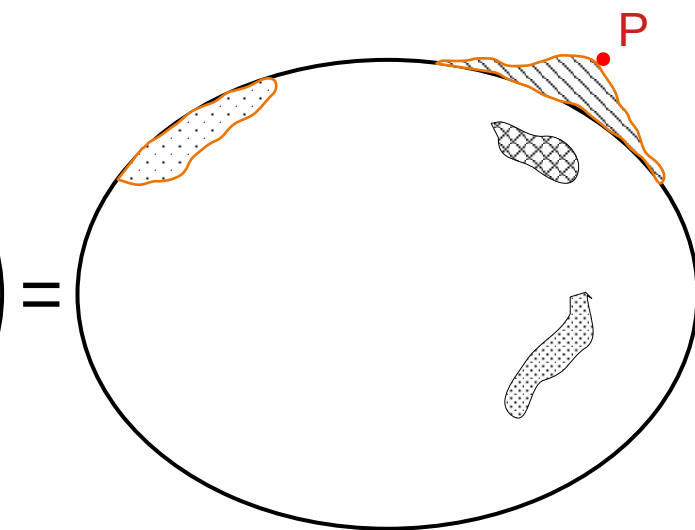
Terra Verdadeira



Terra Normal



Terra Verdadeira \ominus Terra Normal

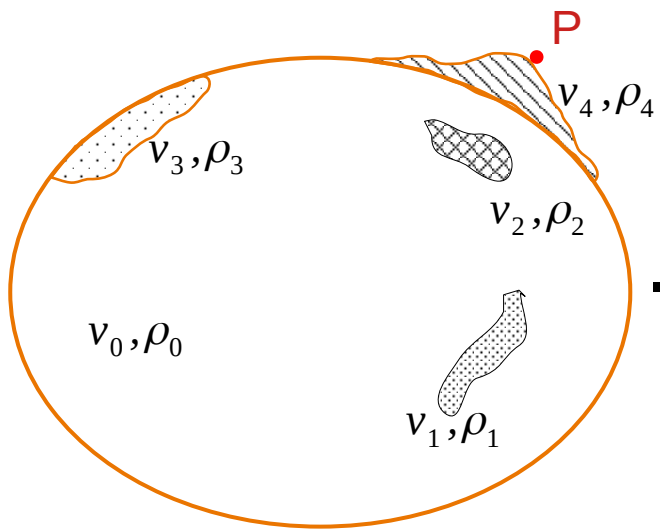


$$v_E = v_0 \cup v_1 \cup v_2 \cup v_3 \cup v_4$$

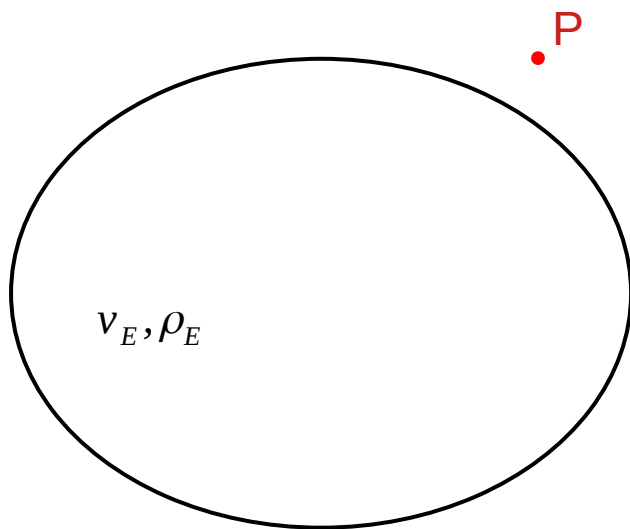
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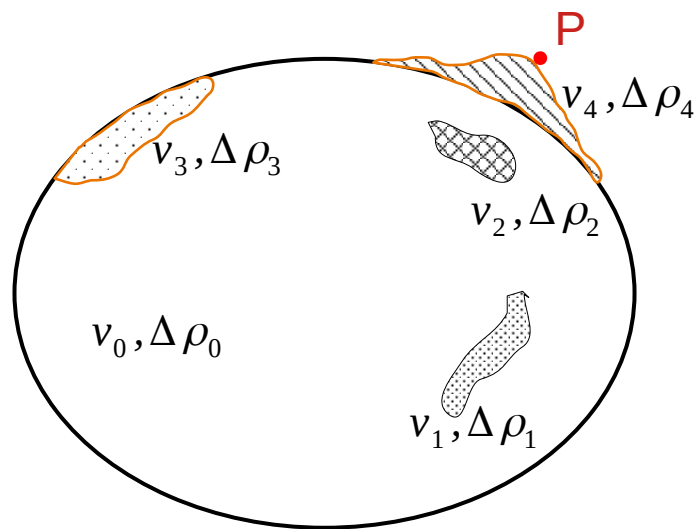
Terra Verdadeira



Terra Normal



Terra Verdadeira - Terra Normal

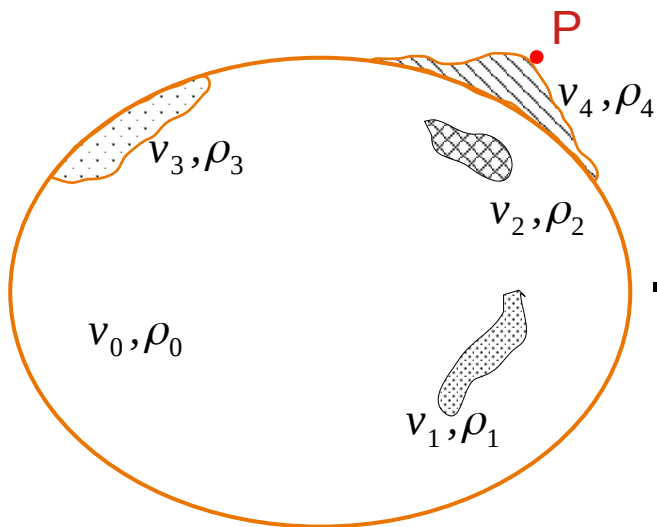


$$v_E = v_0 \cup v_1 \cup v_2 \cup v_3 \cup v_4$$

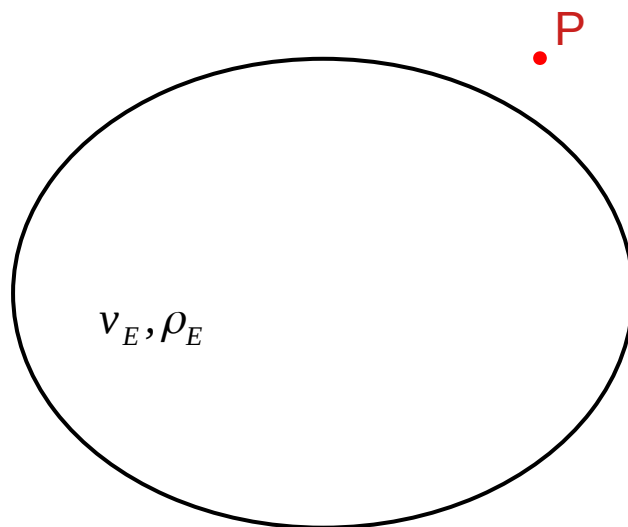
$P = (x, y, z)$



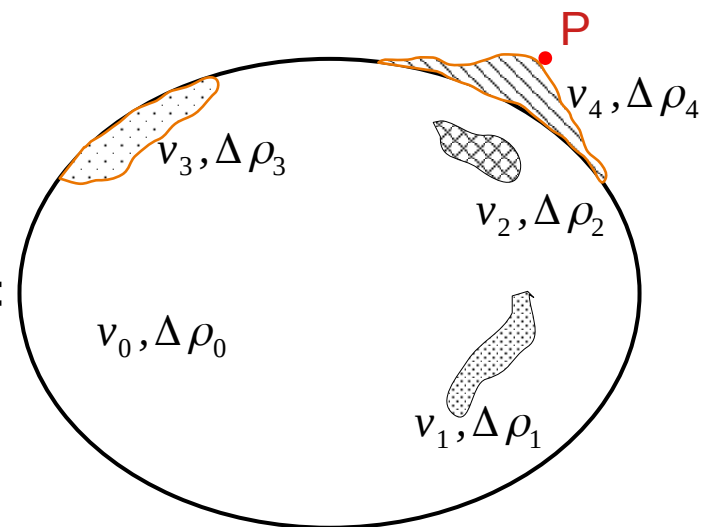
Terra Verdadeira



Terra Normal



Terra Verdadeira - Terra Normal



$$P = (x, y, z)$$

$$v_E = v_0 \cup v_1 \cup v_2 \cup v_3 \cup v_4$$



$$\square \quad \Delta \rho_0 = \rho_0 - \rho_E$$

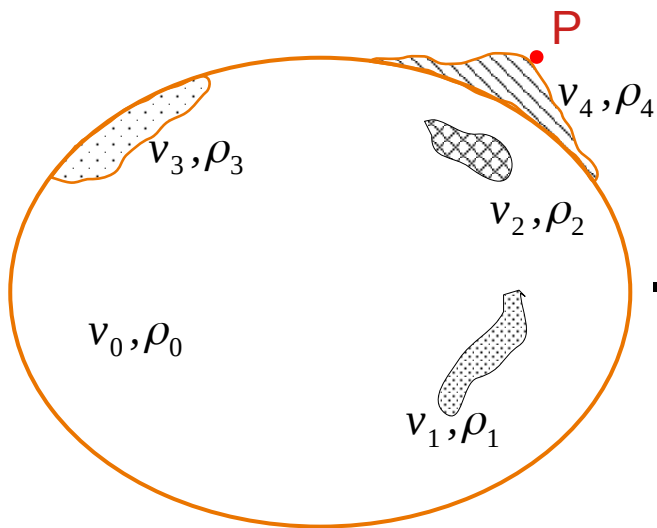
$$\text{dotted} \quad \Delta \rho_1 = \rho_1 - \rho_E$$

$$\text{cross-hatched} \quad \Delta \rho_2 = \rho_2 - \rho_E$$

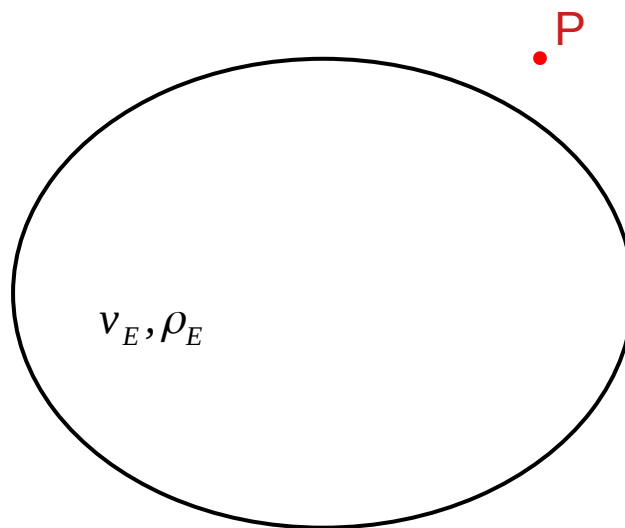
$$\text{dotted} \quad \Delta \rho_3 = \rho_3 - \rho_E$$

$$\text{diagonal lines} \quad \Delta \rho_4 = \rho_4 - 0 = \rho_4$$

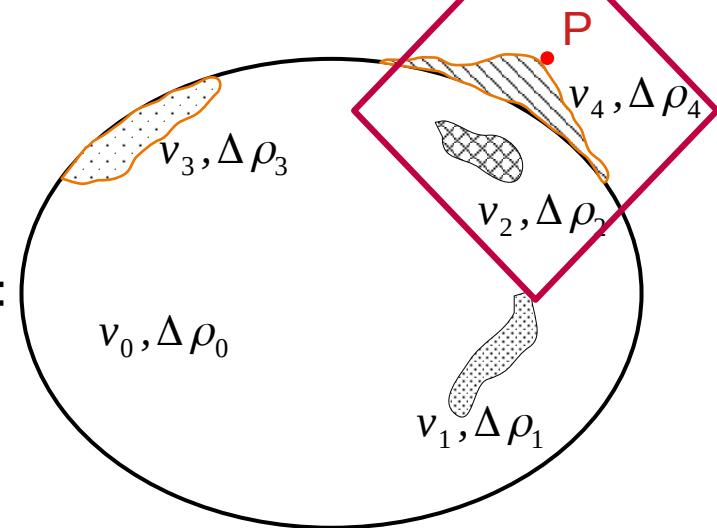
Terra Verdadeira



Terra Normal



Terra Verdadeira - Terra Normal



$P = (x, y, z)$

$$v_E = v_0 \cup v_1 \cup v_2 \cup v_3 \cup v_4$$



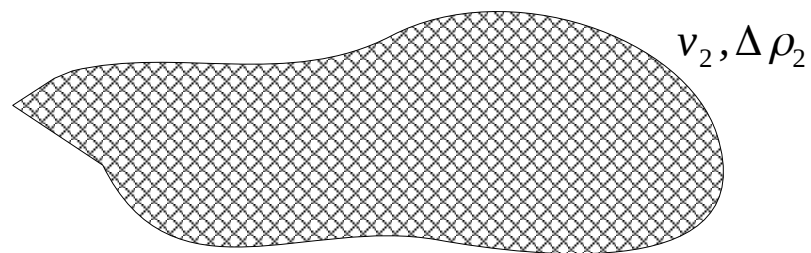
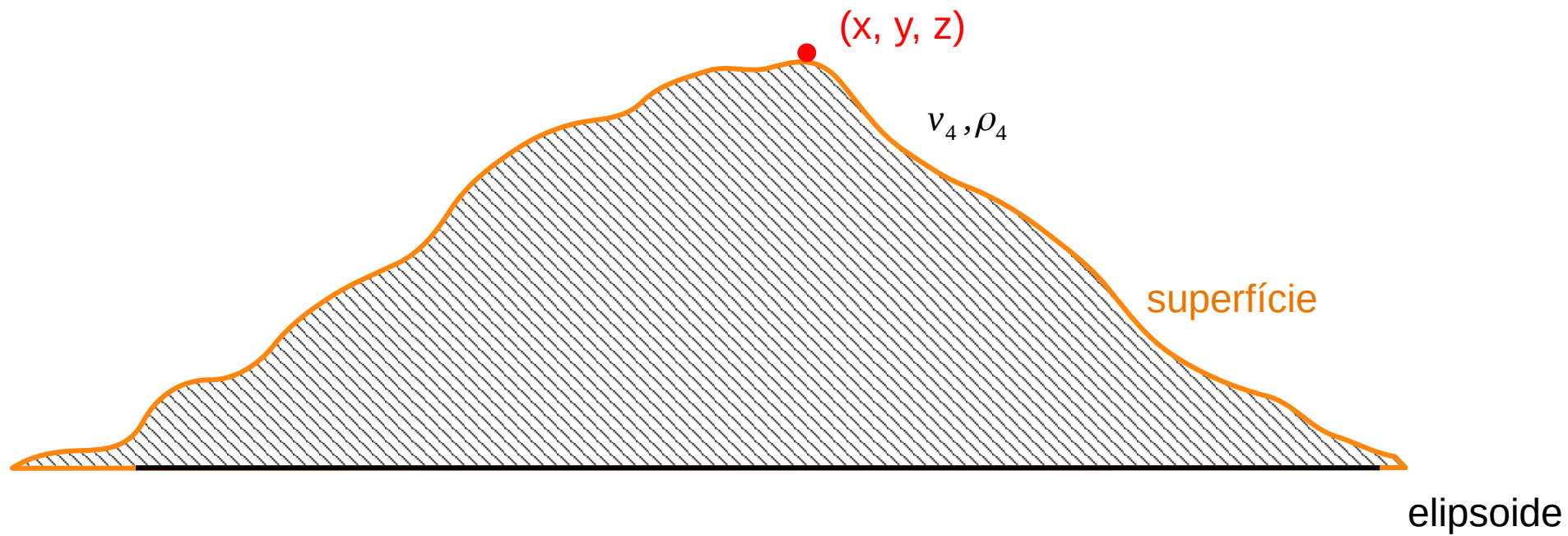
$$\square \quad \Delta \rho_0 = \rho_0 - \rho_E$$

$$\text{dotted} \quad \Delta \rho_1 = \rho_1 - \rho_E$$

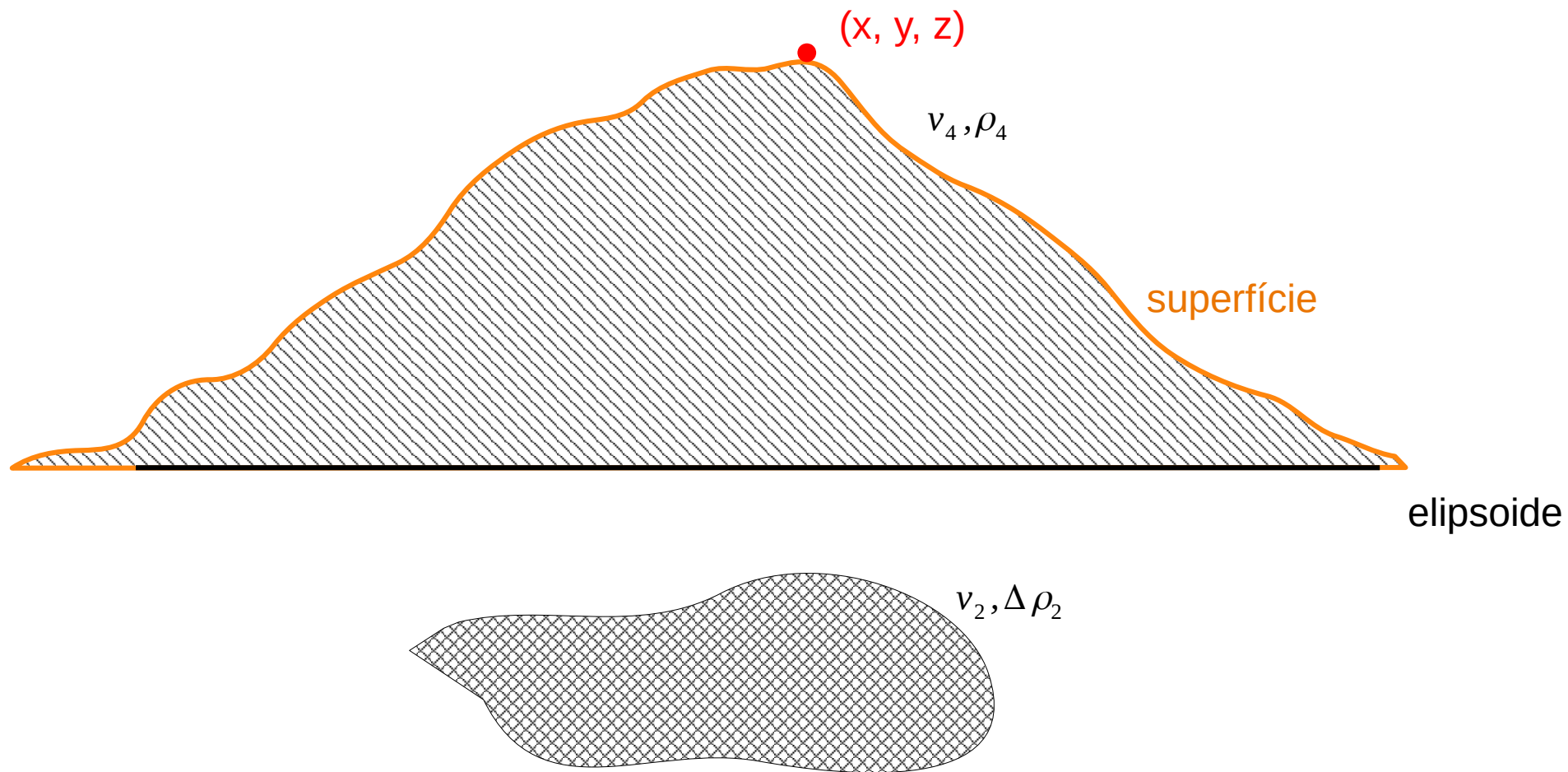
$$\text{cross-hatched} \quad \Delta \rho_2 = \rho_2 - \rho_E$$

$$\text{dotted} \quad \Delta \rho_3 = \rho_3 - \rho_E$$

$$\text{diagonal lines} \quad \Delta \rho_4 = \rho_4 - 0 = \rho_4$$

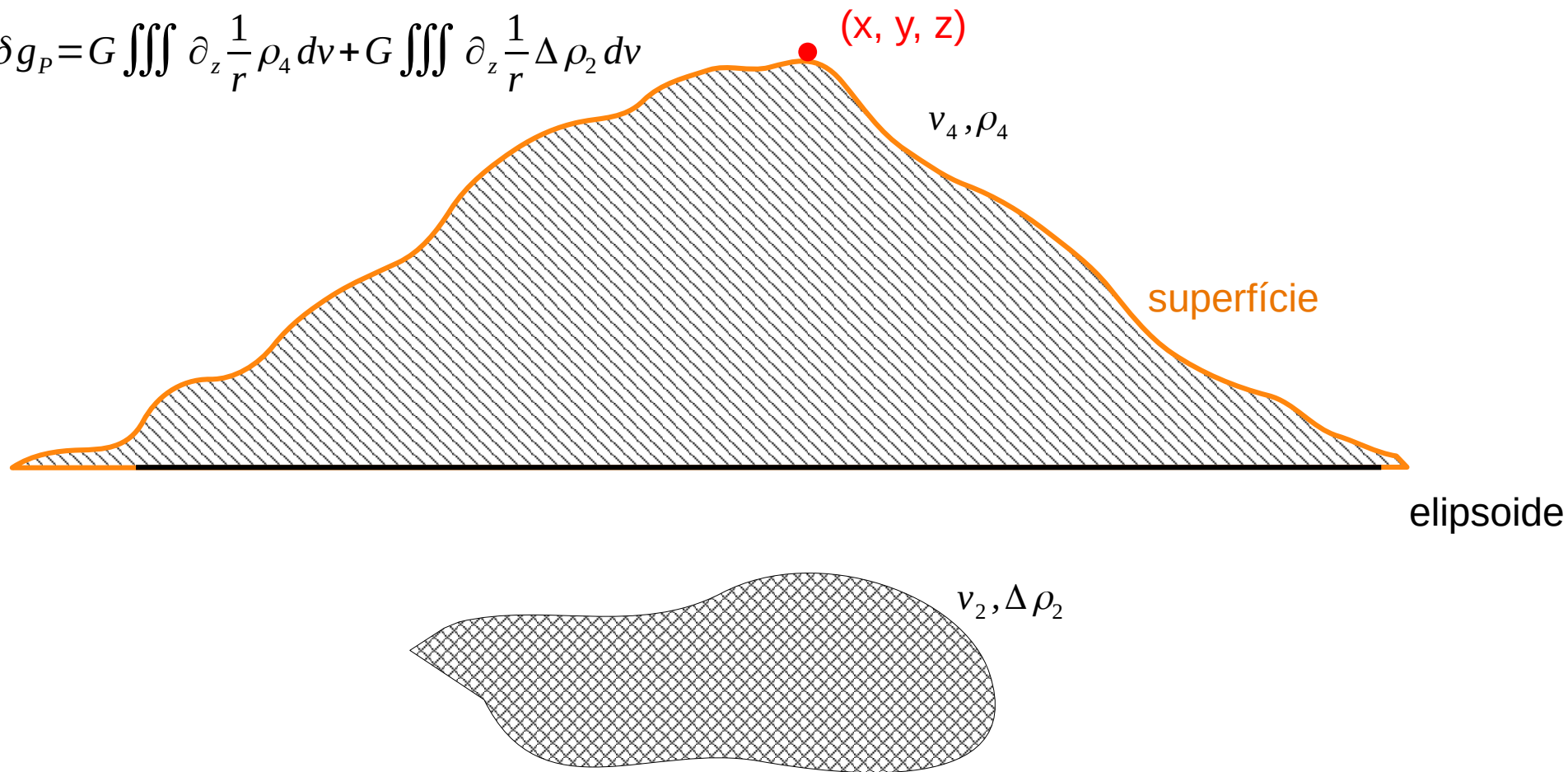


$$\delta g_P = g_P - \gamma_P$$



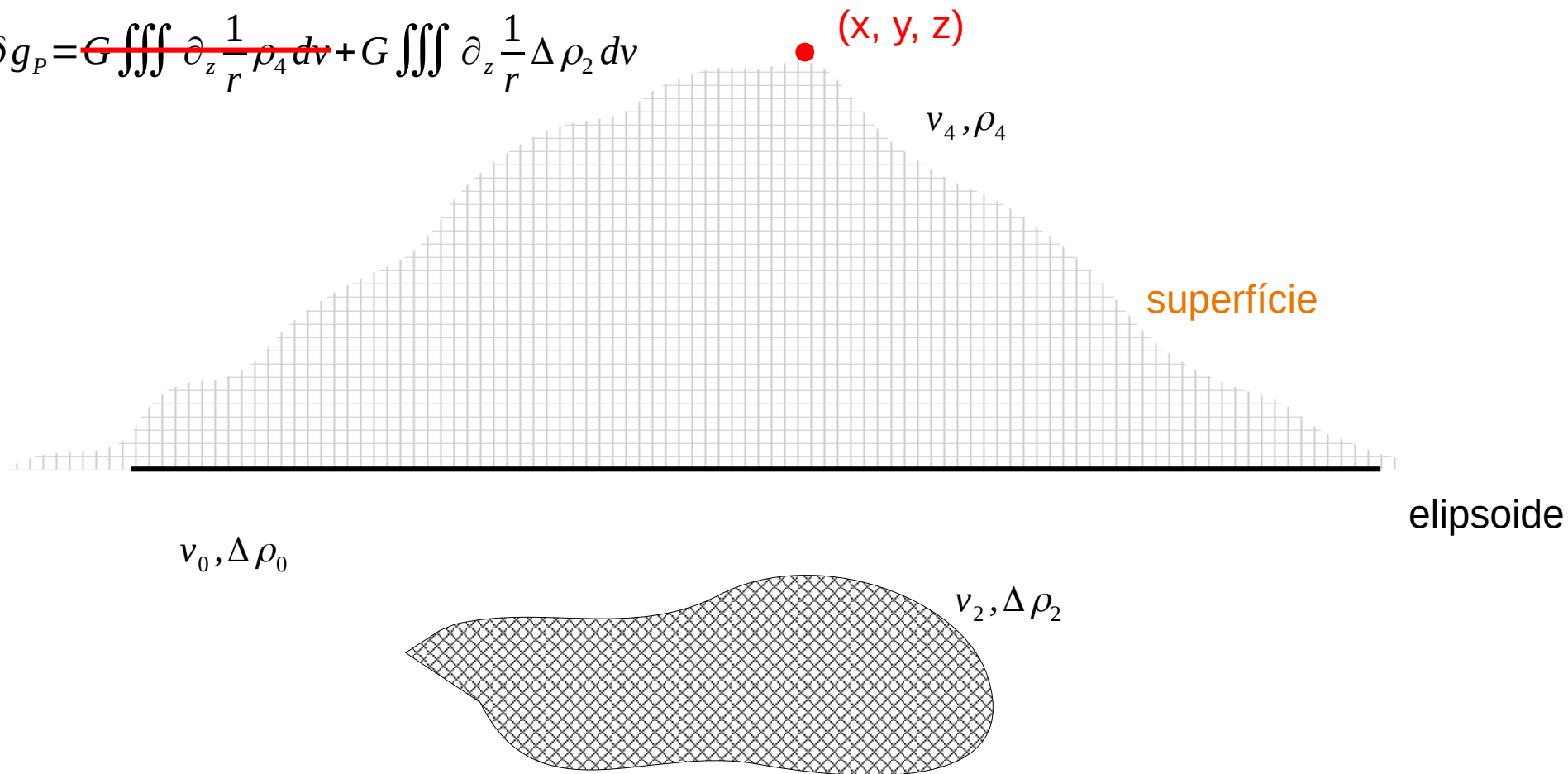
$$\delta g_P = g_P - \gamma_P$$

$$\delta g_P = G \iiint \partial_z \frac{1}{r} \rho_4 dv + G \iiint \partial_z \frac{1}{r} \Delta \rho_2 dv$$

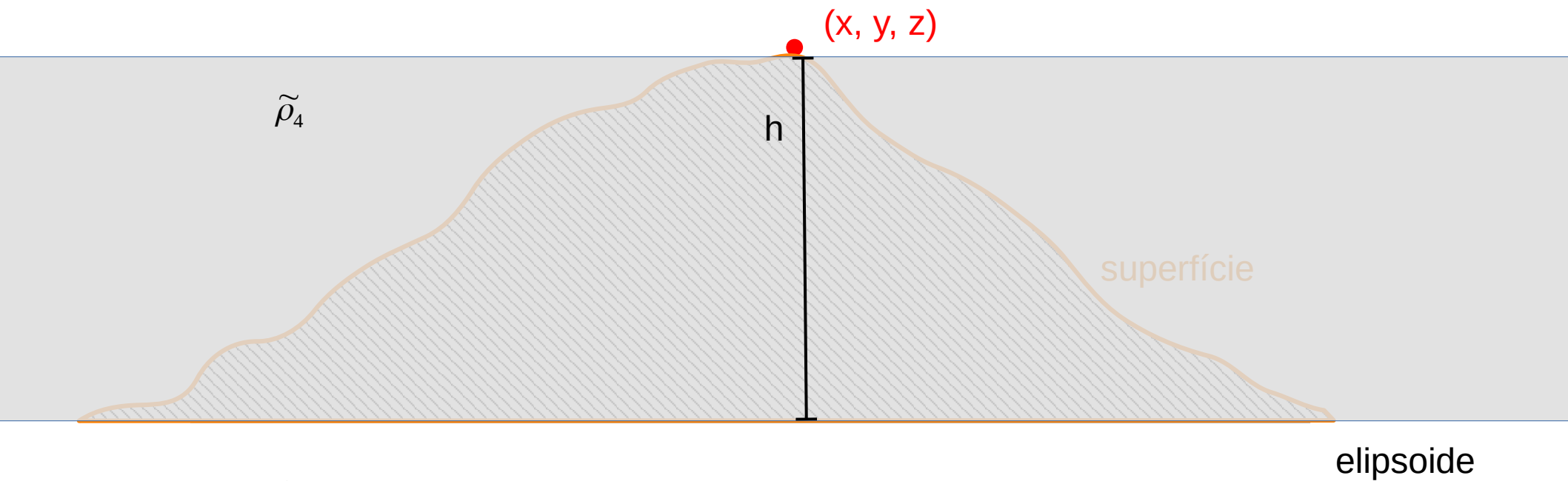


$$\delta g_P = g_P - \gamma_P$$

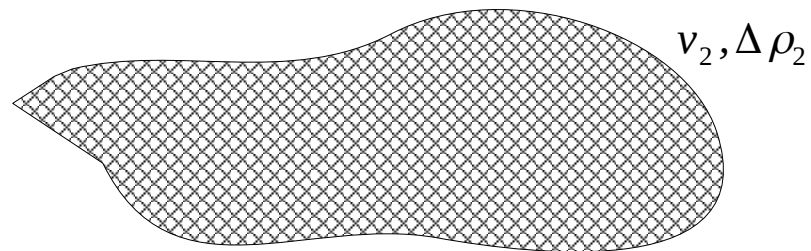
$$\delta g_P = G \iiint \cancel{\partial_z \frac{1}{r} \rho_4 dv} + G \iiint \partial_z \frac{1}{r} \Delta \rho_2 dv$$



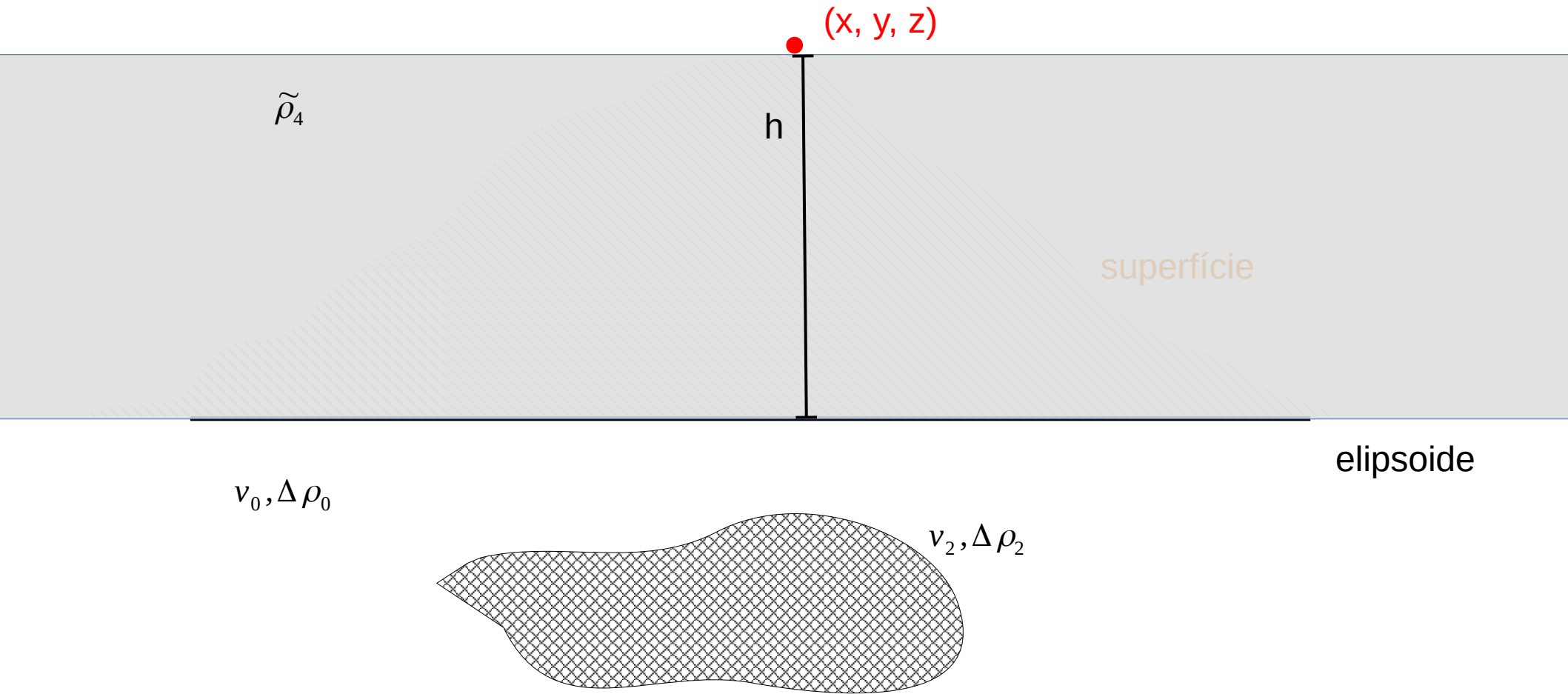
$$\delta g_P = g_P - \gamma_P$$



$v_0, \Delta \rho_0$



$$\delta g_P = g_P - \gamma_P - 2\pi G \tilde{\rho}_4 h$$



$$\delta g_P = g_P - \gamma_P - 2\pi G \tilde{\rho}_4 h$$

$\tilde{\rho}_4$

h

(x, y, z)

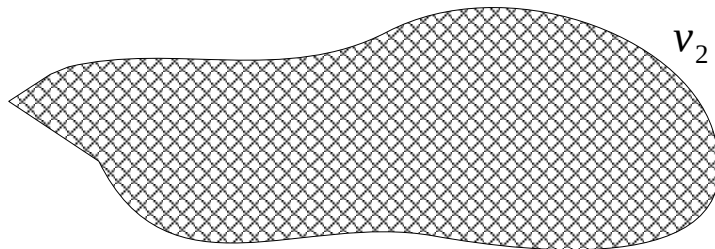
superfície

$$\delta g_P = \cancel{G \iiint \partial_z \frac{1}{r} \rho_4 dv} + G \iiint \partial_z \frac{1}{r} \Delta \rho_2 dv$$

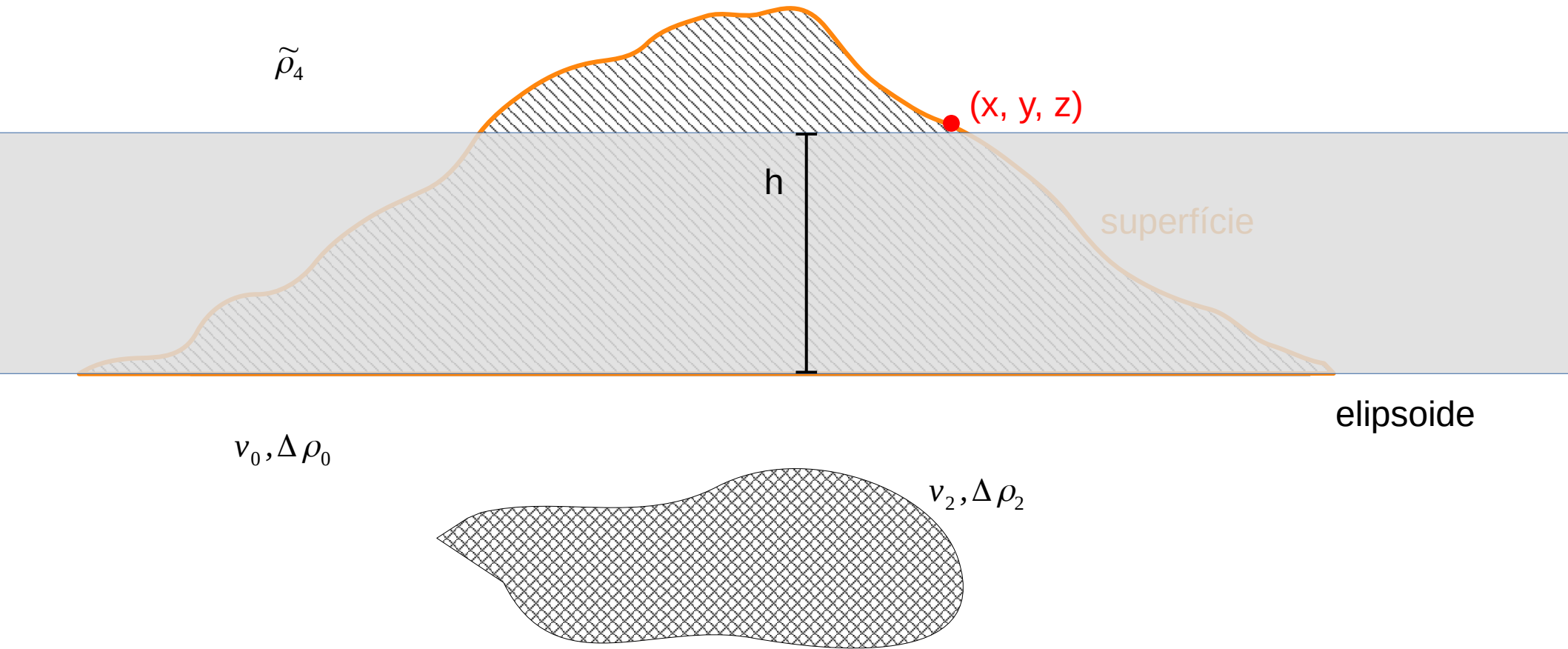
elipsoide

$v_0, \Delta \rho_0$

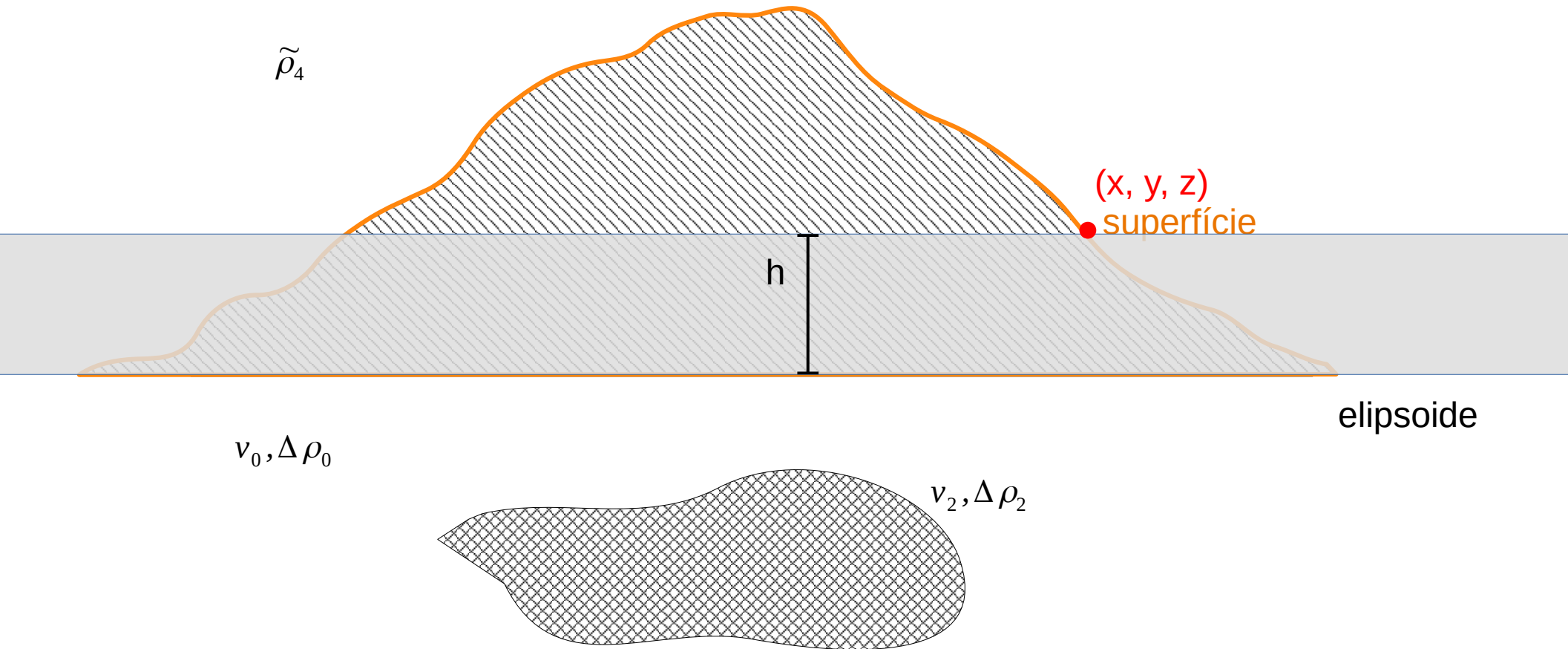
$v_2, \Delta \rho_2$



$$\delta g_P = g_P - \gamma_P - 2\pi G \tilde{\rho}_4 h$$

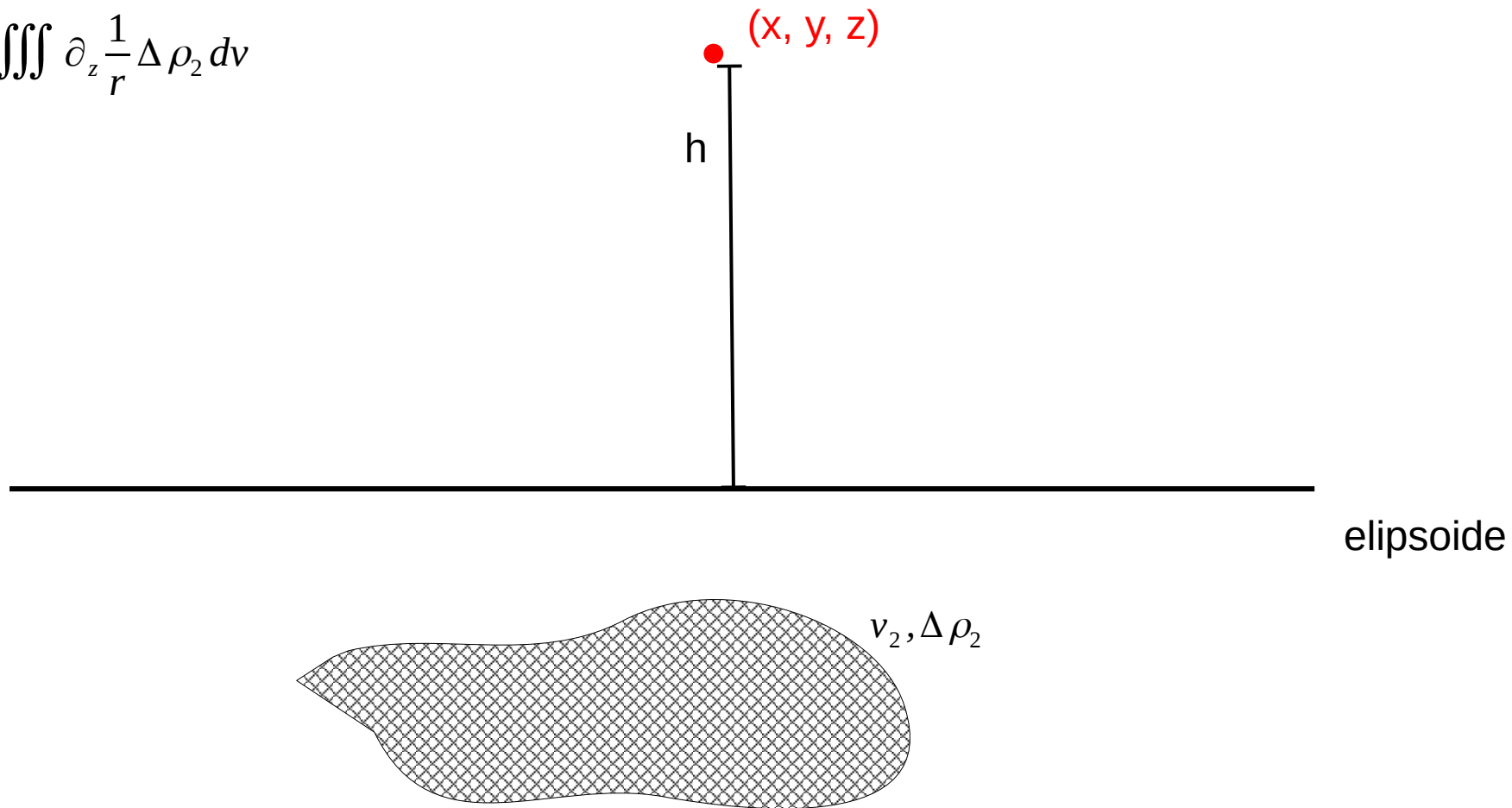


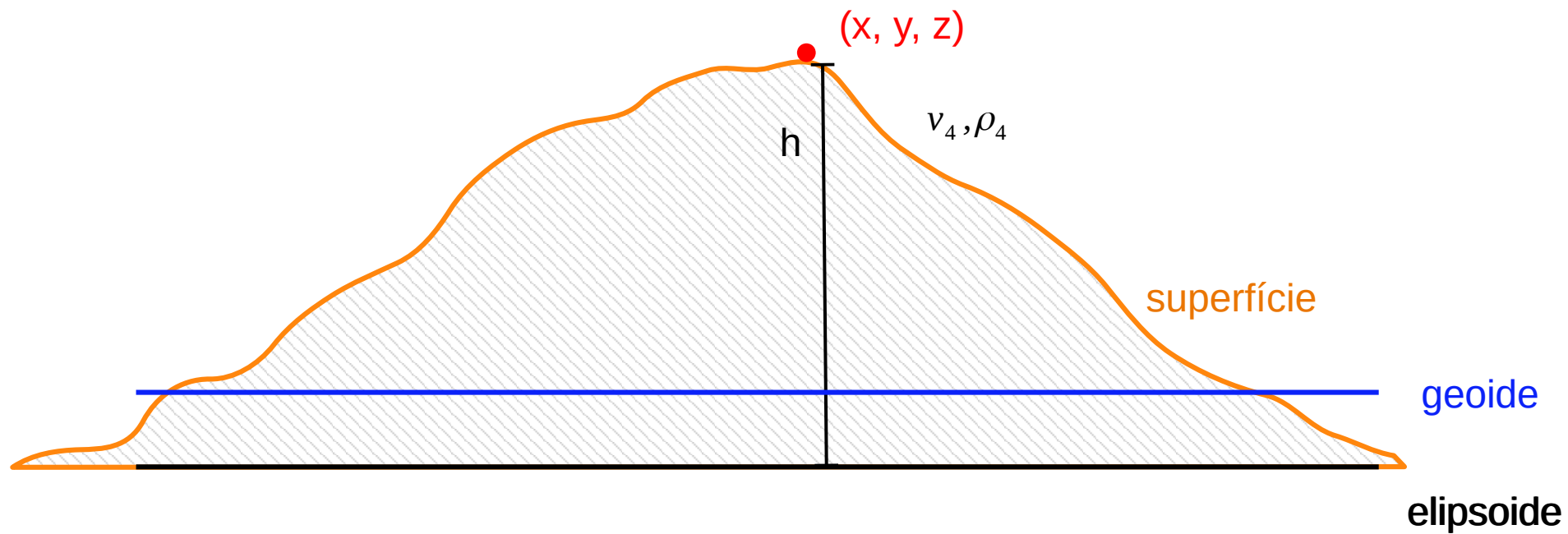
$$\delta g_P = g_P - \gamma_P - 2\pi G \tilde{\rho}_4 h$$

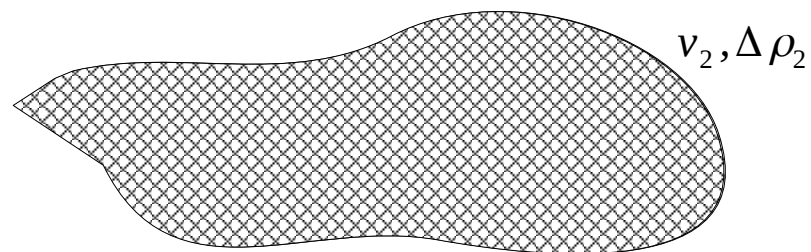
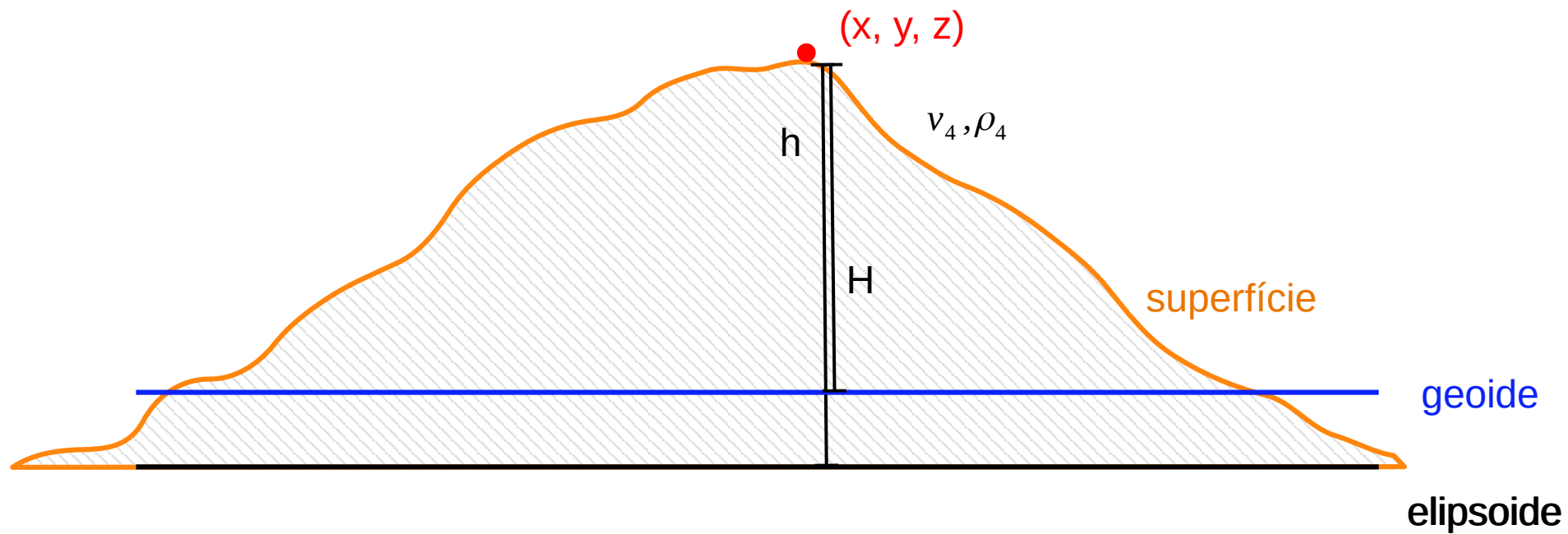


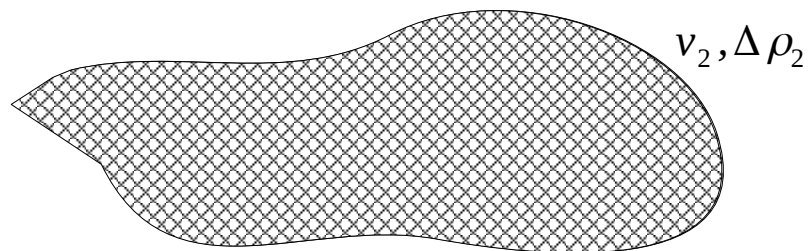
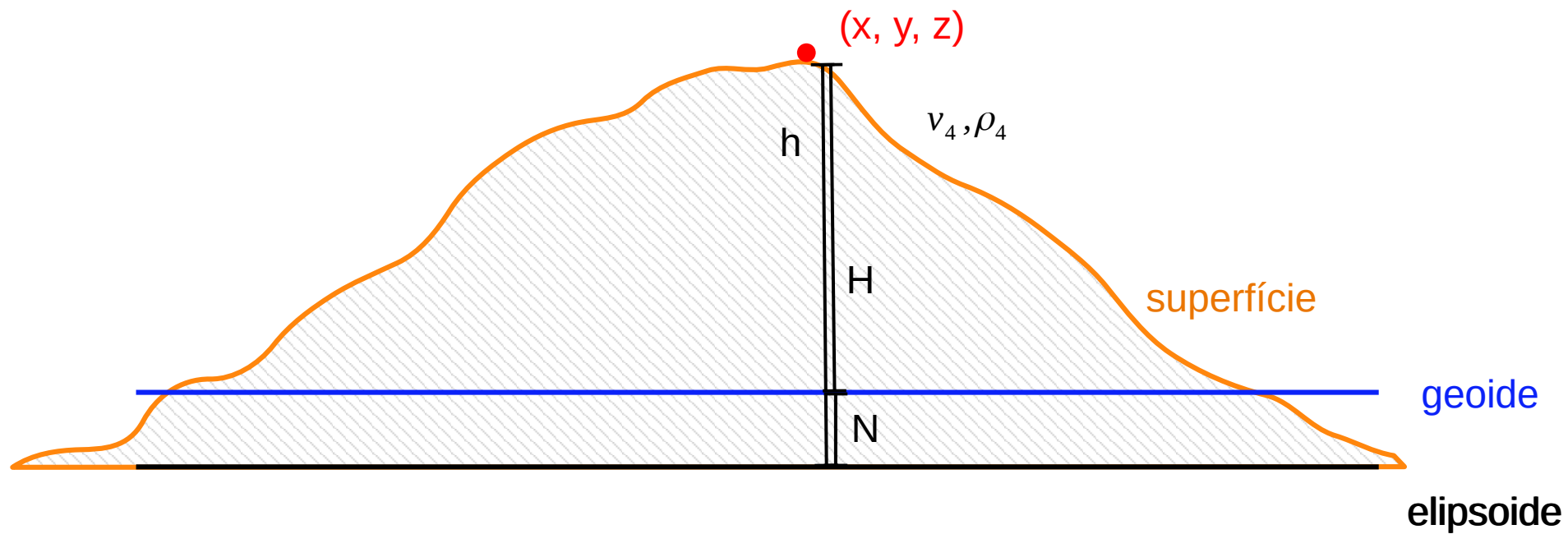
$$\delta g_P = g_P - \gamma_P$$

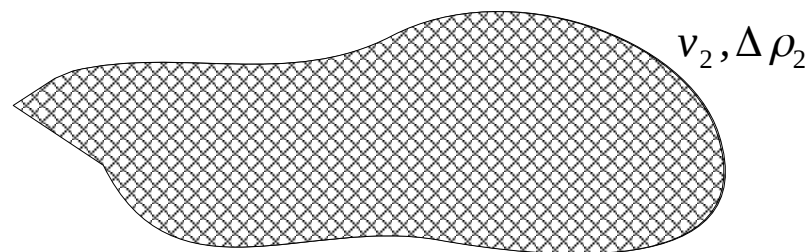
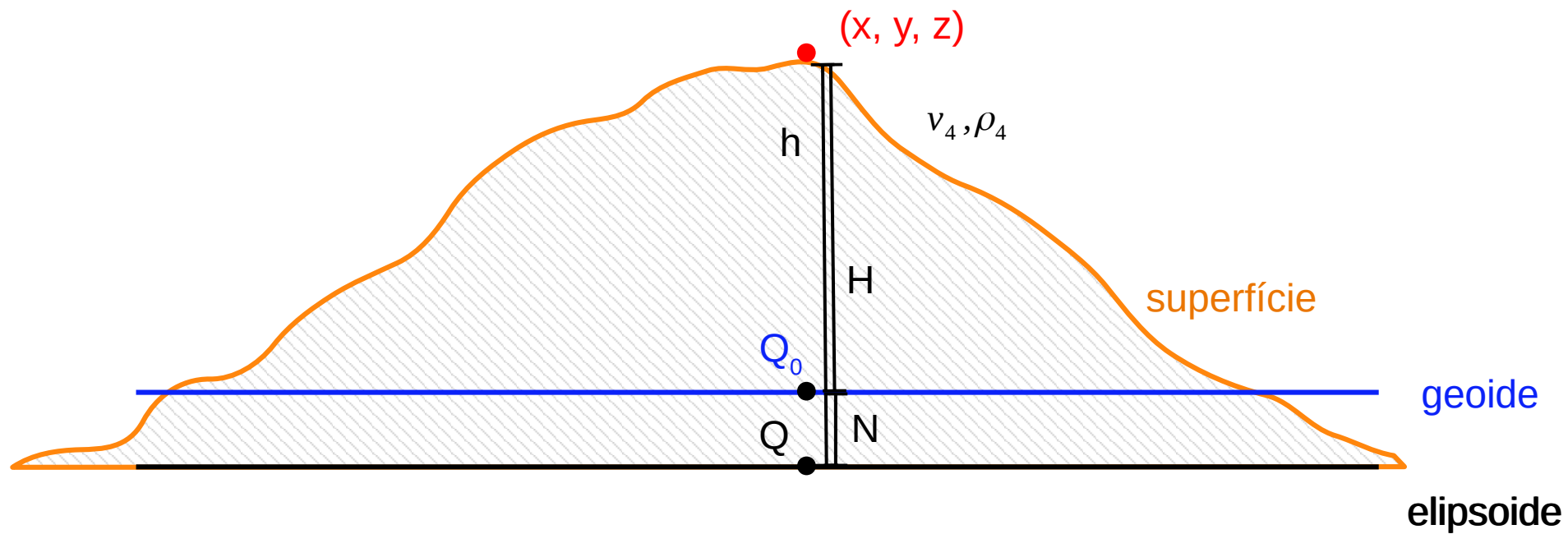
$$\delta g_P = G \iiint \partial_z \frac{1}{r} \Delta \rho_2 dv$$



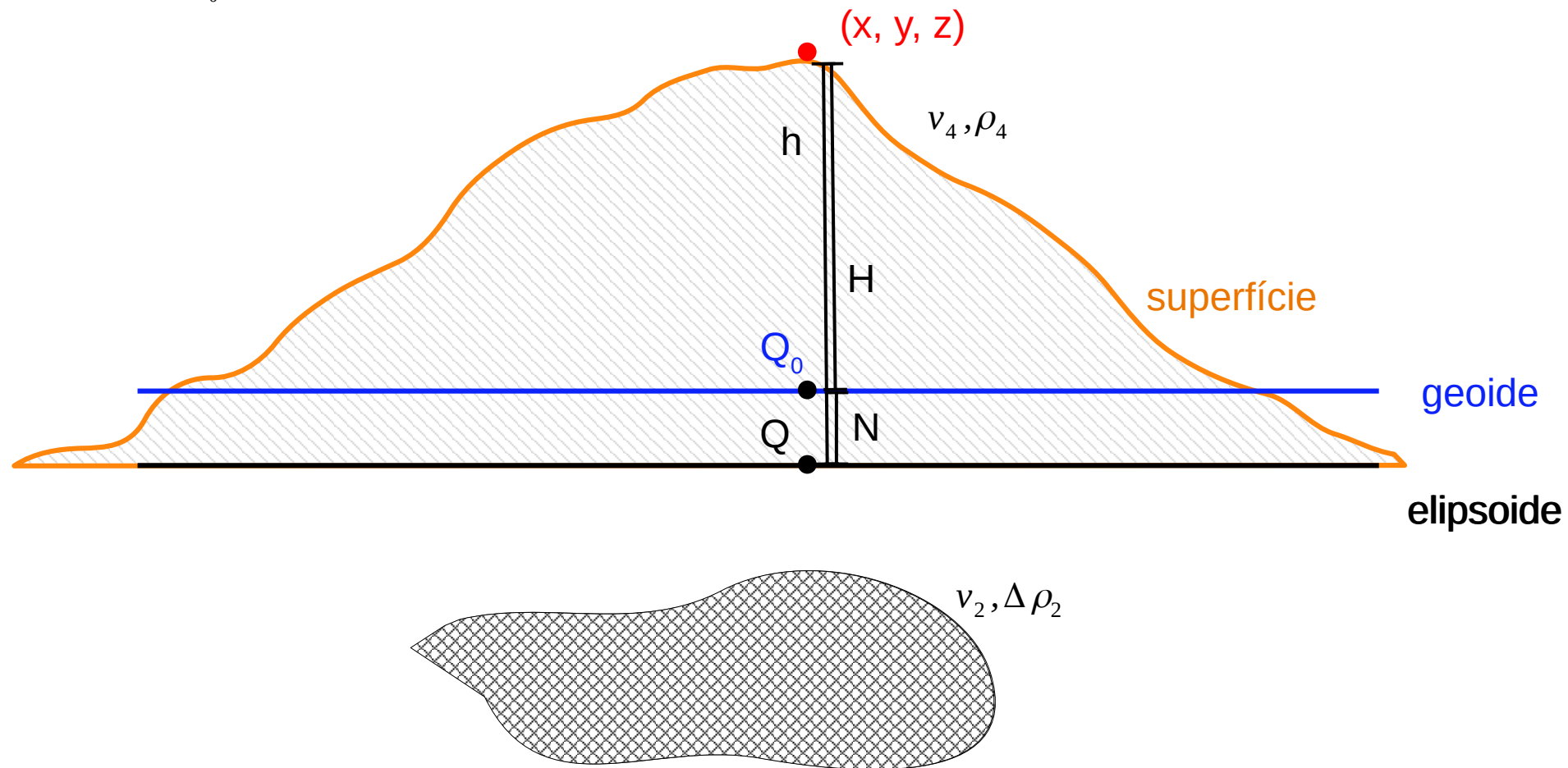




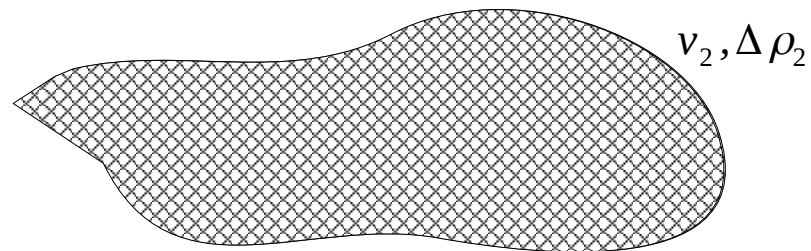
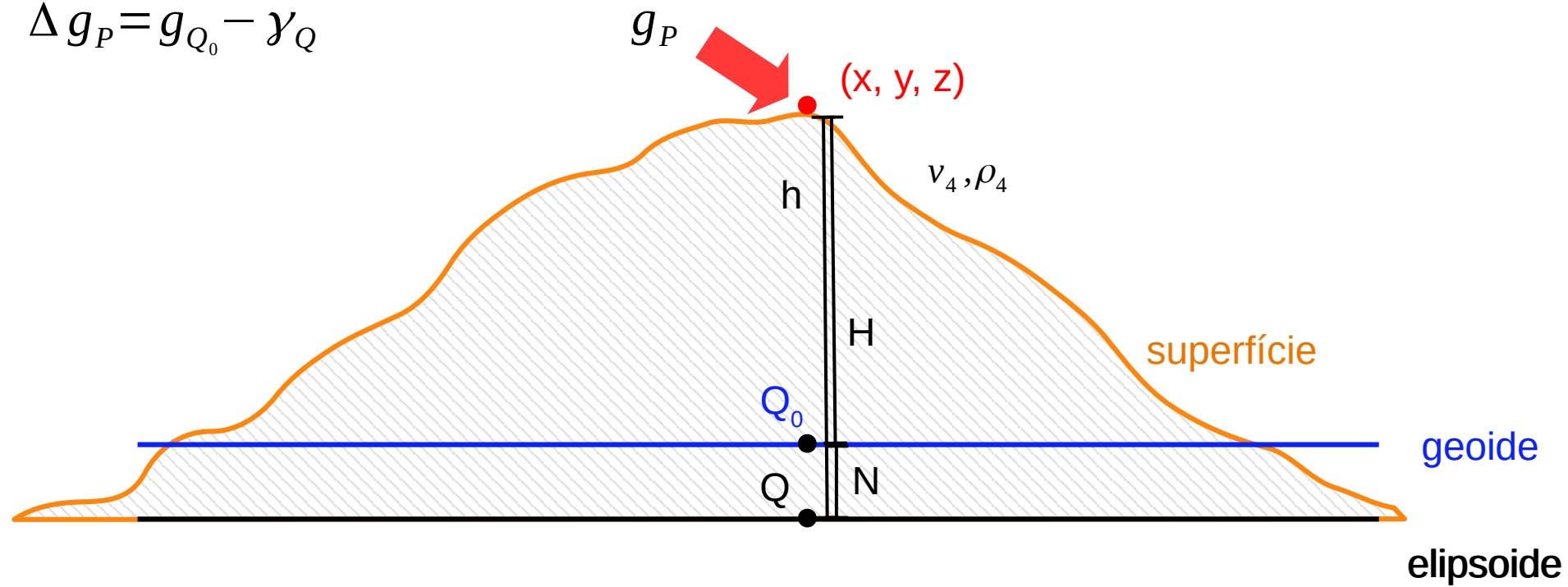




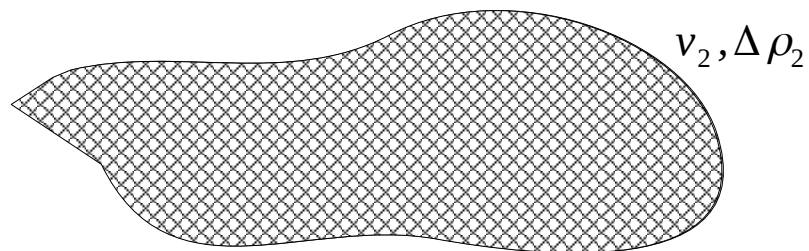
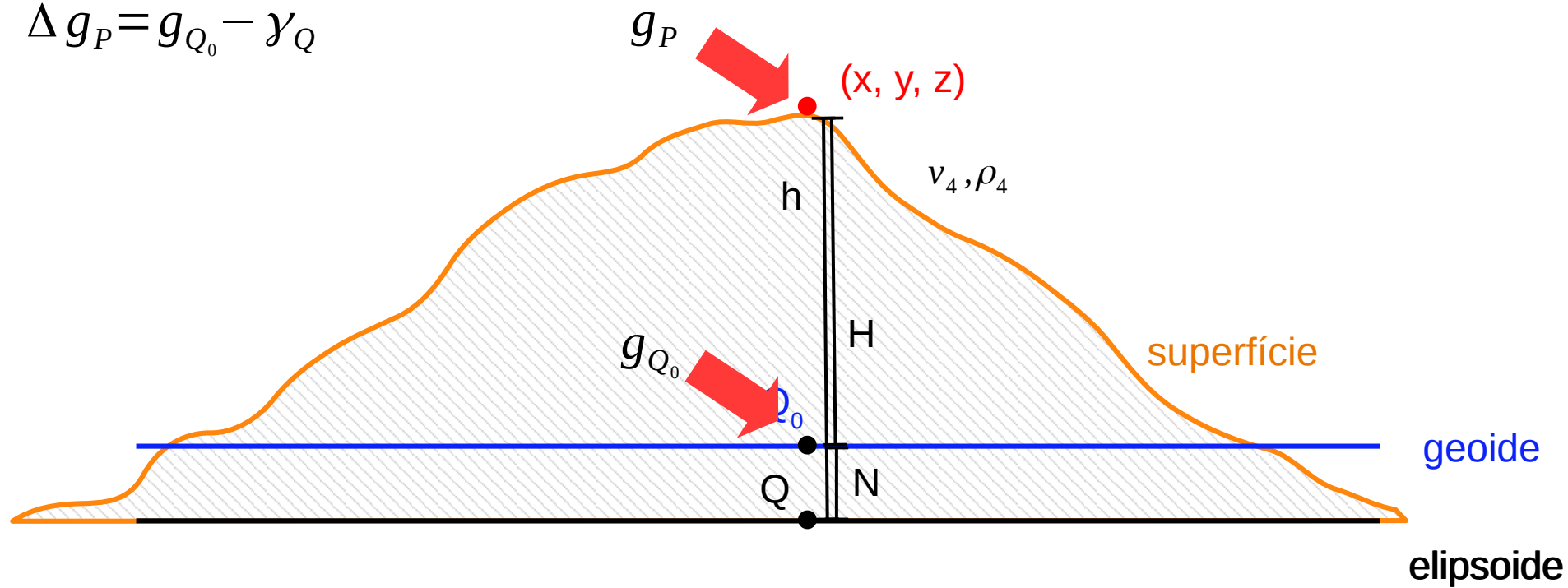
$$\Delta g_P = g_{Q_0} - \gamma_Q$$



$$\Delta g_P = g_{Q_0} - \gamma_Q$$

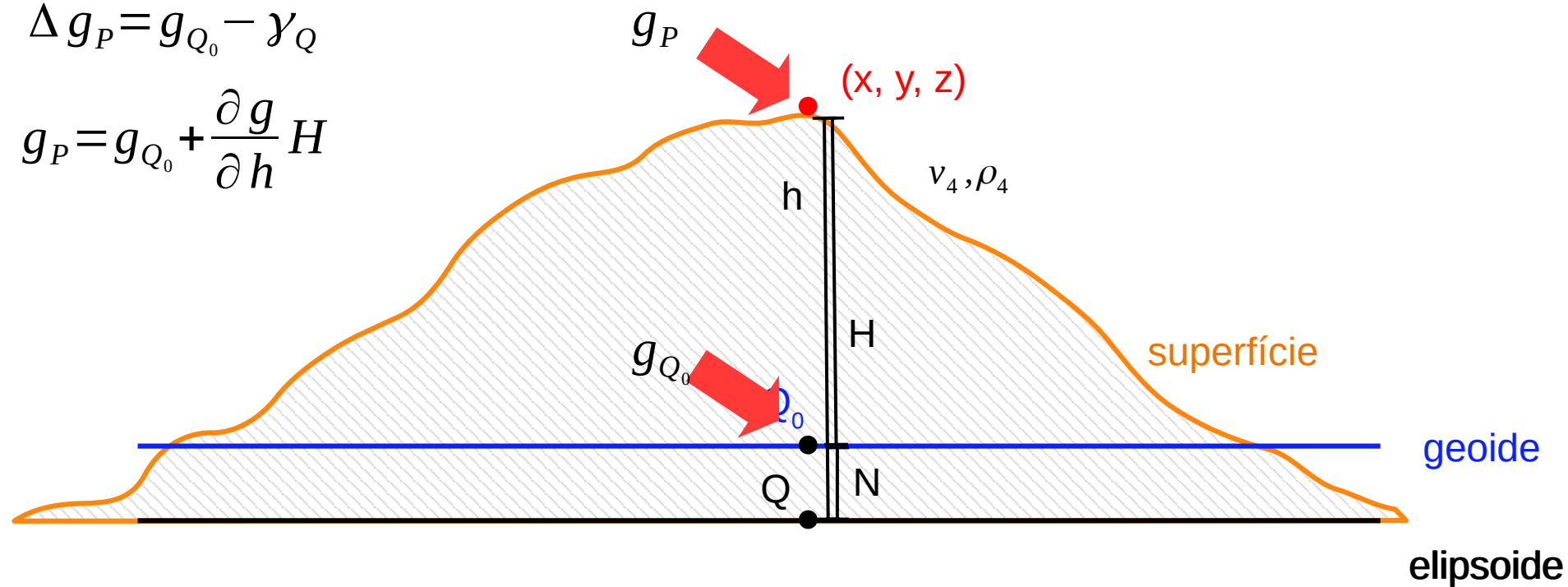


$$\Delta g_P = g_{Q_0} - \gamma_Q$$



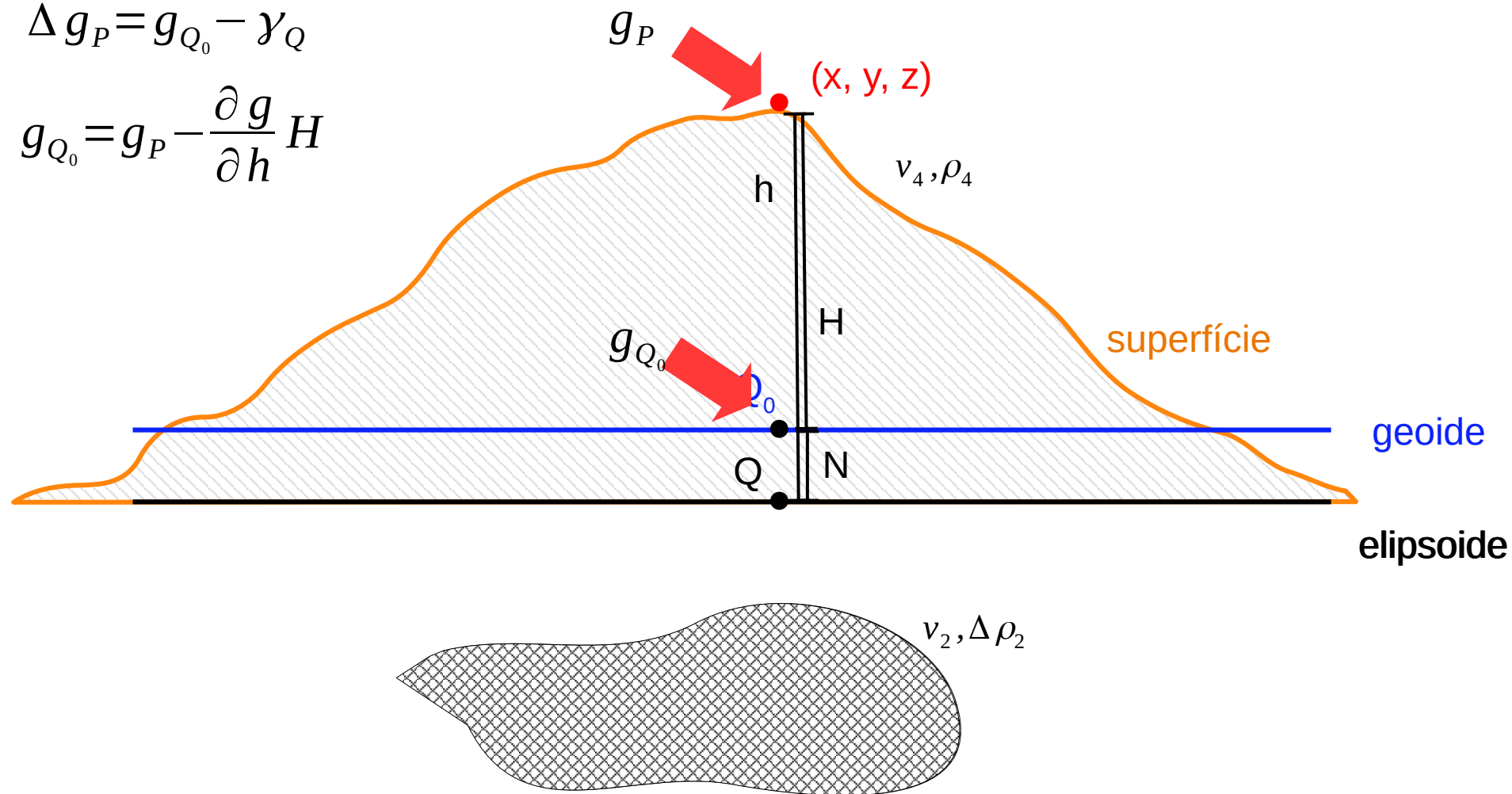
$$\Delta g_P = g_{Q_0} - \gamma_Q$$

$$g_P = g_{Q_0} + \frac{\partial g}{\partial h} H$$



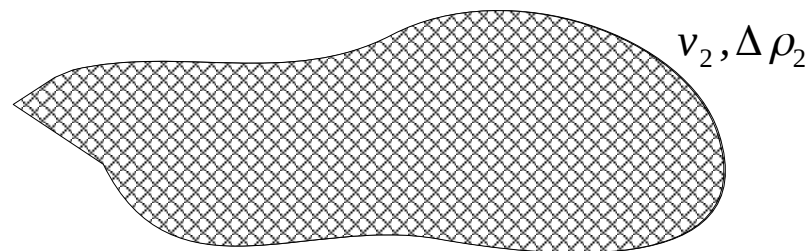
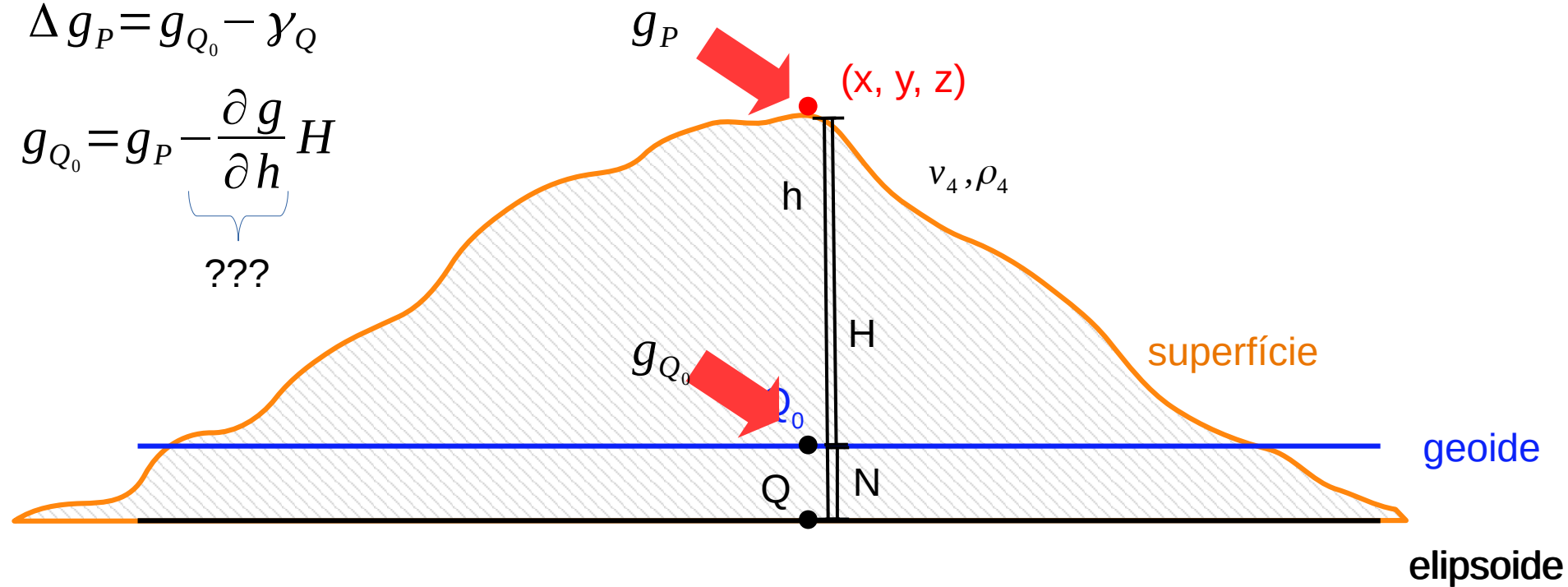
$$\Delta g_P = g_{Q_0} - \gamma_Q$$

$$g_{Q_0} = g_P - \frac{\partial g}{\partial h} H$$



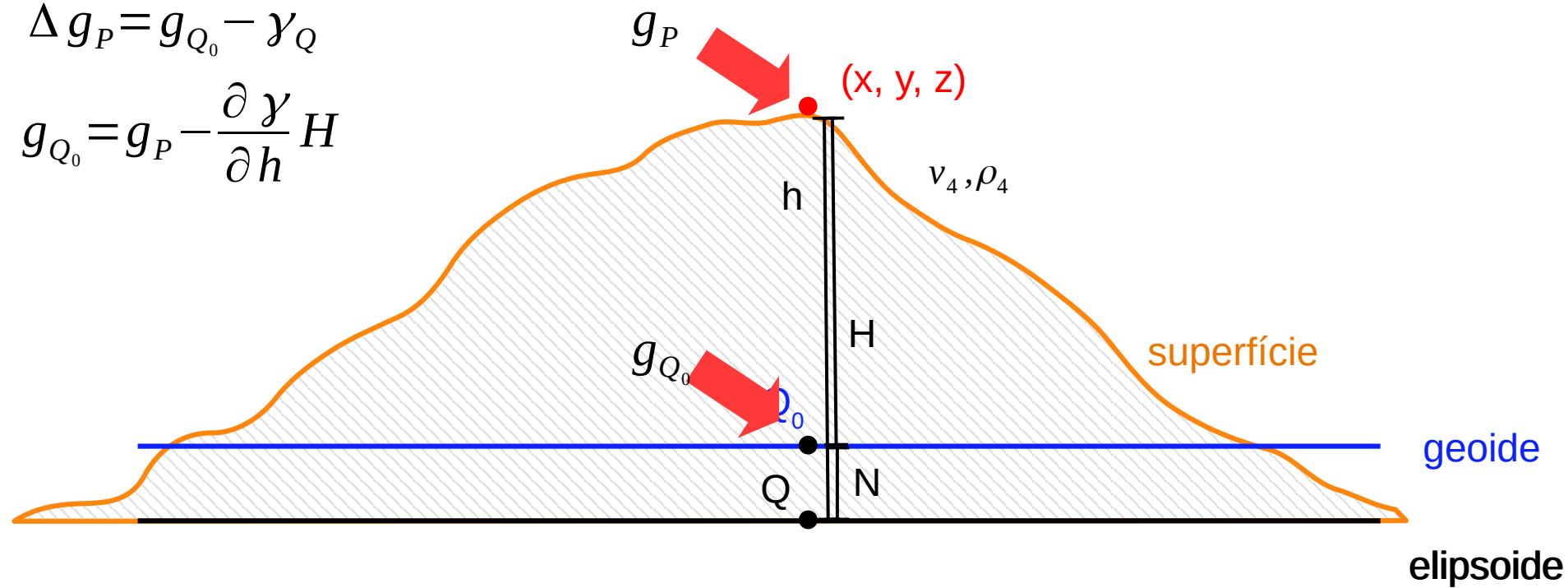
$$\Delta g_P = g_{Q_0} - \gamma_Q$$

$$g_{Q_0} = g_P - \underbrace{\frac{\partial g}{\partial h}}_{???} H$$

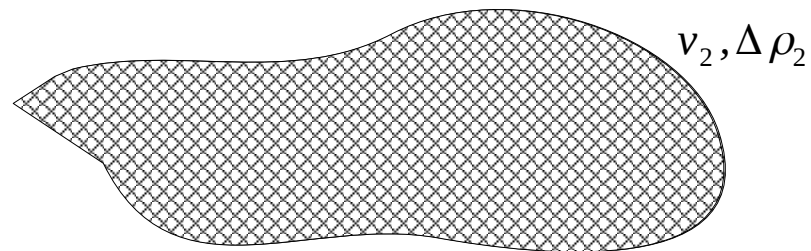
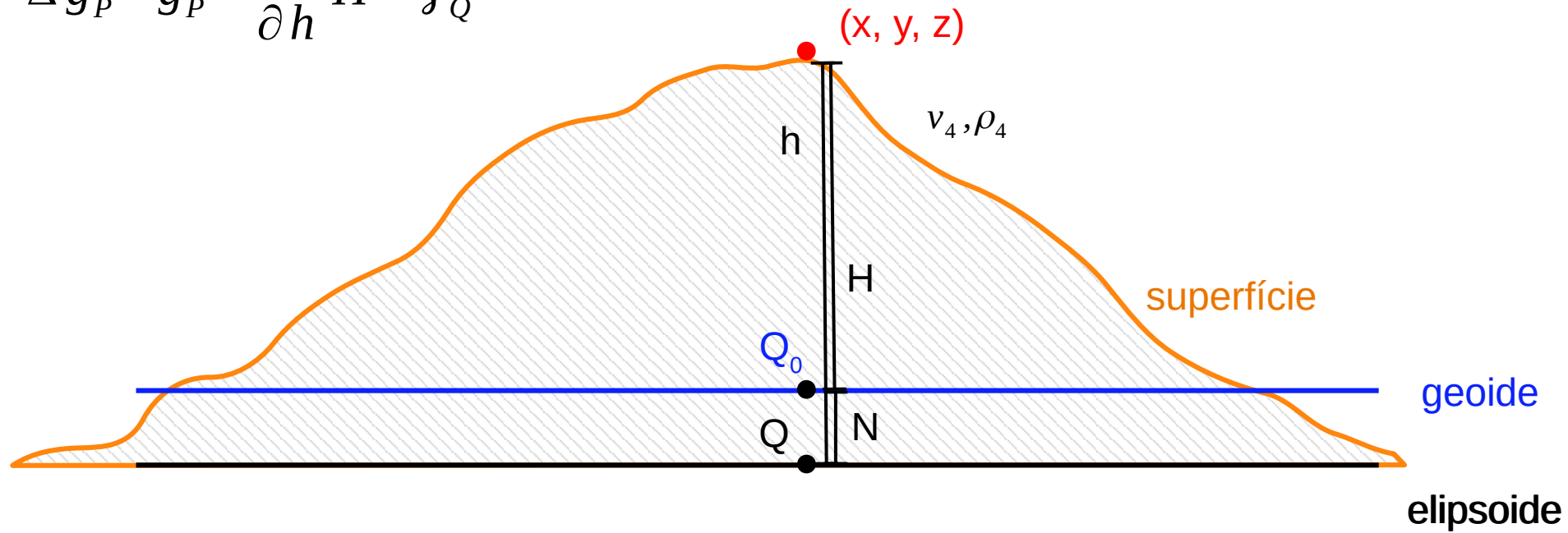


$$\Delta g_P = g_{Q_0} - \gamma_Q$$

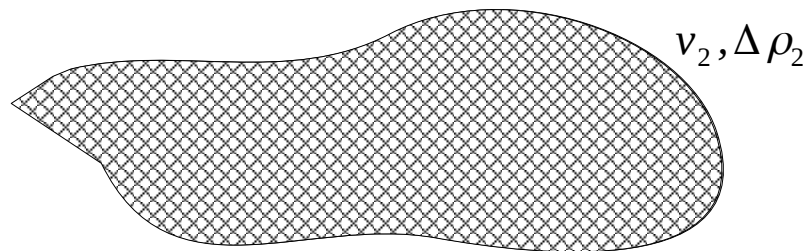
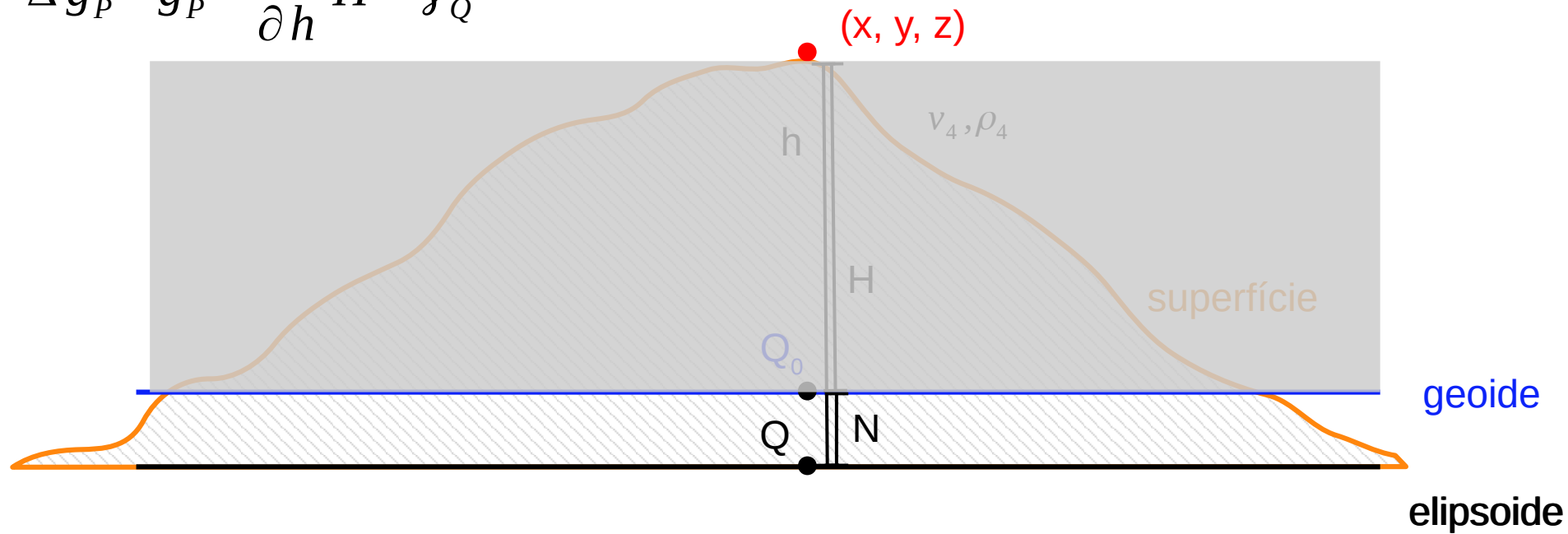
$$g_{Q_0} = g_P - \frac{\partial \gamma}{\partial h} H$$



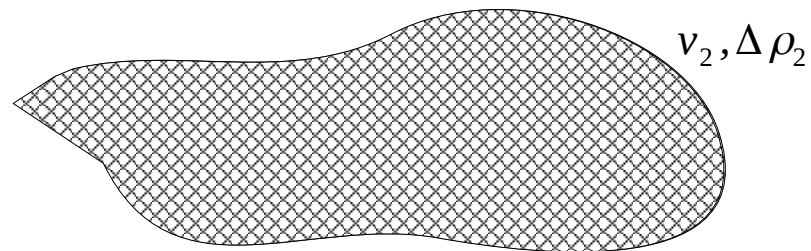
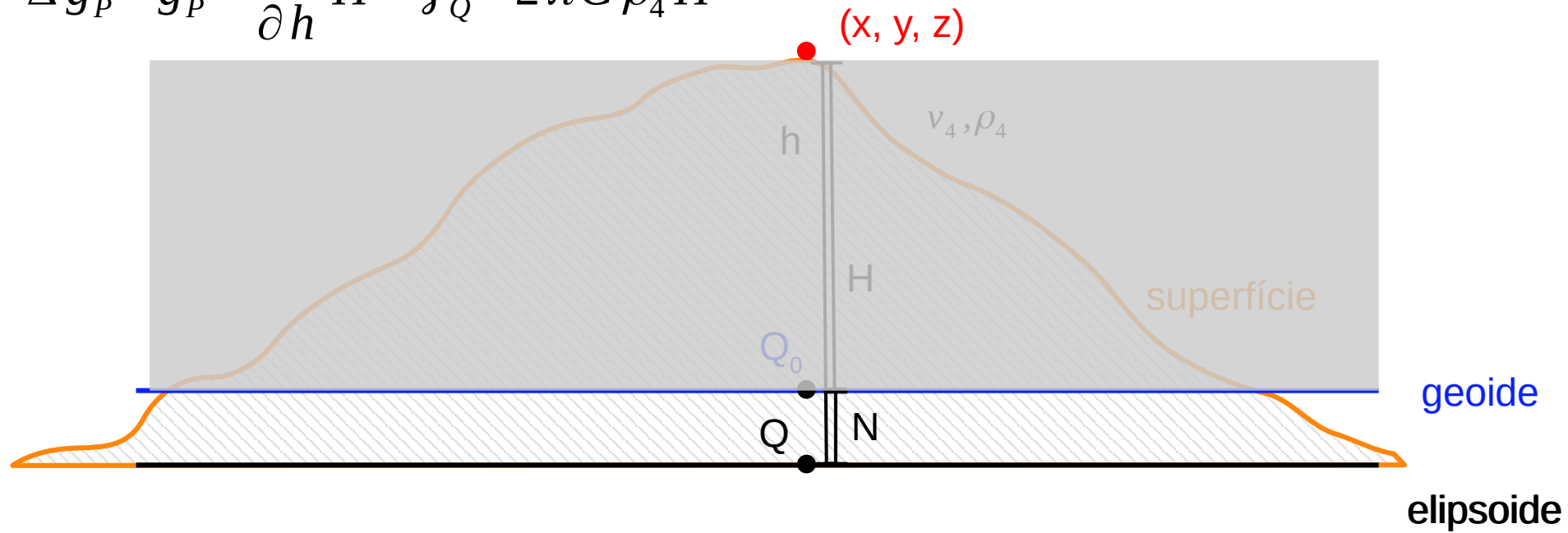
$$\Delta g_P = g_P - \frac{\partial \gamma}{\partial h} H - \gamma_Q$$



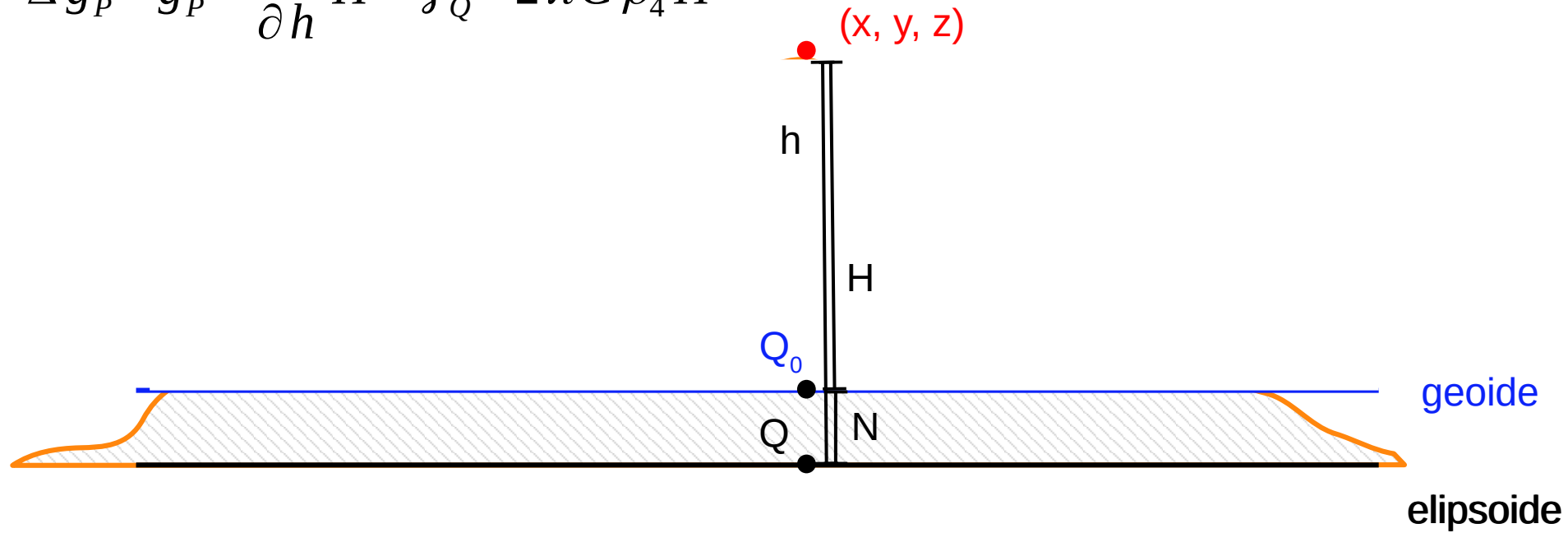
$$\Delta g_P = g_P - \frac{\partial \gamma}{\partial h} H - \gamma_Q$$



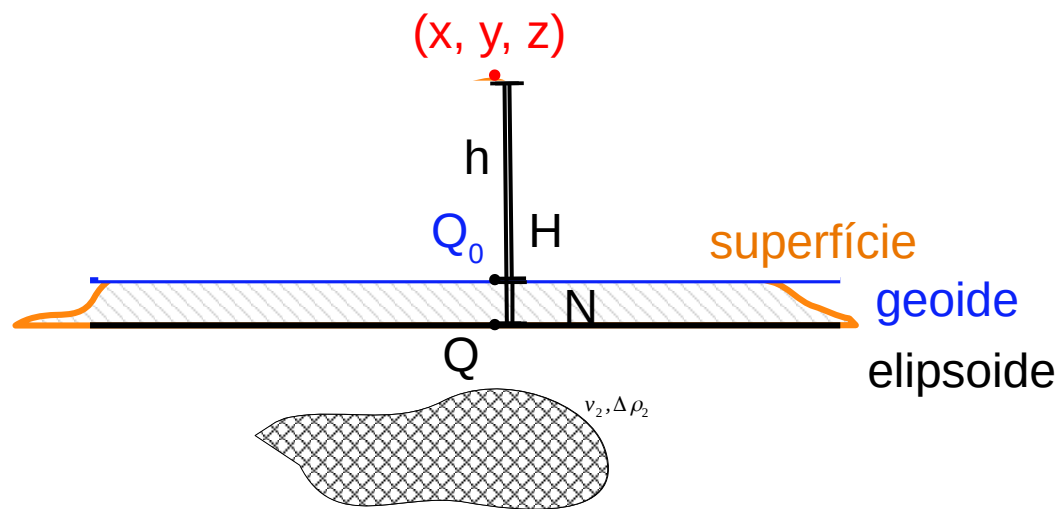
$$\Delta g_P = g_P - \frac{\partial \gamma}{\partial h} H - \gamma_Q - 2\pi G \tilde{\rho}_4 H$$



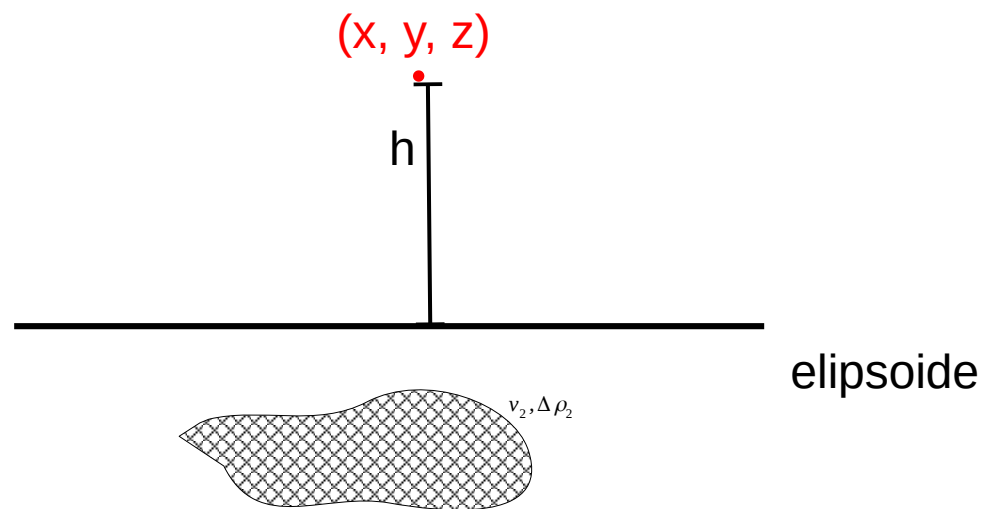
$$\Delta g_P = g_P - \frac{\partial \gamma}{\partial h} H - \gamma_Q - 2\pi G \tilde{\rho}_4 H$$



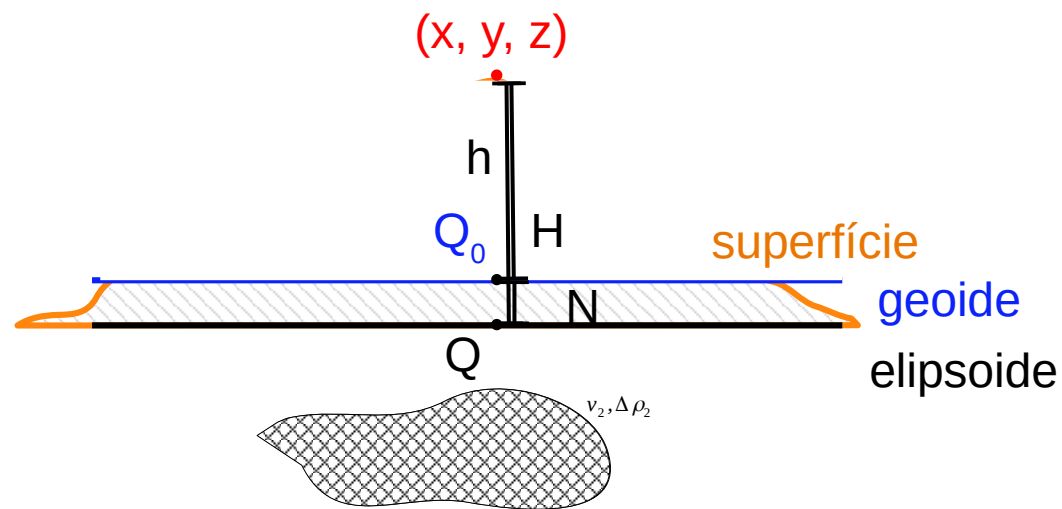
$$\Delta g_P = g_P - \frac{\partial \gamma}{\partial h} H - \gamma_Q - 2\pi G \tilde{\rho}_4 H$$



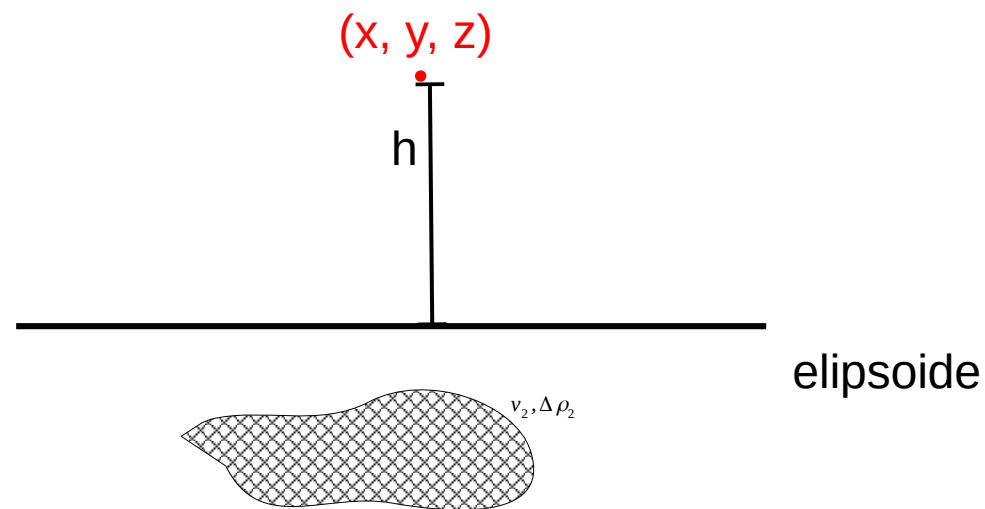
$$\delta g_P = g_P - \gamma_P - 2\pi G \tilde{\rho}_4 h$$



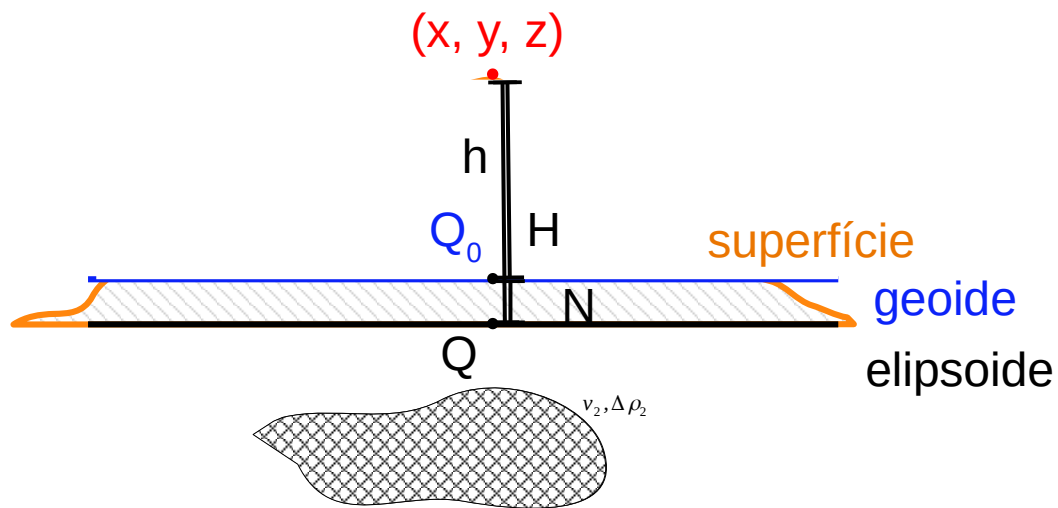
$$\Delta g_P = g_P - \frac{\partial \gamma}{\partial h} H - \gamma_Q - 2\pi G \tilde{\rho}_4 H$$



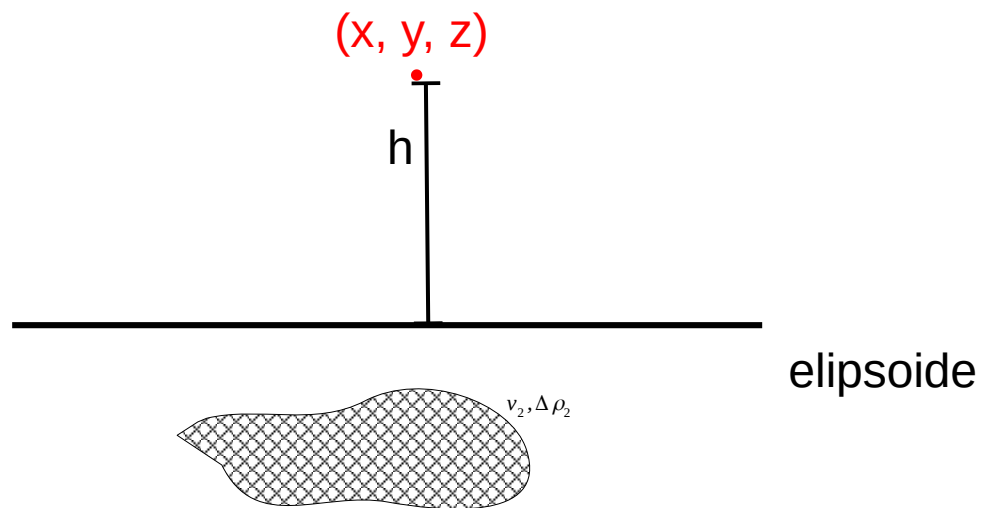
$$\delta g_P = g_P - \gamma_P - 2\pi G \tilde{\rho}_4 h$$



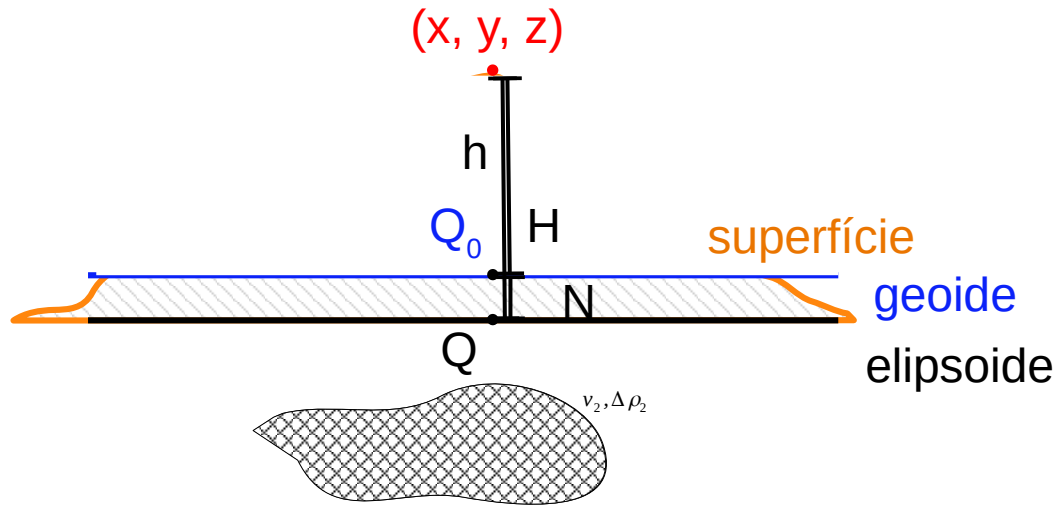
$$\Delta g_P = g_P - \frac{\partial \gamma}{\partial h} H - \gamma_Q - 2\pi G \tilde{\rho}_4 H$$



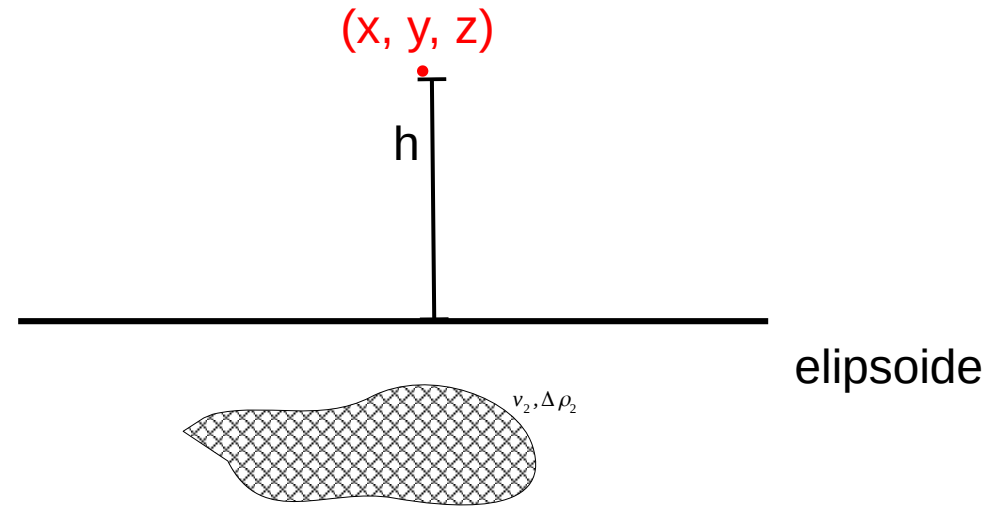
$$\delta g_P = g_P - \gamma_P - 2\pi G \tilde{\rho}_4 h$$




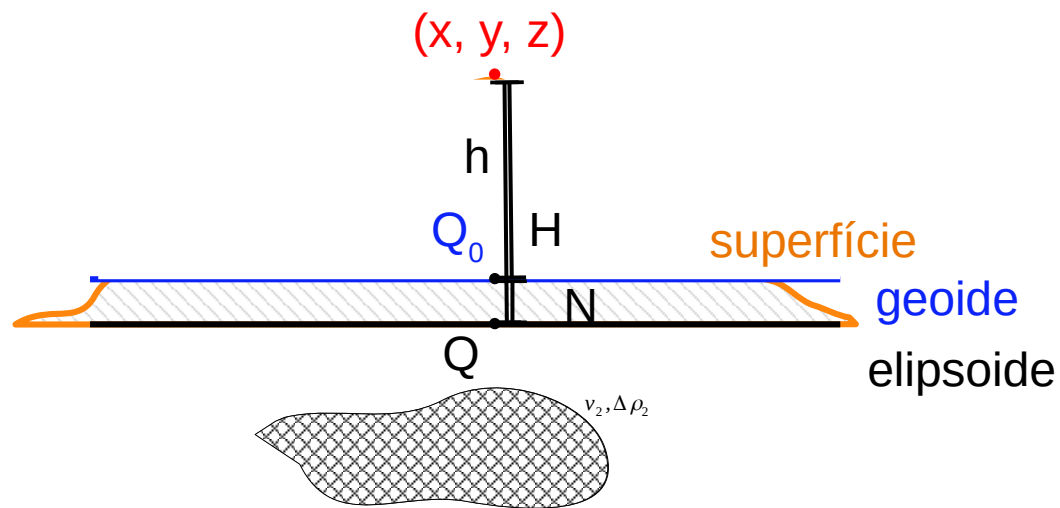
$$\Delta g_P = g_P - \frac{\partial \gamma}{\partial h} H - \gamma_Q - 2\pi G \tilde{\rho}_4 H$$



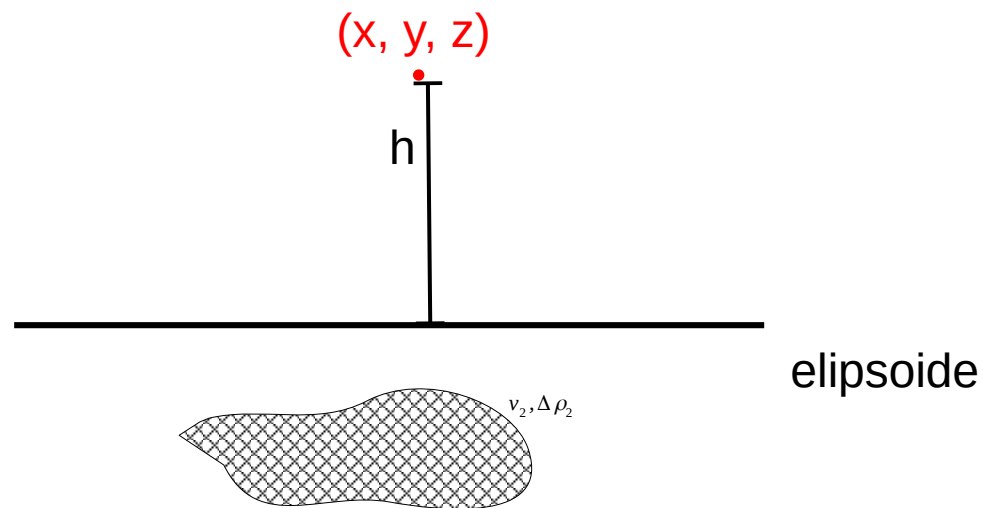
$$\delta g_P = g_P - \gamma_P - 2\pi G \tilde{\rho}_4 h$$



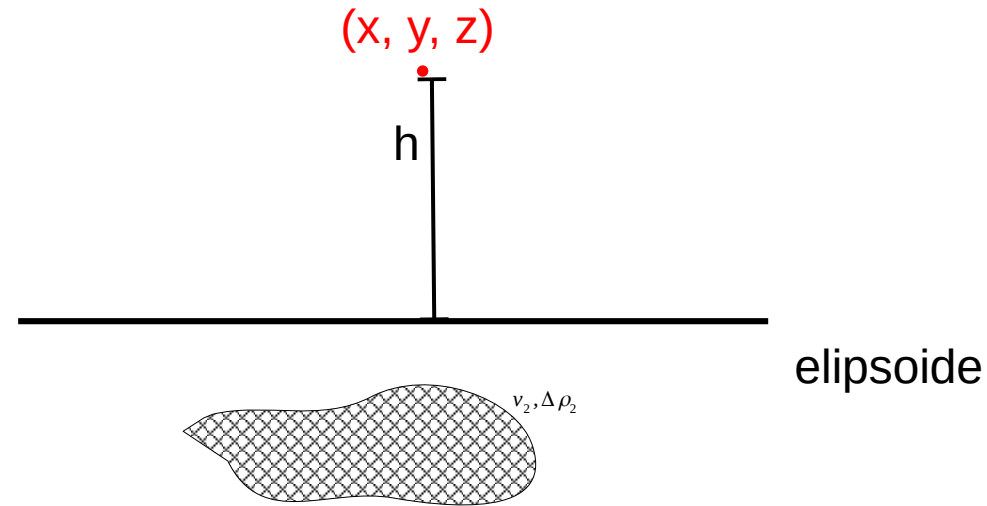
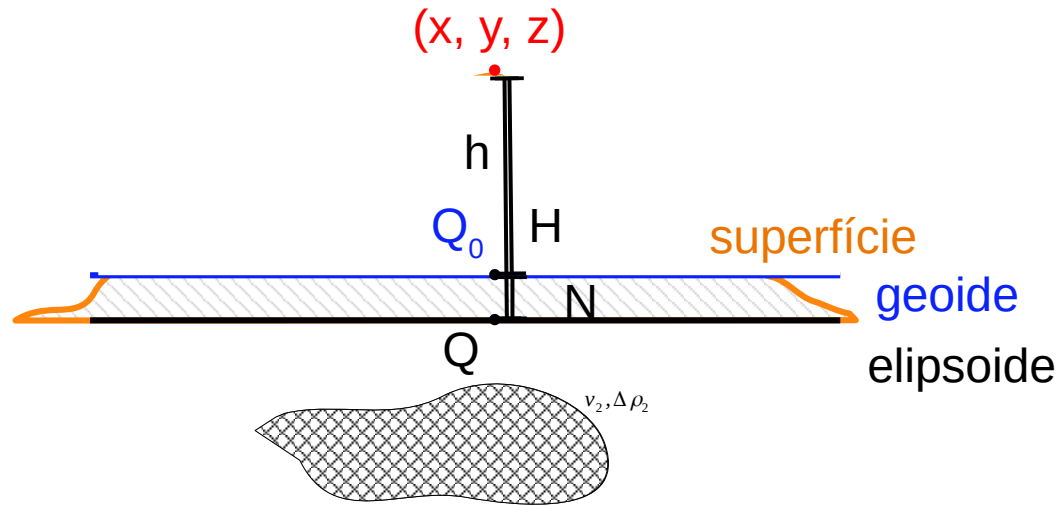
$$\Delta g_P = g_P - \frac{\partial \gamma}{\partial h} H - \gamma_Q - 2\pi G \tilde{\rho}_4 H$$




$$\delta g_P = g_P - \gamma_P - 2\pi G \tilde{\rho}_4 h$$

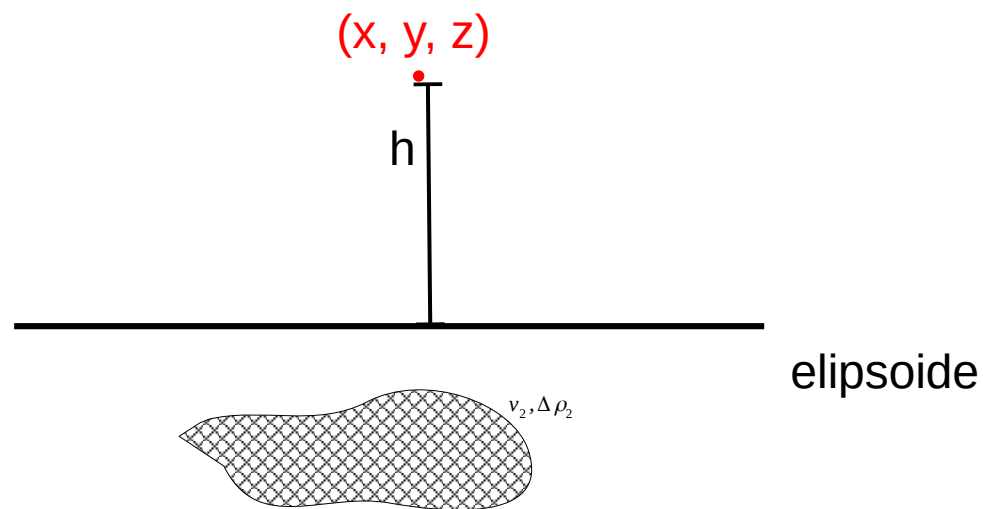
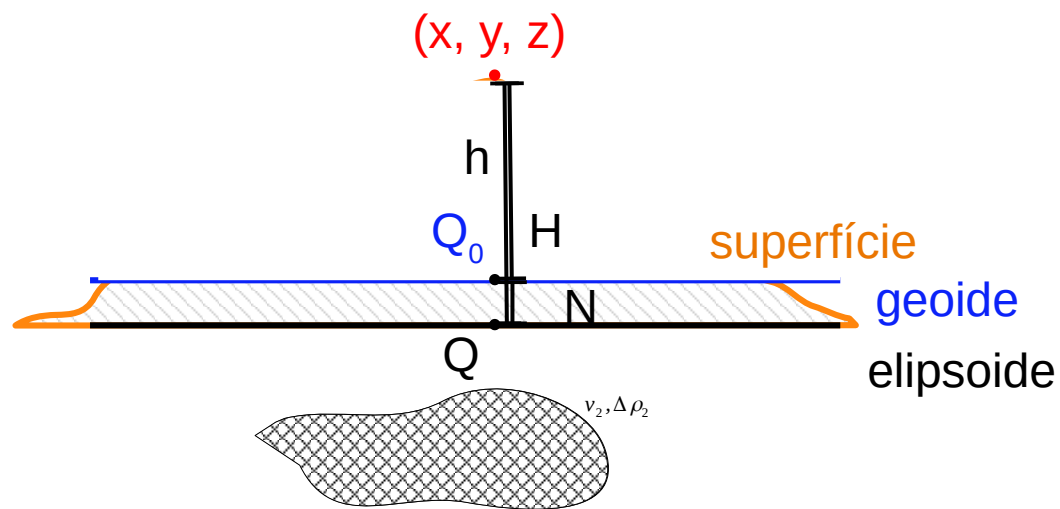



$$\Delta g_P = g_P - \frac{\partial \gamma}{\partial h}(h - N) - \gamma_Q - 2\pi G \tilde{\rho}_4(h - N) \quad \delta g_P = g_P - \gamma_P - 2\pi G \tilde{\rho}_4 h$$



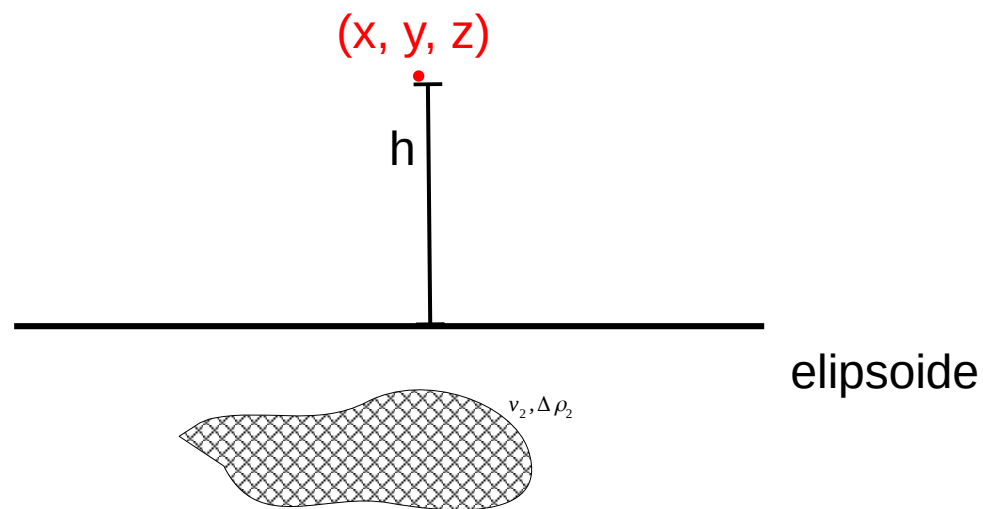
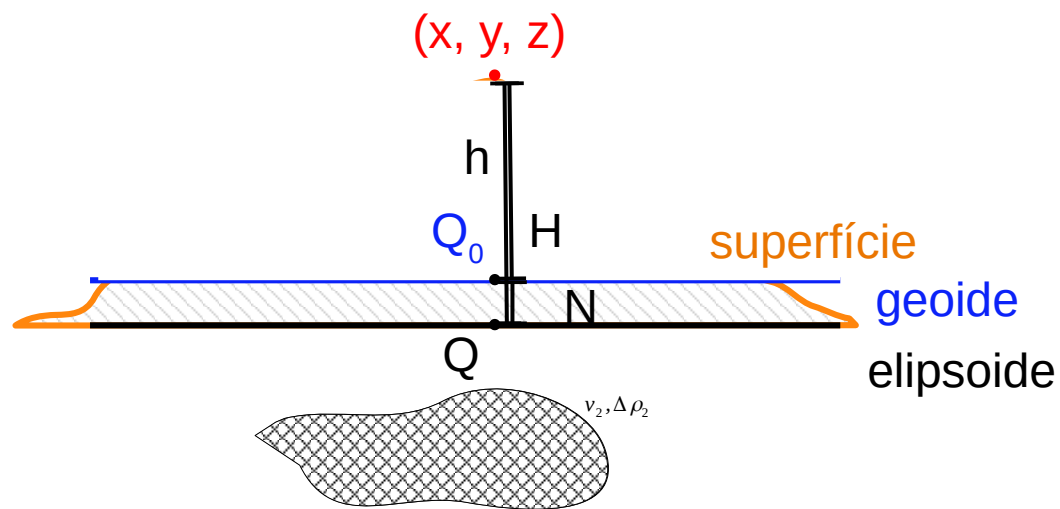
$$\Delta g_P = g_P - \frac{\partial \gamma}{\partial h} h + \frac{\partial \gamma}{\partial h} N - \gamma_Q - 2\pi G \tilde{\rho}_4 h + 2\pi G \tilde{\rho}_4 N$$

$$\delta g_P = g_P - \gamma_P - 2\pi G \tilde{\rho}_4 h$$

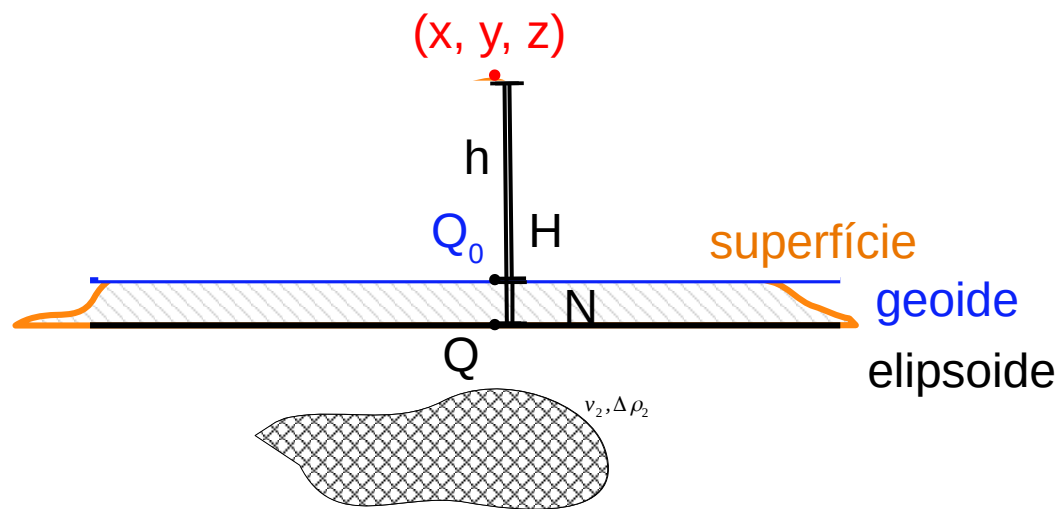


$$\Delta g_P = g_P - \frac{\partial \gamma}{\partial h} h + \frac{\partial \gamma}{\partial h} N - \gamma_Q - 2\pi G \tilde{\rho}_4 h + 2\pi G \tilde{\rho}_4 N$$


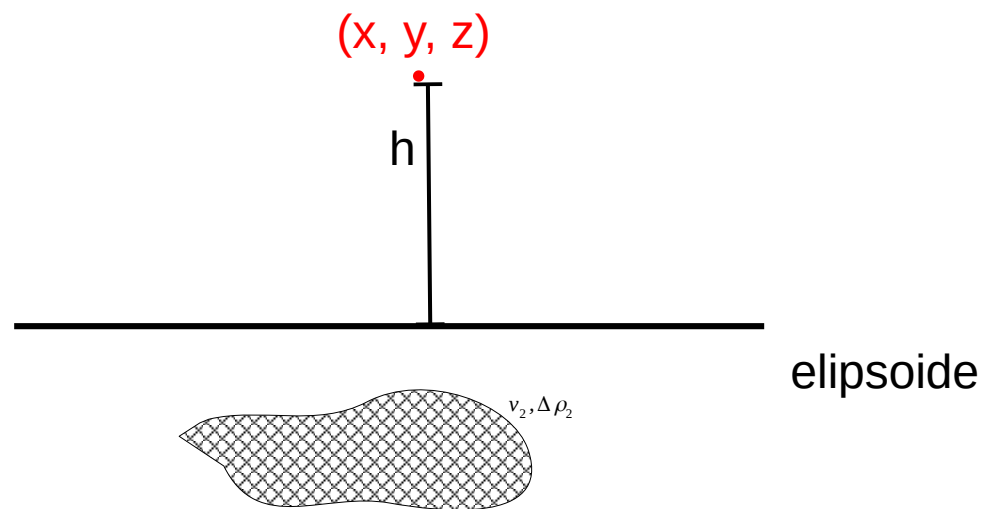
$$\delta g_P = g_P - \gamma_P - 2\pi G \tilde{\rho}_4 h$$



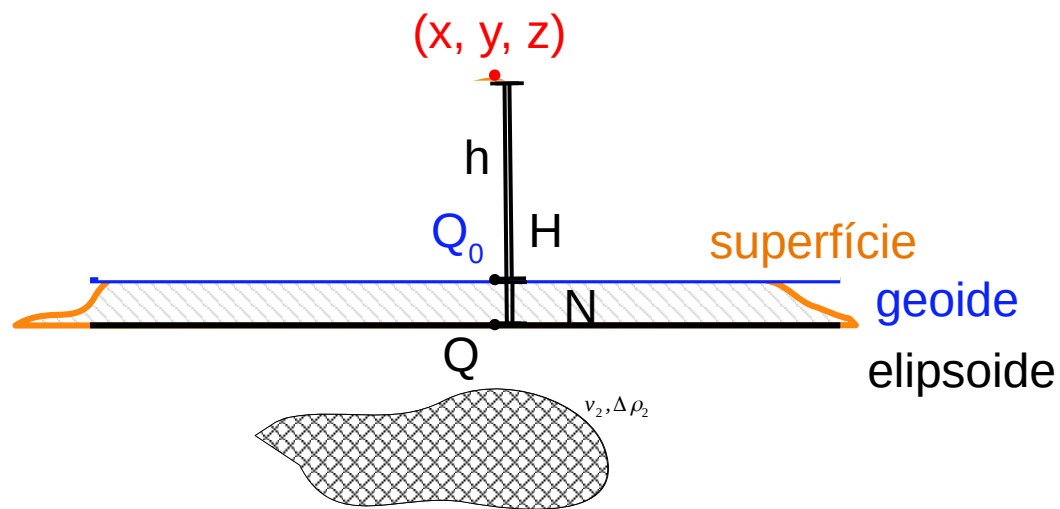
$$\Delta g_P = g_P - \frac{\partial \gamma}{\partial h} h - \gamma_Q - 2\pi G \tilde{\rho}_4 h + \frac{\partial \gamma}{\partial h} N + 2\pi G \tilde{\rho}_4 N$$



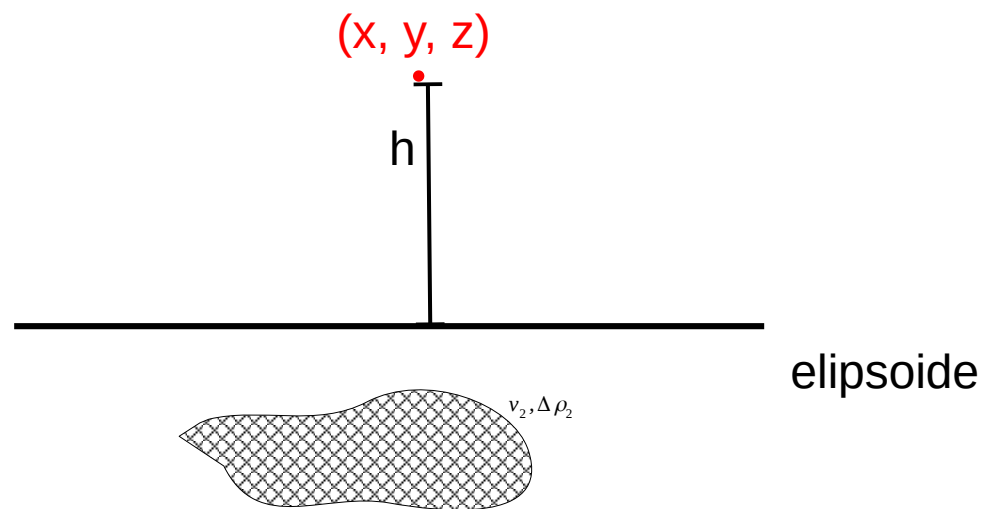
$$\delta g_P = g_P - \gamma_P - 2\pi G \tilde{\rho}_4 h$$



$$\Delta g_P = g_P - \underbrace{\frac{\partial \gamma}{\partial h} h - \gamma_Q}_{-\gamma_P} - 2\pi G \tilde{\rho}_4 h + \frac{\partial \gamma}{\partial h} N + 2\pi G \tilde{\rho}_4 N$$

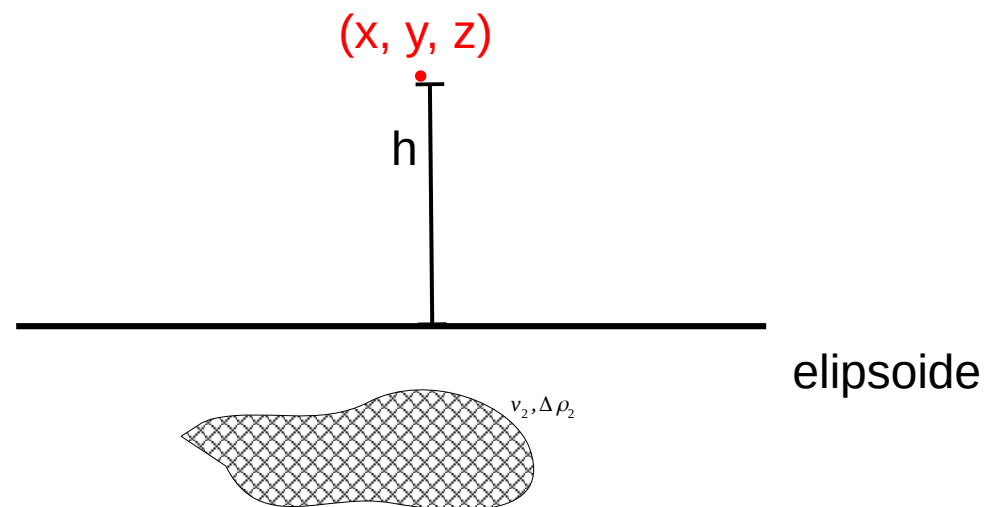
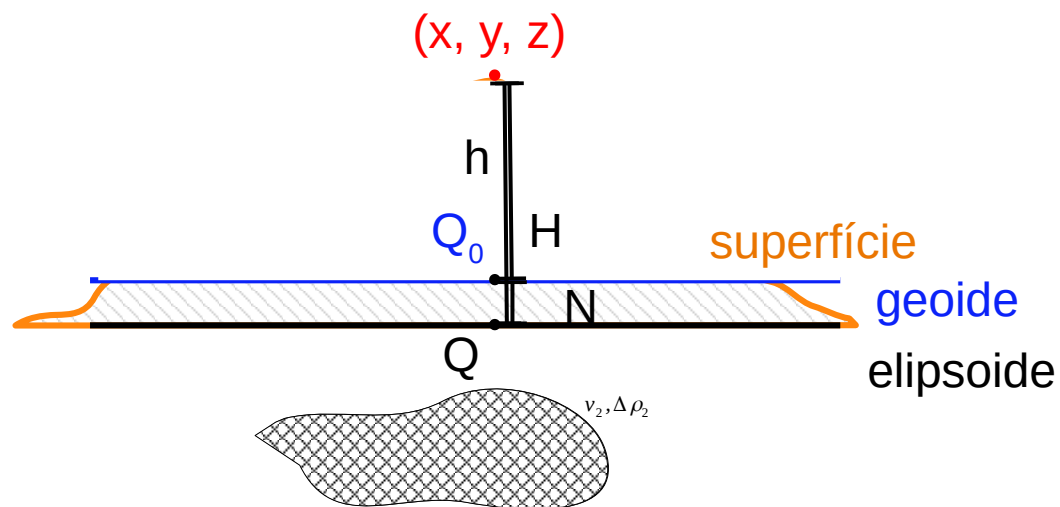


$$\delta g_P = g_P - \gamma_P - 2\pi G \tilde{\rho}_4 h$$

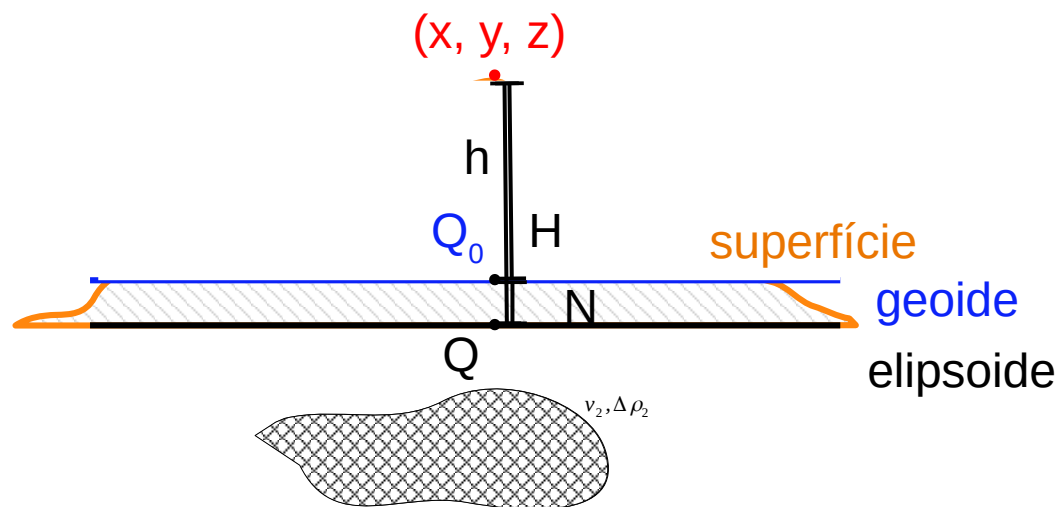


$$\Delta g_P = g_P - \gamma_P - 2\pi G \tilde{\rho}_4 h + \frac{\partial \gamma}{\partial h} N + 2\pi G \tilde{\rho}_4 N$$

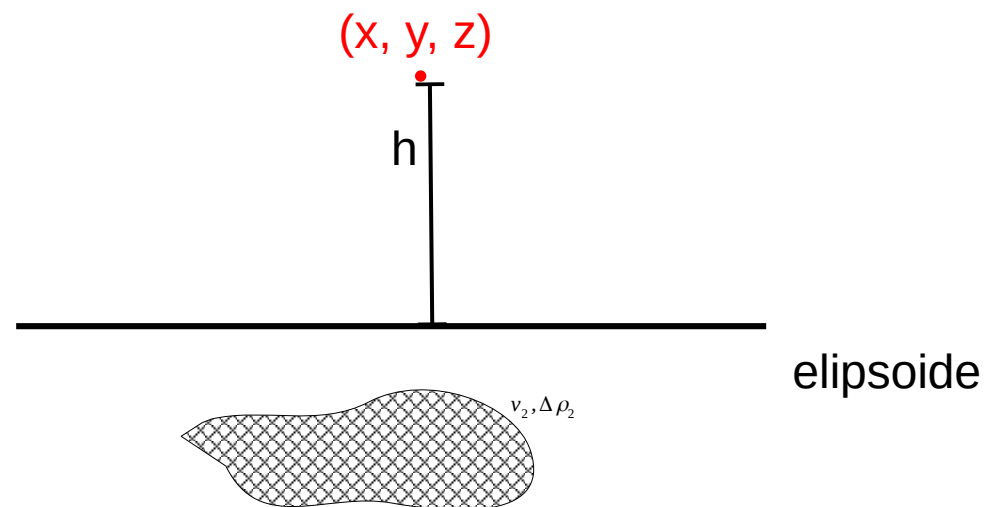
$$\delta g_P = g_P - \gamma_P - 2\pi G \tilde{\rho}_4 h$$



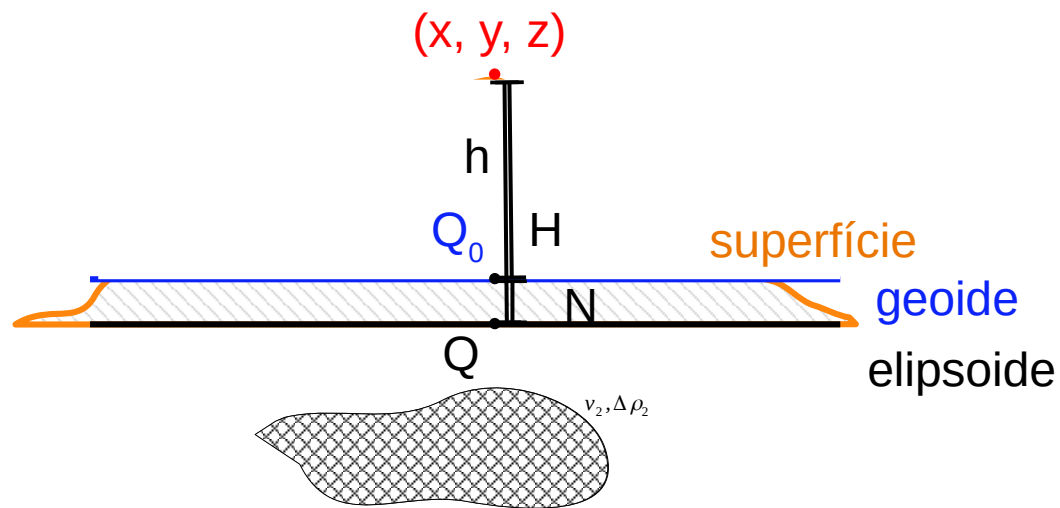
$$\Delta g_P = g_P - \gamma_P - 2\pi G \tilde{\rho}_4 h + \underbrace{\frac{\partial \gamma}{\partial h} N}_{-0.3086 \frac{mGal}{m}} + 2\pi G \tilde{\rho}_4 N$$



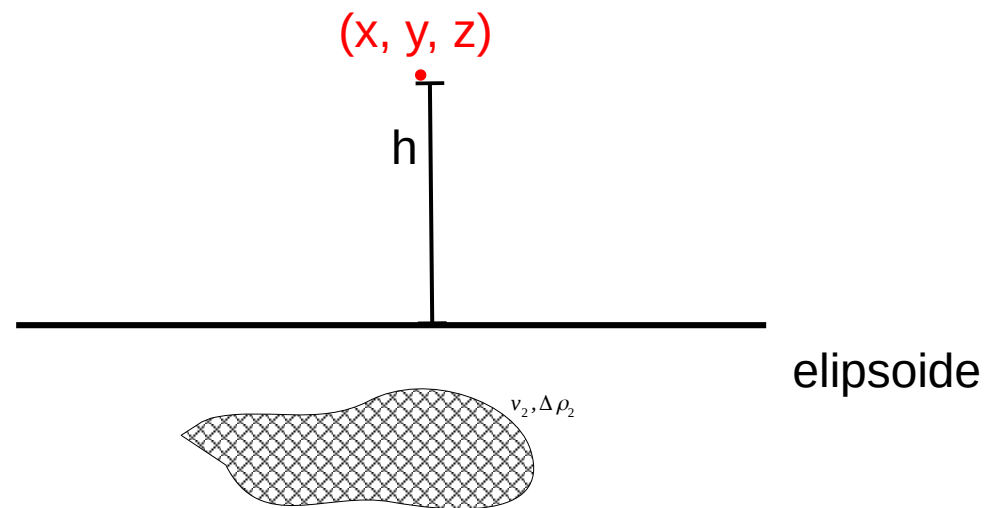
$$\delta g_P = g_P - \gamma_P - 2\pi G \tilde{\rho}_4 h$$



$$\Delta g_P = g_P - \gamma_P - 2\pi G \tilde{\rho}_4 h - 0.3086 N + 2\pi G \tilde{\rho}_4 N$$

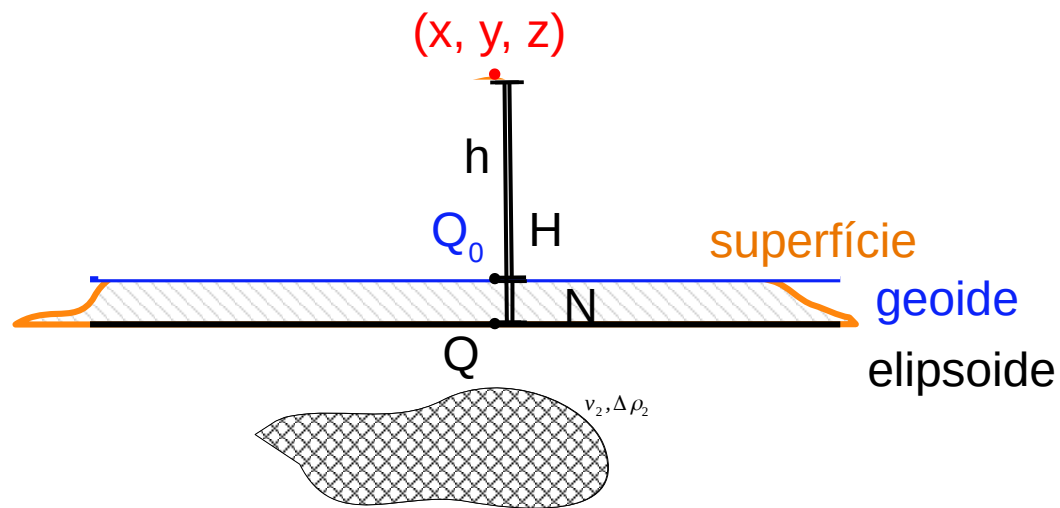


$$\delta g_P = g_P - \gamma_P - 2\pi G \tilde{\rho}_4 h$$

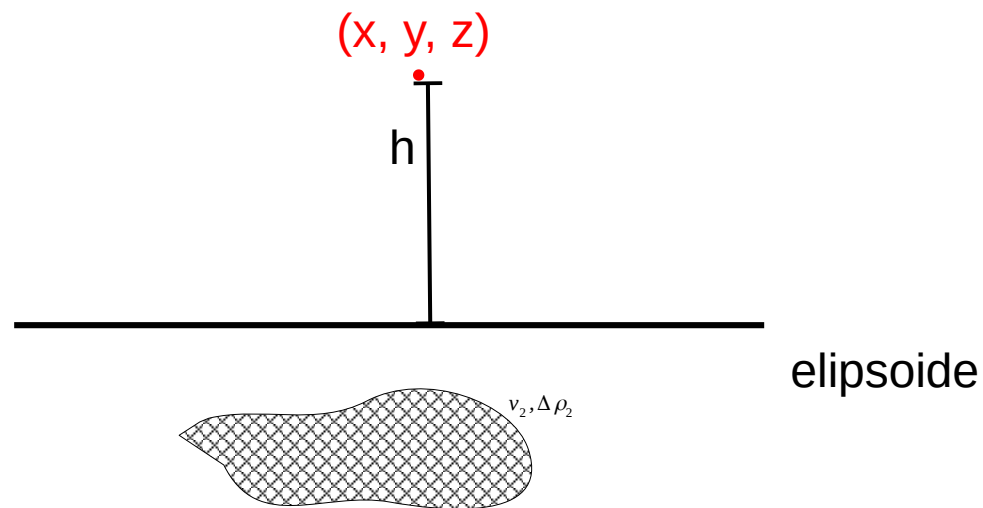


$$\Delta g_P = g_P - \gamma_P - 2\pi G \tilde{\rho}_4 h - 0.3086 N + 2\pi G \tilde{\rho}_4 N$$

Ar-livre

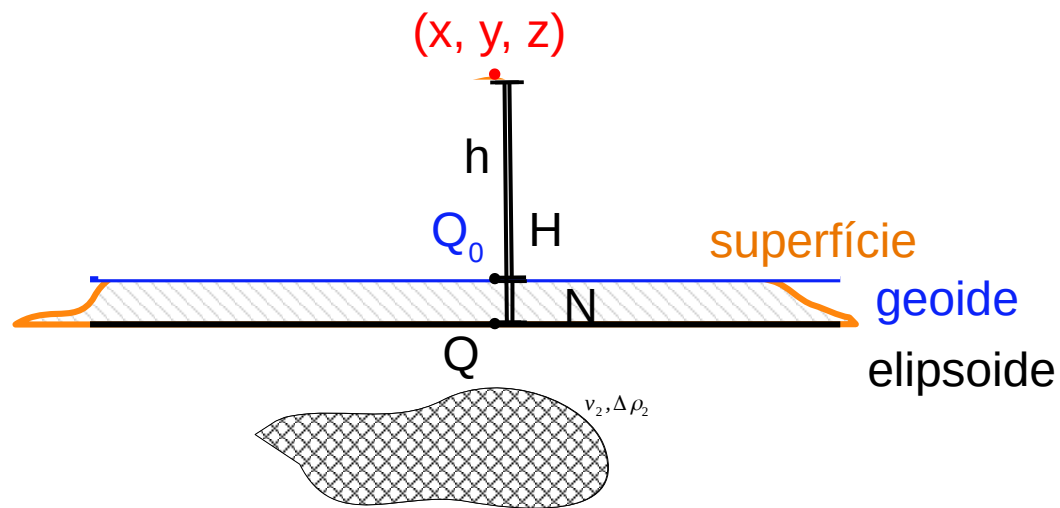


$$\delta g_P = g_P - \gamma_P - 2\pi G \tilde{\rho}_4 h$$

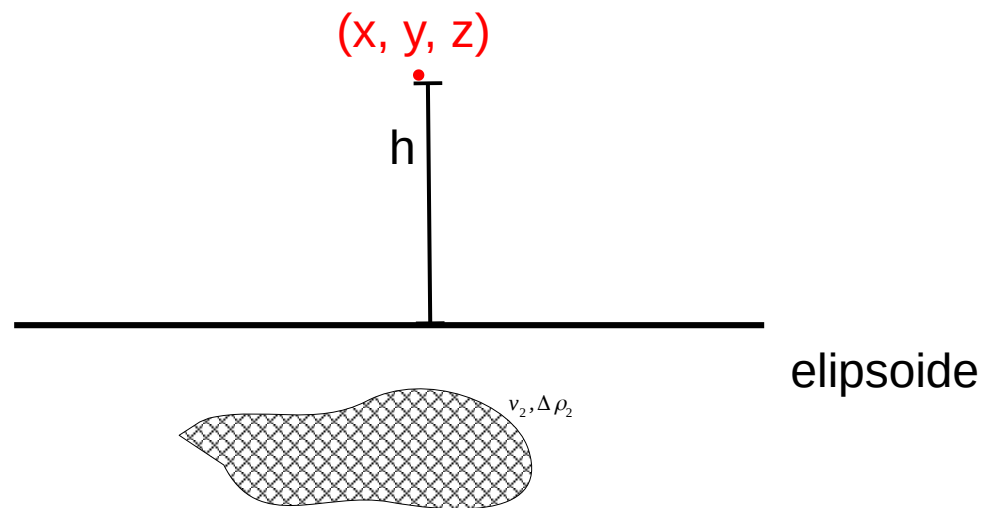


$$\Delta g_P = g_P - \gamma_P - 2\pi G \tilde{\rho}_4 h - 0.3086 N + 2\pi G \tilde{\rho}_4 N$$

Bouguer

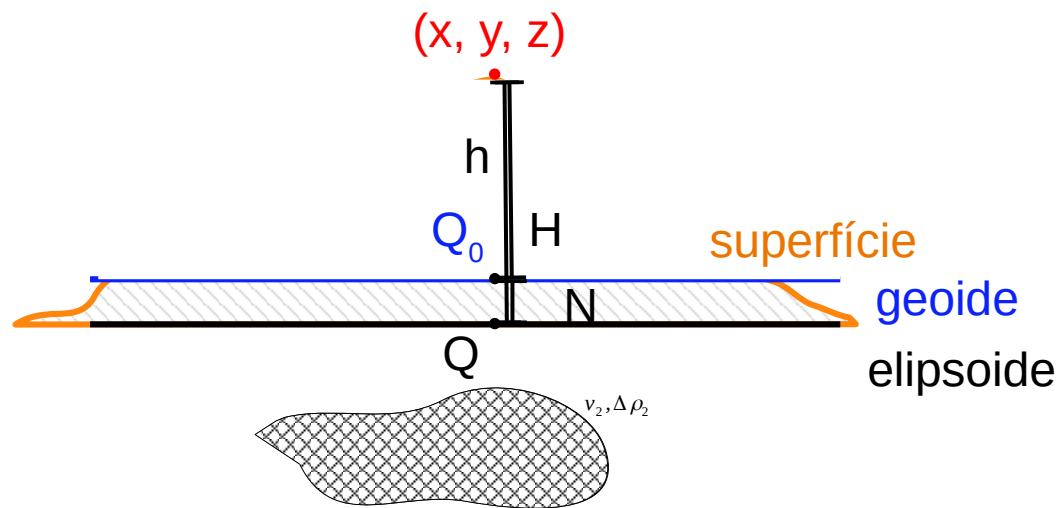


$$\delta g_P = g_P - \gamma_P - 2\pi G \tilde{\rho}_4 h$$

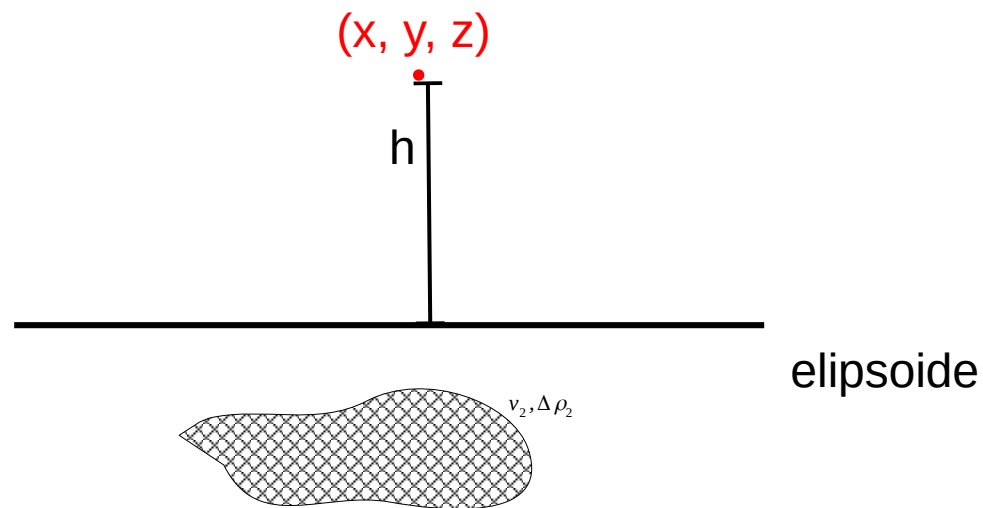


$$\Delta g_P = g_P - \gamma_P - 2\pi G \tilde{\rho}_4 h - 0.3086 N + 2\pi G \tilde{\rho}_4 N$$

disturbio

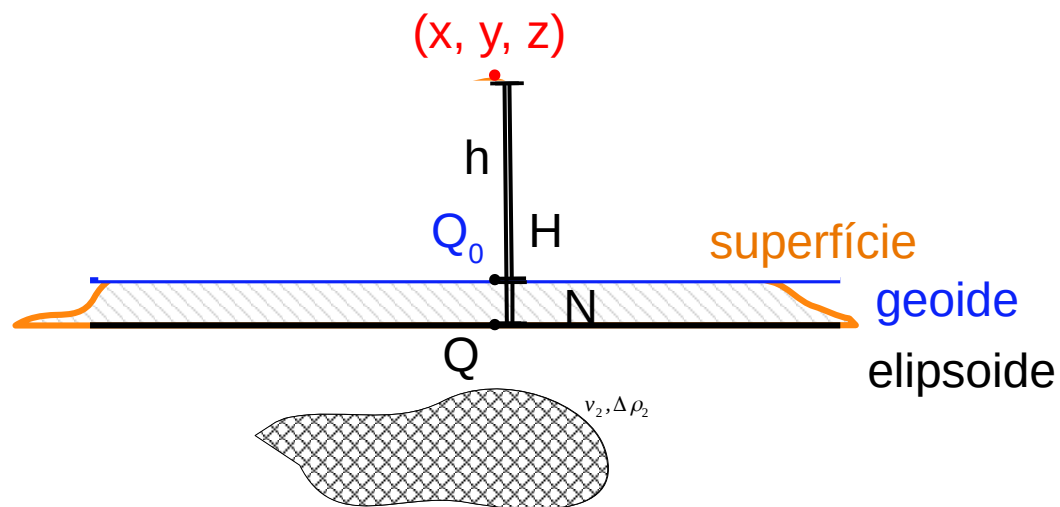


$$\delta g_P = g_P - \gamma_P - 2\pi G \tilde{\rho}_4 h$$

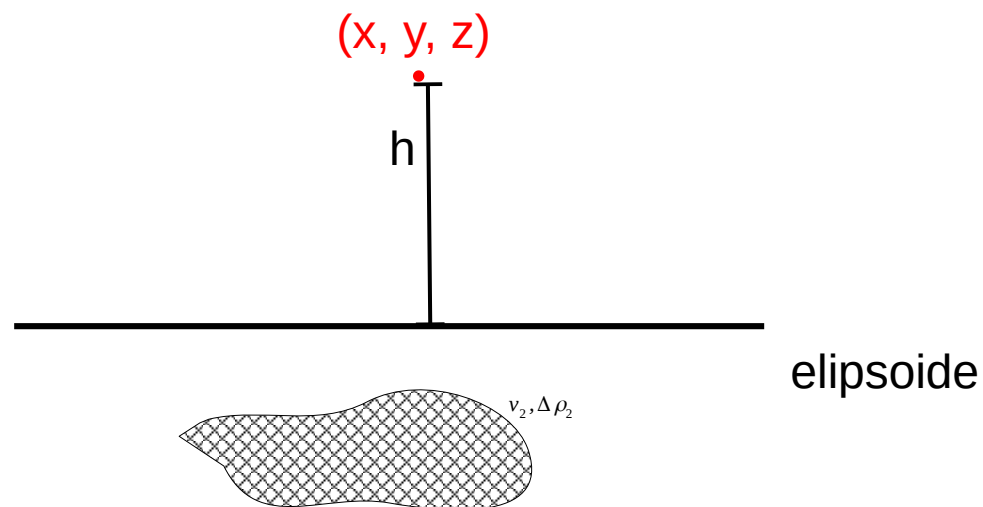


$$\Delta g_P = g_P - \gamma_P - 2\pi G \tilde{\rho}_4 h - 0.3086 N + 2\pi G \tilde{\rho}_4 N$$

disturbio



$$\delta g_P = g_P - \gamma_P - 2\pi G \tilde{\rho}_4 h$$

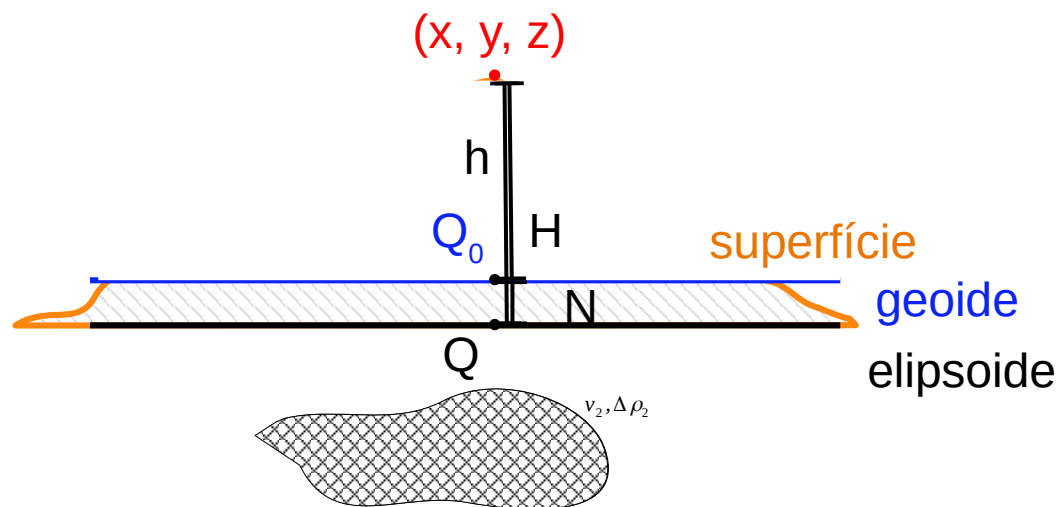


$$\Delta g_P = g_P - \gamma_P - 2\pi G \tilde{\rho}_4 h - 0.3086 N + 2\pi G \tilde{\rho}_4 N$$

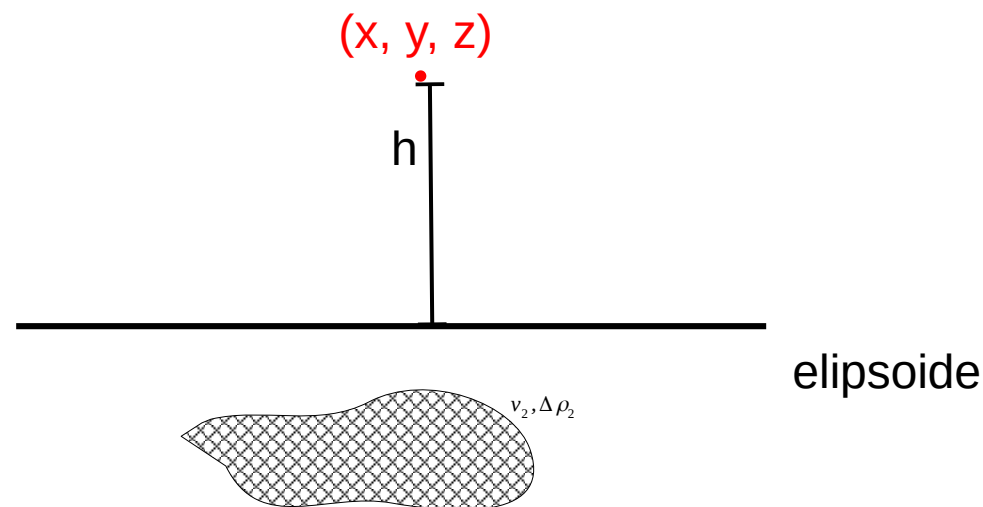
distúrbio

Efeito geofísico indireto

(Hinze et al 2005)

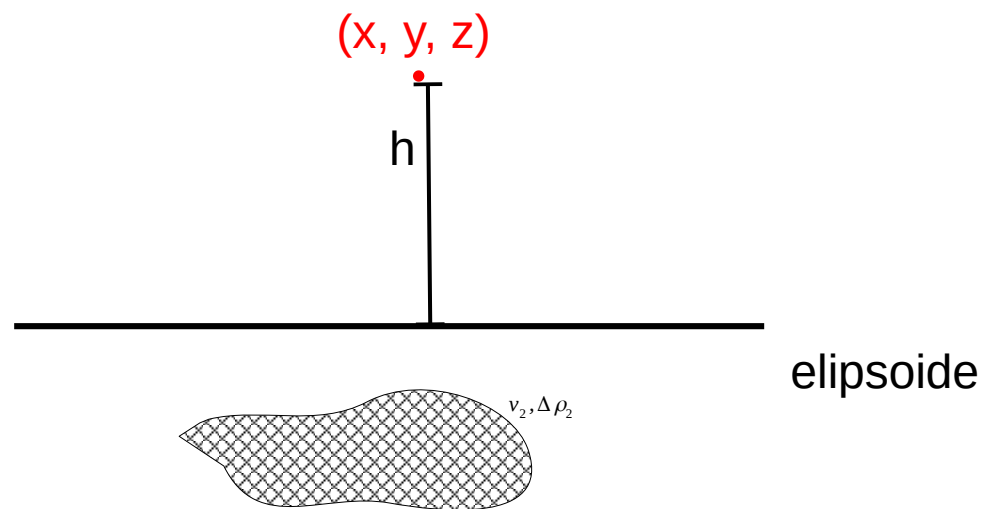
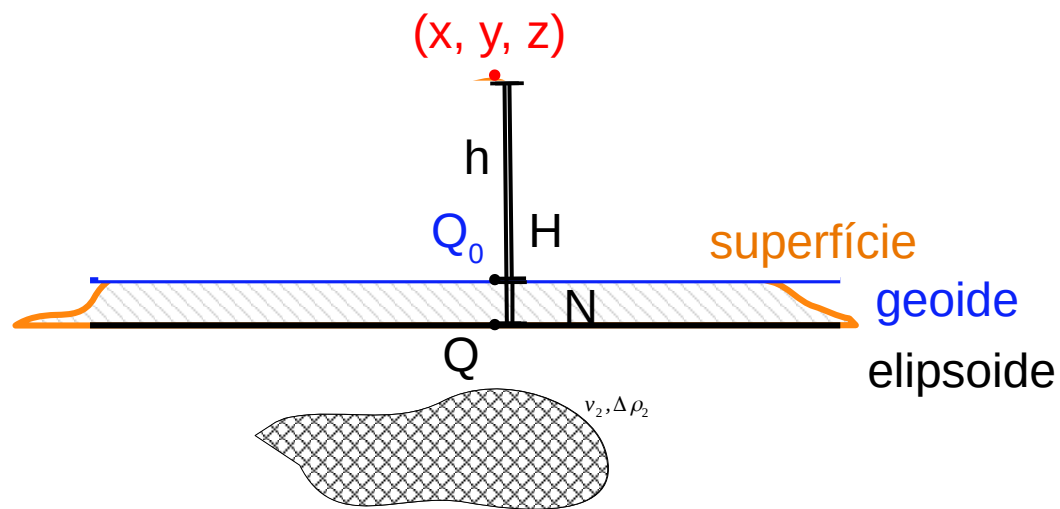


$$\delta g_P = g_P - \gamma_P - 2\pi G \tilde{\rho}_4 h$$

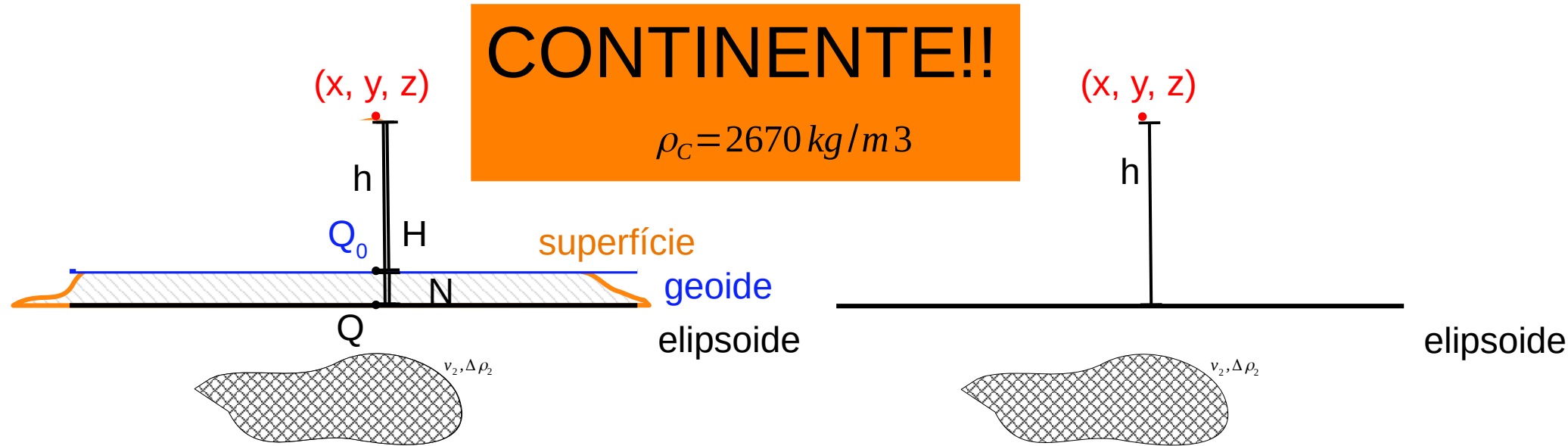


$$\Delta g_P = g_P - \gamma_Q - (0.3086 H + 2 \pi G \tilde{\rho}_4 10^{-5} H)$$

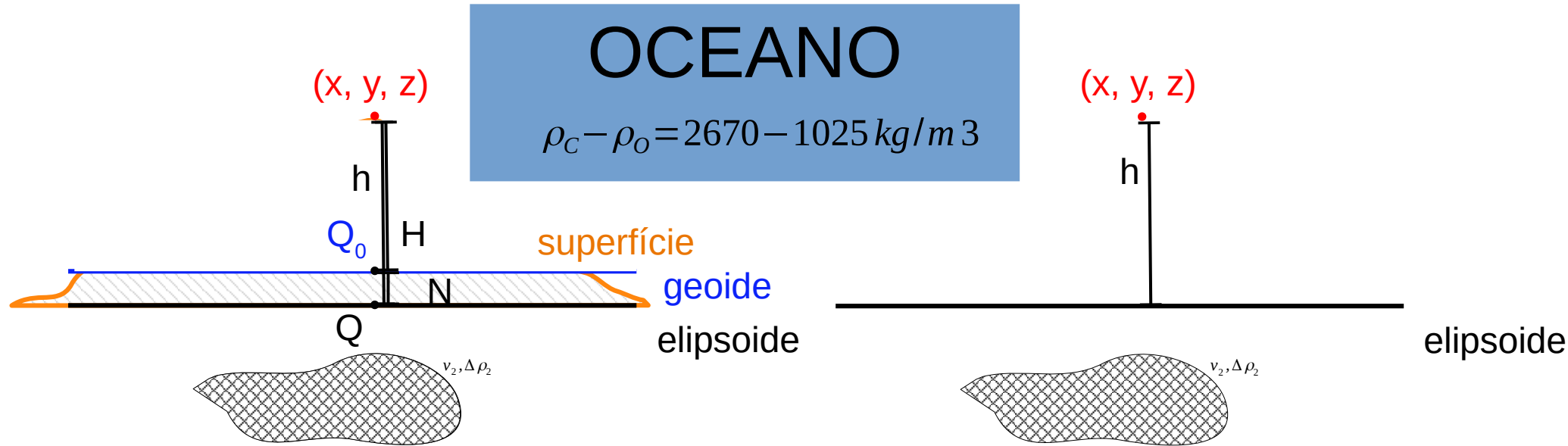
$$\delta g_P = g_P - \gamma_P - 2 \pi G \tilde{\rho}_4 10^{-5} h$$



$$\Delta g_P = g_P - \gamma_Q - (0.3086 H + 2 \pi G \tilde{\rho}_4 10^{-5} H) \quad \delta g_P = g_P - \gamma_P - 2 \pi G \tilde{\rho}_4 10^{-5} h$$



$$\Delta g_P = g_P - \gamma_Q - (0.3086 H + 2 \pi G \tilde{\rho}_4 10^{-5} H) \quad \delta g_P = g_P - \gamma_P - 2 \pi G \tilde{\rho}_4 10^{-5} h$$



Exercício aula 13

- Calcule as altitudes geométrica, ortométrica e geoidal
 - Altitude geoidal: N = geoide
 - Altitude ortométrica: H = topography
 - Altitude geométrica: $h = H+N$
- Calcule o γ_P e γ_Q usando a função que já está no notebook
- Calcule o distúrbio de gravidade usando a fórmula:

$$\delta g_P = g_P - \gamma_P$$

- Calcule o distúrbio corrigido da topografia

$$\delta g_P = g_P - \gamma_P - 2 \pi G \tilde{\rho}_4 10^5 h$$

- Calcule a anomalia ar-livre

$$\Delta g_P = g_P - \gamma_Q - (-0.3086 H)$$

- Calcule a anomalia Bouguer

$$\Delta g_P = g_P - \gamma_Q - (0.3086 H + 2 \pi G \tilde{\rho}_4 10^{-5} H)$$

Exercício aula 13

- Observações:
- Uso da função Gamma:

```
import gamma
a, f, GM, omega = gamma.WGS84()
gamma_P = gamma.closedform(a, f, GM, omega, latitude, h_surface)
a, f, GM, omega = gamma.WGS84()
gamma_Q = gamma.closedform(a, f, GM, omega, latitude, np.zeros_like(h))
```
- Caso a área contenha continente e oceano, para calcular o distúrbio e a anomalia considerando os dois, são necessárias algumas modificações:
 - Calcular o distúrbio corrigido da topografia em duas etapas:
 - Calcular o distúrbio para os pontos no continente usando o $\rho_{\text{continete}} = 2067$
 - Calcular o distúrbio para os pontos no oceano usando $(\rho_{\text{oceano}} - \rho_{\text{continete}})$: $\rho_{\text{oceano}} = 1025$
 - Calcular a anomalia bouguer em duas etapas da mesma forma acima
- Variáveis:
 $G = 6.674 \cdot 10^{-11}$

Referencias

- Hinze, W. J., C. Aiken, J. Brozena, B. Coakley, D. Dater, G. Flanagan, R. Forsberg, T. Hildenbrand, G. R. Keller, J. Kellogg, R. Kucks, X. Li, A. Mainville, R. Morin, M. Pilkington, D. Plouff, D. Ravat, D. Roman, J. Urrutia-Fucugauchi, M. Véronneau, M. Webring, and D. Winester, 2005, New standards for reducing gravity data: The north american gravity database: *Geophysics*, 70, J25–J32. doi: 10.1190/1.1988183