

Solution

$$\frac{d^2}{dx^2} \left(\arcsin \left(\frac{b}{L} \sin \left(\arccos \left(\frac{x}{b} \right) \right) \right) \right) = -\frac{b\sqrt{L^2} \left(x^4 - b^4 + b^2 L^2 \right)}{L\sqrt{b^2} \left(L^2 - b^2 + x^2 \right) \left(b^2 - x^2 \right) \sqrt{-x^2 + b^2} \sqrt{x^2 + L^2 - b^2}}$$

Steps

$$\frac{d^2}{dx^2} \left(\arcsin \left(\frac{b}{L} \sin \left(\arccos \left(\frac{x}{b} \right) \right) \right) \right)$$

Simplify
$$\arcsin\left(\frac{b}{L}\sin\left(\arccos\left(\frac{x}{b}\right)\right)\right)$$
: $\arcsin\left(\frac{b\sqrt{b^2-x^2}}{L\sqrt{b^2}}\right)$

Show Steps

$$= \frac{d^2}{dx^2} \left(\arcsin \left(\frac{b\sqrt{b^2 - x^2}}{L\sqrt{b^2}} \right) \right)$$

$$\frac{d}{dx} \left(\arcsin \left(\frac{b\sqrt{b^2 - x^2}}{L\sqrt{b^2}} \right) \right) = -\frac{bx\sqrt{L^2}}{L\sqrt{b^2}\sqrt{L^2 - b^2 + x^2}\sqrt{b^2 - x^2}}$$

Show Steps

$$= \frac{d}{dx} \left(-\frac{bx\sqrt{L^2}}{L\sqrt{b^2}\sqrt{L^2 - b^2 + x^2}\sqrt{b^2 - x^2}} \right)$$

$$\frac{d}{dx} \left(-\frac{bx\sqrt{L^2}}{L\sqrt{b^2}\sqrt{L^2 - b^2 + x^2}\sqrt{b^2 - x^2}} \right) = -\frac{b\sqrt{L^2}\left(x^4 - b^4 + b^2L^2\right)}{L\sqrt{b^2}\left(L^2 - b^2 + x^2\right)\left(b^2 - x^2\right)\sqrt{-x^2 + b^2}\sqrt{x^2 + L^2 - b^2}}$$
Show Steps

$$= -\frac{b\sqrt{L^2}(x^4 - b^4 + b^2L^2)}{L\sqrt{b^2}(L^2 - b^2 + x^2)(b^2 - x^2)\sqrt{-x^2 + b^2}\sqrt{x^2 + L^2 - b^2}}$$