

$$f(z) = P_0 + P_1 * \int_{-\infty}^x e^{-\left(\frac{z^2}{2}\right)} dz$$

$$z = \frac{\sqrt{x'} - \sqrt{\mu'}}{2\sigma} ; z^2 = \frac{x + \mu - 2\sqrt{\mu'}\sqrt{x'}}{4\sigma^2}$$

$$\frac{z^2}{2} = \frac{x + \mu - 2\sqrt{\mu'}\sqrt{x'}}{8\sigma^2} .$$

$$\frac{\partial f}{\partial \mu} = P_1 * \left[\frac{\partial}{\partial \mu} \left\{ \int_{-\infty}^{x'} e^{-\frac{x}{8\sigma^2}} e^{-\frac{\mu}{8\sigma^2}} e^{\frac{\sqrt{\mu'}\sqrt{x'}}{4\sigma^2}} dz \right\} \right]$$

$$\frac{\partial f}{\partial \mu} = P_1 * \left[\int_{-\infty}^{x'} -\frac{1}{8\sigma^2} e^{-\left(\frac{z^2}{2}\right)} dz + \int_{-\infty}^{x'} \frac{1}{8\sigma^2} \frac{\sqrt{x'}}{\sqrt{\mu'}} e^{-\left(\frac{z^2}{2}\right)} dz \right]$$

In the code: $\text{freq}(x) = \int_{-\infty}^{x'} e^{-\left(\frac{z^2}{2}\right)} dz$

$$\frac{\partial f}{\partial \mu} = -\frac{P_1}{8\sigma^2} \text{freq}(x) + \frac{P_1}{8\sqrt{\mu'}\sigma^2} \int_{-\infty}^{x'} \sqrt{x'} e^{-\left(\frac{z^2}{2}\right)} dz$$

Let's remember: $z = \frac{\sqrt{x'} - \sqrt{\mu'}}{2\sigma}$

$$\sqrt{x'} = 2\sigma z + \sqrt{\mu'}$$

$$\int_{-\infty}^{x'} \sqrt{x'} e^{-\left(\frac{z^2}{2}\right)} dz = \int_{-\infty}^{x'} 2\sigma z e^{-\left(\frac{z^2}{2}\right)} dz + \underbrace{\sqrt{\mu'} \int_{-\infty}^{x'} e^{-\left(\frac{z^2}{2}\right)} dz}_{\text{freq}(x)}$$

$$\frac{\partial f}{\partial \mu} = -\frac{P_1}{8\sigma^2} \text{freq}(x) + \frac{P_1}{8\sqrt{\mu'}\sigma^2} \int_{-\infty}^{x'} \sqrt{x'} e^{-\left(\frac{z^2}{2}\right)} dz$$

$$\frac{\partial f}{\partial \mu} = -\cancel{\frac{P_1}{8\sigma^2} \text{freq}(x)} + \cancel{\frac{P_1}{8\sigma^2} \text{freq}(x)} +$$

$$\sigma^2 \frac{P_1}{8\sqrt{\mu'}} \int_{-\infty}^{x'} 2\sigma z e^{-\left(\frac{z^2}{2}\right)} dz$$

→ need to integrate

$$\int_{-\infty}^{x'} z e^{-\left(\frac{z^2}{2}\right)} dz = e^{-\left(\frac{z^2}{2}\right)} \Big|_{-\infty}^{x'}$$

in our case $-\infty \rightarrow 0$ and $x' = 200$

$$\text{So } \int_0^{\infty} z e^{\left(-\frac{z^2}{2}\right)} dz = 1$$

$$\text{Therefore: } \frac{\partial f}{\partial \mu} = \frac{P_1}{4\sqrt{\mu}\sigma}$$

OK, we need to check but it looks reasonable. Now, let's work on $\frac{\partial f}{\partial \sigma} \dots$

$$\frac{\partial f}{\partial \sigma} = P_1 * \left[\frac{\partial}{\partial \sigma} \left\{ \int_{-\infty}^x e^{-\frac{x^2}{8\sigma^2}} e^{-\frac{\mu^2}{8\sigma^2}} e^{\frac{\sqrt{\mu}\sqrt{x}}{4\sigma^2}} dz \right\} \right]$$

$$\frac{\partial f}{\partial \sigma} = P_1 * \left[\frac{\partial}{\partial \sigma} \left\{ \int_0^{\infty} e^{-\frac{1}{8\sigma^2}(x+\mu - 2\sqrt{\mu}\sqrt{x})} dz \right\} \right]$$

$$\beta = \frac{1}{\sigma^2} \quad \therefore \quad \frac{d\beta}{d\sigma} = -\frac{1}{\sigma^3}$$

$$\frac{\partial f}{\partial \sigma} = P_1 * \frac{\partial \beta}{\partial \sigma} \frac{\partial}{\partial \beta} \left\{ \int_0^{\infty} e^{-\frac{1}{8}\beta(x+\mu - 2\sqrt{\mu}\sqrt{x})} dz \right\}$$

$$\frac{\partial f}{\partial \sigma} = p_1 * \left(-\frac{1}{2\sigma^3}\right) \left\{ -\frac{1}{8} \int_0^{2\sigma} (x+\mu - 2\sqrt{\mu'}\sqrt{x'}) e^{-\frac{1}{8}\beta(x')} dz \right\}$$

Remember: $\frac{z^4}{2} = \frac{x+\mu - 2\sqrt{\mu'}\sqrt{x'}}{8\sigma^2}$

$$\frac{\partial f}{\partial \sigma} = \frac{p_1}{2\sigma} * \left\{ \int_0^{2\sigma} \frac{z^2}{2} e^{-\left(\frac{z^2}{2}\right)} dz \right\}$$