

University of Applied Sciences Würzburg-Schweinfurt Faculty of Computer Science and
Business Information Systems

Bachelor-Thesis

Evaluation and implementation of gradient descent algorithms on streaming data

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Summary

TODO

Abstract

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Note of thanks

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1 Introduction

The following chapter will give the reader a short explanation what inspired the work for this thesis, what its purpose is and what it wishes to achieve, as well as an explanation how this work is structured, to give the reader a better orientation for how to navigate this work.

1.1 Inspiration for this Thesis

1.2 Purpose of this Thesis

1.3 Outline of the Thesis

In the second Chapter of this thesis will give a short overview over the basics of Machine Learning that are relevant for the understanding of the premise for the thesis. It will give also a short description about what is special about Data stream in Machine learning algorithms and what is important to take into account when working with them. It will also give a short introduction about the criteria with which the comparison of the different implementations of the Algorithm take place and why these criteria are used for comparison. In the last part of the first chapter will be the framework introduced that was used for implementation and comparison.

The next chapter will then continue to give a deeper look into the deeper parts of the subsection of Machine learning and the Algorithm that is the basis for the different variation of implementation for the Algorithms. It will also give a short introduction about the version that this algorithm was based on, as this is important to later understand the variations and differences in the other implementations. In the last part of that chapter will then explain the different methods and the implementations of the variants in greater detail.

The fourth chapter will then list and describe the used synthetic and real world streaming

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data sets that were used to perform the experiments. Furthermore will be describe how the experiments were conducted and with which methods the results were controlled.

Following this, the next chapter will be dedicated for the result evaluation what what we informations were hopefully gained from conducting these experiments for the comparison of these implementations.

The last chapter will summarize all the work that was done and give a final evaluation to the algorithms.

2 Basics

The Goal of this Chapter is to give the Reader a basic understanding of how Machine Learning Algorithms work. Furthermore, it will describe what the difference is between unsupervised and supervised learning.

There will be also an introduction and description on how the Gradient Descent Algorithm, that is the basis for the Modified versions of the Algorithms that will be compared in this work, works and how it decides what to do. After this is done there will be also a short description on what Streaming Data is and on the framework that is used to realise the implementation of the Experiments.

Finally there will be an explanation on how the criteria for the comparison of the Algorithms were chosen and how these criteria work.

2.1 Machine Learning

The term 'Machine Learning' stands for a collection of self-learning algorithms, that learn from input Data to make fast and correct decisions and predictions. It is important to remember that it is not a real Artificial intelligence, but rather a sequence of statistical analyses on given data, with the goal to make gradual improvements to the prediction models of the algorithm. A Machine can do this optimization a lot faster and effectively than a human, especially if this optimization has to be done in real time on big data input sets. This gives also a bigger flexibility, as a machine that can learn from a changing environment needs lesser redesigns, which leads to less time that gets wasted and can be used more productively on other tasks.

All these are reasons why Machine Learning has an ever increasing importance in the field of computer science, but also a growing impact on everyday life. It is thanks to Machine learning that there are intelligent assistant softwares that can recognize voice commands and questions (Apples SIRI, Amazon Alexa or Microsofts Cortana), e-mail spam filter, nearly self-driving cars, reliable search-engines, faster and more precise weather forecasts and challenging game ai's nowadays

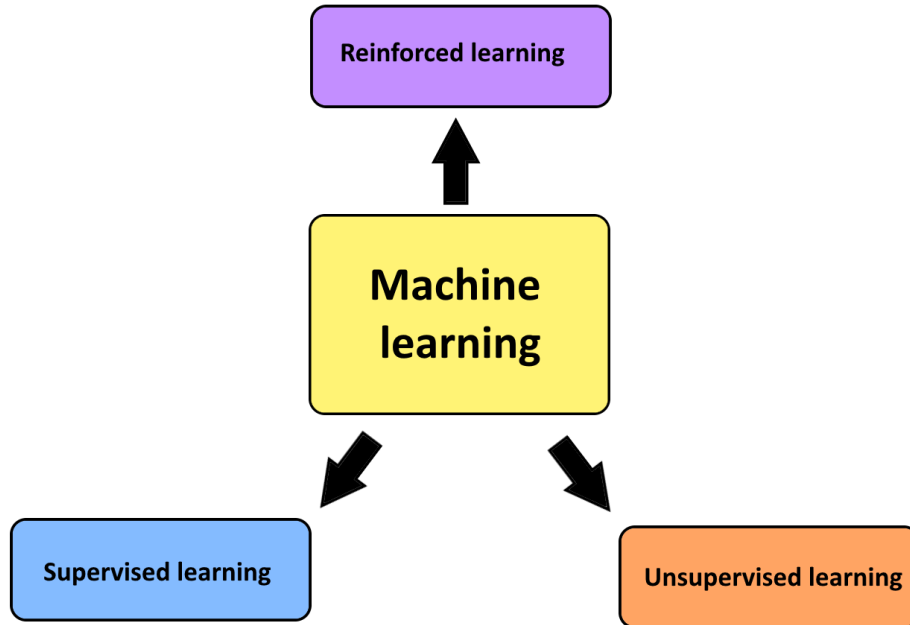


Figure 2.1: Overview of the Machine Learning Strategy's.

Machine Learning Algorithms can be categorisized depending on how they learn from the available training Data to create a model for the predictions. There are three main subdivisions, under wich these algorithms can fall. The first one is the Supervised learning strategy, then the Unsupervised learning strategy and the Reinforced learning strategy.

Only the Supervised Learning strategy will be explained in more detail on the following pages, as the focus of this thesis lays in the comparision of several different implemen-tations of classification algorthims that are based on Supervised Learning.

[12]

2.1.1 Supervised Learning

The idea behind Supervised learning is to create a model from a already labeled training data set, that then can make prediction and decision on new or unknown data based on the learned model from the training set. The following example will help to understand this easier. Lets say a fruit farmer wants to automatically sort the harvested Fruits in either categorie A or B for the market. The sorting device is equiepped with 2 sensors to measure 2 features, one for colour and another one for the size of the fruit. It then decides to wich of the two classes the fruit belongs to. As this is a System that is capable of dividing features into a discrete number of classes the system can be called a *classifier*. This is a typical exampel of an *classification task*. To configure the System in such a way that it correctly sorts the fruits into the right category, a specailist hand picks several fruits from a small test set and then sorts them depending on the already named features. In other words, the specailist classiefies them. Based on this by hand sortet training set the machine will then later decide how the other fruits should be sorted. It is used as a *model* for the classification. [14] Another type of Supervised learning is the *regression task*. The difference to the *classification task* is, that instead of a *discrete* number of classes that gets returned, a *continous* number of classes will be returned. An example of a *regressive task* is, for example, the prediction of the Stock market or the price of medications.

The Process as seen in figure 2.2 and as described as in the example of the farmer and his sorted fruits shows how the supervised learning works. The Algorithm (marked in green) learns with the help of the labeled training data. The result of this learning is then that the trained Algorithm, now called predictive model, can be used in a production enviroment. New, unlabeled, data can then be send into the predictiv model to get a predictied model as an output. [16]

To better understand how this predictiv model is formed, one has to understand how the classification task works. In the classification task the computer programm is asked to specify which of k catergories a input belongs to. To solve this task, the learning algorithm is usually asked to produce a function $f : \mathbb{R} \rightarrow 1, \dots, k$. When $y = f(\mathbf{x})$, the model assigns an input described by vector \mathbf{x} to a category identified by numeric code y . There are other variants of the classification task, for example, where f outputs a probability distribution over classes. An example of a classification task is object recognition, where the input is an image (usually described as a set of pixel brightness values), and the output is a numeric code identifying the object in the image. [8]

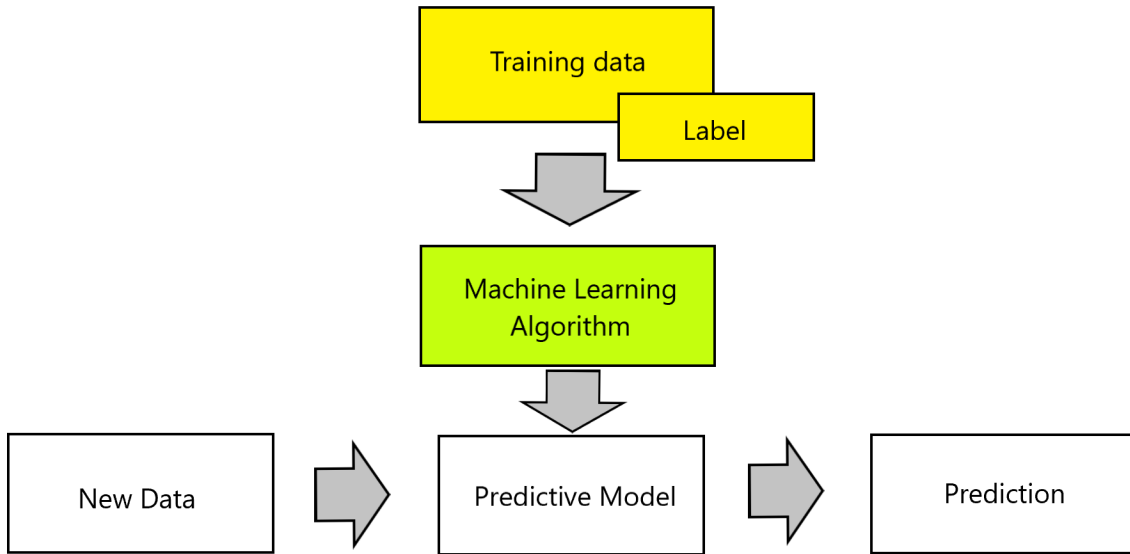


Figure 2.2: Process of the Supervised Learning. [16]

Then there must be also differentiated between the type of data that is put into the classification process. In batch or offline classification, a classifier-building algorithm is given a set of labeled examples. The algorithm creates a model, a classifier in this case. The model is then deployed, that is, used to predict the label for unlabeled instances that the classifier builder never saw. If we go into more detail, we know that it is good methodology in the first phase to split the dataset available into two parts, the training and the testing dataset, or to resort to cross-validation, to make sure that the classifier is reasonably accurate. But in any case, there is a first training phase, clearly separated in time from the prediction phase.

In the online setting, and in particular in streaming, like it is this thesis, this separation between training, evaluating, and testing is far less clear-cut, and is interleaved. We need to start making predictions before we have all the data, because the data may never end. We need to use the data whose label we predict to keep training the model, if possible. And probably we need to continuously evaluate the model in some way to decide if the model needs more or less aggressive retraining. [3]

2.1.2 Gradient Descent

The Gradient descent Algorithm is one of the most popular Algorithms to perform optimizations on and is by far the most common way to optimize neural networks. This is also the reason why nearly every state-of-the-art Deep learning library has various forms of implementations to perform optimization on the gradient descent. The Problem, however is, that these Algorithms often perform as some form of black-box, because a practical explanation of what their strengths and weaknesses is are hard to find and explain. Gradient descent is a way to minimize an objective function $J(\theta)$ parameterized by a model's parameters $\theta \in \mathbb{R}^d$ by updating the parameters in the opposite direction of the gradient of the objective function $\nabla_{\theta} J(\theta)$ with respect to the parameters. The learning rate η determines the size of the steps we take to reach a local minimum. In other words, we follow the direction of the slope of the surface created by the objective function downhill until we reach a valley. [17]

The normal gradient descent, also known as batch-gradient descent, computes the gradient of the function with respect to the parameters θ for the entire training set:

$$\theta = \theta - \eta * \nabla_{\theta} J(\theta) \quad (2.1)$$

Since we need to calculate the gradients for the complete dataset to get just one update, batch gradient descent can get very slow and is intractable for dataset that do not fit into the memory. For this reason the batch gradient descent implementation can not be used in this comparison, as it is not able to perform updates "on-the-fly", as this is a necessity for use on streaming Data.

In contrast to that, the Stochastic Gradient Descent (short: SGD) can perform a update for *each* training example $x^{(i)}$ and label $y^{(i)}$:

$$\theta = \theta - \eta * \nabla_{\theta} J(\theta; x^{(i)}; y^{(i)}) \quad (2.2)$$

While the batch gradient descent performed redundant computations for large datasets, as it recomputes gradients for similar examples before each update, the SGD puts away this redundancy by performing one update at a time. Because of that it performs much faster and can be used on Streaming Data. The SGD performs frequent updates with a high variance, that causes the objective function to fluctuate heavily.

This fluctuation enables the SGD to jump to new and potentially better local minima, while the batch gradient only converges to the minimum of the basin the parameters are placed in. But this also ultimately complicates the convergence to the exact minimum, as

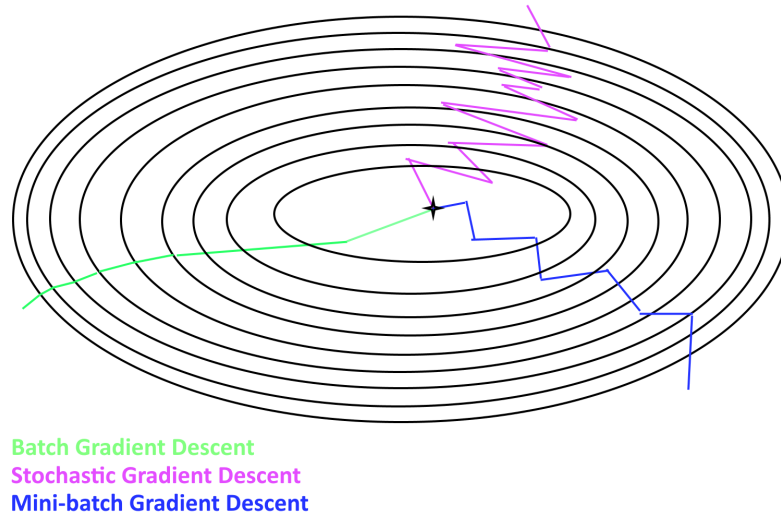


Figure 2.3: Visualisation differences of the three Gradient Descent Algorithms

the SGD keeps overshooting. This can be fixed by slowly decreasing the learning rate, as the SGD then shows the same convergence behaviour as the batch gradient descent. It then almost certainly converges to a local or global minimum for non-convex and convex optimization respectively. [17] These advantages lead to the fact that the SGD is the most common Gradient descent algorithm.

Then there is also the Mini-batch gradient descent algorithm. It takes the best of both worlds and performs an update for every mini-batch on n training examples:

$$\theta = \theta - \eta * \nabla_{\theta} J(\theta; x^{(i:i+n)}; y^{(i:i+n)}) \quad (2.3)$$

This way it reduces the variance of the parameter updates, which can lead to a more stable convergence. It can also make use of highly optimized matrix optimizations common for state-of-the-art deep learning libraries, that makes computing the gradient with respect to a mini-batch very efficient. Common mini-batch sizes range between 50 and 256, but can vary for different applications. Typically the Mini-batch gradient descent is the algorithm of choice when there is a neural network to train and the term SGD is usually also employed even when a mini-batches are used. [17]

2.2 Streaming Data

Data streams are an algorithmic abstraction to support real-time analytics. They are sequences of items, possibly infinite, each item having a timestamp, and so a temporal order. Data items arrive one by one, and we would like to build and maintain models, such as patterns or predictors, of these items in real time. There are two main algorithmic challenges when dealing with streaming data: the stream is large and fast, and we need to extract information in real time from it. That means that usually we need to accept approximate solutions in order to use less time and memory. Also, the data may be evolving, so our models have to adapt when there are changes in the data. [3]

2.2.1 Challenges with Streaming Data

[7]

2.3 Framework

The following section will shortly introduce the python based scikit-multiflow framework, with which the the comperssion of the different implementations of the RSLVQ algorithm where done.

2.3.1 SCIKIT-Multiflow

Scikit-multiflow is a framework that is inspired by the Massive Online Analysis (MOA), the most popular open source framework for machine learning on data streams, and MEKA, an open source implementation of methods for multi labeling. Scikit-multiflow is also inpired by scikit-learn, the most popular framework for machine learning in Python. Following the Scikit philosophy, scikit-multiflow is an open source machine-learning framework for multi-output/multi-label and stream data.

The Scikit-multiflow does not provide a graphical user interface like the MOA framework that it was inspired by. On the other hand can it be used within Jupyter notebooks, a popular interface in the data scientist community that is based on python. It is mainly a library that contains stream generators, learning methods, change detectors and evaluation methods for Machien learning algorithms on streaming data. Scilit-

multiflow lays a special focus on its design, so that it is user friendly to new user and familiar for more experienced ones.[11]

It achieves this by having a simple workflow that can be easily describe in 4 steps:

1. Create a stream:

A stream can be generate by use of either one of the predefiend Stream generators or by importing a Stream from a file.

2. Instantiate a classifier:

In this step the user has to choose by which type of algorithm the classifikation process should be accomplished.

3. Setup the evaluator:

Next the user has to choose if the evaluation process should be done presequential or by Hold-out method. Prequential-evaluation or interleaved-testthen-train evaluation, is a popular performance evaluation method for the stream setting only, where tests are performed on new data before using it to train the model. Hold-out evaluation is a popular performance evaluation method for batch and stream settings, where tests are performed in a separate test set. [11]

4. Run the evaluation:

The evaluator will perform the following subtask in this final step, first, it will check if there are still samples in the stream and then it will pass the next sample to the classifier, which will either test the sample with the `predict()` method or it willl update the clasefier with the `partial_fit()` method of the clasifier.

To give better understanding how this exactly works, 2.1 will provide a small example where a synthetic waveform gets generated with the WaveformGenerator. This generator will create a synthetic stream that generates default samples with 21 numeric attributes and 3 target values, based on a random differentiation of some base waveforms. For the classifier is the Hoeffding Tree choosen with default parameters. After this we chose a prequential evaluator with the following parameters:

- `show_plot = true`, this will generate us a dynamic plot that will update as the classifier is trained.
- `pretrain_size = 200`, this parameter sets the number of samples that is used for the first training set.
- `max_sample = 20000`, this parameter set the maximum number of samples that should be used.

In the last step we then call evaluator method, that will then update the results and the plot. It is to note that at the time this thesis was written, the accuracy score stand for the performance in the framework. [11]

Listing 2.1: Simple example of the scikit-multiflow workflow

```

1  """1. Create a stream"""
2  stream = WaveformGenerator()
3  stream.prepare_for_use()
4
5
6  """2. Instantiate the HoeffdingTree classifier"""
7  ht = HoeffdingTree()
8
9  """3. Setup the evaluator"""
10 evaluator = EvaluatePrequential(show_plot=True,
11                                pretrain_size=200,
12                                max_samples=20000)
13
14 """4. Run evaluation"""
15 evaluator.evaluate(stream=stream, model=ht)

```

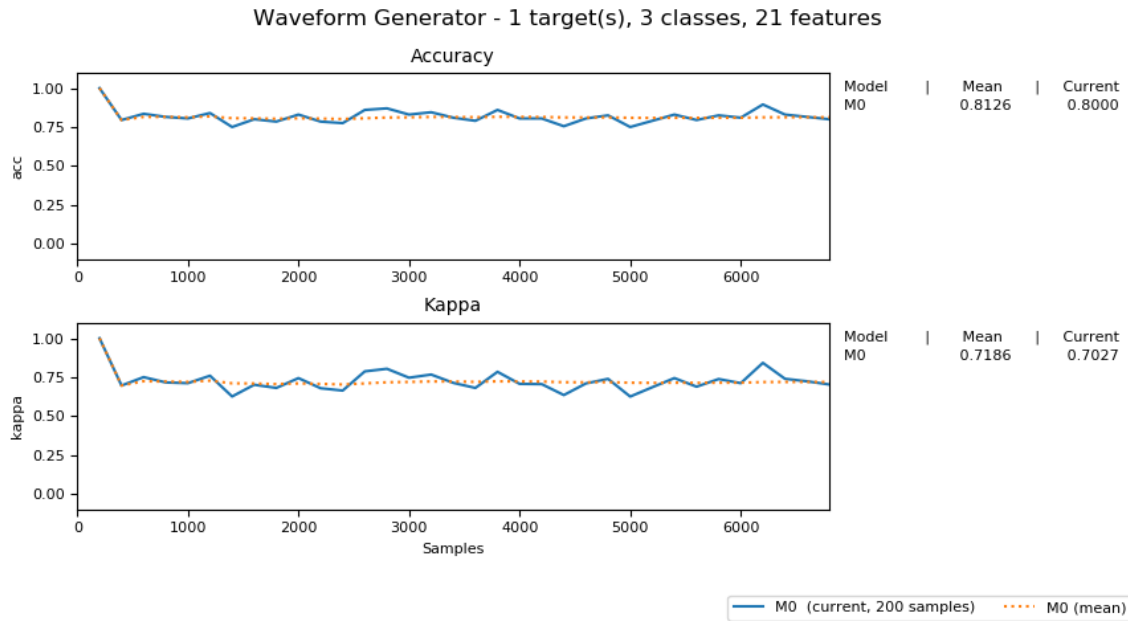


Figure 2.4: Result Table of the example in 2.1

2.4 Criteria for the Comparison

This section will explain on what criteria this thesis will base the comparison of the different implementations. It will also describe what the difference between the criteria is and why this is important to know. It will define what this thesis understands under the terms performance and accuracy, as well as what the differences between the used error-estimations are.

2.4.1 Evaluations for Data Streams

To evaluate a learning algorithm, it must be known which examples were used to train the algorithm and which are used to test the model output by the algorithms. Which procedure is used in batch learning has partly depended on data size. For small data sets with ≤ 1000 examples the procedure of cross-validation was well suited, as it made maximum use of the data that it could use. A Problem arose when the size of the data kept increasing, as this practically created a time limit for procedures that kept repeating the training process to many times. For this reason it is common practice to try to reduce the number of folds and repetitions for big data sets to allow experiments to conclude in reasonable time. One way to achieve this is to take several hundreds of thousand samples in a single batch and take them for a single holdout run, as this requires the least computational effort. The rationalization for this, beside the practical time issues, is that the reliability we may lose by not having repeated runs is compensated by the reliability gained by the sheer number of samples that are used. There are two main approaches that we have to consider for the evaluation process, the first one being Holdout and the second being Prequential. [1]

These two approaches will be now be described in more detail:

- **Holdout:** It is often acceptable to measure the performance with a single holdout set when the batch learning would otherwise reach a scale where cross-validation would be too time consuming. This can get very helpful, as the results of different studies can be directly compared to each other. To do this, the division between the train and test set have to be predefined. To track model performance over time, the model can be evaluated periodically, for example, after every one million training examples. Testing the model too often has potential to significantly slow the evaluation process, depending on the size of the test set. A source for holdout data sets are for example sets of data of the stream that have not yet been used to train the learning algorithm. These sets could be taken from "further ahead" in the stream to be used as test sets and could then later be used again to train the learning algorithm again after the testing is complete. This procedure would be recommendable in scenarios with concept-drift, as it would measure a model's ability to adapt to the latest trends in the data. In scenarios without drift,

a single static holdout set should be sufficient, as this would avoid varying estimates between test sets. If it is assumed that the test set is independent and sufficiently large in relation to the complexity of the target concept, it can be concluded that it then will provide an accurate measurement of generalization accuracy. [1]

- **Prequential:** An alternative approach to evaluate data stream algorithm is to interleave testing with training. Each individual set can be used to test the model before it is used for training and then the accuracy can be incrementally updated from this. When it is performed in this order the model will always be tested by sets that it has not seen yet. This has the advantage that no holdout set is needed to perform testing. This also results in a smooth plot of the accuracy over time, as each individual set will become increasingly more insignificant to the overall average. This approach also has its disadvantages, as it make it difficult to accurately separate and measure training and testing times. It also obscures the true accuracy that the algorithm can achieve at a given point, as the algorithm gets punished for mistakes that it made earlier regardless of the level of accuracy they are eventually capable of. It also has to be said that this effect will diminish over time. With this approach the statistics are updated with every set from the stream and can be recorded at this level of detail if desired. To increase the efficiency a sampling parameter can be used to reduce the required storage for the results, by recording only at periodic intervals like the holdout method. [1]

2.4.2 Performance

Performance is the ability of the classifier not to label as positive an instance that is negative.

2.4.3 Accuracy score

Accuracy is the number of instances correct classified / total number of instances.

3 Used Algorithms

3.1 Theoretical Work

This chapter will try to give a short explanation about how the Robust Soft Learning Vector Quantization Algorithm (short: RSLVQ) works and will also explain the algorithm that it is based on. Furthermore will it explain what momentum based gradient descent algorithms there are and how they work. These are used in the different optimization implementation of the RSLVQ that will be compared in the later chapters.

3.2 Learning Vector Quantization

3.3 Robust Soft Learning Vector Quantization

[18]

3.4 Momentum Based Gradient Descent

The following section will outline three algorithms that are widely used in the Deep learning Community and that will later be used to optimize the RSLVQ Algorithm in hopes to improve its performance and accuracy.

3.4.1 Momentum

SGD has trouble navigating ravines, i.e. areas where the surface curves much more steeply in one dimension than in another [20, 17], which are common around local

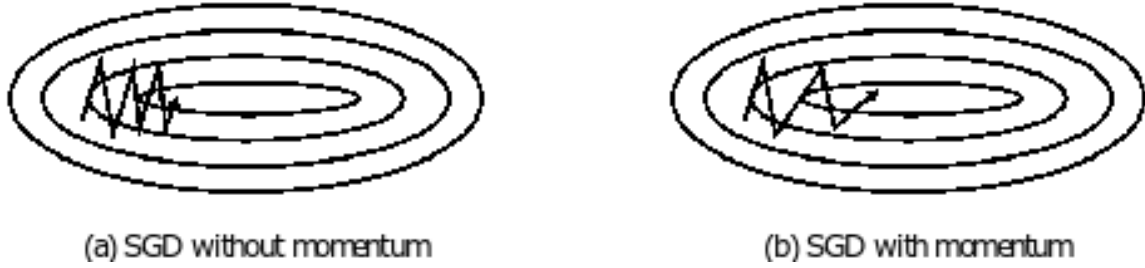


Figure 3.1: Differences of a SGD with and without momentum.¹

optima. In these scenarios, SGD oscillates across the slopes of the ravine while only making hesitant progress along the bottom towards the local optimum as in figure.

Momentum [15, 17] is a method that helps accelerate SGD in the relevant direction and dampens oscillations as can be seen in figure . It does this by adding a fraction γ of the update vector of the past time step to the current update vector

$$\begin{aligned} v_t &= \gamma v_{t-1} + \eta \theta - \eta \nabla_{\theta} J(\theta) \\ \theta &= \theta - v_t \end{aligned} \tag{3.1}$$

The momentum term γ is usually set to 0.9 or a similar value.

In his Article, Ruder [17] describes it like if we would push a ball down a hill. The ball accumulates momentum as long as it rolls downhill, becoming faster and faster on the way (until it reaches its terminal velocity, if there is air resistance, i.e. $\gamma < 1$). The same thing happens to our parameter updates: The momentum term increases for dimensions whose gradients point in the same directions and reduces updates for dimensions whose gradients change directions. As a result, we gain faster convergence and reduced oscillation.

3.4.2 Adagrad

The first algorithm that will be described is the Adagrad [21]. It has to be noted that this algorithm will not be part of the comparison, but as this algorithm is the base from which the Adadelta and later the RMSprop were developed from, it will be shortly explained nonetheless. The Adagrad is an algorithm for gradient-based optimization that adapts to updates for each individual parameter to perform larger or smaller updates

¹Genevieve B. Orr

3 Used Algorithms

depending on their importance. The learning rate gets adapted to the parameters, were it performs larger updates if the parameters are more infrequent and smaller updates if they are frequent. Hence, it is well-suited to deal with sparse data. As other works [4] have shown, this greatly improves the robustness of SGD, which lead to its wide use to train large Neural Networks. It was also used to train GloVe word embeddings as infrequent words require much larger updates than frequent ones [13, 17].

For the reason that Adagrad uses a different learning rate for every parameter θ_i at every time step t , Adagrad's per-parameter update is first shown and then vectorized. For brevity, we set $g_{t,i}$ to be the gradient of the objective function w.r.t. the parameter θ_i at the time step t :

$$g_{t,i} = \nabla_{\theta_i} J(\theta_{t,i}) \quad (3.2)$$

The update for every SGD parameter θ_i at time t becomes to:

$$\theta_{t+1,i} = \theta_{t,i} - \eta \cdot g_{t,i} \quad (3.3)$$

In its update rule, Adagrad modifies the general learning rate η each time step t for every parameter θ_i based on the past gradients that have been computed for θ_i :

$$\theta_{t+1,i} = \theta_{t,i} - \frac{\eta}{G_{t,ii} + \epsilon} g_{t,i} \quad (3.4)$$

$G_t \in \mathbb{R}^{d \times d}$ here is a diagonal matrix where each diagonal element i , i is the sum of the squares of the gradients w.r.t. θ_i up to time step t [6], while ϵ is a smoothing term that avoids division by zero (usually on the order of $1e-8$).

As G_t contains the sum of the squares of the past gradients w.r.t. to all parameters θ along its diagonal, we can now vectorize our implementation by performing an element-wise matrix-vector multiplication \odot between G_t and g_t :

$$\Delta\theta_t = -\frac{\eta}{\sqrt{G_t + \epsilon}} \odot g_t \quad (3.5)$$

One of Adagrad's main benefits is that it eliminates the need to manually tune the learning rate. Most implementations use a default value of 0.01 and leave it at that. Adagrad's main weakness is its accumulation of the squared gradients in the denominator: Since every added term is positive, the accumulated sum keeps growing during

training. This in turn causes the learning rate to shrink and eventually become infinitesimally small, at which point the algorithm is no longer able to acquire additional knowledge. [17]

3.4.3 Adadelta

One of the more often used momentum-based algorithm is the Adadelta approach. It is an extension of the Adagrad that seeks to reduce its aggressive, monotonically decreasing learning rate. Instead of accumulating all past squared gradients, Adadelta restricts the window of accumulated past gradients to some fixed size ω .

Rather than inefficiently storing ω previous squared gradients, the sum of gradients is recursively defined as a decaying average of all past squared gradients. The running average $E[g^2]_t$ at time step t then depends (as a fraction γ similarly to the Momentum term) only on the previous average and the current gradient:

$$E[g^2]_t = \gamma E[g^2]_{t-1} + (1 - \gamma) g_t^2 \quad (3.6)$$

We then set γ to a similar value as the momentum, around 0.9. The SGD update will then be rewritten in terms of the parameter update vector $\Delta\theta_t$:

$$\begin{aligned} \Delta\theta_t &= -\eta \cdot g_{t,i} \\ \theta_{t+1} &= \theta_t - \Delta\theta_t \end{aligned} \quad (3.7)$$

Because of this, the parameter update vector, that is base of the parameter update vector of the Adagrad (see equation 3.5), takes the form of:

$$\Delta\theta_t = -\frac{\eta}{\sqrt{G_t + \epsilon}} \odot g_t \quad (3.8)$$

In the next step the diagonal Matrix G_t gets replaced with the decaying average over past squared gradients $E[g^2]_t$:

$$\Delta\theta_t = -\frac{\eta}{\sqrt{E[g^2]_t + \epsilon}} g_t \quad (3.9)$$

3 Used Algorithms

As the denominator is just the root mean squared (RMS) error criterion of the gradient, we can replace it with the criterion short-hand:

$$\Delta\theta_t = -\frac{\eta}{RMS[g]_t} g_t \quad (3.10)$$

As in [5] noted, the units in this update (as well as in the SGD, Momentum and Adagrad) do not match, i.e. the update should have the same hypothetical units as the parameter. To realize this, they first define another decaying average, this time not of squared gradients but of squared parameter updates:

$$E[\Delta\theta^2]_t = \gamma E[\Delta\theta^2]_{t-1} + (1 - \gamma) \Delta\theta_t^2 \quad (3.11)$$

This leads to that the root mean squared error of the parameter updates is:

$$RMS[\Delta\theta]_t = \sqrt{E[\Delta\theta^2]_t + \epsilon} \quad (3.12)$$

Because the $RMS[\Delta\theta]_t$ value is unknown to us, we try to approximate it with the RMS of parameter updates until the previous time step. Replacing the learning rate η in the previous update rule with $RMS[\Delta\theta]_{t-1}$ leads to the final update rule for the Adadelta:

$$\Delta\theta_t = -\frac{RMS[\Delta\theta]_{t-1}}{RMS[g]_t} g_t \theta_{t+1} = \theta_t + \Delta\theta_t \quad (3.13)$$

In the Adadelta we do not need to set a learning rate η , eliminated from the update rule. [17]

3.4.4 RMSprop

RMSprop is an adaptive learning rate method proposed by Geoff Hinton in Lecture 6e of his Coursera Class. [9] As a result of the need to resolve the Adagrad's radically diminishing learning rates, both the Adadelta and the RMSprop had been developed independently from each other at the same time. RMSprop in fact is identical to the first

update vector of Adadelta that we derived above:

$$\begin{aligned} E[g^2]_t &= 0.9E[g^2]_{t-1} + 0.1g_t^2 \\ \theta_{t+1} &= \theta_t - \frac{\eta}{\text{RMS}[g]_t} g_t \end{aligned} \tag{3.14}$$

RMSprop as well divides the learning rate by an exponentially decaying average of squared gradients. Hinton suggests γ to be set to 0.9, while a good default value for the learning rate η is 0.001. [17]

3.4.5 Adam

As described in [Incorporating Nesterov Momentum into Adam], the Adaptive Moment Estimation (Adam) is another way to compute the adaptive learning rate for each parameter. Additionally to storing an exponentially decaying average of past squared gradients v_t like Adadelta or RMSprop, Adam also keeps an exponentially decaying average of past gradients m_t , similar to momentum:

$$\begin{aligned} m_t &= \beta_1 m_{t-1} + (1 - \beta_1) g_t \\ v_t &= \beta_2 v_{t-1} + (1 - \beta_2) g_t^2 \end{aligned} \tag{3.15}$$

m_t and v_t are estimates of the first moment (the mean) and the second moment (the uncentered variance) of the gradients respectively, hence the name of the method. As m_t and v_t are initialized as vectors of 0's, the authors of Adam observe that they are biased towards zero, especially during the initial time steps, and especially when the decay rates are small (i.e. β_1 and β_2 are close to 1).

To counteract these biases they compute a bias-corrected estimate of the first and second moment:

$$\begin{aligned} \hat{m}_t &= \frac{m_t}{1 - \beta_1^t} \\ \hat{v}_t &= \frac{v_t}{1 - \beta_2^t} \end{aligned} \tag{3.16}$$

3 Used Algorithms

These are then used to update the parameters just as we have seen in Adadelta and RMSprop, which yields the Adam update rule:

$$\theta_{t+1} = \theta_t - \frac{\eta}{\sqrt{\hat{v}_t} + \epsilon} \hat{m}_t \quad (3.17)$$

The authors recommend in their work to use as default values of 0.9 for β_1 , 0.999 for β_2 and 10^{-8} for ϵ . They show empirically that Adam works well in practice and compares favorably to other adaptive learning-method algorithms. [10]

Algorithm 1 Adam algorithm, as proposed in [10]. The authors recommend for default settings the value 0.9 for β_1 , 0.999 for β_2 and 10^{-8} for ϵ as well as a stepsize α of 0.001.

Require: α : Stepsize

Require: $\beta_1, \beta_2 \in [0, 1)$: Exponential decay rates for the moment estimates

Require: $f(\theta)$: Stochastic objective function with parameters θ

Require: θ_0 : Initial parameter vector

- 1: Initialize first moment vector: $m_0 = 0$
 - 2: Initialize second moment vector: $v_0 = 0$
 - 3: Initialize timestep: $t = 0$
 - 4: **while** θ_t not converged **do**
 - 5: $t = t + 1$
 - 6: Get the gradients at timestamp t : $g_t = \nabla_{\theta} J(\theta_{t-1})$ (see equation 3.2)
 - 7: Update first moment estimate: $m_t = \beta_1 m_{t-1} + (1 - \beta_1) g_t$
 - 8: Update second moment estimate: $v_t = \beta_2 v_{t-1} + (1 - \beta_2) g_t^2$
 - 9: Compute bias-corrected first moment estimate: $\hat{m}_t = \frac{m_t}{1 - \beta_1^t}$
 - 10: Compute bias-corrected second moment estimate: $\hat{v}_t = \frac{v_t}{1 - \beta_2^t}$
 - 11: Update the parameters: $\theta_{t+1} = \theta_t - \frac{\eta}{\sqrt{\hat{v}_t} + \epsilon} \hat{m}_t$
 - 12: **return** Resulting parameters: θ_t
-

3.5 Implementation of the RSLVQ variants

3.5.1 RSLVQ SGD

3.5.2 RSLVQ prop

3.5.3 RSLVQ adadelta

3.5.4 RSLVQ adam

4 Test realisation

4.1 Used Streaming Datat sets

In this section will be a short description of the data streams, synthetic and real world data, that where used to perform the experiments.

4.1.1 Synthetic data

- Sea Concepts: !not finsihed rework required!
This dataset consists of 50000 instances with three attributes of which only two are relevant. The two class decision boundary is given by $f1 + f2 = b$, where $f1$, $f2$ are the two relevant features and b a predefined threshold. Abrupt drift is simulated with four different concepts, by changing the value of b every 12500 samples. Also included are 10% of noise. [19]
- Moving Squares:
placeholder

4.1.2 Real world data

- Weather Dataset:
This dataset contains eight different features like the minimum and maximum tempreature, visibility, wind speed, air pressure, etc. that were measured at the Offutt Air Force Base in Bellevue, Nebraska. These measuredments were measured in the period of 1949-1999. The goal of this dataset is to predict if it is going to rain on certains day or not. It contains 18159 instances with an imbalance towards no rain (69%) and was introduced by Elwell et al..
- Electicity Market Dataset:
First described by Harris et al., it is often used for performance comparison, as

it is a good benchmark for concept drift classification. It holds the information of the Australian New South Wales Electricity Market, whose prices are affected by supply and demand. Each sample is characterized by the following attributes: day of the week, time stamp, market demand, etc.. Each of the samples refers to a period of 30 minutes and the class label identifies the relative change compared to the last 24 hours. The used Dataset is the normalized version of the original dataset.

- **Poker Dataset:**

To create this dataset, one million poker hands, each represented by five cards that got encoded with its suit and rank, were randomly drawn. The class is the resulting poker hand itself such as one pair, full house and so forth. Since the poker hand can not change by definition and each instance was randomly generated, this dataset had in its original form no drift in it. As this is the version as it was introduced by [2], virtual drift is present in this dataset. This was achieved by sorting the instances of the dataset by rank and suit. Duplicate hands were also removed. Additionally, this version was also normalized.

- **Outdoor Objects:**

This Dataset was obtained by images that were recorded by a mobile in a garden environment. The goal is to classify 40 different objects, each approached ten times under varying lighting conditions affecting the color based representation. Every ten images represent one approach and each approach is in temporal order within the dataset. The objects are encoded in a normalized 21-dimensional RG-Chromaticity histogram.

4.2 Implementation of the Comparison and Results

4.2.1 Experiment begrenzung

4.2.2 Experiment aufbau

4.2.3 Experiment durchlauf

Listing 4.1: Beispiel für einen Quelltext

```
1
2 public void foo() {
3     // Kommentar
4 }
```

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5 Result Evaluation

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5 Result Evaluation

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Statutory Declaration

Hiermit versichere ich, dass ich die vorgelegte Bachelorarbeit selbstständig verfasst und noch nicht anderweitig zu Prüfungszwecken vorgelegt habe. Alle benutzten Quellen und Hilfsmittel sind angegeben, wörtliche und sinngemäße Zitate wurden als solche gekennzeichnet.

Florian Hohn, am February 3, 2020