

UNIVERSITY OLDENBURG

WIND PHYSICS MEASUREMENT PROJECT

Exercise 2 - Energy Meteorology

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Contents

| | | |
|----------|--|-----------|
| 1 | Wind roses | 3 |
| 2 | Weibull distribution | 6 |
| 3 | Vertical wind profiles | 8 |
| 4 | Seasonal aspects of the vertical wind profile | 10 |
| A | Appendix | 12 |
| A.1 | Task 1 | 12 |
| A.2 | Code | 12 |

Introduction

The goal of this exercise was to perform a comparison of meteorologic conditions in the North Sea and the Baltic Sea. For the comparison data from the met masts FINO 1, located in the North Sea, and FINO 2, located in the Baltic Sea, has been used. The FINO 1 data includes wind vanes at heights of $33m, 40m, 50m, 60m, 70m, 80m, 90m$ and eight anemometers at heights $33m, 40m, 50m, 60m, 70m, 80m, 90m$ and $100m$. The given data of FINO 2 contains 4 wind vanes at heights $31m, 51m, 71m$ and $91m$ with anemometers at heights $32m, 42m, 52m, 62m, 72m, 82m, 92m, 102m$.

The given time period of ten minutes intervals is of 5 years, starting on 01.01.2010. The following tasks deal with wind roses, Weibull distributions and vertical wind profile fitting.

1 Wind roses

In this task we were asked to create wind roses for FINO 1 and FINO 2 at around 90m height. We used an already existing routine to create wind roses (Windrose.m by Daniel Pereira). In order to obtain correct wind directions we used the following plot routine:

```
1 WindRose(fino1_d90 , fino1_v90 , 'AngleNorth' , 0 , 'AngleEast' , 90);
```

By using the optional arguments *AngleNorth* and *AngleEast* we made sure that the axes are initialized correctly. Before we started to analyze our plots we double checked our wind roses by using a pdf-plot of the wind directions. See Figure 1.

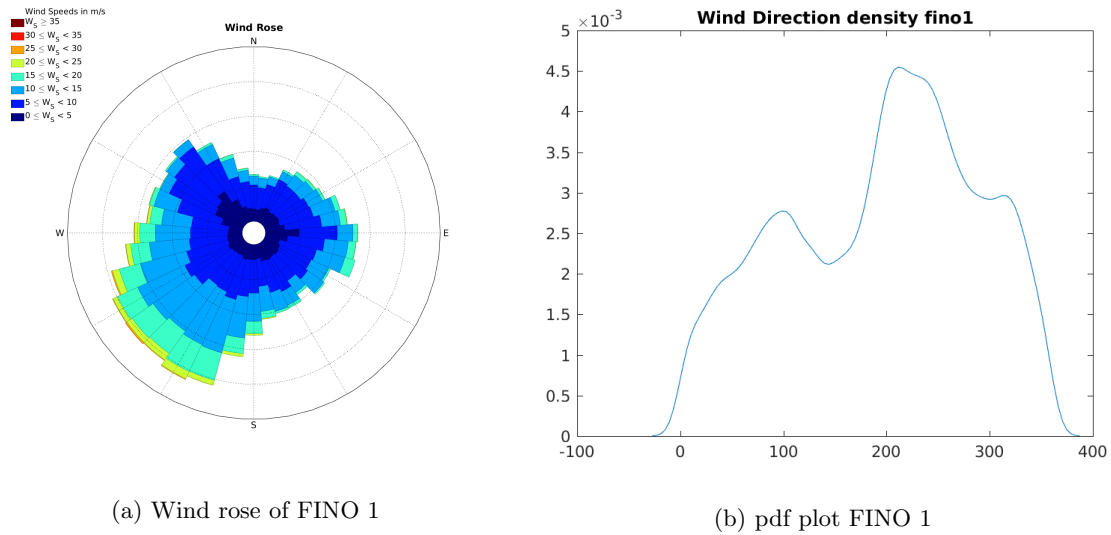


Figure 1: Validation of Wind Rose

The pdf plot confirms that most of the wind is coming from south-west direction. This is identical with our FINO 1 wind rose. The same approach was used to confirm the wind rose created from FINO 2 data (see Appendix). After validating our results we now can compare the two windroses. See Figure 2.

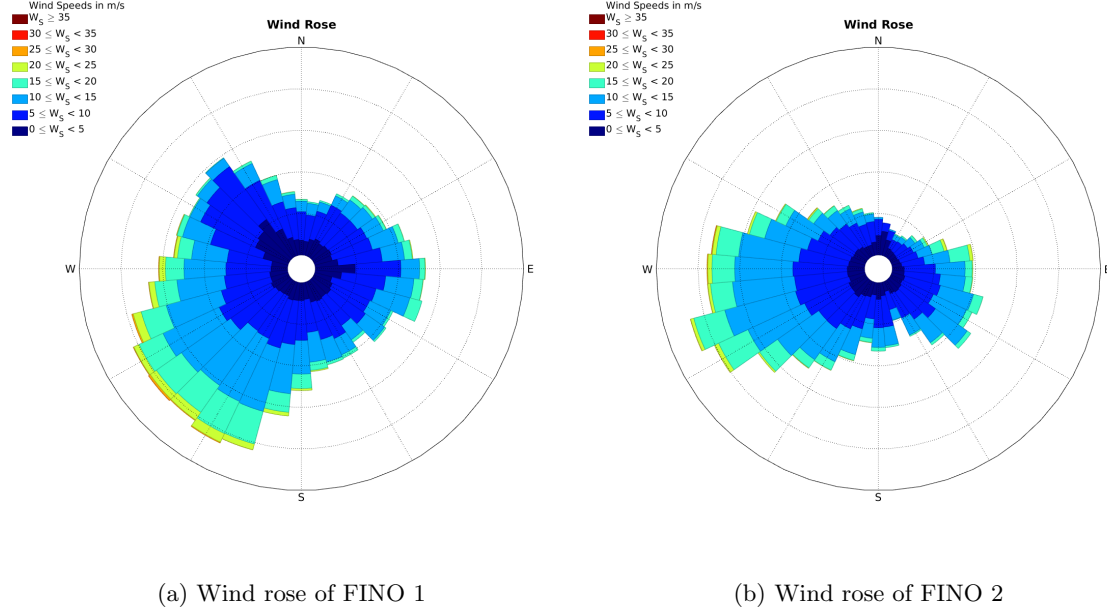


Figure 2: Comparison of windroses

We observe that most of the measured wind directions at FINO 1 are of south-western direction. For FINO 2, located in the Baltic Sea, the wind is less distributed and has almost exclusively western and eastern directions. Both met masts are located in the Northern Hemisphere. That means high pressure fields rotate clockwise and low pressure fields anti-clockwise. The wind directions are influenced by the isobars of the different pressure fields. Keeping this information in mind and looking at the content provided during the lecture (see Figure 3) the measured wind directions have two components. First the large scale wind movements are responsible for the south-western direction measured at FINO 1 and respectively western direction for FINO 2. The strong fluctuation in the lower wind speeds is due to the movement of the different pressure fields. Most of the time we have a high pressure field in the Baltic sea which might explain the additional components measured in eastern direction. For the north sea we observe an additional south western component.

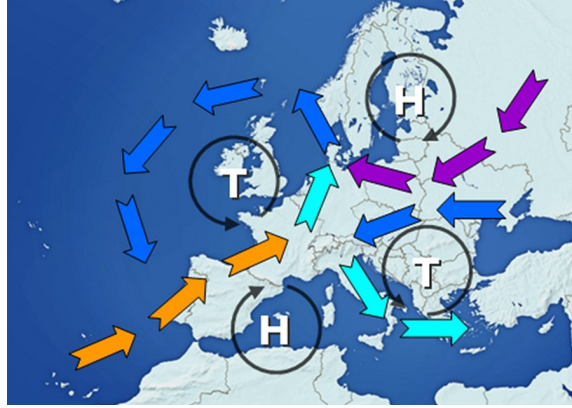


Figure 3: Typical weather pattern over Europe

Both measurement systems are located in the open sea, so in general there are no obstacles that can create additional turbulence. However the construction of wind farms may influence the measurement. This holds especially for FINO 1 which is nearly entirely surrounded by wind farms. (see Figure 4).

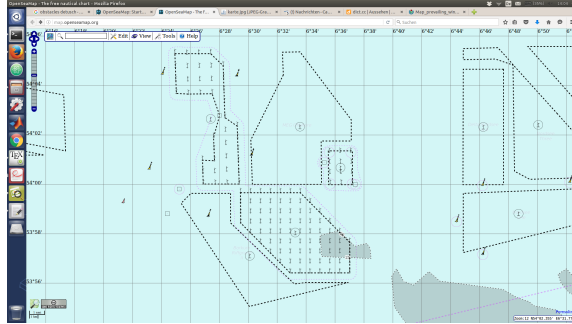


Figure 4: Location of FINO 1

2 Weibull distribution

In Task 2 we created histograms at around 90m height. Next we calculated the Weibull parameters with the mean and standard deviation of the measured wind speeds. For the further calculation we used the equalities provided during the lecture:

$$\mu = \lambda \cdot \Gamma\left(1 + \frac{1}{k}\right)$$
$$\sigma^2 = \lambda^2 \cdot \left(\Gamma\left(1 + \frac{2}{k}\right) - \Gamma\left(1 + \frac{1}{k}\right)^2\right)$$

By substitution we obtain:

$$\sigma^2 = \left(\frac{\mu}{\Gamma(1 + \frac{1}{k})}\right)^2 \cdot \left(\Gamma\left(1 + \frac{2}{k}\right) - \Gamma\left(1 + \frac{1}{k}\right)^2\right)$$

which gives

$$0 = \left(\frac{\mu}{\sigma}\right)^2 \cdot \left(\frac{\Gamma(1 + \frac{2}{k})}{\Gamma(1 + \frac{1}{k})^2} - 1\right) - 1$$

We implemented this equation in Matlab and solved for the Weibull parameters A and k. With the calculated parameters we created a corresponding Weibull distribution.

```
1 %% Task 2
  mean1 = nanmean(fino1_v90);
3 dev1 = nanstd(fino1_v90);

5 mean2 = nanmean(fino2_v92);
  dev2 = nanstd(fino2_v92);
7
  % interpolate
9 k_Fino1 = 1;
  Func_Fino1 = @(k_Fino1) (mean1*mean1/(dev1*dev1))*((gamma(1+2/k_Fino1))/(gamma(1+1/
    k_Fino1))^2-1)-1
11 k_Fino1 = fsolve(Func_Fino1,k_Fino1);
  disp(k_Fino1);
13 A_Fino1 = mean1/gamma(1+1/k_Fino1);
  weibull_Fino1 = wblpdf(1:30,A_Fino1,k_Fino1);
15

  k_Fino2 = 1;
17 Func_Fino2 = @(k_Fino2) (mean2*mean2/(dev2*dev2))*((gamma(1+2/k_Fino2))/(gamma(1+1/
    k_Fino2))^2-1)-1
  k_Fino2 = fsolve(Func_Fino2,k_Fino2);
```

```

19 disp(k_Fino2);
   A_Fino2 = mean2/gamma(1+1/k_Fino2);
21 weibull_Fino2 = wblpdf(1:30,A_Fino2,k_Fino2);

```

Figure 5 shows the wind speed distributions for Fino 1 and Fino 2 with the corresponding Weibull fit.

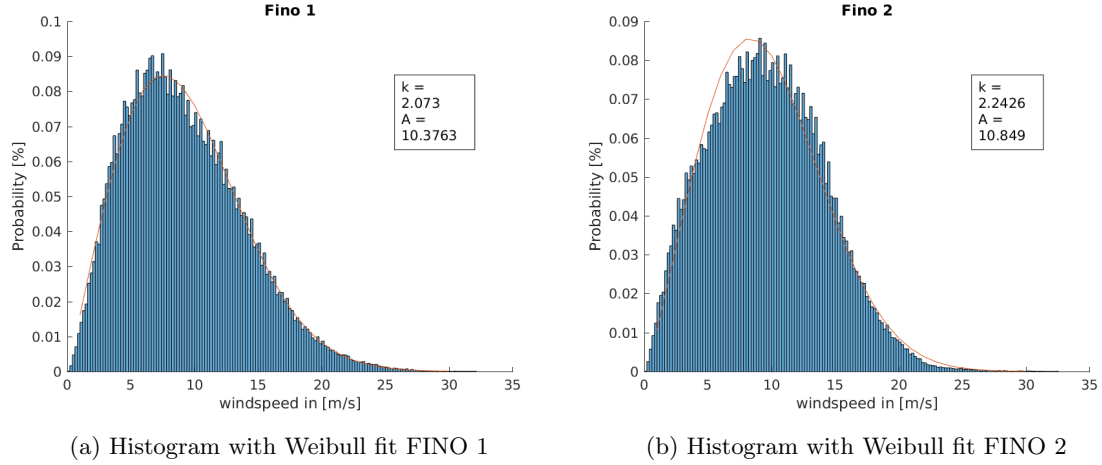


Figure 5: Wind speed distributions

In order to evaluate which region is more favorable for wind power utilization, we implemented two wind turbine power curves and calculated the energy yield. The location of FINO 2 seems to be better for wind power utilization. This goes in hand with our first impression, because the curve of FINO 1 is a little shifted to the left hand side. However there are some concerns: The measured data might be influenced by the surrounding wind farms. The original wind speeds might be higher. In addition we only evaluated one height. We have not included measurements at different heights. We just assume that we have a comparable vertical wind speed distribution.

3 Vertical wind profiles

In the following task we calculated the vertical wind speed profile for the wind sector in the range of 240–285 degrees. In the lecture we discussed two common methods for the vertical wind profile: the empirical power law profile and the logarithmic wind speed profile. We were asked to fit these methods to our data. The following code snippet shows how we implemented the fitting routine in Matlab:

```
1 logProfileModel = @(b,z) b(1)/0.4 * (log(z/b(2)));
  empPowerModel = @(c,x) avgPerHeight(8) * ((x/90).^c(1));
3 opts = statset('nlinfit');
  opts.RobustWgtFun = 'bisquare';
5 logProfileCoeffs = nlinfit([33,40,50,60,70,80,90,100], avgPerHeight, logProfileModel
  , [0.2, 10^-6], opts);
  [x,y] = fplot(@(z) logProfileCoeffs(1)/0.4 * (log(z/logProfileCoeffs(2))), [0 100]);
7 plot(y,x, 'Color', 'b');
  empPowerCoeff = real(nlinfit([33,40,50,60,70,80,90,100], avgPerHeight, empPowerModel
  , [0.11], opts));
9 [x,y] = fplot(@(z) avgPerHeight(8) * (z/90)^(empPowerCoeff), [0 100]);
  plot(y,x, 'Color', 'r');
```

Figure 6 shows the result of our fitting.

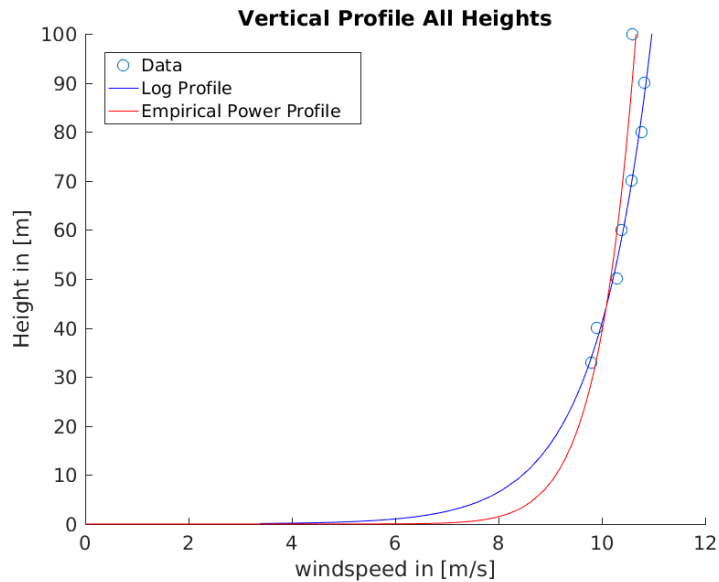


Figure 6: Vertical profile fits

The figure shows the data points, calculated by the mean wind speed of the different heights and the corresponding logarithmic and empirical power law profile. Our results suggest that the logarithmic profile is more accurate for the given data. The power law profile has a stronger gradient and is especially different for low wind speeds. While the logarithmic model fits most of the data points quite well (except $z = 100m$) the power law model fits the extreme values better. In this case we would thus prefer the logarithmic model because we consider the data point at $100m$ as a non-physical measurement error (e.g. defect anemometer at that height during one winter). However we cannot check which method is better for lower wind speeds. As starting values for the non-linear regression we chose $u_* = 0.2$ for the friction velocity and $z_0 = 10^{-6}$ for the roughness length in the logarithmic model and $\alpha = 0.11$ for the power law model according to the lecture notes recommending these values in case of water surface. The two regressions end with the following values:

$$u_* = 0.434$$

$$z_0 = 0.0041$$

$$\alpha = 0.0682$$

4 Seasonal aspects of the vertical wind profile

In the extra task (3b) we were to study seasonal aspects of the vertical wind speed profile by comparing the vertical profile during summer time (May-July) with winter time (November-January). For both seasons we considered western/south-western winds again in the range of $240 - 285$ degrees. For both seasons we performed a non-linear regression again with the logarithmic model and the power law model. Results for this are depicted in Figure 7.

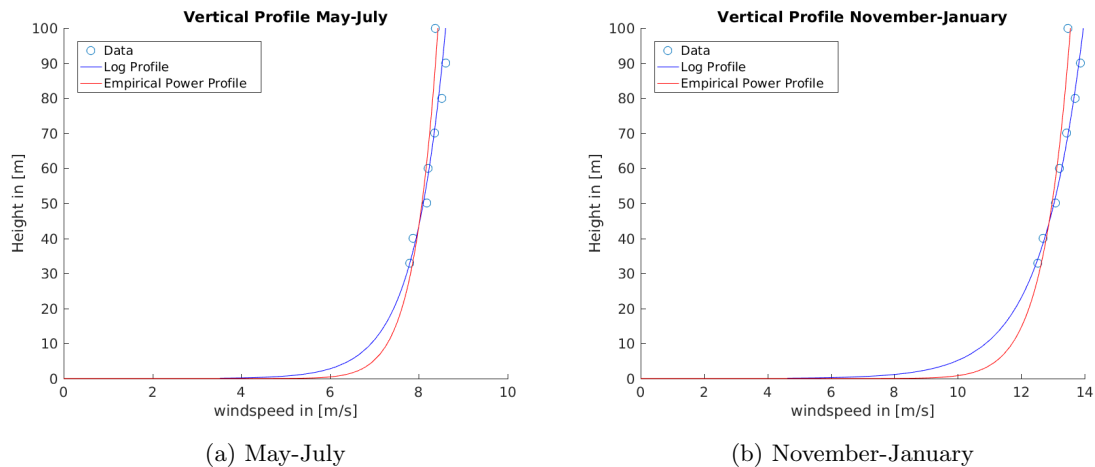


Figure 7: vertical profiles in summer and winter

Not surprisingly the overall wind speed is higher in winter. But from this graphic the shape of the curves are very much similar with regard to the vertical profile. In order to detect differences we normalized the model curves to a wind speed of 1 at height $z = 90$. By doing so we can state that the vertical wind speed profile during summer is clearly steeper (red dashed curve in Figure 8) than in winter (blue dashed curve) regarding the logarithmic regression model.

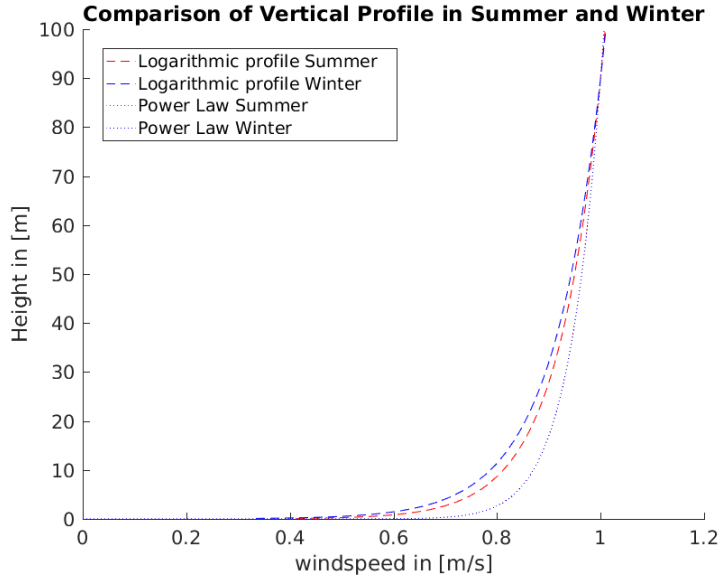


Figure 8: Vertical profile fits

This means that the wind shear in summer time is lower compared to the wind shear in winter. In the empirical power law model this difference does not hold (the curves for summer and winter are identical). However, as stated previously we consider the logarithmic model to be more accurate and reason that the seasonal variation in vertical wind shear is due to more turbulent and overall higher winds with higher waves in winter while summer sees more steady and constant wind. We can make this observation even more obvious by looking at the final values of the variables in the logarithmic regression model. In summer the regression ends with values of $v_* = 0.2906$ and $z_0 = 0.0007$ while in winter we obtain $v_* = 0.5338$ and $z_0 = 0.0029$. Thus the friction velocity and the surface roughness are almost doubled in winter which accounts for the higher vertical wind shear.

A Appendix

A.1 Task 1

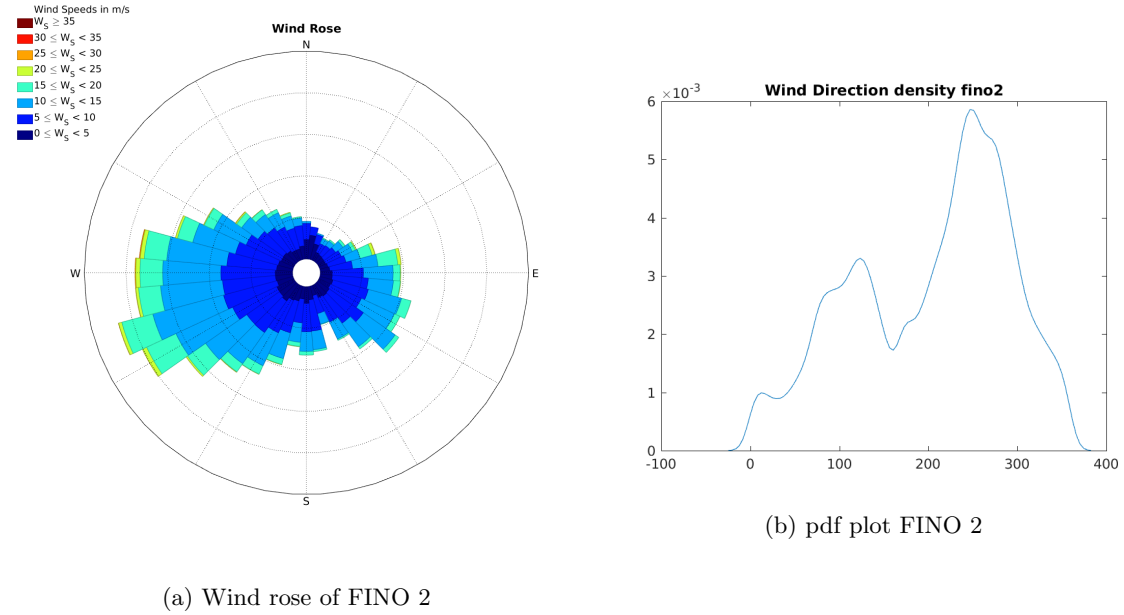


Figure 9: Validation of Wind Rose 2

A.2 Code

```
%% Task 1
2 disp('Load Data')
  load('WMP.WEnMet.data.mat');
4
  fino1_v90 = Fino1.ws90;
6  fino1_d90 = Fino1.wd90;
  fino2_v92 = Fino2.ws92;
8  fino2_d91 = Fino2.wd91;

10 % Plot
  WindRose(fino1_d90, fino1_v90, 'AngleNorth', 0, 'AngleEast', 90);
12 saveas(gcf, 'figures/WindRose-Fino1.png')
  WindRose(fino2_d91, fino2_v92, 'AngleNorth', 0, 'AngleEast', 90);
14 saveas(gcf, 'figures/WindRose-Fino2.png')

16
  % Validate wind rose ...
```



```

        fino1_vestasyield(i,1) = y_vestas(i)*weibull_Fino1(i);
60    fino2_vestasyield(i,1) = y_vestas(i)*weibull_Fino2(i);
        fino1_enerconyield(i,1) = y_enercon(i)*weibull_Fino1(i);
62    fino2_enerconyield(i,1) = y_enercon(i)*weibull_Fino2(i);
    end
64
    if sum(fino1_vestasyield) > sum(fino2_vestasyield)
66        disp('Fino 1 besser , vestas')
    else
68        disp('Fino 2 besser , vestas')
    end
70
    if sum(fino1_enerconyield) > sum(fino2_enerconyield)
72        disp('Fino 1 besser , enercon')
    else
74        disp('Fino 2 besser , enercon')
    end
76
    figure();
78    hold on;
    histogram(fino1_v90 , 'Normalization' , 'pdf');
80    plot(weibull_Fino1)
    xlabel('windspeed in [m/s]');
82    ylabel('Probability [%]');
    title('Fino 1')
84    dim = [.7 .5 .3 .3];
    annotation('textbox',dim,'String',{ 'k =',num2str(k_Fino1), 'A =', num2str(A_Fino1)},
        'FitBoxToText','on');
86    saveas(gcf,'figures/Hist_withfit_Fino1.png')
    hold off;
88
    figure();
90    hold on;
    histogram(fino2_v92 , 'Normalization' , 'pdf');
92    plot(weibull_Fino2)
    xlabel('windspeed in [m/s]');
94    ylabel('Probability [%]');
    title('Fino 2')
96    dim = [.7 .5 .3 .3];
    annotation('textbox',dim,'String',{ 'k =',num2str(k_Fino2), 'A =', num2str(A_Fino2)},
        'FitBoxToText','on');
98    saveas(gcf,'figures/Hist_withfit_Fino2.png')
    hold off;
100
%% Task 3
102    wind_sector = [];
    windsOnHeight = [];

```

```

104 j = 1
    for i = 1:length(fino1_v90)
106         if (fino1_d90(i) >= 240 && fino1_d90(i) <= 285)
                wind_sector(j,2) = fino1_v90(1,i);
108                wind_sector(j,1) = fino1_d90(1,i);
                windsOnHeight(j,1) = Fino1.ws33(1,i);
110                windsOnHeight(j,2) = Fino1.ws40(1,i);
                windsOnHeight(j,3) = Fino1.ws50(1,i);
112                windsOnHeight(j,4) = Fino1.ws60(1,i);
                windsOnHeight(j,5) = Fino1.ws70(1,i);
114                windsOnHeight(j,6) = Fino1.ws80(1,i);
                windsOnHeight(j,7) = Fino1.ws90(1,i);
116                windsOnHeight(j,8) = Fino1.ws100(1,i);
                j= j+1;
118        end
    end
120
    wind_sector_mean = nanmean(wind_sector(:,2));
122    wind_prof = [];
    for i = 1:100
124        wind_prof(i,1) = 0.2/0.4 * (log(i/10^-6));
        wind_prof(i,2) = wind_sector_mean*(i/90)^(0.11);
126    end
    figure();
128    hold on;
    plot(1:100, wind_prof(:,1))
130    plot(1:100, wind_prof(:,2), 'o')
    plot(90, wind_sector_mean, '*')
132    xlabel('Height in [m]');
    ylabel('windspeed in [m/s]');
134    title('Vertical Profile');

136    avgPerHeight = [8];
    for i=1:8
138        avgPerHeight(i) = nanmean(windsOnHeight(:,i));
    end
140    figure();
    hold on;
142    plot(avgPerHeight(:), [33,40,50,60,70,80,90,100], 'o')

144    logProfileModel = @(b,z) b(1)/0.4 * (log(z/b(2)));
    empPowerModel = @(c,x) avgPerHeight(8)*((x/90).^c(1));
146    opts = statset('nlinfit');
    opts.RobustWgtFun = 'bisquare';
148    logProfileCoeffs = nlinfit([33,40,50,60,70,80,90,100], avgPerHeight, logProfileModel
        , [0.2, 10^-6], opts);
    [x,y]=fplot(@(z) logProfileCoeffs(1)/0.4 * (log(z/logProfileCoeffs(2))), [0 100]);

```



```

150 plot(y,x,'Color','b');
    empPowerCoeff = real(nlinfit([33,40,50,60,70,80,90,100],avgPerHeight,empPowerModel
        ,[0.11],opts));
152 [x,y]=fplot(@(z) avgPerHeight(8)*(z/90)^(empPowerCoeff),[0 100]);
    plot(y,x,'Color','r');
154
155 ylabel('Height in [m]');
156 xlabel('windspeed in [m/s]');
    title('Vertical Profile All Heights');
158 legend('Data','Log Profile','Empirical Power Profile','Location','northwest');
    saveas(gcf,'figures/verticalProfileFits.png')
160 hold off;

162 %% ExtraTask 3(b)

164 windsOnHeightSommer = [];
    windsOnHeightWinter = [];
166 jS = 1
    jW = 1
168
    for i = 1:length(fino1_v90)
170         if (fino1_d90(i) >= 240 && fino1_d90(i) <= 285)
            if ((i>6*24*(31+28+31+30) && i<=6*24*(31+28+31+30+31+30+31)) ... %May-July
                2010
172             || (i>6*24*(31+28+31+30+365) && i<=6*24*(31+28+31+30+31+30+31+365)) ...
                %May-July 2011
                || (i>6*24*(31+29+31+30+365+365) && i<=6*24*
                (31+29+31+30+31+30+31+365+365)) ... %May-July 2012
174             || (i>6*24*(31+28+31+30+365+365+366) && i<=6*24*
                (31+28+31+30+31+30+31+365+365+366)) ... %May-July 2013
                || (i>6*24*(31+28+31+30+365+365+366+365) && i<=6*24*
                (31+28+31+30+31+30+31+365+365+366+365)) ... %May-July 2014
176             || (i>6*24*(31+28+31+30+365+365+366+365+365) && i<=6*24*
                (31+28+31+30+31+30+31+365+365+366+365+365)) ... %May-July 2015
                windsOnHeightSommer(jS,1) = Fino1.ws33(1,i);
178                windsOnHeightSommer(jS,2) = Fino1.ws40(1,i);
                windsOnHeightSommer(jS,3) = Fino1.ws50(1,i);
180                windsOnHeightSommer(jS,4) = Fino1.ws60(1,i);
                windsOnHeightSommer(jS,5) = Fino1.ws70(1,i);
182                windsOnHeightSommer(jS,6) = Fino1.ws80(1,i);
                windsOnHeightSommer(jS,7) = Fino1.ws90(1,i);
184                windsOnHeightSommer(jS,8) = Fino1.ws100(1,i);
                jS= jS+1;
186            end
            if ((i>0 && i<=6*24*31) ... %January 2010
188             || (i>6*24*(365-31-30) && i<=6*24*(365+31)) ... %Nov2010-Jan2011
                || (i>6*24*(365+365-31-30) && i<=6*24*(365+365+31)) ... %Nov2011-Jan2012

```

```

190         || (i>6*24*(365+365+366-31-30) && i<=6*24*(365+365+366+31)) ... %Nov2012
    -Jan2013
        || (i>6*24*(365+365+366+365-31-30) && i<=6*24*(365+365+366+365+31)) ...
    %Nov2013-Jan2014
192         || (i>6*24*(365+365+366+365+365-31-30) && i<=6*24*
    (365+365+366+365+365+31)) ... %Nov2014-Jan2015
        || (i>6*24*(365+365+366+365+365+365-31-30) && i<=6*24*
    (365+365+366+365+365+365)+1)) %Nov2015-Dez2015
194         windsOnHeightWinter(jW,1) = Fino1.ws33(1,i);
        windsOnHeightWinter(jW,2) = Fino1.ws40(1,i);
196         windsOnHeightWinter(jW,3) = Fino1.ws50(1,i);
        windsOnHeightWinter(jW,4) = Fino1.ws60(1,i);
198         windsOnHeightWinter(jW,5) = Fino1.ws70(1,i);
        windsOnHeightWinter(jW,6) = Fino1.ws80(1,i);
200         windsOnHeightWinter(jW,7) = Fino1.ws90(1,i);
        windsOnHeightWinter(jW,8) = Fino1.ws100(1,i);
202         jW= jW+1;

    end

204     end
end

206 %Evaluation of Sommer Months 2010-2015
207 avgPerHeightSommer = [8];
    for i=1:8
210         avgPerHeightSommer(i) = nanmean(windsOnHeightSommer(:,i));
    end
212 figure();
    hold on;
214 plot(avgPerHeightSommer(:),[33,40,50,60,70,80,90,100], 'o')

216 logProfileModel = @(b,z) b(1)/0.4 *(log(z/b(2)));
    empPowerModel = @(c,z) avgPerHeightSommer(8)*(z/90).^c(1);
218 opts = statset('nlinfit');
    opts.RobustWgtFun = 'bisquare';
220 logProfileCoeffsSom = nlinfit([33,40,50,60,70,80,90,100],avgPerHeightSommer,
    logProfileModel,[0.2,10^-6],opts);
    [xLogSom,yLogSom]=fplot(@(z) logProfileCoeffsSom(1)/0.4 *(log(z/logProfileCoeffsSom
    (2))),[0 100]);
222 plot(yLogSom,xLogSom, 'Color','b');
    empPowerCoeffSom = nlinfit([33,40,50,60,70,80,90,100],avgPerHeightSommer,
    empPowerModel,[0.11],opts);
224 [xPowSom,yPowSom]=fplot(@(z) avgPerHeightSommer(8)*(z/90)^(empPowerCoeffSom),[0
    100]);
    plot(yPowSom,xPowSom, 'Color','r');
226
    ylabel('Height in [m]');
228 xlabel('windspeed in [m/s]');

```

```

    title('Vertical Profile May–July');
230 legend('Data', 'Log Profile', 'Empirical Power Profile', 'Location', 'northwest');
    saveas(gcf, 'figures/verticalProfileFitsSommer.png')
232 hold off;

234 %Evaluation of Winter Months 2010–2015
    avgPerHeightWinter = [8];
236 for i=1:8
        avgPerHeightWinter(i) = nanmean(windsOnHeightWinter(:, i));
238 end
    figure();
240 hold on;
    plot(avgPerHeightWinter(:), [33, 40, 50, 60, 70, 80, 90, 100], 'o')
242
    logProfileModelWin = @(b, z) b(1)/0.4 * (log(z/b(2)));
244 empPowerModelWin = @(c, z) avgPerHeightWinter(8) * ((z/90).^c(1));
    opts = statset('nlinfit');
246 opts.RobustWgtFun = 'bisquare';
    logProfileCoeffsWin = real(nlinfit([33, 40, 50, 60, 70, 80, 90, 100], avgPerHeightWinter,
        logProfileModelWin, [0.1, 10^-5], opts));
248 [xLogWin, yLogWin] = fplot(@(z) logProfileCoeffsWin(1)/0.4 * (log(z/logProfileCoeffsWin
        (2))), [0 100]);
    plot(yLogWin, xLogWin, 'Color', 'b');
250 empPowerCoeffWin = nlinfit([33, 40, 50, 60, 70, 80, 90, 100], avgPerHeightWinter,
        empPowerModelWin, 0.063, opts);
    [xPowWin, yPowWin] = fplot(@(z) avgPerHeightWinter(8) * (z/90)^(empPowerCoeffWin), [0
        100]);
252 plot(yPowWin, xPowWin, 'Color', 'r');

254 ylabel('Height in [m]');
    xlabel('windspeed in [m/s]');
256 title('Vertical Profile November–January');
    legend('Data', 'Log Profile', 'Empirical Power Profile', 'Location', 'northwest');
258 saveas(gcf, 'figures/verticalProfileFitsWinter.png')
    hold off;

260 %comparison of normed log profiles in summer and winter
262 figure();
    hold on;
264 yLogSomNormed = yLogSom/logProfileModel(logProfileCoeffsSom, 90);
    yLogWinNormed = yLogWin/logProfileModelWin(logProfileCoeffsWin, 90);
266 plot(yLogSomNormed, xLogSom, '—', 'Color', 'r');
    plot(yLogWinNormed, xLogWin, '—', 'Color', 'b');
268
    yPowSomNormed = yPowSom/empPowerModel(empPowerCoeffSom, 90);
270 yPowWinNormed = yPowWin/empPowerModelWin(empPowerCoeffWin, 90);

```

```

272 plot(yPowSomNormed,xPowSom,':','Color','r');
    plot(yPowWinNormed,xPowWin,':','Color','b');
274 ylabel('Height in [m]');
    xlabel('windspeed in [m/s]');
276 title('Comparison of Vertical Profile in Summer and Winter');
    legend('Logarithmic profile Summer', 'Logarithmic profile Winter','Power Law Summer'
        , 'Power Law Winter','Location','northwest');
278 saveas(gcf,'figures/verticalProfilesComparison.png')
    hold off;

280
    disp(logProfileCoeffsSom);
282 disp(empPowerCoeffSom);
    disp(logProfileCoeffsWin);
284 disp(empPowerCoeffWin);

```
