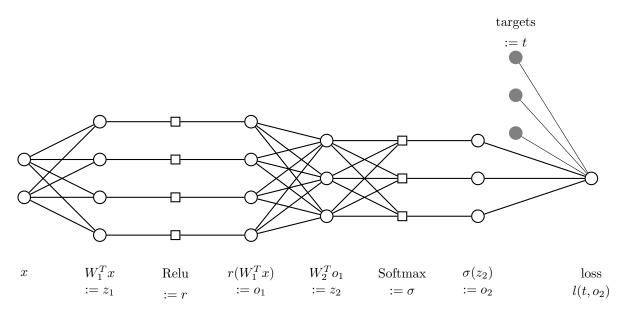
#### Exercise 9

Deadline: 30.06.2017, 2:15 pm

Regulations: You should hand in the exercises in groups of two or three persons. Please send a *compressed* (!) directory or file containing your solutions including all graphics, descriptions and source code to *thorsten.beier@iwr.uni-heidelberg.de*. The subject line of this email should start with [MLCV17][EX09] followed by the full names of all group members. Please cross-reference your code files in your writeup, such that it is clear which file has to be run for each exercise.

#### 1 Neural Networks



Given the neural network above with

- $x \in \mathbb{R}^P$
- $y \in \{1, 2, \dots, K\}$
- Relu non-linearity :

$$r(W_1^T x) = \max(0, W_1^T x) \tag{1}$$

• Softmax function (soft version of argmax)

$$\sigma(z_2) = \frac{\exp(z_2)}{\sum\limits_{k=1}^{K} \exp(z_{2_k})}$$
(2)

• the negative log-likelihood loss function:

$$l(t, o_2) = -t^T \cdot \ln(o_2) \tag{3}$$

one needs to find the the derivatives of the loss function l w.r.t. to the weights  $W_1$  and  $W_2$ . to perform gradient decent.

Proof that the following is true:

$$\frac{\partial l}{\partial W_1} = X^T \cdot \left( (o_2^T - t^T) \cdot w_2^T \right) \qquad \underbrace{I(o_1 > 0)}_{\text{1 where } o_1 > 0 \text{, 0 elsewhere}} \tag{4}$$

$$\frac{\partial l}{\partial W_2} = o_1^T \cdot \left( o_2^T - t^T \right) \tag{5}$$

Hint:

$$\frac{\partial l}{\partial W_2} = \underbrace{o_1^T}_{\text{Shape}=(\text{nHidden,nInput})} \cdot \underbrace{(o_2^T - t^T)}_{\text{Shape}=(\text{nHidden,nInput})}$$
 (6)

$$\frac{\partial l}{\partial z_2} = -t^T + o_2^T \tag{7}$$

## 2 Bonus 5P

Experiment neural networks using playground.tensorflow.org. Try to fit all dataset without additional features. Show your architectures.

# 3 Implementation 20P

See next page for a printout of an ipython notebook including the implementation tasks and descriptions.

# Implementing a Neural Network

In this exercise we will develop a neural network with two fully-connected layers to perform classification, and test it out on the MNIST dataset of handwritten digits.

**Credits:** We have based this exercise on an assignment (Assignment #1 of Winter 2016) of the very good course on Neural Networks from the Stanford University <a href="http://cs231n.github.io/">http://cs231n.github.io/</a> (<a href="http://cs231n.github.io/">http://cs231n.github.io/</a> (<a

How to solve this exercise: You will have to work with both, the source file cs231nHD/neural\_net.py, and this ipython notebook. This notebook allows you to verify your implementation of a neural net through predefined test cases. The source file neural\_net.py contains a skeleton implementation with a lot of comments to show you what you are expected to do. Special blocks of TODOs indicate where you are supposed to add the implementation, and what to do there. The methods of the neural net you write in the separate file will be reloaded automatically whenever you save the neural net.py file. The class TwoLayerNet is imported from this file as below.

```
In []: # A bit of setup
import numpy as np
import matplotlib.pyplot as plt

from cs231nHD.neural_net import TwoLayerNet

%matplotlib inline
plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
plt.rcParams['image.interpolation'] = 'nearest'
plt.rcParams['image.cmap'] = 'gray'

# for auto-reloading external modules
# see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ip
%load_ext autoreload
%autoreload 2
```

We will use the class TwoLayerNet in the file cs231n/neural\_net.py to represent instances of our network. The network parameters are stored in the instance variable self.params where keys are string parameter names and values are numpy arrays. Below, we initialize toy data and a toy model that we will use to develop your implementation.

**Hint:** If you need more information on classes and object oriented programming, check out the great tutorial at <a href="http://www.python-course.eu/python3">http://www.python-course.eu/python3</a> object oriented programming.php (<a href="http://www.python-course.eu/python3">http://www.python-course.eu/python3</a> object oriented programming.php)

```
# Note that we set the random seed for repeatable experiments!
input_size = 4
hidden_size = 10
num_classes = 3
num_inputs = 5

def init_toy_model():
    np.random.seed(0)
    return TwoLayerNet(input_size, hidden_size, num_classes, std=le-1)

def init_toy_data():
    np.random.seed(1)
    X = 10 * np.random.randn(num_inputs, input_size)
    y = np.array([0, 1, 2, 2, 1])
    return X, y

net = init_toy_model()
X, y = init_toy_data()
```

## Forward pass: compute scores

Open the file cs231n/neural\_net.py and look at the method TwoLayerNet.loss. This function takes the data and weights and should compute the class scores, the loss, and the gradients on the parameters.

Implement the first part of the forward pass which uses the weights and biases to compute the scores for all inputs. Then run the cell below to see whether you have computed the right thing.

```
In [ ]: scores = net.loss(X)
    print('Your scores:')
    print(scores)
    print()
    print('correct scores:')
    correct_scores = np.asarray([
        [-0.81233741, -1.27654624, -0.70335995],
        [-0.17129677, -1.18803311, -0.47310444],
        [-0.51590475, -1.01354314, -0.8504215 ],
        [-0.15419291, -0.48629638, -0.52901952],
        [-0.00618733, -0.12435261, -0.15226949]])
    print(correct_scores)
    print()

# The difference should be very small. We get < 1e-7
    print('Difference between your scores and correct scores:')
    print(np.sum(np.abs(scores - correct_scores)))</pre>
```

# Forward pass: compute loss

In the same function, implement the second part that computes the data and regularization loss. For the data loss, use the average cross-entropy softmax loss.

### **Backward pass**

Implement the rest of the function. This will compute the gradient of the loss with respect to the variables W1, b1, W2, and b2. Now that you (hopefully!) have a correctly implemented forward pass, you can debug your backward pass using a numeric gradient check:

```
In [ ]: from cs231nHD.gradient_check import eval_numerical_gradient

def rel_error(x, y):
    """ returns relative error """
    return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y)))

# Use numeric gradient checking to check your implementation of the backward
# If your implementation is correct, the difference between the numeric and
# analytic gradients should be less than 1e-8 for each of W1, W2, b1, and b2

loss, grads = net.loss(X, y, reg=0.1)

# these should all be less than 1e-8 or so
for param_name in grads:
    f = lambda W: net.loss(X, y, reg=0.1)[0]
    param_grad_num = eval_numerical_gradient(f, net.params[param_name], verl_print('{} max relative error: {} '.format(param_name, rel_error(param_grad_name))
```

#### Train the network

To train the network we will use stochastic gradient descent (SGD). Look at the function TwoLayerNet.train and fill in the missing sections to implement the training procedure. You will also have to implement TwoLayerNet.predict, as the training process periodically performs prediction to keep track of accuracy over time while the network trains.

Once you have implemented the method, run the code below to train a two-layer network on toy data. You should achieve a training loss less than 0.02.

# Applying the Network to a larger dataset

Now that you have implemented a two-layer network that passes gradient checks and works on toy data, it's time to load up the MNIST dataset from <a href="http://yann.lecun.com/exdb/mnist/">http://yann.lecun.com/exdb/mnist/</a> (http://yann.lecun.com/exdb/mnist/) so we can use it to train a classifier on a real dataset. The load\_mnist() method downloads the data (~11MB) automatically if it is not present yet!

Each data point is now a 28 \* 28 grayscale image of a digit, reshaped into a vector.

```
# Invoke the above function to get our data.
X_train, y_train, X_val, y_val, X_test, y_test = load_mnist()
print('Train data shape: ', X_train.shape)
print('Train labels shape: ', y_train.shape)
print('Validation data shape: ', X_val.shape)
print('Validation labels shape: ', y_val.shape)
print('Test data shape: ', X_test.shape)
print('Test labels shape: ', y_test.shape)
print('Classes: ', np.unique(y_test), ', number of classes is ', len(np.unic)

In []: # show one of the images
plt.imshow(np.reshape(X_train[42,:], [28,28]))
print("Image Class: ", y_train[42])
```

### Train a network

To train our network we will use SGD with momentum. In addition, we will adjust the learning rate with an exponential learning rate schedule as optimization proceeds; after each epoch, we will reduce the learning rate by multiplying it by a decay rate. (This is already implemented, just run the cell!)

```
In [ ]: import time
        input size = 28 * 28 * 1
        num_classes = 10
        hidden size = 20
        net = TwoLayerNet(input_size, hidden_size, num_classes)
        start_time = time.clock()
        # Train the network
        stats = net.train(X_train, y_train, X_val, y_val,
                    num_iters=1000, batch_size=200,
                     learning_rate=0.05, learning_rate_decay=0.95,
                    reg=0.1, verbose=True)
        end time = time.clock()
        print("Training took ", end_time - start_time, " seconds")
        # Predict on the validation set
        val_acc = (net.predict(X_val) == y_val).mean()
        print('Validation accuracy: ', val_acc)
```

# **Debug the training**

With the default parameters we provided above, you should get a validation accuracy of about 0.75 on the validation set. This isn't very good. In the next exercise we will look at ways to improve a network's performance.

One strategy for getting insight into what's wrong is to plot the loss function and the accuracies on the training and validation sets during optimization.

Another strategy is to visualize the weights that were learned in the first layer of the network. In most neural networks trained on visual data, the first layer weights typically show some distinctive structure when visualized.

```
plt.subplot(2, 1, 1)
plt.plot(stats['loss_history'])
plt.title('Loss history')
plt.xlabel('Iteration')
plt.ylabel('Loss')

plt.subplot(2, 1, 2)
plt.plot(stats['train_acc_history'], label='train')
plt.plot(stats['val_acc_history'], label='val')
plt.title('Classification accuracy history')
plt.xlabel('Epoch')
plt.ylabel('Clasification accuracy')
plt.legend()
plt.show()
```

```
In []: from cs231nHD.vis_utils import visualize_grid

# Visualize the weights of the network

def show_net_weights(net):
    W1 = net.params['W1']
    W1 = W1.reshape(28, 28, 1, -1).transpose(3, 0, 1, 2)
    img = visualize_grid(W1, padding=1).astype('uint8')
    plt.imshow(img[:,:,0])
    plt.gca().axis('off')
    plt.show()

show_net_weights(net)
```