

## Dynamics

$$\dot{x} = \begin{bmatrix} u \\ 1 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix} + \begin{bmatrix} 1 \\ 0 \end{bmatrix} u$$

$$f_{u}(x)$$

$$\dot{\chi} = \int_{\alpha} (x) + \int_{\alpha} (x) \cdot u$$

## Measurement

We need to calculate:

First interesting term:

$$\frac{L_{f_0}h}{L_{f_0}} = \frac{2}{2\pi} \left[ \frac{3}{4} \right] \cdot f_0$$

$$= \begin{bmatrix} \frac{\partial}{\partial g} & \frac{\partial}{\partial a} & \frac{\partial}{\partial a} & \frac{\partial}{\partial a} \\ 0 \end{bmatrix} \cdot \begin{bmatrix} 0 \\ 0 \end{bmatrix}$$

$$= \left[ \frac{1}{d} - \frac{9}{d^2} \right] \left[ 0 \right]$$

$$=$$
  $\left[\frac{1}{4}\right]$ 

$$|f_{i}|^{2}h = \frac{2}{2\pi} \left[ L_{i}h \right] f_{i}$$

$$= \frac{\partial}{\partial x} \left[ \frac{1}{d} \right] f_1$$

$$= \begin{bmatrix} 0 & -\frac{1}{4^2} \end{bmatrix} \begin{bmatrix} 0 \\ 0 \end{bmatrix}$$

G = 
$$\left\{ \begin{bmatrix} 9 \\ \overline{d} \end{bmatrix}, \begin{bmatrix} 0 \\ 0 \end{bmatrix}, \begin{bmatrix} -1 \\ \overline{d} \end{bmatrix} u_1, \begin{bmatrix} 0 \\ 0 \end{bmatrix} u_1 \right\}$$

reminber these terms exist if

$$\int_{Ac} (G) \left| \begin{array}{c} x_0 \\ x_0 \\ 0 \end{array} \right|_{Ac} = \left[ \begin{array}{c} \frac{1}{4} & \frac{3}{4}z \\ 0 & 0 \\ 0 \cdot u_1 & \frac{1}{4}z \end{array} \right] = O$$

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If  $u_1 = 0$ ,  $J_{ac}(G)$  is not full rank for any  $\chi_0$ If  $u_1 \neq 0$ ,  $J_{ac}(G)$  is full rank if  $d \neq \infty$ and  $d \neq 0$ .

Therefore, system is observable iff U, \$0 => System must be accelerating.

Doing the derivatives is tedious... con be done symbolically.