Standard Code Library

FLself

SCUT

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一切的开始

一些宏定义

● 需要 C++11

```
// #define DEBUG
   // #define InTerminal
   // #define std cpp17
   #include<bits/stdc++.h>
   #define int long long
   #define PII std::pair<int, int>
   #define VI std::vector<int>
   #define VPII std::vector<std::pair<int, int> >
   #define VVI std::vector<std::vector<int> >
   #define ALL(a) (a).begin(), (a).end()
   #define SIZ(a) ((int)(a).size())
11
   #define FOR(i, l, r) for (int i = (l); i \le (r); ++i)
   #define REP(i, r, l) for (int i = (r); i \ge (l); --i)
13
   #define lowbit(x) ((x) & (-(x)))
   #define lbpos(x) (__builtin_ctz(x))
15
   #define hbpos(x) (31 - __builtin_clz(x))
16
17
    template<typename S, typename T> std::istream &operator>>(std::istream &is, std::pair<S, T> &pp) { is >> pp.first >>
18

    pp.second; return is; }

     \textbf{template} < \textbf{typename S, typename T} > \textbf{std}::ostream \& \textbf{operator} << (\textbf{std}::ostream \& \textbf{os, std}::pair < \textbf{S, T} > \textbf{pp}) \  \  \{ \  \  \textbf{os} << \  \  "(" < < \  \  \texttt{ostream} ) \} 
19
     template<typename S, std::size_t _siz> std::istream &operator>>(std::istream &is, std::array<S, _siz> &arr) { for
    template<typename S, std::size_t _siz> std::ostream &operator<<(std::ostream &os, std::array<S, _siz> arr) { os <</pre>
     \textbf{template} < \textbf{typename T} > \textbf{std}:: \textbf{istream \& operator} >> (\textbf{std}:: \textbf{istream \& is, std}:: \textbf{vector} < \textbf{T} > \textbf{\&vec}) ~ \{ \textbf{ for (auto \& x: vec) is } >> \textbf{x; } \}
22

→ return is: }

    template<typename T> std::ostream &operator<<(std::ostream &os, const std::vector<T> &vec) { os << '{'}; for (auto
23
     ⇔ &x: vec) os << x << ", "; return os << "}";}</pre>
    #ifdef std cpp17
24
    template < class Tuple, std::size_t... Is> void print_tuple_impl(std::ostream &os, const Tuple &t,
    ⇔ std::index_sequence<Is...>) { ((os << (Is == 0? "" : ", ") << std::get<Is>(t)), ...); }
    template <class... Args> std::ostream &operator << (std::ostream &os, const std::tuple <Args...> &t) { os << "(";

    print_tuple_impl(os, t, std::index_sequence_for<Args...>{}); return os << ")"; }
</pre>
    #endif
27
    #ifdef DEBUG
   #ifdef InTerminal
29
    #define dbg(x...) do { std::cerr << "\033[32;1m" << #x << " -> "; <math>err(x); } while (0)
    void err() { std::cerr << "\033[39;0m" << std::endl; }</pre>
31
32
    #define dbg(x...) do { std::cerr << \#x << " -> "; err(x); } while (0)
   void err() { std::cerr << std::endl; }</pre>
34
    template<typename T, typename... A>
36
    void err(T a, A... x) { std::cerr << a << ' '; err(x...); }</pre>
37
    #else
38
    #define dbg(...)
39
    #endif
41
42
    using namespace std;
    const int maxn = 2e5 + 3;
43
    const int INF = 0x3f3f3f3f3f3f3f3f3f3f3;
44
    const int mod = 998244353;
    mt19937 RD(time(0));
46
47
48
49
50
   void solv() {
51
52
53
        return ;
54
   }
55
56
    signed main() {
        // freopen("./data.in", "r", stdin);
```

```
std::ios::sync_with_stdio(false), std::cin.tie(0), std::cout.tie(0);
58
59
        int beg__TT = clock();
60
        signed _ttt;
61
62
        cin >> _ttt;
63
        while(_ttt--)
64
65
            solv():
66
        #ifdef DEBUG
67
        std::cerr << "use : " << (clock() - beg__TT) << "ms\n";
68
        #endif
70
        return 0;
   }
71
    数据结构
    ST 表
        一维
    class Sparcetable {
        vector<vector<int> > st;
        int siz;
        bool MX_flg = 0;
        inline int renew(int x, int y) {
            if (MX_flg) return max(x, y);
            return min(x, y);
    public:
        // 注意 bhpos(0) 返回-1
10
        bool (*comp)(int, int);
11
        Sparcetable():siz(maxn) {st.resize(hbpos(maxn - 1) + 1, std::vector<int> (maxn));}
        Sparcetable(const std::vector<int>& a, bool _MX_flg = 1): siz(a.size()), MX_flg(_MX_flg) {
13
14
            int n = a.size();
            st.resize(hbpos(n) + 1, vector < int > (n + 1));
15
            for (int i = 1; i <= n; ++i) st[0][i] = a[i];</pre>
16
            for (int i = 1; i <= hbpos(siz); ++i) {</pre>
17
                 for (int j = 1; j + (1 << i) <= siz + 1; ++j) {
18
19
                     st[i][j] = renew(st[i - 1][j], st[i - 1][j + (1 << (i - 1))]);
                 }
20
            }
21
22
        int query(int l, int r) {
23
            int len = hbpos(r - l + 1);
24
            return renew(st[len][l], st[len][r - (1 << len) + 1]);</pre>
25
27
   };
        二维
    int f[10][10][maxn][maxn];
    #define _highbit(x) (31 - __builtin_clz(x))
    inline int calc(int x, int y, int xx, int yy, int p, int q) {
            \label{eq:max} \max(f[p][q][x][y], \ f[p][q][xx - (1 << p) + 1][yy - (1 << q) + 1]),
            \max(f[p][q][xx - (1 << p) + 1][y], f[p][q][x][yy - (1 << q) + 1])
        );
   }
8
    void init() {
        for (int x = 0; x <= _highbit(n); ++x)</pre>
10
        for (int y = 0; y <= _highbit(m); ++y)</pre>
11
            for (int i = 0; i \le n - (1 \le x); ++i)
12
            for (int j = 0; j \le m - (1 \le y); ++j) {
13
                 if (!x && !y) { f[x][y][i][j] = a[i][j]; continue; }
14
15
                 f[x][y][i][j] = calc(
16
                     i, j,
                     i + (1 << x) - 1, j + (1 << y) - 1,
17
```

max(x - 1, 0), max(y - 1, 0)

18

);

```
}
20
21
    inline int get_max(int x, int y, int xx, int yy) {
22
23
        return calc(x, y, xx, yy, _highbit(xx - x + 1), _highbit(yy - y + 1));
    Fenwick Tree(树状数组)
       一维
    template<typename T>
1
    class FenwickT {
        int n:
        vector<T> tr;
    public:
5
        FenwickT(int siz): tr(siz), n(siz) {}
        FenwickT(int siz, T ini): tr(siz, ini), n(siz) {}
        void add(int p, T x) {
            for (int i = p; i < n; i += i & (-i)) tr[i] += x;</pre>
10
11
        T query(int p) {
12
            T ret = T(0);
            for (int i = p; i > 0; i -= i & (-i)) ret += tr[i];
13
14
            return ret;
15
16
        T range_sum(int l, int r) {
            return (query(r) - query(l - 1));
17
18
   };
    线段树
    class SegT{
1
        struct Pt{
            int val, ls, rs, sl;
3
            Pt():val(0), ls(0), rs(0), sl(0) {}
            Pt(int v, int l, int r, int s): val(v), ls(l), rs(r), sl(s) {}
            ~Pt() {}
        int renew(int x, int y) {
            return x + y;
10
        int renewsl(int x, int y) {
11
12
            return x + y;
        }
13
14
        int renewqj(int x, int y, int l, int r) {
            return x + y * (r - l + 1);
15
16
    public:
17
        std::vector<Pt> tr;
18
        int cnt = 0; // 结点数目
19
        SegT() {cnt = 1; tr.emplace_back();} // 建一棵空树
20
21
        // 修改
22
23
        void add(int l, int r, int p, int ql, int qr, int x) {
24
            if (ql <= l && r <= qr) {
                tr[p].val = renewqj(tr[p].val, x, l, r);
25
                tr[p].sl = renewsl(tr[p].sl, x);
27
                return;
28
            int mid = l + (r - l) / 2;
29
            if (tr[p].sl) {
30
                if (!tr[p].ls) tr[p].ls = cnt++;
                if (!tr[p].rs) tr[p].rs = cnt++;
32
                if (cnt >= tr.size()) tr.resize(cnt + 1);
33
34
                int ls = tr[p].ls, rs = tr[p].rs;
               tr[ls].val = renewqj(tr[ls].val, tr[p].sl, l, mid), tr[rs].val = renewqj(tr[rs].val, tr[p].sl, mid + 1, r);
35
                tr[ls].sl = renewsl(tr[ls].sl, tr[p].sl), tr[rs].sl = renewsl(tr[rs].sl, tr[p].sl);
                tr[p].sl = 0;
37
            }
```

```
if (ql <= mid) {
39
40
                if (!tr[p].ls) tr[p].ls = cnt++;
                if (cnt >= tr.size()) tr.resize(cnt + 1);
41
42
                add(l, mid, tr[p].ls, ql, qr, x);
43
            if (qr > mid) {
44
                if (!tr[p].rs) tr[p].rs = cnt++;
45
                if (cnt >= tr.size()) tr.resize(cnt + 1);
46
                add(mid + 1, r, tr[p].rs, ql, qr, x);
47
48
            tr[p].val = renew(tr[p].ls? tr[tr[p].ls].val: 0, tr[p].rs? tr[tr[p].rs].val: 0);
49
50
        };
51
52
        int query(int l, int r, int p, int ql, int qr) {
53
            if (ql <= l && r <= qr) return tr[p].val;</pre>
54
            int mid = l + (r - l) / 2;
55
            if (tr[p].sl) {
56
                if (!tr[p].ls) tr[p].ls = cnt++;
                if (!tr[p].rs) tr[p].rs = cnt++;
58
59
                if (cnt >= tr.size()) tr.resize(cnt + 1);
60
                int ls = tr[p].ls, rs = tr[p].rs;
               tr[ls].val = renewqj(tr[ls].val, tr[p].sl, l, mid), tr[rs].val = renewqj(tr[rs].val, tr[p].sl, mid + 1, r);
61
                tr[ls].sl = renewsl(tr[ls].sl, tr[p].sl), tr[rs].sl = renewsl(tr[rs].sl, tr[p].sl);
                tr[p].sl = 0;
63
64
            int ret = 0;
65
            if (ql <= mid) {
66
67
                if (!tr[p].ls) tr[p].ls = cnt++;
                if (cnt >= tr.size()) tr.resize(cnt + 1);
68
                ret = renew(ret, query(l, mid, tr[p].ls, ql, qr));
69
70
            if (qr > mid) {
71
72
                if (!tr[p].rs) tr[p].rs = cnt++;
                if (cnt >= tr.size()) tr.resize(cnt + 1);
73
                ret = renew(ret, query(mid + 1, r, tr[p].rs, ql, qr));
74
75
            tr[p].val = renew(tr[p].ls? tr[tr[p].ls].val: 0, tr[p].rs? tr[tr[p].rs].val: 0);
76
77
            return ret;
78
        };
   };
```

数学

数论

数论整数

```
constexpr int P = 998244353;
    // assume -P \le x \le 2P
    int norm(int x) {
        // x %= P;
        if (x < 0) \{ x += P; \}
        if (x >= P) { x -= P; }
        return x;
    }
    template<typename E>
10
    E power(E n, int k) {
        E ret = E(1);
11
12
        while (k) {
            if (k & 1) ret *= n;
13
            n \star = n;
            k >>= 1;
15
        } return ret;
16
17
    struct Z {
18
        int x;
        Z(int x = 0) : x(norm(x)) \{ \}
20
        int val() const { return x; }
21
        Z operator-() const { return Z(norm(P - x)); }
22
```

```
Z inv() const { assert(x != 0); return power(*this, P - 2); }
23
24
                 Z & operator *= (const Z & rhs) { x = (long long)(x) * rhs.x % P; return *this; }
                 Z &operator+=(const Z &rhs) { x = norm(x + rhs.x); return *this; }
25
                 Z &operator-=(const Z &rhs) { x = norm(x - rhs.x); return *this; }
26
27
                 Z &operator/=(const Z &rhs) { return *this *= rhs.inv(); }
                 friend Z operator*(const Z &lhs, const Z &rhs) { Z res = lhs; res *= rhs; return res; }
28
                 friend Z operator+(const Z &lhs, const Z &rhs) { Z res = lhs; res += rhs; return res;
29
                 friend Z operator-(const Z &lhs, const Z &rhs) { Z res = lhs; res -= rhs; return res; }
30
                 friend Z operator/(const Z &lhs, const Z &rhs) { Z res = lhs; res /= rhs; return res; }
31
                 friend std::istream &operator>>(std::istream &is, Z &a) { long long v; is >> v; a = Z(v); return is; }
32
                 friend std::ostream &operator<<(std::ostream &os, const Z &a) { return os << a.val(); }</pre>
33
       };
        拉格朗日差值法
        欧几里得
                • 扩展欧几里得
        int exgcd(int a, int b, int& x, int& y) {
2
                 if (a == 0) {
                        x = 0, y = 1;
                         return b;
                 int ret = exgcd(b % a, a, x, y), xx = x;
                 x = y - b / a * x;
                y = xx;
                 return ret;
        类欧几里得
               • f(a,b,c,n) = \sum_{i=0}^n \lfloor \frac{ai+b}{c} \rfloor: 当 a \geq c or b \geq c 时, f(a,b,c,n) = (\frac{a}{c})n(n+1)/2 + (\frac{b}{c})(n+1) + f(a \bmod c, b \bmod c, c, n); 否则 f(a,b,c,n) = nm - f(c,c-b-1,a,m-1) 。
               • g(a,b,c,n) = \sum_{i=0}^{n} i \lfloor \frac{ai+b}{c} \rfloor : \exists a \geq c \text{ or } b \geq c \text{ fl}, g(a,b,c,n) = (\frac{a}{c})n(n+1)(2n+1)/6 + (\frac{b}{c})n(n+1)/2 + (\frac{b}{c
                    g(a \bmod c, b \bmod c, c, n); 否则 g(a, b, c, n) = \frac{1}{2}(n(n+1)m - f(c, c-b-1, a, m-1) - h(c, c-b-1, a, m-1))。
               • h(a,b,c,n) = \sum_{i=0}^{n} \lfloor \frac{ai+b}{c} \rfloor^2: \exists a \geq c \text{ or } b \geq c \text{ pl}, h(a,b,c,n) = (\frac{a}{c})^2 n(n+1)(2n+1)/6 + (\frac{b}{c})^2 (n+1) + (\frac{b}{c})^2 (n+1)
                    (\frac{a}{c})(\frac{b}{c})n(n+1)+h(a \bmod c,b \bmod c,c,n)+2(\frac{a}{c})g(a \bmod c,b \bmod c,c,n)+2(\frac{b}{c})f(a \bmod c,b \bmod c,c,n);否则
                    h(a,b,c,n) = nm(m+1) - 2g(c,c-b-1,a,m-1) - 2f(c,c-b-1,a,m-1) - f(a,b,c,n)
        template<typename T>
        T lintp(const vector<int>& x, const vector<T>& y, int k) {
                 T ans = 0:
                 for (int i = 0; i < x.size(); ++i) {</pre>
                         if (k == x[i])
                                return y[i];
                         T u = 1, v = 1;
                         for (int j = 0; j < x.size(); ++j) {</pre>
                                 if (i == j) continue;
                                 u *= (k - x[j]);
10
11
                                 v *= (x[i] - x[j]);
12
                         ans += y[i] * u / v;
13
15
                 return ans:
        中国剩余定理
        int CRT(std::vector<int> a, std::vector<int> r) {
                long long n = 1, ans = 0, k = a.size();
                 for (int i = 0; i < k; ++i) n = n * r[i];</pre>
                 for (int i = 0; i < k; ++i) {</pre>
                         long long m = n / r[i], b, y;
                         exgcd(m, r[i], b, y);
                        ans = (ans + a[i] * m % n * b % n + n) % n;
                }
```

```
9 return ans;
10 }
```

各种筛

筛法	场景	效率
Min-25 筛 PN 筛 杜教筛	$f(p)$ 是一个关于 p 的多项式, $f(p^c)$ 能快速求 找一个好求前缀和的积性函数 $g()$ 在 p 处 $f(p)=g(p)$ 找一个 $g()$ 使得 $f*g()$ 好求前缀和	$O(\frac{n^{\frac{3}{4}}}{\log n})$ $O(\sqrt{n})$ $O(n^{\frac{2}{3}})$

Min-25 筛

1

namespace Min_25{

```
bool INI = 0;
         int M = 0, sqn = 0;
3
         std::vector<int> primes;
        Z (*fp)(int, int); // f(p^{\wedge}c)
Z fp_single(int p, int c) {
             return power(Z(p), c);
         Z sgp(int n, int c) {
             if (c == 0) return Z(n);
10
             if (c == 1) return Z(n+ 1) * n / 2;
11
             if (c == 2) return Z(2*n+1) * (n+1) * n / 6;
12
             // if (c == 3) return Z(n) * n * (n+1) * (n+1) / 4;
13
             // if (c == 4) return Z(n) * (n+1) * (2*n+1) * (3*n*n%P + 3*n - 1) / 30;
        }
15
         struct Gpoly{
16
17
             int M, sqn, a;
             std::vector<Z> F_prime1, F_prime2;
18
19
             Gpoly(int scale, int a, int c): M(scale), a(a) {
                 sqn = sqrt(M) + 3;
20
21
                 F_prime1.resize(sqn), F_prime2.resize(sqn);
22
                 int st = M, ed = 1;
23
                 for (int i = 1; st >= ed; st = min(M / ++i, st - 1)) {
24
                      (*this)[st] = sgp(st, c) - 1;
25
26
                 for (int j = 1; j < primes.size(); ++j) {</pre>
27
                      st = M, ed = primes[j] * primes[j];
28
                      for (int i = 1; st >= ed; st = min(M / ++i, st - 1)) {
29
                           (*\textbf{this})[st] -= fp\_single(primes[j], c) * ((*\textbf{this})[st/primes[j]] - (*\textbf{this})[primes[j-1]]);
30
31
                 }
32
33
             void seta(int aa) {a = aa;}
34
             Z & operator [](int idx) {
35
36
                 if (idx < sqn) return F_prime1[idx];</pre>
                 return F_prime2[M/idx];
37
             }
        };
39
40
         std::vector<Gpoly> Gp;
41
         Z G(int x){
42
43
             Z res = 0;
             for (auto &g: Gp) res += g[x] * g.a;
44
45
             return res;
46
         void init(int scale) {
47
             if (M < scale) INI = 0;</pre>
48
             M = scale, sqn = sqrt(M) + 5;
49
             if (!INI) {
51
                 INI = 1;
52
                 std::vector<signed> vis(sqn);
53
                 primes.resize(1, 1);
54
55
                 for (int i = 2; i < sqn; ++i) {</pre>
```

```
if (!vis[i]) primes.push_back(i);
56
57
                    for (int j = 1; j < primes.size(); ++j) {</pre>
58
                        auto prm = primes[j];
                        if (prm * i >= sqn) break;
59
                        vis[i * prm] = 1;
                        if (i % prm == 0) break;
61
                    }
62
               }
63
64
           }
66
67
           Gp.clear();
68
           Gp.emplace_back(scale, N, 0);
            // Gp.emplace_back(scale, a, c); // a*p^c
69
70
        Z seive(int n, int k) {
71
72
           Z res = G(n) - G(primes[k-1]);
            for (int i = k; i < primes.size() && primes[i] * primes[i] <= n; ++i) {</pre>
73
74
                Z fpj = fp(primes[i], 1), fpj1;
                75
                    fpj1 = fp(primes[i], j + 1);
76
                    res += fpj * seive(n/pc, i + 1) + fpj1;
77
                }
78
            }
            return res;
80
81
82
        Z S_f(int n) {
           return seive(n, 1) + 1;
83
        void seta(const vector<int>& a) {for (int i = 0; i < Gp.size() && i < a.size(); ++i) Gp[i].seta(a[i]);}</pre>
85
   }
86
   PN 筛 (Powerful Number)
    // f = (g*h); f(p) = g(p) + h(p) [with f(p) = g(p)] -> h[p] = 0.
   namespace PowerfulNumber{
2
        bool INI = 0;
        std::vector<int> primes;
4
        std::vector<std::vector<Z> > h;
5
        int M;
        Z (*fp)(int, int); // f(p^c)
        Z (*gp)(int, int); // g(p^c)
                           // preffix sum of g()
       Z (*S_g)(int);
10
        // if lack of a formula of h(i, j), you need to set f() and g() beforehand
11
        void init(int scale) {
12
13
            if (M < scale) INI = 0;</pre>
           M = scale;
14
            int n = std::sqrt(M)+10;
15
            if (!INI) {
16
                INI = 1;
17
18
                primes.resize(0);
                std::vector<signed> vis(n);
19
20
                for (int i = 2; i < n; ++i) {
                    if (!vis[i]) primes.push_back(i);
21
                    for (auto prm: primes) {
22
                        if (prm * i >= n) break;
23
                        vis[i * prm] = 1;
24
25
                        if (i % prm == 0) break;
                    }
26
                h.resize(primes.size(), std::vector<Z>((int)(log2(M))+1));
28
           }
29
30
            // get the function h() (with f() and g() set or with formula of h())
31
            for (int i = 0; i < h.size(); ++i) {</pre>
                int pp = primes[i] * primes[i];
33
34
                if (pp > M) break;
                h[i][0] = 1;
35
                for (int j = 2; pp <= M && j < h[i].size(); ++j, pp *= primes[i]) {</pre>
36
                    Z sgh = 0;
```

```
for (int k = 1, xp = primes[i]; k <= j; ++k, xp *= primes[i]) {</pre>
38
39
                          sgh += gp(primes[i], xp) * h[i][j-k];
40
41
                     h[i][j] = fp(pp, j) - sgh;
42
                     // h[i][j] = Z(j-1) * (pp * primes[i] % P - pp % P);
                     // h[i][j] = Z(-pp) / (j * (j-1));
43
44
                     // [a formula of h(i, j)], better faster than log, this example can be optimized to O(1).
                 }
45
            }
46
        }
47
48
49
        // assistance func to get the sum
        Z PN_sieve(int n, int flr, Z hd) {
50
             Z res = S_g(n)*hd;
51
             for(int i = flr+1; i < primes.size(); ++i) {</pre>
52
                 int prm=primes[i], k=1;
53
54
                 int val=n/prm, pk=prm;
55
                 if(val < prm) break;</pre>
                 while(val >= prm) {
57
58
                     val /= prm;
59
                     pk *= prm;
                     ++k;
60
                     res += PN_sieve(val, i, hd*h[i][k]);
62
63
                 }
             }
64
            return res;
65
66
        // func to get the sum
67
        Z getsumf(int n) {
68
            return PN_sieve(n, -1, 1);
69
70
71
    }
    杜教筛
    // g(1)S(n) = \sum_{i=1}^{n} (f*g)(i) - \sum_{i=2}^{n} g(i)S(n/i)
    namespace dujiaoshai{
2
        vector<Z> smallS;
        map<int, Z> bigS;
4
        void Set_smallS(int);
        Z (*S_fg)(int);
        Z (*S_g)(int);
        Z getS(int n) {
             if (n < smallS.size()) return smallS[n];</pre>
10
             else if (bigS.count(n)) return bigS[n];
11
             Z res = S_fg(n);
12
             for (int l = 2, r; l <= n; l = r + 1) {
13
                 r = n / (n / 1);
14
                 res -= (S_g(r) - S_g(l-1)) * getS(n/l);
15
16
17
             // res /= S_g(1);
             return (bigS[n] = res);
18
19
    }
20
21
22
    void dujiaoshai::Set_smallS(int siz) {
        int n = pow(siz, 0.67);
23
24
        smallS.assign(n, 0);
        smallS[1] = 1;
25
        vector<signed> vis(n), primes;
26
        for (int i = 2; i < n; ++i) {</pre>
27
28
             if (!vis[i]) {
                 primes.push_back(i);
                 smallS[i] = i - 1;
30
31
             for (auto &prm: primes) {
32
                 if (i * prm >= n) break;
33
                 vis[i * prm] = 1;
```

```
if (i % prm == 0) {
35
36
                     smallS[i * prm] = smallS[i] * prm;
37
                     break;
                 }
38
                 smallS[i * prm] = smallS[i] * (prm - 1);
40
41
             smallS[i] = smallS[i-1] + smallS[i]*i;
42
    }
43
    多项式
        • Poly with NTT
    std::vector<int> rev;
    std::vector<Z> roots{0, 1};
    void dft(std::vector<Z> &a) {
        int n = a.size();
5
        if ((int)(rev.size()) != n) {
             int k = __builtin_ctz(n) - 1;
             rev.resize(n);
             for (int i = 0; i < n; i++) {</pre>
                 rev[i] = rev[i >> 1] >> 1 | (i & 1) << k;
10
11
        }
12
        for (int i = 0; i < n; i++) {
14
15
             if (rev[i] < i) {
                 std::swap(a[i], a[rev[i]]);
16
17
18
        if ((int)(roots.size()) < n) {</pre>
19
             int k = __builtin_ctz(roots.size());
20
            roots.resize(n);
21
            while ((1 << k) < n)  {
22
                 Z = power(Z(3), (P - 1) >> (k + 1));
23
                 for (int i = 1 << (k - 1); i < (1 << k); i++) {
24
25
                     roots[2 * i] = roots[i];
                     roots[2 * i + 1] = roots[i] * e;
26
                 }
27
                 k++;
28
            }
29
30
        for (int k = 1; k < n; k *= 2) {</pre>
31
             for (int i = 0; i < n; i += 2 * k) {
                 for (int j = 0; j < k; j++) {
33
                     Z u = a[i + j];
Z v = a[i + j + k] * roots[k + j];
34
35
                     a[i + j] = u + v;
36
                     a[i + j + k] = u - v;
                 }
38
            }
39
40
    }
41
    void idft(std::vector<Z> &a) {
        int n = a.size();
43
44
        std::reverse(a.begin() + 1, a.end());
        dft(a);
45
        Z inv = (1 - P) / n;
46
        for (int i = 0; i < n; i++) {</pre>
47
            a[i] *= inv;
48
49
    }
50
    struct Poly {
51
        std::vector<Z> a;
52
53
        Poly() {}
54
        Poly(const std::vector<Z> &a) : a(a) {}
        Poly(const std::initializer_list<Z> &a) : a(a) {}
55
        int size() const {
57
            return a.size();
```

```
58
59
         void resize(int n) {
60
             a.resize(n);
         }
61
         Z operator[](int idx) const {
62
             if (idx < size()) {
63
                  return a[idx];
64
             } else {
65
                  return 0;
66
67
             }
68
69
         Z & operator[](int idx) {
70
             return a[idx];
71
         Poly mulxk(int k) const {
72
             auto b = a;
73
74
             b.insert(b.begin(), k, 0);
             return Poly(b);
75
76
         Poly modxk(int k) const {
77
             k = std::min(k, size());
78
79
             return Poly(std::vector<Z>(a.begin(), a.begin() + k));
80
         Poly divxk(int k) const {
              if (size() <= k) {
82
83
                  return Poly();
84
             return Poly(std::vector<Z>(a.begin() + k, a.end()));
85
86
         friend Poly operator+(const Poly &a, const Poly &b) {
87
             std::vector<Z> res(std::max(a.size(), b.size()));
88
             for (int i = 0; i < (int)(res.size()); i++) {</pre>
89
                  res[i] = a[i] + b[i];
90
91
             }
             return Poly(res);
92
93
         friend Poly operator-(const Poly &a, const Poly &b) {
94
             std::vector<Z> res(std::max(a.size(), b.size()));
95
             for (int i = 0; i < (int)(res.size()); i++) {</pre>
                  res[i] = a[i] - b[i];
97
98
             return Poly(res);
99
100
101
         friend Poly operator*(Poly a, Poly b) {
             if (a.size() == 0 || b.size() == 0) {
102
103
                  return Poly();
104
105
             int sz = 1, tot = a.size() + b.size() - 1;
             while (sz < tot) {</pre>
106
                  sz *= 2;
107
108
             a.a.resize(sz);
109
             b.a.resize(sz);
             dft(a.a);
111
             dft(b.a);
112
             for (int i = 0; i < sz; ++i) {</pre>
113
                  a.a[i] = a[i] * b[i];
114
115
             idft(a.a);
116
             a.resize(tot);
117
118
             return a;
119
120
         friend Poly operator*(Z a, Poly b) {
             for (int i = 0; i < (int)(b.size()); i++) {</pre>
121
122
                  b[i] *= a;
             }
123
             return b;
124
125
         friend Poly operator*(Poly a, Z b) {
126
127
             for (int i = 0; i < (int)(a.size()); i++) {</pre>
                  a[i] *= b;
128
```

```
129
             return a;
130
131
         Poly &operator+=(Poly b) {
132
             return (*this) = (*this) + b;
133
134
         Poly &operator-=(Poly b) {
135
             return (*this) = (*this) - b;
136
137
138
         Poly &operator*=(Poly b) {
             return (*this) = (*this) * b;
139
140
         Poly deriv() const {
141
             if (a.empty()) {
142
                  return Poly();
143
144
145
             std::vector<Z> res(size() - 1);
             for (int i = 0; i < size() - 1; ++i) {</pre>
146
                  res[i] = (i + 1) * a[i + 1];
147
             }
148
             return Poly(res);
149
         Poly integr() const {
151
             std::vector<Z> res(size() + 1);
152
             for (int i = 0; i < size(); ++i) {</pre>
153
                  res[i + 1] = a[i] / (i + 1);
154
155
             return Poly(res);
156
157
         Poly inv(int m) const {
158
             Poly x{a[0].inv()};
159
             int k = 1;
160
             while (k < m) {
161
                  k *= 2;
                  x = (x * (Poly{2} - modxk(k) * x)).modxk(k);
163
164
             return x.modxk(m);
165
166
167
         Poly log(int m) const {
             return (deriv() * inv(m)).integr().modxk(m);
168
169
         Poly exp(int m) const {
170
             Poly x{1};
171
172
             int k = 1;
             while (k < m) {</pre>
173
174
                  k *= 2;
                  x = (x * (Poly{1} - x.log(k) + modxk(k))).modxk(k);
175
176
             return x.modxk(m);
177
178
179
         Poly pow(int k, int m) const {
             int i = 0;
180
             while (i < size() && a[i].val() == 0) {</pre>
                  i++;
182
183
             if (i == size() || 1LL * i * k >= m) {
184
                  return Poly(std::vector<Z>(m));
185
186
187
             Z v = a[i];
             auto f = divxk(i) * v.inv();
188
             return (f.log(m - i * k) * k).exp(m - i * k).mulxk(i * k) * power(v, k);
189
190
         Poly sqrt(int m) const {
             Poly x{1};
192
             int k = 1;
193
             while (k < m) {</pre>
194
                  k *= 2;
195
                  x = (x + (modxk(k) * x.inv(k)).modxk(k)) * ((P + 1) / 2);
196
197
             return x.modxk(m);
198
         }
199
```

```
Poly mulT(Poly b) const {
200
             if (b.size() == 0) {
201
                 return Poly();
202
203
             int n = b.size();
             std::reverse(b.a.begin(), b.a.end());
205
             return ((*this) * b).divxk(n - 1);
206
207
         std::vector<Z> eval(std::vector<Z> x) const {
208
209
             if (size() == 0) {
                 return std::vector<Z>(x.size(), 0);
210
211
212
             const int n = std::max((int)(x.size()), size());
             std::vector<Poly> q(4 * n);
213
214
             std::vector<Z> ans(x.size());
             x.resize(n);
215
216
             std::function<void(int, int, int)> build = [&](int p, int l, int r) {
                 if (r - l == 1) {
217
218
                      q[p] = Poly{1, -x[l]};
                 } else {
219
                      int m = (l + r) / 2;
220
                      build(2 * p, l, m);
221
                      build(2 * p + 1, m, r);
222
                      q[p] = q[2 * p] * q[2 * p + 1];
223
                 }
224
             };
225
             build(1, 0, n);
226
             std::function<void(int, int, int, const Poly &)> work = [&](int p, int l, int r, const Poly &num) {
227
                 if (r - l == 1) {
228
                      if (l < (int)(ans.size())) {
229
                          ans[l] = num[0];
230
                     }
231
                 } else {
232
233
                      int m = (l + r) / 2;
                      work(2 * p, l, m, num.mulT(q[2 * p + 1]).modxk(m - l));
234
                      work(2 * p + 1, m, r, num.mulT(q[2 * p]).modxk(r - m));
235
236
             };
237
238
             work(1, 0, n, mulT(q[1].inv(n)));
             return ans:
239
    };
241
        • FFT
    namespace FFT { // n_ 是初始的数组长度,不一定为 2 的幂次; n 是 init 之后的长度,保证为 2 的幂次长度
1
         const double PI = acos(-1);
         int rev[1 << 20];</pre>
3
         int init(int n_) {
             int step = 0, n = 1;
5
             for (; n < n_; n <<= 1) ++step;</pre>
6
             for (int i = 1; i < n; ++i) {</pre>
                 rev[i] = (rev[i >> 1] >> 1) | ((i & 1) << (step - 1));
             }
             return n;
10
11
         void FFT(complex<double> a[], int n, int f) {
12
             for (int i = 0; i < n; ++i) {</pre>
13
14
                 if (i < rev[i]) std::swap(a[i], a[rev[i]]);</pre>
15
             for (int h = 2; h <= n; h <<= 1) {
16
                 complex<double> wn(cos(f * 2 * PI / h), sin(f * 2 * PI / h));
17
                 for (int i = 0; i < n; i += h) {</pre>
18
19
                      complex<double> w(1, 0), u;
                      for (int j = i, k = h >> 1; j < i + k; ++j) {
20
                          u = a[j + k] * w;
21
                          a[j + k] = a[j] - u;
22
                          a[j] = a[j] + u;
23
24
                          w = w * wn;
25
                      }
26
                 }
             }
27
```

```
if (f == -1) {
28
29
                 for (int i = 0; i < n; ++i) {</pre>
                     a[i] = {a[i].real() / n, 0};
30
31
             }
33
        void conv(complex<double> a[], complex<double> b[], int n_) { // n_ does not represent the pow of 2.
34
            int n = init(n_);
35
             FFT(a, n, 1);
36
37
             FFT(b, n, 1);
             for (int i = 0; i < n; ++i) a[i] *= b[i];</pre>
38
            FFT(a, n, -1);
40
   }
```

组合数学

卡特兰数

可以将问题划分为两个子问题的问题,满足递推式:

$$H_n = \begin{cases} \sum_{i=1}^n H_{i-1} H_{n-i} & n \geq 2, n \in \mathbb{N}_+ \\ 1 & n = 0, 1 \end{cases}$$

递推式:
$$H_n=\frac{H_{n-1}(4n-2)}{n+1}$$
 通项式: $H_n=\binom{2n}{n}-\binom{2n}{n-1}$

斯特林数

将 n 个不相同的元素划分为 k 个互不区分的集合, $\binom{n}{k}$, 也记作 S(n,k) .

递推式: $S(n,k) = S(n-1,k) + k \times S(n-1,k)$

第二类斯特林数

```
struct Stirling2 {
        std::vector<std::vector<Z> > S;
        Stirling2 (int n) {
             S.resize(n+1, vector<Z>(n+1));
             S[0][0] = 1;
             for (int i = 1; i <= n; ++i) {
                 for (int j = 1; j <= n; ++j) {</pre>
                     S[i][j] = S[i-1][j-1] + S[i-1][j] * j;
                 }
            }
10
11
        std::vector<Z> &operator [](int idx) {return S[idx];}
12
    };
13
15
    struct Stirling2_oneline {
16
17
        std::vector<Z> S;
        int n;
18
        // S[n][k] = \sum \frac {i^n (-1)^{m-i}}{i! (m-i)!}
        // that is convolution of f(x) = x^n / (x!) and g(x) = (-1)^x / (x!)
20
        Stirling2_oneline(int _n): n(_n) {
21
            vector\langle Z \rangle f(n+1), g(n+1), ifact(n+1);
22
             g[0] = 1;
23
            Z fact = 1;
25
             for (int i = 1; i <= n; ++i) fact *= i;</pre>
26
            ifact[n] = fact.inv();
27
             for (int i = n-1; i >= 1; --i) {
                 ifact[i] = ifact[i+1] * (i+1);
30
31
            for (int i = 1; i <= n; ++i) {</pre>
32
```

```
f[i] = power(Z(i), n) * ifact[i];
g[i] = ifact[i] * (i % 2? -1: 1);

f(i) = power(Z(i), n) * ifact[i];
g[i] = ifact[i] * (i % 2? -1: 1);

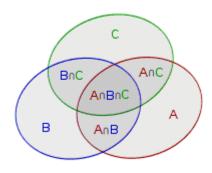
f(i) = power(Z(i), n) * ifact[i];
```

分拆数

将n分成k个部分的分拆,称为k部分拆,记作p(n,k)

递推式: p(n,k) = p(n-1,k-1) + p(n-k,k)

容斥原理



 $|A \cup B \cup C| = |A| + |B| + |C| - |A \cap B| - |B \cap C| - |C \cap A| + |A \cap B \cap C|$

进一步推广:

$$\begin{split} \left|\bigcup_{i=1}^n S_i\right| &= \sum_i |S_i| - \sum_{i < j} |S_i \cap S_j| + \sum_{i < j < k} |S_i \cap S_j \cap S_k| - \cdots \\ &+ (-1)^{m-1} \sum_{a_i < a_{i+1}} \left|\bigcap_{i=1}^m S_{a_i}\right| + \cdots + (-1)^{n-1} |S_1 \cap \cdots \cap S_n| \end{split}$$

经典例子: 不定方程非负整数解

线性代数

线性基

```
struct LinearBase{
        std::vector<int> LBP;
        LinearBase(): LBP(64) {}
        LinearBase(int _n): LBP(_n) {}
        void insert(int x) {
            for (int i = (int)LBP.size() - 1; i >= 0; --i) {
                if ((x >> i) & 1) {
                    if (!LBP[i]) {LBP[i] = x; break;}
                    else x ^= LBP[i];
11
                else continue;
            }
14
        bool query(int x) {
            for (int i = (int)LBP.size() - 1; i >= 0; --i) {
                if ((x >> i) & 1) x ^= LBP[i];
            return (x == 0);
19
```

```
int MaxSum() {
    int ret = 0;
    for (int i = (int)LBP.size() - 1; i >= 0; --i) {
        if ((ret >> i) & 1) continue;
        else ret ^= LBP[i];
    }
    return ret;
}
```

博弈论

Sprague-Grundy Theorem (SG 定理), 将多个游戏的 SG 值异或起来就能表示组合起来的胜负状态. 可以归纳法来证明.

图论

LCA

● 倍增

```
void dfs(int u, int fa) {
        pa[u][0] = fa; dep[u] = dep[fa] + 1;
        for (int i = 1; i < SP; ++i) pa[u][i] = pa[pa[u][i - 1]][i - 1];</pre>
        for (int& v: G[u]) {
            if (v == fa) continue;
            dfs(v, u);
        }
   }
8
    int lca(int u, int v) {
10
        if (dep[u] < dep[v]) swap(u, v);</pre>
        int t = dep[u] - dep[v];
12
        for (int i = 0; i < SP; ++i) if (t & (1 << i)) u = pa[u][i];</pre>
13
        for (int i = SP-1; i >= 0; --i) {
14
            int uu = pa[u][i], vv = pa[v][i];
15
16
            if (uu != vv) { u = uu; v = vv; }
        }
17
18
        return u == v ? u : pa[u][0];
   }
19
       ● 树链剖分
    namespace HLD{
1
        const int N = 1e5+3;
        std::vector<std::pair<int, int> > g[N]; // 原本的树
        int idx[N]; // idx[x] -> 点 x 的 dfs 序号
        int ridx[N];// ridx[id] -> dfs 序为 id 的点号
        int dep[N]; // dep[x] -> 点 x 的深度
        int siz[N]; // siz[x] -> 以点 x 为根的树的大小
        int top[N]; // top[x] -> 点 x 所在重链的顶点
        int fa[N]; // fa[x] \rightarrow 点 x 的父亲结点
        int son[N]; // son[x] -> 点 x 的重儿子
10
11
        int clk = 0;// clk -> dfs 序号
12
        void init() {
13
            for (int i = 0; i <= clk; ++i)</pre>
                g[i].clear();
15
            clk = 0;
16
17
        int lca(int u, int v) {
18
19
            while (top[u] != top[v]) {
                if (dep[top[u]] < dep[top[v]]) std::swap(u, v);</pre>
20
21
                u = fa[top[u]];
22
23
            if (dep[u] > dep[v]) std::swap(u, v);
24
            return u;
25
26
        void HLDinit(int rt) {
            std::function<void(int, int)> predfs1 = [&](int u, int f) {
27
```

```
siz[u] = 1;
28
29
                int maxs = son[u] = -1;
                for (auto &[to, w]: g[u]) {
30
                    if (to == f) continue;
31
                    fa[to] = u, dep[to] = dep[u] + 1;
                    predfs1(to, u);
33
                    siz[u] += siz[to];
34
                    if (maxs == -1 \mid | siz[to] > siz[maxs]) maxs = to;
35
36
37
            };
           std::function<void(int, int)> predfs2 = [&](int u, int tp) {
38
39
                top[u] = tp;
                idx[u] = ++clk, ridx[clk] = u;
40
                if (son[u] != -1) {
41
42
                    predfs2(son[u], tp);
43
44
                for (auto &[to, w]: g[u]) {
                    if (to != fa[u] && to != son[u]) predfs2(to, to);
45
47
           };
           predfs1(rt, -1);
48
49
           predfs2(rt, rt);
50
52
        void add(int u, int v, int w = 0) {
53
            g[u].emplace_back(v, w);
            g[v].emplace_back(u, w);
54
       }
55
   }
   连通性
   tarjan
   const int N = 1e5 + 3;
   std::vector<int> g[N];
   int dfn[N], dfnx = 0; // dfs 序
   int low[N]; // 最高点
   int col[N], colx = 0; // 连通块标号
   int stk[N], stktp = 0; // 当前链
    bool instk[N];
   void tarjan(int u, int f) {
       dfn[u] = low[u] = ++dfnx;
        stk[++stktp] = u;
10
        for (auto to: g[u]) {
11
            // if (to == f) continue;
12
            if (dfn[to]) {if (instk[to]) low[u] = std::min(dfn[to], low[u]);}
13
            else tarjan(to, u), low[u] = std::min(low[u], low[to]);
15
        if (low[u] == dfn[u]) {
16
17
            while (stk[stktp] != u) instk[stk[stktp]] = 0, col[stk[stktp--]] = colx;
18
            instk[stk[stktp]] = 0, col[stk[stktp--]] = colx;
19
       }
20
   }
21
    树
    虚树
         用栈处理形式上与笛卡尔树类似,按顺序后处理右链部分
   namespace VirtualTree{
        const int N = 3e5+3;
2
        std::vector<std::pair<int, int> > g[N]; // 原本的树
        int idx[N]; // idx[x] -> 点 x 的 dfs 序号
        int ridx[N];// ridx[id] -> dfs 序为 id 的点号
        int dep[N]; // dep[x] -> 点 x 的深度
        int siz[N]; // siz[x] -> 以点 x 为根的树的大小
        int top[N]; // top[x] -> 点 x 所在重链的顶点
```

```
int fa[N]; // fa[x] -> 点 x 的父亲结点
10
        int son[N]; // son[x] -> 点 x 的重儿子
        int clk = 0;// clk -> dfs 序号
11
12
13
        void init() {
             for (int i = 0; i <= clk; ++i)</pre>
14
                 g[i].clear();
15
            clk = 0;
16
17
18
        int lca(int u, int v) {
            while (top[u] != top[v]) {
19
20
                 if (dep[top[u]] < dep[top[v]]) std::swap(u, v);</pre>
21
                 u = fa[top[u]];
22
             if (dep[u] > dep[v]) std::swap(u, v);
23
             return u;
24
25
        void HLDinit(int rt) {
26
27
             std::function<void(int, int)> predfs1 = [&](int u, int f) {
28
                 siz[u] = 1;
                 int maxs = son[u] = -1;
29
                 for (auto &[to, w]: g[u]) {
                     if (to == f) continue;
31
                     fa[to] = u, dep[to] = dep[u] + 1;
32
33
                     predfs1(to, u);
                     siz[u] += siz[to];
34
35
                     if (maxs == -1 || siz[to] > siz[maxs]) maxs = to;
                 }
36
             };
             std::function<void(int, int)> predfs2 = [&](int u, int tp) {
38
39
                 top[u] = tp;
                 idx[u] = ++clk, ridx[clk] = u;
40
                 if (son[u] != -1) {
41
42
                     predfs2(son[u], tp);
43
                 for (auto &[to, w]: g[u]) {
44
                     if (to != fa[u] && to != son[u]) predfs2(to, to);
45
46
47
             };
             predfs1(rt, -1);
48
49
             predfs2(rt, rt);
        }
50
51
52
        int stk[N]; // 栈
        bool isl[N];
53
54
        std::vector<int> vg[N]; // 虚树
        std::vector<int> lst; // 当前虚树中的点
55
        void buildvt(std::vector<int> pt, int rt = 0) {
             for (auto x: lst) vg[x].clear(), isl[x] = 0;
57
58
             lst.clear();
             sort(pt.begin(),\ pt.end(),\ [](\textbf{int}\ u,\ \textbf{int}\ v)\ \{\textbf{return}\ idx[u]\ \langle\ idx[v];\});
59
60
             int tp = 0;
             stk[++tp] = rt; lst.push_back(rt);
62
             for (auto u: pt) {
63
64
                 if (u != rt) {
                     int ll = lca(u, stk[tp]);
65
                     if (ll != stk[tp]) {
                          while (idx[ll] < idx[stk[tp-1]])</pre>
67
                              vg[stk[tp-1]].push_back(stk[tp]), --tp;
68
69
                          vg[ll].push_back(stk[tp]);
                          if (idx[ll] > idx[stk[tp-1]]) stk[tp] = ll, lst.push_back(ll);
70
71
                          else --tp;
72
73
                     stk[++tp] = u, lst.push_back(u);
74
75
                 isl[u] = 1;
            while (tp > 1) {
77
78
                 vg[stk[tp-1]].push_back(stk[tp]);
79
                 --tp;
```

```
}
81
82
         void add(int u, int v, int w = 0) {
83
             g[u].emplace_back(v, w);
84
             g[v].emplace_back(u, w);
85
86
    }
87
    网络流
    Dinic
    class Dinic{
        struct E{
             int to, cp;
             E(int t, int c): to(t), cp(c) {}
        };
5
        int n, m, s, t;
         std::vector<E> edges;
8
         std::vector<std::vector<int> > G;
        int *d, *cur;
10
11
         bool BFS() {
12
13
             memset(d, 0, sizeof(int) * (n));
             std::queue<int> Q;
14
             Q.push(s); d[s] = 1;
15
             while (!Q.empty()) {
16
                 int x = Q.front(); Q.pop();
17
                  for (auto &i: G[x]) {
18
                      E &e = edges[i];
19
                      if (!d[e.to] && e.cp > 0) {
20
                          d[e.to] = d[x] + 1;
                          Q.push(e.to);
22
                      }
23
                 }
24
             }
25
             return d[t];
26
27
28
         int DFS(int u, int cp) {
29
             if (u == t || !cp) return cp;
30
             int tmp = cp, f;
31
             for (int& i = cur[u]; i < G[u].size(); ++i) {</pre>
32
33
                 E& e = edges[G[u][i]];
                 if (d[u] + 1 == d[e.to]) {
34
                      f = DFS(e.to, std::min(cp, e.cp));
35
                      e.cp -= f;
36
                      edges[G[u][i] ^ 1].cp += f;
37
38
                      cp -= f;
                      if (!cp) break;
39
                 }
40
41
42
             return tmp - cp;
43
44
45
        Dinic(\textbf{int} \ nn): \ n(nn), \ G(nn), \ m(\theta) \ \{d = \textbf{new int}[nn], \ cur = \textbf{new int}[nn]; \}
46
47
         ~Dinic() {delete[] d; delete[] cur;}
48
         void add(int u, int v, int cap) {
49
50
             edges.emplace_back(v, cap);
             edges.emplace_back(u, \Theta);
51
52
             G[u].push_back(m++);
53
             G[v].push_back(m++);
54
55
56
         int go(int ss, int tt) {
57
             s = ss, t = tt;
             int flow = 0;
58
```

```
while (BFS()) {
59
60
              memset(cur, 0, sizeof(int) * n);
61
              flow += DFS(s, INF);
62
          }
          return flow;
      }
64
   };
   上下界只需要在建图的时候把上下界之差的出入不平衡的调整一下
```

计算几何

最大流 == 最小割

二维几何: 点与向量

```
const double EPS = 1e-9;
    inline int sign(double a) { return a < -EPS ? -1 : a > EPS; }
3
    inline int cmp(double a, double b){ return sign(a-b); }
4
    struct P {
        double x, y;
        P() {}
8
        P(double _x, double _y) : x(_x), y(_y) {}
        P operator+(P p) { return \{x + p.x, y + p.y\}; \}
10
        P operator-(P p) { return \{x - p.x, y - p.y\}; \}
11
        P operator*(double d) { return {x * d, y * d}; }
12
        P operator/(double d) { return {x / d, y / d}; }
13
14
        bool operator<(P p) const {</pre>
15
            int c = cmp(x, p.x);
            if (c) return c == -1;
17
            return cmp(y, p.y) == -1;
18
19
        }
20
21
        bool operator==(P o) const{
            return cmp(x,o.x) == 0 \&\& cmp(y,o.y) == 0;
22
23
24
        double dot(P p) \{ return x * p.x + y * p.y; \}
25
26
        double det(P p) { return x * p.y - y * p.x; }
27
        double distTo(P p) { return (*this-p).abs(); }
28
        double alpha() { return atan2(y, x); }
29
        void read() { std::cin >> x >>y; }
30
        void write() {std::cout << "(" << x << "," << y << ")" << std::endl;}</pre>
31
        double abs() { return sqrt(abs2());}
32
33
        double abs2() { return x * x + y * y; }
        P rot90() { return P(-y,x);}
34
        P unit() { return *this/abs(); }
35
        int quad() const { return sign(y) == 1 \mid \mid (sign(y) == 0 \&\& sign(x) >= 0); }
36
37
        P rot(double an) { return \{x*\cos(an)-y*\sin(an),x*\sin(an) + y*\cos(an)\}; }
38
   };
39
    struct L{ //ps[0] -> ps[1]
41
        P ps[2];
42
        P& operator[](int i) { return ps[i]; }
43
        P dir() { return ps[1] - ps[0]; }
        L (P a, P b) {
44
45
            ps[0]=a;
            ps[1]=b;
46
47
        bool include(P p) { return sign((ps[1] - ps[0]).det(p - ps[0])) > 0; }
48
        L push(){ // push eps outward
49
50
            const double eps = 1e-8;
            P delta = (ps[1] - ps[0]).rot90().unit() * eps;
51
            return {ps[0] + delta, ps[1] + delta};
53
        }
   };
54
```

```
56
    #define cross(p1,p2,p3) ((p2.x-p1.x)*(p3.y-p1.y)-(p3.x-p1.x)*(p2.y-p1.y))
    #define crossOp(p1,p2,p3) sign(cross(p1,p2,p3))
57
    字符串
    KMP
          可以尝试从 fail 树的角度理解
    bool kmp(string &s, string &p) {
        int n = p.size();
        vector<int> nex(n + 1);
        for (int i = 1, l = 0; i < n; ++i) {</pre>
            while (l && p[l] != p[i]) {l = nex[l];}
            if (p[l] != p[i]) nex[i] = 0;
            else nex[i] = ++l;
        }
        n = s.size();
        for (int i = 0, now = 0; i < n; ++i) {</pre>
10
11
            while (now \&\& s[i] != p[now]) now = nex[now - 1];
            if (s[i] == p[now]) ++now;
12
13
            if (now == p.size()) return true;
14
15
        return false;
    }
16
    后缀自动机
    struct SuffixAutomaton {
1
        static constexpr int ALPHABET_SIZE = 26;
2
        int N = 1e5;
        struct Node {
            int len;
            int link;
            // int next[ALPHABET_SIZE];
            std::vector<int> next;
            Node() : len(0), link(0), next(ALPHABET_SIZE) {}
10
        };
        std::vector<Node> t;
11
12
        int cntNodes;
        int extend(int p, int c) {
13
14
            if (t[p].next[c]) {
15
                int q = t[p].next[c];
                if (t[q].len == t[p].len + 1)
16
17
                    return q;
                int r = ++cntNodes;
18
                t[r].len = t[p].len + 1;
                t[r].link = t[q].link;
20
                // std::copy(t[q].next, t[q].next + ALPHABET_SIZE, t[r].next);
21
22
                t[r].next = t[q].next;
                t[q].link = r;
23
                while (t[p].next[c] == q) {
                    t[p].next[c] = r;
25
                    p = t[p].link;
26
                }
27
                return r;
28
29
            int cur = ++cntNodes;
30
31
            t[cur].len = t[p].len + 1;
            while (!t[p].next[c]) {
32
33
                t[p].next[c] = cur;
34
                p = t[p].link;
35
36
            t[cur].link = extend(p, c);
            return cur;
37
```

SuffixAutomaton($int N_{-}$): t(2 * N_{-}), N(N_{-}) {

cntNodes = 1;

38

39

40

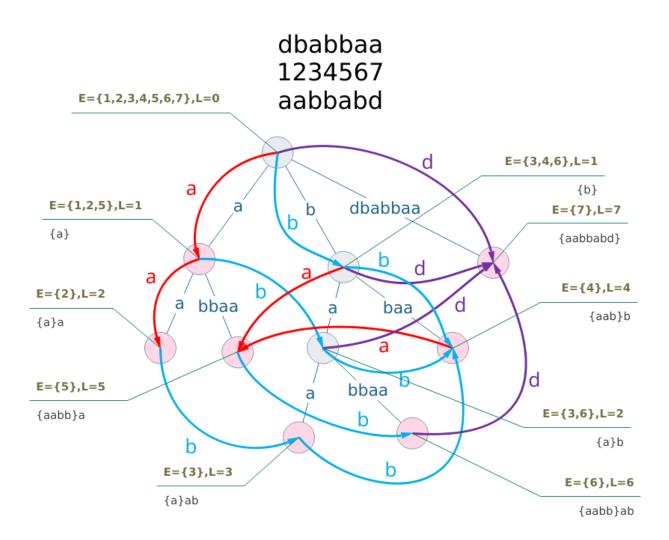


Figure 1: 后缀自动机图解

```
// std::fill(t[0].next, t[0].next + ALPHABET_SIZE, 1);
41
            t[0].next.assign(ALPHABET_SIZE, 1);
42
            t[0].len = -1;
43
        }
44
        SuffixAutomaton(string s): t(2 * s.size()), N(s.size()) {
45
            cntNodes = 1;
46
            t[0].next.assign(ALPHABET_SIZE, 1);
47
            t[0].len = -1;
48
49
50
            int p = 1;
            for (auto ch: s) \{
51
                p = extend(p, ch-'a');
52
53
54
        }
   };
55
   杂项
   STL

    copy

   template <class InputIterator, class OutputIterator>
     OutputIterator copy (InputIterator first, InputIterator last, OutputIterator result);
```