Standard Code Library

FLself

SCUT

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一切的开始

一些宏定义

● 需要 C++11

```
// #define DEBUG
   // #define InTerminal
   // #define std cpp17
   #include<bits/stdc++.h>
   #define int long long
   #define PII std::pair<int, int>
   #define VI std::vector<int>
   #define VPII std::vector<std::pair<int, int> >
   #define VVI std::vector<std::vector<int> >
   #define ALL(a) (a).begin(), (a).end()
   #define SIZ(a) ((int)(a).size())
11
   #define FOR(i, l, r) for (int i = (l); i \le (r); ++i)
   #define REP(i, r, l) for (int i = (r); i \ge (l); --i)
13
   #define lowbit(x) ((x) & (-(x)))
   #define lbpos(x) (__builtin_ctz(x))
15
   #define hbpos(x) (31 - __builtin_clz(x))
16
17
   template<typename S, typename T> std::istream &operator>>(std::istream &is, std::pair<S, T> &pp) { is >> pp.first >>
18

    pp.second; return is; }

   19
    template<typename S, std::size_t _siz> std::istream &operator>>(std::istream &is, std::array<S, _siz> &arr) { for
    template<typename S, std::size_t _siz> std::ostream &operator<<(std::ostream &os, std::array<S, _siz> arr) { os <</pre>
    \textbf{template} < \textbf{typename T} > \textbf{std}:: \textbf{istream \& operator} >> (\textbf{std}:: \textbf{istream \& is, std}:: \textbf{vector} < \textbf{T} > \textbf{\&vec}) ~ \{ \textbf{ for (auto \& x: vec) is } >> \textbf{x; } \}
22

→ return is: }

   template<typename T> std::ostream &operator<<(std::ostream &os, const std::vector<T> &vec) { os << '{'}; for (auto
23
    ⇔ &x: vec) os << x << ", "; return os << "}";}</pre>
   #ifdef std cpp17
24
   template < class Tuple, std::size_t... Is> void print_tuple_impl(std::ostream &os, const Tuple &t,
    ⇔ std::index_sequence<Is...>) { ((os << (Is == 0? "" : ", ") << std::get<Is>(t)), ...); }
   template <class... Args> std::ostream &operator << (std::ostream &os, const std::tuple <Args...> &t) { os << "(";

    print_tuple_impl(os, t, std::index_sequence_for<Args...>{}); return os << ")"; }
</pre>
   #endif
27
   #ifdef DEBUG
   #ifdef InTerminal
29
   #define dbg(x...) do { std::cerr << "\033[32;1m" << #x << " -> "; <math>err(x); } while (0)
   void err() { std::cerr << "\033[39;0m" << std::endl; }</pre>
31
32
   #define dbg(x...) do { std::cerr << \#x << " -> "; err(x); } while (0)
   void err() { std::cerr << std::endl; }</pre>
34
   template<typename T, typename... A>
36
   void err(T a, A... x) { std::cerr << a << ' '; err(x...); }</pre>
37
   #else
38
   #define dbg(...)
39
   #endif
41
42
   using namespace std;
   const int maxn = 2e5 + 3;
43
   const int INF = 0x3f3f3f3f3f3f3f3f3f3f3;
44
   const int mod = 998244353;
   mt19937 RD(time(0));
46
47
48
49
50
   void solv() {
51
52
53
       return ;
54
   }
55
56
   signed main() {
       // freopen("./data.in", "r", stdin);
```

```
std::ios::sync_with_stdio(false), std::cin.tie(0), std::cout.tie(0);
58
59
        int beg__TT = clock();
60
        signed _ttt;
61
62
        cin >> _ttt;
63
        while(_ttt--)
64
65
            solv():
66
        #ifdef DEBUG
67
        std::cerr << "use : " << (clock() - beg__TT) << "ms\n";
68
        #endif
70
        return 0;
   }
71
    数据结构
    ST 表
       一维
    class Sparcetable {
        vector<vector<int> > st;
        int siz;
        bool MX_flg = 0;
        inline int renew(int x, int y) {
            if (MX_flg) return max(x, y);
            return min(x, y);
    public:
        // 注意 bhpos(0) 返回-1
10
        bool (*comp)(int, int);
11
        Sparcetable():siz(maxn) {st.resize(hbpos(maxn - 1) + 1, std::vector<int> (maxn));}
        Sparcetable(const std::vector<int>& a, bool _MX_flg = 1): siz(a.size()), MX_flg(_MX_flg) {
13
14
            int n = a.size();
            st.resize(hbpos(n) + 1, vector < int > (n + 1));
15
            for (int i = 1; i <= n; ++i) st[0][i] = a[i];</pre>
16
            for (int i = 1; i <= hbpos(siz); ++i) {</pre>
17
                 for (int j = 1; j + (1 << i) <= siz + 1; ++j) {
18
19
                     st[i][j] = renew(st[i - 1][j], st[i - 1][j + (1 << (i - 1))]);
                }
20
            }
21
22
        int query(int l, int r) {
23
            int len = hbpos(r - l + 1);
24
            return renew(st[len][l], st[len][r - (1 << len) + 1]);</pre>
25
27
   };
       二维
    int f[10][10][maxn][maxn];
    #define _highbit(x) (31 - __builtin_clz(x))
    inline int calc(int x, int y, int xx, int yy, int p, int q) {
            \max(f[p][q][x][y], f[p][q][xx - (1 << p) + 1][yy - (1 << q) + 1]),
            \max(f[p][q][xx - (1 << p) + 1][y], f[p][q][x][yy - (1 << q) + 1])
        );
   }
8
    void init() {
        for (int x = 0; x <= _highbit(n); ++x)</pre>
10
        for (int y = 0; y <= _highbit(m); ++y)</pre>
11
            for (int i = 0; i \le n - (1 \le x); ++i)
12
            for (int j = 0; j \le m - (1 \le y); ++j) {
13
                 if (!x && !y) { f[x][y][i][j] = a[i][j]; continue; }
14
15
                 f[x][y][i][j] = calc(
16
                     i, j,
                     i + (1 << x) - 1, j + (1 << y) - 1,
17
```

max(x - 1, 0), max(y - 1, 0)

18

);

```
}
20
21
    inline int get_max(int x, int y, int xx, int yy) {
22
23
        return calc(x, y, xx, yy, _highbit(xx - x + 1), _highbit(yy - y + 1));
    Fenwick Tree(树状数组)
       一维
    template<typename T>
1
    class FenwickT {
        int n:
        vector<T> tr;
    public:
5
        FenwickT(int siz): tr(siz), n(siz) {}
        FenwickT(int siz, T ini): tr(siz, ini), n(siz) {}
        void add(int p, T x) {
            for (int i = p; i < n; i += i & (-i)) tr[i] += x;</pre>
10
11
        T query(int p) {
12
            T ret = T(0);
            for (int i = p; i > 0; i -= i & (-i)) ret += tr[i];
13
14
            return ret;
15
16
        T range_sum(int l, int r) {
            return (query(r) - query(l - 1));
17
18
   };
    线段树
    class SegT{
1
        struct Pt{
            int val, ls, rs, sl;
3
            Pt():val(0), ls(0), rs(0), sl(0) {}
            Pt(int v, int l, int r, int s): val(v), ls(l), rs(r), sl(s) {}
            ~Pt() {}
        int renew(int x, int y) {
            return x + y;
10
        int renewsl(int x, int y) {
11
12
            return x + y;
        }
13
14
        int renewqj(int x, int y, int l, int r) {
            return x + y * (r - l + 1);
15
16
    public:
17
        std::vector<Pt> tr;
18
        int cnt = 0; // 结点数目
19
        SegT() {cnt = 1; tr.emplace_back();} // 建一棵空树
20
21
        // 修改
22
23
        void add(int l, int r, int p, int ql, int qr, int x) {
24
            if (ql <= l && r <= qr) {
                tr[p].val = renewqj(tr[p].val, x, l, r);
25
                tr[p].sl = renewsl(tr[p].sl, x);
27
                return;
28
            int mid = l + (r - l) / 2;
29
            if (tr[p].sl) {
30
                if (!tr[p].ls) tr[p].ls = cnt++;
                if (!tr[p].rs) tr[p].rs = cnt++;
32
                if (cnt >= tr.size()) tr.resize(cnt + 1);
33
34
                int ls = tr[p].ls, rs = tr[p].rs;
               tr[ls].val = renewqj(tr[ls].val, tr[p].sl, l, mid), tr[rs].val = renewqj(tr[rs].val, tr[p].sl, mid + 1, r);
35
                tr[ls].sl = renewsl(tr[ls].sl, tr[p].sl), tr[rs].sl = renewsl(tr[rs].sl, tr[p].sl);
                tr[p].sl = 0;
37
            }
```

```
if (ql <= mid) {
39
40
                if (!tr[p].ls) tr[p].ls = cnt++;
                if (cnt >= tr.size()) tr.resize(cnt + 1);
41
42
                add(l, mid, tr[p].ls, ql, qr, x);
43
            if (qr > mid) {
44
                if (!tr[p].rs) tr[p].rs = cnt++;
45
                if (cnt >= tr.size()) tr.resize(cnt + 1);
46
                add(mid + 1, r, tr[p].rs, ql, qr, x);
47
48
            tr[p].val = renew(tr[p].ls? tr[tr[p].ls].val: 0, tr[p].rs? tr[tr[p].rs].val: 0);
49
50
        };
51
52
        int query(int l, int r, int p, int ql, int qr) {
53
            if (ql <= l && r <= qr) return tr[p].val;</pre>
54
            int mid = l + (r - l) / 2;
55
            if (tr[p].sl) {
56
                if (!tr[p].ls) tr[p].ls = cnt++;
                if (!tr[p].rs) tr[p].rs = cnt++;
58
59
                if (cnt >= tr.size()) tr.resize(cnt + 1);
60
                int ls = tr[p].ls, rs = tr[p].rs;
               tr[ls].val = renewqj(tr[ls].val, tr[p].sl, l, mid), tr[rs].val = renewqj(tr[rs].val, tr[p].sl, mid + 1, r);
61
                tr[ls].sl = renewsl(tr[ls].sl, tr[p].sl), tr[rs].sl = renewsl(tr[rs].sl, tr[p].sl);
                tr[p].sl = 0;
63
64
            int ret = 0;
65
            if (ql <= mid) {
66
67
                if (!tr[p].ls) tr[p].ls = cnt++;
                if (cnt >= tr.size()) tr.resize(cnt + 1);
68
                ret = renew(ret, query(l, mid, tr[p].ls, ql, qr));
69
70
            if (qr > mid) {
71
72
                if (!tr[p].rs) tr[p].rs = cnt++;
                if (cnt >= tr.size()) tr.resize(cnt + 1);
73
                ret = renew(ret, query(mid + 1, r, tr[p].rs, ql, qr));
74
75
            tr[p].val = renew(tr[p].ls? tr[tr[p].ls].val: 0, tr[p].rs? tr[tr[p].rs].val: 0);
76
77
            return ret;
78
        };
   };
```

数学

数论

• 数论整数

```
constexpr int P = 998244353;
    // assume -P <= x < 2P
    int norm(int x) {
        // x %= P;
        if (x < 0) \{ x += P; \}
        if (x >= P) \{ x -= P; \}
        return x;
   }
    template<typename E>
    E power(E n, int k) {
10
        E ret = E(1);
11
        while (k) {
12
13
            if (k & 1) ret *= n;
            n \star = n;
            k >>= 1;
15
        } return ret;
16
17
   }
   struct Z {
18
19
        int x;
        Z(int x = 0) : x(norm(x)) {}
20
        int val() const { return x; }
21
        Z operator-() const { return Z(norm(P - x)); }
22
```

```
Z inv() const { assert(x != 0); return power(*this, P - 2); }
23
24
        Z \cdot \text{coperator} = (\text{const } Z \cdot \text{chs}) \{ x = (\text{long long})(x) * \text{rhs.} x \% P; \text{ return } *\text{this}; \}
        Z & operator += (const Z &rhs) { x = norm(x + rhs.x); return *this; }
25
        Z &operator-=(const Z &rhs) { x = norm(x - rhs.x); return *this; }
26
27
        Z &operator/=(const Z &rhs) { return *this *= rhs.inv(); }
        friend Z operator*(const Z &lhs, const Z &rhs) { Z res = lhs; res *= rhs; return res; }
28
        friend Z operator+(const Z &lhs, const Z &rhs) { Z res = lhs; res += rhs; return res;
29
        friend Z operator-(const Z &lhs, const Z &rhs) { Z res = lhs; res -= rhs; return res; }
30
        friend Z operator/(const Z &lhs, const Z &rhs) { Z res = lhs; res /= rhs; return res; }
31
32
        friend std::istream &operator>>(std::istream &is, Z &a) { long long v; is >> v; a = Z(v); return is; }
        friend std::ostream &operator<<(std::ostream &os, const Z &a) { return os << a.val(); }</pre>
33
34
    };
    拉格朗日差值法
    template<typename T>
    T lintp(const vector<int>& x, const vector<T>& y, int k) {
        T ans = 0;
        for (int i = 0; i < x.size(); ++i) {</pre>
4
             if (k == x[i])
5
                 return y[i];
            T u = 1, v = 1;
             for (int j = 0; j < x.size(); ++j) {</pre>
                 if (i == j) continue;
10
                 u *= (k - x[j]);
                 v *= (x[i] - x[j]);
11
             }
12
             ans += y[i] * u / v;
14
        return ans;
    }
16
```

各种筛

筛法	场景	效率
Min-25 筛 PN 筛 杜教筛	$f(p)$ 是一个关于 p 的多项式, $f(p^c)$ 能快速求 找一个好求前缀和的积性函数 $g()$ 在 p 处 $f(p)=g(p)$ 找一个 $g()$ 使得 $f*g()$ 好求前缀和	$\frac{O(\frac{n^{\frac{3}{4}}}{\log n})}{O(\sqrt{n})}$ $O(n^{\frac{2}{3}})$

Min-25 筛

```
namespace Min_25{
1
        bool INI = 0;
        int M = 0, sqn = 0;
        std::vector<int> primes;
        Z (*fp)(int, int); // f(p^c)
        Z fp_single(int p, int c) {
            return power(Z(p), c);
        Z sgp(int n, int c) {
            if (c == 0) return Z(n);
10
            if (c == 1) return Z(n+1) * n / 2;
11
            if (c == 2) return Z(2*n+1) * (n+1) * n / 6;
12
            // if (c == 3) return Z(n) * n * (n+1) * (n+1) / 4;
13
            // if (c == 4) return Z(n) * (n+1) * (2*n+1) * (3*n*n%P + 3*n - 1) / 30;
15
16
        struct Gpoly{
17
            int M, sqn, a;
            std::vector<Z> F_prime1, F_prime2;
18
            Gpoly(int scale, int a, int c): M(scale), a(a) {
19
                sqn = sqrt(M) + 3;
20
                F_prime1.resize(sqn), F_prime2.resize(sqn);
21
22
                int st = M, ed = 1;
23
                for (int i = 1; st >= ed; st = min(M / ++i, st - 1)) {
24
                    (*this)[st] = sgp(st, c) - 1;
25
```

```
26
27
                 for (int j = 1; j < primes.size(); ++j) {</pre>
                     st = M, ed = primes[j] * primes[j];
28
                     for (int i = 1; st >= ed; st = min(M / ++i, st - 1)) {
29
                          (*this)[st] -= fp_single(primes[j], c) * ((*this)[st/primes[j]] - (*this)[primes[j-1]]);
                     }
31
                 }
32
            }
33
            void seta(int aa) {a = aa;}
34
            Z & operator [](int idx) {
                 if (idx < sqn) return F_prime1[idx];</pre>
36
37
                 return F_prime2[M/idx];
            }
38
        };
39
40
        std::vector<Gpoly> Gp;
41
42
        Z G(int x){
            Z res = 0;
43
44
             for (auto &g: Gp) res += g[x] * g.a;
45
            return res;
46
        void init(int scale) {
47
            if (M < scale) INI = 0;</pre>
48
            M = scale, sqn = sqrt(M) + 5;
50
            if (!INI) {
51
52
                 INI = 1;
                 std::vector<signed> vis(sqn);
53
                 primes.resize(1, 1);
                 for (int i = 2; i < sqn; ++i) {</pre>
55
                     if (!vis[i]) primes.push_back(i);
56
                     for (int j = 1; j < primes.size(); ++j) {</pre>
57
                         auto prm = primes[j];
58
59
                          if (prm * i >= sqn) break;
                         vis[i * prm] = 1;
60
                          if (i % prm == 0) break;
61
                     }
62
                 }
63
            }
65
            Gp.clear();
67
            Gp.emplace_back(scale, N, 0);
68
69
            // Gp.emplace_back(scale, a, c); // a*p^c
70
71
        Z seive(int n, int k) {
            Z res = G(n) - G(primes[k-1]);
72
73
             for (int i = k; i < primes.size() && primes[i] * primes[i] <= n; ++i) {</pre>
                 Z fpj = fp(primes[i], 1), fpj1;
74
                 for (int j = 1, pc = primes[i]; pc * primes[i] <= n; ++j, pc *= primes[i], fpj = fpj1) {</pre>
75
                     fpj1 = fp(primes[i], j + 1);
                     res += fpj * seive(n/pc, i + 1) + fpj1;
77
                 }
            }
79
            return res;
80
81
        Z S_f(int n) {
82
            return seive(n, 1) + 1;
84
        void seta(const vector<int>& a) {for (int i = 0; i < Gp.size() && i < a.size(); ++i) Gp[i].seta(a[i]);}</pre>
85
   }
86
    PN 筛 (Powerful Number)
    // f = (q*h); f(p) = q(p) + h(p) [with f(p) = q(p)] -> h[p] = 0.
    namespace PowerfulNumber{
        bool INI = 0;
        std::vector<int> primes;
        std::vector<std::vector<Z> > h;
        int M;
        Z (*fp)(int, int); // f(p^c)
```

```
Z (*gp)(int, int); // g(p^c)
8
9
        Z (*S_g)(int);
                             // preffix sum of g()
10
        // if lack of a formula of h(i, j), you need to set f() and g() beforehand
11
        void init(int scale) {
12
            if (M < scale) INI = 0;</pre>
13
            M = scale;
14
            int n = std::sqrt(M)+10;
15
            if (!INI) {
16
17
                 INI = 1;
                 primes.resize(0):
18
19
                 std::vector<signed> vis(n);
                 for (int i = 2; i < n; ++i) {</pre>
20
                     if (!vis[i]) primes.push_back(i);
21
22
                     for (auto prm: primes) {
                          if (prm * i >= n) break;
23
24
                         vis[i * prm] = 1;
                          if (i % prm == 0) break;
25
                     }
                 }
27
                 h.resize(primes.size(), std::vector<Z>((int)(log2(M))+1));
28
            }
29
30
             // get the function h() (with f() and g() set or with formula of h())
            for (int i = 0; i < h.size(); ++i) {</pre>
32
33
                 int pp = primes[i] * primes[i];
                 if (pp > M) break;
34
                 h[i][0] = 1;
35
                 for (int j = 2; pp <= M && j < h[i].size(); ++j, pp *= primes[i]) {</pre>
                     Z sgh = 0:
37
                     for (int k = 1, xp = primes[i]; k <= j; ++k, xp *= primes[i]) {</pre>
38
39
                         sgh += gp(primes[i], xp) * h[i][j-k];
40
41
                     h[i][j] = fp(pp, j) - sgh;
                     // h[i][j] = Z(j-1) * (pp * primes[i] % P - pp % P);
42
                     // h[i][j] = Z(-pp) / (j * (j-1));
43
                     // [a formula of h(i, j)], better faster than log, this example can be optimized to O(1).
44
                }
45
            }
46
        }
47
48
        // assistance func to get the sum
49
        Z PN_sieve(int n, int flr, Z hd) {
50
51
            Z res = S_g(n)*hd;
            for(int i = flr+1; i < primes.size(); ++i) {</pre>
52
53
                 int prm=primes[i], k=1;
                 int val=n/prm, pk=prm;
54
                 if(val < prm) break;</pre>
56
57
                 while(val >= prm) {
58
                     val /= prm;
                     pk *= prm;
59
                     ++k;
61
62
                     res += PN_sieve(val, i, hd*h[i][k]);
                 }
63
            }
64
65
            return res;
66
        }
        // func to get the sum
67
68
        Z getsumf(int n) {
69
            return PN_sieve(n, -1, 1);
70
   }
71
    杜教筛
    // g(1)S(n) = \sum_{i=1}^{n} (f*g)(i) - \sum_{i=2}^{n} g(i)S(n/i)
    namespace dujiaoshai{
2
        vector<Z> smallS;
        map<int, Z> bigS;
```

```
6
        void Set_smallS(int);
        Z (*S_fg)(int);
        Z (*S_g)(int);
        Z getS(int n) {
             if (n < smallS.size()) return smallS[n];</pre>
10
             else if (bigS.count(n)) return bigS[n];
11
            Z res = S_fg(n);
12
            for (int l = 2, r; l <= n; l = r + 1) {
13
                 r = n / (n / l);
14
                 res -= (S_g(r) - S_g(l-1)) * getS(n/l);
15
16
            // res /= S_g(1);
17
            return (bigS[n] = res);
18
19
        }
   }
20
21
    void dujiaoshai::Set_smallS(int siz) {
22
23
        int n = pow(siz, 0.67);
        smallS.assign(n, 0);
24
        smallS[1] = 1;
25
26
        vector<signed> vis(n), primes;
27
        for (int i = 2; i < n; ++i) {</pre>
            if (!vis[i]) {
28
                 primes.push_back(i);
29
                 smallS[i] = i - 1;
30
31
            for (auto &prm: primes) {
32
                 if (i * prm >= n) break;
                 vis[i * prm] = 1;
34
                 if (i % prm == 0) {
35
                     smallS[i * prm] = smallS[i] * prm;
36
37
                     break;
38
                 }
                 smallS[i * prm] = smallS[i] * (prm - 1);
39
40
            smallS[i] = smallS[i-1] + smallS[i]*i;
41
42
        }
   }
43
    多项式
        • Poly with NTT
   std::vector<int> rev;
    std::vector<Z> roots{0, 1};
    void dft(std::vector<Z> &a) {
3
        int n = a.size();
4
        if ((int)(rev.size()) != n) {
             int k = __builtin_ctz(n) - 1;
            rev.resize(n);
             for (int i = 0; i < n; i++) {</pre>
                 rev[i] = rev[i >> 1] >> 1 | (i & 1) << k;
10
11
12
        }
13
14
        for (int i = 0; i < n; i++) {</pre>
            if (rev[i] < i) {
15
                 std::swap(a[i], a[rev[i]]);
16
            }
17
18
        if ((int)(roots.size()) < n) {</pre>
19
            int k = __builtin_ctz(roots.size());
20
            roots.resize(n);
21
            while ((1 << k) < n)  {
22
                 Z = power(Z(3), (P - 1) >> (k + 1));
23
24
                 for (int i = 1 << (k - 1); i < (1 << k); i++) {
                     roots[2 * i] = roots[i];
25
                     roots[2 * i + 1] = roots[i] * e;
26
27
                 }
```

```
k++;
28
29
            }
30
        for (int k = 1; k < n; k *= 2) {</pre>
31
32
             for (int i = 0; i < n; i += 2 * k) {
                 for (int j = 0; j < k; j++) {
33
                     Z u = a[i + j];
Z v = a[i + j + k] * roots[k + j];
34
35
                      a[i + j] = u + v;
36
                      a[i + j + k] = u - v;
37
                 }
38
             }
39
        }
40
    }
41
    void idft(std::vector<Z> &a) {
42
        int n = a.size();
43
44
        std::reverse(a.begin() + 1, a.end());
        dft(a);
45
46
        Z inv = (1 - P) / n;
        for (int i = 0; i < n; i++) {
47
             a[i] *= inv;
48
49
50
    }
    struct Poly {
        std::vector<Z> a;
52
53
        Poly() {}
        Poly(const std::vector<Z> &a) : a(a) {}
54
        Poly(const std::initializer_list<Z> &a) : a(a) {}
55
        int size() const {
            return a.size();
57
58
        void resize(int n) {
59
             a.resize(n);
60
61
        Z operator[](int idx) const {
62
             if (idx < size()) {</pre>
63
                 return a[idx];
64
65
             } else {
                 return 0;
             }
67
68
        Z & operator[](int idx) {
69
             return a[idx];
70
71
        Poly mulxk(int k) const {
72
73
             auto b = a;
            b.insert(b.begin(), k, 0);
74
75
             return Poly(b);
76
77
        Poly modxk(int k) const {
             k = std::min(k, size());
78
             return Poly(std::vector<Z>(a.begin(), a.begin() + k));
79
        Poly divxk(int k) const {
81
82
             if (size() <= k) {
                 return Poly();
83
84
             return Poly(std::vector<Z>(a.begin() + k, a.end()));
85
86
        friend Poly operator+(const Poly &a, const Poly &b) {
87
88
             std::vector<Z> res(std::max(a.size(), b.size()));
89
             for (int i = 0; i < (int)(res.size()); i++) {</pre>
                 res[i] = a[i] + b[i];
             }
91
92
             return Poly(res);
93
94
        friend Poly operator-(const Poly &a, const Poly &b) {
95
             std::vector<Z> res(std::max(a.size(), b.size()));
             for (int i = 0; i < (int)(res.size()); i++) {</pre>
96
97
                 res[i] = a[i] - b[i];
98
```

```
return Poly(res);
99
100
         friend Poly operator*(Poly a, Poly b) {
101
              if (a.size() == 0 || b.size() == 0) {
102
                  return Poly();
104
              int sz = 1, tot = a.size() + b.size() - 1;
105
              while (sz < tot) {</pre>
106
                  sz *= 2;
107
108
              a.a.resize(sz);
109
110
              b.a.resize(sz);
              dft(a.a);
111
              dft(b.a);
112
              for (int i = 0; i < sz; ++i) {</pre>
113
                  a.a[i] = a[i] * b[i];
114
115
              idft(a.a);
116
117
              a.resize(tot);
118
              return a;
119
120
         friend Poly operator*(Z a, Poly b) {
              for (int i = 0; i < (int)(b.size()); i++) {</pre>
121
                  b[i] *= a;
122
              }
123
              return b;
124
125
         friend Poly operator*(Poly a, Z b) {
126
127
              for (int i = 0; i < (int)(a.size()); i++) {</pre>
                  a[i] *= b;
128
129
130
              return a;
131
132
         Poly & operator += (Poly b) {
              return (*this) = (*this) + b;
133
134
         Poly &operator-=(Poly b) {
135
              return (*this) = (*this) - b;
136
137
         Poly &operator*=(Poly b) {
138
139
              return (*this) = (*this) * b;
140
         Poly deriv() const {
141
142
              if (a.empty()) {
                  return Poly();
143
144
              std::vector<Z> res(size() - 1);
145
146
              for (int i = 0; i < size() - 1; ++i) {</pre>
                  res[i] = (i + 1) * a[i + 1];
147
148
149
              return Poly(res);
150
         Poly integr() const {
              std::vector<Z> res(size() + 1);
152
153
              for (int i = 0; i < size(); ++i) {</pre>
154
                  res[i + 1] = a[i] / (i + 1);
155
156
              return Poly(res);
157
         Poly inv(int m) const {
158
159
              Poly x{a[0].inv()};
              int k = 1;
160
              while (k < m) {
                  k *= 2;
162
163
                  x = (x * (Poly{2} - modxk(k) * x)).modxk(k);
164
165
              return x.modxk(m);
166
         Poly log(int m) const {
167
168
              return (deriv() * inv(m)).integr().modxk(m);
169
```

```
Poly exp(int m) const {
170
171
             Poly x\{1\};
             int k = 1;
172
             while (k < m) {
173
174
                  k *= 2;
                  x = (x * (Poly{1} - x.log(k) + modxk(k))).modxk(k);
175
176
177
             return x.modxk(m);
178
179
         Poly pow(int k, int m) const {
              int i = 0;
180
181
             while (i < size() && a[i].val() == 0) {</pre>
                 i++;
182
183
             if (i == size() || 1LL * i * k >= m) {
184
                  return Poly(std::vector<Z>(m));
185
186
             Z v = a[i];
187
188
             auto f = divxk(i) * v.inv();
             return (f.log(m - i * k) * k).exp(m - i * k).mulxk(i * k) * power(v, k);
189
190
         Poly sqrt(int m) const {
             Poly x{1};
192
             int k = 1;
193
             while (k < m) {
194
                  k \star = 2;
195
                  x = (x + (modxk(k) * x.inv(k)).modxk(k)) * ((P + 1) / 2);
196
197
198
             return x.modxk(m);
199
         Poly mulT(Poly b) const {
200
             if (b.size() == 0) {
201
                  return Poly();
202
             int n = b.size();
204
             std::reverse(b.a.begin(), b.a.end());
205
             return ((*this) * b).divxk(n - 1);
206
207
208
         std::vector<Z> eval(std::vector<Z> x) const {
             if (size() == 0) {
209
210
                  return std::vector<Z>(x.size(), 0);
211
             const int n = std::max((int)(x.size()), size());
212
213
             std::vector<Poly> q(4 * n);
             std::vector<Z> ans(x.size());
214
215
             x.resize(n);
             std::function<void(int, int, int)> build = [&](int p, int l, int r) {
216
217
                  if (r - l == 1) {
                      q[p] = Poly{1, -x[l]};
218
                  } else {
219
                      int m = (l + r) / 2;
                      build(2 * p, l, m);
221
                      build(2 * p + 1, m, r);
222
                      q[p] = q[2 * p] * q[2 * p + 1];
223
                  }
224
225
             };
             build(1, 0, n);
226
             std::function<void(int, int, int, const Poly &)> work = [&](int p, int l, int r, const Poly &num) {
227
                  if (r - l == 1) {
228
                      if (l < (int)(ans.size())) {
229
230
                           ans[l] = num[0];
                      }
231
                  } else {
232
                      int m = (l + r) / 2;
233
234
                      work(2 * p, l, m, num.mulT(q[2 * p + 1]).modxk(m - l));
                      work(2 \ * \ p \ + \ 1, \ m, \ r, \ num.mulT(q[2 \ * \ p]).modxk(r \ - \ m));
235
236
237
             };
             work(1, 0, n, mulT(q[1].inv(n)));
238
             return ans;
239
         }
240
```

```
};
241
        • FFT
    namespace FFT { // n_ 是初始的数组长度,不一定为 2 的幂次; n 是 init 之后的长度,保证为 2 的幂次长度
         const double PI = acos(-1);
         int rev[1 << 20];</pre>
         int init(int n_) {
             int step = 0, n = 1;
             for (; n < n_; n <<= 1) ++step;</pre>
             for (int i = 1; i < n; ++i) {</pre>
                 rev[i] = (rev[i >> 1] >> 1) | ((i & 1) << (step - 1));
             }
             return n;
10
11
         void FFT(complex<double> a[], int n, int f) {
12
             for (int i = 0; i < n; ++i) {
13
                 if (i < rev[i]) std::swap(a[i], a[rev[i]]);</pre>
14
15
             for (int h = 2; h <= n; h <<= 1) {
                 complex<double> wn(cos(f * 2 * PI / h), sin(f * 2 * PI / h));
17
                 for (int i = 0; i < n; i += h) {</pre>
18
                      complex<double> w(1, 0), u;
19
                      for (int j = i, k = h >> 1; j < i + k; ++j) {
20
                          u = a[j + k] * w;
                          a[j + k] = a[j] - u;
22
23
                          a[j] = a[j] + u;
                          w = w * wn;
24
                     }
25
                 }
27
             if (f == -1) {
28
                 for (int i = 0; i < n; ++i) {</pre>
29
                     a[i] = {a[i].real() / n, 0};
30
                 }
31
             }
32
33
         void conv(complex<double> a[], complex<double> b[], int n_) { // n_ does not represent the pow of 2.
34
             int n = init(n_);
35
36
             FFT(a, n, 1);
37
             FFT(b, n, 1);
             for (int i = 0; i < n; ++i) a[i] *= b[i];</pre>
             FFT(a, n, -1);
39
    }
```

类欧几里得

- $m = \lfloor \frac{an+b}{c} \rfloor$.
- $f(a,b,c,n) = \sum_{i=0}^{n} \lfloor \frac{ai+b}{c} \rfloor$: 当 $a \geq c$ or $b \geq c$ 时, $f(a,b,c,n) = (\frac{a}{c})n(n+1)/2 + (\frac{b}{c})(n+1) + f(a \bmod c, b \bmod c, c, n)$; 否则 f(a,b,c,n) = nm f(c,c-b-1,a,m-1)。
- $g(a,b,c,n) = \sum_{i=0}^{n} i \lfloor \frac{ai+b}{c} \rfloor$: 当 $a \geq c$ or $b \geq c$ 时, $g(a,b,c,n) = (\frac{a}{c})n(n+1)(2n+1)/6 + (\frac{b}{c})n(n+1)/2 + g(a \mod c,b \mod c,c,n)$; 否则 $g(a,b,c,n) = \frac{1}{2}(n(n+1)m-f(c,c-b-1,a,m-1)-h(c,c-b-1,a,m-1))$ 。
- $h(a,b,c,n) = \sum_{i=0}^n \lfloor \frac{ai+b}{c} \rfloor^2$: 当 $a \geq c$ or $b \geq c$ 时, $h(a,b,c,n) = (\frac{a}{c})^2 n(n+1)(2n+1)/6 + (\frac{b}{c})^2 (n+1) + (\frac{a}{c})(\frac{b}{c})n(n+1) + h(a \bmod c, b \bmod c, c, n) + 2(\frac{a}{c})g(a \bmod c, b \bmod c, c, n) + 2(\frac{b}{c})f(a \bmod c, b \bmod c, c, n)$;否则 h(a,b,c,n) = nm(m+1) 2g(c,c-b-1,a,m-1) 2f(c,c-b-1,a,m-1) f(a,b,c,n)。

图论

LCA

● 倍增

```
void dfs(int u, int fa) {
    pa[u][0] = fa; dep[u] = dep[fa] + 1;
    FOR (i, 1, SP) pa[u][i] = pa[pa[u][i - 1]][i - 1];
    for (int& v: G[u]) {
```

```
if (v == fa) continue;
6
             dfs(v, u);
   }
    int lca(int u, int v) {
10
        if (dep[u] < dep[v]) swap(u, v);</pre>
11
        int t = dep[u] - dep[v];
12
        FOR (i, 0, SP) if (t & (1 << i)) u = pa[u][i];
13
        FORD (i, SP - 1, -1) {
14
             int uu = pa[u][i], vv = pa[v][i];
15
16
             if (uu != vv) { u = uu; v = vv; }
17
        return u == v ? u : pa[u][0];
18
    }
19
```

计算几何

二维几何: 点与向量

```
#define y1 yy1
1
    #define nxt(i) ((i + 1) % s.size())
    typedef double LD;
    const LD PI = 3.14159265358979323846;
    const LD eps = 1E-10;
    int sgn(LD x) \{ return fabs(x) < eps ? 0 : (x > 0 ? 1 : -1); \}
    struct L;
    struct P:
    typedef P V;
    struct P {
10
11
        LD x, y;
        explicit P(LD x = 0, LD y = 0): x(x), y(y) {}
12
        explicit P(const L& l);
13
14
    struct L {
15
16
        Ps, t;
        L() {}
17
        L(P s, P t): s(s), t(t) {}
18
19
20
    P operator + (const P& a, const P& b) { return P(a.x + b.x, a.y + b.y); }
21
    P operator - (const P& a, const P& b) { return P(a.x - b.x, a.y - b.y); }
22
    P operator * (const P& a, LD k) { return P(a.x * k, a.y * k); }
23
24
    P operator / (const P& a, LD k) { return P(a.x / k, a.y / k); }
    inline bool operator < (const P& a, const P& b) {</pre>
25
        return sgn(a.x - b.x) < 0 \mid \mid (sgn(a.x - b.x) == 0 && sgn(a.y - b.y) < 0);
26
27
    bool operator == (const P& a, const P& b) { return |sgn(a.x - b.x) && |sgn(a.y - b.y); }
29
    P::P(const L& l) { *this = l.t - l.s; }
    ostream &operator << (ostream &os, const P &p) {
30
        return (os << "(" << p.x << "," << p.y << ")");
31
32
33
    istream &operator >> (istream &is, P &p) {
34
        return (is >> p.x >> p.y);
35
    }
36
    LD dist(const P& p) { return sqrt(p.x * p.x + p.y * p.y); }
37
    LD dot(const V& a, const V& b) { return a.x * b.x + a.y * b.y; }
    LD det(const V& a, const V& b) { return a.x * b.y - a.y * b.x; }
    LD cross(const P& s, const P& t, const P& o = P()) { return det(s - o, t - o); }
    // ---
```

字符串

KMP

可以尝试从 fail 树的角度理解

```
bool kmp(string &s, string &p) {
    int n = p.size();
    vector<int> nex(n + 1);

for (int i = 1, l = 0; i < n; ++i) {
        while (l && p[l] != p[i]) {l = nex[l];}
        if (p[l] != p[i]) nex[i] = 0;
        else nex[i] = ++l;

    }

n = s.size();
for (int i = 0, now = 0; i < n; ++i) {
    while (now && s[i] != p[now]) now = nex[now - 1];
    if (s[i] == p[now]) ++now;
    if (now == p.size()) return true;
}

return false;
}</pre>
```

后缀自动机

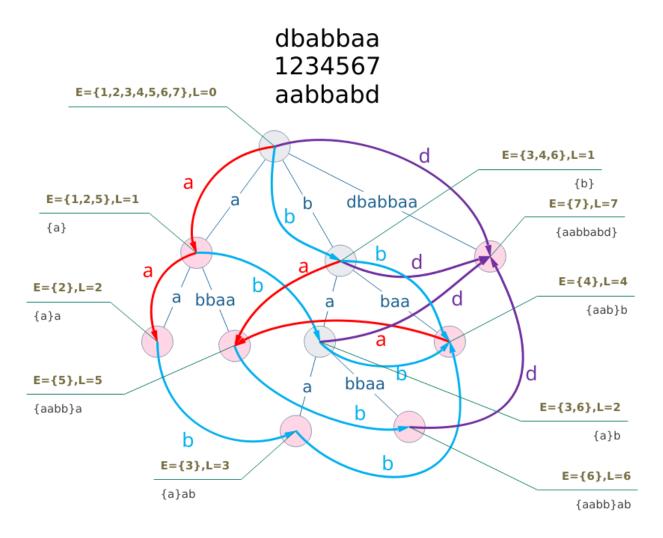


Figure 1: 后缀自动机图解

```
struct SuffixAutomaton {
static constexpr int ALPHABET_SIZE = 26;
int N = 1e5;
struct Node {
int len;
int link;
// int next[ALPHABET_SIZE];
```

```
std::vector<int> next;
8
            Node() : len(0), link(0), next(ALPHABET_SIZE) {}
        };
10
        std::vector<Node> t;
11
12
        int cntNodes;
        int extend(int p, int c) {
13
14
             if (t[p].next[c]) {
                 int q = t[p].next[c];
15
                 if (t[q].len == t[p].len + 1)
16
17
                     return q;
                 int r = ++cntNodes;
18
19
                 t[r].len = t[p].len + 1;
                 t[r].link = t[q].link;
20
                 // std::copy(t[q].next, t[q].next + ALPHABET_SIZE, t[r].next);
21
                 t[r].next = t[q].next;
22
                 t[q].link = r;
23
24
                 while (t[p].next[c] == q) {
                     t[p].next[c] = r;
25
26
                     p = t[p].link;
                 }
27
                 return r;
28
29
            int cur = ++cntNodes;
30
            t[cur].len = t[p].len + 1;
            while (!t[p].next[c]) {
32
33
                 t[p].next[c] = cur;
34
                 p = t[p].link;
35
36
            t[cur].link = extend(p, c);
            return cur;
37
38
        SuffixAutomaton(int N_{-}): t(2 * N_{-}), N(N_{-}) {
39
            cntNodes = 1;
40
            // std::fill(t[0].next, t[0].next + ALPHABET_SIZE, 1);
41
            t[0].next.assign(ALPHABET_SIZE, 1);
42
43
            t[0].len = -1;
44
        SuffixAutomaton(string s): t(2 * s.size()), N(s.size()) {
45
46
            cntNodes = 1;
            t[0].next.assign(ALPHABET_SIZE, 1);
47
48
            t[0].len = -1;
49
            int p = 1;
50
51
            for (auto ch: s) {
                 p = extend(p, ch-'a');
52
53
54
    };
    杂项
    STL

    copy

    template <class InputIterator, class OutputIterator>
      OutputIterator copy (InputIterator first, InputIterator last, OutputIterator result);
```