Standard Code Library

FLself

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Contents

一切的开始

一些宏定义

● 需要 C++11

```
// #define DEBUG
   // #define InTerminal
   // #define std_cpp17
   #include<bits/stdc++.h>
   #define int long long
   #define PII std::pair<int, int>
    #define VI std::vector<int>
   #define VPII std::vector<std::pair<int, int> >
   #define VVI std::vector<std::vector<int> >
   #define ALL(a) (a).begin(), (a).end()
   #define SIZ(a) ((int)(a).size())
11
    #define FOR(i, l, r) for (int i = (l); i \le (r); ++i)
   #define REP(i, r, l) for (int i = (r); i \ge (l); --i)
13
   #define lowbit(x) ((x) & (-(x)))
   #define lbpos(x) (__builtin_ctz(x))
15
   #define hbpos(x) (31 - \_builtin\_clz(x))
16
17
    template<typename S, typename T> std::istream &operator>>(std::istream &is, std::pair<S, T> &pp) { is >> pp.first >>
18
     → pp.second; return is; }
    \textbf{template} < \textbf{typename S}, \ \textbf{typename T} > \ \textbf{std}:: ostream \ \& \textbf{operator} <<( \textbf{std}:: ostream \ \& \textbf{os}, \ \textbf{std}:: pair <S, \ T> \ pp) \ \{ \ os \ << \ "(" << \ \textbf{os}, \ \textbf{os}) \} 
19
    template<typename S, std::size_t _siz> std::istream &operator>>(std::istream &is, std::array<S, _siz> &arr) { for
    template<typename S, std::size_t _siz> std::ostream &operator<<(std::ostream &os, std::array<S, _siz> arr) { os <</pre>
    template<typename T> std::istream &operator>>(std::istream &is, std::vector<T> &vec) { for (auto &x: vec) is >> x;
22

→ return is: }

    template<typename T> std::ostream &operator<<(std::ostream &os, const std::vector<T> &vec) { os << '{'}; for (auto
23
    ⇔ &x: vec) os << x << ", "; return os << "}";}</pre>
    #ifdef std cpp17
24
    template < class Tuple, std::size_t... Is> void print_tuple_impl(std::ostream &os, const Tuple &t,
    \leftrightarrow std::index_sequence<Is...>) { ((os << (Is == 0? "" : ", ") << std::get<Is>(t)), ...); }
    template<class... Args> std::ostream &operator<<(std::ostream &os, const std::tuple<Args...> &t) { os << "(";</pre>
    → print_tuple_impl(os, t, std::index_sequence_for<Args...>{}); return os << ")"; }</pre>
    #endif
27
    #ifdef DEBUG
   #ifdef InTerminal
29
    #define dbg(x...) do { std::cerr << "\033[32;1m" << #x << " -> "; <math>err(x); } while (0)
   void err() { std::cerr << "\033[39;0m" << std::endl; }</pre>
31
32
    #define dbg(x...) do { std::cerr << \#x << " -> "; err(x); } while (0)
   void err() { std::cerr << std::endl; }</pre>
34
    template<typename T, typename... A>
36
    void err(T a, A... x) { std::cerr << a << ' '; err(x...); }</pre>
37
    #else
38
    #define dbg(...)
39
    #endif
41
42
    using namespace std;
    const int maxn = 2e5 + 3:
43
    const int INF = 0x3f3f3f3f3f3f3f3f3f3f3;
44
    const int mod = 998244353;
   mt19937 RD(time(0));
46
47
48
   void solv() {
49
50
51
        return ;
52
53
   }
54
55
    signed main() {
        // freopen("./data.in", "r", stdin);
56
        std::ios::sync_with_stdio(false), std::cin.tie(0), std::cout.tie(0);
```

```
int beg__TT = clock();
58
59
         signed _ttt;
60
61
         cin >> _ttt;
62
        while(_ttt--)
63
             solv();
64
65
        #ifdef DEBUG
66
         std::cerr << "use : " << (clock() - beg__TT) << "ms\n";
67
         #endif
68
69
         return 0;
70
    }
```

数据结构

ST 表

一维 class Sparcetable { vector<vector<int> > st; int siz; bool MX_flg = 0; inline int renew(int x, int y) { if (MX_flg) return max(x, y); return min(x, y); public: // 注意 bhpos(0) 返回-1 10 11 bool (*comp)(int, int); Sparcetable():siz(maxn) {st.resize(hbpos(maxn - 1) + 1, std::vector<int> (maxn));} 12 Sparcetable(const std::vector<int>& a, bool _MX_flg = 1): siz(a.size()), MX_flg(_MX_flg) { 13 14 int n = a.size(); st.resize(hbpos(n) + 1, vector<int> (n + 1)); 15 for (int i = 1; i <= n; ++i) st[0][i] = a[i];</pre> 16 for (int i = 1; i <= hbpos(siz); ++i) {</pre> 17 for (int j = 1; j + (1 << i) <= siz + 1; ++j) { 18 st[i][j] = renew(st[i - 1][j], st[i - 1][j + (1 << (i - 1))]);19 20 } } 21 22 int query(int l, int r) { 23 int len = hbpos(r - l + 1); 24 return renew(st[len][l], st[len][r - (1 << len) + 1]);</pre> 25 26 }; 27 28 二维 int f[10][10][maxn][maxn]; #define $_$ highbit(x) (31 - $_$ _builtin $_$ clz(x)) inline int calc(int x, int y, int xx, int yy, int p, int q) { $\max(f[p][q][x][y], f[p][q][xx - (1 << p) + 1][yy - (1 << q) + 1]),$ $\max(f[p][q][xx - (1 << p) + 1][y], f[p][q][x][yy - (1 << q) + 1])$); } 8 void init() { for (int x = 0; x <= _highbit(n); ++x)</pre> 10 for (int y = 0; y <= _highbit(m); ++y)</pre> 11 for (int i = 0; $i \le n - (1 \le x)$; ++i) 12 for (int j = 0; j <= m - (1 << y); ++j) { 13 if (!x && !y) { f[x][y][i][j] = a[i][j]; continue; } 14 15 f[x][y][i][j] = calc(16 i, j, i + (1 << x) - 1, j + (1 << y) - 1,17 max(x - 1, 0), max(y - 1, 0)18);

```
}
20
21
    inline int get_max(int x, int y, int xx, int yy) {
22
        return calc(x, y, xx, yy, _highbit(xx - x + 1), _highbit(yy - y + 1));
23
    Fenwick Tree(树状数组)
        一维
    template<typename T>
1
    class FenwickT {
        int n:
        vector<T> tr;
    public:
5
        FenwickT(int siz): tr(siz), n(siz) {}
        FenwickT(int siz, T ini): tr(siz, ini), n(siz) {}
        void add(int p, T x) {
8
            for (int i = p; i < n; i += i & (-i)) tr[i] += x;</pre>
10
        T query(int p) {
11
12
            T ret = T(0);
            for (int i = p; i > 0; i -= i & (-i)) ret += tr[i];
13
14
            return ret;
15
16
        T range_sum(int l, int r) {
            return (query(r) - query(l - 1));
17
18
        int kth(T k) {
19
            int x = 0;
20
21
            for (int i = 1 << std::__lg(n); i; i /= 2) {</pre>
                if (x + i <= n && k >= a[x + i - 1]) {
22
                    x += i;
23
                     k = a[x - 1];
24
                }
25
26
            }
            return x;
27
28
    };
29
    并查集
    class DSU {
1
2
        std::vector<int> fa, siz;
    public:
3
4
        DSU(int n): fa(n), siz(n, 1) {std::iota(fa.begin(), fa.end(), 0);}
        int findfa(int x) {
            int rt = x;
            while (rt != fa[rt]) rt = fa[rt];
            for (int i = x; i != rt; i = x) {
                siz[i] -= siz[x];
                x = fa[i], fa[i] = rt;
10
            }
11
            return rt;
12
13
14
        bool merge(int x, int y) {
            x = findfa(x), y = findfa(y);
15
            if (x == y) return false;
17
            if (siz[x] > siz[y])
                fa[y] = x, siz[x] += siz[y];
18
19
            else
                fa[x] = y, siz[y] += siz[x];
20
            return true;
22
        bool same(int x, int y) { return findfa(x) == findfa(y); }
23
24
        int size(int x) { return siz[findfa(x)]; }
    };
25
```

带权并查集

```
class DSU {
1
        std::vector<int> fa, siz;
2
        std::vector<int> tag;
    public:
        DSU(int n): fa(n), siz(n, 1), tag(n, 0) {std::iota(fa.begin(), fa.end(), 0);}
        int findfa(int x) {
            int rt = x, tg = tag[x];
            while (rt != fa[rt]) rt = fa[rt], tg ^= tag[rt];
            for (int i = x; i != rt; i = x) {
                siz[i] -= siz[x];
                x = fa[i], fa[i] = rt;
11
                // std::swap(tg, tag[i]); tg ^= tag[i];
12
                tg ^= tag[i] ^= tg ^= tag[i] ^= tg;
13
14
15
            return rt;
16
        bool merge(int x, int y, int tg = 0) {
17
            if (findfa(x) == findfa(y)) {
18
                if ((tag[x] ^ tag[y]) != tg) return false;
                return true;
20
21
            tg ^= tag[x] ^ tag[y];
22
            x = findfa(x), y = findfa(y);
23
            if (siz[x] > siz[y])
24
                fa[y] = x, siz[x] += siz[y], tag[y] = tg;
25
26
                fa[x] = y, siz[y] += siz[x], tag[x] = tg;
27
            return true:
28
        bool same(int x, int y) { return findfa(x) == findfa(y); }
30
        int size(int x) { return siz[findfa(x)]; }
31
32
   };
33
    线段树
    class SegT{
1
        struct Pt{
2
            int val, ls, rs, sl;
            Pt():val(0), ls(0), rs(0), sl(0) \{ \}
            Pt(int v, int l, int r, int s): val(v), ls(l), rs(r), sl(s) {}
5
            ~Pt() {}
        };
        int renew(int x, int y) {
            return x + y;
10
        int renewsl(int x, int y) {
11
12
            return x + y;
13
        int renewqj(int x, int y, int l, int r) {
14
            return x + y * (r - l + 1);
15
16
    public:
17
18
        std::vector<Pt> tr;
        int cnt = 0; // 结点数目
19
        SegT() {cnt = 1; tr.emplace_back();} // 建一棵空树
20
21
22
        void add(int l, int r, int p, int ql, int qr, int x) {
23
            if (ql <= l && r <= qr) {</pre>
24
25
                tr[p].val = renewqj(tr[p].val, x, l, r);
                tr[p].sl = renewsl(tr[p].sl, x);
26
27
                return;
28
            int mid = l + (r - l) / 2;
29
30
            if (tr[p].sl) {
                if (!tr[p].ls) tr[p].ls = cnt++;
31
                if (!tr[p].rs) tr[p].rs = cnt++;
32
33
                if (cnt >= tr.size()) tr.resize(cnt + 1);
```

```
int ls = tr[p].ls, rs = tr[p].rs;
34
35
                tr[ls].val = renewqj(tr[ls].val, tr[p].sl, l, mid), tr[rs].val = renewqj(tr[rs].val, tr[p].sl, mid + 1, r);
                 tr[ls].sl = renewsl(tr[ls].sl, tr[p].sl), tr[rs].sl = renewsl(tr[rs].sl, tr[p].sl);
36
37
                 tr[p].sl = 0;
             if (ql <= mid) {
39
                 if (!tr[p].ls) tr[p].ls = cnt++;
40
                 if (cnt >= tr.size()) tr.resize(cnt + 1);
41
                 add(l, mid, tr[p].ls, ql, qr, x);
42
43
             if (qr > mid) {
44
45
                 if (!tr[p].rs) tr[p].rs = cnt++;
46
                 if (cnt >= tr.size()) tr.resize(cnt + 1);
                 add(mid + 1, r, tr[p].rs, ql, qr, x);
47
48
             tr[p].val = renew(tr[p].ls? tr[tr[p].ls].val: 0, tr[p].rs? tr[tr[p].rs].val: 0);
49
50
         };
51
52
         // 查询
         int query(int l, int r, int p, int ql, int qr) {
53
             if (ql <= l && r <= qr) return tr[p].val;</pre>
54
             int mid = l + (r - l) / 2;
55
             if (tr[p].sl) {
56
                 if (!tr[p].ls) tr[p].ls = cnt++;
                 if (!tr[p].rs) tr[p].rs = cnt++;
58
59
                 if (cnt >= tr.size()) tr.resize(cnt + 1);
60
                 int ls = tr[p].ls, rs = tr[p].rs;
                tr[ls].val = renewqj(tr[ls].val, tr[p].sl, l, mid), tr[rs].val = renewqj(tr[rs].val, tr[p].sl, mid + 1, r);
61
                 tr[ls].sl = renewsl(tr[ls].sl, tr[p].sl), tr[rs].sl = renewsl(tr[rs].sl, tr[p].sl);
62
                 tr[p].sl = 0;
63
64
             int ret = 0;
65
             if (ql <= mid) {
66
67
                 if (!tr[p].ls) tr[p].ls = cnt++;
                 if (cnt >= tr.size()) tr.resize(cnt + 1);
68
                 ret = renew(ret, query(l, mid, tr[p].ls, ql, qr));
69
70
             if (qr > mid) {
71
72
                 if (!tr[p].rs) tr[p].rs = cnt++;
                 if (cnt >= tr.size()) tr.resize(cnt + 1);
73
74
                 ret = renew(ret, query(mid + 1, r, tr[p].rs, ql, qr));
75
             tr[p].val = renew(tr[p].ls? tr[tr[p].ls].val: 0, tr[p].rs? tr[tr[p].rs].val: 0);
76
77
             return ret;
78
        };
79
    };
80
81
    // 静态线段树
82
    template<class Info,
         class Merge = std::plus<Info> >
83
    struct SegmentTree {
84
        const int n;
85
         const Merge merge;
         std::vector<Info> info;
87
         SegmentTree(int n) : n(n), merge(Merge()), info(4 << std::__lg(n)) {}
88
89
         SegmentTree(std::vector<Info> init) : SegmentTree(init.size()) {
             std::function<void(int, int, int)> build = [&](int p, int l, int r) {
90
                 if (r - l == 1) {
91
92
                     info[p] = init[l];
93
                     return;
94
                 }
                 int m = (l + r) / 2;
95
                 build(2 * p, l, m);
                 build(2 * p + 1, m, r);
97
98
                 pull(p);
99
             }:
             build(1, 0, n);
100
101
         void pull(int p) {
102
             info[p] = merge(info[2 * p], info[2 * p + 1]);
103
104
```

```
void modify(int p, int l, int r, int x, const Info &v) {
105
106
            if (r - l == 1) {
                 info[p] = v;
107
                 return;
108
            int m = (l + r) / 2;
110
            if (x < m) {
111
                 modify(2 * p, l, m, x, v);
112
            } else {
113
114
                 modify(2 * p + 1, m, r, x, v);
115
116
            pull(p);
117
        void modify(int p, const Info &v) {
118
119
            modify(1, 0, n, p, v);
120
121
        Info rangeQuery(int p, int l, int r, int x, int y) {
            if (l >= y || r <= x) {
122
123
                 return Info();
124
            if (l >= x && r <= y) {
125
126
                 return info[p];
127
            int m = (l + r) / 2;
128
            return merge(rangeQuery(2 \star p, l, m, x, y), rangeQuery(2 \star p + 1, m, r, x, y));
129
130
131
        Info rangeQuery(int l, int r) {
            return rangeQuery(1, 0, n, l, r);
132
133
    };
134
    吉如一线段树
    区间赋值、区间取 min, 求和、求最大值、求历史最大值
    namespace JRY_SegT{
        // namespace JRY_SegT
2
        // O(n log n) luogu n,m 5e5 max1.62s
        using i64 = long long;
        5
        struct Info {
            i64 sum,mx,smx,hmx,cnt;
            Info(i64 sum=0,i64 mx=-INF,i64 smx=-INF,i64 hmx=-INF,i64 cnt=0)
                 : sum(sum), mx(mx), smx(smx), hmx(hmx), cnt(cnt) {}
10
        };
        Info merge(Info x,Info y) {
11
            Info r;
12
            r.sum = x.sum + y.sum;
13
            r.mx = std::max(x.mx, y.mx);
14
            r.hmx = std::max(x.hmx, y.hmx);
15
16
            if(x.mx == y.mx) r.smx = std::max(x.smx, y.smx), r.cnt = x.cnt + y.cnt;
            else if(x.mx > y.mx) r.smx = std::max(x.smx, y.mx), r.cnt = x.cnt;
17
18
            else r.smx = std::max(x.mx, y.smx), r.cnt = y.cnt;
            return r;
19
20
        struct Tag {
21
            i64 lzm,lzo,hlzm,hlzo;
22
23
            Tag() : lzm(0), lzo(0), hlzm(0), hlzo(0) {}
            void clear() {
24
                 lzm = lzo = hlzm = hlzo = 0;
25
26
27
            bool is0() {
                 return lzm == 0 && lzo == 0 && hlzm == 0 && hlzo == 0;
28
29
30
        };
        struct SegT {
31
            int n;
32
33
            std::vector<Info> t;
            std::vector<Tag> z;
34
35
            std::vector<int> le,ri;
            SegT(int n,const std::vector<i64>&a) : n(n), t(4*n), z(4*n), le(4*n), ri(4*n) {
```

```
build(1,0,n,a);
37
38
             void build(int p,int l,int r,const std::vector<i64>&a) {
39
                  le[p] = l, ri[p] = r;
40
41
                  if(r - l == 1) {
                      t[p] = Info(a[l],a[l],-INF,a[l],1);
42
43
44
                  int mid = l + r >> 1;
45
                  build(p << 1, l, mid, a);
46
                  build(p << 1 | 1, mid, r, a);
47
48
                  pull(p);
49
             void pull(int p) {
50
51
                  t[p] = merge(t[p << 1], t[p << 1 | 1]);
52
53
             void update(int p,i64 lzm,i64 lzo,i64 hlzm,i64 hlzo) {
                  t[p].sum += lzm * t[p].cnt + (ri[p] - le[p] - t[p].cnt) * lzo;
54
55
                  t[p].hmx = std::max(t[p].hmx, t[p].mx + hlzm);
                  t[p].mx += lzm;
56
57
                  if(t[p].smx != -INF) t[p].smx += lzo;
58
                  z[p].hlzm = std::max(z[p].hlzm, z[p].lzm + hlzm), z[p].lzm += lzm;
59
                  z[p].hlzo = std::max(z[p].hlzo, z[p].lzo + hlzo), z[p].lzo += lzo;
             void pushdown(int p) {
61
                  if(z[p].is0()) return;
62
                  int mx = std::max(t[p << 1].mx, t[p << 1 | 1].mx);</pre>
63
                  for(auto ps : {p << 1, p << 1 | 1}) {
64
                      if(t[ps].mx == mx) update(ps, z[p].lzm, z[p].lzo, z[p].hlzm, z[p].hlzo);
65
                      else update(ps, z[p].lzo, z[p].lzo, z[p].hlzo, z[p].hlzo);
66
                  }
67
68
                  z[p].clear();
             }
69
70
             void range_add(int p,int L,int R,i64 v) {
                  if(ri[p] <= L || R <= le[p]) return;
71
                  if(L <= le[p] && ri[p] <= R) {
72
                      update(p,v,v,v,v);
73
                      return;
74
75
                  pushdown(p);
76
77
                  range_add(p << 1, L, R, v);
                  range_add(p \ll 1 | 1, L, R, v);
78
                  pull(p);
79
80
             void range_min(int p,int L,int R,i64 v) {
81
82
                  if(ri[p] <= L || R <= le[p] || t[p].mx <= v) return;</pre>
                  if(L <= le[p] && ri[p] <= R && t[p].smx < v) {</pre>
83
84
                      update(p, v - t[p].mx, \theta, v - t[p].mx, \theta);
85
                      return;
86
87
                  pushdown(p);
                  range_min(p << 1, L, R, v);
88
                  range_min(p \ll 1 | 1, L, R, v);
                  pull(p);
90
91
             i64 query_sum(int p,int L,int R) {
92
                  if(ri[p] <= L || R <= le[p]) return Oll;</pre>
93
                  if(L <= le[p] && ri[p] <= R) return t[p].sum;</pre>
94
95
                  pushdown(p):
96
                  return query_sum(p << 1, L, R) + query_sum(p << 1 | 1, L, R);</pre>
97
             i64 query_mx(int p,int L,int R) {
98
                  if(ri[p] <= L || R <= le[p]) return -INF;</pre>
                  if(L <= le[p] && ri[p] <= R) return t[p].mx;</pre>
100
101
                  pushdown(p);
                  return std::max(query_mx(p \iff 1, L, R), query_mx(p \iff 1 | 1, L, R));
102
103
             i64 query_hmx(int p,int L,int R) {
104
                  if(ri[p] <= L || R <= le[p]) return -INF;</pre>
105
                  if(L <= le[p] && ri[p] <= R) return t[p].hmx;</pre>
                  pushdown(p);
107
```

主席树

57

可持久化线段树, 感觉主要是利用单点 \log 次的性质以及离散化的思路. 比如区间第 k 小就是构造 n 个线段树 (每多加一个实际上只多加了 \log 个点), 然后再用离散化的点 (实际上就是其排名值) 找到前缀和之差为 k(此时为第 k 小,可以这样想: 第 r 棵树的 r 个点中包含了第 l-1 棵树的 l-1 个点, 减掉那些点, 剩下的就是区间 [l,r] 的点, 然后找第 k 个) 的点. 用离线不那么方便. 代码暂时先留空了...

```
// 主席树
   // 对权值建立可持久化线段树, 再二分一样求区间第 k 大
   struct HJTtr {
        std::vector<int> ls, rs, rt;
        std::vector<int> ind, sum;
5
        int tot, _n;
        int getid(const int% val) {
            return std::lower_bound(ind.begin(), ind.end(), val) - ind.begin();
        int build(int l, int r) {
10
11
            int root = tot++;
            sum[root] = 0;
12
            if (l == r) return root;
            int mid = l + (r - l) / 2;
14
15
            ls[root] = build(l, mid);
            rs[root] = build(mid + 1, r);
16
17
            return root;
18
        int update(int k, int x = 1) {
19
            auto upd=[&](auto upd, int l, int r, int root) {
20
                int dir = tot++;
21
                ls[dir] = ls[root], rs[dir] = rs[root], sum[dir] = sum[root] + x;
22
23
                if (l == r) return dir;
                int mid = l + (r - l) / 2;
24
                if (k <= mid) ls[dir] = upd(upd, l, mid, ls[dir]);</pre>
25
                else rs[dir] = upd(upd, mid + 1, r, rs[dir]);
26
27
                return dir;
            };
28
            return upd(upd, 0, _n - 1, rt.back());
29
        HJTtr(int n): ls(n * 20), rs(n * 20), ind(n), sum(n * 20), tot(0), _n(n) {}
31
        void init(const std::vector<int> &a) {
            tot = 0;
33
34
            ind.assign(a.begin(), a.end());
35
            std::sort(ind.begin(), ind.end());
            ind.erase(std::unique(ind.begin(), ind.end());
36
            rt.push_back(build(0, _n - 1));
            for (int i = 0; i < a.size(); ++i) rt.push_back(update(getid(a[i])));</pre>
38
39
        /// @brief 查询区间第 k 大,注意区间是左闭右闭。
40
        /// @param l 左区间
41
        /// @param r 右区间
42
        /// @param k 第 k 大
43
        /// @return
44
        /// @note l, r, k are all 1-indexed.
45
        int query(int l, int r, int k) {
46
            auto qry=[&](auto qry, int u, int v, int vl, int vr, int kk) {
47
                if (vl == vr) return ind[vl];
48
                int mid = vl + (vr - vl) / 2, cnt = sum[ls[v]] - sum[ls[u]];
49
                if (kk <= cnt) return qry(qry, ls[u], ls[v], vl, mid, kk);</pre>
50
51
                else return qry(qry, rs[u], rs[v], mid + 1, vr, kk - cnt);
52
            };
53
            return qry(qry, rt[l-1], rt[r], 0, _n - 1, k);
54
   };
55
```

```
Trie
```

```
template<typename T>
    struct Trie {
2
        struct Node {
            T val;
            int to[2];
            Node(): val{0} {memset(to, 0, sizeof(to));}
            Node(T v): val(v) {memset(to, 0, sizeof(to));}
        };
        std::vector<Node> a;
        int cnt;
        Trie(): a(1), cnt(1) {}
11
        Trie(int siz): a(siz), cnt(1) {}
        int at(char ch) {return ch - '0';}
13
        Node& operator [](int idx) {return a[idx];}
14
15
        int go(int cur, char ch) {
            int &stat = a[cur].to[at(ch)];
16
17
            if (stat == 0) {
                stat = cnt++;
18
                while (cnt > a.size()) a.emplace_back();
20
            return a[cur].to[at(ch)];
21
22
   };
23
    笛卡尔树
    本质就是一个单调栈,可以用来求一个序列的最大子序列的左右端点
   std::vector<std::array<int, 2> > g;
1
    int dikaer(std::vector<int> a) {
2
        std::stack<int> stk;
        g.resize(a.size());
        for (int i = 1; i < a.size(); ++i) {</pre>
            int las = -1;
            while (!stk.empty() && a[stk.top()] <= a[i]) las = stk.top(), stk.pop();</pre>
            if (~las) g[i][0] = las;
            if (!stk.empty()) g[stk.top()][1] = i;
10
            stk.push(i);
11
12
        int rt = -1;
        while (!stk.empty()) rt = stk.top(), stk.pop();
13
14
        return rt;
15
   }
16
    fhq-treap
    // Definition
    class Treap {
      private:
        struct node {
            node *left, *right;
            int size, val, key;
            node();
            node(int);
            ~node();
11
            void pushup();
12
13
        } * root;
14
        int getNodeSize(node *);
        node *find(node *, int);
16
17
        std::pair<node *, node *> split(node *, int);
        std::pair<node *, node *> splitByValue(node *, int);
18
        node *merge(node *, node *);
19
```

```
public:
21
22
        Treap();
        ~Treap();
23
24
25
        void insert(int);
        void erase(int);
26
27
        int getRank(int);
        int getKth(int);
28
        void print(node *p, int dep);
29
        void print() { print(root, 0); }
    };
31
32
    // === Treap ===
33
34
    // struct Treap::node
35
36
37
    std::mt19937 Rnd(std::chrono::steady_clock::now().time_since_epoch().count());
38
39
        : left(nullptr), right(nullptr), size(0), val(0), key(Rnd()) {}
40
41
42
    Treap::node::node(int _val)
        : left(nullptr), right(nullptr), size(1), val(_val), key(Rnd()) {}
43
    Treap::node::~node() {
45
46
        delete left, right;
47
48
    inline void Treap::node::pushup() {
        size = 1;
50
        if (left != nullptr) size += left->size;
51
        if (right != nullptr) size += right->size;
52
53
    // class Treap
55
    Treap::Treap()
57
        : root(nullptr) {}
58
59
    Treap::~Treap() {
60
61
        delete root;
62
63
64
    inline int Treap::getNodeSize(Treap::node *node) {
        return node == nullptr ? 0 : node->size;
65
66
67
    std::pair<Treap::node *, Treap::node *> Treap::split(Treap::node *p, int k) {
        if (p == nullptr) return std::make_pair(nullptr, nullptr);
69
        std::pair<Treap::node *, Treap::node *> o;
70
        if (k <= getNodeSize(p->left)) {
71
            o = split(p->left, k);
72
            p->left = o.second;
            p->pushup();
74
75
            o.second = p;
76
        } else {
            o = split(p->right, k - getNodeSize(p->left) - 1);
77
            p->right = o.first;
79
            p->pushup();
            o.first = p;
80
81
        return o;
82
83
84
85
    std::pair<Treap::node *, Treap::node *> Treap::splitByValue(Treap::node *p, int val) {
        if (p == nullptr) return std::make_pair(nullptr, nullptr);
86
87
        std::pair<Treap::node *, Treap::node *> o;
88
        if (p->val < val) {</pre>
            o = splitByValue(p->right, val);
89
            p->right = o.first;
            p->pushup();
91
```

```
o.first = p;
92
93
         } else {
             o = splitByValue(p->left, val);
94
             p->left = o.second;
95
             p->pushup();
             o.second = p;
97
98
         return o:
99
    }
100
101
     Treap::node *Treap::merge(Treap::node *x, Treap::node *y) {
102
103
         if (x == nullptr) return y;
         if (y == nullptr) return x;
104
         if (x->key > y->key) {
105
             x->right = merge(x->right, y);
106
             x->pushup();
107
108
             return x;
109
110
         y->left = merge(x, y->left);
         y->pushup();
111
         return y;
112
113
114
     Treap::node *Treap::find(Treap::node *p, int val) {
115
         if (p == nullptr) return nullptr;
116
         if (p->val == val) return p;
117
         if (p->val > val) return find(p->left, val);
118
         return find(p->right, val);
119
120
121
     void Treap::insert(int val) {
122
         auto o = splitByValue(root, val);
123
         o.first = merge(o.first, new Treap::node(val));
124
125
         root = merge(o.first, o.second);
    }
126
127
     void Treap::erase(int val) {
128
         auto o = splitByValue(root, val);
129
130
         auto t = o;
         if (find(o.second, val) != nullptr) {
131
132
             t = split(o.second, 1);
             delete t.first;
133
134
135
         root = merge(o.first, t.second);
    }
136
137
     int Treap::getRank(int val) {
138
139
         auto x = splitByValue(root, val);
         int r = getNodeSize(x.first) + 1;
140
         root = merge(x.first, x.second);
141
142
         return r;
    }
143
144
     int Treap::getKth(int k) {
145
         auto x = split(root, k - 1);
146
         auto y = split(x.second, 1);
147
         Treap::node *o = y.first;
148
         root = merge(x.first, merge(y.first, y.second));
149
         return o == nullptr ? 0 : o->val;
150
151
152
     void Treap::print(Treap::node *p, int dep) {
153
154
         if (p == nullptr) return;
         print(p->left, dep + 1);
155
156
         for (int i = 0; i < dep; ++i) std::cout << " ";</pre>
         std::cout << p->val << '\n';</pre>
157
158
         print(p->right, dep + 1);
159
    }
160
```

数学

数论

```
数论整数
```

```
constexpr int P = 998244353;
    // assume -P <= x < 2P
    int norm(int x) {
        // x %= P;
        if (x < 0) \{ x += P; \}
        if (x >= P) { x -= P; }
        return x;
    template<typename E>
    E power(E n, int k) {
        E ret = E(1);
11
        while (k) {
12
            if (k & 1) ret *= n;
13
            n *= n;
14
15
            k >>= 1;
        } return ret;
16
17
18
   struct Z {
        int x;
19
20
        Z(int x = 0) : x(norm(x)) \{\}
        int val() const { return x; }
21
22
        Z operator-() const { return Z(norm(P - x)); }
        Z inv() const { assert(x != 0); return power(*this, P - 2); }
23
24
        Z & operator \star = (const \ Z \ \&rhs) \ \{ \ x = (long \ long)(x) \ * \ rhs. x \% \ P; \ return \ *this; \}
        Z &operator+=(const Z &rhs) { x = norm(x + rhs.x); return *this; }
25
        Z &operator-=(const Z &rhs) { x = norm(x - rhs.x); return *this; }
26
27
        Z &operator/=(const Z &rhs) { return *this *= rhs.inv(); }
        friend Z operator*(const Z &lhs, const Z &rhs) { Z res = lhs; res *= rhs; return res; }
28
        friend Z operator+(const Z &lhs, const Z &rhs) { Z res = lhs; res += rhs; return res; }
        friend Z operator-(const Z &lhs, const Z &rhs) { Z res = lhs; res -= rhs; return res; }
30
        friend Z operator/(const Z &lhs, const Z &rhs) { Z res = lhs; res /= rhs; return res; }
31
        friend std::istream &operator>>(std::istream &is, Z &a) { long long v; is >> v; a = Z(v); return is; }
32
        friend std::ostream &operator<<(std::ostream &os, const Z &a) { return os << a.val(); }</pre>
33
    Z operator"" _z(unsigned long long x) { return Z(x); }
    拉格朗日差值法
    template<typename T>
1
    T lintp(const vector<int>& x, const vector<T>& y, int k) {
        T ans = 0;
3
        for (int i = 0; i < x.size(); ++i) {</pre>
            if (k == x[i])
                return y[i];
            T u = 1, v = 1;
            for (int j = 0; j < x.size(); ++j) {</pre>
                if (i == j) continue;
                u *= (k - x[j]);
10
                v *= (x[i] - x[j]);
11
12
            ans += y[i] * u / v;
13
15
        return ans:
   }
16
    欧几里得
       • 扩展欧几里得
    int exgcd(int a, int b, int& x, int& y) {
        if (a == 0) {
2
            x = 0, y = 1;
            return b;
        }
```

```
int ret = exgcd(b % a, a, x, y), xx = x;
    x = y - b / a * x;
    y = xx;
    return ret;
}
```

类欧几里得

- $m = \lfloor \frac{an+b}{c} \rfloor$.
- $g(a,b,c,n) = \sum_{i=0}^{n} i \lfloor \frac{ai+b}{c} \rfloor$: 当 $a \geq c$ or $b \geq c$ 时, $g(a,b,c,n) = (\frac{a}{c})n(n+1)(2n+1)/6 + (\frac{b}{c})n(n+1)/2 + g(a \bmod c, b \bmod c, c, n)$; 否则 $g(a,b,c,n) = \frac{1}{2}(n(n+1)m f(c,c-b-1,a,m-1) h(c,c-b-1,a,m-1))$ 。
- $h(a,b,c,n) = \sum_{i=0}^n \lfloor \frac{ai+b}{c} \rfloor^2$: 当 $a \geq c$ or $b \geq c$ 时, $h(a,b,c,n) = (\frac{a}{c})^2 n(n+1)(2n+1)/6 + (\frac{b}{c})^2 (n+1) + (\frac{a}{c})(\frac{b}{c})n(n+1) + h(a \bmod c, b \bmod c, c, n) + 2(\frac{a}{c})g(a \bmod c, b \bmod c, c, n) + 2(\frac{b}{c})f(a \bmod c, b \bmod c, c, n)$; 否则 h(a,b,c,n) = nm(m+1) 2g(c,c-b-1,a,m-1) 2f(c,c-b-1,a,m-1) f(a,b,c,n) 。

```
template<typename T>
    T lintp(const vector<int>& x, const vector<T>& y, int k) {
        T ans = 0;
        for (int i = 0; i < x.size(); ++i) {</pre>
             if (k == x[i])
                return y[i];
             T u = 1, v = 1;
             for (int j = 0; j < x.size(); ++j) {</pre>
                 if (i == j) continue;
                 u \star = (k - x[j]);
10
                 v *= (x[i] - x[j]);
11
             }
             ans += y[i] * u / v;
13
15
        return ans:
```

Miller-Rabin 和 Pollard-Rho

• Miller-Rabin

```
long long pow_128(__int128_t n, long long k, long long mo) {
        __int128_t ret = 1;
2
        while (k) {
            if (k & 1) (ret *= n) %= mo;
            (n *= n) \%= mo;
            k >>= 1;
        } return ret;
    bool miller_rabin(long long n) {
10
        static const long long jp[] = { 2, 3, 5, 7, 11, 13, 17, 19, 23, 29 };
11
12
13
        if (n <= 1 || (n > 2 && !(n & 1))) return false;
        for (long long p : jp) if (n % p == 0) return n == p;
14
15
        long long r = n - 1, x, y;
16
        long long e = 0;
17
18
        while (~r & 1) r >>= 1, ++e;
        for (long long p : jp) {
19
            x = pow_128(p, r, n);
            for (long long t = 0; t < e && x > 1; ++t) {
21
                y = (__int128_t)x * x % n;
                if (y == 1 && x != n - 1) return false;
23
                x = y;
24
25
            if (x != 1) return false;
26
        return true:
28
29
    }
```