Three-Reaction Example

Model Description

A simple system of three species and three reactions. The species are $A,\,B$ and C. The reactions are:

\emptyset $\frac{k_1}{}$	$\rightarrow A$	[R1]
, ka		

$$\emptyset \xrightarrow{\kappa_2} B \qquad [R2]$$

$$A + B \xrightarrow{k_3} C$$
 [R3]

This model is part of each of the provided PRISM model files.

Properties

The property of interest is the probability to reach an *objective* state before a given time limit, T. The *objective* state is identified using a label in the PRISM model:

label "objective" = a=0 & b=0 & c=2;

Then, in PRISM syntax, the CSL property is given as P=? [F[0,T] "objective"].

Analysis

This model has infinite states (in principle) but the objective is unreachable if A > 2 or B > 2 or C > 2. This is visually clear in the state diagram:

The absorbing states are indicated using a constraint label in the PRISM model file:

label "constraint" = a+c<maxConstraint & b+c<maxConstraint;</pre>

The constraint is controlled by the maxConstraint constant. The lowest valid setting of maxConstraint is 3. The "constrained" importance sampling

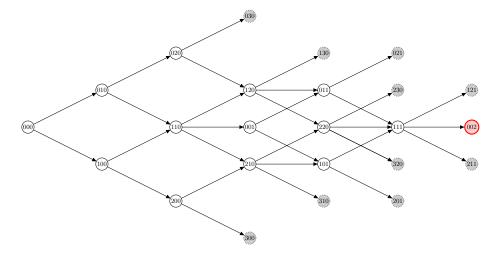


Figure 1: State diagram for the three-reaction model. The objective (red) is not achievable from the gray shaded states, so they are treated as absorbing states.

heuristic works by rejecting any transitions that violate the constraint. When maxConstrain is 3, all simulated paths reach the objective, which is optimum. When maxConstraint is greater than 3, simulated paths can terminate in absorbing states.