

Module 16

Partha Pratim  
Das

Week Recap

Objectives &  
Outline

Relational  
Algebra

Select

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Module Summary

# Database Management Systems

Module 16: Formal Relational Query Languages/1

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# Week Recap

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Module Summary

- SQL Examples have been practiced for basic query structures
- Nested Subquery in SQL
- Data Modification
- SQL expressions for Join and Views
- Transactions
- Integrity Constraints
- More data types in SQL
- Authorization in SQL
- Functions and Procedures in SQL
- Triggers

# Module Objectives

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Module Summary

- To understand formal query language through relational algebra

# Module Outline

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Module Summary

- Relational Algebra

# Formal Relational Query Language

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Module Summary

- Relational Algebra
  - Procedural and Algebra based
- Tuple Relational Calculus
  - Non-Procedural and Predicate Calculus based
- Domain Relational Calculus
  - Non-Procedural and Predicate Calculus based

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Module Summary

# Relational Algebra

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Module Summary

- Created by Edgar F Codd at IBM in 1970
- Procedural language
- Six basic operators
  - select:  $\sigma$
  - project:  $\Pi$
  - union:  $\cup$
  - set difference:  $-$
  - Cartesian product:  $\times$
  - rename:  $\rho$
- The operators take one or two relations as inputs and produce a new relation as a result

# Select Operation

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Module Summary

- Notation:  $\sigma_p(r)$
- $p$  is called the **selection predicate**
- Defined as:

$$\sigma_p(r) = \{t | t \in r \text{ and } p(t)\}$$

where  $p$  is a formula in propositional calculus consisting of **terms** connected by :  $\wedge$  (**and**),  $\vee$  (**or**),  $\neg$  (**not**)

Each **terms** is one of:

$$<attribute> op <attribute> or <constant>$$

where op is one of:  $=, \neq, >, \geq, ., <, \leq$

- Example of selection:

$$\sigma_{dept\_name = 'Physics'}(instructor)$$

A	B	C	D
$\alpha$	$\alpha$	1	7
$\alpha$	$\beta$	5	7
$\beta$	$\beta$	12	3
$\beta$	$\beta$	23	10

A	B	C	D
$\alpha$	$\alpha$	1	7
$\beta$	$\beta$	23	10

$$\sigma_{A=B \wedge D > 5}(r)$$

# Project Operation

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Module Summary

- Notation:  $\Pi_{A_1, A_2, \dots, A_k}(r)$   
 where  $A_1, A_2$  are attribute names and  $r$  is a relation
- The result is defined as the relation of  $k$  columns obtained by erasing the columns that are not listed
- Duplicate rows removed from result, since relations are sets
- Example: To eliminate the *dept\_name* attribute of *instructor*

$$\Pi_{ID, name, salary}(instructor)$$

A	B	C
$\alpha$	10	1
$\alpha$	20	1
$\beta$	30	1
$\beta$	40	2

$$\begin{array}{|c|c|} \hline A & C \\ \hline \alpha & 1 \\ \alpha & 1 \\ \beta & 1 \\ \beta & 2 \\ \hline \end{array}
 = 
 \begin{array}{|c|c|} \hline A & C \\ \hline \alpha & 1 \\ \beta & 1 \\ \beta & 2 \\ \hline \end{array}$$

# Union Operation

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Module Summary

- Notation:  $r \cup s$
- Defined as:  $r \cup s = \{t | t \in r \text{ or } t \in s\}$
- For  $r \cup s$  to be valid.
  - $r, s$  must have the *same arity* (same number of attributes)
  - The attribute domains must be **compatible** (example: 2nd column of  $r$  deals with the same type of values as does the 2nd column of  $s$ )
  - Example: to find all courses taught in the Fall 2009 semester, or in the Spring 2010 semester, or in both

$$\Pi_{course\_id}(\sigma_{semester="Fall"} \wedge year=2009(section)) \cup \Pi_{course\_id}(\sigma_{semester="Spring"} \wedge year=2010(section))$$

A	B
$\alpha$	1
$\alpha$	2
$\beta$	1

*r*

A	B
$\alpha$	2
$\beta$	3

*s*

A	B
$\alpha$	1
$\alpha$	2
$\beta$	1
$\beta$	3

*r ∪ s*

# Difference Operation

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Module Summary

- Notation  $r - s$
- Defined as:  $r - s = \{t | t \in r \text{ and } t \notin s\}$
- Set differences must be taken between **compatible** relations
  - $r$  and  $s$  must have the **same** arity
  - attribute domains of  $r$  and  $s$  must be compatible
- Example: to find all courses taught in the Fall 2009 semester, but not in the Spring 2010 semester

$$\Pi_{course\_id}(\sigma_{semester="Fall"} \wedge year=2009(section)) - \\ \Pi_{course\_id}(\sigma_{semester="Spring"} \wedge year=2010(section))$$

A	B
$\alpha$	1
$\alpha$	2
$\beta$	1

*r*

A	B
$\alpha$	2
$\beta$	3

*s*

 $r - s$ 

A	B
$\alpha$	1
$\beta$	1

# Intersection Operation

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Module Summary

- Notation:  $r \cap s$
- Defined as:

$$r \cap s = \{t | t \in r \text{ and } t \in s\}$$

- Assume:
  - $r, s$  have the *same arity*
  - attributes of  $r$  and  $s$  are compatible
- Note:  $r \cap s = r - (r - s)$

A	B
$\alpha$	1
$\alpha$	2
$\beta$	1

*r*

A	B
$\alpha$	2
$\beta$	3

*s*

A	B
$\alpha$	2

*r ∩ s*



# Cartesian-Product Operation

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Module Summary

- Notation  $r \times s$
- Defined as:

$$r \times s = \{t \mid q \in r \text{ and } q \in s\}$$

- Assume that attributes of  $r(R)$  and  $s(S)$  are disjoint.  
(That is,  $R \cap S = \emptyset$ )
- If attributes of  $r(R)$  and  $s(S)$  are not disjoint, then renaming must be used

A	B
$\alpha$	1
$\beta$	2

 $r$ 

C	D	E
$\alpha$	10	a
$\beta$	10	a
$\beta$	20	b
$\gamma$	10	b

 $s$ 

A	B	C	D	E
$\alpha$	1	$\alpha$	10	a
$\alpha$	1	$\beta$	10	a
$\alpha$	1	$\beta$	20	b
$\alpha$	1	$\gamma$	10	b
$\beta$	2	$\alpha$	10	a
$\beta$	2	$\beta$	10	a
$\beta$	2	$\beta$	20	b
$\beta$	2	$\gamma$	10	b

 $r \times s$

# Rename Operation

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Module Summary

- Allows us to name, and therefore to refer to, the results of relational-algebra expressions.
- Allows us to refer to a relation by more than one name.
- Example:

$$\rho_x(E)$$

returns the expression  $E$  under the name  $X$

- If a relational-algebra expression  $E$  has arity  $n$ , then

$$\rho_{x(A_1, A_2, \dots, A_n)}(E)$$

returns the result of expression  $E$  under the name  $X$ , and with the attributes renamed to

$$A_1, A_2, \dots, A_n$$



# Division Operation

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Module Summary

- The division operation is applied to two relations
- $R(Z) \div S(X)$ , where  $X$  subset  $Z$ . Let  $Y = Z - X$  (and hence  $Z = X \cup Y$ ); that is, let  $Y$  be the set of attributes of  $R$  that are not attributes of  $S$
- The result of DIVISION is a relation  $T(Y)$  that includes a tuple  $t$  if tuples  $t_R$  appear in  $R$  with  $t_R[Y] = t$ , and with
  - $t_R[X] = t_s$  for every tuple  $t_s$  in  $S$ .
- For a tuple  $t$  to appear in the result  $T$  of the DIVISION, the values in  $t$  must appear in  $R$  in combination with every tuple in  $S$
- Division is a derived operation and can be expressed in terms of other operations
- $r \div s \equiv \Pi_{R-S}(r) - \Pi_{R-S}(r)((\Pi_{R-S}(r) \times s) - \Pi_{R-S,S}(r))$



# Division Examples

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Module Summary

• R

Lecturer	Module
Brown	Compilers
Brown	Databases
Green	Prolog
Green	Databases
Lewis	Prolog
Smith	Databases

S

Subject
Prolog

R | S

Lecturer
Green
Lewis



# Division Examples (2)

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Module Summary

• R

Lecturer	Module
Brown	Compilers
Brown	Databases
Green	Prolog
Green	Databases
Lewis	Prolog
Smith	Databases

S

Subject
Databases
Prolog

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Green

# Division Examples (3)

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Module Summary

**A**

<i>sno</i>	<i>pno</i>
s1	p1
s1	p2
s1	p3
s1	p4
s2	p1
s2	p2
s3	p2
s4	p2
s4	p4

**B1**

<i>pno</i>
p2

**B2**

<i>pno</i>
p2
p4

**A/B1**

<i>sno</i>
s1
s2
s3
s4

**A/B2**

<i>sno</i>
s1
s4

**B3**

<i>pno</i>
p1
p2
p4

**A/B3**

<i>sno</i>
s1



# Division Example (4)

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Module Summary

- Relations  $r, s$ :

A	B
$\alpha$	1
$\alpha$	2
$\alpha$	3
$\beta$	1
$\gamma$	1
$\delta$	1
$\delta$	3
$\delta$	4
$\epsilon$	6
$\epsilon$	1
$\beta$	2

r

B
1
2

s

A
$\alpha$
$\beta$

- $r \div s$ :

e.g. A is customer name

B is branch-name

1 and 2 here show two specific branch-names

(Find customers who have an account in all branches of the bank)



# Division Example (5)

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Module Summary

- Relations  $r, s$ :

A	B	C	D	E
a	a	a	a	1
a	a	γ	a	1
a	a	γ	b	1
β	a	γ	a	1
β	a	γ	b	3
γ	a	γ	a	1
γ	a	γ	b	1
γ	a	β	b	1

$r$

D	E
a	1
b	1

$s$

e.g. Students who have taken both "a" and "b" courses, with instructor "1"

(Find students who have taken all courses given by instructor 1)

- $r \div s$ :

A	B	C
a	a	γ
γ	a	γ

# Module Summary

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Module Summary

- Discussed relational algebra with examples

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**Edited and new slides are marked with “PPD”.**

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Predicate Logic

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Module Summary

# Database Management Systems

Module 17: Formal Relational Query Languages/2

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Module Summary

- Relational Algebras and its Operations

# Module Objectives

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Module Summary

- To understand formal calculus-based query language through relational algebra

# Module Outline

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Module Summary

- Tuple Relational Calculus (Overview only)
- Domain Relational Calculus (Overview only)
- Equivalence of Algebra and Calculus

# Formal Relational Query Language

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Module Summary

- Relational Algebra
  - Procedural and Algebra based
- Tuple Relational Calculus
  - Non-Procedural and Predicate Calculus based
- Domain Relational Calculus
  - Non-Procedural and Predicate Calculus based

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Module Summary

# Predicate Logic

# Predicate Logic

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Module Summary

**Predicate Logic** or **Predicate Calculus** is an extension of **Propositional Logic** or **Boolean Algebra**.

It adds the concept of predicates and quantifiers to better capture the meaning of statements that cannot be adequately expressed by propositional logic.

**Tuple Relational Calculus** and **Domain Relational Calculus** are based on **Predicate Calculus**

# Predicate

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Module Summary

- Consider the statement, “ $x$  is greater than 3”. It has two parts. The first part, the variable  $x$ , is the subject of the statement. The second part, “is greater than 3”, is the predicate. It refers to a property that the subject of the statement can have.
- The statement “ $x$  is greater than 3” can be denoted by  $P(x)$  where  $P$  denotes the predicate “is greater than 3” and  $x$  is the variable.
- The predicate  $P$  can be considered as a function. It tells the truth value of the statement  $P(x)$  at  $x$ . Once a value has been assigned to the variable  $x$ , the statement  $P(x)$  becomes a proposition and has a *truth* or *false* value.
- In general, a statement involving  $n$  variables  $x_1, x_2, x_3, \dots, x_n$  can be denoted by  $P(x_1, x_2, x_3, \dots, x_n)$ . Here  $P$  is also referred to as *n*-place predicate or a *n*-ary predicate.

# Quantifiers

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Module Summary

In predicate logic, predicates are used alongside quantifiers to express the extent to which a predicate is true over a range of elements. Using *quantifiers* to create such propositions is called *quantification*. There are two types of quantifiers:

- **Universal Quantifier**
- **Existential Quantifier**

# Universal Quantifier

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Module Summary

**Universal Quantification:** Mathematical statements sometimes assert that a property is true for all the values of a variable in a particular domain, called the **domain of discourse**

- Such a statement is expressed using universal quantification.
- The universal quantification of  $P(x)$  for a particular domain is the proposition that asserts that  $P(x)$  is *true* for all values of  $x$  in this domain
- The domain is very important here since it decides the possible values of  $x$
- Formally, The universal quantification of  $P(x)$  is the statement “ $P(x)$  for all values of  $x$  in the domain”.
- The notation  $\forall P(x)$  denotes the universal quantification of  $P(x)$ . Here  $\forall$  is called the universal quantifier.  $\forall P(x)$  is read as “for all  $x P(x)$ ”.
- Example: Let  $P(x)$  be the statement “ $x + 2 > x$ ”. What is the truth value of the statement  $\forall x P(x)$ ?  
Solution: As  $x + 2$  is greater than  $x$  for any real number, so  $P(x) \equiv T$  for all  $x$  or  $\forall x P(x) \equiv T$

# Existential Quantifier

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Module Summary

**Existential Quantification:** Some mathematical statements assert that there is an element with a certain property. Such statements are expressed by existential quantification. Existential quantification can be used to form a proposition that is true if and only if  $P(x)$  is *true* for at least one value of  $x$  in the domain.

- Formally, the existential quantification of  $P(x)$  is the statement "There exists an element  $x$  in the domain such that  $P(x)$ ".
- The notation  $\exists P(x)$  denotes the existential quantification of  $P(x)$ . Here  $\exists$  is called the existential quantifier.  $\exists P(x)$  is read as "There is atleast one such  $x$  such that  $P(x)$ "
- Example: Let  $P(x)$  be the statement " $x > 5$ ". What is the truth value of the statement  $\exists x P(x)$ ?

Solution:  $P(x)$  is *true* for all real numbers greater than 5 and *false* for all real numbers less than 5. So  $\exists x P(x) \equiv T$

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# Tuple Relational Calculus

# Tuple Relational Calculus

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Module Summary

TRC is a non-procedural query language, where each query is of the form

$$\{t \mid P(t)\}$$

where  $t$  = resulting tuples,

$P(t)$  = known as predicate and these are the conditions that are used to fetch  $t$ .

$P(t)$  may have various conditions logically combined with OR ( $\vee$ ), AND ( $\wedge$ ), NOT ( $\neg$ ).

It also uses quantifiers:

$\exists t \in r(Q(t))$  = “there exists” a tuple in  $t$  in relation  $r$  such that predicate  $Q(t)$  is true.

$\forall t \in r(Q(t))$  =  $Q(t)$  is true “for all” tuples in relation  $r$ .

- $\{P \mid \exists S \in Students \text{ and } (S.CGPA > 8 \wedge P.name = S.sname \wedge P.age = S.age)\}$  : returns the name and age of students with a CGPA above 8.

# Predicate Calculus Formula

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Module Summary

- a) Set of attributes and constants
- b) Set of comparison operators: (e.g.,  $<$ ,  $\leq$ ,  $=$ ,  $\neq$ ,  $>$ ,  $\geq$ )
- c) Set of connectives: and ( $\wedge$ ), or ( $\vee$ ), not ( $\neg$ )
- d) Implication ( $\Rightarrow$ ) :  $x \Rightarrow y$ , if  $x$  if true, then  $y$  is true  
$$x \Rightarrow y \equiv \neg x \vee y$$
- e) Set of quantifiers:
  - $\exists t \in r(Q(t)) \equiv$  “there exists” a tuple in  $t$  in relation  $r$  such that predicate  $Q(t)$  is true
  - $\forall t \in r(Q(t)) \equiv Q$  is true “for all” tuples  $t$  in relation  $r$



# TRC Example

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Student			
Fname	Lname	Age	Course
David	Sharma	27	DBMS
Aaron	Lilly	17	JAVA
Sahil	Khan	19	Python
Sachin	Rao	20	DBMS
Varun	George	23	JAVA
Simi	Verma	22	JAVA

Q.1 Obtain the first name of students whose age is greater than 21.

**Solution:**

$$\{t.Fname \mid Student(t) \wedge t.age > 21\}$$

$$\{t.Fname \mid t \in Student \wedge t.age > 21\}$$

$$\{t \mid \exists s \in Student(s.age > 21 \wedge t.Fname = s.Fname)\}$$

Fname
David
Varun
Simi

# TRC Example (2)

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Module Summary

Consider the relational schema

**student**(rollNo, name, year, courselD)  
**course**(courselD, cname, teacher)

Q.2 Find out the names of all students who have taken the course name 'DBMS'.

- $\{t \mid \exists s \in \text{student} \exists c \in \text{course}(s.\text{courselD} = c.\text{courselD} \wedge c.\text{cname} = \text{'DBMS'} \wedge t.\text{name} = s.\text{name})\}$
- $\{s.\text{name} \mid s \in \text{student} \wedge \exists c \in \text{course}(s.\text{courselD} = c.\text{courselD} \wedge c.\text{cname} = \text{'DBMS'})\}$

Q.3 Find out the names of all students and their rollNo who have taken the course name 'DBMS'.

- $\{s.\text{name}, s.\text{rollNo} \mid s \in \text{student} \wedge \exists c \in \text{course}(s.\text{courselD} = c.\text{courselD} \wedge c.\text{cname} = \text{'DBMS'})\}$
- $\{t \mid \exists s \in \text{student} \exists c \in \text{course}(s.\text{courselD} = c.\text{courselD} \wedge c.\text{cname} = \text{'DBMS'} \wedge t.\text{name} = s.\text{name} \wedge t.\text{rollNo} = s.\text{rollNo})\}$

# TRC Example (3)

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Module Summary

Consider the following relations:

**Flights**(fno, from, to, distance, departs, arrives)

**Aircraft**(aid, aname, cruisingrange)

**Certified**(eid, aid)

**Employees**(eid, ename, salary)

Q.4. Find the eids of pilots certified for Boeing aircraft.

**RA**

$$\Pi_{eid}(\sigma_{aname='Boeing'}(Aircraft \bowtie Certified))$$

**TRC**

- $\{C.eid \mid C \in Certified \wedge \exists A \in Aircraft (A.aid = C.aid \wedge A.aname = 'Boeing')\}$
- $\{T \mid \exists C \in Certified \exists A \in Aircraft (A.aid = C.aid \wedge A.aname = 'Boeing' \wedge T.eid = C.eid)\}$

# TRC Example (4)

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Module Summary

Consider the following relations:

**Flights**(flno, *from*, *to*, *distance*, *departs*, *arrives*)

**Aircraft**(aid, *aname*, *cruisingrange*)

**Certified**(eid, aid)

**Employees**(eid, *ename*, *salary*)

Q.5. Find the names and salaries of certified pilots working on Boeing aircrafts.

**RA**

$$\Pi_{ename, salary}(\sigma_{aname='Boeing'}(Aircraft \bowtie Certified \bowtie Employees))$$

**TRC**

$$\{P \mid \exists E \in Employees \exists C \in Certified \exists A \in Aircraft (A.aid = C.aid \wedge A.aname = 'Boeing' \wedge E.eid = C.eid \wedge P.ename = E.ename \wedge P.salary = E.salary)\}$$



# TRC Example (5)

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Module Summary

Consider the following relations:

**Flights**(fno, *from*, *to*, *distance*, *departs*, *arrives*)

**Aircraft**(aid, *aname*, *cruisingrange*)

**Certified**(eid, aid)

**Employees**(eid, *ename*, *salary*)

Q.6 Identify the flights that can be piloted by every pilot whose salary is more than \$100,000.

- $\{F.fno \mid F \in \text{Flights} \wedge \exists C \in \text{Certified} \exists E \in \text{Employees} (E.salary > 100,000 \wedge E.eid = C.eid)\}$



# Safety of Expressions

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Module Summary

- It is possible to write tuple calculus expressions that generate infinite relations
- For example,  $\{t \mid \neg t \in r\}$  results in an infinite relation if the domain of any attribute of relation  $r$  is infinite
- To guard against the problem, we restrict the set of allowable expressions to safe expressions
- An expression  $\{t \mid P(t)\}$  in the tuple relational calculus is *safe* if every component of  $t$  appears in one of the relations, tuples, or constants that appear in  $P$ .
  - NOTE: this is more than just a syntax condition
  - E.g.  $\{t \mid t[A] = 5 \vee \text{true}\}$  is not safe — it defines an infinite set with attribute values that do not appear in any relation or tuples or constants in  $P$

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# Domain Relational Calculus

# Domain Relational Calculus

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Module Summary

- A non-procedural query language equivalent in power to the tuple relational calculus
- Each query is an expression of the form:

$$\{< x_1, x_2, \dots, x_n > | P(x_1, x_2, \dots, x_n) \}$$

- $x_1, x_2, \dots, x_n$  represent domain variables
- P represents a formula similar to that of the predicate calculus

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Module Summary

# Equivalence of Algebra and Calculus

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Module Summary

## **Select Operation**

$R = (A, B)$

Relational Algebra:       $\sigma_{B=17}(r)$

Tuple Calculus:       $\{t \mid t \in r \wedge B = 17\}$

Domain Calculus:       $\{\langle a, b \rangle \mid \langle a, b \rangle \in r \wedge b = 17\}$

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Module Summary

## ***Project Operation***

$$R = (A, B)$$

Relational Algebra:       $\Pi_A(r)$

Tuple Calculus:       $\{t \mid \exists p \in r (t[A] = p[A])\}$

Domain Calculus:       $\{\langle a \rangle \mid \exists b (\langle a, b \rangle \in r)\}$

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Module Summary

## ***Combining Operations***

$R = (A, B)$

Relational Algebra:       $\Pi_A(\sigma_{B=17}(r))$

Tuple Calculus:       $\{t \mid \exists p \in r (t[A] = p[A] \wedge p[B] = 17)\}$

Domain Calculus:       $\{\langle a \rangle \mid \exists b (\langle a, b \rangle \in r \wedge b = 17)\}$

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Module Summary

## *Union*

$$R = (A, B, C) \quad S = (A, B, C)$$

Relational Algebra:  $r \cup s$

Tuple Calculus:  $\{t \mid t \in r \vee t \in s\}$

Domain Calculus:  $\{<a, b, c> \mid <a, b, c> \in r \vee <a, b, c> \in s\}$

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Module Summary

## ***Set Difference***

$$R = (A, B, C) \quad S = (A, B, C)$$

Relational Algebra:       $r - s$

Tuple Calculus:       $\{t \mid t \in r \wedge t \notin s\}$

Domain Calculus:       $\{\langle a, b, c \rangle \mid \langle a, b, c \rangle \in r \wedge \langle a, b, c \rangle \notin s\}$

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Module Summary

## ***Intersection***

$$R = (A, B, C) \quad S = (A, B, C)$$

Relational Algebra:  $r \cap s$

Tuple Calculus:  $\{t \mid t \in r \wedge t \in s\}$

Domain Calculus:  $\{\langle a, b, c \rangle \mid \langle a, b, c \rangle \in r \wedge \langle a, b, c \rangle \in s\}$

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Module Summary

## ***Cartesian/Cross Product***

$$R = (A, B) \quad S = (C, D)$$

Relational Algebra:  $r \times s$

Tuple Calculus:  $\{t \mid \exists p \in r \exists q \in s (t[A] = p[A] \wedge t[B] = p[B] \wedge t[C] = q[C] \wedge t[D] = q[D])\}$

Domain Calculus:  $\{\langle a, b, c, d \rangle \mid \langle a, b \rangle \in r \wedge \langle c, d \rangle \in s\}$

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Module Summary

***Natural Join***

$$R = (A, B, C, D) \quad S = (B, D, E)$$

Relational Algebra:  $r \bowtie s$ 

$$\Pi_{r.A, r.B, r.C, r.D, s.E}(\sigma_{r.B=s.B \wedge r.D=s.D}(r \times s))$$

Tuple Calculus:  $\{t \mid \exists p \in r \exists q \in s (t[A] = p[A] \wedge t[B] = p[B] \wedge t[C] = p[C] \wedge t[D] = p[D] \wedge t[E] = q[E] \wedge p[B] = q[B] \wedge p[D] = q[D])\}$ Domain Calculus:  $\{\langle a, b, c, d, e \rangle \mid \langle a, b, c, d \rangle \in r \wedge \langle b, d, e \rangle \in s\}$

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Module Summary

## ***Division***

$$R = (A, B) \qquad S = (B)$$

Relational Algebra:  $r \div s$

Tuple Calculus:  $\{t \mid \exists p \in r \ \forall q \in s (p[B] = q[B] \Rightarrow t[A] = p[A])\}$

Domain Calculus:  $\{\langle a \rangle \mid \langle a \rangle \in r \wedge \forall \langle b \rangle (\langle b \rangle \in s \Rightarrow \langle a, b \rangle \in r)\}$

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# Module Summary

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Module Summary

- Introduced tuple relational and domain relational calculus
- Illustrated equivalence of algebra and calculus

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ER Model

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Module Summary

# Database Management Systems

Module 18: Entity-Relationship Model/1

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Module 18

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Module Summary

- Predicate Calculus
- Tuple Relational and Domain Relational Calculus
- Equivalence of Relational Algebra and Relational Calculus



# Module Objectives

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Module Summary

- To understand the Design Process for Database Systems
- To study the E-R Model for real world representation

# Module Outline

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Module Summary

- Design Process
- E-R Model
  - Entity and Entity Set
  - Relationship
    - ▷ Cardinality
  - Attributes
  - Weak Entity Sets

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Module Summary

# Design Process



# What is Design?

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Module Summary

## A Design:

- Satisfies a given (perhaps informal) functional specification
- Conforms to limitations of the target medium
- Meets implicit or explicit requirements on performance and resource usage
- Satisfies implicit or explicit design criteria on the form of the artifact
- Satisfies restrictions on the design process itself, such as its length or cost, or the tools available for doing the design

# Role of Abstraction

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Module Summary

- *Disorganized Complexity* results from
  - *Storage (STM) limitations* of human brain – an individual can simultaneously comprehend of the order of seven, plus or minus two chunks of information
  - *Speed limitations* of human brain – it takes the mind about five seconds to accept a new chunk of information
- **Abstraction** provides the major tool to handle Disorganized Complexity by *chunking information*
- Ignore inessential details, deal only with the generalized, idealized model of the world

Consider: A binary number 110010101001

Hard to remembers. Right?

Try the octal form: (110)(010)(101)(001) ⇒ 6251

Or the hex form: (1100)(1010)(1001) ⇒ CA9

# Model Building

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Module Summary

- Physics
  - Time-Distance Equation
  - Quantum Mechanics
- Chemistry
  - Valency-Bond Structures
- Geography
  - Maps
  - Projections

- Electrical Circuits
  - Kirchoff's Loop Equations
  - Time Series Signals and FFT
  - Transistor Models
  - Schematic Diagram
  - Interconnect Routing
- Building & Bridges
  - Drawings – Plan, Elevation, Side view
  - Finite Element Models

- Models are common in all engineering disciplines
  - Model building follows principles of decomposition, abstraction, and hierarchy
  - Each model describes a specific aspect of the system
  - Build new models upon old proven models

# Design Approach

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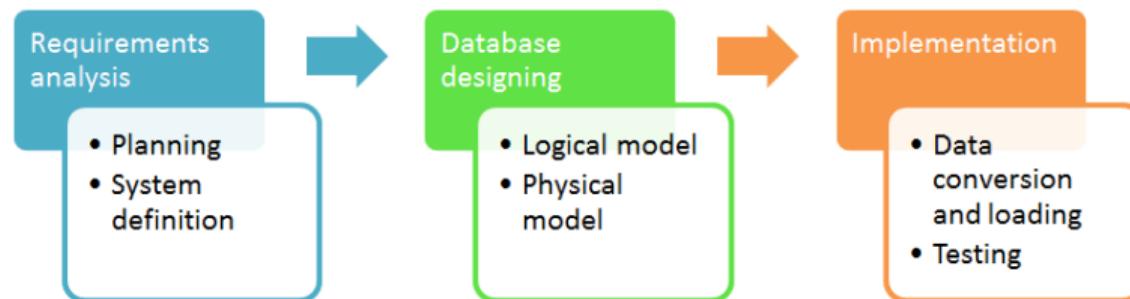
Cardinality

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Module Summary

- **Requirement Analysis:** Analyse the data needs of the prospective database users
  - Planning
  - System Definition
- **Database Designing:** Use a modeling framework to create abstraction of the real world
  - Logical Model
  - Physical Model
- **Implementation**
  - Data Conversion and Loading
  - Testing



# Design Approach (2): Database Designing

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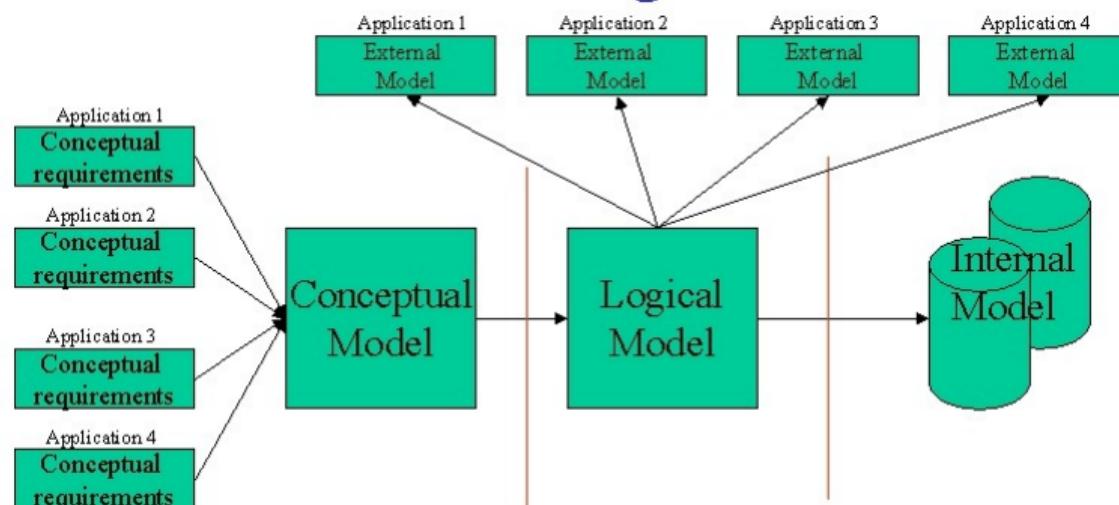
Cardinality

Constraints

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Module Summary

- **Logical Model:** Deciding on a **good** database schema
  - *Business Decision:* What attributes should we record in the database?
  - *Computer Science Decision:* What relation schema should we have and how should the attributes be distributed among the various relation schema?
- **Physical Model:** Deciding on the physical layout of the database



# Design Approach (3): Database Designing: Logical Model

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Module Summary

- **Entity Relationship Model**

- Models an enterprise as a collection of entities and relationships
  - ▷ *Entity*: A distinguishable “thing” or “object” in the enterprise
    - Described by a set of attributes
    - ▷ *Relationship*: An association among multiple entities
- Represented by an *Entity-Relationship or ER Diagram*

- **Database Normalization (Chapter 8)**

- Formalize what designs are bad, and test for them

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**ER Model**

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Module Summary

# Entity Relationship (ER) Model

# ER Model: Database Modeling

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Module Summary

- The ER data model was developed to facilitate database design by allowing specification of an **enterprise schema** that represents the overall logical structure of a database
- The ER model is useful in mapping the meanings and interactions of real-world enterprises onto a conceptual schema
- The ER data model employs three basic concepts:
  - Attributes
  - Entity sets
  - Relationship sets
- The ER model also has an associated diagrammatic representation, the ER diagram, which can express the overall logical structure of a database graphically

# Attributes

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Module Summary

- An **Attribute** is a property associated with an entity / entity set. Based on the values of certain attributes, an entity can be identified uniquely
- Attribute types:
  - **Simple** and **Composite** attributes
  - **Single-valued** and **Multivalued** attributes
    - ▷ Example: Multivalued attribute: *phone\_numbers*
  - **Derived** attributes
    - ▷ Can be computed from other attributes
    - ▷ Example: age, given date\_of\_birth
- **Domain:** Set of permitted values for each attribute

# Attributes (2): Composite

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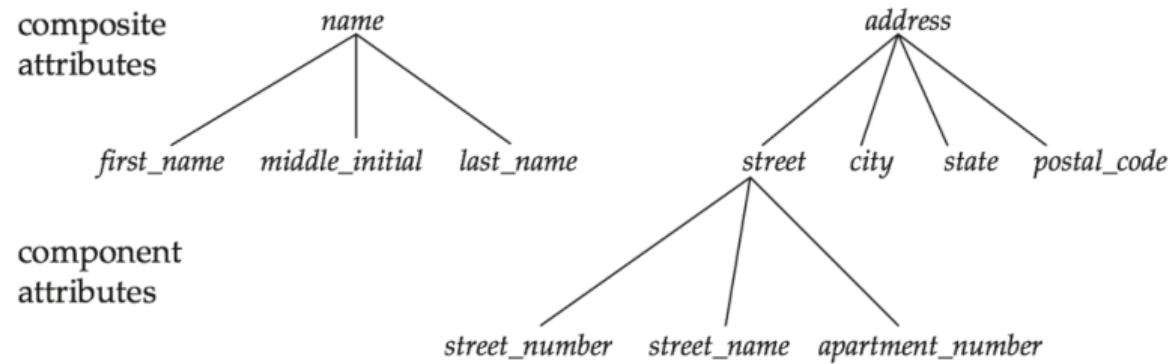
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# Entity Sets

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Module Summary

- An **entity** is an object that exists and is distinguishable from other objects.
  - Example: specific person, company, event, plant
- An **entity set** is a set of entities of the same type that share the same properties.
  - Example: set of all persons, companies, trees, holidays
- An entity is represented by a set of attributes; i.e., descriptive properties possessed by all members of an entity set.
  - Example:  
 $\text{instructor} = (\underline{\text{ID}}, \text{name}, \text{street}, \text{city}, \text{salary})$   
 $\text{course} = (\underline{\text{course\_id}}, \text{title}, \text{credits})$
- A subset of the attributes form a **primary key** of the entity set; that is, uniquely identifying each member of the set.
  - Primary key of an entity set is represented by underlining it

# Entity Sets – *instructor* and *student*

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Module Summary

instructor\_ID instructor\_name

76766	Crick
45565	Katz
10101	Srinivasan
98345	Kim
76543	Singh
22222	Einstein

*instructor*

student-ID student\_name

98988	Tanaka
12345	Shankar
00128	Zhang
76543	Brown
76653	Aoi
23121	Chavez
44553	Peltier

*student*

# Relationship Sets

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Module Summary

- A **relationship** is an association among several entities

Example:

44553 (Peltier)      advisor      22222 (Einstein)  
*student* entity      relationship set      *instructor* entity

- A **relationship set** is a mathematical relation among  $n \geq 2$  entities, each taken from entity sets

$$\{(e_1, e_2, \dots, e_n) \mid e_1 \in E_1, e_2 \in E_2, \dots, e_n \in E_n\}$$

where  $(e_1, e_2, \dots, e_n)$  is a relationship.

- Example:       $(44553, 22222) \in \text{advisor}$

# Relationship Set (2) *advisor*

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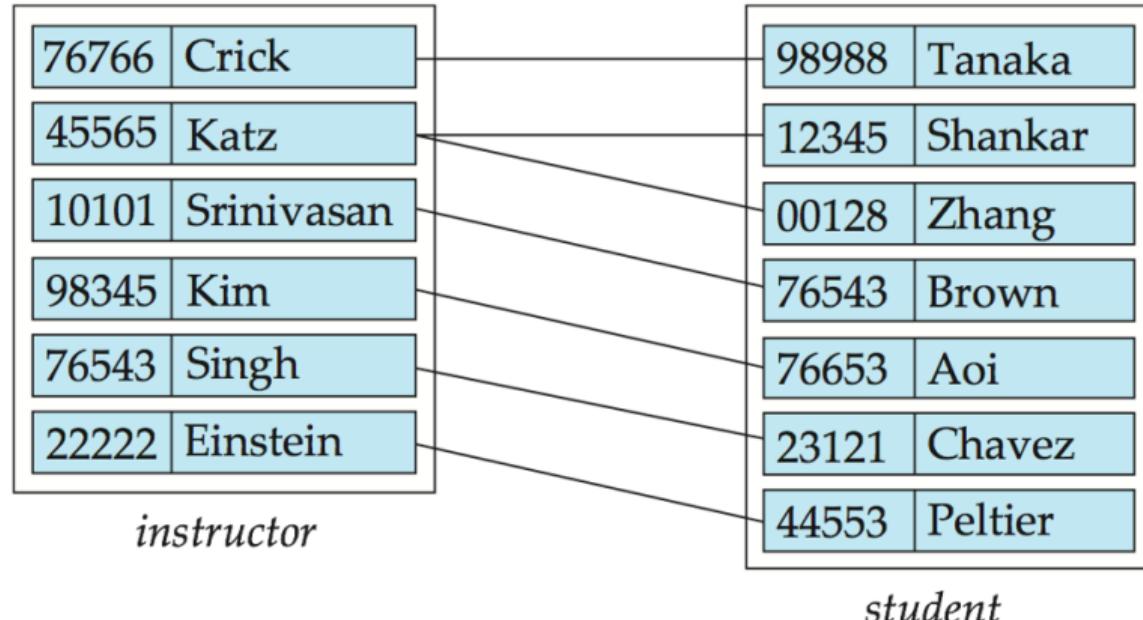
Entity Sets

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# Relationship Sets (3)

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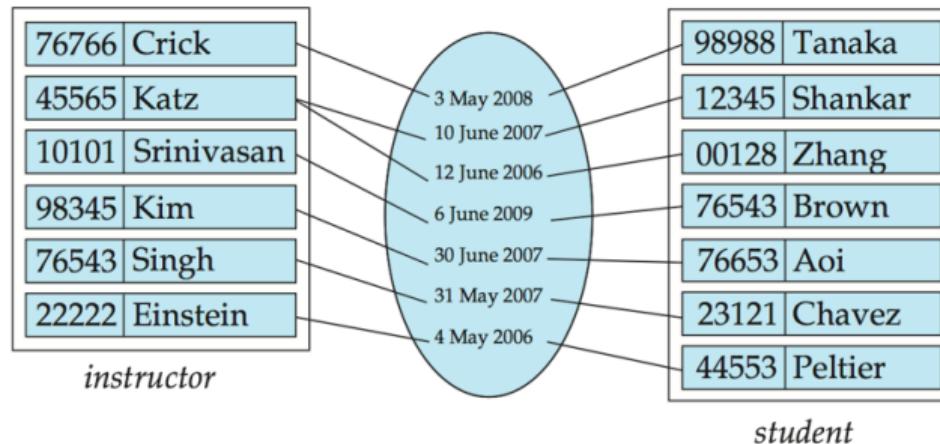
Cardinality

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Module Summary

- An attribute can also be associated with a relationship set.
- For instance, the *advisor* relationship set between entity sets *instructor* and *student* may have the attribute *date* which tracks when the student started being associated with the advisor



# Relationship Set (4): Degree

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Module Summary

- Binary relationship
  - involves two entity sets (or degree two).
  - most relationship sets in a database system are binary.
- Relationships between more than two entity sets are rare. Most relationships are binary
  - Example: *students* work on research projects under the guidance of an *instructor*.
  - relationship *proj\_guide* is a ternary relationship between *instructor*, *student*, and *project*

# Attributes (3): Redundant

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Weak Entity Sets

Module Summary

- Suppose we have entity sets:
  - *instructor*, with attributes: *ID*, *name*, *dept\_name*, *salary*
  - *department*, with attributes: *dept\_name*, *building*, *budget*
- We model the fact that each instructor has an associated department using a relationship set *inst\_dept*
- The attribute *dept\_name* appears in both entity sets. Since it is the primary key for the entity set *department*, it replicates information present in the relationship and is therefore redundant in the entity set *instructor* and needs to be removed
- BUT: When converting back to tables, in some cases the attribute gets reintroduced, as we will see later

# Mapping Cardinality Constraints

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Weak Entity Sets

Module Summary

- Express the number of entities to which another entity can be associated via a relationship set.
- Most useful in describing binary relationship sets.
- For a binary relationship set the mapping cardinality must be one of the following types:
  - One to one
  - One to many
  - Many to one
  - Many to many

# Mapping Cardinalities

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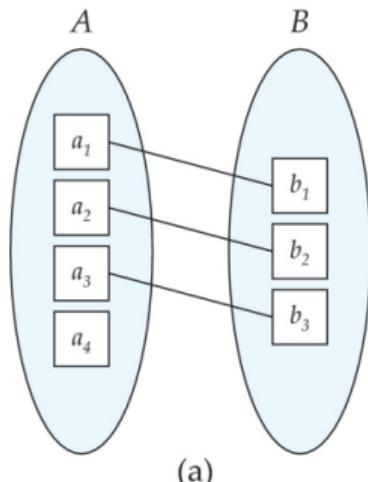
Entity Sets

Relationship

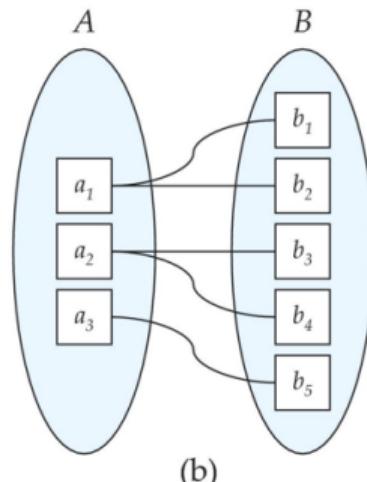
Cardinality  
Constraints

Weak Entity Sets

Module Summary



One to one



One to many

Note: Some elements in A and B may not be mapped to any elements in the other set

# Mapping Cardinalities

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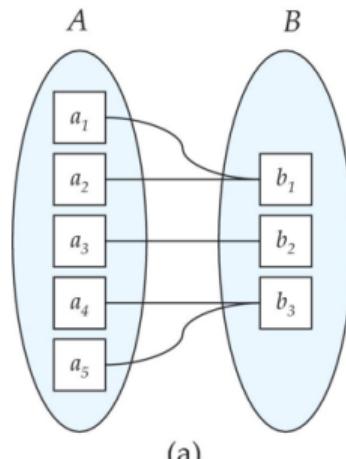
Entity Sets

Relationship

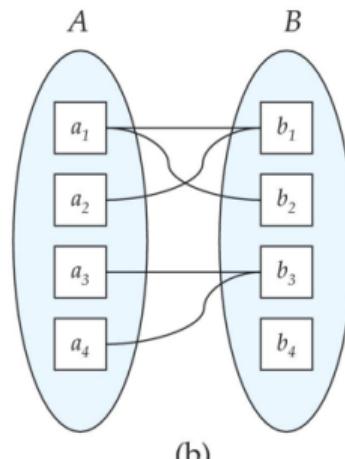
Cardinality  
Constraints

Weak Entity Sets

Module Summary



Many to  
one



Many to  
many

Note: Some elements in A and B may not be mapped to any elements in the other set



# Weak Entity Sets

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Weak Entity Sets

Module Summary

An entity set may be of two types:

- Strong entity set
  - A strong entity set is an entity set that contains sufficient attributes to uniquely identify all its entities
  - In other words, *a primary key exists for a strong entity set*
  - Primary key of a strong entity set is represented by underlining it
- Weak entity set
  - A weak entity set is an entity set that does not contain sufficient attributes to uniquely identify its entities
  - In other words, *a primary key does not exist for a weak entity set*
  - However, it contains a partial key called as a **discriminator**
  - Discriminator can identify a group of entities from the entity set
  - Discriminator is represented by underlining with a dashed line

# Weak Entity Sets (2)

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Weak Entity Sets

Module Summary

- Since a weak entity set does not have primary key, it cannot independently exist in the ER Model
- It features in the model in relationship with a strong entity set. This is called the **identifying relationship**
- Primary Key of Weak Entity Set
  - The combination of discriminator and primary key of the strong entity set makes it possible to uniquely identify all entities of the weak entity set
  - Thus, this combination serves as a primary key for the weak entity set.
  - Clearly, this primary key is not formed by the weak entity set completely.
  - **Primary Key of Weak Entity Set = Its own discriminator + Primary Key of Strong Entity Set**
- Weak entity set must have **total participation** in the identifying relationship. That is all its entities must feature in the relationship

# Weak Entity Sets (3): Example

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Weak Entity Sets

Module Summary

- **Strong Entity Set:** *Building*(building\_no, building\_name, address). building\_no is its primary key
- **Weak Entity Set:** *Apartment*(door\_no, floor). door\_no is its discriminator as door\_no alone can not identify an apartment uniquely. There may be several other buildings having the same door number
- **Relationship:** *BA* between *Building* and *Apartment*
- By **total participation** in *BA*, each apartment must be present in at least one building
- In contrast, *Building* has **partial participation** in *BA* only as there might exist some buildings which has no apartment
- **Primary Key:** To uniquely identify any apartment
  - First, building\_no is required to identify the particular building
  - Second, door\_no of the apartment is required to uniquely identify the apartment
- Primary key of Apartment = Primary key of Building + Its own discriminator  
= building\_no + door\_no

# Weak Entity Sets (4): Example

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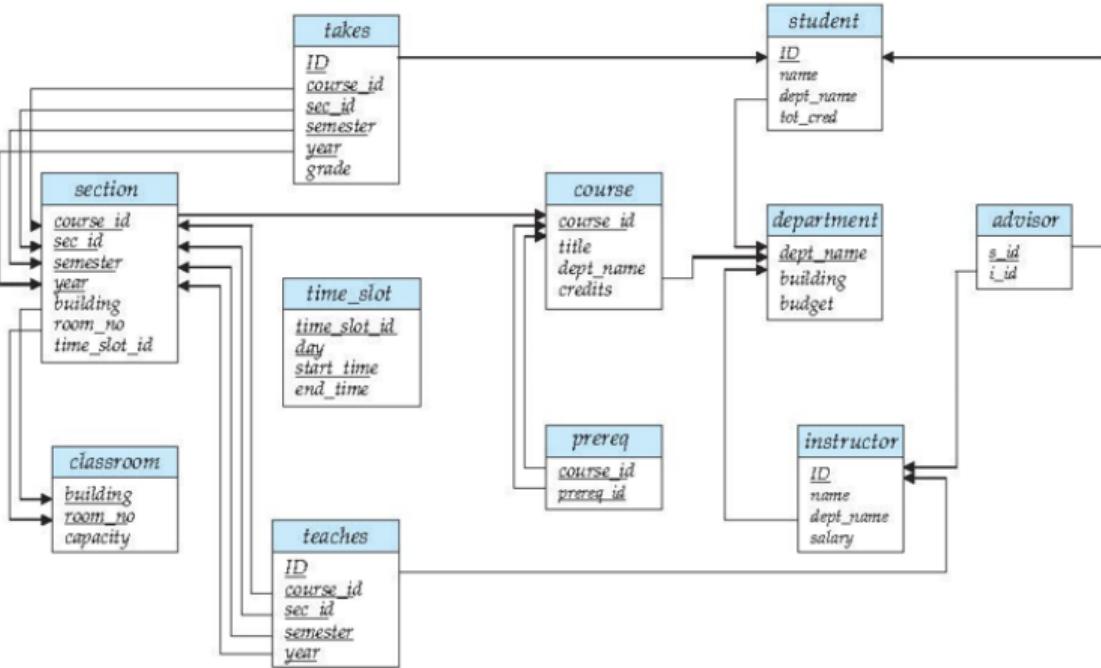
Relationship

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Weak Entity Sets

Module Summary

- Consider a section entity, which is uniquely identified by a *course\_id*, *semester*, *year*, and *sec\_id*.
- Clearly, section entities are related to course entities. Suppose we create a relationship set *sec\_course* between entity sets *section* and *course*.
- Note that the information in *sec\_course* is redundant, since section already has an attribute *course\_id*, which identifies the course with which the section is related.



# Module Summary

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Weak Entity Sets

Module Summary

- Introduced the Design Process for Database Systems
- Elucidated the E-R Model for real world representation with entities, entity sets, attributes, and relationships

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**Edited and new slides are marked with “PPD”.**

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Attributes  
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Module Summary

# Database Management Systems

Module 19: Entity-Relationship Model/2

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## Module 19

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Module Summary

- Design Process for Database Systems
- ER Model for real world representation with entities, entity sets, attributes, and relationships

# Module Objectives

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Module Summary

- To illustrate ER Diagram notation for ER Models
- To explore translation of ER Models to Relational Schemas

# Module Outline

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Module Summary

- ER Diagram
- ER Model to Relational Schema

**Module 19**

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**ER Diagram**

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Module Summary

# ER Diagram

# Entity Sets

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Module Summary

- Entities can be represented graphically as follows:
  - Rectangles represent entity sets.
  - Attributes are listed inside entity rectangle.
  - Underline indicates primary key attributes.

<i>instructor</i>
<u>ID</u>
<i>name</i>
<i>salary</i>

<i>student</i>
<u>ID</u>
<i>name</i>
<i>tot_cred</i>

# Relationship Sets

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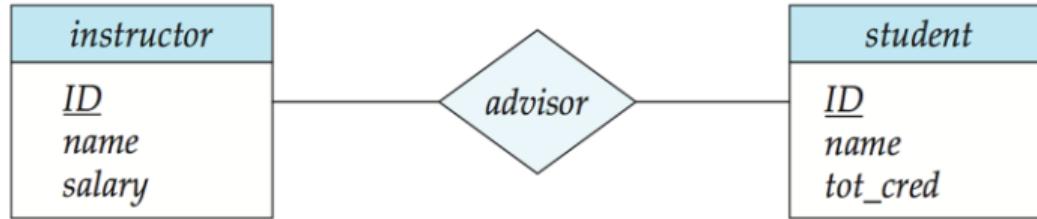
Composite Attributes

Multivalued  
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Module Summary

- Diamonds represent relationship sets.



# Relationship Sets with Attributes

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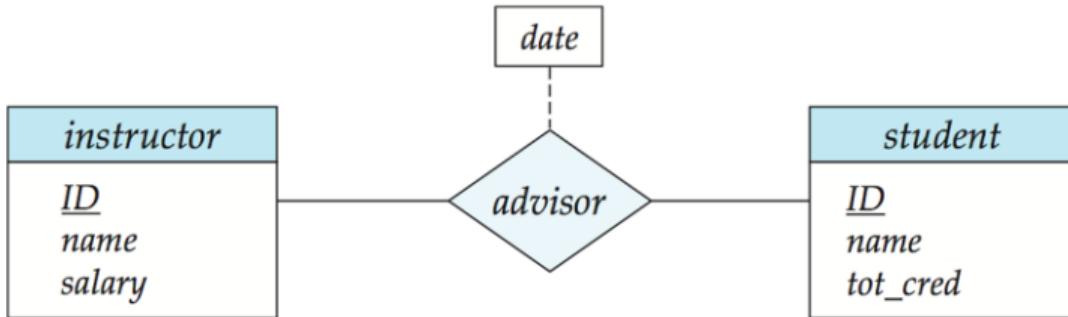
Relationship

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Module Summary



# Roles

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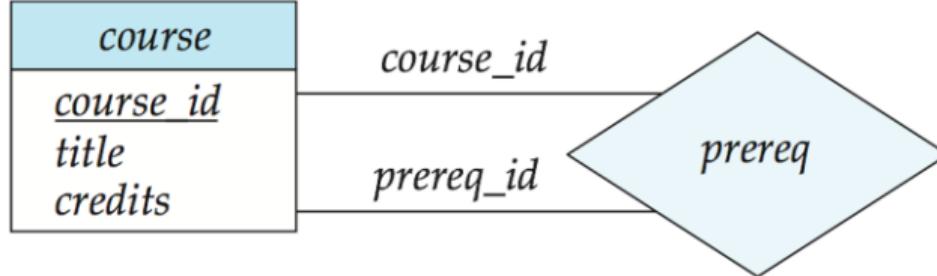
Composite Attributes

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Module Summary

- Entity sets of a relationship need not be distinct. Each occurrence of an entity set plays a “role” in the relationship.
- The labels “*course\_id*” and “*prereq\_id*” are called **roles**.



# Cardinality Constraints

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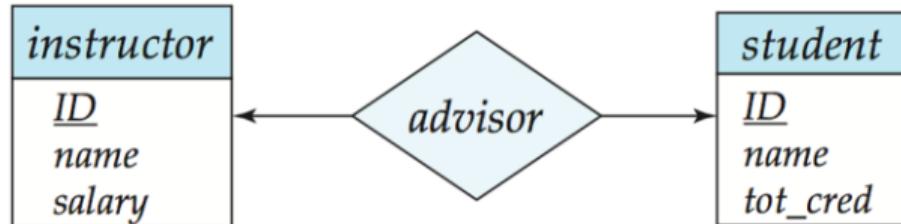
Composite Attributes

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Module Summary

- We express cardinality constraints by drawing either a directed line ( $\rightarrow$ ), signifying “one,” or an undirected line (—), signifying “many,” between the relationship set and the entity set.
- One-to-one relationship between an *instructor* and a *student* :
  - A student is associated with at most one instructor via the relationship *advisor*
  - An instructor is associated with at most one student via the relationship *advisor*



# One-to-Many Relationship

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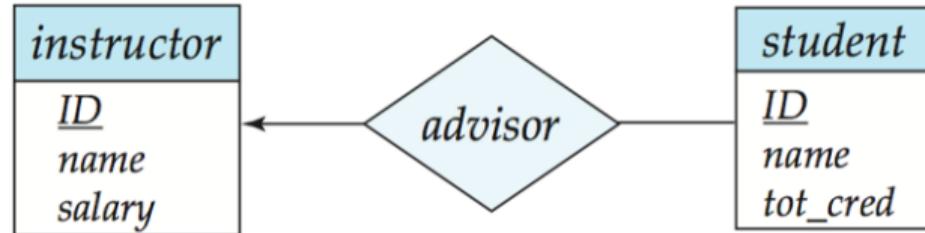
Composite Attributes

Multivalued  
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Redundancy

Module Summary

- one-to-many relationship between an *instructor* and a *student*
  - an instructor is associated with several (including 0) students via advisor
  - a student is associated with at most one instructor via advisor



# Many-to-One Relationships

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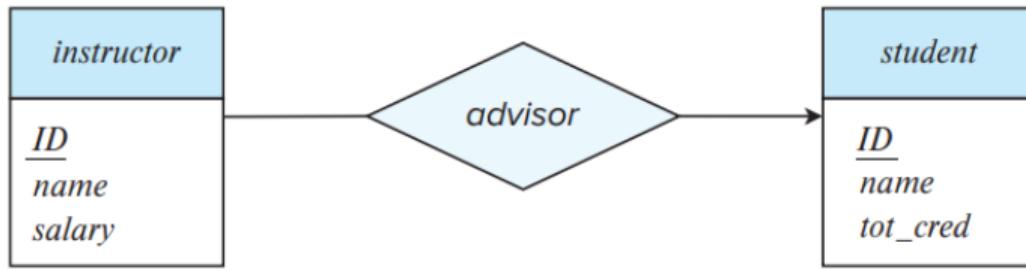
Composite Attributes

Multivalued  
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Redundancy

Module Summary

- many-to-one relationship between a *student* and an *instructor*,
  - an instructor is associated with at most one student via advisor,
  - and a student is associated with several (including 0) instructors via advisor



# Many-to-Many Relationship

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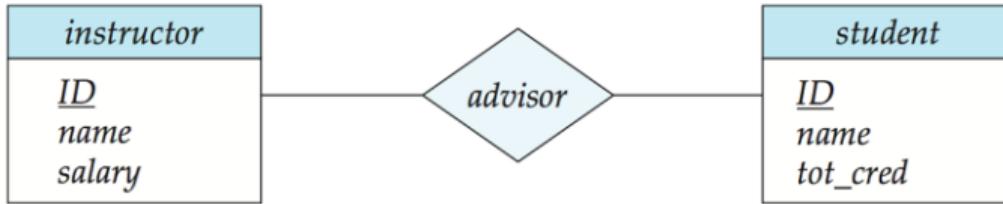
Composite Attributes

Multivalued  
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Redundancy

Module Summary

- An instructor is associated with several (possibly 0) students via *advisor*
- A student is associated with several (possibly 0) instructors via *advisor*



# Total and Partial Participation

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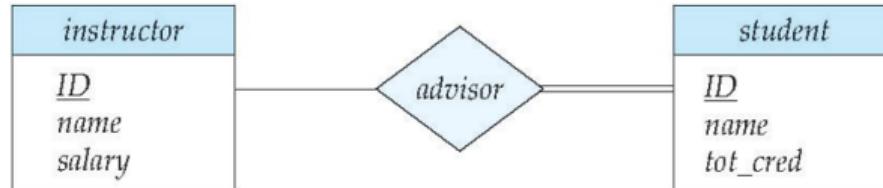
Composite Attributes

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Module Summary

- Total participation (indicated by double line): every entity in the entity set participates in at least one relationship in the relationship set



- participation of *student* in *advisor* relation is total
  - ▷ every *student* must have an associated *instructor*
- Partial participation: some entities may not participate in any relationship in the relationship set
  - Example: participation of *instructor* in *advisor* is partial

# Notation for Expressing More Complex Constraints

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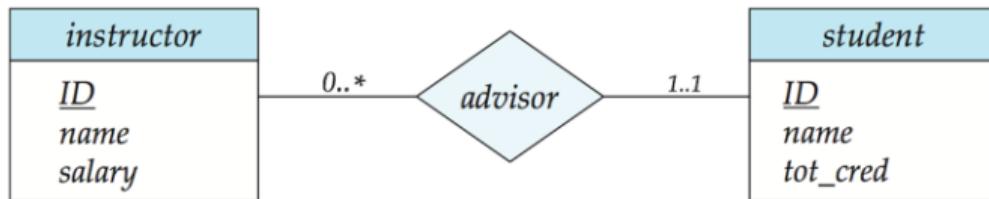
Composite Attributes

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Module Summary

- A line may have an associated minimum and maximum cardinality, shown in the form  $l..h$ , where ***l*** is the minimum and ***h*** the maximum cardinality
  - A minimum value of 1 indicates total participation.
  - A maximum value of 1 indicates that the entity participates in at most one relationship
  - A maximum value of \* indicates no limit.



Instructor can advise 0 or more students.

A student must have 1 advisor; cannot have multiple advisors

# Notation to Express Entity with Complex Attributes

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Module Summary

<i>instructor</i>
<u>ID</u>
<i>name</i>
<i>first_name</i>
<i>middle_initial</i>
<i>last_name</i>
<i>address</i>
<i>street</i>
<i>street_number</i>
<i>street_name</i>
<i>apt_number</i>
<i>city</i>
<i>state</i>
<i>zip</i>
{ <i>phone_number</i> }
<i>date_of_birth</i>
<i>age ()</i>

# Expressing Weak Entity Sets

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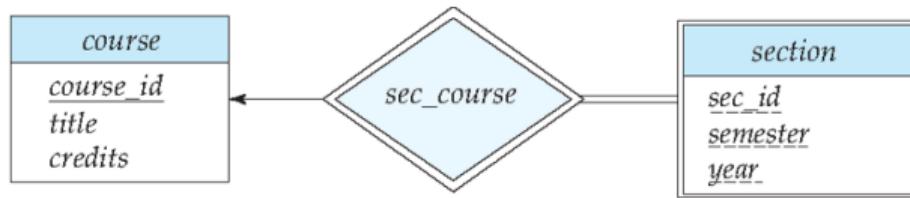
Composite Attributes

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Module Summary

- In ER diagrams, a weak entity set is depicted via a double rectangle
- We underline the discriminator of a weak entity set with a dashed line
- The relationship set connecting the weak entity set to the identifying strong entity set is depicted by a double diamond
- Primary key for *section* – (*course\_id*, *sec\_id*, *semester*, *year*)



# ER Diagram for a University Enterprise

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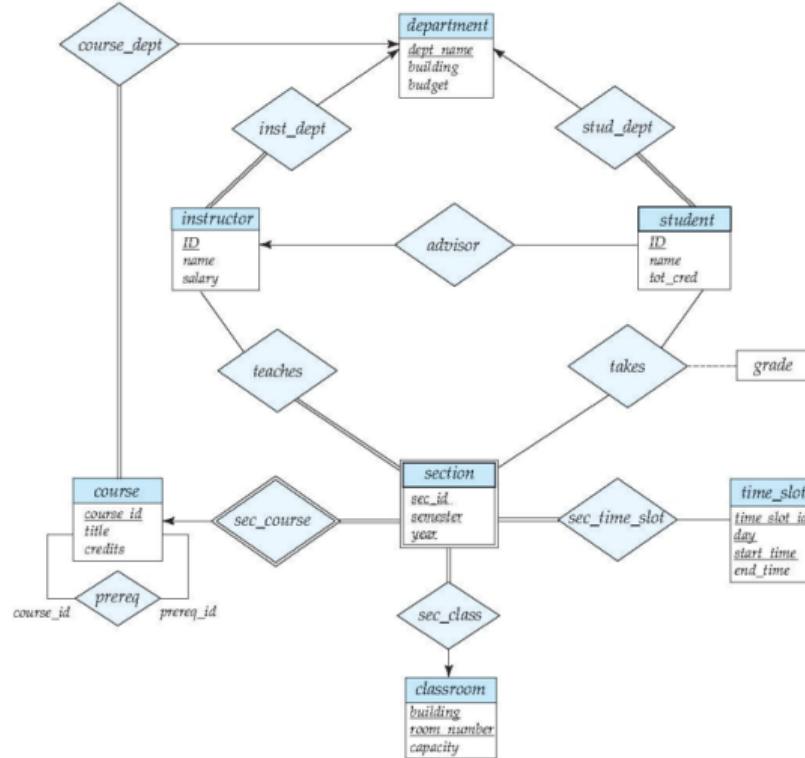
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Module Summary

# ER Model to Relational Schema

# Reduction to Relation Schema

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Module Summary

- Entity sets and relationship sets can be expressed uniformly as *relation schemas* that represent the contents of the database
- A database which conforms to an ER diagram can be represented by a collection of schemas
- For each entity set and relationship set there is a unique schema that is assigned the name of the corresponding entity set or relationship set
- Each schema has a number of columns (generally corresponding to attributes), which have unique names

# Representing Entity Sets

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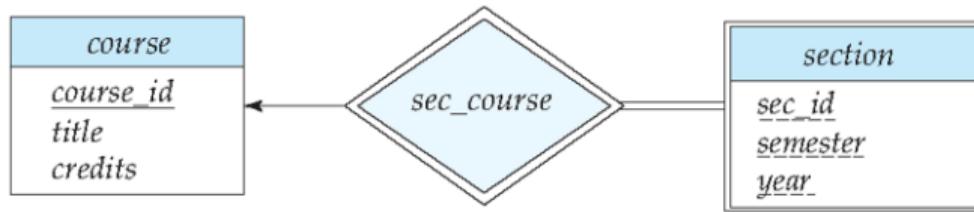
Module Summary

- A strong entity set reduces to a schema with the same attributes

*student(ID, name, tot\_cred)*

- A weak entity set becomes a table that includes a column for the primary key of the identifying strong entity set

*section (course\_id, sec\_id, sem, year )*



# Representing Relationship Sets

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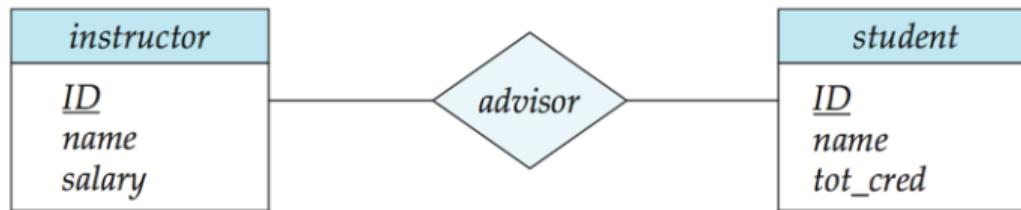
Multivalued  
Attributes

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Module Summary

- A many-to-many relationship set is represented as a schema with attributes for the primary keys of the two participating entity sets, and any descriptive attributes of the relationship set.
- Example: schema for relationship set *advisor*

$$\textit{advisor} = (\underline{s\_id}, \underline{i\_id})$$



# Representation of Entity Sets with Composite Attributes

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Module Summary

instructor
<i>ID</i>
<i>name</i>
<i>first_name</i>
<i>middle_initial</i>
<i>last_name</i>
<i>address</i>
<i>street</i>
<i>street_number</i>
<i>street_name</i>
<i>apt_number</i>
<i>city</i>
<i>state</i>
<i>zip</i>
<i>{phone_number}</i>
<i>date_of_birth</i>
<i>age()</i>

- Composite attributes are flattened out by creating a separate attribute for each component attribute
  - Example: given entity set **instructor** with composite attribute **name** with component attributes **first\_name** and **last\_name** the schema corresponding to the entity set has two attributes **name\_first\_name** and **name\_last\_name**
    - ▷ Prefix omitted if there is no ambiguity (**name\_first\_name** could be **first\_name**)
- Ignoring multivalued attributes, extended instructor schema is
  - **instructor(ID, first\_name, middle\_initial, last\_name, street\_number, street\_name, apt\_number, city, state, zip\_code, date\_of\_birth)**

# Representation of Entity Sets with Multivalued Attributes

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Module Summary

- A multivalued attribute  $M$  of an entity  $E$  is represented by a separate schema  $EM$
- Schema  $EM$  has attributes corresponding to the primary key of  $E$  and an attribute corresponding to multivalued attribute  $M$
- Example: Multivalued attribute `phone_number` of *instructor* is represented by a schema: `inst_phone = ( ID, phone_number )`
- Each value of the multivalued attribute maps to a separate tuple of the relation on schema  $EM$ 
  - For example, an *instructor* entity with primary key 22222 and phone numbers 456-7890 and 123-4567 maps to two tuples: (22222, 456-7890) and (22222, 123-4567)

# Redundancy of Schema

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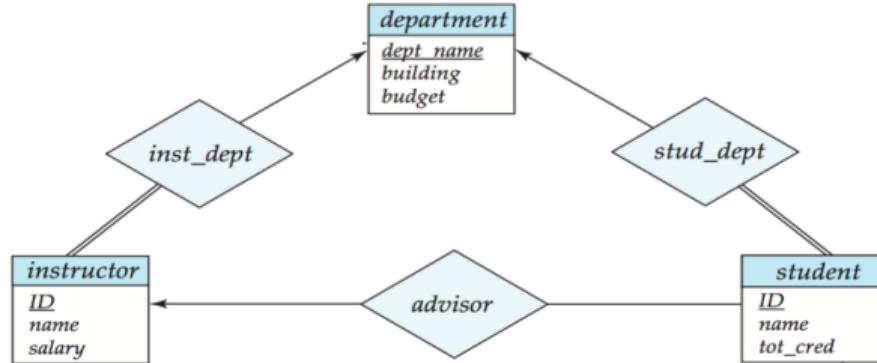
Composite Attributes

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Module Summary

- Many-to-one and one-to-many relationship sets that are total on the many-side can be represented by adding an extra attribute to the “many” side, containing the primary key of the “one” side
- Example: Instead of creating a schema for relationship set *inst\_dept*, add an attribute *dept\_name* to the schema arising from entity set *instructor*



# Redundancy of Schema (2)

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Composite Attributes

Multivalued  
Attributes

Redundancy

Module Summary

- For one-to-one relationship sets, either side can be chosen to act as the “many” side
  - That is, an extra attribute can be added to either of the tables corresponding to the two entity sets
- If participation is *partial* on the “many” side, replacing a schema by an extra attribute in the schema corresponding to the “many” side could result in null values

# Redundancy of Schema (3)

Module 19

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DasObjectives &  
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ER Diagram

Entity Sets

Relationship Sets

Cardinality  
Constraints

Participation

Bounds

ER Model to  
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Entity Sets

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Multivalued  
Attributes

Redundancy

Module Summary

- The schema corresponding to a relationship set linking a weak entity set to its identifying strong entity set is redundant.
- Example: The *section* schema already contains the attributes that would appear in the *sec\_course* schema



# Module Summary

Module 19

Partha Pratim  
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Objectives &  
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ER Diagram

Entity Sets

Relationship Sets

Cardinality  
Constraints

Participation

Bounds

ER Model to  
Relational  
Schema

Entity Sets

Relationship

Composite Attributes

Multivalued  
Attributes

Redundancy

Module Summary

- Illustrated ER Diagram notation for ER Models
- Discussed translation of ER Models to Relational Schema

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**Edited and new slides are marked with “PPD”.**

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Module Summary

# Database Management Systems

Module 20: Entity-Relationship Model/3

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Module 20

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Module Summary

- ER Diagram for ER Models
- Translation of ER Models to Relational Schema

# Module Objectives

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ER Notation

Module Summary

- To understand extended features of ER Model
- To discuss various design issues

# Module Outline

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Module Summary

- Extended ER Features
- Design Issues

# Extended ER Features

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# Extended ER Features

# Non-binary Relationship Sets

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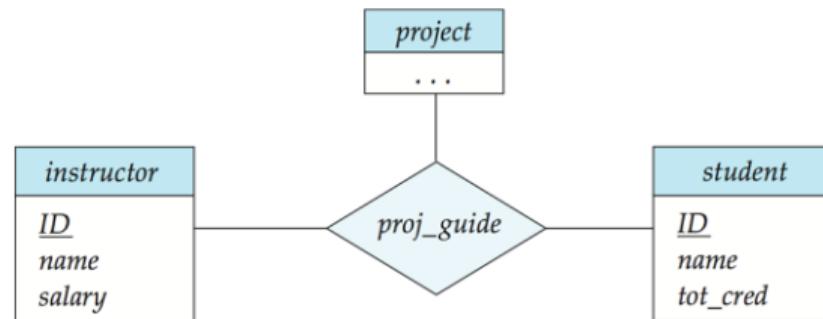
Binary vs Non-Binary

Design Decisions

ER Notation

Module Summary

- Most relationship sets are binary
- There are occasions when it is more convenient to represent relationships as non-binary
- ER Diagram with a Ternary Relationship



# Cardinality Constraints on Ternary Relationship

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ER Notation

Module Summary

- We allow at most one arrow out of a ternary (or greater degree) relationship to indicate a cardinality constraint
- For example, an arrow from *proj\_guide* to *instructor* indicates each student has at most one guide for a project
- If there is more than one arrow, there are two ways of defining the meaning.
  - For example, a ternary relationship R between A, B and C with arrows to B and C could mean
    - a) Each A entity is associated with a unique entity from B and C or
    - b) Each pair of entities from (A, B) is associated with a unique C entity, and each pair (A ,C) is associated with a unique B
  - Each alternative has been used in different formalisms
  - To avoid confusion we outlaw more than one arrow

# Specialization: ISA

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Module Summary

- **Top-down design process:** We designate sub-groupings within an entity set that are distinctive from other entities in the set
- These sub-groupings become lower-level entity sets that have attributes or participate in relationships that do not apply to the higher-level entity set
- Depicted by a *triangle* component labeled ISA (e.g., *instructor* “is a” *person*)
- **Attribute inheritance:** A lower-level entity set inherits all the attributes and relationship participation of the higher-level entity set to which it is linked

# Specialization: ISA (2)

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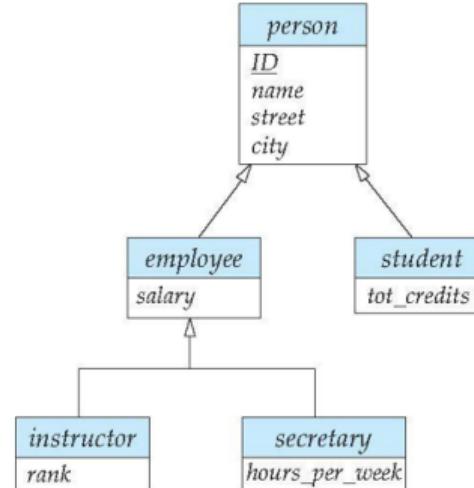
Binary vs Non-Binary

Design Decisions

ER Notation

Module Summary

- **Overlapping:** *employee* and *student*
- **Disjoint:** *instructor* and *secretary*
- Total and Partial



# Representing Specialization via Schema

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ER Notation

Module Summary

- Method 1:

- Form a schema for the higher-level entity
- Form a schema for each lower-level entity set, include primary key of higher-level entity set and local attributes

schema	attributes
person	ID, name, street, city
student	ID, tot_cred
employee	ID, salary

- Drawback: Getting information about, an *employee* requires accessing two relations, the one corresponding to the low-level schema and the one corresponding to the high-level schema

# Representing Specialization as Schema (2)

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ER Notation

Module Summary

- Method 2:

- Form a schema for each entity set with all local and inherited attributes

schema	attributes
person	ID, name, street, city
student	ID, name, street, city, tot_cred
employee	ID, name, street, city, salary

- Drawback: *name*, *street* and *city* may be stored redundantly for people who are both students and employees

# Generalization

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ER Notation

Module Summary

- **Bottom-up design process:** Combine a number of entity sets that share the same features into a higher-level entity set
- Specialization and generalization are simple inversions of each other; they are represented in an ER diagram in the same way
- The terms specialization and generalization are used interchangeably

# Design Constraints on a Specialization / Generalization

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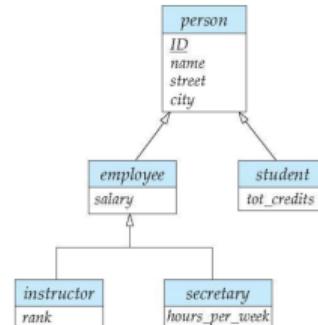
Binary vs Non-Binary

Design Decisions

ER Notation

Module Summary

- **Completeness constraint:** Specifies whether or not an entity in the higher-level entity set must belong to at least one of the lower-level entity sets within a generalization
  - **total:** an entity must belong to one of the lower-level entity sets
  - **partial:** an entity need not belong to one of the lower-level entity sets
- Partial generalization is the default. We can specify total generalization in an ER diagram by adding the keyword **total** in the diagram and drawing a dashed line from the keyword to the corresponding hollow arrow-head to which it applies (for a total generalization), or to the set of hollow arrow-heads to which it applies (for an overlapping generalization).
- The *student* generalization is total. All student entities must be either graduate or undergraduate. Because the higher-level entity set arrived at through generalization is generally composed of only those entities in the lower-level entity sets, the completeness constraint for a generalized higher-level entity set is usually total.



# Aggregation

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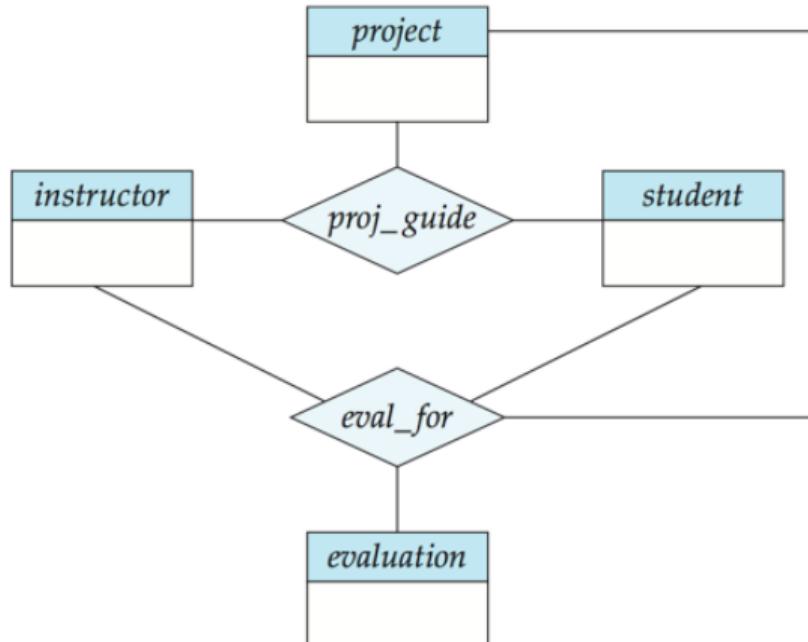
Binary vs Non-Binary

Design Decisions

ER Notation

Module Summary

- Consider the ternary relationship *proj\_guide*, which we saw earlier
- Suppose we want to record evaluations of a student by a guide on a project



# Aggregation (2)

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Design Decisions

ER Notation

Module Summary

- Relationship sets *eval\_for* and *proj\_guide* represent overlapping information
  - Every *eval\_for* relationship corresponds to a *proj\_guide* relationship
  - However, some *proj\_guide* relationships may not correspond to any *eval\_for* relationships
    - ▷ So we cannot discard the *proj\_guide* relationship
- Eliminate this redundancy via *aggregation*
  - Treat relationship as an abstract entity
  - Allows relationships between relationships
  - Abstraction of relationship into new entity

# Aggregation (3)

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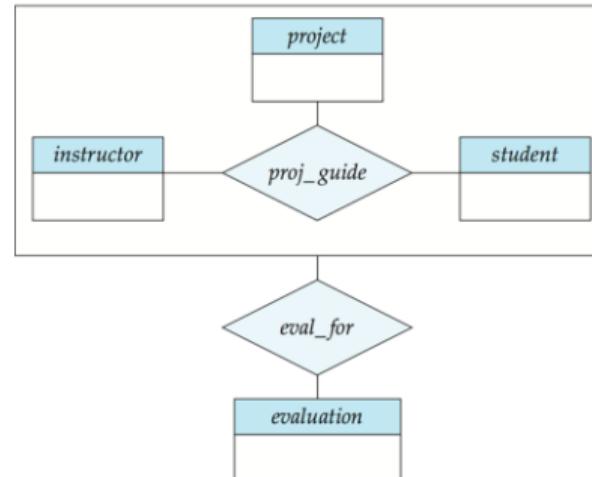
Binary vs Non-Binary

Design Decisions

ER Notation

Module Summary

- Eliminate this redundancy via *aggregation* without introducing redundancy, the following diagram represents:
  - A student is guided by a particular instructor on a particular project
  - A student, instructor, project combination may have an associated evaluation



# Representing Aggregation via Schema

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ER Notation

Module Summary

- To represent aggregation, create a schema containing
  - Primary key of the aggregated relationship,
  - The primary key of the associated entity set
  - Any descriptive attributes
- In our example:
  - The schema  
*textiteval\_for* is:  
$$\text{eval\_for} (s\_ID, project\_id, i\_ID, evaluation\_id)$$
  - The schema *proj\_guide* is redundant

# Design Issues

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## Design Issues

# Entities vs. Attributes

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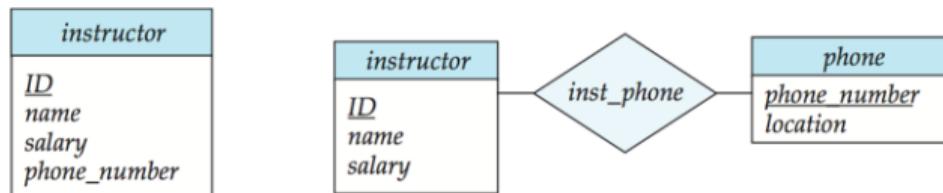
Binary vs Non-Binary

Design Decisions

ER Notation

Module Summary

- Use of entity sets vs. attributes



- Use of phone as an entity allows extra information about phone numbers (plus multiple phone numbers)

# Entities vs Relationship Sets

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ER Notation

Module Summary

- **Use of entity sets vs. relationship sets**

Possible guideline is to designate a relationship set to describe an action that occurs between entities



- **Placement of relationship attributes**

For example, attribute date as attribute of advisor or as attribute of student

# Binary vs Non-Binary Relationships

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Module Summary

- Although it is possible to replace any non-binary ( $n$ -ary, for  $n > 2$ ) relationship set by a number of distinct binary relationship sets, a  $n$ -ary relationship set shows more clearly that several entities participate in a single relationship
- Some relationships that appear to be non-binary may be better represented using binary relationships
  - For example, a ternary relationship *parents*, relating a child to his/her father and mother, is best replaced by two binary relationships, *father* and *mother*
    - ▷ Using two binary relationships allows partial information (e.g., only mother being known)
  - But there are some relationships that are naturally non-binary
    - ▷ Example: *proj-guide*

# Binary vs Non-Binary Relationships (2): Conversion

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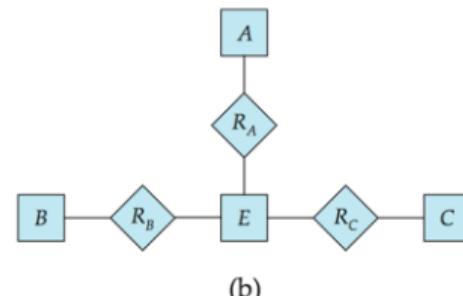
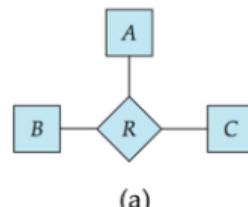
Binary vs Non-Binary

Design Decisions

ER Notation

Module Summary

- In general, any non-binary relationship can be represented using binary relationships by creating an artificial entity set.
  - Replace R between entity sets A, B and C by an entity set E, and three relationship sets:
    1.  $R_A$ , relating E and A
    2.  $R_B$ , relating E and B
    3.  $R_C$ , relating E and C
  - Create an identifying attribute for E and add any attributes of R to E
  - For each relationship  $(a_i, b_i, c_i)$  in R, create
    - a) a new entity  $e_i$  in the entity set E
    - b) add  $(e_i, a_i)$  to  $R_A$
    - c) add  $(e_i, b_i)$  to  $R_B$
    - d) add  $(e_i, c_i)$  to  $R_C$



# Binary vs Non-Binary Relationships (3): Conversion

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Design Decisions

ER Notation

Module Summary

- Also need to translate constraints
  - Translating all constraints may not be possible
  - There may be instances in the translated schema that cannot correspond to any instance of R.
    - ▷ Exercise: *add constraints to the relationships  $R_A$ ,  $R_B$  and  $R_C$  to ensure that a newly created entity corresponds to exactly one entity in each of entity sets —A, B and C*
  - We can avoid creating an identifying attribute by making E, a weak entity set (described shortly) identified by the three relationship sets

# ER Design Decisions

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ER Notation

Module Summary

- The use of an attribute or entity set to represent an object
- Whether a real-world concept is best expressed by an entity set or a relationship set
- The use of a ternary relationship versus a pair of binary relationships
- The use of a strong or weak entity set
- The use of specialization/generalization – contributes to modularity in the design
- The use of aggregation – can treat the aggregate entity set as a single unit without concern for the details of its internal structure

# Symbols Used in ER Notation

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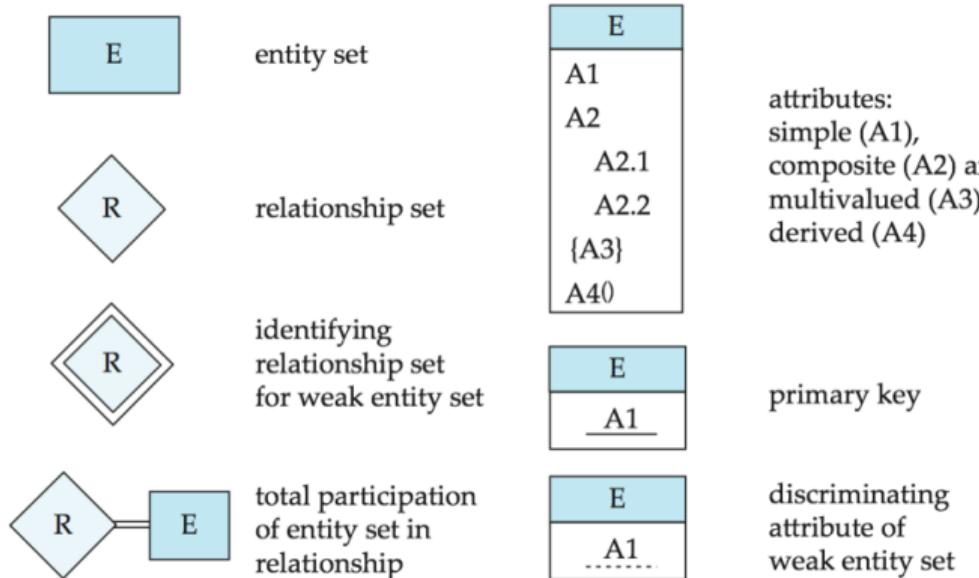
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# Symbols Used in ER Notation (2)

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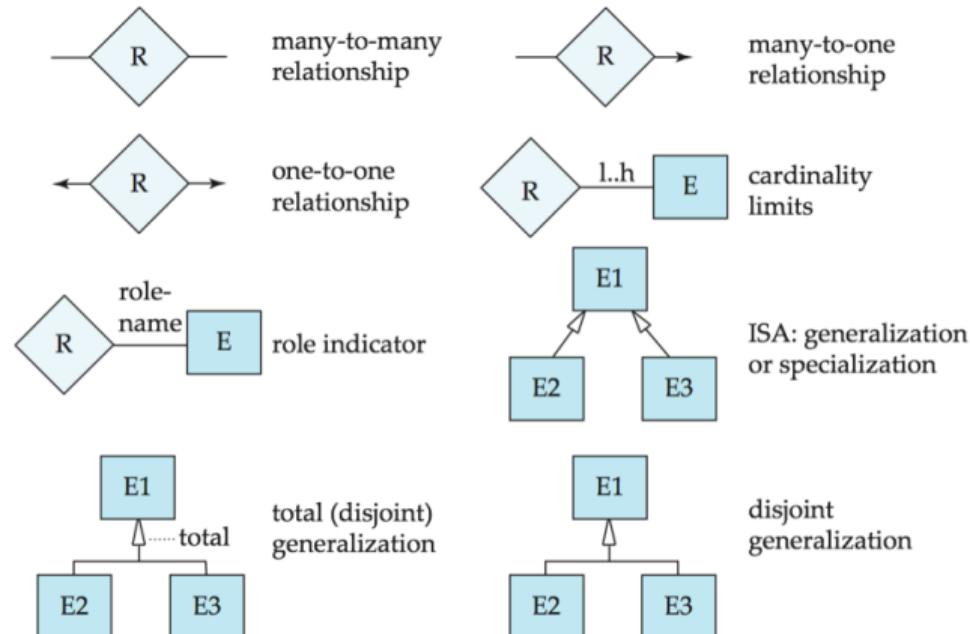
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# Symbols Used in ER Notation (3): Alternate

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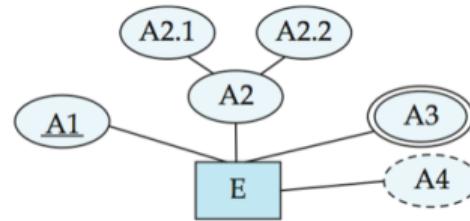
Design Decisions

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Module Summary

- Chen, IDE1FX,...

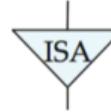
entity set E with  
simple attribute A1,  
composite attribute A2,  
multivalued attribute A3,  
derived attribute A4,  
and primary key A1



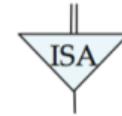
weak entity set



generalization



total  
generalization



# Symbols Used in ER Notation (4): Alternates

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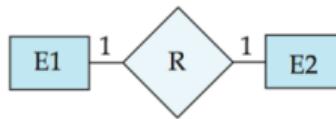
**Chen**

many-to-many  
relationship

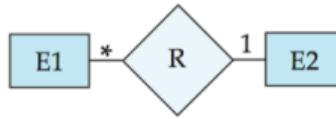


**IDE1FX (Crows feet notation)**

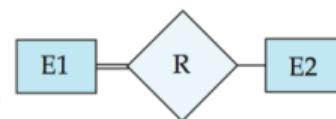
one-to-one  
relationship



many-to-one  
relationship



participation  
in R: total (E1)  
and partial (E2)



# Module Summary

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Module Summary

- Discussed the extended features of ER Model
- Deliberated on various design issues

# Tutorial: TUPLE RELATIONAL CALCULUS

# Introduction

TRC is a nonprocedural query language, where each query is of the form

$$\{t \mid P(t)\}$$

where  $t$  = resulting tuples,

$P(t)$  = known as predicate and these are the conditions that are used to fetch  $t$ .

$P(t)$  may have various conditions logically combined with OR ( $\vee$ ), AND ( $\wedge$ ), NOT( $\neg$ ).

It also uses quantifiers:

$\exists t \in r(Q(t))$  = "there exists" a tuple in  $t$  in relation  $r$  such that predicate  $Q(t)$  is true.

$\forall t \in r(Q(t))$  =  $Q(t)$  is true "for all" tuples in relation  $r$ .

- $\{P \mid \exists S \in Students(S.CGPA > 8 \wedge P.name = S.sname \wedge P.age = S.age)\}$  : returns the name and age of students with a CGPA above 8.

# TRC - Example

Student			
Fname	Lname	Age	Course
David	Sharma	27	DBMS
Aaron	Lilly	17	JAVA
Sahil	Khan	19	Python
Sachin	Rao	20	DBMS
Varun	George	23	JAVA
Simi	Verma	22	JAVA

Q.1 Obtain the first name of students whose age is greater than 21.

**Solution:**

$$\{t.Fname \mid Student(t) \wedge t.age > 21\}$$

$$\{t.Fname \mid t \in Student \wedge t.age > 21\}$$

$$\{t \mid \exists s \in Student(s.age > 21 \wedge t.Fname = s.Fname)\}$$

Fname
David
Varun
Simi

# TRC- Example

Consider the relational schema

**student**(rollNo, name, year, courseld)

**course**(courseld, cname, teacher)

Q.2 Find out the names of all students who have taken the course name 'DBMS'.

- $\{t \mid \exists s \in \text{student} \exists c \in \text{course}(s.\text{courseld} = c.\text{courseld} \wedge c.\text{cname} = \text{'DBMS'} \wedge t.\text{name} = s.\text{name})\}$
- $\{s.\text{name} \mid s \in \text{student} \wedge \exists c \in \text{course}(s.\text{courseld} = c.\text{courseld} \wedge c.\text{cname} = \text{'DBMS'})\}$

Q.3 Find out the names of all students and their rollNo who have taken the course name 'DBMS'.

- $\{s.\text{name}, s.\text{rollNo} \mid s \in \text{student} \wedge \exists c \in \text{course}(s.\text{courseld} = c.\text{courseld} \wedge c.\text{cname} = \text{'DBMS'})\}$
- $\{t \mid \exists s \in \text{student} \exists c \in \text{course}(s.\text{courseld} = c.\text{courseld} \wedge c.\text{cname} = \text{'DBMS'} \wedge t.\text{name} = s.\text{name} \wedge t.\text{rollNo} = s.\text{rollNo})\}$

# TRC - Example

Consider the following relations:

**Flights**(flno, from, to, distance, departs, arrives)

**Aircraft**(aid, aname, cruisingrange)

**Certified**(eid, aid)

**Employees**(eid, ename, salary)

Q.4. Find the eids of pilots certified for Boeing aircraft.

**RA**

$$\Pi_{eid}(\sigma_{aname='Boeing'}(Aircraft \bowtie Certified))$$

**TRC**

- $\{C.eid \mid C \in Certified \wedge \exists A \in Aircraft (A.aid = C.aid \wedge A.aname = 'Boeing')\}$
- $\{T \mid \exists C \in Certified \exists A \in Aircraft (A.aid = C.aid \wedge A.aname = 'Boeing' \wedge T.eid = C.eid)\}$

## TRC - Example(Cont..)

Consider the following relations:

**Flights**(flno, from, to, distance, departs, arrives)

**Aircraft**(aid, aname, cruisingrange)

**Certified**(eid, aid)

**Employees**(eid, ename, salary)

Q.5. Find the names and salaries of certified pilots working on Boeing aircrafts.

**RA**

$$\Pi_{ename, salary}(\sigma_{aname='Boeing'}(Aircraft \bowtie Certified \bowtie Employees))$$

**TRC**

$$\{P \mid \exists E \in Employees \ \exists C \in Certified \ \exists A \in Aircraft (A.aid = C.aid \wedge A.aname = 'Boeing' \wedge E.eid = C.eid \wedge P.ename = E.ename \wedge P.salary = E.salary)\}$$

## TRC - Example(Cont..)

Consider the following relations:

**Flights**(fno, *from*, *to*, *distance*, *departs*, *arrives*)

**Aircraft**(aid, *aname*, *cruisingrange*)

**Certified**(eid, aid)

**Employees**(eid, *ename*, *salary*)

Q.6 Identify the flights that can be piloted by every pilot whose salary is more than \$100,000.

(Hint: The pilot must be certified for at least one plane with a sufficiently large cruising range.)

- $\{F.fno \mid F \in \text{Flights} \wedge \exists A \in \text{Aircraft} \exists C \in \text{Certified} \exists E \in \text{Employees} (A.cruisingrange > F.distance \wedge A.aid = C.aid \wedge E.salary > 100,000 \wedge E.eid = C.eid)\}$

# Tutorial: Case study on E-R diagram

# E-R Diagram

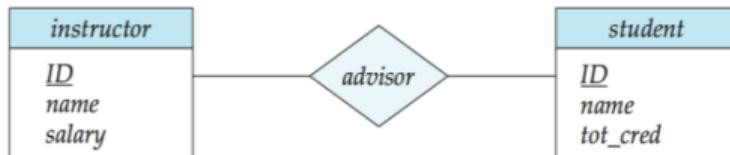
**Entity:** An entity is a “thing” or “object” in the real world that is distinguishable from all other objects.

- An entity is represented by a set of attributes
- An entity set is a set of entities of the same type that share the same properties, or attributes.

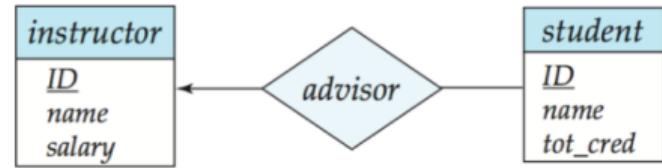
**Relationship:** A relationship is an association among several entities.

- A relationship set is a set of relationships of the same type.

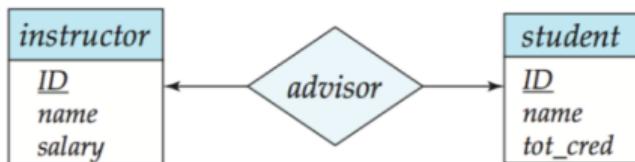
# Mapping Constraints



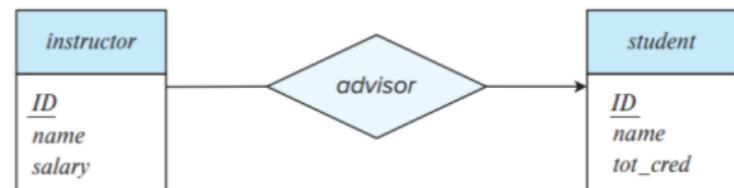
**many-to-many relationship**



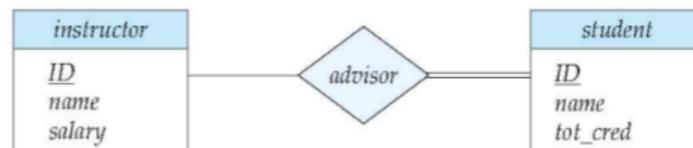
**one-to-many relationship**



**one-to-one relationship**



**many-to-one relationship**

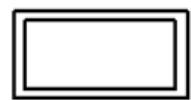


**Total and Partial Participation**

# E-R diagrams symbols



entity class



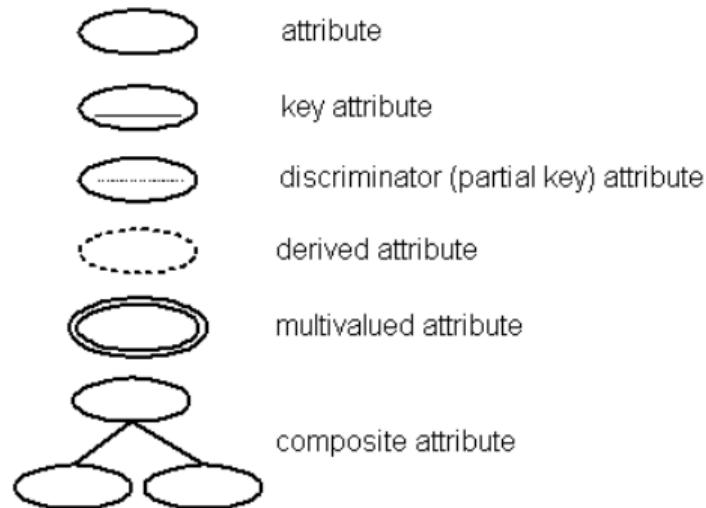
weak entity class



relationship type



identifying relationship type



attribute

key attribute

discriminator (partial key) attribute

derived attribute

multivalued attribute

composite attribute

# Steps to draw E-R diagram

- ① Identify the Entities in ER diagram
- ② Add attributes to each Entity
- ③ Identify the Relationships between Entities
- ④ Add Cardinality to every Relationship

# Case Study

Case Study: The Prescriptions-R-X chain of pharmacies has offered to give you and your two neighbors a free lifetime supply of medicine if you design its database. Given the rising cost of health care, you agree. Here are the requirements:

## Requirements

- Patients are identified by an SSN, and their names, addresses, and ages must be recorded.
- Doctors are identified by an SSN. For each doctor, the name, specialty, and years of experience must be recorded.
- Every patient has a primary physician. Every doctor has at least one patient.
- Doctors prescribe drugs for patients. A doctor could prescribe one or more drugs for several patients, and a patient could obtain prescriptions from several doctors.
- Each prescription has a date and a quantity associated with it. You can assume that if a doctor prescribes the same drug for the same patient more than once, only the last such prescription needs to be stored.
- Each pharmaceutical company is identified by name and has a phone number.
- For each drug, the trade name and formula must be recorded. Each drug is sold by a given pharmaceutical company, and the trade name identifies a drug uniquely from among the products of that company. If a pharmaceutical company is deleted, you need not keep track of its products any longer.
- Each pharmacy has a name, address, and phone number.
- Pharmaceutical companies have long-term contracts with pharmacies. A pharmaceutical company can contract with several pharmacies, and a pharmacy can contract with several pharmaceutical companies. For each contract, you have to store a start date, an end date, and the text of the contract.
- Pharmacies appoint a supervisor for each contract. There must always be a supervisor for each contract, but the contract supervisor can change over the lifetime of the contract.
- Each pharmacy sells several drugs and has a price for each. A drug could be sold at several pharmacies, and the price could vary from one pharmacy to another.