## Translation from OCaml to WhyML

All the auxiliary functions and predicates are total definitions. Fig. 1 and Fig. 2 present the definition of the selected  $\mathsf{OCaml}$  and  $\mathsf{WhyML}$  subsets, respectively. On the  $\mathsf{WhyML}$  side, definition of t which stands for the logical subset of  $\mathsf{WhyML}$ . Cameleer will report a dedicated error message if a user tries to translate an  $\mathsf{OCaml}$  program that syntactically falls out of the supported fragment.

Expressions. Selected OCaml expressions include variables (x ranges over program variables, while f is used for function names), the conditional if..then..else, local bindings of (possibly recursive) expressions, function application, records manipulation (for simplicity, we assume every field to be mutable), treatment of exceptions, loop construction, and finally the assert false expression. Values include numerical and Boolean constants, as well as anonymous functions where arguments are annotated with a ghost status. We only consider functions as valid recursive definitions and application is limited to the application of a function name to a list of arguments. The latter is just to ease our presentation; the former is due to recursive definitions in WhyML being limited to functions. Finally,  $\mathcal A$  notation stands for a (possibly empty) placeholder of OCaml attributes, representing the original place in the expression where

```
:= x \mid \nu \mid \text{ if } e \text{ then } e \text{ else } e \mid \text{ match } e \text{ with } \overline{\parallel p \Rightarrow e}
                                                                                                                                                               Expressions
           | let A x = e A in e
             let \mathcal{A} rec f = e \mathcal{A} and f = e \mathcal{A} in e \mid f \bar{e}
             \{\overline{f=e}\} \mid e.f \mid e.f \leftarrow e
             raise E\bar{e} \mid \text{try } e \text{ with } \overline{E\bar{x} \Rightarrow e}
           \mid while e do \mathcal{A} e done \mid assert false
         ::= |x| \overline{p} | C(p) | p | p | p as x | p : \tau | exception p
                                                                                                                                                                     Patterns
         ::= n \mid \texttt{true} \mid \texttt{false} \mid \texttt{fun} \, \mathcal{A} \, (x\beta) \rightarrow e
                                                                                                                                                                          Values
         ::= reg | ghost
                                                                                                                                                        Ghost attribute
         := \alpha \mid \tau \to \tau \mid \overline{\tau} \mid \overline{\tau} C
                                                                                                                                                       Type expression
                                                                                                                                          Type with ghost status
         ::= exception E:\overline{\pi} \mid \text{type } td \ \overline{\text{and } td}
                                                                                                                                            Top-level declarations
           \mid let \mathcal{A} f = e \mathcal{A} \mid let \mathcal{A} \operatorname{rec} f = e \mathcal{A} \overline{\operatorname{and} f = e \mathcal{A}}
           \mid module \mathcal{M}=m
         ::= \overline{\alpha} T \mid \overline{\alpha} T = \tau \mid \overline{\alpha} T = \{ \overline{f : \pi} \} \mathcal{A} \mid \overline{\alpha} T = \overline{\| C \circ \overline{\tau} \|}
td
                                                                                                                                                         Type definition
         ::= struct \overline{d} end | functor(\mathcal{X}:mt) \rightarrow m
                                                                                                                                                                      Modules
        ::= \operatorname{\mathtt{sig}} \overline{s} \operatorname{\mathtt{end}}
                                                                                                                                                            Module types
mt
         ::= \operatorname{val} A f : \pi A \mid \operatorname{type} td \overline{\operatorname{and} td}
                                                                                                                                                                  Signatures
         := \overline{d}
                                                                                                                                                                     Program
```

Figure 1: Syntax of core OCaml.

```
:= x \mid \nu \mid \text{ if } e \text{ then } e \text{ else } e \mid \text{ match } e \text{ with } \overline{\mid p \Rightarrow e} \text{ end}
                                                                                                                                                           Expressions
        | let \mathcal{K} \beta x = e in e
         |\operatorname{rec} \mathcal{K} f(\overline{\beta x}) \mathcal{S} = e \text{ with } \mathcal{K} f(\overline{\beta x}) = e \mathcal{S} \text{ in } e | f \overline{e}
         \mid \{\overline{f=e}\} \mid e.f \mid e.f \leftarrow e
            raise E\bar{e} \mid {\sf try} \ e \ {\sf with} \ \overline{E\bar{x} \Rightarrow e} \ {\sf end}
         \mid while e do \mathcal{I} e done \mid absurd \mid ghost e
       ::= |x| \overline{p} | Cp | p | p | p as x | p : \tau | exception p
                                                                                                                                                                 Patterns
       := n \mid \mathsf{true} \mid \mathsf{false} \mid \mathsf{fun} \, \mathcal{K} \, (\overline{\beta x}) \, \mathcal{S} \to e
                                                                                                                                                                     Values
      ::= reg | ghost
                                                                                                                                                         Ghost status
      := \alpha \mid \tau \to \tau \mid \overline{\tau} \mid C\overline{\tau}
                                                                                                                                                  Type expression
       ::= \beta \tau
                                                                                                                                     Type with ghost status
\mathcal{K}
     ::= reg | logic
                                                                                                                                                      Function kind
      ::= requires ar{t} ensures ar{t} variant ar{t}
                                                                                                                                       Function specification
       ::= invariant ar{t} variant ar{t}
                                                                                                                                               Loop specification
      ::= exception E:\overline{\pi}\mid type td with td
                                                                                                                                       Top-level declarations
        | let \mathcal{K} f = e
         | let rec \mathcal{K} f(\overline{\beta x}) \mathcal{S} = e with \mathcal{K} f(\overline{\beta x}) \mathcal{S} = e
         \mid val \mathcal{K} \ \beta f(\overline{x:\pi}) \ \mathcal{S} : \pi \mid scope \mathcal{M} \ \overline{d} end
      ::= \ T\overline{\alpha} \ | \ T\overline{\alpha} = \tau \ | \ T\overline{\alpha} = \{ \ \overline{f:\pi} \ \} \ \text{invariant} \ \overline{t} \ | \ T\overline{\alpha} = \overline{\left[\!\!\left[ \ C \ \overline{\tau} \right.\right]}
                                                                                                                                                    Type definition
       := module \mathcal{M} \overline{d} end
                                                                                                                                                                Program
```

Figure 2: Syntax of core WhyML.

GOSPEL elements are introduced. For instance, the first  $\mathcal{A}$  in a let.rec expression can contain the [@ghost] and [@logic] attribute, while the second one stands for the function specification. We omit the definition of  $\tau$  and t, respectively from the OCaml and the WhyML sides. The former stands for the grammar of OCaml types, while the latter is the logical subset of WhyML.

Top-level declarations. Selected top-level declarations include exceptions and type declaration, (mutually-recursive) function definition, and introduction of sub-modules. An exception takes a list of  $\pi$  values, types annotated with a ghost status, to account for the possibility of ghost arguments. In Why3 vocabulary, this is the mask of an exception. The attribute  $\mathcal{A}$  after a record type definition is used to express in GOSPEL a type invariant, i.e., a predicate that every inhabitant of such type must satisfy. Type invariants are readily supported by Why3, as depicted in rule (TDRECORD) in Fig. 5. Each field of the record type is also annotated with a ghost status.

Modules. The most interesting cases in our translation is how we deal with the modules language from the OCaml side. A WhyML program is a list of modules, a module is a list of top-level declarations, and declarations can be organized within scopes.

$$(\text{EFasurd}) = \frac{\text{assert false superassion absurd}}{\text{assert false superassion absurd}}$$

$$(\text{EFun}) = \frac{\text{phost}(A) = \beta - A \text{ function spec } S - e \text{ superassion } e'}{\text{fun } Ax \to e \text{ superassion } \text{fun } (\beta x) S = e'} = \frac{z \text{ superassion } e'}{f \epsilon \text{ superassion } f e'} (\text{EApp})$$

$$(\text{ERec})$$

$$= \frac{1}{\text{superassion } \beta y, e'_1} - \frac{1}{A_2} \text{ function spec } S_1 - e_0 \text{ function } x \beta, e'_0}{\epsilon 1 \text{ function } \beta y, e'_1} - \frac{1}{A_2} \text{ function spec } S_1 - e_0 \text{ function } x \beta, e'_0}{\epsilon 1 \text{ function } \beta y, e'_1} - \frac{1}{A_2} \text{ function spec } S_1 - e_0 \text{ function } x \beta, e'_0}{\epsilon 1 \text{ function } \beta y, e'_1} - \frac{1}{A_2} \text{ function spec } S_1 - e_0 \text{ function } x \beta, e'_0}{\epsilon 1 \text{ function } \beta y, e'_1} - \frac{1}{A_2} \text{ function spec } S_1 - e_0 \text{ function } x \beta, e'_0}{\epsilon 1 \text{ function } \beta y, e'_1} - \frac{1}{A_2} \text{ function spec } S_2 - e_2 \text{ expression } e'_2}{\epsilon 1 \text{ function } \beta y, e'_1} - \frac{1}{A_2} \text{ function spec } S_2 - e_2 \text{ expression } e'_2}{\epsilon 1 \text{ function } \beta y, e'_1} - \frac{1}{A_2} \text{ function spec } S_2 - e_2 \text{ expression } e'_2}{\epsilon 1 \text{ function } \beta y, e'_1} - \frac{1}{A_2} \text{ function spec } S_2 - e_2 \text{ expression } e'_2}{\epsilon 1 \text{ function } \beta y, e'_1} - \frac{1}{A_2} \text{ function spec } S_2 - e_2 \text{ expression } e'_2}{\epsilon 1 \text{ function } \beta y, e'_1} - \frac{1}{A_2} \text{ function } \delta y, e'_2}{\epsilon 1 \text{ function } \delta y, e'_1} - \frac{1}{A_2} \text{ function } \delta y, e'_2}{\epsilon 1 \text{ function } \delta y, e'_1} - \frac{1}{A_2} \text{ function } \delta y, e'_2}{\epsilon 1 \text{ function } \delta y, e'_1} - \frac{1}{A_2} \text{ function } \delta y, e'_2}{\epsilon 1 \text{ function } \delta y, e'_1} - \frac{1}{A_2} \text{ function } \delta y, e'_2}{\epsilon 1 \text{ function } \delta y, e'_1} - \frac{1}{A_2} \text{ function } \delta y, e'_2}{\epsilon 1 \text{ function } \delta y, e'_1} - \frac{1}{A_2} \text{ function } \delta y, e'_2}{\epsilon 1 \text{ function } \delta y, e'_1} - \frac{1}{A_2} \text{ function } \delta y, e'_2}{\epsilon 1 \text{ function } \delta y, e'_1} - \frac{1}{A_2} \text{ function } \delta y, e'_2}{\epsilon 1 \text{ function } \delta y, e'_1} - \frac{1}{A_2} \text{ function } \delta y, e'_2}{\epsilon 1 \text{ function } \delta y, e'_2} - \frac{1}{A_2} \text{ function } \delta y, e'_2}{\epsilon 1 \text{ function } \delta y, e'_2} - \frac{1}{A_2} \text{ function } \delta y, e'_2}{\epsilon 1 \text{ fu$$

Figure 3: Translation of OCaml expressions into WhyML.

The first module expression we take into account is the struct..end construction. This is translated into a WhyML declarations, as depicted in rule (MSTRUCT) (Appendix C). We note this does not change the structure and code organization of the original program, since a struct..end expression follows a module declaration. Hence, a declaration of the form module  $\mathcal{M}$   $\bar{d}$  end is translated into scope  $\mathcal{M}$   $\bar{d}$  end.

Functors are a central notion when programming in OCaml, so it is out of question to develop a verification tool for OCaml without a (at least minimal) support for functors. WhyML does not feature a syntactic construction for functors; instead, these are represented as modules containing only abstract symbols [?]. Thus, we propose the following translation rule:

$$(\text{MFUNCTOR}) \; \frac{mt \; \stackrel{\textit{module type}}{\longrightarrow} \; \overline{d} \qquad m \; \stackrel{\textit{module}}{\longrightarrow} \; \overline{d'}}{\mathsf{functor}(\mathcal{X}:mt) \to m \; \stackrel{\textit{module}}{\longrightarrow} \; \mathsf{scope} \; \mathcal{X} \; \overline{d} \; \mathsf{end} \; \overline{d'}}$$

Each functor expression is translated into a WhyML scope followed by a list of declarations. For instance, the OCaml functor module Make = functor (X: ...) -> struct ... end, is translated into the following WhyML excerpt: scope Make scope X ... end ... end. The given transformation is the dual of what is actually implemented in the Why3 extraction machinery: every WhyML expression of the form scope A scope B ... is translated into module A (B: ...) ..., as long as scope B features only abstract symbols.

Signatures. The argument of a functor is expressed as a module type, i.e., a signature of the form sig..end. This encapsulates a list of declarations belonging to the OCaml signature language, which are translated into a list of WhyML expressions, according to rule (MTSIG) (Appendix C). Contrarily to OCaml, WhyML does not impose a separation between signature (interface) and structure (implementation) elements. In particular, the WhyML surface language allows one to include non-defined val functions and regular let definitions in the same namespace. We give the following translation rule for val declarations:

$$(\text{SVal}) \xrightarrow{\neg is\_ghost(\mathcal{A})} \frac{kind(\mathcal{A}) = \mathcal{K}}{kind(\mathcal{A}) = \mathcal{K}} \underbrace{\mathcal{A}' \xrightarrow{function \ spec} \mathcal{S}}_{\text{val} \ \mathcal{A} \ f: \pi \ \mathcal{A}'} \underbrace{\pi' \xrightarrow{function \ args}}_{\text{val} \ \mathcal{K} \ f(\overline{x} : \overline{\pi})} \mathcal{S} : \pi_{res}$$

The name of the arguments are retrieved from the function specification (Sec. ?? features an example of such case). Non-defined functions can also be declared as ghost and/or logical functions. For brevity, the case of ghost val is omitted. The complete set of translation rule for signature items can be found in Appendix D.

**Programs.** An OCaml program is simply a list of top-level declarations. These are translated into a WhyML module, as follows:

$$(\text{Program}) \ \frac{\overline{d} \ \underline{declaration} \ \overline{d'}}{\overline{d} \ \underline{program} \ \text{module} \ \mathcal{M} \ \overline{d'} \ \text{end}}$$

The name  $\mathcal{M}$  of the generated module is issued from the OCaml file that contains the original program. If file foo.ml contains the program p, it gets translated into module Foo p end. In summary, we generate a WhyML program containing a single module, which represents the top-level module of an OCaml file. In turn, each sub-module is translated into a WhyML scope, with a special treatment for functorial definitions.

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# A Translation of expressions

#### B Translation of top-level declarations and type definitions

$$(\text{DModule}) \frac{m \ \textit{module} \ \vec{d}}{\text{module} \ M = m \ \textit{declaration} \ \text{scope} \ M \ \vec{d} \ \text{end}}$$

$$is\_\textit{ghost}(A) \quad kind(A') = K \quad is\_\textit{functional}(e)$$

$$A \ \textit{function spec} \ S \quad e \ \textit{function} \ \vec{\beta} \vec{x}, e'$$

$$\text{let } A \ f = e \ A' \ \textit{declaration} \ \text{let } f \ K = \text{fun}(\vec{\beta} x) \ S \rightarrow \text{ghost } e'$$

$$(\text{DLET}) \frac{A \ \textit{function spec} \ S \quad e \ \textit{functional}(e)}{1 \text{let } A \ f = e \ A' \ \textit{declaration} \ \text{let } f \ K = \text{fun}(\vec{\beta} x) \ S \rightarrow \text{ghost } e'}$$

$$(\text{DREC}) \frac{A \ \textit{function spec} \ S \quad e \ \textit{function} \ \vec{\beta} \vec{x}, e'}{1 \text{let } A \ f = e \ A' \ \textit{declaration} \ \text{let } f \ K = \text{fun}(\vec{\beta} x) \ S \rightarrow e'}$$

$$(\text{DREC}) \frac{A \ \textit{function spec} \ S_1 \quad e_0 \quad \textit{function} \ \vec{x} \vec{\beta}, e'_0}{1 \text{let } A_0 \ \text{rec } f_0 = e_0 \ A_1 \ \text{and } f_1 = e_1 \ A_2 \ \textit{declaration} \ \text{rec } K \ f(\vec{\beta} x) \ S_1 = e'_0 \ \text{with } K \ f_1(\vec{y} : \vec{\pi}) = e'_1 \ S_2}$$

$$(\text{DRECGHOST}) \frac{is\_\textit{ghost}(A_0) \quad kind(A_0) = K \quad A_1 \quad \textit{function spec} \ S_2}{1 \quad \text{function spec} \ S_2}$$

$$\text{let } A_0 \ \text{rec } f_0 = e_0 \ A_1 \ \text{and } f_1 = e_1 \ A_2 \ \textit{declaration} \ \text{rec } K \ f(\vec{\beta} x) \ S_1 = \text{ghost } e'_0 \ \text{with } K \ f_1(\vec{y} : \vec{\pi}) = e'_1 \ S_2}$$

$$\text{let } A_0 \ \text{rec } f_0 = e_0 \ A_1 \ \text{and } f_1 = e_1 \ A_2 \ \textit{declaration} \ \text{rec } K \ f(\vec{\beta} x) \ S_1 = \text{ghost } e'_0 \ \text{with } K \ f_1(\vec{y} : \vec{\pi}) = e'_1 \ S_2}$$

$$\text{let } A_0 \ \text{rec } f_0 = e_0 \ A_1 \ \text{and } f_1 = e_1 \ A_2 \ \textit{declaration} \ \text{rec } K \ f(\vec{\beta} x) \ S_1 = \text{ghost } e'_0 \ \text{with } K \ f_1(\vec{y} : \vec{\pi}) = e'_1 \ S_2}$$

$$\text{(DType)} \quad \frac{td_0 \ \textit{type definition}}{type \ td_0 \ \text{and } td_1 \ \textit{declaration} \ \text{type } td'_0 \ \text{with } td'_1} \ \text{type } td'_0 \ \text{with } td'_1}$$

$$\text{(DEXN)} \quad \frac{e^{-1} \ declaration}{e^{-1} \ \text{exception } E : \vec{\pi} \ \textit{declaration} \ \text{exception } E : \vec{\pi} \ \textit{declaration} \ \text{exception } E : \vec{\pi}$$

Figure 4: Translation of OCaml top-level declarations into WhyML.

$$(\text{TDAbstract}) \xrightarrow{\overline{\alpha} \, T \, \text{type definition } \, T\overline{\alpha}} \qquad \overline{\alpha} \, T = \tau \, \text{type definition } \, T\overline{\alpha} = \tau \, \text{(TDAlias)}$$

$$(\text{TDRecord}) \, \xrightarrow{\overline{\alpha} \, T = \{\, \overline{f} : \overline{\pi} \,\} \, A \, \text{declaration } \, T\overline{\alpha} = \{\, \overline{f} : \overline{\pi} \,\} \, \text{invariant } \overline{t}}$$

$$(\text{TDVARIANT}) \, \xrightarrow{\overline{\alpha} \, T = \, \overline{\parallel} \, C \, \text{of } \, \overline{\tau} \, \text{type definition } \, T\overline{\alpha} = \, \overline{\parallel} \, C \, \overline{\tau}}$$

Figure 5: Translation of OCaml type definitions into WhyML.

## C Translation of module expressions and module types

$$(\text{MSTRUCT}) \frac{\overline{d} \stackrel{declaration}{\longrightarrow} \overline{d'}}{\text{struct } \overline{d} \text{ end } \stackrel{module}{\longrightarrow} \overline{d'}}$$

$$(\text{MFUNCTOR}) \frac{mt \stackrel{module}{\longrightarrow} type}{\overline{d}} \overline{d} \qquad m \stackrel{module}{\longrightarrow} \overline{d'}}{\text{functor}(\mathcal{X}:mt) \to m \stackrel{module}{\longrightarrow} \text{scope } \mathcal{X} \overline{d} \text{ end } \overline{d'}}$$

$$(\text{MTSIG}) \frac{\overline{s} \stackrel{signature}{\longrightarrow} \overline{d}}{\text{sig } s \text{ end } \stackrel{module}{\longrightarrow} type} \overline{d}}$$

Figure 6: Translation of OCaml module expressions and module types into WhyML.

## D Translation of signatures

$$(SVAL) \xrightarrow{A' \xrightarrow{function \ spec} \mathcal{S} \qquad \pi, A' \xrightarrow{function \ args} \overline{x : \pi'}, \pi_{res}}$$

$$val \ Af : \pi \ A' \xrightarrow{signature} val \ K f(\overline{x : \pi}) \ \mathcal{S} : \pi_{res}$$

$$\xrightarrow{\neg is\_ghost}(A) \qquad kind(A) = K$$

$$(SVALGHOST) \xrightarrow{A' \xrightarrow{function \ spec} \mathcal{S} \qquad \pi, A' \xrightarrow{function \ args} \overline{x : \pi'}, \pi_{res}}$$

$$val \ Af : \pi \ A' \xrightarrow{signature} val \ K \ ghost f(\overline{x : \pi}) \ \mathcal{S} : \pi_{res}$$

$$(STYPE) \xrightarrow{td_0 \xrightarrow{type \ definition} td'_0} td'_0 \xrightarrow{td_1} \xrightarrow{type \ definition} td'_1}$$

$$type \ td_0 \ \overline{and} \ td_1 \xrightarrow{signature} type \ td'_0 \ \overline{with} \ td'_1$$

Figure 7: Translation of OCaml signatures into WhyML.