

Consider the problem

$$f(u, v, p, n) = (v - pn) + 2 \frac{\|v - (v - pn)\|}{\|u - (v - pn)\|} \cdot (u - (v - pn)) \quad (1)$$

and the following substitutions

$$\begin{aligned} a &= v - pn & b &= v - a & c &= u - a & d &= b/c \\ e &= \|d\| = \sqrt{d^T d} = \sqrt{f} & f &= d^T d = d \cdot d & z &= a + 2ce \end{aligned}$$

Since

$$\begin{aligned} a' &= v' - (p'n + pn') & b' &= v' - a' & c' &= u' - a' & d' &= \frac{b'c - bc'}{c^2} \\ e' &= \frac{f'}{2e} & f' &= 2d'd & z' &= a' + 2(c'e + ce') \end{aligned}$$

we have

$$\begin{aligned} f'(u, v, p, n) &= a' + 2(c'e + ce') \\ &= a' + 2 \left((u' - a')e + c \left(\frac{f'}{2e} \right) \right) \\ &= a' + 2 \left((u' - a')e + c \left(\frac{2d'd}{2e} \right) \right) \\ &= a' + 2 \left((u' - a')e + c \left(\frac{2 \left(\frac{b'c - bc'}{c^2} \right) d}{2e} \right) \right) \\ &= a' + 2 \left((u' - a')e + c \left(\frac{2 \left(\frac{(v' - a')c - b(u' - a')}{c^2} \right) d}{2e} \right) \right) \end{aligned}$$