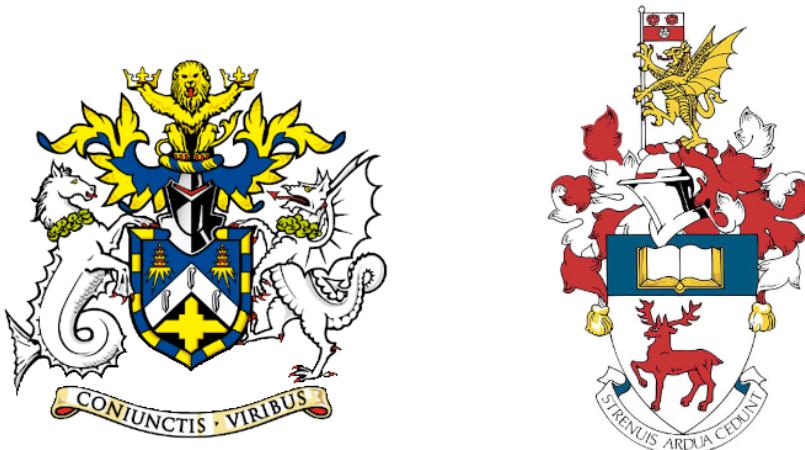


¹ ADVANCING NEUTRINO
² DETECTION AND TRIGGERING IN
³ DUNE



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⁷ of the Degree of Doctor of Philosophy

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13

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Abstract

31

32 Work in progress ...

¡Oh memoria, enemiga mortal de mi descanso!

El ingenioso hidalgo don Quijote de la Mancha

MIGUEL DE CERVANTES SAAVEDRA

Acknowledgements

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List of Abbreviations

ADC	Analog to Digital Converter.
ALEPH	Apparatus for LEP PHysics.
ALICE	A Large Ion Collider Experiment.
BDT	Boosted Decision Tree.
CC	Charged Current.
DM	Dark Matter.
DUNE	Deep Underground Neutrino Experiment.
ECal	Electromagnetic Calorimeter.
FD	Far Detector.
FHC	Forward Horn Current.
HPgTPC	High Pressure gaseous Time Projection Chamber.
LBL	Long BaseLine.
MuID	Muon IDentification system.
NC	Neutral Current.
ND	Near Detector.
ND-GAr	Near Detector Gaseous Argon.
ND-LAr	Near Detector Liquid Argon.
PDG	Particle Data Group.
RHC	Reverse Horn Current.

1

600

Introduction

601

602

603

Neutrino physics

604 *Little particles of inspiration sleet through the universe all the time traveling
605 through the densest matter in the same way that a neutrino passes through a
606 candyfloss haystack, and most of them miss.*

607

– Terry Pratchett, *Sourcery*

608 Ever since they were postulated in 1930 by Wolfgang Pauli to explain the continuous
609 β decay spectrum [15] and later found by F. Reines and C. Cowan at the Savannah
610 River reactor in 1953 [16], neutrinos have had a special place among all other elementary
611 particles. They provide a unique way to probe a wide range of quite different physics,
612 from nuclear physics to cosmology, from astrophysics to colliders. Moreover, there is
613 compelling evidence to believe that the study of neutrinos may be key to unveil different
614 aspects of physics beyond the SM, difficult to test elsewhere.

615 In this Chapter, I will review the basics of neutrino physics, from its role within the
616 SM to the main open questions related to the neutrino sector, paying special attention
617 to the phenomenology of neutrino oscillations.

618 2.1 Neutrinos in the SM

619 The SM of fundamental interactions was initially proposed in 1967 by S. Glashow, S.
620 Weinberg and A. Salam[17–19]. This theoretical framework describes the dynamics
621 of leptons and quarks, by introducing a collection of mediating gauge vector bosons
622 and one scalar particle, known as the Higgs boson. It assumes that the local $SU(3) \times$

CHAPTER 2. NEUTRINO PHYSICS

623 $SU(2)_L \times U(1)_Y$ gauge symmetry is an internal symmetry of the system, with $SU(3)$
624 describing quantum chromodynamics, and $SU(2)_L \times U(1)_Y$ being the gauge groups of
625 the electroweak sector. For a detailed overview of the SM of electroweak interactions,
626 see Ref. [20].

627 In the SM, neutrinos appear in three flavours, namely ν_e , ν_μ , and ν_τ . These are
628 associated with the corresponding charged leptons, e , μ , and τ . Neutrinos exist only
629 as left-handed particles, grouped in doublets with the charged leptons, while the later
630 come in both chirality states:

$$\begin{pmatrix} \nu_e \\ e_L^- \end{pmatrix}, \quad \begin{pmatrix} \nu_\mu \\ \mu_L^- \end{pmatrix}, \quad \begin{pmatrix} \nu_\tau \\ \tau_L^- \end{pmatrix}, \quad e_R^-, \quad \mu_R^-, \quad \tau_R^-. \quad (2.1)$$

631 Similarly, quarks also exist in both chirality states, and are grouped as:

$$\begin{pmatrix} u_L \\ d_L \end{pmatrix}, \quad \begin{pmatrix} s_L \\ c_L \end{pmatrix}, \quad \begin{pmatrix} t_L \\ b_L \end{pmatrix}, \quad u_R, \quad d_R, \quad s_R, \quad c_R, \quad t_R, \quad b_R. \quad (2.2)$$

632 The fact that there are no right-handed neutrino fields implies that neutrinos are
633 strictly massless within the SM. This restriction follows from the experimental observation
634 that all neutrinos produced via weak interactions are pure left-handed helicity states
635 (and similarly antineutrinos are pure right-handed states). The hypothetical existence
636 of right-handed neutrinos could be indirectly inferred from the observation of non-zero
637 neutrino masses, nevertheless the existence of neutrino masses is not a sufficient condition
638 for the existence of such fields.

639 Left and right-handed fermions transform differently under $SU(2)_L \times U(1)_Y$ rotations,
640 as the right-handed particles are singlets under $SU(2)_L$. Applying a local transformation,
641 they change as:

$$\begin{aligned} \psi_L &\longrightarrow e^{-iY\beta(x)/2} e^{-iT_a\alpha_a(x)} \psi_L, \\ \psi_R &\longrightarrow e^{-iY\beta(x)/2} \psi_R, \end{aligned} \quad (2.3)$$

642 where $Y/2$ and T_a are the generators of $SU(2)_L$ and $U(1)_Y$, respectively, and $\beta(x)$ and

2.1. NEUTRINOS IN THE SM

Table 2.1: Values of T_3 and $Y/2$ assigned to the first generation of fermions.

	e_L	ν_e	e_R	u_L	d_L	u_R	d_R
T_3	-1/2	1/2	0	1/2	-1/2	0	0
$Y/2$	-1/2	-1/2	-1	1/6	1/6	2/3	-1/3

643 $\alpha_a(x)$ are the parameters of the rotation.

644 The values of the quantum numbers $Y/2$ and T_3 , the third component of the weak
 645 isospin, have to be assigned to the different particles. The values of T_3 follow from the
 646 commutation relations of the generators of $SU(2)$. After the spontaneous symmetry
 647 breaking $SU(2)_L \times U(1)_Y \rightarrow U(1)_{EM}$, one finds the relation which determines the electric
 648 charge:

$$Q = T_3 + \frac{Y}{2}, \quad (2.4)$$

649 Setting the electric charge to -1 for electrons, we can find the values of the hypercharge
 650 for the rest of the fermions. The resulting values for the first generation of leptons and
 651 quarks are shown in Tab. 2.1.

652 It is clear that the free Lagrangian of the theory is not be invariant under the gauge
 653 transformations, as the kinetic terms contain derivatives. Therefore, to make it invariant,
 654 one needs to introduce a set of gauge bosons. They appear in the so-called covariant
 655 derivative, which replaces the common derivative and transforms in the same way as the
 656 fermion fields under local rotations. This constrain fixes completely the transformations
 657 of the spin-1 fields. For left and right-handed particles, the covariant derivatives are
 658 given by:

$$\begin{aligned} D_\mu \psi_L &= \left(\partial_\mu + ig' \frac{Y}{2} B_\mu + ig T_a W_\mu^a \right) \psi_L, \\ D_\mu \psi_R &= \left(\partial_\mu + ig' \frac{Y}{2} B_\mu \right) \psi_R, \end{aligned} \quad (2.5)$$

659 where W_μ^i , $i = 1, 2, 3$ and B_μ are the gauge bosons for the $SU(2)_L$ and $U(1)_Y$ factors,
 660 respectively, and g and g' are the corresponding gauge couplings. It can be shown that
 661 these fields transform in the adjoint representation of the gauge group.

CHAPTER 2. NEUTRINO PHYSICS

Table 2.2: Neutral current couplings.

	u	d	ν_e	e
$2v_f$	$1 - \frac{8}{3}\sin^2\theta_W$	$-1 + \frac{4}{3}\sin^2\theta_W$	1	$-1 + 4\sin^2\theta_W$
$2a_f$	1	-1	1	-1

So far, the theory only contains massless particles, as adding bare mass terms to the Lagrangian would spoil the gauge symmetry. Therefore, the mass terms need to be induced by a spontaneous violation of the symmetries. In the SM, the responsible for this is the Higgs mechanism. The Higgs doublet is coupled to the gauge bosons through the covariant derivative, and to the fermions through the Yukawa couplings. Upon spontaneous symmetry breaking, the vacuum expectation value of the Higgs field generate the mass terms of the particles.

In order to obtain the physical intermediate vector boson states, we need to perform the following redefinitions:

$$\begin{aligned} A_\mu &= \sin \theta_W W_\mu^3 + \cos \theta_W B_\mu, \\ Z_\mu &= \cos \theta_W W_\mu^3 - \sin \theta_W B_\mu, \\ W_\mu^\pm &= \frac{1}{\sqrt{2}} (W_\mu^1 \mp i W_\mu^2), \end{aligned} \tag{2.6}$$

where A_μ is the photon field, and Z_μ and W_μ^\pm are the neutral and the charged weak boson fields, respectively. The Weinberg angle, θ_W , relates the weak coupling constants and the electric charge:

$$e = g' \cos \theta_W = g \sin \theta_W. \tag{2.7}$$

At this point, the interacting part of the electroweak Lagrangian can be re-written as the sum of three contributions: the electromagnetic (EM), charged-current (CC) and neutral-current (NC) components:

$$\begin{aligned} \mathcal{L}_{\text{EW}}^{\text{int}} &= \mathcal{L}_{\text{EM}} + \mathcal{L}_{\text{CC}} + \mathcal{L}_{\text{NC}} \\ &= -e A_\mu J_{\text{EM}}^\mu - \frac{g}{2\sqrt{2}} (W_\mu^+ J_{\text{CC}}^\mu + \text{h.c.}) - \frac{g}{2\cos\theta_W} Z_\mu J_{\text{NC}}^\mu, \end{aligned} \tag{2.8}$$

2.2. TROUBLE IN THE NEUTRINO SECTOR

677 with the currents defined as:

$$\begin{aligned} J_{\text{EM}}^\mu &= \sum_f Q_f \bar{f} \gamma^\mu f, \\ J_{\text{CC}}^\mu &= \sum_\ell \bar{\nu}_\ell \gamma^\mu (1 - \gamma_5) \ell + \sum_f \bar{u}_f \gamma^\mu (1 - \gamma_5) d_f, \\ J_{\text{NC}}^\mu &= \sum_f \bar{f} \gamma^\mu (v_f - a_f \gamma_5) f, \end{aligned} \quad (2.9)$$

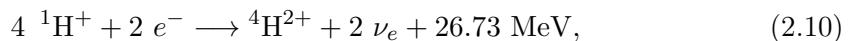
678 where f denotes any SM fermion, ℓ and ν_ℓ a charged lepton and a neutrino of any flavour,
679 and u_f and d_f an up-like and a down-like quarks of any flavour. For the NC case, the
680 values of the v_f and a_f couplings are given in Tab. 2.2.

681 As seen in Eq. (5.8), in the electroweak theory neutrinos are coupled to the Z boson
682 in a universal way. Therefore, by measuring the so-called invisible decay width of the Z
683 boson we have an estimate of the number of light (i.e. lighter than the Z boson) neutrino
684 flavours. This number was measured by LEP in a combined analysis of $e^+ e^- \rightarrow \mu^+ \mu^-$
685 and $e^+ e^- \rightarrow$ hadrons to be $N_\nu = 2.9840 \pm 0.0082$ [21].

686 2.2 Trouble in the neutrino sector

687 2.2.1 The solar neutrino problem

688 Neutrinos are produced everywhere in vast amounts. One of the most prominent sources
689 of neutrinos in our vicinity is our Sun. The Sun is powered mainly by two nuclear fusion
690 reactions, the p – p chain and the CNO cycle. In both cases, the overall reaction is:



691 where part of the released energy is lost to the neutrinos. The electron neutrinos
692 produced are often labelled after the processes that generate them. Figure 2.1 shows the
693 solar neutrino flux as a function of the neutrino energy, broken down by the production
694 process.

CHAPTER 2. NEUTRINO PHYSICS

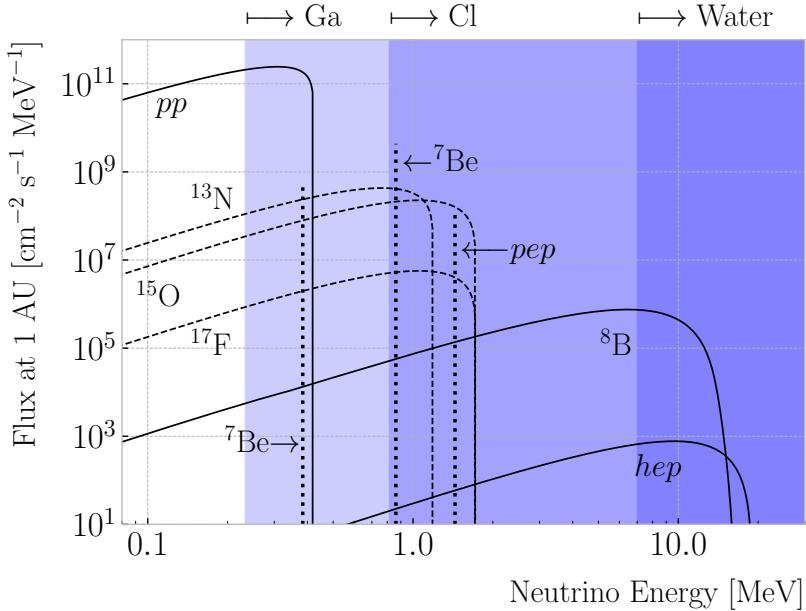


Figure 2.1: Solar neutrino fluxes for the solar model BS05(OP). The detection thresholds for Gallium, Chlorine and water-based experiments are also shown. Figure adapted from Ref. [1].

In the late 1960s, the Brookhaven Solar Neutrino Experiment, led by R. Davis, started data taking with the goal of measuring the solar neutrino flux [22]. The experiment used a tank containing 380 m^3 of tetrachloroethene (C_2Cl_4), a liquid commonly used in dry-cleaning, located 1.5 km underground in the Homestake mine, in Lead, South Dakota. The incoming neutrinos would get captured following the reaction:

$$\nu_e + {}^{37}\text{Cl} \longrightarrow {}^{37}\text{Ar} + e^-, \quad (2.11)$$

therefore allowing to measure the neutrino flux by counting the ${}^{37}\text{Ar}$ isotopes. The threshold for this reaction is 0.814 MeV, just below the 0.862 MeV line from the ${}^7\text{Be}$ ground state transition.

The results of the experiment were compared to the theoretical predictions made by J. Bahcall [23]. During its operation from 1968 to 2002, the experiment observed a solar ν_e flux that was approximately a third of the total prediction [24].

In the early 1990s, the SAGE [25] and GALLEX [26] experiments started operations.

2.2. TROUBLE IN THE NEUTRINO SECTOR

707 The detection principle used for both experiments was similar to that of the Homestake
 708 experiment, but using ^{71}Ga instead of C_2Cl_4 . With a detection threshold of 0.233 MeV,
 709 the Gallium-based experiments were able to observe the pp neutrino flux. Both
 710 experiments measured a solar electron neutrino flux that was a factor of two lower
 711 than the predictions, demonstrating that this deficit was energy-dependent.

712 In the early 2000s, the SNO experiment put an end to the solar neutrino puzzle
 713 [27, 28]. Thanks to its directionality capabilities, being a Cherenkov light detector, as
 714 well as to its heavy water target, SNO measured the total solar neutrino flux through
 715 the NC process:

$$\nu_\alpha + d \longrightarrow n + p + \nu_\alpha, \quad (2.12)$$

716 where $\alpha = e, \mu, \tau$. This measurement agreed with the solar model predictions. Then,
 717 measuring the CC reaction:

$$\nu_e + d \longrightarrow p + p + e^-, \quad (2.13)$$

718 they were able to establish that the ν_μ and ν_τ solar fluxes are in fact non-zero, revealing
 719 that electron neutrinos were transitioning into different flavours.

720 2.2.2 The atmospheric neutrino problem

721 When cosmic-rays interact with the atoms in the upper atmosphere, a plethora of
 722 hadrons, mainly π and K mesons, are produced. In particular, for the charged pions,
 723 we have the following decay chain dominates:

$$\begin{aligned} \pi^+ &\longrightarrow \mu^+ + \nu_\mu, \\ \mu^+ &\longrightarrow e^+ + \bar{\nu}_\mu + \nu_e, \end{aligned} \quad (2.14)$$

724 and similar for the antiparticles. For neutrino energies < 1 GeV, the ratio:

$$\frac{N(\nu_\mu + \bar{\nu}_\mu)}{N(\nu_e + \bar{\nu}_e)}, \quad (2.15)$$

725 of produced neutrinos and antineutrinos is, in good approximation, equal to two [29].

CHAPTER 2. NEUTRINO PHYSICS

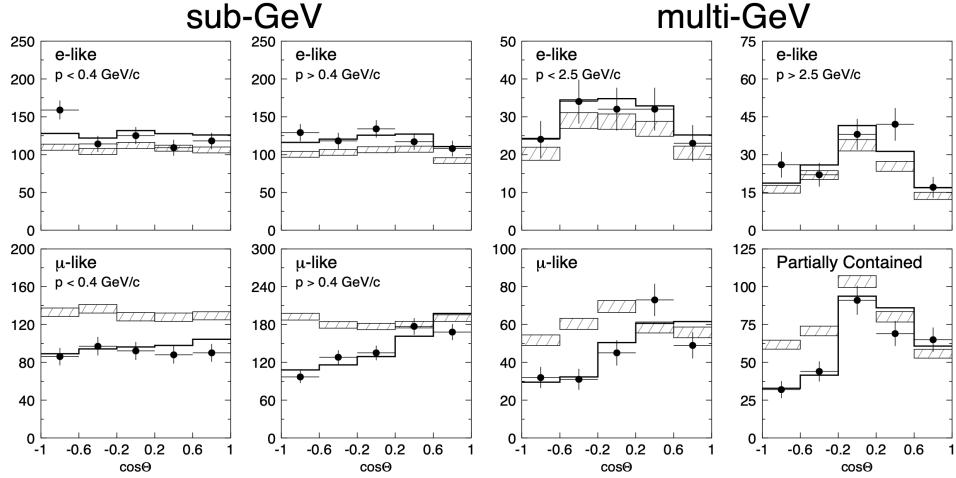


Figure 2.2: Zenith angle distributions for the selected ν_e (top row) and ν_μ (bottom row) events in the SK detector. The hatched region corresponds to the expectation in the case of no oscillations, whereas the solid line indicates the best-fit in the case of $\nu_\mu \rightarrow \nu_\tau$ oscillations. Figure taken from Ref. [34].

During the 1980s, several proton decay experiments, like Kamiokande [30], IMB [31],

MACRO [32], and Soudan-2 [33], measured the flux of atmospheric neutrinos. This was an important part of their research programme, as the atmospheric neutrinos constitute their main background. All these experiments reported an atmospheric neutrino ratio lower than the predictions.

A few years before the SNO discovery, in 1998, Super-Kamiokande (SK) collaboration

measured the atmospheric ν_e and ν_μ spectra as a function of the zenith angle [34]. Upward-going particles have negative zenith angle, $\cos \Theta < 0$, indicating that they entered from the bottom of the detector. These upward-going neutrinos had to travel through the Earth in order to reach the detector, allowing SK to probe a broad range of baselines. Figure 2.2 shows the reported distributions (black dots), compared to the no oscillations prediction (hatched region). This measurement confirmed that muon neutrinos transition to other flavours, and that this phenomenon depends both on the energy and the path length of the neutrino.

The SK and SNO findings provided definitive evidence for the existence of neutrino

oscillations, and therefore non-zero neutrino masses. This constitutes one of the groundbreaking discoveries of modern physics and has acted as driving force for beyond

2.3. MASSIVE NEUTRINOS

the Standard Model (BSM) physics. The minimal extension of the SM we can do to address these phenomena is introducing different masses for at least two of the neutrinos. This way, we are left with three neutrino mass eigenstates ν_1 , ν_2 , and ν_3 , with masses m_1 , m_2 , and m_3 respectively, which in general will not coincide with the flavour eigenstates, ν_e , ν_μ , and ν_τ .

2.3 Massive neutrinos

The existence of neutrino oscillations imply that neutrinos are massive particles. However, as we have seen before, within the SM neutrinos are massless, as they do not have a mass term in the Lagrangian. If one wants to give neutrinos a mass, the particle content of the SM needs to be expanded.

A way of generating massive neutrinos while maintaining gauge invariance is by introducing an arbitrary number of sterile neutrinos N_i , $i = 1, \dots, m$. These allow for two different types of neutrino mass terms:

$$-\mathcal{L}_{M_\nu} = \sum_{i=1}^m \sum_{j=1}^3 M_D^{ij} \bar{N}_i \nu_{Lj} + \frac{1}{2} \sum_{i=1}^m \sum_{j=1}^m M_N^{ij} \bar{N}_i N_j^c + \text{h.c.}, \quad (2.16)$$

where M_D is a complex $m \times 3$ matrix and M_N a complex and symmetric $m \times m$ matrix. The first term, often referred to as the Dirac mass term, arises from the corresponding Yukawa interaction after the spontaneous electroweak symmetry breaking, similar to the other fermions. The second term, called the Majorana mass term, is allowed in the Lagrangian, as it is a singlet of the gauge group. However, it violates lepton number conservation by two units.

If one imposes lepton number symmetry conservation, the Majorana term must banish, $M_N = 0$. In this case, if $m = 3$ we can identify the sterile neutrinos as the right-handed component of the neutrino field. The Dirac mass matrix can be diagonalised using two unitary matrices, V_R^ν and V_L^ν , as:

$$M_D = V_R^\nu \text{ diag}(m_1, m_2, m_3) V_L^{\nu\dagger}, \quad (2.17)$$

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766 where m_i , $i = 1, 2, 3$ are the masses of the three neutrino mass eigenstates.

767 The neutrino mass term can be written in term of the resulting eigenstates as:

$$-\mathcal{L}_{M_\nu} = \sum_{i=1}^3 m_i \bar{\nu}_{Di} \nu_{Di}, \quad (2.18)$$

768 with:

$$\nu_{Di} = \left(V_L^{\nu\dagger} \nu_L \right)_i + \left(V_R^{\nu\dagger} N \right)_i. \quad (2.19)$$

769 In this scenario, both the low energy particle budget and the symmetries of the SM
 770 have to be modified. Moreover, the masses of the neutrinos are generated exclusively
 771 through the Higgs mechanism, which does not explain why they are much smaller than
 772 those of the charged leptons.

773 Going back to the general case, we can re-write Eq. (2.16) in matrix form as:

$$-\mathcal{L}_{M_\nu} = \frac{1}{2} \begin{pmatrix} \bar{\nu}_L^c & \bar{N} \end{pmatrix} \begin{pmatrix} 0 & M_D^T \\ M_D & M_N \end{pmatrix} \begin{pmatrix} \nu_L \\ N^c \end{pmatrix} + \text{h.c.} = \bar{\nu}^c M_\nu \nu + \text{h.c.}, \quad (2.20)$$

774 with $\nu = (\nu_L, N^c)^T$ being a $(3+m)$ -dimensional vector grouping the active and the
 775 sterile neutrinos. The matrix M_ν , which is a complex $(3+m) \times (3+m)$ symmetric
 776 matrix, can be diagonalised by means of a unitary matrix V^ν , yielding:

$$M_\nu = V^\nu \text{ diag}(m_1, m_2, \dots, m_{3+m}) V^{\nu T}. \quad (2.21)$$

777 Using this eigendecomposition, the neutrino mass term can be expressed as:

$$-\mathcal{L}_{M_\nu} = \frac{1}{2} \sum_{i=1}^{3+m} m_i \bar{\nu}_{Mi} \nu_{Mi}, \quad (2.22)$$

778 where the states ν_{Mi} , commonly referred to as Majorana neutrinos, are defined as:

$$\nu_{Mi} = \left(V^{\nu\dagger} \nu \right)_i + \left(V^{\nu\dagger} \nu \right)_i^c, \quad (2.23)$$

779 in such a way that the Majorana condition, $\nu_M^c = \nu_M$, holds true.

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780 As a consequence of the Majorana condition, the neutrino and the antineutrino states
 781 can be described in terms of a single field. As opposed to the charged leptons, which
 782 need to be represented by a four-component or Dirac spinor, the Majorana neutrino is
 783 described by a two-component or Weyl spinor.

784 If the eigenvalues of the Majorana mass matrix, M_N , are much larger than the
 785 electroweak symmetry breaking scale, the diagonalisation of M_ν leads to 3 light and m
 786 heavy neutrino states:

$$-\mathcal{L}_{M_\nu} = \frac{1}{2}\bar{\nu}_l M_l \nu_l + \frac{1}{2}\bar{\nu}_h M_h \nu_h, \quad (2.24)$$

787 where the two mass matrices are given by:

$$\begin{aligned} M_l &\simeq -V_l^T M_D^T M_N^{-1} M_D V_l, \\ M_h &\simeq V_h^T M_N V_h, \end{aligned} \quad (2.25)$$

788 with V_l and V_h two unitary matrices.

789 This scenario represents the so-called see-saw mechanism [35–39]. The name comes
 790 from the fact that the masses of the heavy states are proportional to M_N , whereas for
 791 the light states they are proportional to M_N^{-1} . While both the heavy and the light
 792 neutrinos are Majorana particles, it can be shown that the heavy states are mainly
 793 right-handed, whereas the light ones are mostly left-handed.

794 2.4 Neutrino oscillation formalism

795 Neutrino oscillations were first proposed in 1958 by B. Pontecorvo [40], inspired by the
 796 neutral kaon oscillation phenomenon [41]. Neutral kaons, K^0 and \bar{K}^0 , have opposite
 797 strangeness (± 1) and are produced in strong processes. It was observed that, when
 798 having a beam initially pure of neutral kaons of one type, these would transition into
 799 their antiparticles while propagating. Because the weak interaction does not conserve
 800 strangeness, neutral kaons can change their identity via the processes shown in Fig. 2.3.

801 The mixing considered initially by Pontecorvo was between the neutrino and the

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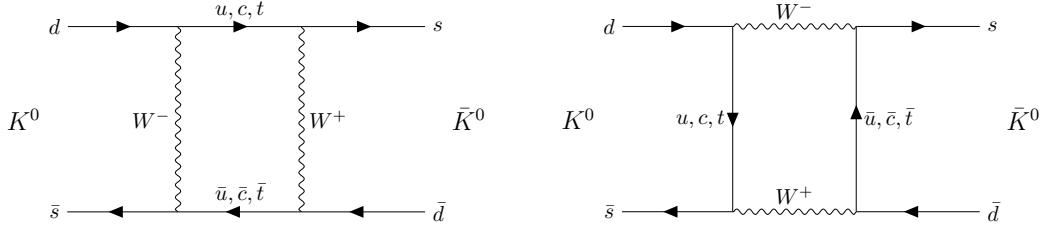


Figure 2.3: $K^0 \rightleftharpoons \bar{K}^0$ mixing through W^\pm exchange.

802 antineutrino states, as only one neutrino flavour was known at the time. After the
 803 discovery of the muon neutrino, the mixing between flavours was also explored [42].

804 In the general case, we have 3 active and m sterile neutrinos, resulting in $3 + m$
 805 neutrino mass eigenstates. Working in the mass basis, the leptonic charged-current
 806 Lagrangian can be written as:

$$-\mathcal{L}_{CC}^{lep} = \frac{g}{\sqrt{2}} (\bar{e}_L, \bar{\mu}_L, \bar{\tau}_L) \gamma^\mu U \begin{pmatrix} \nu_1 \\ \nu_2 \\ \vdots \\ \nu_{3+m} \end{pmatrix} W_\mu^+ + \text{h.c.}, \quad (2.26)$$

807 where U is a $3 \times (3 + m)$ matrix which obeys $UU^\dagger = I_{3 \times 3}$, but in general will not be
 808 unitary, $U^\dagger U \neq I_{(3+m) \times (3+m)}$.

809 The leptonic mixing matrix, U , establishes how the neutrino mass states couple to
 810 the charged leptons. In general, a complex $n \times n$ matrix can be fully specified by $2n^2$ real
 811 parameters. If the matrix is unitary, then the number of independent parameters reduces
 812 to n^2 , as one has to impose n normalisation and $n(n - 1)$ orthogonality constraints.
 813 In our case, we can further reduce the number of parameters by performing a phase
 814 redefinition of the charged lepton fields, without affecting the physics. This is not true
 815 for the neutrinos. As they may be their own antiparticles, one is not allowed to remove
 816 any physically relevant phases. If we consider n generations of leptons, the total number
 817 of parameters in the mixing matrix is $n^2 - n$. Out of these, half of them are mixing
 818 angles, while the other half are complex phase factors.

819 Considering the extended SM without any additional sterile neutrino states, the
 820 resulting 3×3 mixing matrix is unitary. This matrix, often called the Pontecorvo-Maki-

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821 Nakagawa-Sakata (PMNS) matrix [43, 44], relates the set of active neutrinos and the
822 three mass eigenstates as:

$$|\nu_\alpha\rangle = \sum_{i=1}^3 U_{\alpha i}^* |\nu_i\rangle, \quad (2.27)$$

823 where the Greek index α denotes the flavour $\{e, \mu, \tau\}$ and the Latin index i the mass state
824 $\{1, 2, 3\}$. This leptonic mixing matrix may be parametrized in terms of 6 parameters, 3
825 of which are mixing angles θ_{12} , θ_{13} and θ_{23} , one CP-violating phase δ_{CP} and 2 Majorana
826 phases α and β :

$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13} e^{-i\delta_{CP}} \\ 0 & 1 & 0 \\ -s_{13} e^{i\delta_{CP}} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & e^{i\alpha} & 0 \\ 0 & 0 & e^{i\beta} \end{pmatrix}, \quad (2.28)$$

827 where $c_{ij} \equiv \cos \theta_{ij}$ and $s_{ij} \equiv \sin \theta_{ij}$. This matrix is analogous to the Cabibbo-Kobayashi-
828 Maskawa (CKM) matrix in the quark sector. If neutrinos are Dirac fermions, we can
829 drop the Majorana phases in the PMNS matrix, as in this case we can perform the
830 phase redefinitions. However, these phases play no role on the neutrino oscillation
831 phenomenology.

832 In the case that additional sterile neutrinos states are present, the full leptonic mixing
833 matrix would not be unitary in general. For instance, in the see-saw scenario, the 3×3
834 submatrix for the three light Majorana neutrinos is not unitary. However, the deviations
835 from unitarity are of the order $\mathcal{O}(M_D/M_N)$, and therefore expected to be negligible.

836 2.4.1 Oscillations in vacuum

837 Consider the case where a neutrino of flavour α is produced at $t = 0$, and then it
838 propagates through vacuum. Such a state will evolve in time according to the relation:

$$|\nu_\alpha(\vec{x}, t)\rangle = \sum_{i=1}^3 U_{\alpha i}^* e^{-i(E_i t - \vec{p}_i \cdot \vec{x})} |\nu_i(\vec{x} = \vec{0}, t = 0)\rangle, \quad (2.29)$$

839 in the plane wave approximation, as the mass eigenstates are also eigenstates of the free
840 Hamiltonian.

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841 This way, the probability for the neutrino to transition from flavour α to flavour β
842 will be given by:

$$P(\nu_\alpha \rightarrow \nu_\beta) = |\langle \nu_\beta | \nu_\alpha(\vec{x}, t) \rangle|^2 = \left| \sum_{i=1}^3 \sum_{j=1}^3 U_{\alpha i}^* U_{\beta j} e^{-i(E_i t - \vec{p}_i \cdot \vec{x})} \langle \nu_j | \nu_i \rangle \right|^2 \\ = \left| \sum_{i=1}^3 U_{\alpha i}^* U_{\beta i} e^{-i(E_i t - \vec{p}_i \cdot \vec{x})} \right|^2, \quad (2.30)$$

843 where we have used the orthogonality relation $\langle \nu_i | \nu_j \rangle = \delta_{ij}$. A usual approximation to
844 take at this point is to consider ultra-relativistic neutrinos, i.e. $p_i \simeq E$, so we can write
845 the dispersion relations as:

$$E_i = \sqrt{p_i^2 + m_i^2} \approx E + \frac{m_i^2}{2E}. \quad (2.31)$$

846 In the end, assuming $t \approx L$ where L is the distance between the production and the
847 detection points, the probability for the $\nu_\alpha \rightarrow \nu_\beta$ transition becomes:

$$P(\nu_\alpha \rightarrow \nu_\beta) = \sum_{i,j} U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j} e^{-i \frac{\Delta m_{ij}^2}{2E} L} \\ = \delta_{\alpha\beta} - 4 \sum_{i < j} \Re e [U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*] \sin^2 \left(\frac{\Delta m_{ij}^2}{4E} L \right) \\ + 2 \sum_{i < j} \Im m [U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*] \sin \left(\frac{\Delta m_{ij}^2}{2E} L \right), \quad (2.32)$$

848 where Δm_{ij}^2 is the difference of the squared masses of the j th and i th neutrino mass
849 eigenvalues. At this point, it is usual to write the phase responsible for the oscillations
850 as:

$$\Delta_{ij} \equiv \frac{\Delta m_{ij}^2}{4E} L \simeq 1.27 \frac{\Delta m_{ij}^2}{(\text{eV}^2)} \frac{L}{(\text{km})} \frac{(\text{GeV})}{E}. \quad (2.33)$$

851 Notice that, in the case of antineutrinos, the only difference would be the sign of the
852 last term in the oscillation probability. As the process $\bar{\nu}_\alpha \rightarrow \bar{\nu}_\beta$ is the CP-mirror image
853 of $\nu_\alpha \rightarrow \nu_\beta$, the differences between their oscillation probabilities would be a measure of

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854 CP symmetry violation:

$$\begin{aligned} A_{CP}^{\alpha\beta} &= P(\nu_\alpha \rightarrow \nu_\beta) - P(\bar{\nu}_\alpha \rightarrow \bar{\nu}_\beta) \\ &= 4 \sum_{i<j} \Im \left[U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^* \right] \sin 2\Delta_{ij}. \end{aligned} \quad (2.34)$$

855 Assuming that CPT invariance holds, then the following relation must be true:

$$P(\nu_\alpha \rightarrow \nu_\beta) = P(\bar{\nu}_\beta \rightarrow \bar{\nu}_\alpha), \quad (2.35)$$

856 as these two process are related by the CPT symmetry. From the definition of probability,
 857 we also must have:

$$\sum_\beta P(\nu_\alpha \rightarrow \nu_\beta) = \sum_\beta P(\bar{\nu}_\alpha \rightarrow \bar{\nu}_\beta) = 1, \quad (2.36)$$

858 where the sum includes all flavours, including α . From these two constraints, one can
 859 probe that:

$$A_{CP}^{\alpha\beta} = -A_{CP}^{\beta\alpha}, \quad (2.37)$$

860 and in particular:

$$A_{CP}^{\alpha\alpha} = 0. \quad (2.38)$$

861 A direct consequence of this last relation is that there are no observable CP-violating
 862 effects in the so-called disappearance experiments. One needs to perform appearance
 863 experiments, where the flavour detected is different from the original flavour, in order
 864 to measure the CP asymmetry. Neutrino experiments often report the amount of CP-
 865 violation through the Jarlskog invariant. In terms of the parametrisation typically used
 866 to write the PMNS matrix, it is given by:

$$J = \frac{1}{8} \cos \theta_{13} \sin 2\theta_{12} \sin 2\theta_{13} \sin 2\theta_{23} \sin \delta_{CP}. \quad (2.39)$$

867 The Jarlskog invariant can be used to compare the amount of CP-violation in the lepton
 868 and the quark sectors, where $J = 3.12^{+0.13}_{-0.12} \times 10^{-5}$ in the latter [45].

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2.4.2 Oscillations in matter

When neutrinos propagate through matter, their oscillation can be affected in mainly two ways. First, neutrinos can inelastically scatter with nuclei, thus destroying the coherent propagation of their quantum state. Nevertheless, in most cases this effect is negligible (even in very dense mediums like the core of the Sun). Second, neutrinos can also experience coherent or forward scatterings, that can affect their oscillation but not lose the coherent propagation of the state.

The first proposed model to account for neutrino oscillations in matter was proposed by Mikhaev, Smirnov and Wolfenstein (MSW) [46]. It relies on the fact that, as the only charged lepton present in ordinary matter is the electron, electron neutrinos can undergo both charged and neutral-current interactions with matter whereas for muon and tau neutrinos just neutral currents are possible.

An illustrative way to introduce the MSW mechanism is by considering the two flavours case. It can be shown that the evolution of the two flavour eigenstates in vacuum is given by the following time-dependent Schrödinger equation:

$$i \frac{d}{dt} \begin{pmatrix} \nu_e \\ \nu_\mu \end{pmatrix} = H_V \begin{pmatrix} \nu_e \\ \nu_\mu \end{pmatrix}, \quad (2.40)$$

with a vacuum Hamiltonian given by:

$$H_V = \frac{\Delta m^2}{4E} \begin{pmatrix} -\cos 2\theta & \sin 2\theta \\ \sin 2\theta & \cos 2\theta \end{pmatrix}, \quad (2.41)$$

where Δm^2 is the mass splitting between the two neutrino states and θ the only mixing angle. For simplicity, I omit the terms of the Hamiltonian that are proportional to the identity, as they do not affect the oscillation phenomenology.

The NC contribution to the matter potential is identical for all the flavours, and has the form:

$$V_{NC} = -\frac{G_F}{\sqrt{2}} N_n(x), \quad (2.42)$$

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890 where G_F is the Fermi constant and $N_n(x)$ the local neutron density. Because it is
 891 common to all flavours, I do not take it into account in the effective Hamiltonian, as it
 892 would appear as a term proportional to the identity. The CC component only affects
 893 the electron neutrino (and antineutrino). It can be written as:

$$V_{\text{CC}} = \pm \sqrt{2} G_F N_e(x), \quad (2.43)$$

894 with $N_e(x)$ being the local electron density in the material. In the end, the effective
 895 Hamiltonian which describes the propagation of the flavour eigenstates in matter only
 896 contains an extra $\nu_e - \nu_e$ element:

$$H_M = H_V + \begin{pmatrix} V_{\text{CC}} & 0 \\ 0 & 0 \end{pmatrix}. \quad (2.44)$$

897 The solution to the Schrödinger equation greatly simplifies if one considers the case
 898 of a constant matter density. In that case, the effective Hamiltonian can be diagonalised,
 899 obtaining the effective neutrino mass eigenstates in matter. It can be re-written in the
 900 same form as the vacuum Hamiltonian:

$$H_M = \frac{\Delta m_m^2}{4E} \begin{pmatrix} -\cos 2\theta_m & \sin 2\theta_m \\ \sin 2\theta_m & \cos 2\theta_m \end{pmatrix}, \quad (2.45)$$

901 where the effective mass splitting and the effective mixing angle are given by:

$$\begin{aligned} \Delta m_m^2 &= \lambda \Delta m_m^2, \\ \sin 2\theta_m &= \frac{\sin 2\theta_m}{\lambda} \end{aligned} \quad (2.46)$$

902 with:

$$\begin{aligned} \lambda &= \sqrt{(\cos 2\theta - A)^2 + \sin^2 2\theta}, \\ A &= \pm \frac{2\sqrt{2} G_F N_e E}{\Delta m^2}. \end{aligned} \quad (2.47)$$

903 In terms of the effective matter oscillation parameters, the transition probability

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904 $\nu_e \rightarrow \nu_\mu$ (in the two flavour approximation) reads:

$$P(\nu_e \rightarrow \nu_\mu) = \sin^2 2\theta_m \sin^2 \left(\frac{\Delta m_m^2}{2E} L \right) \quad (2.48)$$

905 From this last equation one can see that, when $\cos 2\theta = A > 0$ the oscillations are
906 greatly enhanced. This effect is known as the MSW resonance. For the neutrinos, this
907 resonant condition is only satisfied if $\Delta m^2 > 0$ (the opposite is true for antineutrinos).
908 This is can be exploited by long baseline experiments, which can gain sensitivity to the
909 neutrino mass hierarchy through matter effects.

910 2.4.3 Current status of neutrino oscillations

911 A wide range of neutrino experiments provide experimental input to the neutrino
912 oscillation framework, both using natural or synthetic neutrino sources. The results
913 from one of the neutrino global fit analyses, shown in Tab. 2.3¹, summarise well our
914 current understanding of the different oscillation parameters.

915 **Solar neutrino experiments** detect neutrinos produced in thermonuclear reactions
916 inside the Sun, mainly from the so-called *pp* chain and the CNO cycle. These neutrinos
917 have a typical energy in the range from 0.1 to 20 MeV. These experiments (Homestake
918 [47], GALLEX [26], SAGE [25], Borexino [48], Super-Kamiokande [49] and SNO [50])
919 provide the best sensitivities to θ_{12} and Δm_{21}^2 .

920 **Atmospheric neutrino experiments** detect the neutrino flux produced when
921 cosmic rays scatter with particles in Earth's atmosphere. These collisions generate particle
922 showers that eventually produce electron and muon neutrinos (and antineutrinos). Their
923 energies range from few MeV to about 10^9 GeV. Experiments, like Super-Kamiokande
924 [51] and IceCube [52] use atmospheric neutrinos to measure oscillations and are specially
925 sensitive to θ_{23} and Δm_{32}^2 .

926 **Reactor neutrino experiments** look for the $\bar{\nu}_e$ spectrum produced by nuclear
927 reactors, with energies in the MeV scale. Depending on the distance to the source,

¹These are the results reported during M. Tórtola's talk at Neutrino 2024 (see this link). I need to keep an eye and see if they publish these or other updated results in the near future.

2.5. OPEN QUESTIONS IN THE NEUTRINO SECTOR

Table 2.3: Summary of neutrino oscillation parameters determined in the Neutrino Global Fit of 2020 [14].

Parameter	Best fit $\pm 1\sigma$	3σ range
Δm_{21}^2 [eV $^2 \times 10^{-5}$]	$7.55^{+0.22}_{-0.20}$	6.98 – 8.19
$ \Delta m_{31}^2 $ [eV $^2 \times 10^{-3}$] (NO)	$2.51^{+0.02}_{-0.03}$	2.43 – 2.58
$ \Delta m_{31}^2 $ [eV $^2 \times 10^{-3}$] (IO)	$2.41^{+0.03}_{-0.02}$	2.34 – 2.49
$\sin^2 \theta_{12}/10^{-1}$	3.04 ± 0.16	2.57 – 3.55
$\sin^2 \theta_{23}/10^{-1}$ (NO)	$5.64^{+0.15}_{-0.21}$	4.23 – 6.04
$\sin^2 \theta_{23}/10^{-1}$ (IO)	$5.64^{+0.15}_{-0.18}$	4.27 – 6.03
$\sin^2 \theta_{13}/10^{-2}$ (NO)	$2.20^{+0.05}_{-0.06}$	2.03 – 2.38
$\sin^2 \theta_{13}/10^{-2}$ (IO)	$2.20^{+0.07}_{-0.04}$	2.04 – 2.38
δ_{CP}/π (NO)	$1.12^{+0.16}_{-0.12}$	0.76 – 2.00
δ_{CP}/π (IO)	$1.50^{+0.13}_{-0.14}$	1.11 – 1.87

long-baseline experiments like KamLAND [53] are sensitive to the solar mass splitting Δm_{21}^2 whereas much shorter baseline experiment such as RENO [54] or DayaBay [55] measure θ_{13} and Δm_{31}^2 .

Accelerator experiments measure neutrino fluxes generated in particle accelerators. Usually mesons are produced in the accelerator to be focused into a beam, then some decay to muon neutrinos and the rest are absorbed by a target. Depending on the configuration one can obtain a beam made of mostly neutrinos or antineutrinos. The typical energies of these neutrinos are in the GeV range. Experiments such as NOvA [56], T2K [57], MINOS [58], OPERA [59] and K2K [60] (and in the future DUNE [61]) are primarily sensitive to θ_{13} , θ_{23} and Δm_{32}^2 . Also, in the coming years DUNE [61] and Hyper-Kamiokande [62] will be sensitive to δ_{CP} .

2.5 Open questions in the neutrino sector

A crucial question that remains open these days, and is of vital importance for oscillation phenomena, is whether the mass eigenvalue ν_3 is the heaviest (what we call normal ordering) or the lightest (referred to as inverted ordering) of the mass eigenstates. In

CHAPTER 2. NEUTRINO PHYSICS

943 other words, this means that we do not know the sign of Δm_{32}^2 , so we can either have
944 $m_1 < m_2 < m_3$ (NO) or $m_3 < m_1 < m_2$ (IO).

945 Another big puzzle is related to the value of δ_{CP} . Nowadays it is poorly constrained,
946 with all values between π and 2π being consistent with data. A prospective measurement
947 different from $\delta_{CP} = 0, \pi$ will predict CP-violation in the leptonic sector, and thus
948 contribute along with the one measured in the quark sector to the total amount of
949 CP-violation. Although it is true that these two contributions by themselves are not
950 enough to explain the matter anti-matter asymmetry in our universe, the amount of
951 CP-violation in the leptonic sector can be key to explain such imbalance.

952 Both of these questions, because of their nature, could be understood thanks to
953 future oscillation experiments.

954 Notwithstanding, there are other mysteries that can not be unveiled just by conducting
955 oscillation experiments, as certain quantities do not influence these phenomena. Among
956 these there is the question of the absolute values of the neutrino masses. Depending
957 on the value of the lightest of the neutrino masses we can have different mass spectra,
958 from hierarchical $m_1 \ll m_2 < m_3$ (NO) or $m_3 \ll m_1 < m_2$ (IO) to quasi-degenerate
959 $m_1 \simeq m_2 \simeq m_3$.

960 Other open question concerns the nature itself of the neutrinos. If neutrinos are Dirac
961 particles then their mass term can be generated through the usual Higgs mechanism
962 by adding right-handed neutrino fields. However, if they are Majorana particles and
963 therefore their own antiparticles, there is no need to add extra fields to have the mass
964 term in the Lagrangian. Experiments like SuperNEMO [63], SNO+ [64] and NEXT
965 [65], which search for neutrino-less double beta decay, will be able to determine whether
966 neutrinos are Dirac or Majorana.

967 2.6 Neutrino interactions

968 The study of neutrino-nucleus interactions is of great importance for long baseline
969 neutrino oscillation experiments. The interaction model provides a mapping between

2.6. NEUTRINO INTERACTIONS

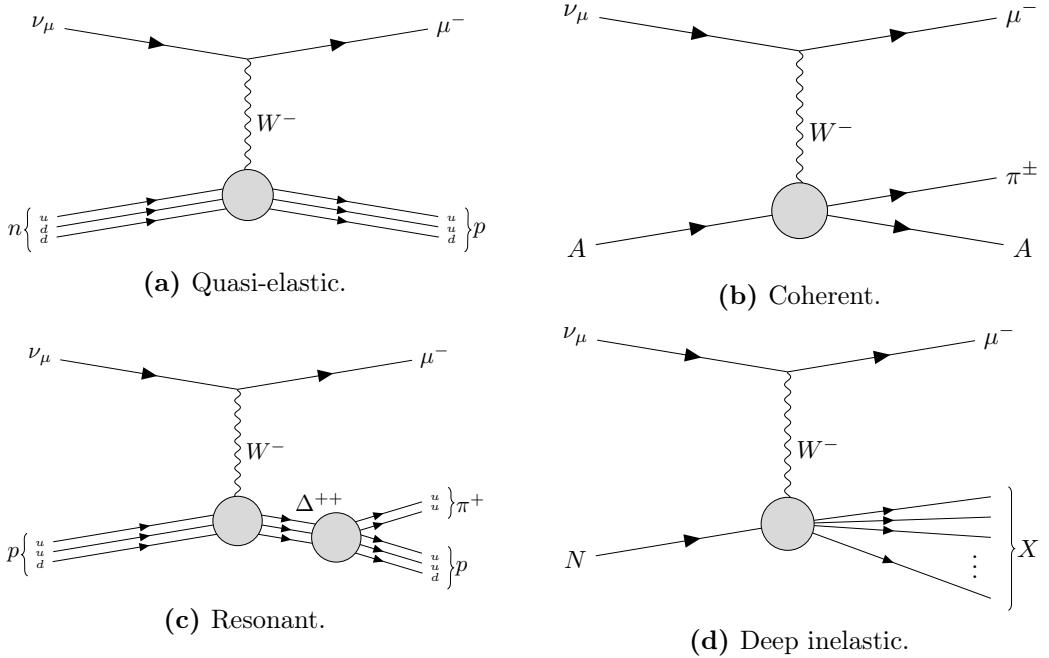


Figure 2.4: Feynman diagrams of the four most relevant CC interactions to long baseline neutrino oscillation experiments.

the energy of the incoming neutrino and the final state particles after the interaction.
 Because in this kind of experiments neutrinos are obtained as secondary decay products of mesons, typically charged pions and kaons, their energies are not known a priori. Not only that, but the kinematics of the interacting nucleon are also unknown. Therefore, we rely on the neutrino interaction models to provide this relation between the observables in the detector and the true kinematics of the neutrino. Interaction modelling is expected to be the one of the leading sources of systematic uncertainties in the next generation of long baseline experiments [66–68].

In the case of neutrino interactions with nuclei, at the energies relevant for long baseline oscillation experiments, around the GeV-scale, the process is dominated by the interaction between the neutrino and a single nucleon within the nuclear medium. Figure 2.4 shows examples of the four most common neutrino CC interactions. In this diagrams A indicated that the interaction happened with the nucleus as a whole, whereas N denotes a single nucleon.

At low energies, below 1 GeV, quasi-elastic (QE) interactions dominate. In a CCQE

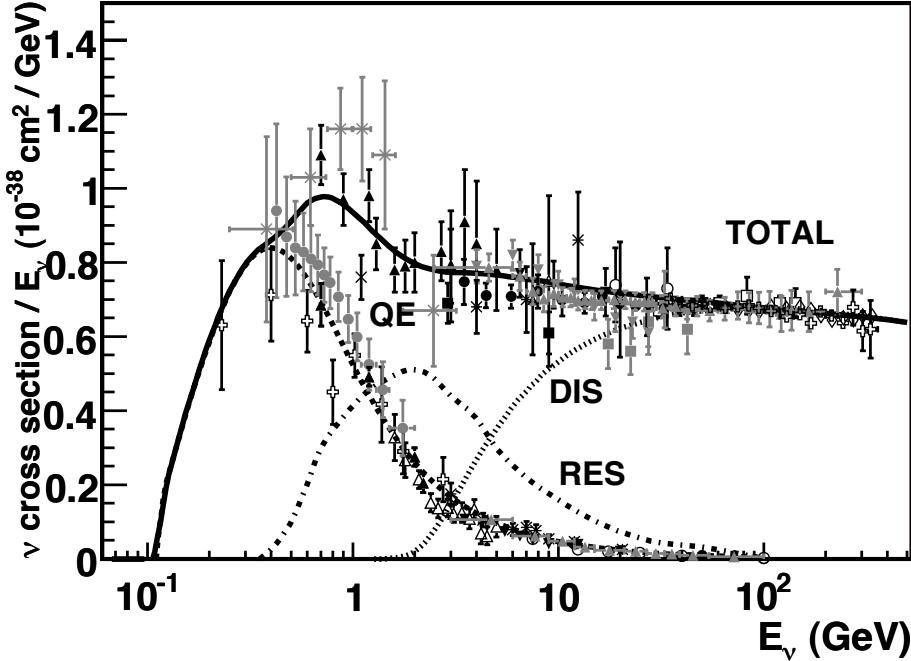


Figure 2.5: Total ν_μ CC cross section per nucleon as a function of the neutrino energy. The contributions from the different channels are shown. Figure taken from Ref. [69].

interaction a neutrino (antineutrino) interacts with a neutron (proton), converting it into a proton (neutron) which is then ejected from the nucleus together with the resulting charged lepton. At energies above 1 GeV the neutrino is able to excite the nucleon into a baryonic resonance, which promptly decays into a nucleon and a pion. These are the so-called resonant (RES) interactions. Neutrinos also interact with entire nucleus coherently, in the process known as coherent (COH) interaction. This kind of reactions also produce a single pion in the final state. At high neutrino energies, above 5 GeV, deep inelastic scattering (DIS) takes place. In these processes, the neutrino interacts with a single quark within the nucleon, breaking the nucleon and producing a hadronic shower.

Figure 2.5 shows a compilation of measurements of the total ν_μ CC cross section (see Ref. [69] for the details of the different experimental results). Also shown are the contributions from the different interaction modes. The contribution of the CCCOH interaction is omitted, as it is negligible compared to the others. This shows how the

2.6. NEUTRINO INTERACTIONS

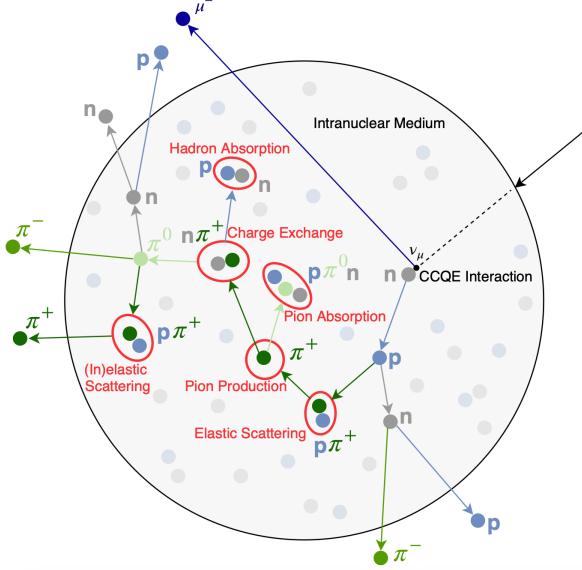


Figure 2.6: Schematic representation of a ν_μ CCQE interaction with a neutron inside a nucleus. The reaction produces a muon and a proton, which travel through the nuclear medium. The outgoing proton undergoes various kinds of hadronic FSIs on its way out. Figure taken from Ref. [70].

999 interaction model needs to accurately predict the neutrino-nucleon cross section for the
 1000 different interaction modes across a broad energy range, to obtain the correct relative
 1001 contributions.

1002 Nuclear effects alter the neutrino cross section, as well as the multiplicities of the
 1003 final state particles. Therefore, the interaction models need to account for the effects
 1004 introduced by the nuclei. There are several models available to describe the initial state
 1005 of the nucleus, like the relativistic Fermi gas model [71], spectral functions [72] or the
 1006 random phase approximation [73]. The other main effect that interaction models have to
 1007 deal with are the so-called final state interactions (FSI). These are the interactions of the
 1008 particles produced in the neutrino-nucleon scattering as they travel through the nuclear
 1009 medium. Typically, the lepton exits the nucleus without interacting. However, hadrons
 1010 tend to get scattered, absorbed or re-emitted. These effects are usually described by
 1011 means of intra-nuclear cascade models [74]. Figure 2.6 illustrates the effects of FSI on
 1012 the observable particle content in the detector after a ν_μ CCQE interaction.

1013 There exists a rich experimental programme dedicated to the measurement of neutrino

CHAPTER 2. NEUTRINO PHYSICS

1014 cross sections. The list of such experiments in the recent years include MiniBooNE
1015 [75], MINERvA [76], MicroBooNE [77] and SBND [78]. Additionally, thanks to their
1016 near detectors, long baseline experiments can perform cross section measurements.
1017 Some recent examples are NOvA [79] or T2K [80]. Future oscillation experiments
1018 will greatly benefit from these measurements, as the measurement of the oscillation
1019 parameters depends on the cross section modelling. However, there are alternative
1020 data-driven approaches to extract the oscillation probabilities without relying on a
1021 neutrino interaction model, which are planned to be explored in the next generation of
1022 experiments [81, 82].

1023

1024

1025

The Deep Underground Neutrino Experiment

1026 The Deep Underground Neutrino Experiment (DUNE) is a next generation long-baseline
1027 neutrino experiment [83]. It will aim to address several questions in neutrino physics,
1028 study neutrinos from astrophysical sources and search for beyond the standard model
1029 physics.

1030 This chapter reviews the main goals of the DUNE experiment, the design of the far
1031 detector modules and their data acquisition (DAQ) system, and the role that the near
1032 detector plays in the physics program of DUNE.

1033 3.1 Overview

1034 The main physics goals of DUNE are:

- 1035 • measure the neutrino mass hierarchy, the amount of CP violation in the leptonic
1036 sector and the θ_{23} octant,
- 1037 • detect rare low energy neutrino events, like neutrinos from supernova bursts, and
- 1038 • search for proton decay and other beyond the standard model phenomena.

1039 The design of DUNE has been tailored with these goals in mind. It will consist
1040 of two neutrino detectors. A near detector (ND) complex will be placed at Fermilab,
1041 574 m downstream of the neutrino production point, whereas a larger far detector

CHAPTER 3. THE DEEP UNDERGROUND NEUTRINO EXPERIMENT

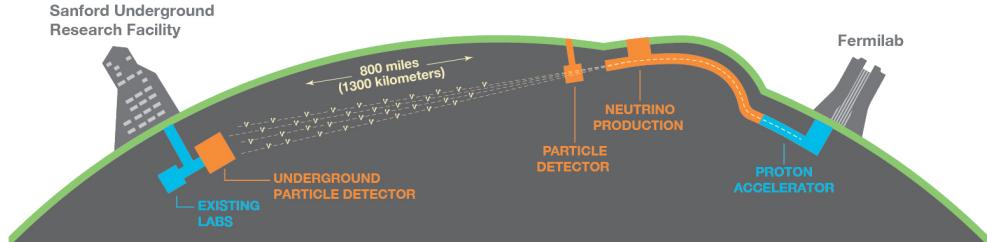


Figure 3.1: Schematic diagram of the DUNE experiment and the LBNF beamline [83].

1042 (FD) will be built in the Sandford Underground Research Facility (SURF), South
 1043 Dakota, approximately 1300 km away. Figure 3.1 shows a simplified view of the various
 1044 components of DUNE (not to scale).

1045 The beam neutrinos will be provided by the Long-Baseline Neutrino Facility (LBNF)
 1046 beamline, the multi-megawatt wide-band neutrino beam planned for Fermilab. It will
 1047 produce neutrinos travelling in the direction of SURF, with the capability to switch
 1048 between neutrino and antineutrino mode.

1049 Before arriving to the FD, the neutrino beam meets the ND complex, which serves
 1050 as the experiment's control. The design of the DUNE ND is mainly driven by the
 1051 needs of the oscillation physics program, as its main role is to measure the unoscillated
 1052 neutrino energy spectra. From these we can predict the unoscillated spectra at the FD,
 1053 which can be compared to the spectra measured at the FD to extract the oscillation
 1054 parameters. Additionally, the ND has a physics programme of its own, including cross
 1055 section measurements and BSM physics searches.

1056 The technology chosen for the FD modules of DUNE is the liquid Argon time
 1057 projection chamber (LArTPC). Its four modules will record neutrino interactions from
 1058 the accelerator-produced beam arriving at predictable times. As it also aims at recording
 1059 rare and low energy events, like supernovae and solar neutrinos, the FD requires trigger
 1060 schemes which can deal with both kinds of physics, and also maximum uptime.

1061 DUNE is planned to be built using a staged approach consisting on two phases,
 1062 which are summarised in Tab. 3.1. Phase I consists of a FD with 50% of the total

3.2. PHYSICS GOALS OF DUNE

Table 3.1: Summary of the two-phased plan for DUNE. Adapted from Ref. [84].

Parameter	Phase I	Phase II	Benefit
FD mass	20 kt fiducial	40 kt fiducial	FD statistics
Beam power	up to 1.2 MW	2.4 MW	FD statistics
ND config.	ND-LAr, TMS, SAND	ND-LAr, ND-GAr, SAND	Systematic constraints

Table 3.2: Exposure and time required to achieve the different physics milestones of the two phases. The predictions assume a Phase II staging scenario where FD modules 3 and 4 are deployed in years 4 and 6 and both the beam and ND are upgraded after 6 years. Adapted from Ref. [84].

Stage	Physics milestone	Exposure (kt-MW-years)	Years (staged)
Phase I	5σ MO ($\delta_{CP} = -\pi/2$)	16	1-2
	5σ MO (100% of the δ_{CP} values)	66	3-5
	3σ CPV ($\delta_{CP} = -\pi/2$)	100	4-6
Phase II	5σ CPV ($\delta_{CP} = -\pi/2$)	334	7-8
	δ_{CP} resolution of 10 degrees ($\delta_{CP} = 0$)	400	8-9
	5σ CPV (50% of the δ_{CP} values)	646	11
	3σ CPV (75% of the δ_{CP} values)	936	14
	$\sin^2(2\theta_{13})$ resolution of 0.004	1079	16

1063 fiducial mass, a reduced version of the ND complex and a 1.2 MW proton beam. It will
1064 be sufficient to achieve some early physics goals, like the determination of the neutrino
1065 mass ordering. For its Phase II, DUNE will feature the full four FD modules, a more
1066 capable ND and a 2.4 MW proton beam. The physics milestones for the two phases are
1067 given in Tab. 3.2, in a staging scenario which assumes that Phase II is completed after
1068 6 years of operation.

1069 A summary of the DUNE science program can be found in the DUNE FD Technical
1070 Design Report (TDR) Volume I [83]. For a detailed discussion on the two-phased
1071 approach the reader is referred to the DUNE Snowmass 2021 report [84].

1072 3.2 Physics goals of DUNE

1073 As noted in the literature (see for instance Ref. [14] for a review), the parameter space of
1074 the neutrino oscillation phenomena within the three-flavour picture is quite constrained

CHAPTER 3. THE DEEP UNDERGROUND NEUTRINO EXPERIMENT

1075 by current experimental data. However, there are still crucial open questions, like the
1076 mass ordering, the value of δ_{CP} or the θ_{23} octant. One of the main goals of DUNE is to
1077 determine precisely the values of these parameters [85].

1078 To address these questions DUNE can look to the subdominant oscillation channel
1079 $\nu_\mu \rightarrow \nu_e$ ($\bar{\nu}_\mu \rightarrow \bar{\nu}_e$) and study the energy dependence of the ν_e ($\bar{\nu}_e$) appearance probability.
1080 When we focus on the antineutrino channel $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ there is a change in the sign of δ_{CP} ,
1081 thus introducing CP-violation. Moreover, due to the fact that there are no positrons in
1082 the composition of Earth, there is a sign difference for the matter effect contribution
1083 when looking to the antineutrino channel. This asymmetry is proportional to the baseline
1084 length L and is sensitive to the sign of Δm_{31}^2 , and thus to the neutrino mass ordering.

1085 Another of the main physics goals of DUNE is the search for baryon-number violating
1086 processes. Specifically, it will try to answer the question of whether protons are stable
1087 or not. There is no symmetry argument that forbids protons from decaying, but its
1088 apparent stability seems to suggest that baryon number is conserved [86]. However,
1089 proton decay is a usual feature of grand-unified theories, where electromagnetic, weak
1090 and strong interactions are unified above a certain energy scale [87].

1091 As the energy deposition scale for this kind of searches is nearly the same as the one
1092 for long-baseline neutrino oscillations, DUNE will be able to look for them. It has several
1093 advantages over other experiments, such as excellent imaging and particle identification,
1094 which can be translated to lower backgrounds.

1095 The last of the main objectives of DUNE is the detection of neutrinos originated in
1096 supernovae explosions, what is called a supernova neutrino burst (SNB). These neutrinos
1097 carry with them information about the core-collapse process, from the progenitor to the
1098 explosion and the remnant; but also may have information about new exotic physics. So
1099 far, the only neutrino events ever recorded from such a process were a few dozens of $\bar{\nu}_e$
1100 events from the 1987A supernova located in the Magellanic Cloud, 50 kpc away from
1101 Earth [88, 89].

1102 DUNE aims to collect SNB events. Although these are quite rare, as the expected
1103 supernovae explosion events are about one every few decades for our galaxy and

3.3. LBNF BEAMLINE

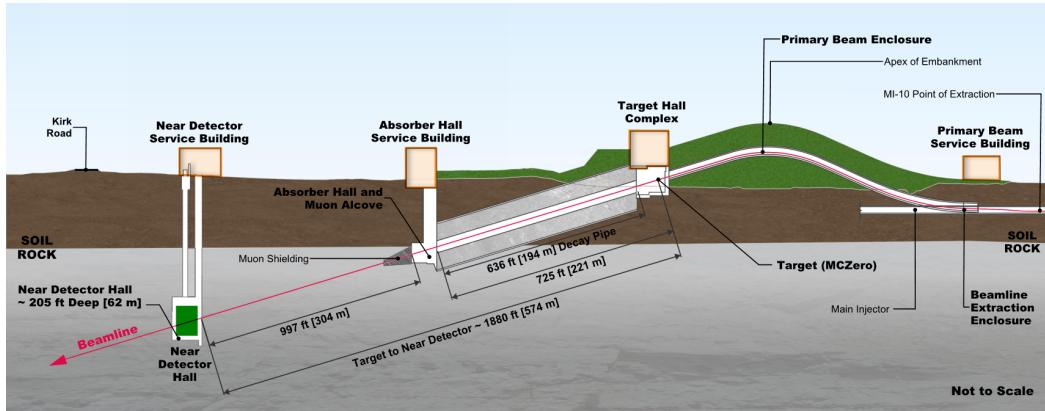


Figure 3.2: Schematic longitudinal section of the LBNF beamline at Fermilab (not to scale). Figure taken from Ref. [90].

1104 Andromeda, the long lifetime of the experiment (around a few decades as well) makes it
 1105 reasonable to expect some. Nowadays the main sensitivity to SNB of most experiments
 1106 is to the $\bar{\nu}_e$ through inverse beta decay. One of the advantages of DUNE is its expected
 1107 sensitivity to ν_e , since the dominant channel will be ν_e CC scattering.

1108 Moreover, due to the stringent requirements that the main physics goals set for
 1109 DUNE, it will allow also to perform searches for all kind of BSM physics. Among
 1110 others, DUNE will be able to look for: active-sterile neutrino mixing, non-unitarity of
 1111 the PMNS matrix, non-standard interactions, Lorentz and CPT violations, neutrino
 1112 trident production, light-mass DM, boosted DM and heavy neutral leptons. The reader
 1113 is referred to the DUNE FD TDR Volume II [85] for a full discussion of the physics
 1114 scope of DUNE.

1115 3.3 LBNF beamline

1116 The LBNF project is responsible for producing the neutrino beam for the DUNE detectors.
 1117 A detailed discussion of the LBNF program can be found in the DUNE/LBNF CDR
 1118 Volume III [90].

1119 A schematic diagram of the longitudinal section of the LBNF beamline is shown in
 1120 Fig. 3.2. First, a beam of 60 – 120 GeV protons is extracted from the Fermilab Main
 1121 Injector. This beam is aimed towards the target area, where it collides with a cylindrical

CHAPTER 3. THE DEEP UNDERGROUND NEUTRINO EXPERIMENT

graphite target to produce pions and kaons.

The diffuse, secondary beam of particles is focused by a pair of magnetic horns. These select the positively charged particles when operated in Forward Horn Current (FHC) mode, or the negatively charged ones when the current is reversed, also known as Reverse Horn Current (RHC) mode. The focused secondary beam then enters a 194 m decay pipe where the pions and kaons will predominantly produce $\mu^+\nu_\mu$ pairs when in FHC mode (or $\mu^-\bar{\nu}_\mu$ in RHC mode).

At the end of the decay pipe a hadron absorber removes the undecayed hadrons and muons from the beam, which reduces the ν_e ($\bar{\nu}_e$) and ν_μ ($\bar{\nu}_\mu$) contamination coming from the μ^+ (μ^-) decays. The resulting neutrino flux at the FD is shown in Fig. 3.3, both for FHC (left) and RHC (right) modes. These predictions show the intrinsic ν_e contamination and wrong sign component from wrong sign and neutral meson decays, as well as muons decaying before reaching the absorber.

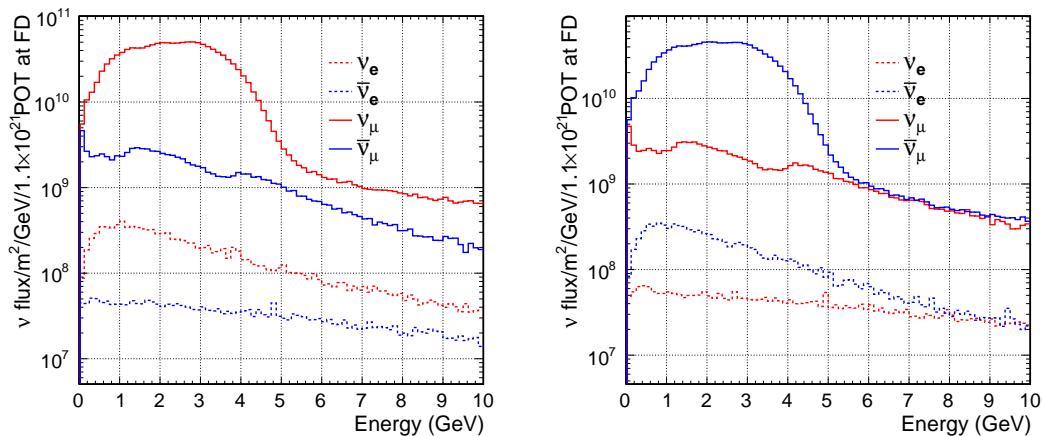


Figure 3.3: Predicted neutrino fluxes at the FD in FHC mode (left panel) and RHC mode (right panel). Figures taken from Ref. [85].

3.4 Near Detector

To estimate the oscillation parameters we measure the neutrino energy spectra at the FD. This reconstructed energy arises from a convolution of the neutrino flux, cross section, detector response and the oscillation probability. Using theoretical and empirical models

3.4. NEAR DETECTOR

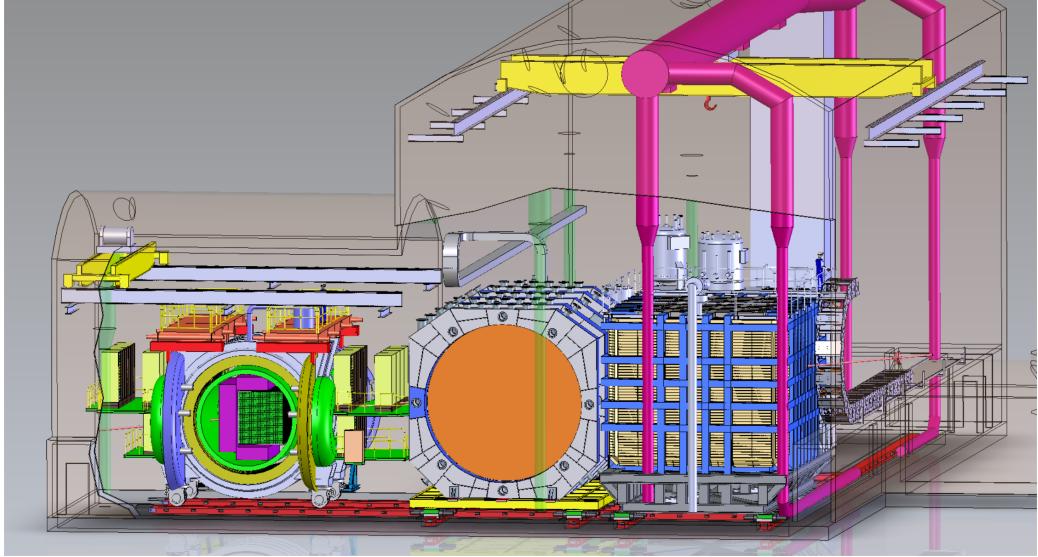


Figure 3.4: Representation of the ND hall in Phase II, showing the different subcomponents. From right to left, in the direction of the beam, we have ND-LAr, ND-GAr and SAND. Figure taken from Ref. [91].

1139 to account for the other effects, one can extract the oscillation probability using the
 1140 measurement. However, these models have associated a number of uncertainties that
 1141 are then propagated to the oscillation parameters.

1142 One of the main roles of the ND is to measure the neutrino interaction rates before
 1143 the oscillation effects become relevant, i.e. close to the production point. By measuring
 1144 the ν_μ and ν_e energy spectra, and that of their corresponding antineutrinos, at the ND
 1145 we can constrain the model uncertainties. A complete cancellation of the uncertainties
 1146 when taking the ratio between the FD and ND measurements is not possible, as that
 1147 would require both detectors to have identical designs and the neutrino fluxes to be
 1148 the same. Because of the distance, the flux probed by the FD will have a different
 1149 energy and flavour composition than that at the ND, as neutrinos oscillate and the beam
 1150 spreads. The differences in the flux also determine the design of the detectors, therefore
 1151 the ND is limited in its capability to match the FD design.

1152 Nevertheless, having a highly capable ND, DUNE can minimise the systematic
 1153 uncertainties affecting the observed neutrino energy. The ND data can be used to
 1154 tune the model parameters by comparison with the prediction. Then, one uses the

CHAPTER 3. THE DEEP UNDERGROUND NEUTRINO EXPERIMENT

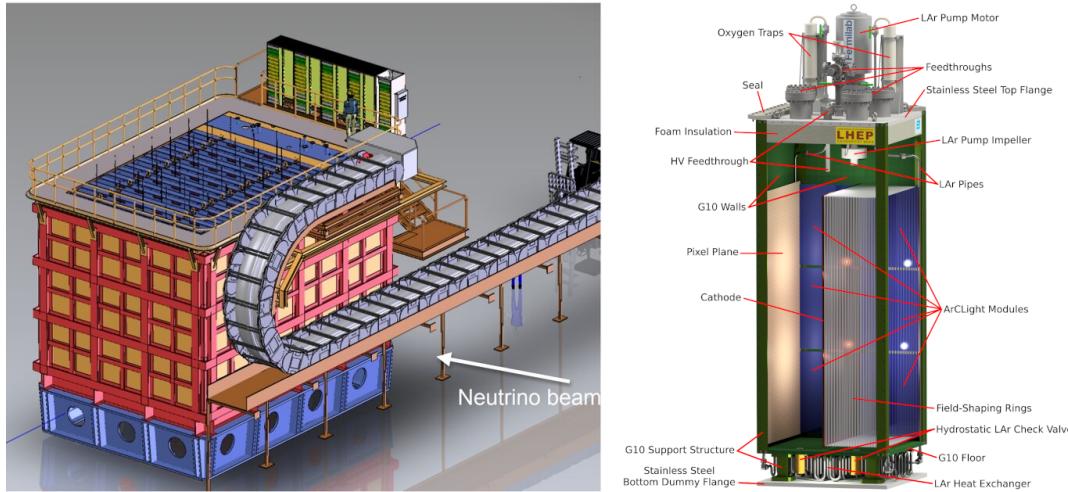


Figure 3.5: Schematic representation of the external components of ND-LAr, including the cryostat and the PRISM movable system (left) and detailed drawing of one ArgonCube module (right). Figure adapted from Ref. [83].

1155 tuned model to predict the unoscillated FD spectra. Comparing the prediction with the
 1156 measured spectra it is possible to extract the oscillation parameters.

1157 Additionally, the ND will have a physics program of its own. In particular, it will
 1158 measure neutrino cross sections that will then be used to constrain the model used in
 1159 the long-baseline oscillation analysis. It will also be used to search for BSM phenomena
 1160 such as heavy neutral leptons, dark photons, millicharged particles, etc.

1161 The DUNE ND can be divided in three main components, a LArTPC known as ND-
 1162 LAr, a magnetised muon spectrometer, which will be the Temporary Muon Spectrometer
 1163 (TMS) in Phase I and ND-GAr in Phase II, and the System for on-Axis Neutrino
 1164 Detection (SAND). The layout of the Phase II DUNE ND can be seen in Fig. 3.4. The
 1165 first two components of the ND will be able to move off-axis, in what is called the
 1166 Precision Reaction-Independent Spectrum Measurement (PRISM) concept. More details
 1167 on the purpose and design of the ND can be found in the DUNE ND Conceptual Design
 1168 Report (CDR) [91].

3.4. NEAR DETECTOR

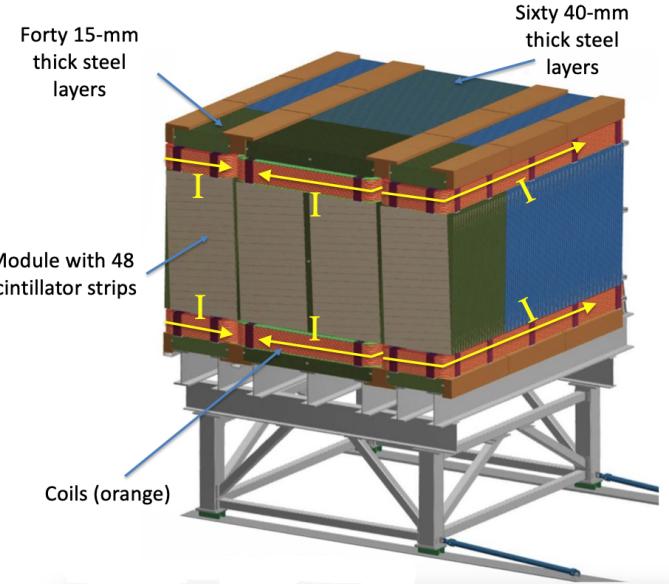


Figure 3.6: Schematic view of the TMS detector, highlighting its main parts. Figure adapted from Ref. [83].

¹¹⁶⁹ 3.4.1 ND-LAr

¹¹⁷⁰ ND-LAr is a LArTPC, as the ND needs a LAr component to reduce cross section and
¹¹⁷¹ detector systematic uncertainties in the oscillation analysis. However, its design differs
¹¹⁷² significantly from those proposed for the FD modules. Because of the high event rates
¹¹⁷³ at the ND, approximately 55 neutrino interaction events per $10 \mu\text{s}$ spill, ND-LAr will be
¹¹⁷⁴ built in a modular way. Each of the modules, based on the ArgonCube technology, is a
¹¹⁷⁵ fully instrumented, optically isolated TPC with a pixelated readout. The pixelisation
¹¹⁷⁶ allows for a fully 3D reconstruction and the optical isolation reduces the problems due
¹¹⁷⁷ to overlapping interactions. Figure 3.5 shows a representation of the external parts of
¹¹⁷⁸ ND-LAr (left) and a detailed diagram of an ArgonCube module (right).

¹¹⁷⁹ With a fiducial mass of 67 t and dimensions $7 \text{ m} (\text{w}) \times 3 \text{ m} (\text{h}) \times 5 \text{ m} (\text{l})$, ND-LAr
¹¹⁸⁰ will be able to provide high statistics and contain the hadronic systems from the beam
¹¹⁸¹ neutrino interactions, but muons with a momentum higher than 0.7 GeV will exit the
¹¹⁸² detector.

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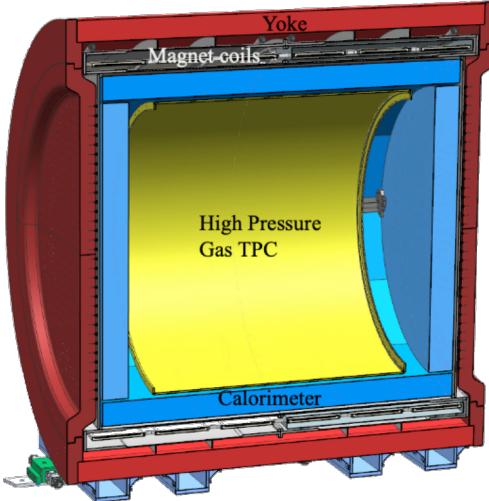


Figure 3.7: Cross section of the ND-GAr geometry, showing the HPgTPC, ECal and magnet. Figure adapted from Ref. [92].

1183 3.4.2 TMS/ND-GAr

1184 To accurately estimate the neutrino energy, the momentum of the outgoing muons needs
 1185 to be determined. That is the reason why a muon spectrometer is needed downstream
 1186 of ND-LAr.

1187 In Phase I that role will be fulfilled by TMS. It is a magnetised sampling calorimeter,
 1188 with alternating steel and plastic scintillator layers. Figure 3.6 shows a schematic view
 1189 of the TMS detector. The magnetic field allows a precise measurement of the sign of the
 1190 muon, so one can distinguish between neutrino and antineutrino interactions.

1191 After the Phase II upgrade, TMS will be replaced with a more capable near detector.
 1192 The current technology considered is ND-GAr. This detector is a magnetised, high-
 1193 pressure GAr TPC (often denoted as HPgTPC) surrounded by an electromagnetic
 1194 calorimeter (ECal) and a muon tagger. A cross section of its geometry can be seen
 1195 in Fig. 3.7. ND-GAr will be able to measure the momenta of the outgoing muons
 1196 while also detect neutrino interactions inside the GAr volume. This allows ND-GAr
 1197 to constrain the systematic uncertainties even further, as it will be able to accurately
 1198 measure neutrino interactions at low energies thanks to the lower tracking thresholds of
 1199 GAr.

3.4. NEAR DETECTOR

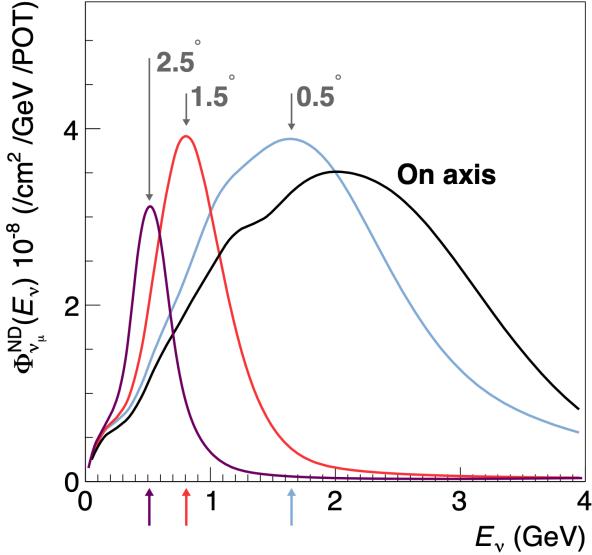


Figure 3.8: Predicted beam muon neutrino flux at the ND location for different off-axis positions. Figure taken from Ref. [91].

1200 3.4.3 PRISM

1201 In general, the observed peak neutrino energy of a neutrino beam decreases as the
 1202 observation angle with respect to the beam direction increases. This feature has been
 1203 used in other long-baseline neutrino experiments, like T2K (2.5° off-axis) and NOvA
 1204 (0.8° off-axis), to achieve narrower energy distributions. The DUNE PRISM concept
 1205 exploits this effect using a movable ND. Within PRISM both ND-LAr and the muon
 1206 spectrometer (TMS in Phase I and ND-GAr in Phase II) can be moved up to 3.2°
 1207 off-axis, equivalent to move the detectors 30.5 m laterally through the ND hall.

1208 This allows to record additional data samples with different energy compositions.
 1209 Figure 3.8 compares the on-axis muon neutrino flux at the ND with the fluxes at different
 1210 off-axis positions. As the off-axis position increases the neutrino flux becomes closer to
 1211 a monoenergetic beam with a lower peak energy. These samples can be used to perform
 1212 a data-driven determination of the relation between true and reconstructed neutrino
 1213 energy, to reduce the dependence on the interaction model. The off-axis samples are
 1214 linearly combined to produce a narrow Gaussian energy distribution centered on a target
 1215 true energy. From the combination coefficients one can build a sample of reconstructed

CHAPTER 3. THE DEEP UNDERGROUND NEUTRINO EXPERIMENT

1216 neutrino events that will determine the energy mapping.

1217 The PRISM samples will be used to form a flux at the ND location similar in shape
1218 to the oscillated flux measured by the FD. This method can be used to extract the
1219 oscillation parameters with minimal input from the neutrino interaction model.

1220 3.4.4 SAND

1221 The role of SAND is to monitor the beam stability by measuring the on-axis neutrino
1222 energy spectra. As the PRISM program requires that ND-LAr and its downstream
1223 muon spectrometer spend about half of the time in off-axis positions, it is not possible
1224 to monitor the stability with the movable detectors. Moreover, for the success of PRISM
1225 it is essential to have a stable beam configuration, or, at least, a quick assessment and
1226 modeling of the distortions.

1227 The SAND detector is magnetised, and features an inner low density tracker, a LAr
1228 target with optical readout and surrounding sampling calorimeter.

1229 3.5 A More Capable Near Detector

1230 In DUNE Phase II, a more capable near detector is needed to achieve the ultimate physics
1231 goals of the experiments. The current leading proposal for this detector is ND-GAr.
1232 As mentioned previously, it will fulfill the role of TMS, measuring the momentum and
1233 sign of the charged particles exiting ND-LAr. Additionally, it will be able to measure
1234 neutrino interactions inside the HPgTPC, achieving lower energy thresholds than those
1235 of the ND and FD LArTPCs. By doing so ND-GAr will allow to constrain the relevant
1236 systematic uncertainties for the LBL analysis even further. A detailed discussion on the
1237 requirements, design, performance and physics of ND-GAr can be found in the DUNE
1238 ND CDR [91] and the ND-GAr white paper [93].

3.5. A MORE CAPABLE NEAR DETECTOR

1239 3.5.1 Requirements

1240 The primary requirement for ND-GAr is to measure the momentum and charge of
1241 muons from ν_μ and $\bar{\nu}_\mu$ CC interactions in ND-LAr, in order to measure their energy
1242 spectrum. To achieve the sensitivity to the neutrino oscillation parameters described
1243 in the DUNE FD TDR Volume II [85], ND-GAr should be able to constrain the muon
1244 energy within a 1% uncertainty or better. The main constraint will come from the
1245 calibration of the magnetic field, which will be performed using neutral kaon decays in
1246 the HPgTPC.

1247 Another requirement for ND-GAr is the precise measurement of neutrino interactions
1248 on argon for the energies relevant to the neutrino oscillation program. The goal is to
1249 constrain the cross section systematic uncertainties in the regions of phase space that
1250 are not accessible to ND-LAr. This requires the kinematic acceptance for muons in
1251 ND-GAr to exceed that of ND-LAr, being comparable to the one observed in the FD.

1252 ND-GAr should also be able to help establishing the relationship between true and
1253 reconstructed energy from neutrino interactions on argon with low thresholds, being
1254 sensitive to particles that are not observed or may be misidentified in ND-LAr. In
1255 particular, ND-GAr needs to have low tracking thresholds in order to measure the
1256 spectrum of pions and protons produced in final-state interactions (FSI). It also must
1257 be able to accurately measure the pion multiplicity in 1, 2 and 3 pions final states, to
1258 inform the pion mass correction in the LArTPCs.

1259 3.5.2 Reference design

1260 The final design of ND-GAr is still under preparation. However, a preliminary baseline
1261 design was in place at the time of the ND CDR. This section summarises the main
1262 features of that design, as it is also the one used for the default geometry in our simulation.
1263 A DUNE Phase II white paper, discussing the different options under consideration for
1264 the ND-GAr design, is in progress.

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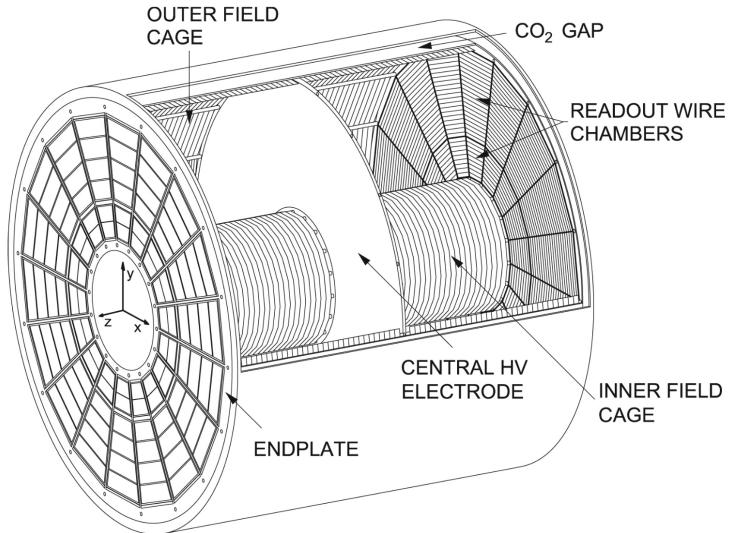


Figure 3.9: Diagram of the ALICE TPC, showing the two drift chambers, inner and outer field cages and readout chambers. Figure taken from Ref. [91].

1265 HPgTPC

1266 The reference design for the ND-GAr HPgTPC follow closely that of the ALICE TPC.
 1267 It is a cylinder with a central high-voltage cathode, generating the electric field for
 1268 the two drift volumes, with a maximum drift distance of 2.5 m each. The anodes will
 1269 be instrumented with charge readout chambers. The original design repurposed the
 1270 multi-wire proportional readout chambers (MWPCs) of ALICE, however some of the
 1271 current R&D efforts focus on a gas electron multiplier (GEM) [94] option instead. Figure
 1272 3.9 shows a schematic diagram of the ALICE TPC design. The basic ND-GAr geometry
 1273 will resemble this, except for the inner field cage.

1274 It will use a 90:10 molar fraction Ar:CH₄ mixture at 10 bar. With this baseline gas
 1275 mixture light collection is not possible, as the quenching gas absorbs most of the VUV
 1276 photons. Additional R&D efforts are underway, to understand if different mixtures allow
 1277 for the light signal to be used to provide a t_0 while maintaining stable charge gain.

3.5. A MORE CAPABLE NEAR DETECTOR

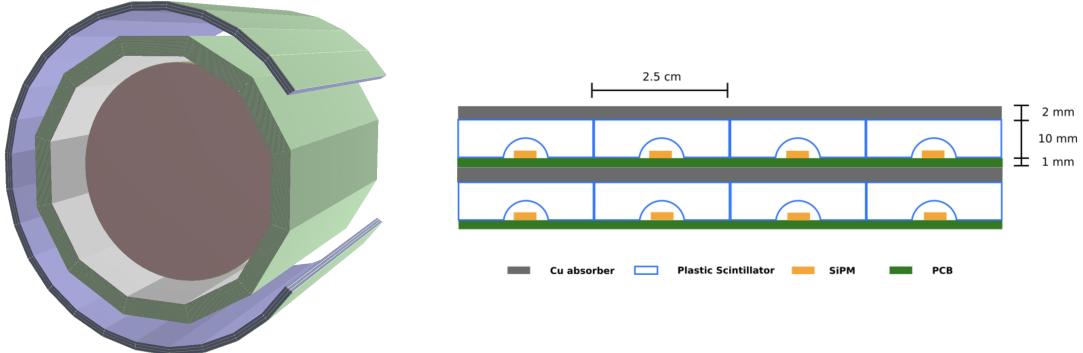


Figure 3.10: View of the 12-sided ECal barrel and outer muon tagger geometries (left) and layout of the ECal tile layers for the 2 mm Cu, 10 mm scintillator option (right). Figure adapted from Ref. [91].

1278 ECal

1279 The main role of the ND-GAr ECal is the calorimetric measurement of the electron
 1280 energies and the reconstruction of photons, in particular those from neutral pion decays.
 1281 Also, the ECal is able to provide a t_0 timestamp for neutrino interactions, by associating
 1282 its activity to the tracks in the HPgTPC. The ECal will also be able to perform
 1283 neutron reconstruction using time of flight and reject external backgrounds, thanks to
 1284 its sub-nanosecond time resolution.

1285 The ECal design features three independent subdetectors, two end caps at each side
 1286 and a barrel surrounding the HPgTPC. Each of the detectors is divided in modules,
 1287 which combine alternating layers of plastic scintillator and absorber material readout
 1288 by SiPMs. The inner scintillator layers consist of $2.5 \times 2.5 \text{ cm}^2$ high-granularity tiles,
 1289 whereas the outer ones are made out of 4 cm wide cross-strips spanning the whole
 1290 module length. The current barrel geometry consists of 8 tile layers and 34 strip layers,
 1291 while the end caps feature 6 and 36 respectively. The thickness of the scintillator layers
 1292 is 7 mm and 5 mm for the Pb absorber layers. The 12-sided geometry of the ECal barrel
 1293 (left) and the layout of the tile layers (left)¹ can be seen in Fig. 3.10.

¹The figure shows the layout of the tile layers for a previous design with 2 mm Cu absorber and 10 mm plastic scintillator, as mentioned in the text the current choice is 5 mm Pb absorber and 7 mm scintillator.

CHAPTER 3. THE DEEP UNDERGROUND NEUTRINO EXPERIMENT

1294 Magnet

1295 The ND-GAr magnet design, know as the Solenoid with Partial Yoke (SPY), consists of
1296 two coupled solenoids with an iron return yoke. The idea behind the design is to have a
1297 solenoid as thin as possible, as well as a return yoke mass distribution that minimises
1298 the material budget between ND-LAr and ND-GAr. The magnet needs to provide a
1299 0.5 T field in the direction perpendicular to the beam, parallel to the drift electric field.
1300 It needs to host the pressure vessel and the surrounding ECal, which points to a inner
1301 diameter of ~ 6.4 m.

1302 The solenoid is a single layer coil, based on niobium titanium superconducting
1303 Rutherford cable. The total length of the coil is 7.5 m. The bobbin will be split in four
1304 segments grouped in pairs with two identical cryostats, connected in series. The iron
1305 yoke features an aperture in the upstream side to allow the muons coming from ND-LAr.
1306 Still, its material will be enough to reduce the magnetic field reaching SAND, and also
1307 stop the charged pions produced inside the HPgTPC.

1308 Muon system

1309 The design of the ND-GAr muon system is still in a preliminary stage. Its role is to
1310 distinguish between muons and pions punching through the ECal. This is especially
1311 important for wrong-sign determination, to separate these from neutral current events.

1312 In its current form, the muon system consists of three layers of longitudinal sampling
1313 structures. It alternates 10 cm Fe absorber slabs with 2 cm plastic scintillator strips.
1314 The transverse granularity required is still under study.

1315 3.5.3 R&D efforts

1316 There are several ND-GAr-related prototypes, mostly focused on the TPC charge
1317 readout and electronics. The priority is to test the full readout chain, in a high-pressure
1318 environment, using a gas mixture with high argon fraction. A detailed summary of these
1319 can be found in the DUNE Phase II white paper [92].

3.5. A MORE CAPABLE NEAR DETECTOR

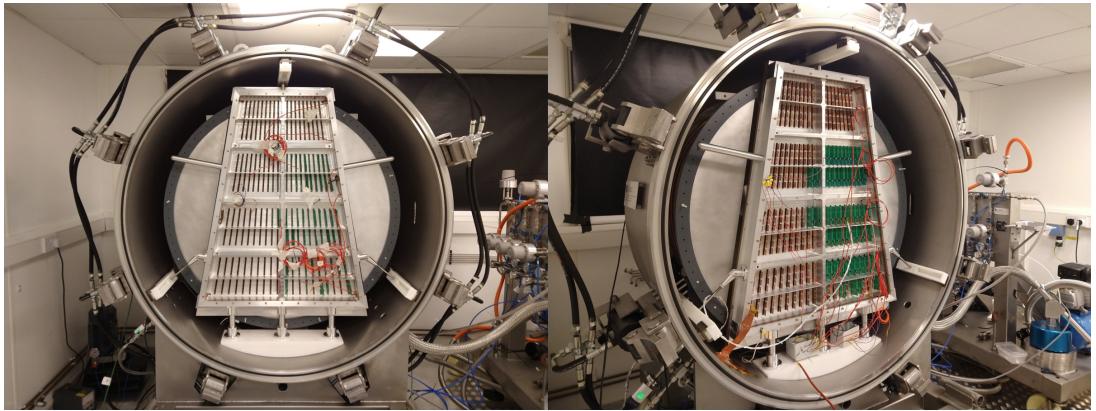


Figure 3.11: Photographs of the TOAD pressure vessel at RHUL. The TPC is mounted inside the vessel, and the OROC is supported by an aluminium frame. Figure taken from Ref. [95].

1320 Multi-Wire Proportional Chambers

1321 As mentioned before, the original ND-GAr design repurposes the MWPCs of the ALICE
1322 TPC, which became available after the recent upgrade [96]. These were operated using
1323 a 90:10:5 Ne:CO₂:N₂ gas mixture at 1 atm. Therefore, their performance needed to be
1324 studied in an argon gas environment at high pressure.

1325 The Gas-argon Operation of ALICE TPC (GOAT) test stand tested the ALICE
1326 readout chambers at high pressure. In particular, it used one of the previously operated
1327 ALICE inner MWPCs, also known as IROCs, in a pressure vessel rated to 10 atm. It
1328 measured the gas gain at various pressure points, voltages and gas mixtures.

1329 The Test stand of an Overpressure Argon Detector (TOAD) tested an ALICE outer
1330 MWPC, also known as OROC, up to 5 atm. During its time at RHUL, it was used to
1331 study the achievable gas gain of the OROC [95]. At the moment, it is being commissioned
1332 at Fermilab for a full detector test of the readout electronics and the DAQ.

1333 Figure 3.11 shows the interior of the TOAD pressure vessel. The TPC is mounted
1334 inside the vessel on three rails. The back of the OROC, supported by an aluminium
1335 frame, can be seen at the front.

CHAPTER 3. THE DEEP UNDERGROUND NEUTRINO EXPERIMENT

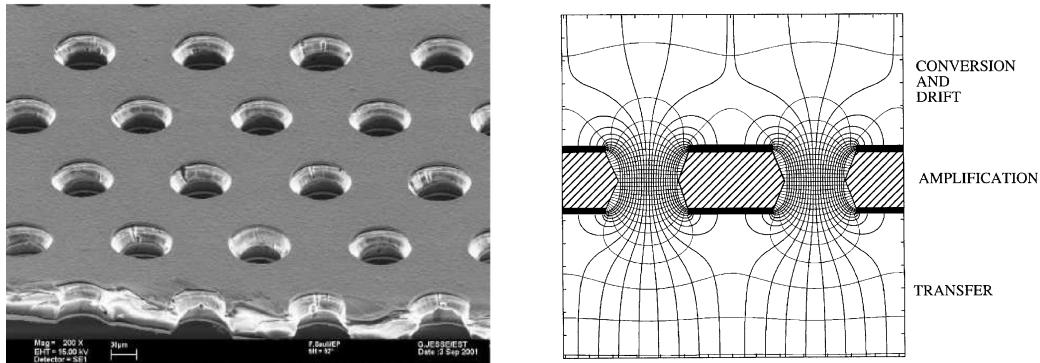


Figure 3.12: Left panel: electron microscope image of a 50 μm thick GEM electrode, with hole pitch and diameter of 140 and 70 μm , respectively. Right panel: Schematics of a GEM electrode cross section, showing the electric field lines around the holes. Figures taken from Ref. [97].

1336 Gas Electron Multiplier

1337 An alternative to the MWPC option is the use of GEMs. These are a type of micro-patter
 1338 detector, where the ionisation electrons passing through the holes in the GEM layers
 1339 are accelerated by a high intensity electric field. The acceleration causes the electrons
 1340 to ionise the medium, resulting in an avalanche which increase the signal exponentially
 1341 [94]. GEMs are used in numerous experiments that need a high spatial resolution, like
 1342 ALICE [98] and CMS [99] after their upgrades.

1343 Figure 3.12 (left panel) shows an electron microscope picture of a 50 μm thick GEM
 1344 electrode, with a pitch between neighbouring holes of 140 μm and a hole diameter of
 1345 70 μm . A schematic representation of the cross section of a GEM layer is shown in Fig.
 1346 3.12 (left panel).

1347 The Gaseous Argon T0 (GAT0²) prototype studies the use of thick GEMs made out
 1348 of glass to achieve optical imaging of the primary ionisation. Using a 10 atm pressure
 1349 vessel, the goal is to study different argon-based mixtures that allow for a precise t_0
 1350 determination.

1351 The GEM Over-pressurized with Reference Gases (GORG³) test stand is currently
 1352 testing a GEM-based charge readout, using a triple-GEM stack.

²Spanish for cat.

³Persian for wolf.

3.6. FAR DETECTOR

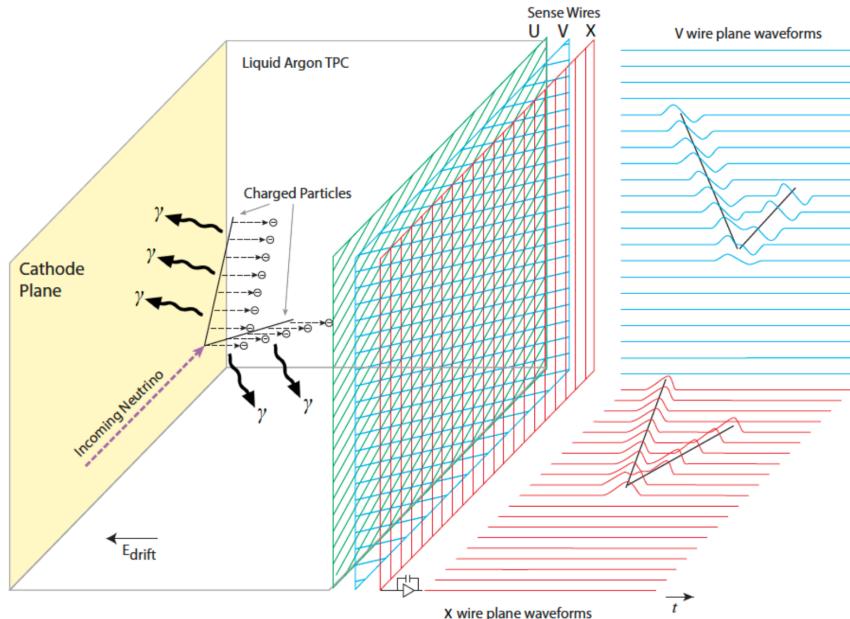


Figure 3.13: Schematic diagram showing the operating principle of a LArTPC with wire readout. Figure taken from Ref. [83].

1353 3.6 Far Detector

1354 The DUNE FD complex will sit 1300 km away from the beam target and 1.5 km
 1355 underground at SURF, South Dakota. Two caverns will host the four FD modules, two
 1356 of them per cavern, each embedded in cryostats of dimensions 18.9 m (w) × 17.8 m (h) ×
 1357 65.8 m (l). A central, smaller cavern will host the cryogenic system.

1358 Three out of the four modules will be liquid argon (LAr) time projection chamber
 1359 detectors, often refer to as LArTPCs, with a LAr fiducial mass of at least 10 kt each.
 1360 The first and second FD modules, FD-1 and FD-2, will use a Horizontal Drift (HD)
 1361 technology, whereas the third module, FD-3, will have a Vertical Drift (VD) direction.
 1362 The technology for the fourth module is still to be decided,

1363 For each event, with energies ranging from a few MeV to several GeV, these detectors
 1364 collect both the scintillation light and the ionisation electrons created when the charged
 1365 particles produced in neutrino-nucleus interactions ionise the argon nuclei. In both HD
 1366 and VD designs the characteristic 128 nm scintillation light of argon is collected by a
 1367 photon detection system (PDS). This light will indicate the time at which electrons

CHAPTER 3. THE DEEP UNDERGROUND NEUTRINO EXPERIMENT

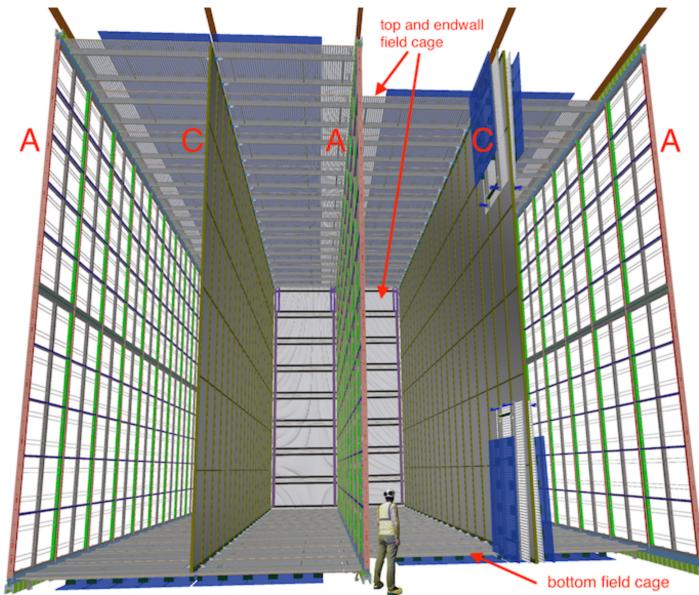


Figure 3.14: Proposed design for the FD-1 and FD-2 modules following the HD principle. Figure taken from Ref. [83].

1368 start to drift, thus enabling reconstruction over the drift coordinate when compared
 1369 to the time when the first ionisation electron arrives to the anode. Reconstruction of
 1370 the topology in the transverse direction is achieved using the charge readout. Fig. 3.13
 1371 illustrates the detection principle described, for the case of a HD detector with a wire
 1372 readout.

1373 3.6.1 Horizontal Drift

1374 The HD design the ionisation electrons produced as charged particles traverse the LAr
 1375 drift horizontally towards the anode planes, due to the effect of an electric field. These
 1376 anode planes are made out of three layers of wire readout. This design, previously
 1377 known as single-phase (SP), was tested by the ProtoDUNE-SP detector at CERN. The
 1378 prototype collected data from a hadron beam and cosmic rays, providing high-quality
 1379 data sets for calibration and performance studies.

1380 Each FD HD detector module is divided in four drift regions, with a maximum drift
 1381 length of 3.5 m, by alternating anode and cathode walls. The surrounding field cage
 1382 ensures the uniformity of the 500 V/cm horizontal electric field across the drift volumes.

3.6. FAR DETECTOR

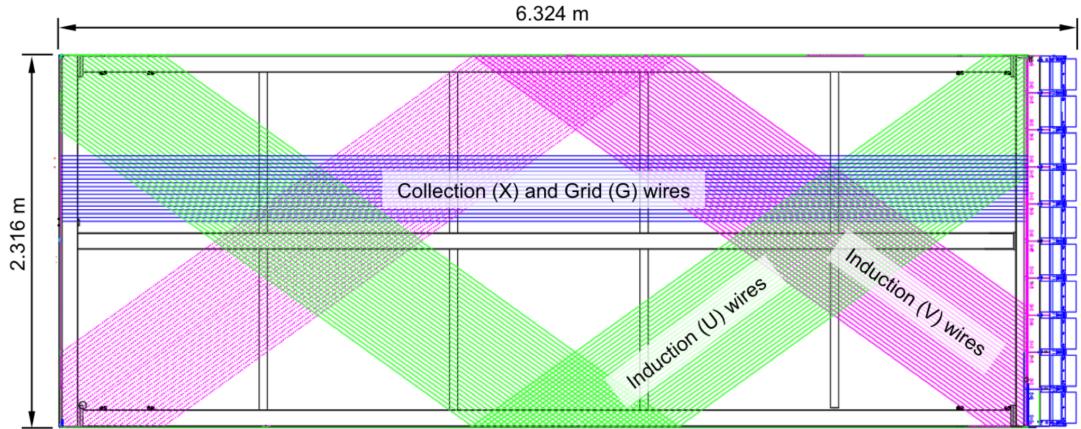


Figure 3.15: Schematic representation of an APA. The black lines represent the APA steel frame. The green and magenta lines correspond to the direction of the U and V induction wires respectively. The blue lines indicate the direction of the X collection wires and the wire shielding G. Figure taken from Ref. [83].

1383 The three anode walls, which constitute the charge readout of the detector, are built by
 1384 stacking anode plane assemblies (APAs), 2 high times 25 wide. The design of the HD
 1385 modules is shown in Fig. 3.14.

1386 Each APA is made of 2560 active wires arranged in three layers, plus an extra grid
 1387 layer, wrapped around a metal frame. The two induction wire planes, U and V, sit at
 1388 $\pm 35.7^\circ$ to the vertical on each side of the APA. The collection and shielding plane wires,
 1389 X and G, run parallel to the vertical direction. The ionisation electrons drift past the
 1390 induction planes, generating bipolar signals on those wires, and are collected by the
 1391 collection plane, producing a monopolar positive signal. The spacing between the wires
 1392 is ~ 5 mm, and it defines the spatial resolution of the APA.

1393 The front-end readout electronics, or cold electronics as they are immerse in the LAr,
 1394 are attached to the top of the up APAs and the bottom of the down APAs. Mounted on
 1395 the front-end mother boards we have a series of ASICs that digitize the signals from the
 1396 collection and induction planes. Each wire signal goes to a charge-sensitive amplifier,
 1397 then there is a pulse-shaping circuit and this is followed by the analogue-to-digital
 1398 converter. This part of the process happens inside the LAr to minimise the number of
 1399 cables penetrating the cryostat. The digitised signals come out finally via a series of

CHAPTER 3. THE DEEP UNDERGROUND NEUTRINO EXPERIMENT

1400 high-speed serial links to the warm interface boards (WIBs), from where the data is sent
1401 to the back-end DAQ through optical fibers.

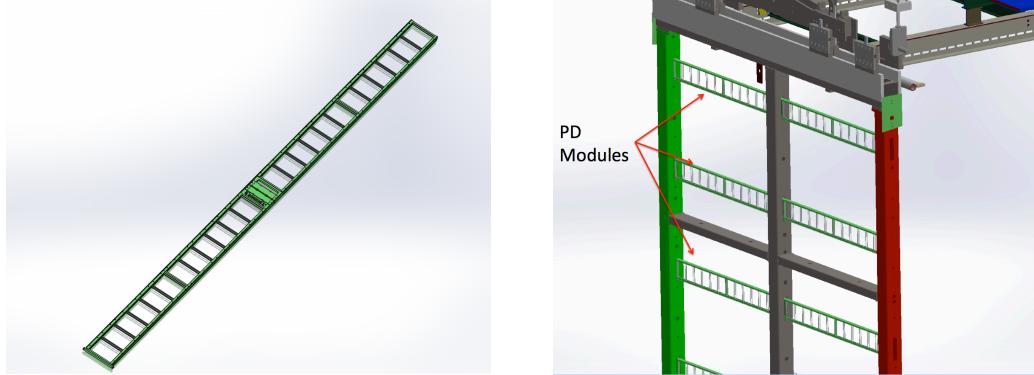


Figure 3.16: A PDS module containing 24 X-ARAPUCAs (left) and the location of the modules on the APAs (right). Figure taken from Ref. [83].

1402 The PDS uses modules of X-ARAPUCA devices, mounted on the APA frames
1403 between the wire planes. Each X-ARAPUCA consists of layers of dichroic filter and
1404 wavelength-shifter. They shift the VUV scintillation light into the visible spectrum,
1405 sending then the visible photons to silicon photomultiplier (SiPM) devices. The PDS
1406 modules are 209 cm × 12 cm × 2 cm bars, containing 24 X-ARAPUCAs. There are 10
1407 of these PDS modules per APA. Fig. 3.16 shows a PDS module (left) and the placement
1408 of the modules on the APAs (right).

1409 3.6.2 Vertical Drift

1410 In the VD case the ionisation electrons will drift vertically until they meet a printed
1411 circuit board-based (PCB) readout plane. It is based on the original dual-phase (DP)
1412 design deployed at CERN, known as ProtoDUNE-DP, used a vertical drift design with
1413 an additional amplification of the ionization electrons using a gaseous argon (GAr) layer
1414 above the liquid phase. The VD module incorporates the positive features of the DP
1415 design without the complications of having the LAr-GAr interface.

1416 The current design of the FD VD module counts with two drift chambers with a
1417 maximum drift distance of 6.5 cm. A cathode plane splits the detector volume along the
1418 drift direction while the two anode planes are connected to the bottom and top walls

3.6. FAR DETECTOR

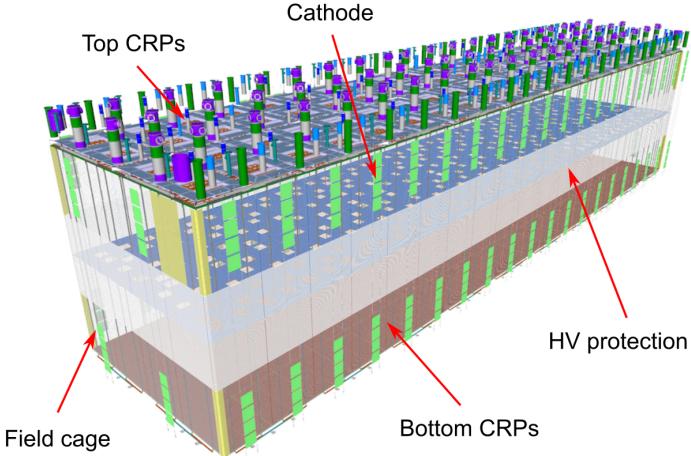


Figure 3.17: Proposed design for the FD-3 module following the VD principle. Figure adapted from Ref. [100].

of the detector. The layout of the VD module is shown in Fig. 3.17. Compared with the HD design, the VD option offers a slightly larger instrumented volume and a more cost-effective solution for the charge readout.

As in the HD design, each drift volume features a 500 V/cm electric field and a field cage that ensures its uniformity. The anode planes are arrays of 3.4 m × 3 m charge-readout planes (CRPs). These are formed by a pair of charge-readout units (CRUs), which are built from two double-sided perforated PCBs, with their perforations aligned. The perforations allow the drift electrons to pass between the layers.

The PCB face opposite to the cathode has a copper guard plane which acts as shielding, while its reverse face is etched with electrode strips forming the first induction plane. The outer PCB has electrode strips on both faces, the ones facing the inner PCB form the second induction plane while the outermost ones form the collection plane. Fig. 3.18 shows the layout of the electrode strips for the top (left) and bottom (right) CRUs. The magenta and blue lines represent the first and second induction planes respectively, and the green lines correspond to the collection plane.

The PDS in the VD module will use the same X-ARAPUCA technology developed for the HD design. The plan is to place the PDS modules on the cryostat walls and on

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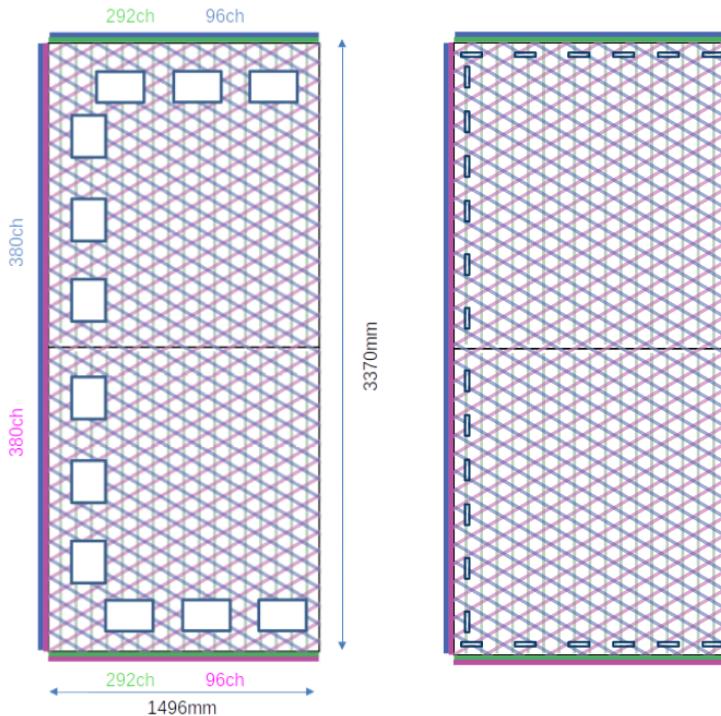


Figure 3.18: Schematic representation of the electrode strip configuration for a top (left) and bottom (right) CRU. Figure taken from Ref. [100].

1436 the cathode, in order to maximise the photon yield.

1437 3.6.3 FD Data Acquisition System

1438 The data acquisition (DAQ) system receives, processes and stores data from the detector
1439 modules. In the case of DUNE the DAQ architecture is designed to work for all FD
1440 modules interchangeably, except some aspects of the upstream part which may depend
1441 on the specific module technology.

1442 The enormous sample rate and the number of channels in TPC and PD readouts
1443 will produce a very large volume of data. These pose really strong requirements and
1444 challenges to the DUNE FD DAQ architecture. It will be required to read out data of
1445 the order of ten thousand or more channels at rates of a few MHz. To cope with the
1446 huge data volume, segmented readouts and compression algorithms are used to reduce
1447 the data rate to manageable levels.

1448 The DAQ system of the DUNE FD is composed of five different subsystems. The

3.6. FAR DETECTOR

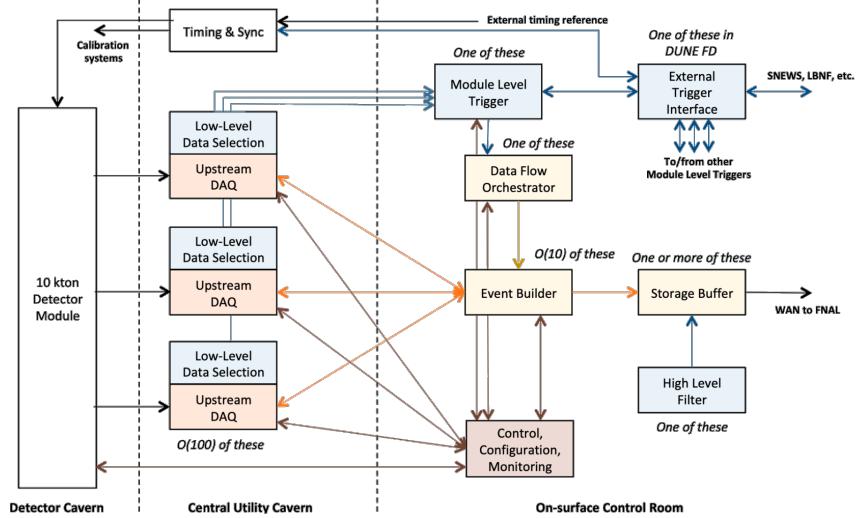


Figure 3.19: Detailed diagram of the DUNE FD DAQ system. Figure taken from Ref. [101].

1449 first one is the upstream DAQ, which receives the raw data from the detector, buffers it
 1450 and perform some low-level pre-processing. The minimally processed data is then fed
 1451 into a hierarchical data selection system, which then performs a module level trigger
 1452 decision. In case of a positive decision a trigger command is produced and executed by
 1453 the data flow orchestrator, located in the back-end (BE) DAQ subsystem. Subsequently
 1454 the DAQ BE retrieves the relevant data from the buffers located in the upstream DAQ,
 1455 adds all the data into a cohesive record and saves it to permanent storage. Watching
 1456 over all the other subsystems we also have the control, configuration and monitoring
 1457 subsystem and the time and synchronization subsystem. Figure 3.19 shows a schematic
 1458 diagram of the DAQ system, showing the different subsystems and their relations.

1459 A notorious challenge for the DUNE DAQ system comes from its broad physics
 1460 goals. We must be prepared to process events spanning a wide range of time windows
 1461 (from 5 ms in the case of beam and cosmic neutrinos and nucleon decay to 100 s in the
 1462 case of SNBs) and therefore this requires a continuous readout of the detector modules.
 1463 Moreover, because of the off-beam measurements we need to ensure the capabilities
 1464 of online data processing and self-triggering. Having this into account, together with
 1465 the technical constraints, the DUNE FD DAQ faces a series of challenges: it needs to

CHAPTER 3. THE DEEP UNDERGROUND NEUTRINO EXPERIMENT

- 1466 be fault tolerant and redundant to reduce downtime, accommodate new components
- 1467 while it keeps serving the operational modules, have large upstream buffers to handle
- 1468 SNB physics, be able to support a wide range of readout windows and last reduce the
- 1469 throughput of data to permanent storage to be at most 30 PB/year.

1470

1471

Matched Filter approach to Trigger

1472

Primitives

4.1 Motivation

1474 The filter implemented in the firmware of the upstream DUNE FD DAQ is a 32nd-order
 1475 low-pass finite impulse-response (FIR) filter. The output of such filter for a discrete
 1476 system can be written as:

$$y[i] = \sum_{j=0}^N h[j]x[i-j], \quad (4.1)$$

1477 where N is the order of the filter, y is the output sequence, x is the input sequence and h
 1478 is the set of coefficients of the filter. The current implementation within `dtp-firmware`
 1479 [102] uses a set of 16 non-zero integer coefficients.

1480 Filtering is a vital step in the hit finder chain. It helps to suppress the noise and
 1481 enhance the signal peaks with respect to the noiseless baseline. A good filtering strategy
 1482 allows us to use lower thresholds when forming the trigger primitives (TPs) and thus
 1483 increasing the sensitivity of our detector to low energy physics events. In such events,
 1484 the hits produced by the ionisation electrons tend to have lower amplitudes than those
 1485 of interest to the baseline physics programme of the DUNE experiment.

1486 This is particularly important for the induction planes. In general, signal peaks in
 1487 the induction wires have smaller amplitude than the ones in the induction plane. This,
 1488 together with the fact that the pulse shapes are bipolar, reduces our capacity to detect

CHAPTER 4. MATCHED FILTER APPROACH TO TRIGGER PRIMITIVES

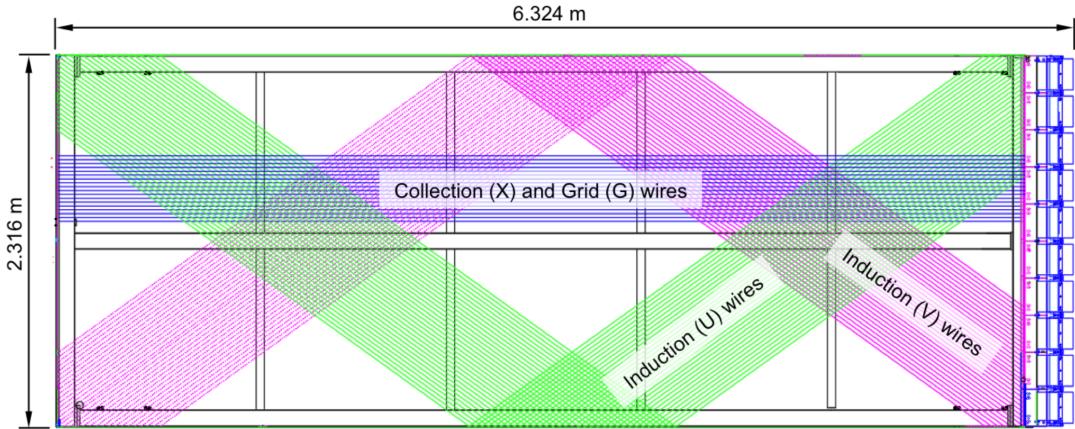


Figure 4.1: Schematic representation of an APA. The black lines represent the APA steel frame. The green and magenta lines correspond to the direction of the U and V induction wires respectively. The blue lines indicate the direction of the X collection wires and the wire shielding G.

1489 the hits on these channels. The inefficiency of detecting TPs in the induction planes
 1490 (denoted as U and V planes) lead trigger algorithms to focus mainly on the TPs from
 1491 the collection plane (so-called X plane). As a result, the possibility of making trigger
 1492 decisions based on the coincidence of TPs across the three wire planes remains nowadays
 1493 unexploited in DUNE. Fig. 4.1 shows a schematic view of an anode plane assembly
 1494 (APA), with the different wire plane orientations highlighted.

1495 A possible improvement of the current hit finder chain could require optimising
 1496 the existing or choosing a new filter implementation. A filter strategy which improves
 1497 the induction signals may be able to enhance the detection efficiency of TPs from the
 1498 induction planes and ideally make it comparable to that of the collection plane.

1499 The goal is to implement a better finite-impulse response filter design and to evaluate
 1500 its performance relative to the current filter. To do so, we need to take into account the
 1501 limitations of the firmware: the FIR filter shall have maximum 32 coefficients (so-called
 1502 taps) whose values are 12-bit unsigned integers. Although it is technically possible to
 1503 include non-integer coefficients, it would be a technical challenge as we have 40 FIR
 1504 instances per APA, as there are 4 FIR per optical link and 10 optical links per APA.
 1505 With these restrictions, the task is to provide a set of 32 coefficients which yield an

4.2. SIGNAL-TO-NOISE RATIO DEFINITION

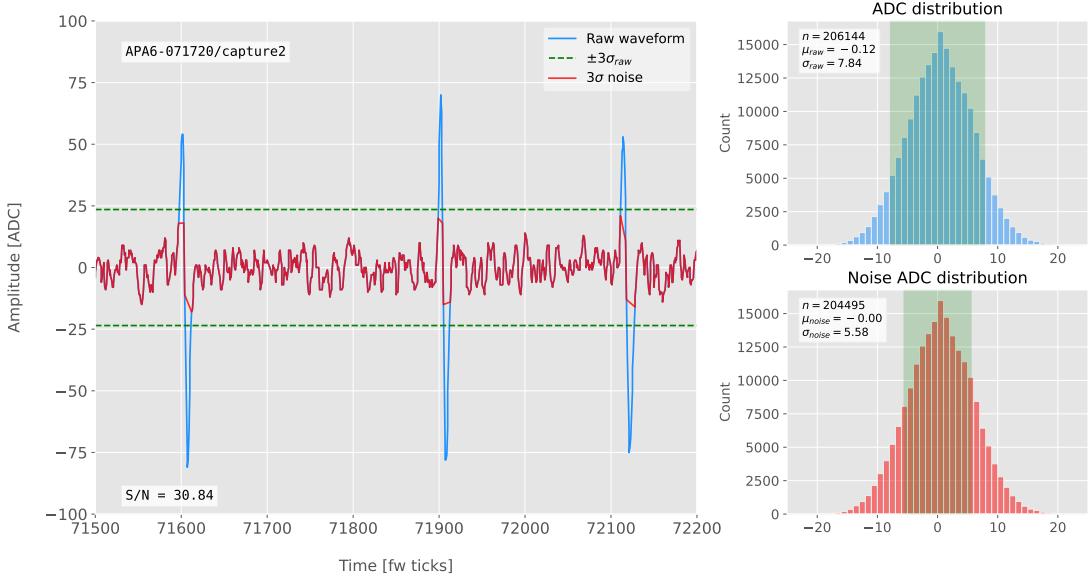


Figure 4.2: Left panel: Zoomed unfiltered waveform corresponding to channel 7840 from the ProtoDUNE-SP raw data capture `felix-2020-07-17-21:31:44` (blue line). The green dashed lines mark the region $\pm 3\sigma_{\text{raw}}$. The resulting noise waveform is also shown (red line). Top right panel: ADC distribution for channel 7840, where the green shaded region represents $\pm \sigma_{\text{raw}}$. Bottom right panel: noise ADC distribution for channel 7840, where the green shaded region represents $\pm \sigma_{\text{noise}}$.

1506 optimal filter performance for the induction wires.

1507 4.2 Signal-to-noise ratio definition

1508 I introduce the signal to noise ratio (S/N) as a measure of the FIR filter performance
 1509 and demonstrate how to extract its value for a set of ProtoDUNE-SP data. The S/N
 1510 metrics allow us to compare different filter implementations and serve as a basis for more
 1511 detailed studies presented later in this document. Specifically, I use the ADC capture
 1512 `felix-2020-07-17-21:31:44` (data capture taken for firmware validation purposes). I
 1513 defined S/N as the height of the signal peaks relative to the size of the noise peaks.
 1514 To quantify this quantity channel by channel one first need to estimate the standard
 1515 deviation of the ADC data for each channel, σ_{ADC} . Then, I define the corresponding
 1516 noise waveform to be the ADC values in the range $\pm 3\sigma_{\text{ADC}}$. From this new noise data
 1517 one can estimate again the mean and standard deviation, μ_{noise} and σ_{noise} , so I can

CHAPTER 4. MATCHED FILTER APPROACH TO TRIGGER PRIMITIVES

1518 write the S/N for any given channel as:

$$S/N = \frac{\max[ADC] - \mu_{noise}}{\sigma_{noise}}, \quad (4.2)$$

1519 where $\max[ADC]$ is simply the maximum ADC value found in the corresponding channel.

1520 One can apply this definition of the S/N with a waveform from one of the channels
1521 of the data capture¹. Fig. 4.2 shows a zoomed region of the waveform corresponding to
1522 channel 7840 (blue line), where one can clearly see three signal peaks and continuous
1523 additive noise (we actually see 6 peaks, 3 positive and 3 negative, but, because by design
1524 for induction channels the expected signal pulse shapes are bipolar, I treat them as a
1525 collection of 3 individual signal peaks). I estimated the standard deviation of this raw
1526 waveform to be $\sigma_{raw} = 7.84$ ADC, so I am able to define the noise waveform (red line)
1527 as the ADC values in the range ± 23.52 ADC. This way one obtains $\mu_{noise} = 0$ and
1528 $\sigma_{noise} = 5.58$ ADC, which gives $S/N = 30.84$.

1529 We can repeat this calculation now for the corresponding filtered waveform (using the
1530 current firmware FIR filter). In Fig. 4.3 I plotted the same time window for the filtered
1531 waveform from channel 7840 (blue line). In this case, the standard deviation of the
1532 waveform is larger than before, giving $\sigma_{raw} = 10.99$ ADC. The resulting noise waveform
1533 (red line) results from selection the ADC values in the range ± 32.91 ADC, giving now
1534 $\mu_{noise} = -0.47$ ADC and $\sigma_{noise} = 7.03$ ADC. Finally, one obtains $S/N = 24.68$. Notice
1535 that the value of S/N decreases after the filtering. Clearly, one can see that the noise
1536 baseline has increased by a factor of 1.35 when we applied the FIR filter and at the same
1537 time the amplitude of the signal peaks has remained almost unchanged, leading to this
1538 poorer S/N value.

¹All the original work was done within the `dtp-simulation` package [103], which offers a variety of tools to read raw data and emulate the TPG block (pedestal subtraction, filtering and hit finder). However, the results shown in this report were re-worked later using the C++ based `dtpemulator` package [104]. Its main purpose is the emulation of the TPG block and, in the same way as its predecessor, it has been cross-checked against the current firmware implementation.

4.3. LOW-PASS FIR FILTER DESIGN

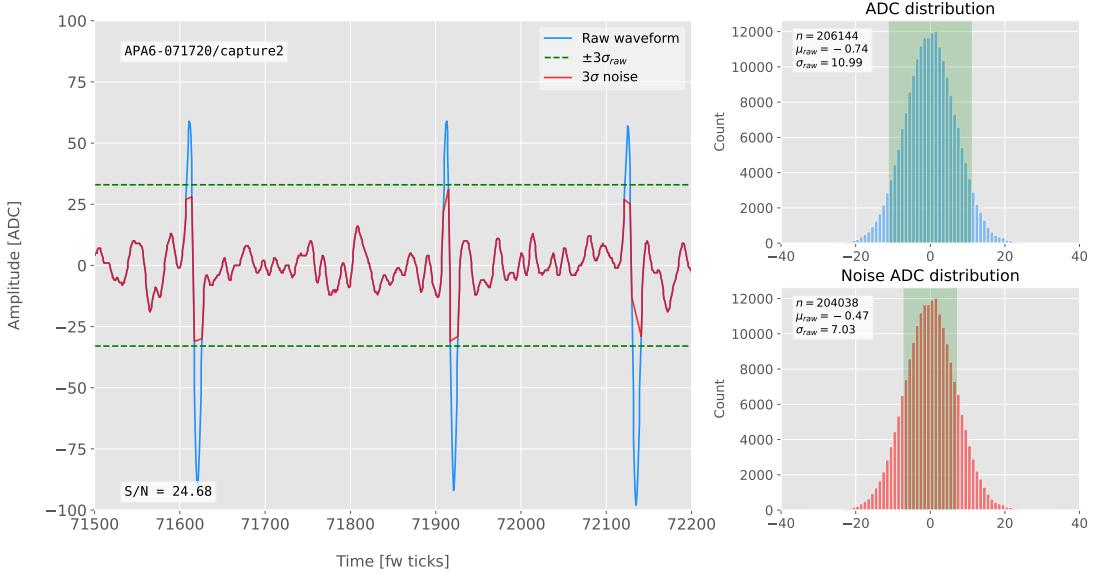


Figure 4.3: Left panel: Zoomed filtered waveform corresponding to channel 7840 from the ProtoDUNE-SP raw data capture `felix-2020-07-17-21:31:44` (blue line). The filter used was the current implementation of the low-pass FIR filter in `dtp-firmware`. The green dashed lines mark the region $\pm 3\sigma_{\text{raw}}$. The resulting noise waveform is also shown (red line). Top right panel: ADC distribution for channel 7840 after filtering, where the green shaded region represents $\pm \sigma_{\text{raw}}$. Bottom right panel: noise ADC distribution for channel 7840 after filtering, where the green shaded region represents $\pm \sigma_{\text{noise}}$

1539 4.3 Low-pass FIR filter design

1540 In general, when one uses a method to optimize the frequency response of a digital filter,
 1541 such as the Parks-McClellan algorithm, one finds a set of N real coefficients that give
 1542 the best response for the specified pass-band and order of the filter [105].

1543 In our case, as the sampling frequency is defined as 1 ticks^{-1} , the Nyquist frequency
 1544 will simply be $1/2 \text{ ticks}^{-1}$. The current implementation of the filter seems to have as
 1545 pass-band the range $[0, 0.1] \text{ ticks}^{-1}$. This can be seen in Fig. 4.4, where I show the
 1546 power spectrum, in decibels, of such filter implementation (blue solid line). For instance,
 1547 the Park-McClellan algorithm finds the optimal Chebyshev FIR filter taking as input
 1548 the boundaries of the target pass-band and stop-band, which can be written in the form:

$$\left\{ \begin{array}{l} [0, f_c] \\ [f_c + \delta f, f_N] \end{array} \right. , \quad (4.3)$$

CHAPTER 4. MATCHED FILTER APPROACH TO TRIGGER PRIMITIVES

where f_c is the cut-off frequency, δf is the transition width and f_N is the aforementioned Nyquist frequency. A similar behaviour to the one in the current filter can be obtained by setting $f_c = 0$ and $\delta f = 0.1 \text{ ticks}^{-1}$. The response of the resulting filter is also shown in Fig. 4.4 (blue solid line). Notice that the suppression of the stop-band is enhanced for this optimal filter. For comparison I included the power response of the filter obtained by taking the integer part of the coefficients resulting from the Parks-McClellan method (red dashed line). One can see that it does not suppress that much the stop-band, in a similar way to the current implementation of the filter.

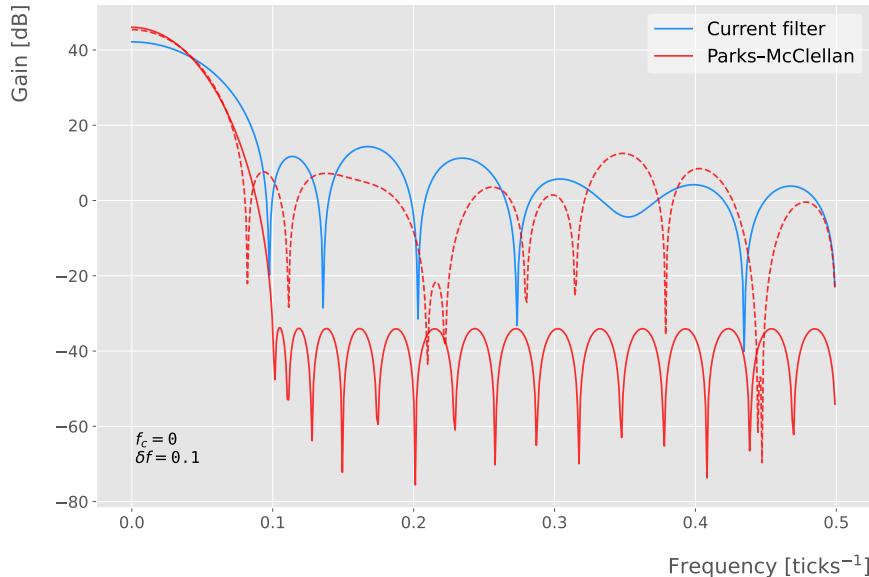


Figure 4.4: Power spectrum in decibels for the current implementation of the low-pass FIR filter in `dtp-firmware` (blue line), compared to the response of an optimal filter obtained using the Parks-McClellan algorithm for the same pass-band (red line). Also for comparison I include the spectrum of the optimal filter when taking only the integer part of the coefficients (red dashed line).

At this point, I tried to improve the performance of the FIR filter using the Parks-McClellan method, i.e. maximize the overall S/N, using the available data captures. I did so by varying the values of the two quantities that parametrize the pass-band and stop-band, the cut-off frequency f_c and the transition width δf .

Fig. 4.5 shows the average relative change in the S/N (i.e. the ratio between the value of the S/N after and before the filtering) for capture `felix-2020-07-17-21:31:44`,

4.3. LOW-PASS FIR FILTER DESIGN

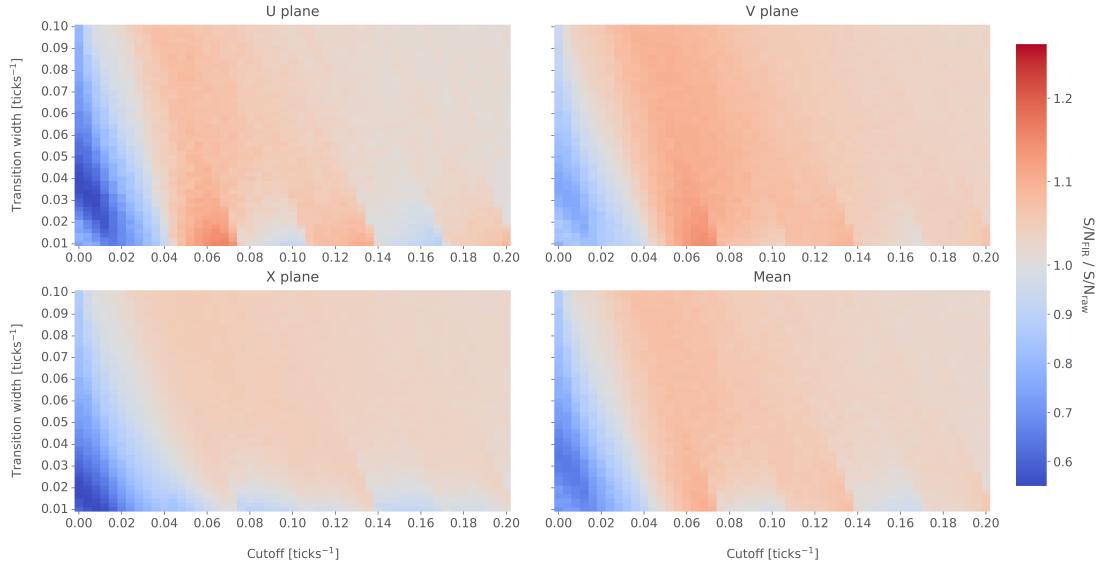


Figure 4.5: Relative change in the S/N for the ProtoDUNE-SP raw data capture `felix-2020-07-17-21:31:44`, using different values of the cutoff frequency f_c and the transition width δf . The optimal Chebyshev filters were applied using just the integer part of the coefficients given by the Parks-McClellan algorithm.

when using filters designed with the Parks-McClellan algorithm for the specified values of the cut-off frequency f_c and the transition width δf , restricted to integer values for the filter coefficients. One can clearly distinguish different regions where we get an improvement of up to a factor of 1.35 for the U plane. For large values of $f_c + \delta f$ the ratio tends to 1, as expected (in that limit the width of the stop-band goes to 0, meaning that no frequencies are filtered out and thus the waveform remains the same).

Using the configuration which gives the best mean performance for the three planes (see bottom right panel of Fig. 4.5), i.e. $f_c = 0.068 \text{ ticks}^{-1}$ and $\delta f = 0.010 \text{ ticks}^{-1}$, we can see how such filter affects the different channels. Fig. 4.6 shows the distribution of the S/N improvement values for all the channels in the raw ADC capture `felix-2020-07-17-21:31:44`, separated by wire plane, after the optimal Chebyshev filter was applied. One can see that there is a clear improvement for both U and V induction wire planes, obtaining a mean change of 1.25 and 1.30 for them respectively. However, in the case of the collection plane X the mean of this distribution is roughly 1, meaning that a good fraction of channels in that plane get a slightly worse S/N after the

CHAPTER 4. MATCHED FILTER APPROACH TO TRIGGER PRIMITIVES

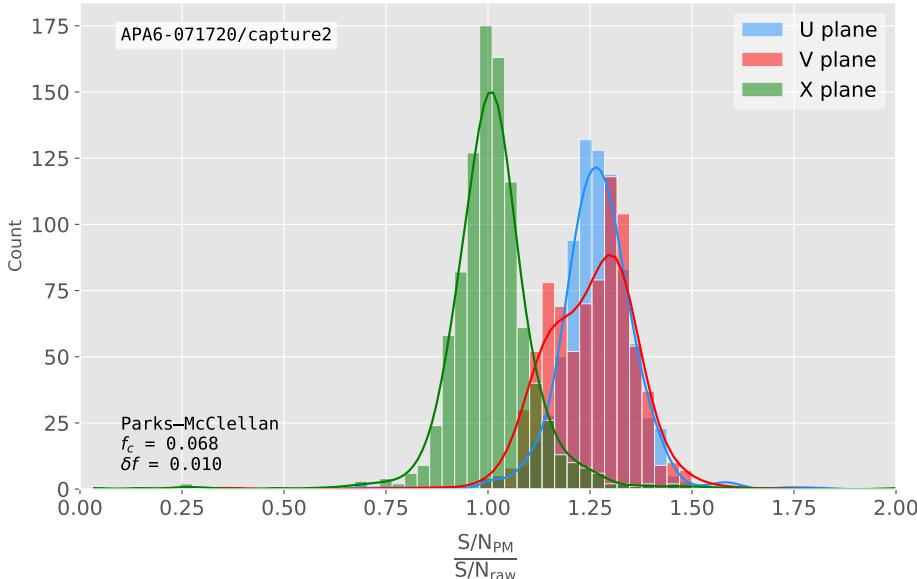


Figure 4.6: Distribution of the relative change of the S/N on the different wire planes from the ProtoDUNE-SP raw data capture *felix-2020-07-17-21:31:44* after the optimal Chebyshev filter was applied. The filter was computed with the Parks-McClellan algorithm using a cutoff of $f_c = 0.068 \text{ ticks}^{-1}$ and a transition width $\delta f = 0.010 \text{ ticks}^{-1}$.

filter is applied. In any case, this is not a big issue as the S/N for collection channels is usually much higher than the one for induction channels.

The results I obtained optimising the low pass filter with the Parks-McClellan method are promising. Nonetheless, the improvement found is rather marginal so I wondered if there could be an alternative approach to the filtering problem which yields better outputs. At this point, I found a possible alternative in matched filters. By construction, this kind of filters offer the best improvement on the S/N.

4.4 Matched filters

In the context of signal processing, a matched filter is the optimal linear filter for maximising the signal-to-noise ratio (S/N) in the presence of additive noise, obtained by convolving a conjugated time-reversed known template with an unknown signal to detect the presence of the template in the signal [106].

Given a known signal sequence $s(t)$ and another (a priori unknown) noise sequence

4.4. MATCHED FILTERS

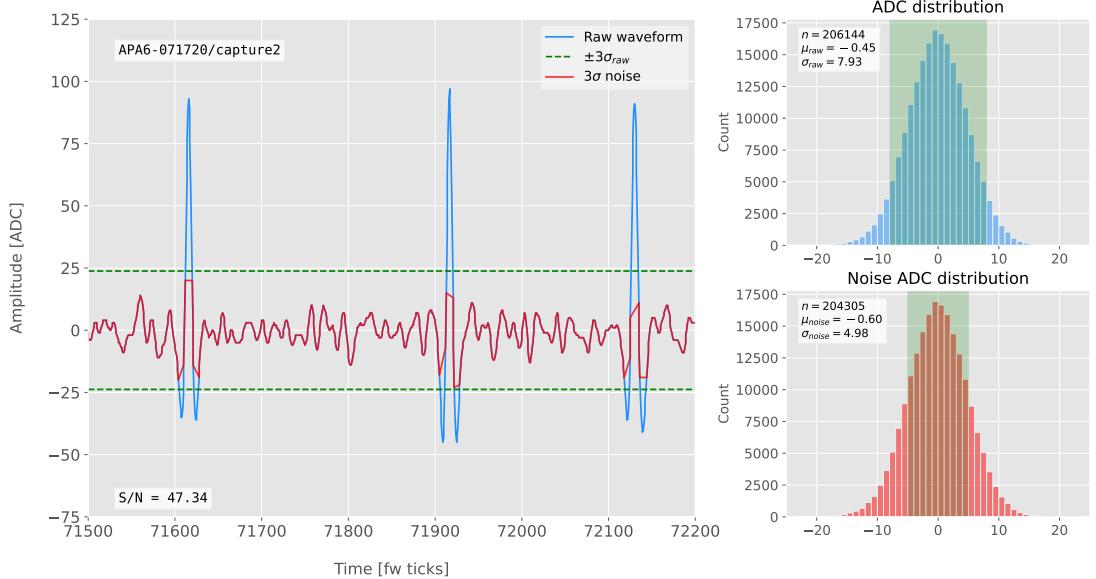


Figure 4.7: Left panel: Zoomed match filtered waveform corresponding to channel 7840 from the ProtoDUNE-SP raw data capture felix-2020-07-17-21:31:44 (blue line). The filter used was directly extracted from the data, being the 32 values around the first peak in the original waveform. The green dashed lines mark the region $\pm 3\sigma_{\text{raw}}$. The resulting noise waveform is also shown (red line). Top right panel: ADC distribution for channel 7840 after match filtering, where the green shaded region represents $\pm \sigma_{\text{raw}}$. Bottom right panel: noise ADC distribution for channel 7840 after match filtering, where the green shaded region represents $\pm \sigma_{\text{noise}}$

1591 $n(t)$, the input signal can be written as:

$$x(t) = s(t) + n(t). \quad (4.4)$$

1592 Now, considering a linear time-invariant filter, whose impulse-response function I
1593 will refer to as $h(t)$, one can write the output signal as:

$$\begin{aligned} y(t) &= x(t) * h(t) \\ &= (s(t) + n(t)) * h(t) \\ &= y_s(t) + y_n(t), \end{aligned} \quad (4.5)$$

1594 where $y_s(t)$ and $y_n(t)$ are simply the outputs of the filter due to the signal and the noise
1595 components respectively.

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1596 The goal of the matched filter is to detect the presence of the signal $s(t)$ in the input
 1597 sample $x(t)$ at a certain time t_0 , which effectively means we need to maximise the S/N.
 1598 This way, what one wants is to have a filter which gives a much bigger output when the
 1599 known signal is present than when it is not. Putting it in other words, the instantaneous
 1600 power of the signal output $y_s(t)$ should be much larger than the average power of the
 1601 noise output $y_n(t)$ at some time t_0 .

1602 For the case of the filtered signal, one can easily re-write it as an inverse Fourier
 1603 transform:

$$y_s(t) = \frac{1}{2\pi} \int_{-\infty}^{\infty} d\omega H(\omega)S(\omega)e^{i\omega t}, \quad (4.6)$$

1604 where $H(\omega)$ and $S(\omega)$ are the Fourier transforms of the impulse-response function (i.e.
 1605 the transfer function of the filter) and of the input signal, respectively.

1606 Now focusing on the noise, we can use the Wiener-Khinchin theorem [107] to write
 1607 the mean power of the noise after filtering as:

$$E|y_n(t)|^2 = \frac{1}{2\pi} \int_{-\infty}^{\infty} d\omega |H(\omega)|^2 S_n(\omega), \quad (4.7)$$

1608 where $S_n(\omega)$ is the power spectral density of the noise.

1609 Having these, one can write the instantaneous S/N at time t_0 as:

$$\begin{aligned} \left(\frac{S}{N} \right)_{t_0} &= \frac{|y_s|^2}{E|y_n(t)|^2} \\ &= \frac{1}{2\pi} \frac{\left| \int_{-\infty}^{\infty} d\omega H(\omega)S(\omega)e^{i\omega t_0} \right|^2}{\int_{-\infty}^{\infty} d\omega |H(\omega)|^2 S_n(\omega)}. \end{aligned} \quad (4.8)$$

1610 Once we have this expression, we need to find the upper limit of it to determine what
 1611 would be the optimal choice for the transfer function. One can use the Cauchy-Schwarz
 1612 inequality, which in the present case takes the form:

$$\left| \int_{-\infty}^{\infty} dx f(x)g(x) \right|^2 \leq \int_{-\infty}^{\infty} dx |f(x)|^2 + \int_{-\infty}^{\infty} dx |g(x)|^2, \quad (4.9)$$

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1613 for any two analytical functions $f(x)$ and $g(x)$. One can prove that making the choice:

$$\begin{aligned} f(x) &= H(\omega) \sqrt{S_n(\omega)} e^{i\omega t_0}, \\ g(x) &= \frac{S(\omega)}{\sqrt{S_n(\omega)}}, \end{aligned} \quad (4.10)$$

1614 leads to the following upper bound for the S/N:

$$\left(\frac{S}{N} \right)_{t_0} \leq \frac{1}{2\pi} \int_{-\infty}^{\infty} d\omega \frac{|S(\omega)|^2}{S_n(\omega)}. \quad (4.11)$$

1615 From Eqs. (4.8), (4.9) and (4.10) one can also derive the form of the transfer function

1616 such that the upper bound is exactly reached [108]:

$$H(\omega) \propto \frac{S^*(\omega) e^{-i\omega t_0}}{S_n(\omega)}. \quad (4.12)$$

1617 From this last expression we can clearly see the way the matched filter acts. As the
1618 transfer function is proportional to the Fourier transform of the signal it will try to only
1619 pick the frequencies present in the signal [109].

1620 The matched filter transfer function can be greatly simplified if the input noise is
1621 Gaussian. In that case, the power spectral density of the noise is a constant, so it can be
1622 re-absorbed in the overall normalisation of the transfer function. Moreover, considering
1623 that the input signal is a real function, one can simply set $S^*(\omega) = S(-\omega)$, which gives:

$$H(\omega) \propto S(-\omega) e^{-i\omega t_0}. \quad (4.13)$$

1624 For a discrete signal, one can think of the input and impulse-response sequences as
1625 vectors of \mathbb{R}^N . Then, the matched filter tries to maximise the inner product of the signal
1626 and the filter while minimising the output due to the noise by choosing a filter vector
1627 orthogonal to the later. In the case of additive noise, that leads to the impulse-response
1628 vector:

$$h = \frac{1}{\sqrt{s^\dagger R_n^{-1} s}} R_n^{-1} s, \quad (4.14)$$

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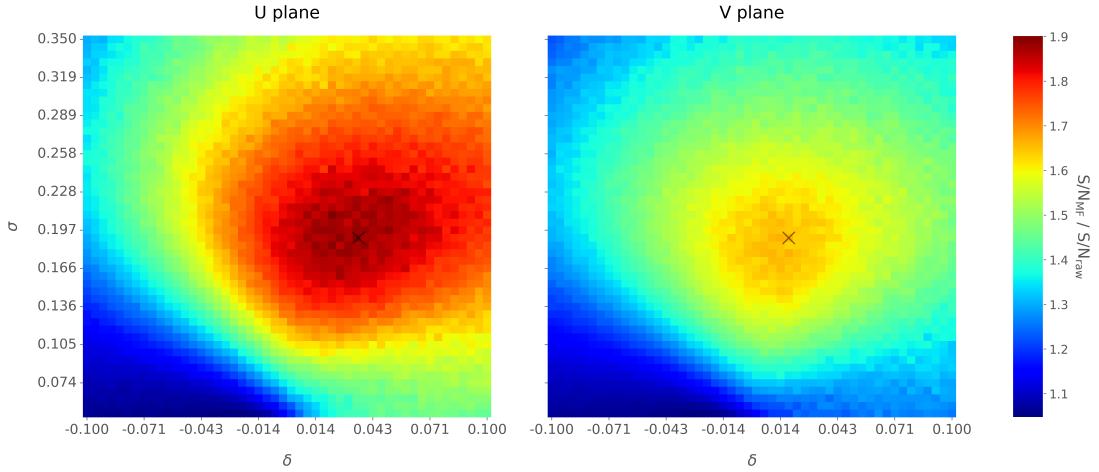


Figure 4.8: Relative improvement in the S/N for the raw data capture `felix-2020-07-17-21:31:44`, using the matched filter following the parametrisation in Eq. (4.17). The black crosses in both panels denote the location of the maximum ratio value.

where s is a reversed signal template sequence of length N equal to the order of the filter and R_n is the covariance matrix associated with the noise sequence n . For the Gaussian noise case, the covariance matrix is simply the unit matrix, so the above expression simplifies again to:

$$h = \frac{s}{|s|}. \quad (4.15)$$

For this first stage of the study, I use a definition of the S/N per channel given by:

$$\text{S/N} = \frac{\max [ADC] - \mu_{noise}}{\sigma_{noise}}, \quad (4.16)$$

where the subscript *noise* refers to a subset of the data obtained by only taking into account waveform values within a $\pm 3\sigma$ range around the mean of the data and $\max [ADC]$ is the maximum of the original waveform. This definition is further discussed in App. 4.2, where I also show examples of its application to raw data and to a waveform filtered with the current low-pass FIR filter.

To test whether this choice of filter is appropriate one needs to choose a signal template. As an example of how a matched filter would affect our signal, I simply took the filter coefficients to be the 32 ADC values around a signal peak present in the data.

4.4. MATCHED FILTERS

1642 In Fig. 4.7 (left panel) I plotted a zoomed region for channel 7840 in the raw data capture
1643 `felix-2020-07-17-21:31:44`, after applying the matched filter described before (blue
1644 line). When compared to the raw and FIR filtered case (see App. 4.2), after applying
1645 the match filter the standard deviation of the noise waveform (red line) decreases and at
1646 the same time the signal peaks are enhanced. This leads to an improvement of the S/N
1647 by a factor of 1.92 when compared to the raw waveform.

1648 In order to obtain the matched filter that is more suitable for our data, I explored
1649 different configurations of signal templates. In order to perform this exploration, I
1650 parametrised the signal using the bipolar function:

$$f(x) = -A(x + \delta) e^{-x^2/\sigma^2}, \quad (4.17)$$

1651 where the parameter δ controls the asymmetry between the positive and negative peaks
1652 and σ controls their width. The amplitude parameter A is set such that it keeps the
1653 height of the biggest peak to be less than 200 ADC in absolute value.

1654 As this parametrisation is only adequate for bipolar signals I will focus exclusively
1655 on the induction channels. Also, the optimal configurations I found for the U and V
1656 plane will be kept separate, i.e. I will have two sets of coefficients that will be applied to
1657 either the U and V planes of wires. I do so as I found this was the choice giving the
1658 best performance. Even so, as I will discuss, the differences are not very pronounced. In
1659 case it is not technically possible to separate channels in the firmware according to the
1660 wire plane they come from and use different sets of filter coefficients for them, we can
1661 just find a common unique set of coefficients. In such case, I do not expect our results
1662 to change dramatically.

1663 In Fig. 4.8 I present the results of our parameter scan, for channels in the induction
1664 planes U (left panel) and V (right panel). For each configuration of σ and δ the resulting
1665 matched filter was applied to all channels in the corresponding plane within the data
1666 capture `felix-2020-07-17-21:31:44`, the S/N improvement was computed with respect
1667 to the raw waveforms and then the S/N mean value was kept as a score for such filter.

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1668 One can see that the improvement obtained for the U plane is in general higher than the
1669 one for the V plane. In any case, I got substantially higher ratios than the ones obtained
1670 for the low-pass FIR filters. For the optimal configurations I attained improvements up
1671 to a factor of 1.85 for the U plane and 1.65 for the V plane.

1672 The sets of optimal matched filter coefficients were obtained for the parameters
1673 $\delta = 0.035$, $\sigma = 0.191$ for the U plane and $\delta = 0.018$, $\sigma = 0.191$ for the V plane. I
1674 show these two sets of coefficients in Fig. 4.9 (left panel). Also in Fig. 4.9 (right
1675 panel) I plot the distribution of the S/N improvement after the optimal match filters
1676 for the U and V were applied to the corresponding channels in the raw data capture
1677 `felix-2020-07-17-21:31:44`. As mentioned before, the mean improvement achieved
1678 for the U plane channels is slightly bigger than the one for the V channels. Note, however,
1679 that the spread of the distribution for the V plane is also smaller than the one for the U
1680 plane.

1681 I also performed a similar scan for the case of a low-pass FIR filter using the Parks-
1682 McClellan algorithm. In that case, the parameters to check were the cutoff frequency
1683 and the transition width of the filter. A summary of the results is given in App. 4.3.

1684 Overall, one can see that the improvements on the S/N are much more significant in
1685 the case of the matched filter than it is for the low-pass FIR filters. The analysis of this
1686 and other raw data captures from ProtoDUNE-SP suggest that matched filters increase
1687 the S/N of induction channels by a factor of 1.5 more than the optimal low-pass FIR
1688 filters.

1689 Although these results are by themselves great points in favour of the matched
1690 filter, more studies are needed to completely assess the robustness of this approach. I
1691 proceeded then to test the matched filter with simulated data samples.

1692 4.5 Using simulated samples

1693 In order to further test the matched filter, the next step was to generate and process
1694 data samples using *LArSoft* [110]. In this way, one can control the particle content of

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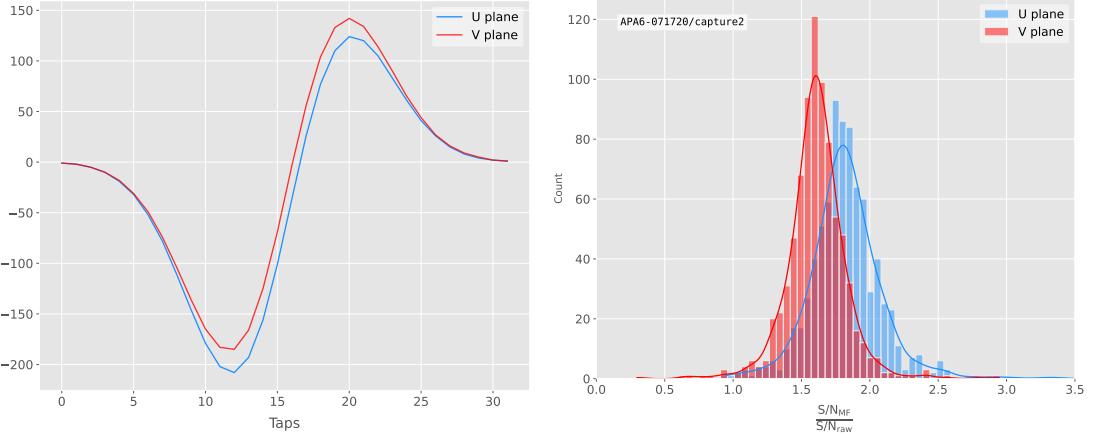


Figure 4.9: Left panel: Optimal matched filter coefficients for the U (blue line) and V (red line) planes. The filters were computed with our parametrisation in Eq. (4.17) for the parameter values $\delta = 0.035$, $\sigma = 0.191$ and $\delta = 0.018$, $\sigma = 0.191$ respectively. Right panel: Distribution of the relative change of the S/N on the two induction wire planes from the ProtoDUNE-SP raw data capture *felix-2020-07-17-21:31:44* after their respective optimal matched filters were applied.

1695 the samples, the orientation of the tracks and their energy, and therefore see how the
1696 matched filter behaves in various situations.

1697 To begin with, I prepared different monoenergetic and isotropic samples containing
1698 a single particle per event. Each sample contains a different particle species, namely
1699 electrons, muons, protons and neutral pions all with a kinetic energy of $E_k = 100$ MeV.
1700 I chose these because of the fairly different topologies they generate in the liquid argon,
1701 ranging from shower-like to track-like. The procedure I followed to generate the samples
1702 and process them is discussed in detail in App. ??.

1703 These were generated with the single particle gun and the Geant4 stage of the
1704 *LArSoft* simulation [110] was performed with the standard configuration for the DUNE
1705 FD 10kt module.

1706 For simplicity, I restricted the particles to start drifting in a single TPC volume
1707 (in this case TPC 0), so I can focus exclusively on the signals coming from one APA.
1708 The chosen kinetic energy for all the particles in my first trial is $E_k = 100$ MeV, so a
1709 necessary check is to see if all our tracks will be typically contained in one TPC volume.
1710 Fig. 4.10 (left panel) shows the distributions of the track lengths in the liquid argon

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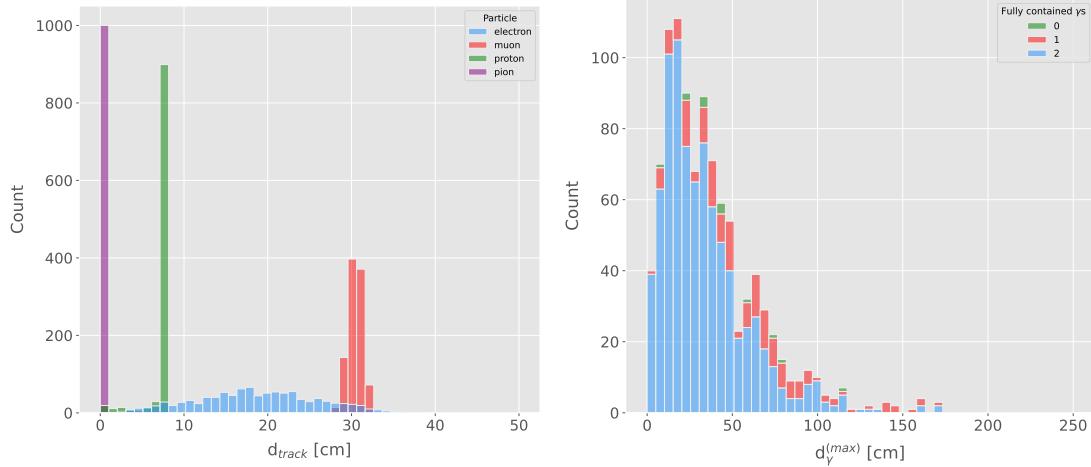


Figure 4.10: Left panel: distributions of the particles track length in the liquid argon for the generated $E_k = 100$ MeV monoenergetic samples, electrons (blue), muons (red), protons (green) and neutral pions (purple). Right panel: distribution of the length of the longest photon in the neutral pion sample after the decay process $\pi^0 \rightarrow \gamma\gamma$.

of all generated particles with $E_k = 100$ MeV. One can see that, in the case of the track-like particles (i.e. muons and protons), their length distributions are quite sharp and centered at relatively low distances (30 and 8 cm, respectively). For electrons, the distribution is quite broad but it does not extend past ~ 30 cm. The case of neutral pions can be misleading, as they decay promptly the track length associated with the true Monte Carlo particle is always < 1 cm. In Fig. 4.10 (right panel) I show the effective length distribution of the longest photon after the pion decays as $\pi^0 \rightarrow \gamma\gamma$, highlighting the number of fully contained photons in the TPC volume per event (either zero, one or both). One can see that the vast majority of events has both photons contained and that just a negligible number of them has none of them contained in the TPC volume. In any case, for the sake of caution, I will only keep the pion events with both photons contained.

Once I have prepared a sample at the Geant4 level, I need to process it through the detector simulation. In order to make adequate estimations of the noise levels and run the filtering and hit finder as I did with the ProtoDUNE data, one needs to turn off the default zero-suppression of the waveforms produced by the simulation. At this first stage I am only concerned with the waveforms with the noise added, so I keep the noise

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addition option as true in the configuration. However, for studies related to the hit finder performance one will also need to store the noiseless waveforms in order to retrieve the truth information of the hits. I will discuss this approach next.

After the detector simulation stage, one needs to extract the no zero-suppressed noisy waveforms, along with their offline channel numbers, and store them in a certain format to be analysed later. To reduce the amount of data that will go for processing, I used the information from the Geant4 step of the simulation to select only the active channels, i.e. the channels where some ionisation electrons arrive. Moreover, as said previously, I only extract the waveforms from APA 0 and exclusively the ones coming from induction channels. The resulting ROOT file contains a tree with two branches, one containing the waveforms for each event and channel and the other with the corresponding offline channel numbers.

Finally, to extract the truth values for the orientation of the tracks and the energies of the particles I used a modified analysis module. This gives a ROOT file with a single tree, containing several branches with different information such as the components of the initial momentum of the particles, initial and final xyz location, track length, etc.

For the analysis of the resulting waveforms and truth values I used a custom set of Python libraries (available at [???]). Among other functionalities, these enable the user to read the ROOT files, export the raw data as pandas objects, apply the filters and compute the S/N of both the raw and filtered signals. So far, the default configuration for the filtering uses the set of optimal matched filter coefficients that I found using the ProtoDUNE data samples.

Additionally, for the analysis of the samples it was necessary to use two different reference frames, to study separately the signals coming from the U and V induction wire planes. As I am focussing on a single APA, the U and V wires have a different orientation in the yz plane. In the case of U wires, these are tilted 35.7° clockwise from the vertical (y direction), whereas the V wires are at the same angle but in the counter clockwise direction. Because of this, the best option is to deal with two new coordinate systems rotated by $\pm 35.7^\circ$ along the x axis, so the new y' and y'' directions are aligned with the

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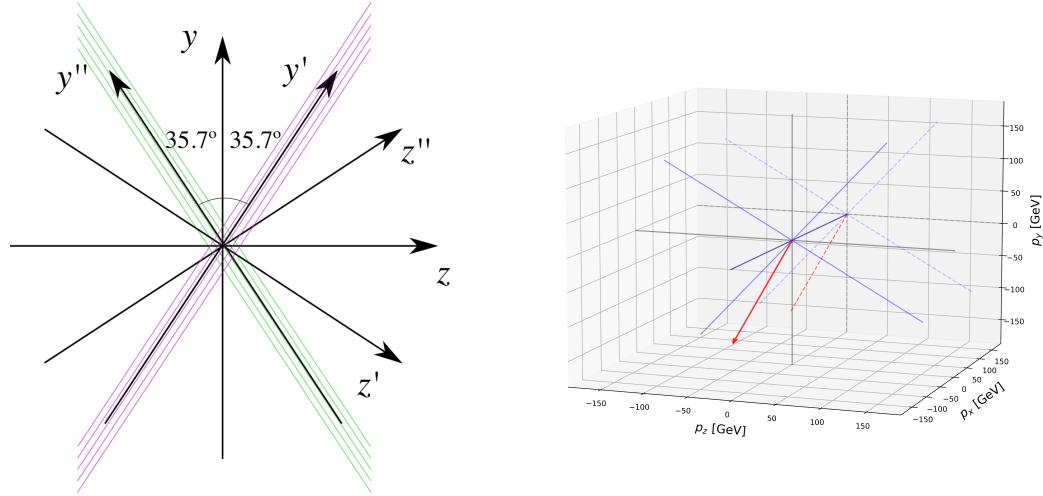


Figure 4.11: Left panel: schematic representation of the two new rotated reference frames used in this analysis (denoted as prime and double prime), viewed from the yz plane. The magenta stack of lines represent the wires in the U plane, whereas the green lines correspond to the wires in the V plane. Right panel: 3D representation of the momentum of one of the generated monoenergetic muons (red arrow) in the original reference frame (black lines), along with the new reference frame used for the U plane waveforms (blue lines). In the yz plane I added the projection of these three.

1757 U and V induction wires. Fig. 4.11 (left panel) shows a schematic representation of
 1758 the original reference frame together with the two rotated ones (denoted by primed and
 1759 double primed). This way, one can easily understand how parallel was a track to the
 1760 wires in the two induction planes. Fig. 4.11 (right panel) shows a 3D representation of
 1761 the momentum of a track (red arrow) in the original reference frame (black lines), along
 1762 with the new reference frame for U wires (blue lines). I added the projection in the yz
 1763 plane of this three, to show the usefulness of the new reference frame to tell whether a
 1764 track is parallel or normal to the wires in the induction plane.

1765 Fig. 4.12 shows the distribution of the average S/N improvement per event when one
 1766 applies the optimal matched filters. I produced separate distributions for the channels
 1767 in the U (red) and V (blue) induction wire planes. Notice that the S/N distributions
 1768 for the track-like particles, i.e. muons (top left panel) and protons (bottom left panel),
 1769 have significantly larger mean values than the distributions of the shower like particles,
 1770 i.e. electrons (top right panel) and neutral pions (bottom right panel). An important

4.5. USING SIMULATED SAMPLES

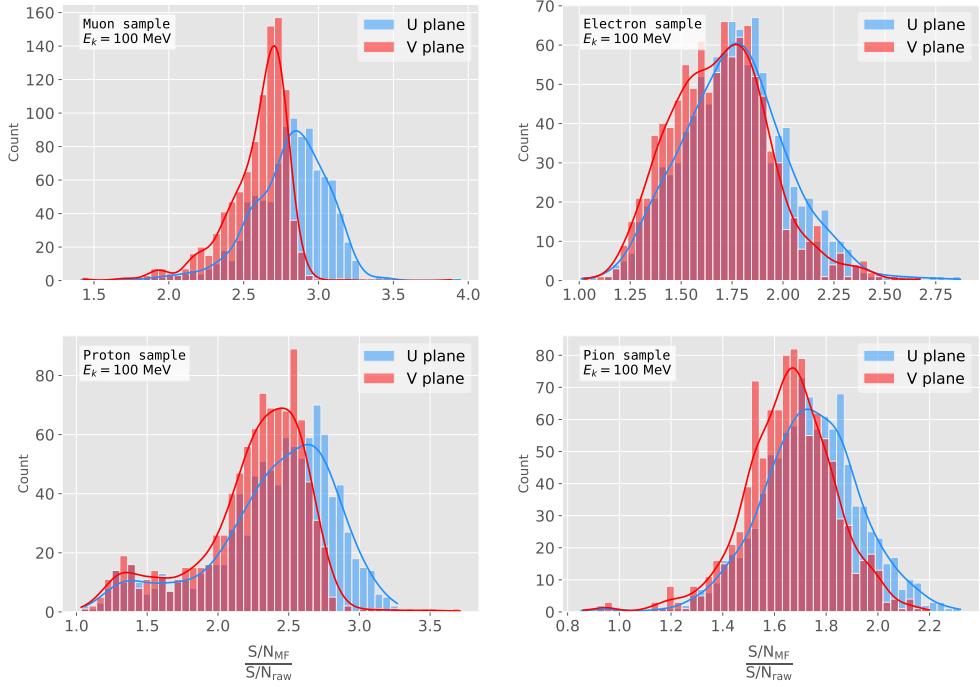


Figure 4.12: Distributions of the mean S/N improvement per event for the corresponding sample after applying the matched filters. Here I separated the change in the U plane (blue) and the V plane (red) channels. From top left to the right: muon, electron, proton and neutral pion. All the events have a fixed kinetic energy of $E_k = 100$ MeV.

difference between these results and the ones seen before for ProtoDUNE data is that, overall, the improvements that I get for simulated data are bigger. This could be due either to the default noise model used in the *LArSoft* simulation or to the simulated hits having higher energy than the ones in the recorded data. Nonetheless, the concluding message is that the previously optimised matched filters give an overall significant improvement of the S/N for the different samples.

About the convention I followed for the plots and results, in the case of the raw and filtered S/N of each event in the sample I simply took the average of the quantities over all the active channels in the event. That is, if a certain event has N_{chan} active channels these two quantities are computed as:

$$(S/N_{fir})_{event} = \frac{\sum_{i=0}^{N_{chan}} (S/N_{fir})_i}{N_{chan}}, \quad (4.18)$$

$$(S/N_{raw})_{event} = \frac{\sum_{i=0}^{N_{chan}} (S/N_{raw})_i}{N_{chan}}.$$

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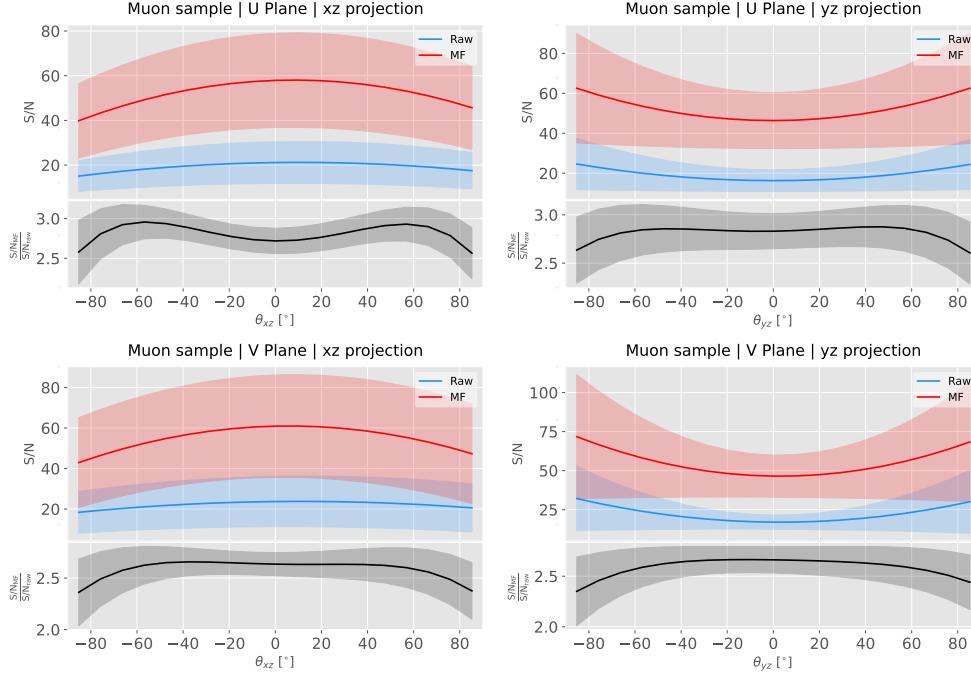


Figure 4.13: Angular dependence of the mean S/N and the S/N improvement, for the different monoenergetic samples considered (from top to bottom: electrons, muons, protons and neutral pions). The two columns on the left represent the values for the U plane waveforms. The top subplots show the mean S/N for raw (green) and filtered (red) waveforms whereas the bottom subplots depict the averaged S/N improvement (black).

1781 However, for the ratio of the raw and filtered S/N (what I called the S/N improvement)
 1782 per event I am not just taking the ratio of the previous two quantities but computing
 1783 the average of the individual ratios per channel in the event:

$$\left(\frac{S/N_{fir}}{S/N_{raw}} \right)_{event} = \frac{\sum_{i=0}^{N_{chan}} \left(\frac{S/N_{fir}}{S/N_{raw}} \right)_i}{N_{chan}}, \quad (4.19)$$

1784 and so:

$$\left(\frac{S/N_{fir}}{S/N_{raw}} \right)_{event} \neq \frac{(S/N_{fir})_{event}}{(S/N_{raw})_{event}}. \quad (4.20)$$

1785 4.5.1 Angular dependence

1786 Having these monoenergetic samples, one can also study the angular dependence of the
 1787 performance of the matched filter. This is an important point, as it is a well established

4.5. USING SIMULATED SAMPLES

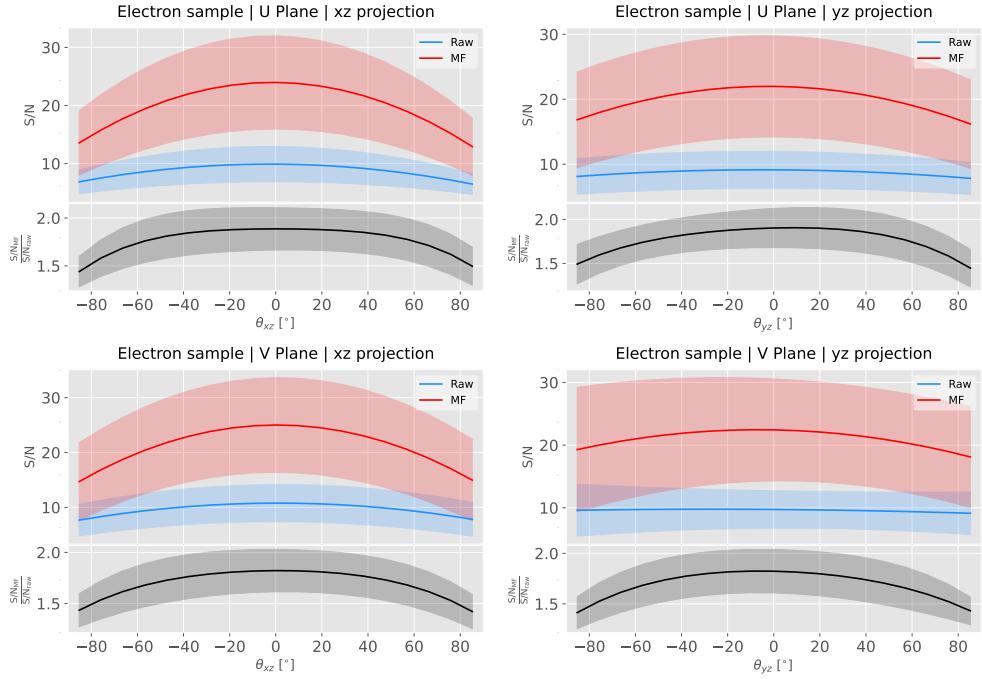


Figure 4.14: Angular dependence of the mean S/N and the S/N improvement, for the different monoenergetic samples considered (from top to bottom: electrons, muons, protons and neutral pions). The two columns on the left represent the values for the U plane waveforms. The top subplots show the mean S/N for raw (green) and filtered (red) waveforms whereas the bottom subplots depict the averaged S/N improvement (black).

fact that for certain configurations (an extreme case configuration being signals normal to the wire plane and perpendicular to the induction wires at the same time) the S/N is much lower than average as the corresponding waveforms are severely distorted. In this sense, I am interested to see how the matched filter behaves for these cases and how the S/N improvement on those compare to the average.

Fig. 4.13 shows the angular dependence of the S/N for the monoenergetic $E_k = 100$ MeV isotropic muons, for the different induction wire planes and projections. The angles for each event are given by the components of the initial value of the momentum of the particles, taking the angles of the projections on the xz and yz planes with respect to the z axis (more accurately, one needs to compute these angles twice for each event, a pair for the $xy'z'$ coordinate system and the other for the $xy''z''$). The top row shows the dependence on the angles corresponding to the U plane, i.e. $\theta_{xz'}$ and $\theta_{y'z'}$, whereas the bottom row shows the angular dependence viewed from the V plane, $\theta_{xz''}$ and $\theta_{y''z''}$. In

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1801 each plot, the top subplot represents the mean values of the S/N for the raw (blue) and
1802 matched filtered (red) signals, and the bottom subplot the averaged S/N improvement
1803 (black). The solid lines represent the mean value obtained for the corresponding angular
1804 value, whereas the semitransparent bands represent one standard deviation around the
1805 mean at each point.

1806 As expected, the S/N is in general higher when tracks are parallel to the APA (i.e.
1807 $\theta_{xz} \sim 0$) and lower when it is normal to the plane ($\theta_{xz} \sim \pm 90^\circ$). In the same way, tracks
1808 parallel to the wires ($\theta_{yz} \sim \pm 90^\circ$) tend to have higher S/N than those perpendicular to
1809 these ($\theta_{yz} \sim \pm 0$).

1810 Fig. 4.14 shows the corresponding angular dependence information for the $E_k =$
1811 100 MeV electrons sample. Notice that, in this case, the S/N behaviour discussed above
1812 does not hold. A possible explanation can be that, because most hits in these events
1813 are produced by the secondary particles generated in the EM shower, the signal peaks
1814 whose S/N ratios were computed do not correspond to the directional information of
1815 the primary electron.

1816 4.5.2 Distortion and peak asymmetry

1817 As a little case of study, I selected two of the simulated $E_k = 100$ MeV monoenergetic
1818 muon events. With respect to the U induction plane, one is parallel to the APA (low
1819 $\theta_{xz'}$) and to the wires (high $\theta_{y'z'}$) and the other is normal to the APA plane (high $\theta_{xz'}$)
1820 and perpendicular to the wires (low $\theta_{y'z'}$). As expected from the results on the angular
1821 dependence discussed above, the former has a higher S/N (before and after the filtering)
1822 when compared to the latter. An interesting thing to notice about these two samples
1823 is that, even though one has a much bigger S/N than the other, it is the one with the
1824 smallest S/N the one that got the biggest averaged S/N improvement. In Table 4.1
1825 I included all the relevant parameters of these two $E_k = 100$ MeV muon events I am
1826 considering, namely, the angles with respect to the $xy'z'$ reference frame, the values of
1827 the S/N, the S/N improvement and also the so-called peak asymmetry Δ_{peak} that I will
1828 discuss next.

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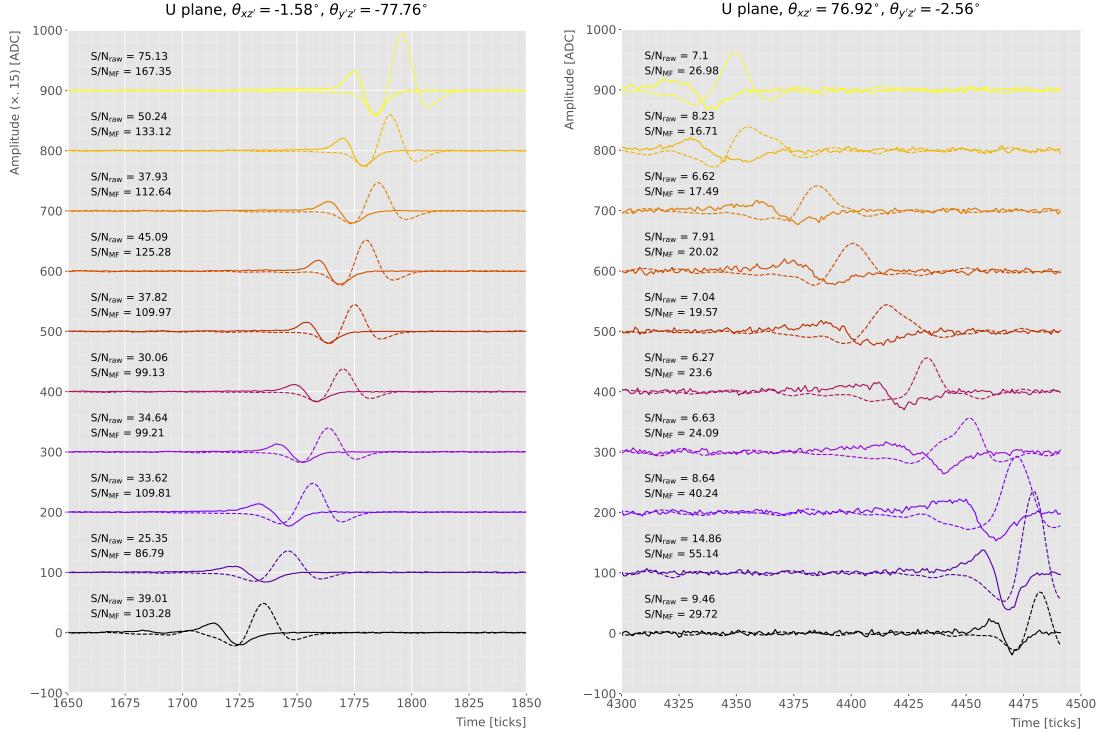


Figure 4.15: Selected consecutive waveforms corresponding to two monoenergetic $E_k = 100$ MeV muon events, one is parallel to the APA and to the wires in the U plane (left panel) and the other is normal to the APA plane and perpendicular to the U plane wires (right panel). The solid lines represent the raw waveforms whereas the dashed lines correspond to the waveforms after the matched filter was applied. The waveforms on the left panel have been scaled by a factor of 0.15 to have similar amplitude to the ones on the right panel.

Table 4.1: Characteristic parameters of the two monoenergetic muon events selected, relative to the U plane: projected angles in the xz' and yz' planes, S/N values for the raw and filtered waveforms, mean improvement of the S/N and peak asymmetry.

	$\theta_{xz'} (\circ)$	$\theta_{yz'} (\circ)$	S/N_{raw}	S/N_{MF}	$\frac{S/N_{\text{MF}}}{S/N_{\text{raw}}}$	$\Delta_{\text{peak}} (\text{ADC})$
High ("parallel")	-1.58	-77.76	41.65	112.44	2.83	-35.73
Low ("normal")	76.92	-2.56	8.07	25.46	3.12	-10.38

1829 One can try to understand better what is going on with these two events by looking
 1830 at the raw and filtered data from some of their active channels. Fig. 4.15 shows a
 1831 selection of consecutive raw and filtered U plane waveforms from the event with high S/N
 1832 (left panel) and the one with low S/N (right panel). Notice that to show both collections
 1833 of waveforms at a similar scale I had to apply a factor of 0.15 to the waveforms with
 1834 high S/N. Additionally, next to each waveform I included the values of the raw and

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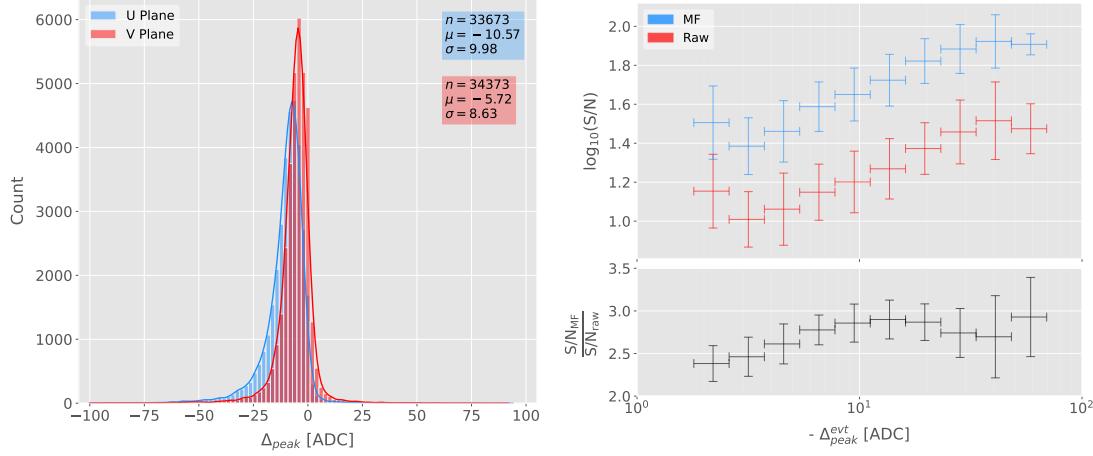


Figure 4.16: Left panel: peak asymmetry distribution for the case of the monoenergetic $E_k = 100$ MeV muon sample. Each value corresponds to a single bipolar signal peak from a channel in any event. The blue distribution represents the peaks on U plane channels, whereas the red corresponds to signal peaks in V wires. Right panel: relation between the mean peak asymmetry per event with the S/N for U channel waveforms from the $E_k = 100$ MeV muon sample. The top subplot shows the decimal logarithm of the mean S/N for the raw (red) and the matched filtered (blue) waveforms. The bottom subplot contains the mean S/N improvement ratio after the matched filter was applied.

1835 matched filtered S/N for the corresponding channel. The first thing to notice in this plot
 1836 is that the amplitude of the signal peaks from the normal track have a much smaller
 1837 amplitude, and also appear quite distorted when compared to the others. On the other
 1838 hand, although the matched filtered S/N is still smaller, the relative improvement is
 1839 bigger than in the parallel case.

1840 A way I found to quantify the difference between the shapes within these two events
 1841 is their different peak asymmetry. One can define the peak asymmetry as the (signed)
 1842 difference between the positive and the negative peaks of the bipolar shape, i.e.:

$$\Delta_{peak} \equiv h_+ - h_-, \quad (4.21)$$

1843 where both heights h_+ and h_- are positive defined. Fig. 4.16 (left panel) shows the
 1844 distribution of this peak asymmetry for all the waveforms corresponding to channels
 1845 in the U (blue) and V (red) planes for the monoenergetic muon sample. One can
 1846 see that these distributions are clearly shifted to negative values (with mean values

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1847 $\mu_{\Delta}^U = -10.57$ ADC and $\mu_{\Delta}^V = -5.72$ ADC respectively). It is interesting to notice
1848 that the peak asymmetry value of the sample with high S/N sits at the left tail of the
1849 distribution whereas the corresponding value of the sample with low S/N lies around
1850 the mean.

1851 Now, one can try to correlate the peak asymmetry with the S/N and the S/N change
1852 per event. Fig. 4.16 (right panel) shows the result of comparing (minus) the mean
1853 peak asymmetry per event to the averaged raw (red) and matched filtered (blue) S/N
1854 per event (top subplot). The horizontal lines sit at the mean value obtained in the fit
1855 and represent the width of the $-\Delta_{peak}$ bins used, while the vertical lines indicate one
1856 standard deviation around that mean value. Notice that, when taking decimal logarithm
1857 on both, there is an approximate linear relation between these quantities, except for
1858 peak asymmetry values bigger than -5 ADC where the S/N remains constant.

1859 Also, in the bottom subplot of Fig. 4.16 (right panel) I show the relation between
1860 the peak asymmetry and the mean S/N improvement. In this case, one see that there is
1861 a maximum at $\Delta_{peak} \sim -10$ ADC. As mentioned previously, this is also the value of the
1862 mean of the peak asymmetry distribution. In fact, it is expected that our filter favours
1863 the signal peaks with the most common values of the peak asymmetry, as this was one
1864 of the features I target in our filter coefficient optimisation through the parameter δ .

1865 These results suggest that events with poorer values of the mean S/N, usually
1866 associated to non-favourable track orientations, tend to have smaller values of the mean
1867 peak asymmetry (in absolute value). Nonetheless, because our matched filters have
1868 been optimised to account for these asymmetries, the improvement on the S/N for these
1869 events is sizeable if not better than the one for events which already had a high S/N.

1870 4.5.3 Hit sensitivity

1871 One of the advantages of the matched filter, directly related to increasing the S/N, is
1872 the capability of picking hits that before fell below the threshold. For instance, Fig. 4.17
1873 shows the raw ADC data from an example event (electron, $E_k = 100$ MeV) with the
1874 produced true hits superimposed (black boxes), together with the hits produced by the

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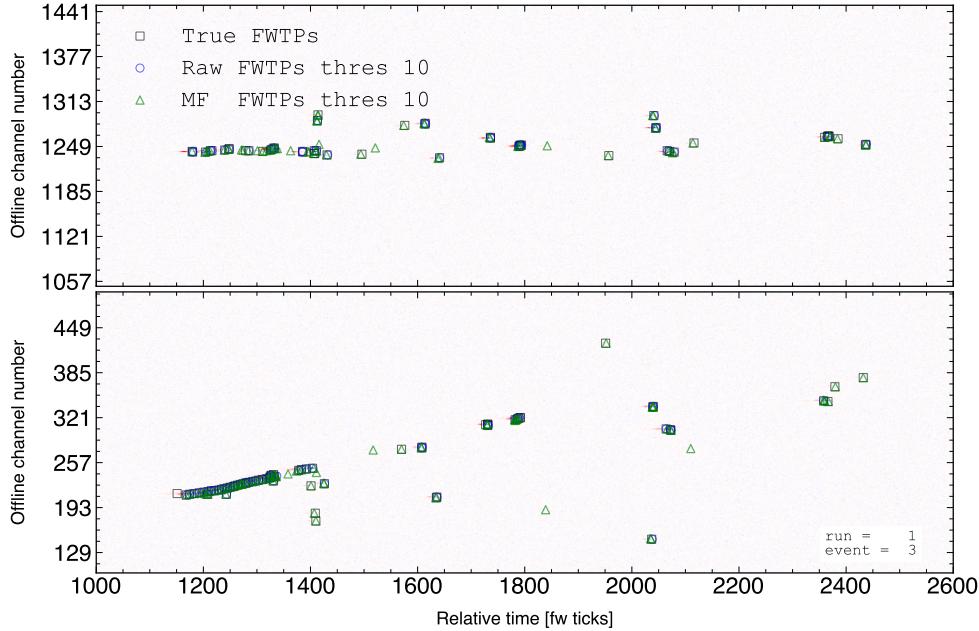


Figure 4.17: Raw data display in the plane time (in firmware ticks) vs. offline channel number for an $E_k = 100$ MeV electron event. The produced true hits are superimposed (black boxes) as well as the hits coming from the standard hit finder chain (blue circles) and the hit finder using the matched filter (green triangles).

standard hit finder chain (blue circles), i.e. using the current FIR filter, and the hits obtained using the matched filters (green triangles). Both the standard and the matched filter hit finders were run with a threshold of 10 ADC. Notice that the standard hits match well the true ones at the initial part of the event (where we have a track-like object), but they miss most of the hits produced by the EM shower at later times. On the other hand, the hits produced with the matched filter have a better agreement with the true hits even for the more diffuse shower activity.

Notwithstanding that now I get more hits with this combination of matched filter and low threshold as a results of the enhancement of the signal peaks relative to the noise level, it is also true that I pick some spurious hits not related to any real activity if one lowers the thresholds too much. Therefore, some optimisation of the threshold is needed. Basically one will need to make a trade-off between precision and sensitivity.

Having this in mind, I tried to compare the produced hits one gets from the standard hit finder and the ones resulting from applying the matched filter with the true hits.

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1889 By running the hit finders on our samples with different values of the threshold one
1890 can understand, for instance, how low one can set the threshold without getting mostly
1891 spurious hits and then evaluate the gains obtained from this.

1892 Because now I am also interested in seeing how the hit sensitivity changes with the
1893 energy, I prepared new isotropic samples with the same types of particles as before
1894 (muons, electrons, protons and neutral pions) but with a flat kinetic energy distribution
1895 ranging from 5 to 100 MeV.

1896 In order to estimate the hit sensitivity, given a certain sample, one needs to recover
1897 the set of true hits to be able to compare these with the ones produced. To do so,
1898 a modification in the procedure I was using to extract the raw waveforms is needed.
1899 For this kind of study I run the detector simulation in two steps, first I produce the
1900 waveforms without noise and extract them in the same format I used for the raw data,
1901 then the noise is added and the noisy waveforms are then written to a file as well.

1902 To have a better comparison between the true hits and the ones produced from
1903 the raw waveforms after applying the two filters, I applied also the FIR filter and the
1904 matched filters to the noiseless waveforms and then I run the hit finder with a minimal
1905 threshold (in this case I used 1 ADC) on these noiseless filtered waveforms. In this way
1906 I generated two sets of true hits, I will refer to them as standard true hits (with the
1907 current/default FIR filter) and matched filter true hits respectively. This allows a more
1908 precise matching between the different groups of hits produced, as it will account for
1909 any delays and distortions introduced by the FIR and the matched filters.

1910 In the case of the raw waveforms (with noise), I run the hit finder on them, with
1911 different values of the threshold, after applying either the FIR or the matched filters. I
1912 will name them simply standard hits and matched filter hits respectively. Then, I match
1913 the generated hits to the true hits (the standard hits with the standard true hits and
1914 the matched filter hits with the matched filter true hits). The matching is performed by
1915 comparing the channel number and the timestamp of the hits. To count as a match,
1916 I require that all hits with the same channel number and timestamp have overlapping
1917 hit windows, i.e. the time windows between their hit end and hit start times need to

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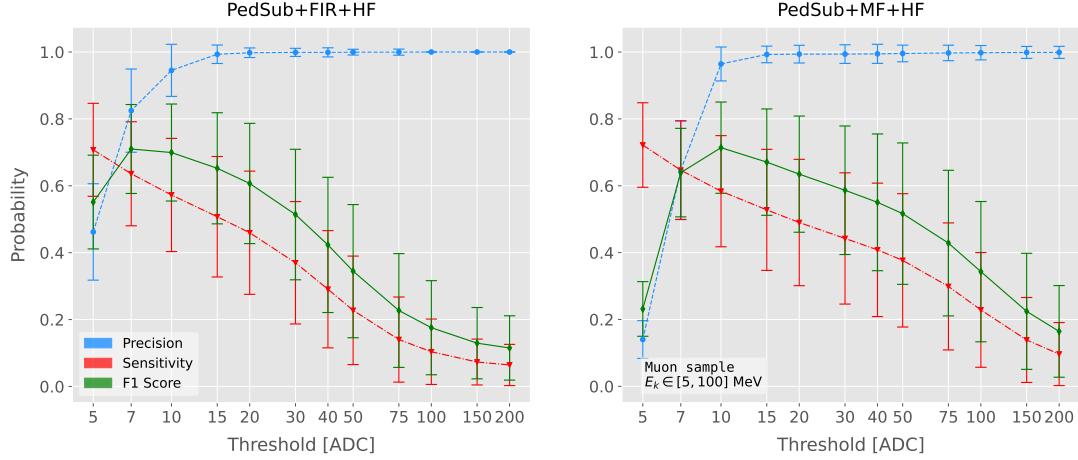


Figure 4.18: Dependence of the precision (blue), sensitivity (red) and F_1 (green) scores on the threshold values used in the hit finder, for the FIR (left panel) and matched filter (right panel) cases. The results were obtained after matching the hits to the true hits in the case of the isotropic muon sample with kinetic energy in the range 5 to 100 MeV, taking only into account the induction plane channels. The points represent the mean value while the error bars indicate one standard deviation around that mean value.

overlap. If more than one hit in one of the groups have hit overlap with the same hit in the other group I only count the hit with closer hit peak time value.

The generation of the samples, the procedure to produce the standard hits (with the default FIR filter) and matched filter hits and the matching of these with the true hits is described in detail in App. ??.

To quantify the performance of the two hit finder approaches, I use a classical method from statistical classification known as confusion matrix [111]. This is basically a way of sorting the outputs of a binary classifier, considering the true values of the classification and the predicted values. It divides the outputs in four categories: true positive (TP, both true and predicted values are 1), false negative (FN, true value is 1 but predicted is 0), false positive (FP, true value is 0 but predicted is 1) and true negative (TN, both true and predicted values are 0)).

The contents of the confusion matrix allow us to compute other derived scores to judge the performance of our classifiers. In this study, I will make use of three of these

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1932 metrics, namely the precision or positive predictive value:

$$\text{PPV} = \frac{\text{TP}}{\text{TP} + \text{FP}}, \quad (4.22)$$

1933 the sensitivity or true positive rate:

$$\text{TPR} = \frac{\text{TP}}{\text{TP} + \text{FN}}, \quad (4.23)$$

1934 and the F_1 score [112]:

$$F_1 = \frac{2\text{TP}}{2\text{TP} + \text{FP} + \text{FN}}, \quad (4.24)$$

1935 which is the harmonic mean of the precision and the sensitivity.

1936 In our specific case I am not going to make use of the true negative value, as its
1937 definition in this context can be ambiguous because one does not have clear instances in
1938 the classification process. This way, I will only count the number of true positives as the
1939 total amount of hits I can match between true and raw populations, the number of false
1940 negatives will be the number of missing true hits and the false positive the number of
1941 hits which do not match any true hit.

1942 In Fig. 4.18 I show the precision (blue), sensitivity (red) and F_1 (green) scores I
1943 obtained for different values of the threshold used in the hit finder for the case of the
1944 muon sample. Because the matched filters are only applied to induction channels, I only
1945 consider here hits coming from the U and V planes. The panel on the left corresponds
1946 to the scores I got when I ran the hit finder on the FIR filtered waveforms, whereas the
1947 right panel contains the scores for the matched filter case. The points are centered at
1948 the threshold value used and represent the mean value obtained for each score using all
1949 the generated events, while the error bars indicate one standard deviation around the
1950 mean value.

1951 One can see that the precision for the matched filter case is lower when the thresholds
1952 are very low, as the noise baseline is slightly amplified, but then rises to high values
1953 quicker than for the FIR case. The other difference one can spot is that the sensitivity

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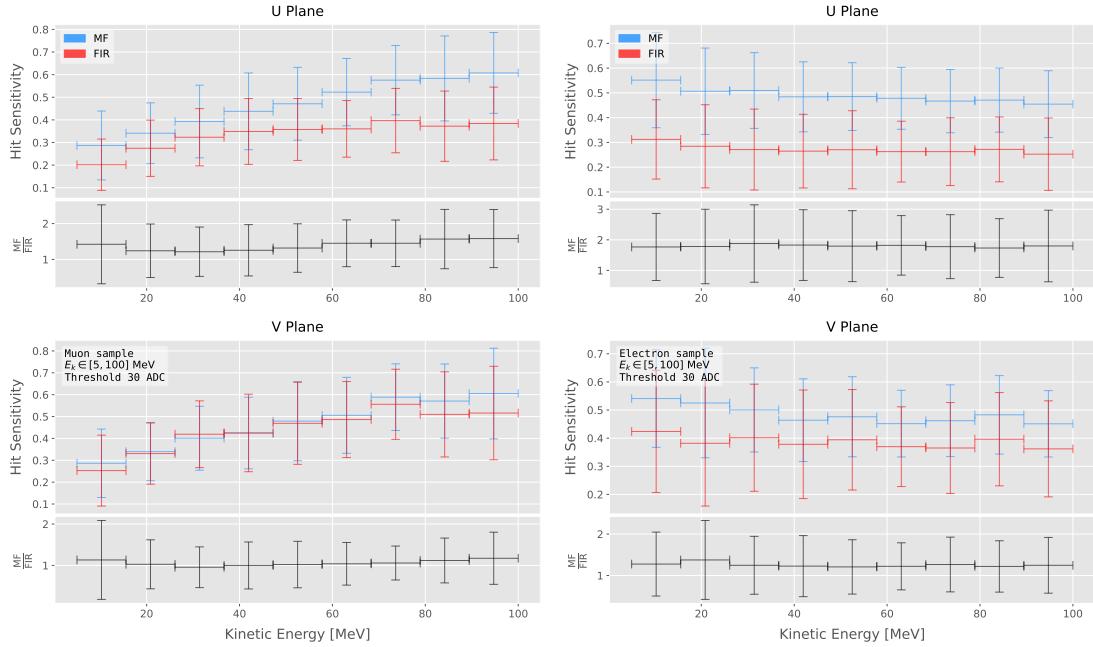


Figure 4.19: Dependence of the averaged hit sensitivity on the kinetic energy of the events for the matched filter (blue) and standard (red) hits, for the case of the muon (left panel) and electron (right panel) samples, separated between U (top plots) and V (bottom plots) induction wire planes. The top subplots contain the hit sensitivities for the two hit finder alternatives, while the bottom subplots show the ratio between the two. The horizontal lines sit at the mean value and represent the size of the energy bins, while the vertical error bars indicate one standard deviation around that mean value.

in the FIR case starts dropping faster at around the same threshold values where the precision stabilizes around 1, while in contrast for the matched filter this rapid decrease starts at higher threshold values. A similar scan for the same thresholds was performed for the electron sample in the same energy range, yielding similar results.

In Fig. 4.19 I show the averaged hit sensitivity versus the kinetic energy of the events, both for the matched filter hits (blue) and the standard hits (red). The left panel corresponds to the muon sample, whereas the one on the right corresponds to the electron sample, both with kinetic energies between 5 and 100 MeV. In each panel the top plot corresponds to hits in the U plane, while the bottom plot contains the same information for the V plane. Each plot contains two subplots, the one on the top shows the hit sensitivity values for the matched filter and standard hits separate, while the bottom subplot depicts the ratio between the matched filter and standard sensitivities.

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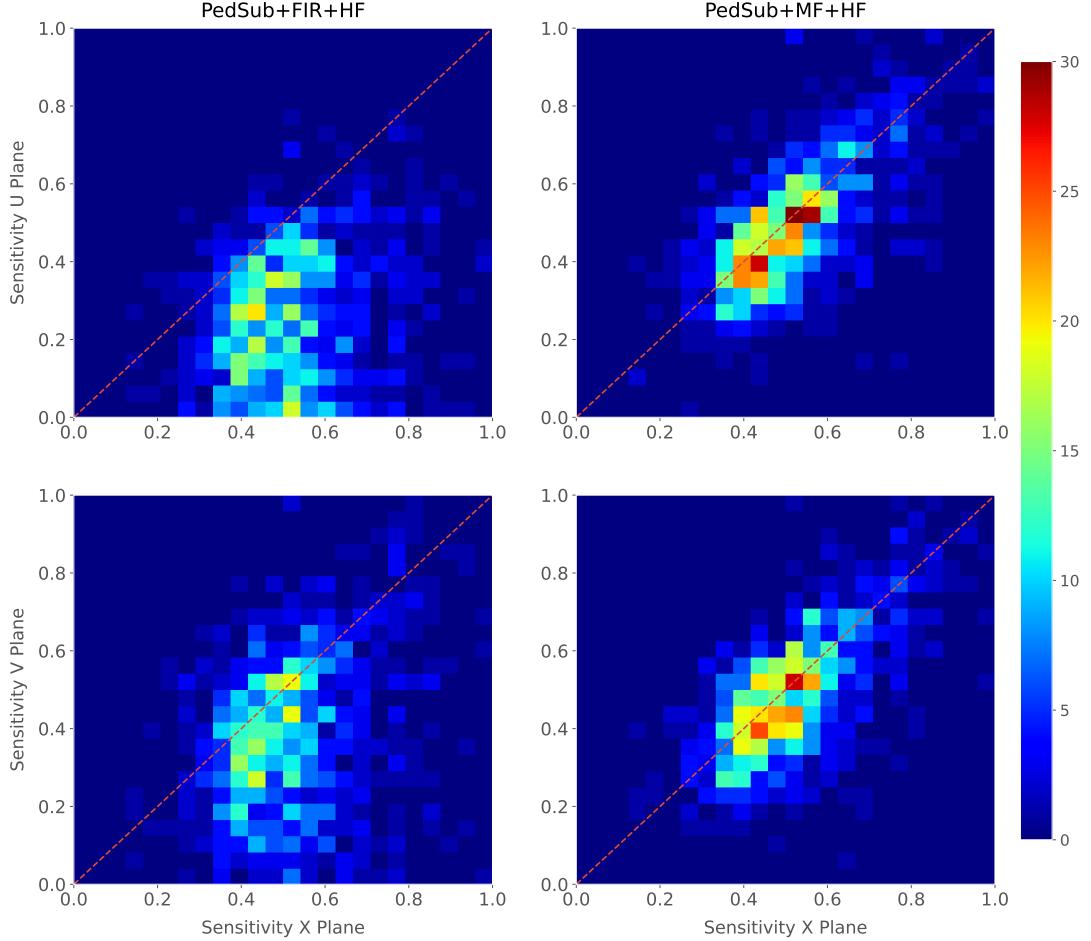


Figure 4.20: Distributions of the hit sensitivity in the U (top panels) and V (bottom panels) planes versus the hit sensitivity in the X plane, both for the standard hits (left panels) and the matched filter hits (right panels), in the case of the electron sample and a threshold of 30 ADC.

1966 The horizontal lines are placed at the mean value obtained in the fit and represent the
 1967 width of the E_k bins used, while the vertical error bars indicate one standard deviation
 1968 around that mean value. In both cases the threshold used was 30 ADC, as I required
 1969 the precision to be higher than 0.99 for both matched filter and standard cases.

1970 One can see that, in general, the improvements are better for the U than for the V
 1971 plane. While for the U channels I achieved a mean improvement of 50% and 80% for
 1972 muons and electrons respectively, the improvement in the V plane is stalled at 10% and
 1973 25%. Nevertheless, if I look at the sensitivities for the matched filter hits in both planes
 1974 one can see these have similar mean values for each energy bin, while on the contrary

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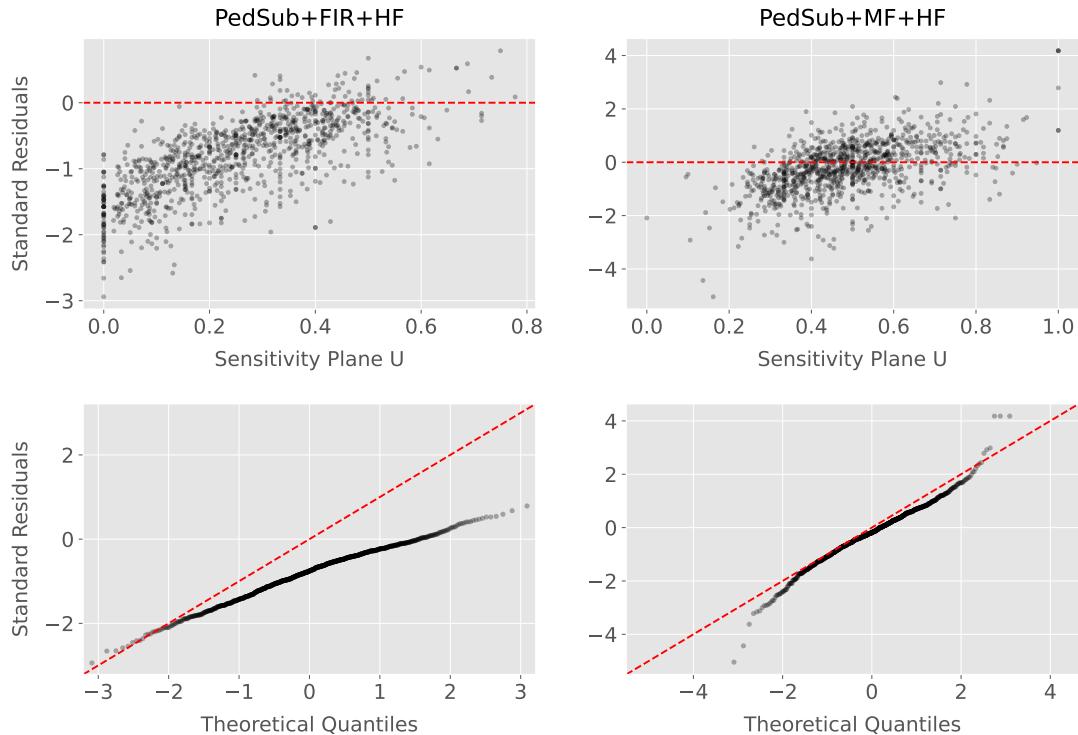


Figure 4.21: Top panels: standard residual plots of the hit sensitivities between the X and U planes. Bottom panels: quantile-quantile plots of the hit sensitivity standard residuals between the X and U planes. In all cases, the left panel corresponds to the standard hits while the right panel represents the matched filter case, all from the electron sample with a 30 ADC threshold.

1975 for the standard hits the sensitivity remains relatively high for the V plane. This way, it
 1976 looks there was a less significant gain because the hit sensitivity was already high.

1977 Another interesting observation is the different behaviors for muons and electrons.
 1978 While hit sensitivity for muons grows significantly with energy, in the case of electrons
 1979 this slightly decreases the higher the kinetic energy of the event is. In any case, when it
 1980 comes to the improvement on the sensitivities, this remains almost constant in all cases.

1981 Furthermore, we can look at how the concurrence of hits between the different wire
 1982 planes has changed. For any given event, I expect to have a similar number of hits in the
 1983 three planes. As the ionisation electrons need to cross the U and V planes prior to reach
 1984 the collection plane X they will induce current in those wire planes. A way to check the
 1985 concurrence of hits across planes is looking at the relation between the hit sensitivities
 1986 for each individual event. One cannot expect the sensitivities to be exactly equal across

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1987 planes, but ideally they should be normally distributed around the diagonal.

1988 Fig. 4.20 shows the hit sensitivity in the U (top panels) and V (bottom panels)
1989 planes versus the hit sensitivity in the X plane, for the case of the standard hits (left
1990 panels) and the matched filter hits (right panels). All plots were generated for the
1991 electron sample and a threshold of 30 ADC. From these one can see a clear trend,
1992 when I use the standard hit finder chain the sensitivities in the induction planes are
1993 systematically lower than the hit sensitivity in the X plane, i.e. most of the points sit
1994 below the diagonal (red dashed line). In contrast, when the matched filters are applied,
1995 the majority of the events are distributed around the diagonal. This points out that the
1996 concurrence of hits across planes has improved.

1997 To exemplify the improvement I obtained, one can consider the residuals of the hit
1998 sensitivities for the X and U planes. Assuming the diagonal hypothesis, i.e. given a
1999 dataset of the form (x, y) for any x I take the predicted y value to be equal to the value
2000 of x , I can compute the standard residuals for the hit sensitivities in U given the ones for
2001 X. In Fig. 4.21 (top panels) I show these standard residuals against the corresponding
2002 values of the hit sensitivity in the U plane, for our electron sample with kinetic energy
2003 between 5 and 100 MeV. If I compare the scatter points in the case of the standard
2004 hits (left panel) and the matched filter hits (right panel), I see that the residuals of the
2005 standard hit finder case follow a certain pattern and their mean deviates from 0.

2006 To see clearly if the residuals are normally distributed, in Fig. 4.21 (bottom panels)
2007 I plot the corresponding quantile-quantile plot for both the standard (left panel) and
2008 matched filter (right panel) standard residuals. One can clearly see that the points for
2009 the standard case follow a strongly non-linear pattern, suggesting that the residuals
2010 do not follow a normal distribution. In contrast, for the matched filter hits the points
2011 conform to a roughly linear path, implying that in this case the normality condition is
2012 fulfilled.

2013 All these results hint at the fact that the concurrence of hits across the wire planes
2014 can be strengthened by applying the matched filters.

2016 DM searches with neutrinos from the Sun

2017 The idea of detecting neutrino signals coming from the Sun’s core to probe DM is not
2018 new. The main focus of these searches has usually been high-energy neutrinos originated
2019 from DM annihilations into heavy particles [113–116], although recent studies have
2020 proposed to look at the low-energy neutrino flux arising from the decay of light mesons
2021 at rest in the Sun [117–120] previously thought undetectable.

2022 In this Chapter I try to demonstrate the capability of DUNE to constrain different
2023 DM scenarios. I used the neutrino fluxes arising from DM annihilations in the core
2024 of the Sun to compute the projected limits that DUNE would be able to set on the
2025 annihilation rates in the Sun and the DM scattering cross sections.

2026 5.1 Gravitational capture of DM by the Sun

2027 The Sun and the centre of the Earth are possible sources of DM annihilations, specially
2028 interesting because of their proximity. Their gravitational attraction ensured the capture
2029 of DM from the local halo through repeated scatterings of DM particles crossing them.
2030 Only neutrinos produced from DM annihilations can escape the dense interior of these
2031 objects. Therefore, neutrino telescopes are the most useful experimental layouts to
2032 pursue DM searches from their cores.

2033 The neutrino flux from DM annihilations inside the Sun depends on the DM capture
2034 rate, which is proportional to the DM scattering cross section, and the annihilation rate,
2035 which is proportional to the velocity-averaged DM annihilation cross-section. The total

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2036 number of DM particles inside the Sun follows the Boltzmann equation [117]:

$$\frac{dN_{DM}}{dt} = C_{\odot} - A_{\odot} N_{DM}^2, \quad (5.1)$$

2037 where C_{\odot} and A_{\odot} are the total Sun DM capture and annihilation rates respectively.
 2038 In this expression I neglected the evaporation term, proportional to N_{DM} , which only
 2039 contribute for $m_{DM} \lesssim 4$ GeV [121]. As the current threshold of neutrino telescopes
 2040 is a few GeV, this region falls below the probed range but can be important in future
 2041 low-energy projects.

2042 This equation has an equilibrium solution:

$$N_{DM}^{eq} = \sqrt{\frac{C_{\odot}}{A_{\odot}}}, \quad (5.2)$$

2043 which represents the amount of DM inside the Sun if the capture and annihilation have
 2044 reached equilibrium. As the Sun is approximately 4.6 Gyr old, it is usually assumed that
 2045 equilibrium has been achieved. Therefore, the anomalous neutrino flux from the Sun
 2046 would only depend on the DM scattering cross section, enabling us to set limits on this
 2047 quantity. If one does not assume equilibrium, some assumptions on the DM annihilation
 2048 cross section are necessary to extract predictions from neutrino signals.

2049 Here, I am going to consider three possible scenarios for the DM interactions: DM
 2050 scattering off electrons, spin-dependent (SD) and spin-independent interactions off nuclei.
 2051 For the case of these last two, the cross sections will be given in terms of the SD and
 2052 SI elastic scattering DM cross section off protons (assuming that DM interactions off
 2053 protons and neutrons are identical), σ_p^{SD} and σ_p^{SI} , as [2, 117]:

$$\sigma_i^{\text{SD}} = \left(\frac{\tilde{\mu}_{A_i}}{\tilde{\mu}_p} \right)^2 \frac{4(J_i + 1)}{3J_i} |\langle S_{p,i} \rangle + \langle S_{n,i} \rangle|^2 \sigma_p^{\text{SD}}, \quad (5.3)$$

$$\sigma_i^{\text{SI}} = \left(\frac{\tilde{\mu}_{A_i}}{\tilde{\mu}_p} \right)^2 A_i^2 \sigma_p^{\text{SI}}, \quad (5.4)$$

2054 where $\tilde{\mu}_{A_i}$ is the reduced mass of the DM-nucleus i system, $\tilde{\mu}_p$ is the reduced mass of

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the DM-proton system, A_i and J_i the mass number and total angular momentum of nucleus i and $\langle S_{p,i} \rangle$ and $\langle S_{n,i} \rangle$ the expectation value of the spins of protons and neutrons averaged over all nucleons, respectively (see Ref. [122] for a review on spin expectation values).

Since the Sun is mainly composed of Hydrogen, the capture of DM from the halo is expected to occur mainly through spin-dependent scattering. However, since the spin-independent cross section is proportional to the square of the atomic mass, heavy elements can contribute to the capture rate (even though they constitute less than 2% of the mass of the Sun). Heavy elements can also contribute to the spin-dependent cross section if the DM has also momentum-dependent interactions.

DM particles can get captured by the Sun if after repeated scatterings off solar targets their final velocity is lower than the escape velocity of the Sun. In the limit of weak cross sections, this capture rate can be approximately written as [2]:

$$C_{\odot}^{\text{weak}} = \sum_i \int_0^{R_{\odot}} dr \ 4\pi r^2 \int_0^{\infty} du_{\chi} \frac{\rho_{\chi}}{m_{\chi}} \frac{f_{v_{\odot}}(u_{\chi})}{u_{\chi}} \omega(r) \int_0^{v_e(r)} dv \ R_i^-(\omega \rightarrow v) |F_i(q)|^2, \quad (5.5)$$

where the summation extends over all possible nuclear targets. In this expression, R_{\odot} is the radius of the Sun, ρ_{χ} is the local DM density, m_{χ} the mass of the DM particle, $f_{v_{\odot}}(u_{\chi})$ the DM velocity distribution seen from the Sun's reference frame, $R_i^-(\omega \rightarrow v)$ is the differential rate at which a DM particle with velocity v scatters a solar target of mass m_i to end up with a velocity ω and $|F_i(q)|$ is the nuclear form factor of target i .

The differential scattering rate takes a rather simple form when considering velocity-independent and isotropic cross sections. In that case, this quantity is given by [2, 123]:

$$R_i^-(\omega \rightarrow v) = \frac{2}{\sqrt{\pi}} \frac{\mu_{i,+}^2}{\mu_i} \frac{v}{\omega} n_i(r) \sigma_i \left[\chi(-\alpha_-, \alpha_+) + \chi(-\beta_-, \beta_+) e^{\mu_i(\omega^2 - v^2)/u_i^2(r)} \right], \quad (5.6)$$

where μ_i is the ratio between the DM mass and the mass of target i , $\mu_{i,\pm}$ is defined as:

$$\mu_{i,\pm} \equiv \frac{\mu_i \pm 1}{2}, \quad (5.7)$$

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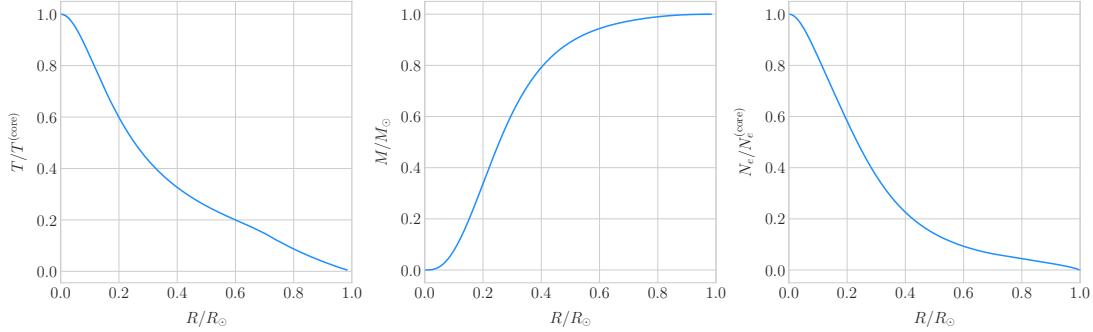


Figure 5.1: Input solar parameters used in our capture rate computation as functions of the Sun’s radius, from left to right: temperature (with respect to the temperature at the core), mass (in solar masses) and electron number density (with respect to the electron density at the core). All quantities shown correspond to the standard solar model BS2005-OP [1].

2076 $n_i(r)$ is the density profile of target i in the solar medium, $u_i(r)$ is the most probable
2077 velocity of target i given by:

$$u_i(r) = \sqrt{\frac{2T_\odot(r)}{m_i}}, \quad (5.8)$$

2078 where $T_\odot(r)$ is the temperature of the Sun, the quantities α_\pm and β_\pm are defined as:

$$\alpha_\pm \equiv \frac{\mu_{i,+}v \pm \mu_{i,-}\omega}{u_i(r)}, \quad (5.9)$$

$$\beta_\pm \equiv \frac{\mu_{i,-}v \pm \mu_{i,+}\omega}{u_i(r)}, \quad (5.10)$$

2079 and the function $\chi(a, b)$ is a Gaussian integral of the form:

$$\chi(a, b) \equiv \int_a^b dx e^{-x^2}. \quad (5.11)$$

2080 Finally, if one assumes the DM halo velocity distribution in the galactic rest frame
2081 to be a Maxwell-Boltzmann distribution, one can write the halo velocity distribution for
2082 an observer moving at the speed of the Sun with respect to the DM rest frame as:

$$f_{v_\odot}(u_\chi) = \sqrt{\frac{3}{2\pi}} \frac{u_\chi}{v_\odot v_d} \left(e^{-\frac{3(u_\chi - v_\odot)^2}{2v_d^2}} - e^{-\frac{3(u_\chi + v_\odot)^2}{2v_d^2}} \right), \quad (5.12)$$

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2083 where:

$$\omega^2 = u_\chi + v_e(r)^2, \quad (5.13)$$

2084 is the DM velocity squared, v_\odot the relative velocity of the Sun from the DM rest frame
 2085 and $v_d \simeq \sqrt{3/2}v_\odot$ the velocity dispersion.

2086 For the case of strong scattering cross section, Eq. (5.5) ceases to be valid, as it
 2087 escalates indefinitely with the cross section. In that limit, the capture rate saturates to
 2088 the case where the probability of interaction is equal to one, which can be written as:

$$C_\odot^{\text{geom}} = \pi R_\odot^2 \left(\frac{\rho_\chi}{m_\chi} \right) \langle v \rangle \left(1 + \frac{3}{2} \frac{v_e^2(R_\odot)}{v_d^2} \right) \xi(v_\odot, v_d), \quad (5.14)$$

2089 where $v_d = \sqrt{8/3\pi}v_d$ is the mean velocity in the DM rest frame and the factor $\xi(v_\odot, v_d)$
 2090 accounts for the suppression due to the motion of the Sun:

$$\xi(v_\odot, v_d) = \frac{v_d^2 e^{-\frac{3v_\odot^2}{2v_d^2}} + \sqrt{\frac{\pi}{6}} \frac{v_d}{v_\odot} (v_d^2 + 3v_e^2(R_\odot) + 3v_\odot^2) \operatorname{Erf} \left(\sqrt{\frac{3}{2}} \frac{v_\odot}{v_d} \right)}{2v_d^2 + 3v_e^2(R_\odot)}. \quad (5.15)$$

2091 Having these into account, one can write the total capture rate as a combination of
 2092 both contributions, allowing a smooth transition between the two, as:

$$C_\odot = C_\odot^{\text{weak}} \left(1 - e^{C_\odot^{\text{geom}} / C_\odot^{\text{weak}}} \right). \quad (5.16)$$

2093 I computed the capture rate from Eq. (5.16) in the case of interactions with
 2094 electrons. To do so, I used the standard solar model BS2005-OP [1]. Fig. 5.1 shows the
 2095 three parameters from the solar model that are needed for the computation, the solar
 2096 temperature (left panel), mass (central panel) and electron density (right panel) profiles.

2097 For the case of the interactions off nuclei, the computations are more convoluted
 2098 as one needs to add up the contributions of the different most abundant nuclei in
 2099 the Sun. Also, in contrast to the electron scenario where the form factor is trivially
 2100 $|F_e(q)|^2 = 1$, for any nucleus i one would need to consider some appropriate nuclear
 2101 density distribution (either a Gaussian approximation, a Woods-Saxon distribution, etc)

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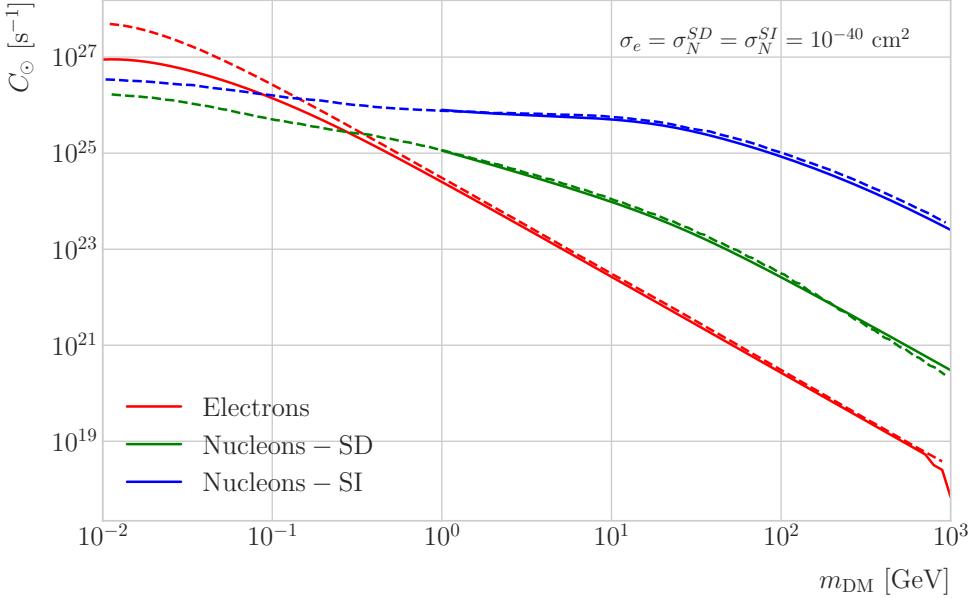


Figure 5.2: Capture rates as a function of the DM mass for the DM-electron interactions (red lines), SD DM-nucleons interactions (green lines) and SI DM-nucleons interactions (blue lines). Solid lines represent the values computed in this work while the dashed lines are the one given in Ref. [2]. All the rates are shown for a choice of scattering cross section of $\sigma_i = 10^{-40} \text{ cm}^2$.

which would complicate the calculations even further.

That is the reason why, at this stage of our study, I decided to take an alternative approach to the computation of the DM-nucleus capture rates. I used the **DarkSUSY** software, that allows us to compute these quantities performing a full numerical integration over the momentum transfer of the form factors. The default standard solar model used by **DarkSUSY** is BP2000¹ [124].

In Fig. 5.2 I show the results I obtained for the capture rates, for the case of interactions off electrons (red solid line), SD (green solid line) and SI (blue solid line) interactions of nucleons. In all cases I used a value of the scattering cross sections of $\sigma_i = 10^{-40} \text{ cm}^2$. Note here one of the limitations of the **DarkSUSY** approach, one can not extend the computation below $m_{\text{DM}} = 1 \text{ GeV}$. Nevertheless, this is not something to worry about in this case, as I will discuss next. As a comparison, I added also the

¹This is what they say in their manual, but I fear it is somewhat outdated. It appears to me this model is relatively old and do not see why they are not using others like [1]. Maybe one can double-check in the code to make sure.

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values computed in Ref. [2] (same color scheme, dashed lines). One can see there is good agreement between these and the **DarkSUSY** computation of the SD and SI interactions for $m_{\text{DM}} \geq 1$ GeV. In this regime their computations also matches quite well our result for the electron capture rate. However, these start to differ significantly below $m_{\text{DM}} = 1$ GeV, being their estimate up to a factor of 5 bigger than ours for low masses.

Let us comment briefly about the assumption I made before about not including an evaporation term in the Boltzmann equation. If I include this term in the equation (which will be proportional to the number of DM particles) the equilibrium solution takes the form:

$$N_{\text{DM}}^{\text{eq}} = \sqrt{\frac{C_{\odot}}{A_{\odot}}} \frac{1}{\kappa + \frac{1}{2} E_{\odot} \tau_{\text{eq}}}, \quad (5.17)$$

where E_{\odot} is the total evaporation rate, τ_{eq} is the equilibrium time in the absence of evaporation:

$$\tau_{\text{eq}} = \frac{1}{\sqrt{C_{\odot} A_{\odot}}}, \quad (5.18)$$

and κ is defined as:

$$\kappa \equiv \sqrt{1 + \left(\frac{E_{\odot} \tau_{\text{eq}}}{2} \right)^2}. \quad (5.19)$$

Now, it is easy to proof that in case evaporation dominates $\kappa \gg 1$ and therefore:

$$N_{\text{DM}}^{\text{eq}} \simeq \frac{C_{\odot}}{E_{\odot}}. \quad (5.20)$$

In contrast, if evaporation is irrelevant $\kappa \simeq 1$ and one recovers Eq. (5.2).

In this way, one can define the evaporation mass as the mass for which the number of DM particles in equilibrium approaches Eq. (5.20) at 10% level:

$$\left| N_{\text{DM}}^{\text{eq}}(m_{\text{evap}}) - \frac{C_{\odot}(m_{\text{evap}})}{E_{\odot}(m_{\text{evap}})} \right| = 0.1 N_{\text{DM}}^{\text{eq}}(m_{\text{evap}}). \quad (5.21)$$

This can be regarded as the minimum testable mass one can reach using the annihilation products of the DM in the Sun.

It was reported in Ref. [2] that, in the case of both SD and SI DM interactions

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off nuclei, this value ranges from 2 to 4 GeV depending on the specific scattering cross section value, compatible with the usual assumptions in the literature. What is interesting is the case of the electron capture. It was found that, when one applies a cutoff in the velocity distribution of the DM trapped in the Sun slightly below the escape velocity, the evaporation mass for the DM-electron interaction decreases remarkably. For a moderate choice of $v_c(r) = 0.9v_e(r)$ one gets an evaporation mass of around 200 to 600 MeV. This possibility opens a region of the parameter space that could be tested with neutrino detectors.

5.2 Neutrino flux from DM annihilations

When WIMPs annihilate inside the Sun a flux of high-energy neutrinos is expected from heavy quarks, gauge bosons and $\tau^+\tau^-$ final states, which decay before losing energy in the dense solar medium, as they will produce a continuum spectra up to $E_\nu \sim m_\chi$ (in the case of direct annihilation to neutrinos one would have a line at $E_\nu = m_\chi$) [118]. This kind of signal has been extensively studied in the literature, allowing to put strong limits on the SD WIMP-proton cross section for large m_χ . However, the number of high-energy neutrinos per WIMP annihilation is small and the spectrum depends on the unknown final state. Moreover, background rejection is easier for large m_χ but neutrinos with $E_\nu \gtrsim 100$ GeV are significantly attenuated by interactions in the Sun.

Nevertheless, most WIMP annihilation final states eventually produce a low-energy neutrino spectrum. In this case one does not just consider the more massive final states but also annihilations into e^+e^- , $\mu^+\mu^-$ and light quarks [117]. In particular, light mesons would be produced and stopped in the dense medium, thus decaying at rest and producing a monoenergetic neutrino signal. The decay-at-rest of kaons will produce a $E_\nu = 236$ MeV ν_μ while in the case of pions one would have a $E_\nu = 29.8$ MeV ν_μ . In practice only K^+ and π^+ contribute to these signals, as K^- and π^- are usually Coulomb-captured in an atomic orbit and get absorbed by the nucleus. There is also a low-energy neutrino signal coming from muon decays, which are produced in kaon or

5.3. COMPUTING LIMITS FROM SOLAR NEUTRINO FLUXES

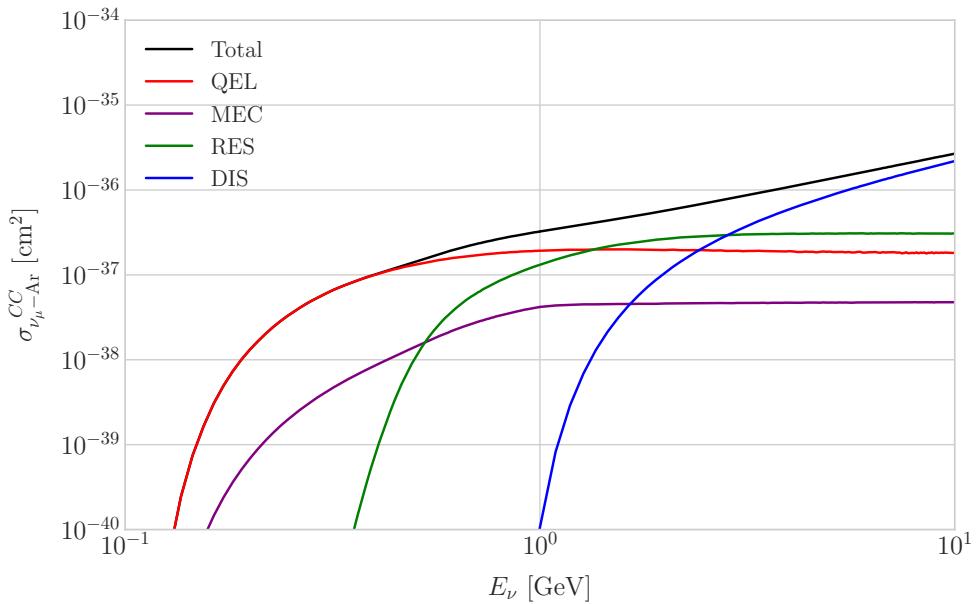


Figure 5.3: *NuWro* computed $\nu_\mu - {}^{40}\text{Ar}$ charged-current scattering cross section as a function of the neutrino energy E_μ . The black line shows to the total cross section, whereas the others correspond to the different contributions (in red quasi-elastic scattering, in green resonant pion exchange, in blue deep inelastic scattering and in purple meson exchange current).

2160 pion decays, leptonic decays of other hadrons and heavy leptons or even directly from
 2161 WIMP annihilations, which can decay at rest and contribute to the previous low-energy
 2162 neutrino flux with a well known spectrum below 52.8 MeV.

2163 These monoenergetic MeV neutrinos were previously considered undetectable but,
 2164 due to the large yield, the known spectra and the modern advances in the detector
 2165 technology, these low-energy neutrino flux can be a good probe of the SD WIMP-proton
 2166 cross-section in standard solar WIMP capture scenario, as it is sensitive to low WIMP
 2167 masses and insensitive to the particular final state. A good place to look for these signals
 2168 are next-generation neutrino experiments such as DUNE.

2169 5.3 Computing limits from solar neutrino fluxes

2170 In order to use the neutrino fluxes from DM annihilations in the Sun, the first thing I
 2171 need to do is to determine the expected number of atmospheric background events, for

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2172 a given exposure, after directionality selection has been applied. I can write this number

2173 as:

$$N_B = \eta_B \int d\Omega \int_{E_{min}}^{E_{max}} dE_\nu \frac{d^2\Phi_{atm}^\mu}{dE_\nu d\Omega} \times \left(A_{eff}^{(\mu)}(E_\nu) T \right), \quad (5.22)$$

2174 where η_B is the background efficiency, E_{min} and E_{max} the minimum and maximum

2175 energies to integrate over, $d^2\Phi_{atm}^\mu/dE_\nu d\Omega$ the differential flux of atmospheric muon

2176 neutrinos, $A_{eff}^{(\mu)}$ is the effective area of DUNE to muon neutrinos and T is the exposure

2177 time. The effective area can be expressed as the product of the neutrino-nucleus scattering

2178 cross section and the number of nuclei in the fiducial volume of the detector. This way

2179 for DUNE I can write:

$$A_{eff}^{(\mu)}(E_\nu) = (6.0 \times 10^{-10} \text{ m}^2) \left(\frac{\sigma_{\nu-\text{Ar}}^{(\mu)}(E_\nu)}{10^{-38} \text{ cm}^2} \right) \left(\frac{M_{target}}{40 \text{ kT}} \right), \quad (5.23)$$

2180 where $\sigma_{\nu-\text{Ar}}^{(\mu)}$ is the $\nu_\mu - {}^{40}\text{Ar}$ charged-current scattering cross section. In Fig. 5.3 I
 2181 show the computed value of this cross section as a function of the neutrino energy E_ν ,
 2182 in the range of interest both for the atmospheric background and signal events. It was
 2183 computed using the NuWro Monte Carlo neutrino event generator [125], including the
 2184 charged-current contributions of the quasi-elastic scattering (red line), resonant pion
 2185 exchange (green line), deep inelastic scattering (blue line) and meson exchange current
 2186 (purple line).

2187 The background rejection will depend on the resolution of the detector and the
 2188 selection one applies on the events. A geometry argument can be used to estimate
 2189 the maximum background rejection one can achieve in this case, considering one can
 2190 efficiently discriminate all events coming from a direction different from that of the
 2191 Sun. In that case, the optimal background efficiency will simply be the relative angular
 2192 coverage of the Sun. Taking the angular diameter of the Sun as seen from the Earth to
 2193 be 0.5° , I have:

$$\eta_B^{(opt)} \approx \frac{\pi \left(\frac{0.5}{2} \right)^2}{360 \times 180} \simeq 3.03 \times 10^{-6}. \quad (5.24)$$

2194 This value will give a very optimistic estimate of the number of background events.

5.3. COMPUTING LIMITS FROM SOLAR NEUTRINO FLUXES

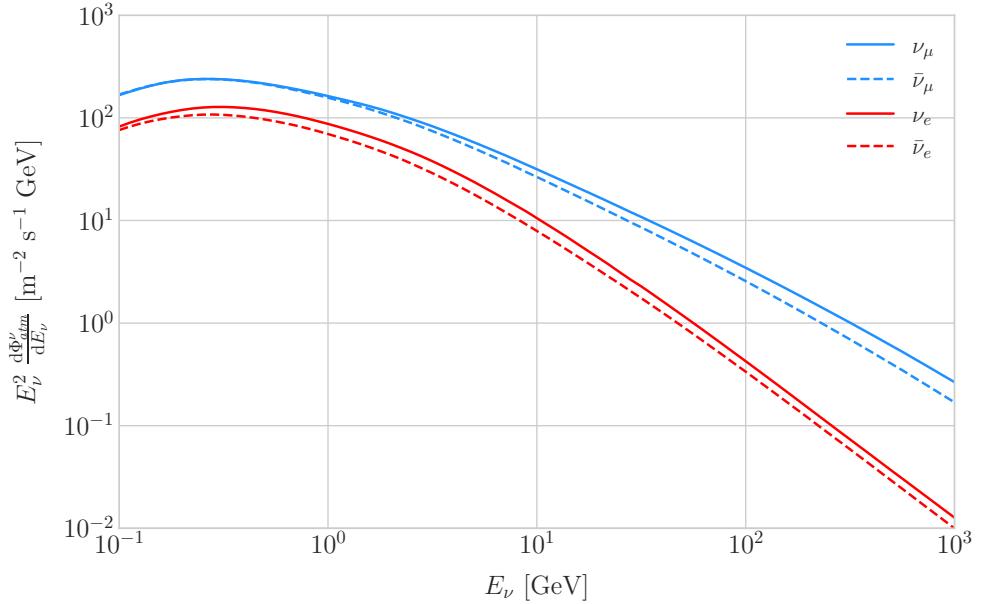


Figure 5.4: Expected atmospheric neutrino flux as a function of the neutrino energy E_ν at Homestake at solar minimum, taken from Ref. [3]. The blue solid (dashed) line correspond to muon neutrinos (antineutrinos) and the red solid (dashed) line correspond to electron neutrinos (antineutrinos).

2195 However, it can be regarded as an lower limit, as it represents the best case scenario.

2196 In Fig. 5.4 I show the fluxes of atmospheric neutrinos at the Homestake mine during
 2197 solar minimum, taken from Ref. [3]. The values are averaged over the two angular
 2198 directions. In blue I have the flux of muon neutrinos while in red I indicate the flux
 2199 of electron neutrinos. Additionally, the dashed lines correspond to both antineutrino
 2200 species.

2201 Using these values for the muon neutrino and the corresponding total CC cross
 2202 section, one can compute the number of expected background events by integrating over
 2203 the given energy range (as in this case the angular integral is trivial). As for the energy
 2204 range to integrate over, I choose the range for DUNE specified in [85], $E_{min} = 10^{-1}$ GeV
 2205 and $E_{max} = 10$ GeV. Taking all these into account, I found the number of background
 2206 events to be:

$$N_B \simeq \eta_B \times (3.827 \times 10^4) \times \left(\frac{\text{exposure}}{400 \text{ kT yr}} \right). \quad (5.25)$$

2207 In order to estimate the sensitivity of DUNE to this kind signal, one can consider a

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2208 hypothetical data set where the number of observed neutrinos is taken to be the expected
 2209 number of background events rounded to the nearest integer, $N_{obs} = \text{round}(N_B)$ [126].
 2210 Now, if I assume that the number of signal and background events seen by DUNE are
 2211 given by Poisson distributions with means equal to the expected number of signal and
 2212 background events, N_S and N_B , one can denote by N_S^{90} to the number of expected
 2213 signal events such that the probability of having an experimental run with a number of
 2214 events greater than N_{obs} is 90%. This number can be obtained as the numerical solution
 2215 to the equation:

$$1 - \frac{\Gamma(N_{obs} + 1, N_S^{90} + N_B)}{N_{obs}!} = 0.9, \quad (5.26)$$

2216 where $\Gamma(x, y)$ is the upper incomplete gamma function.

2217 The number of signal events is related to the neutrino flux from DM annihilations in
 2218 a similar way as the background events to the atmospheric neutrino flux. In this case I
 2219 have:

$$N_S = \eta_S \Gamma_A^{eq} \int_{z_{min}}^{z_{max}} dz \frac{dN_\nu}{dAdN_A dz} \times \left(A_{eff}^\mu(z) T \right), \quad (5.27)$$

2220 where η_S is the signal efficiency, Γ_A^{eq} is the total annihilation rate of DM particles at
 2221 equilibrium, $\Gamma_A^{eq} = A_\odot (N_{DM}^{eq})^2$, z_{min} and z_{max} the minimum and maximum relative
 2222 energies to integrate over (in such a way that $z_{min,max} \leq E_{min,max}/m_{DM}$ for each m_{DM})
 2223 and $dN_\nu/dAdN_A dz$ the muon neutrino flux per DM annihilation in the Sun.

2224 Knowing N_S^{90} one can use the relation in Eq. (5.27) to obtain $\Gamma_A^{eq,90}$ for different
 2225 values of the DM mass. From there I can directly translate those values into the
 2226 upper limits for DUNE on the DM scattering cross sections, for a given exposure. The
 2227 relation between the annihilation rate and the DM-nucleon cross section comes from the
 2228 equilibrium condition through the solar DM capture rate. The details of the evolution
 2229 of the number of DM particles inside the Sun and the computation of the capture rates
 2230 are discussed in App. 5.1.

5.4. EXAMPLE: KALUZA-KLEIN DARK MATTER

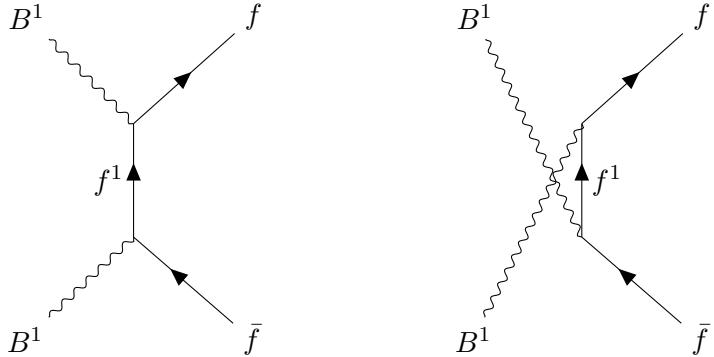


Figure 5.5: Feynman diagrams for $B^1 B^1$ annihilation into SM fermions.

2231 5.4 Example: Kaluza-Klein Dark Matter

2232 Even though there are plenty of BSM theories which provide viable dark matter
2233 candidates, Kaluza-Klein type of models [127, 128] within the universal extra dimensions
2234 (UED) paradigm naturally predict the existence of a massive, stable particle that can
2235 play the role of the dark matter. In the UED scenario all the SM fields can propagate
2236 in one or more compact extra dimensions [129], as opposed to the idea of brane worlds
2237 [130, 131], where just gravity can propagate in the bulk while SM particles live at fixed
2238 points.

2239 Furthermore, in UED there is no violation of the translational invariance along the
2240 extra dimensions, thus leading to degenerate KK modes masses and also the conservation
2241 of the KK number in the effective four dimensional theory. At loop level, radiative
2242 corrections and boundary terms shift the masses of the KK modes and break KK
2243 number conservation into a KK parity. As a result, this theory only contains interactions
2244 between an even number of odd KK modes and therefore the lightest among the first KK
2245 excitations will be stable. This particle is usually denoted as the lightest Kaluza-Klein
2246 particle (LKP) and its mass is proportional to $1/R$, being R the size of the extra
2247 dimension.

2248 A viable DM candidate needs to be electrically neutral and non-baryonic, therefore
2249 good candidates among the first Kaluza-Klein excitations would be the KK neutral

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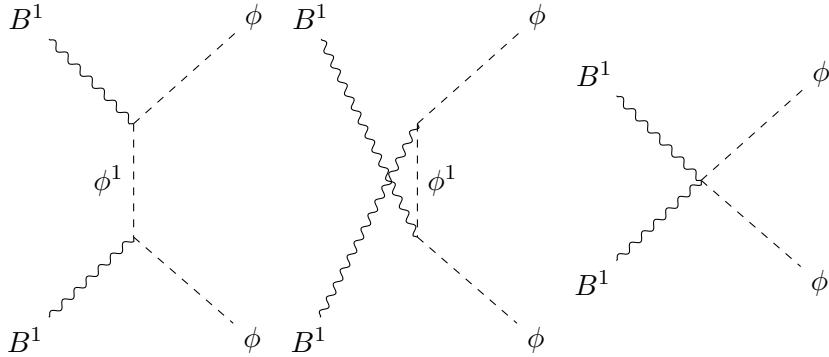


Figure 5.6: Feynman diagrams for B^1B^1 annihilation into a Higgs boson pair.

gauge bosons and the KK neutrinos [132]. Another possible candidate is the first KK excitation of the graviton, which receives negligible radiative contributions and therefore has a mass almost equal to $1/R$, but it has been shown that the lightest eigenstate from the mixing of the gauge mass states (B^1, W_3^1) would be lighter, as B^1 and W_3^1 receive negative radiative corrections [133]. It is also understood that, when these corrections become sizeable, the eigenstates become approximately pure B^1 and W_3^1 states as the Weinberg mixing angle grows small with the KK number [133]. In that case, the LKP can be well-approximated as being entirely B^1 .

I need to compute the neutrino flux produced by the annihilations of the LKP in the core of the Sun, taking into account their propagation in the solar medium, as well as neutrino oscillations. To this end I used `WimpSim` [134, 135] to generate one million annihilation events in the Sun over a time span of four years and propagate them to the DUNE FD location ($44^\circ 20' \text{ N}, 103^\circ 45' \text{ W}$), for different values of M_{LKP} . In Fig. 5.7 I show the obtained muon neutrino spectra arriving to the detector from LKP annihilations in the Sun, per unit area and per annihilation, plotted in relative energy units for different values of the mass. As one could expect the spectra get steeper the higher is the mass, due to the absorption of high-energy neutrinos in the solar medium. Also, one can see the peak at $z = 1$ due to the direct annihilation into neutrinos $\chi\chi \rightarrow \nu\bar{\nu}$.

Now, one can estimate the sensitivity of DUNE to this particular model by using

5.4. EXAMPLE: KALUZA-KLEIN DARK MATTER

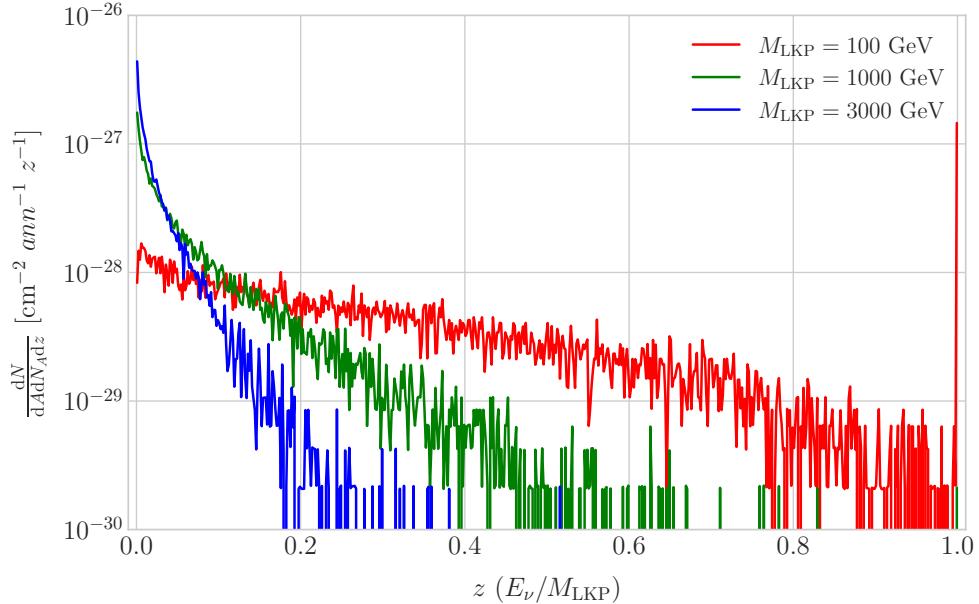


Figure 5.7: Computed spectra of muon neutrinos at the DUNE FD site from B^1 annihilations in the Sun for three different values of M_{LKP} , plotted in relative energy units for legibility.

the methods I previously discussed. To begin with, I will use the optimistic estimation
 of the background efficiency in Eq. (5.24) to get our upper bound. Using it, one can
 directly compute the number of expected background events to be $N_B = 0.1101$ for an
 exposure of 400 kT yr. Then, Eq. (5.26) give us a value of $N_S^{90} = 2.20$ for the 90%
 exclusion number of expected signal events. By using the NuWro generated cross sections
 and the computed neutrino fluxes from B^1 annihilations in the Sun I can estimate the
 limits on the SD and SI DM-nucleus cross section using the relation in Eq. (5.2) and
 the capture rates I computed with DarkSUSY.

In Fig. 5.8 I show the projected sensitive for DUNE on the spin-dependent B^1 -proton
 scattering cross section versus the mass of the DM particle, for a exposure of 400 kT yr
 (green dots). I also include the previous results from IceCube [4] (blue line) and Antares
 [5] (red line). The shaded area represents the disfavoured region from combined searches
 for UED by ATLAS and CMS [6].

From the experimental point of view, this estimation lacked a detailed simulation of
 the detector response and thus this must be consider as a mere optimistic sensitivity

CHAPTER 5. DM SEARCHES WITH NEUTRINOS FROM THE SUN

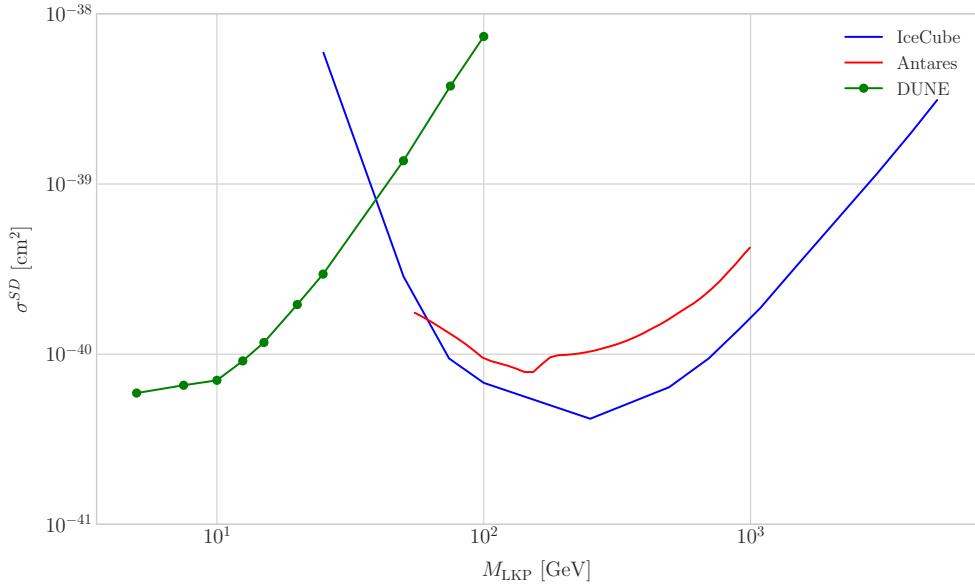


Figure 5.8: Projected 90% confidence level upper limit for DUNE (400 kT yr) on the spin-dependent B^1 -proton scattering cross section as a function of M_{LKP} (green dots). I also show the previous limits from IceCube [4] (blue line) and Antares [5] (red line) on the LKP cross section. The shaded area represents the disfavoured region (at 95% confidence level) on the mass of the LKP from LHC data [6].

computation. However, it shows the potential of DUNE to constrain this kind of exotic scenarios, showing the region where it will be in a position to compete with other neutrino telescopes. A more detailed analysis is needed if I am to make a realistic estimation. Even though the region of the parameter space where DUNE would be sensitive to this particular model is quite constrained by collider searches [6] and other rare decay measurements [136, 137], it still constitutes an alternative indirect probe.

5.5 High energy DM neutrino signals

To have better estimates on the capability of the DUNE FD to constrain the parameter space of DM using solar neutrino fluxes, I need to start accounting for the detector resolution effects and the topologies of the different signatures. As a starting point, I will focus on specific annihilation channels. For the case of DUNE, the relevant ones are mainly the hard channels $\tau^+\tau^-$ and $\nu\bar{\nu}$ and the soft channel $b\bar{b}$. These are the open annihilation channels for relatively low mass WIMPs that will actually give neutrino

5.5. HIGH ENERGY DM NEUTRINO SIGNALS

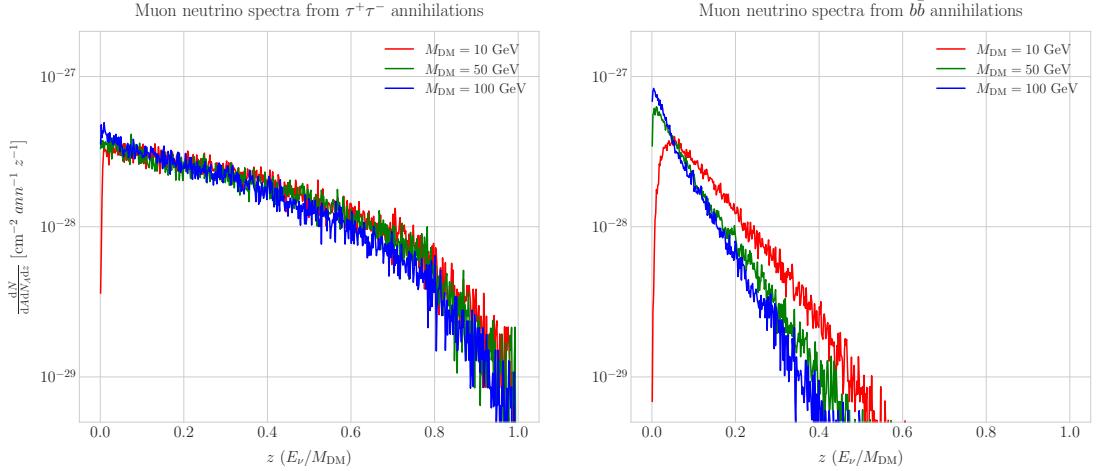


Figure 5.9: Computed spectra of muon neutrinos at the DUNE FD site from $\tau^+\tau^-$ (left panel) and $b\bar{b}$ (right panel) annihilations in the Sun for the DM masses $m_{\text{DM}} = 10 \text{ GeV}$ (red line), 50 GeV (green line) and 100 GeV (blue line), plotted in relative energy units.

2298 fluxes. Other channels, like W^+W^- and ZZ , are open for more massive WIMPs, but
 2299 those will produce usually a higher energy neutrino flux that will be out of reach for
 2300 DUNE (usually the maximum neutrino energy is taken to be $E_{\max} = 10 \text{ GeV}$).

2301 In Fig. 5.9 I show the `WimpSim` [134, 135] generated muon neutrino spectra at the
 2302 DUNE FD location ($44^\circ 20' \text{ N}, 103^\circ 45' \text{ W}$) from $\tau^+\tau^-$ (left panel) and $b\bar{b}$ (right panel)
 2303 annihilations in the core of the Sun, for different DM masses. Here, one can clearly see
 2304 the meaning of the previous distinction between hard and soft channels. For the same
 2305 DM mass value, the muon neutrino spectrum from the $\tau^+\tau^-$ channel is more flat and
 2306 reaches higher energies than the one from the $b\bar{b}$ channel, which drops faster.

2307 In this case, I prepared two sets of files, one for $\tau^+\tau^-$ and the other for $b\bar{b}$, for DM
 2308 masses in the range from 5 to 100 GeV (actually for $b\bar{b}$ the first mass point I took is
 2309 7.5 GeV , as a WIMP with $m_{\text{DM}} = 5 \text{ GeV}$ can not kinematically self annihilate into $b\bar{b}$).
 2310 Then, I prepared the `WimpSim` output fluxes in a specific way to use them as inputs to
 2311 `NuWro`, which simulates the neutrino interaction with the argon.

2312 Because `WimpSim` outputs an event list together with the fluxes, I can use the former
 2313 to generate the events. The direction of these is given in terms of the azimuth and
 2314 altitude angles viewed from the specified location, so first I need to convert these into the

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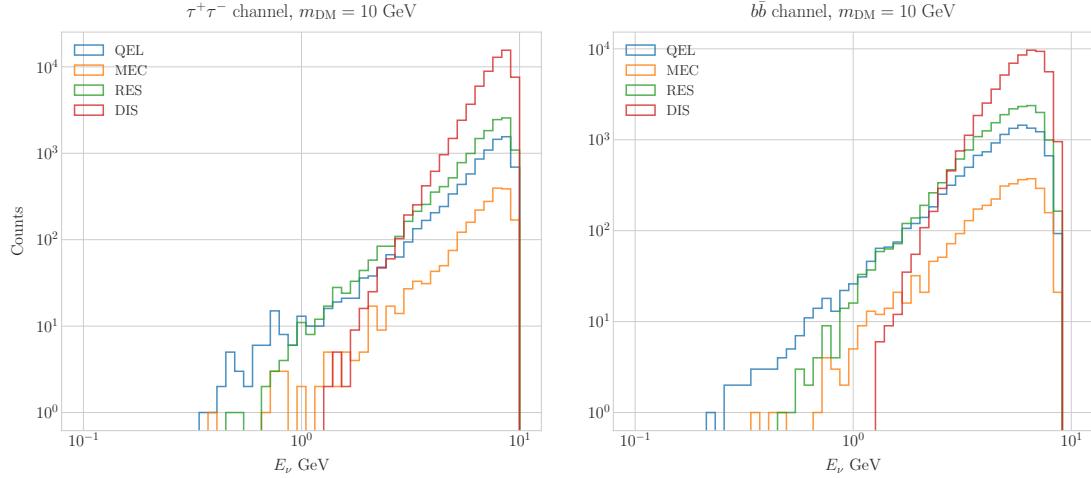


Figure 5.10: Distribution of the muon neutrino energies from the $\tau^+\tau^-$ (left panel) and $b\bar{b}$ (right panel) annihilation channels, for $m_{\text{DM}} = 10$ GeV, separated by CC interaction type: QEL (blue), MEC (orange), RES (green) and DIS (red).

2315 DUNE FD coordinates. Once I have done it, each event can be processed with `NuWro`.
 2316 To increase the number of samples and optimise the computation time, I generate 100
 2317 interactions (i.e. `NuWro` events) for each `WimpSim` event². I restrict the event generation
 2318 to charged current interactions, but I allow all the different contributions to the CC
 2319 cross section, i.e. quasielastic scattering (QEL), meson exchange current process (MEC),
 2320 resonant pion production (RES) and deep inelastic scattering (DIS). I just take into
 2321 account the CC contribution because I am only interested in final states with charged
 2322 leptons, as we have better chances of reconstructing the kinematics of CC events.

2323 For the atmospheric fluxes I follow a similar procedure, only that this time I do not
 2324 have a set of events but the fluxes binned in azimuth and altitude angles. This way, I
 2325 transform these to DUNE coordinates and process the fluxes for each bin separated with
 2326 `NuWro`.

2327 At this point, I have two sets of events with different energies and final states.
 2328 In Fig. 5.10 one can see the distribution of the muon neutrino energies for the case
 2329 $m_{\text{DM}} = 10$ GeV, both for the $\tau^+\tau^-$ (left panel) and $b\bar{b}$ (right panel) channels, separated

²This also solves a problem related with the generation of the neutrino interactions in `NuWro`, as if you only produce one event each time you launch `NuWro` it will always produce an interaction of the dominant interaction type for that particular energy.

5.5. HIGH ENERGY DM NEUTRINO SIGNALS

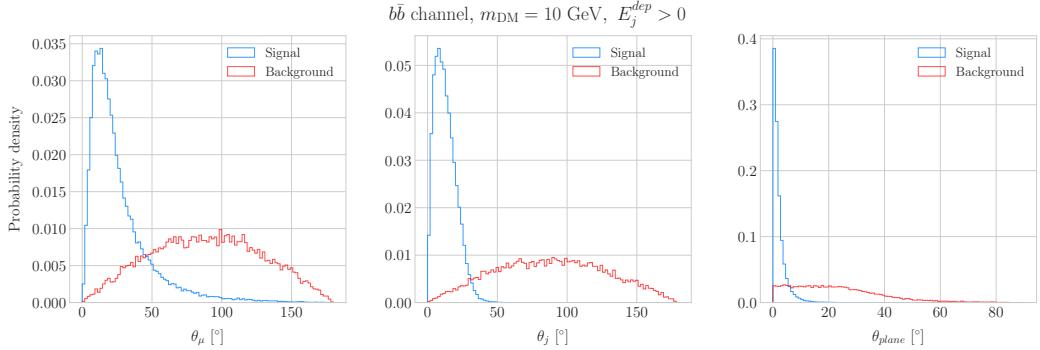


Figure 5.11: Distributions of θ_μ (left panel), θ_j (central panel) and θ_{plane} (right panel) for the $b\bar{b}$ sample with $m_{\text{DM}} = 10$ GeV (blue) and the atmospheric background (red).

by interaction. One can clearly see that there are different energy regimes where the primary interaction type is different. This leads to a plurality of event topologies, therefore making it difficult to implement a general approach to the selection of events in detriment of the background. As a way to proceed, I decided to split our samples, based on the different interaction modes and contents of the final state, into a CC DIS sample and a single proton CC QEL sample.

5.5.1 DIS events

To begin with, I consider the high energy part of the spectrum. In this region DIS events dominate, i.e. interactions of the form $\nu_\mu + q_d(\bar{q}_u) \rightarrow \mu^- + q_u(\bar{q}_d)$. Therefore, our final states will contain a muon and a hadronic jet from the fragmentation of the outgoing quark. As all these events have $E_\nu \gtrsim 1$ GeV the momentum transfer to the remnant nucleus is negligible, for this reason the neutrino energy can be effectively reconstructed just taking into account the momenta of the muon and the jet. This technique was successfully used in Ref. [138] to select monoenergetic DM solar neutrino events from $\nu\bar{\nu}$ annihilation channels.

Using momentum conservation one sees that the plane generated by the momenta of the muon and the jet needs to also contain the momentum of the neutrino. As we are interested in neutrinos coming from the Sun, the momentum of the neutrino can be regarded as known beforehand. This will allow us to define the angle of the outgoing

CHAPTER 5. DM SEARCHES WITH NEUTRINOS FROM THE SUN

2349 muon and jet with respect to the incoming neutrino. Moreover, one can also use that
 2350 information to reject poorly reconstructed jets, checking for deviations of these from the
 2351 momentum conservation plane.

2352 To account for the limited angular resolution of the detector, I smeared the momenta
 2353 of the muons and hadrons. In a liquid argon TPC muons are expected to be tracked with
 2354 high precision, therefore I take the associated angular resolution to be 1° . In the case of
 2355 jets, it is expected that for the hadrons dominating the cascade a detector like DUNE
 2356 has an angular resolution between 1° to 5° [85], so I take the latter, more conservative,
 2357 estimate.

2358 As a first selection step, I will just take into account particles with kinetic energies
 2359 above the detection threshold of DUNE. For muons and photons the specified threshold
 2360 energy is 30 MeV, for charged pions 100 MeV and for other hadrons 50 MeV [85]. This
 2361 way, if the outgoing muon in a certain event has an energy lower than the required
 2362 threshold I will drop such event. For the case of hadrons and photons, I will only require
 2363 to have at least one particle above the energy threshold, so then one can compute the
 2364 jet momentum using the (smeared) momenta of the N particles above threshold as:

$$\vec{p}_j = \sum_{i=1}^N \vec{p}_i. \quad (5.28)$$

2365 Additionally, I will also define an estimation of the deposited hadronic energy as:

$$E_j^{dep} = m_{^{39}\text{Ar}} - m_{^{40}\text{Ar}} + \sum_{i=1}^N \sqrt{|\vec{p}_i|^2 + m_i^2}. \quad (5.29)$$

2366 This quantity is useful to select events with enough hadronic visible energy in the
 2367 detector. For events where most of the hadronic energy is scattered across plenty of
 2368 hadrons with individual energies below the detection threshold, this estimation will
 2369 give $E_j^{dep} \leq 0$. In these cases it could be expected that the jet momentum is poorly
 2370 reconstructed, and therefore I require events to pass the cut $E_j^{dep} > 0$.

2371 For the events I can compute the angles for the muon and jet with respect to the

5.5. HIGH ENERGY DM NEUTRINO SIGNALS

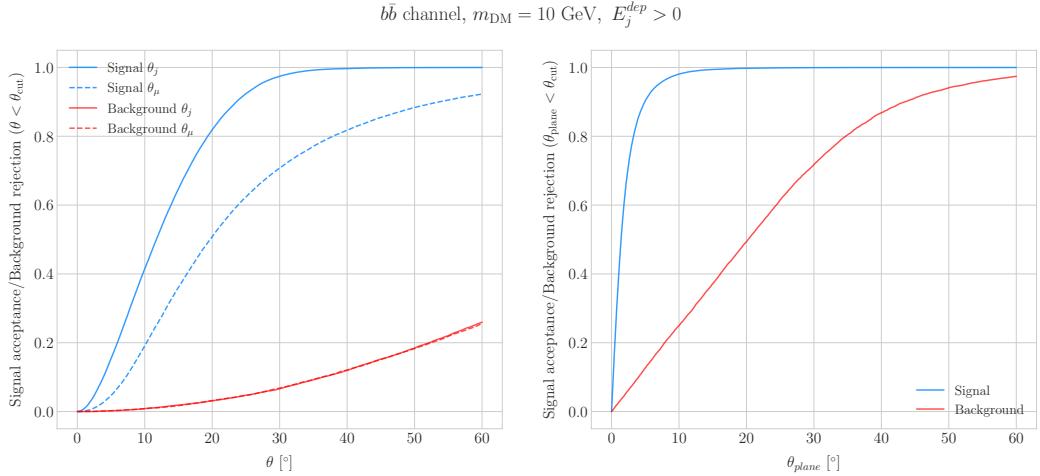


Figure 5.12: Left panel: signal efficiencies (blue lines) and background rejections (red lines) for events passing the cuts $\theta < \theta_{cut}$ for the jet (solid lines) and muon (dashed lines) angles. Right panel: signal efficiency (blue line) and background rejection (red line) for events passing the cut $\theta_{plane} < \theta_{cut}$ for the momentum conservation plane deviation.

2372 incoming neutrino as:

$$\cos \theta_\mu = \hat{p}_\nu \cdot \hat{p}_\mu, \quad (5.30)$$

$$\cos \theta_j = \hat{p}_\nu \cdot \hat{p}_j, \quad (5.31)$$

2373 and the deviation from the momentum conservation plane as:

$$\sin \theta_{plane} = \left| \frac{\hat{p}_\mu \times \hat{p}_\nu}{|\hat{p}_\mu \times \hat{p}_\nu|} \cdot \hat{p}_j \right|. \quad (5.32)$$

2374 In Fig. 5.11 I show some distributions of these quantities for the case of the $b\bar{b}$ sample
 2375 with $m_{DM} = 10$ GeV (blue histograms) and for the atmospheric backgrounds (red).
 2376 In order to select the atmospheric events I followed the same criteria as for the signal
 2377 events. However, because in the signal case I used the true direction of the neutrino
 2378 as input, as it should be that of the Sun at that time and therefore known, in the
 2379 atmospheric case I used a set of solar positions as our ansatz for the neutrino direction.
 2380 From the distributions, one can see that the muon and the jet for the signal events are
 2381 predominantly forward and also that the deviations from the momentum conservation

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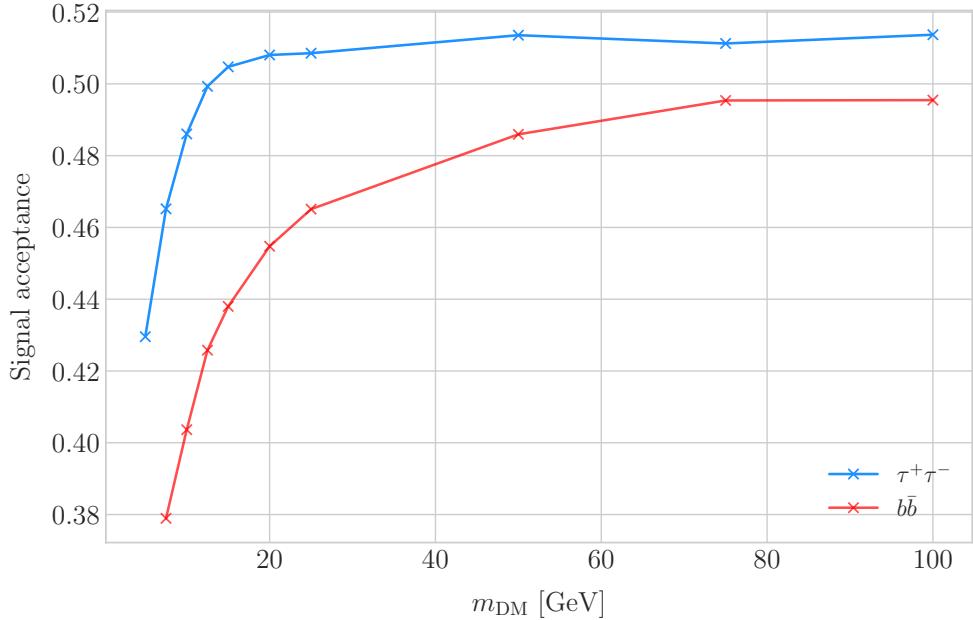


Figure 5.13: Signal efficiencies for the $\tau^+\tau^-$ (blue line) and $b\bar{b}$ (red line) DIS samples as functions of the DM mass, m_{DM} , obtained by applying the optimal angular cuts $\theta_\mu < 27^\circ$, $4^\circ < \theta_j < 26^\circ$ and $\theta_{\text{plane}} < 3.5^\circ$.

2382 plane are peaked at zero, as one should expect.

2383 Now, I can start applying cuts to maximise our signal selection efficiency while at
 2384 the same time I try to minimise the amount of atmospheric background events passing
 2385 the selection. To this end, I will need to find some lower and upper cuts for θ_j and
 2386 θ_μ and an upper bound for θ_{plane} . In Fig. 5.12 I show how upper bound cuts in the
 2387 different angular variables affect the signal efficiency (blue lines) and the background
 2388 rejection (red lines). Notice that the signal efficiency behaves in a quite different way
 2389 when I apply cuts in the jet and the muon angles. On the contrary, the cuts on both
 2390 variables have a similar effect on the background rejection.

2391 In order to obtain the optimal set of cuts, I perform a multidimensional scan. I
 2392 do this separately for the $\tau^+\tau^-$ and the $b\bar{b}$ samples. For each case, I scan the possible
 2393 cuts for each mass point and then I take the mean value of the signal efficiency for
 2394 each configuration, to get the mean efficiency for each set of cuts. I do a similar scan
 2395 for the atmospheric sample independently. Then, I take the sets of cuts such that
 2396 the background rejection achieved is greater than 99.8% and search for the one which

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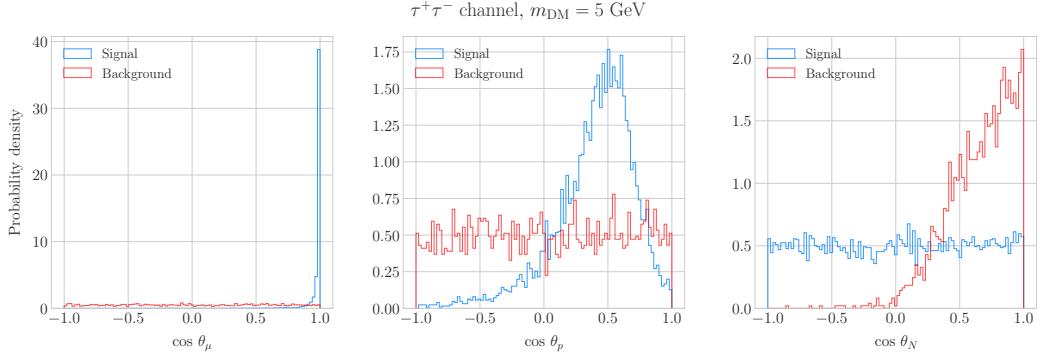


Figure 5.14: Distributions of $\cos \theta_\mu$ (left panel), $\cos \theta_p$ (central panel) and $\cos \theta_N$ (right panel) for the $\tau^+\tau^-$ QEL sample with $m_{\text{DM}} = 5 \text{ GeV}$ (blue) and the atmospheric background (red).

2397 maximises the $\tau^+\tau^-$ and $b\bar{b}$ sample mean efficiencies. I found that with the cuts $\theta_\mu < 27^\circ$,
 2398 $4^\circ < \theta_j < 26^\circ$ and $\theta_{\text{plane}} < 3.5^\circ$ I get a background rejection of 99.80% while achieving
 2399 a 49.40% and 44.92% mean signal efficiencies for the $\tau^+\tau^-$ and $b\bar{b}$ signals respectively.

2400 In Fig. 5.13 I show the signal efficiencies as a function of the DM mass for the $\tau^+\tau^-$
 2401 (blue line) and the $b\bar{b}$ (red line) DIS events, after applying the cuts discussed above, as
 2402 well as the energy threshold and hadronic visible energy selections. One can see that
 2403 the efficiency grows with the mass, as annihilations of more massive DM particles will
 2404 produce a neutrino spectrum centered at higher energies, where DIS events dominate.
 2405 Notice also that the efficiency is higher for the $\tau^+\tau^-$ case at every mass point, as in
 2406 general this channel produces neutrinos at higher energies than the corresponding $b\bar{b}$
 2407 channel.

2408 5.5.2 Single proton QEL events

2409 Now, one can try to explore the low energy tail of the neutrino energy distributions. This
 2410 regime is dominated by the QEL interactions, i.e. events of the type $\nu_\mu + n \rightarrow \mu^- + p$.
 2411 In this case, as the typical energies are $E_\nu \lesssim 1 \text{ GeV}$, the momentum transfer to the
 2412 remnant nucleus is sizeable. Therefore, I can not make the approximation I did before
 2413 and assume that the momentum of the muon and the proton will give an adequate
 2414 estimation of the reconstructed neutrino energy.

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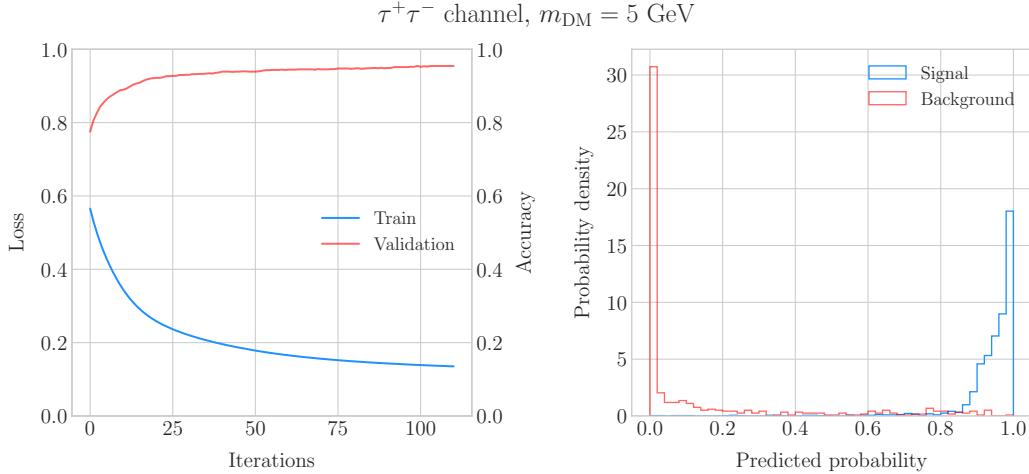


Figure 5.15: Left panel: value of the loss function for the training sample (blue line) and accuracy for the validation sample (red line) versus the number of iterations for the MLP classifier training. Right panel: distributions of the predicted probabilities assigned by the MLP classifier to the test sample for the $\tau^+\tau^-$ QEL signal with $m_{\text{DM}} = 5 \text{ GeV}$ (blue) and the atmospheric background (red).

2415 In any case, as before, I can take the direction of the incoming neutrino as known.

2416 That way, one can estimate the energy of the neutrino as:

$$E_\nu^{reco} = E_\mu + E_p + m_{^{39}\text{Ar}} - m_{^{40}\text{Ar}}, \quad (5.33)$$

2417 and using momentum conservation I can write the momentum of the remnant nucleus

2418 as:

$$\vec{p}_N = \hat{p}_\nu (E_\mu + E_p + m_{^{39}\text{Ar}} - m_{^{40}\text{Ar}}) - \vec{p}_\mu - \vec{p}_p. \quad (5.34)$$

2419 As in the previous case, I need to drop the events where the muon or the proton fall
 2420 below the kinetic energy detection threshold [85]. Also, I again apply a smearing to the
 2421 momenta of the particles, a 1% for muons and 5% for protons.

2422 Having done that, one can compute the following angular variables for our selected
 2423 events:

$$\cos \theta_\mu = \hat{p}_\nu \cdot \hat{p}_\mu, \quad (5.35)$$

$$\cos \theta_p = \hat{p}_\nu \cdot \hat{p}_p, \quad (5.36)$$

5.5. HIGH ENERGY DM NEUTRINO SIGNALS

$$\cos \theta_N = \hat{p}_\nu \cdot \hat{p}_N. \quad (5.37)$$

2424 Fig. 5.14 shows the distributions of these angular variables for the $\tau^+\tau^-$ QEL
 2425 sample with $m_{\text{DM}} = 5$ GeV (blue) and the atmospheric background (red). Again, for
 2426 the atmospheric events I used a random solar position as the ansatz for the incoming
 2427 neutrino direction. Notice that now, opposed to the DIS case where the signal had very
 2428 sharp distributions for the variables considered, the shapes of the angular distributions
 2429 for signal and background are not that much different.

2430 This effectively means that the usual approach of applying simple angular cuts would
 2431 not work as well as in the previous situation. Therefore, as a possible solution, I tried to
 2432 use a multilayer perceptron (MLP) classifier to separate between signal and background
 2433 events. Thus, the power of the hypothesis test will serve as an estimate of the signal
 2434 efficiency, and in the same way one can take the size of the test to be our background
 2435 rejection.

2436 For each DM mass value and channel, as well as for the background sample, I divide
 2437 our events into training, validation and test samples. The input variables for the classifier
 2438 were the reconstructed neutrino energy from Eq. (5.33) and the angular variables defined
 2439 in Eqs. (5.35 - 5.37). I used the MLP classifier implemented in `scikit-learn` [139], with
 2440 a total of five hidden layers, the rectified linear unit activation function and adaptive
 2441 learning rate. In order to account for fluctuations due to artifacts in the training process I
 2442 repeated the training a thousand times for each sample, redefining each time the training,
 2443 validation and test subsets, so one can take as our signal efficiency and background
 2444 rejection the mean values of the powers and sizes of the tests.

2445 The results of one of these training processes for the $\tau^+\tau^-$ QEL signal with $m_{\text{DM}} =$
 2446 5 GeV is shown in Fig. 5.15. On the left panel I show the loss function values (blue) and
 2447 accuracy (red) at each iteration for the training and the validation samples respectively.
 2448 The training stops either when the maximum number of iterations is reached (1000 in
 2449 this case) or when the accuracy for the validation sample reaches a certain tolerance
 2450 (I chose 10^{-4} as our tolerance). On the right panel I have the distributions for the

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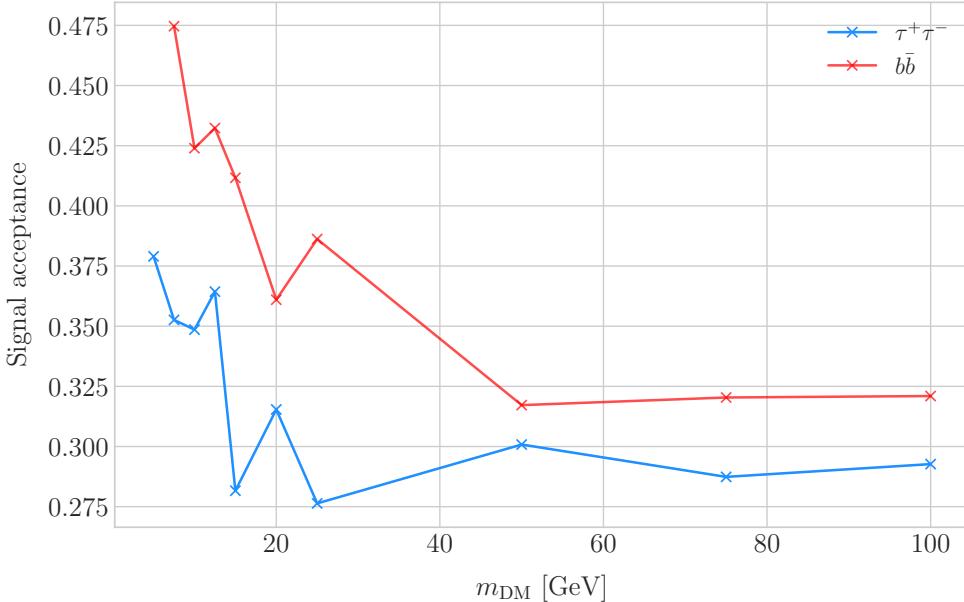


Figure 5.16: Signal efficiencies for the $\tau^+\tau^-$ (blue line) and $b\bar{b}$ (red line) single proton QEL samples as functions of the DM mass, m_{DM} , obtained by requiring a minimum predicted probability from the MLP classifier of 0.97 in order to achieve a background rejection greater than 99.8%.

predicted probability by the model, separated in true signal (blue) and background (red) events, for the test sample. One can see that both populations are well separated, obtaining a power of 44.97% and a size of 0.17% when I require a predicted probability greater than 0.97.

Applying this criteria for each sample, I obtain the mean signal efficiencies shown in Fig. 5.16. Notice that the efficiencies for the channel $\tau^+\tau^-$ (blue line) are consistently lower than the ones for the $b\bar{b}$ channel (red line). This can be due to the fact that, for each DM mass point, the neutrino spectrum coming from the $b\bar{b}$ annihilation channel is centered at lower energies when compared to the $\tau^+\tau^-$ spectrum. This directly translates into more low energy neutrinos undergoing QEL interactions, which give signals that can be easily separated from the atmospheric background. This explanation also help us understand why in both cases the signal acceptance drops when the DM mass increases. In all cases, the background rejection took values between 99.8% to 99.9%. I will assume a 99.8% background rejection value in all cases to keep our estimation conservative.

5.5. HIGH ENERGY DM NEUTRINO SIGNALS

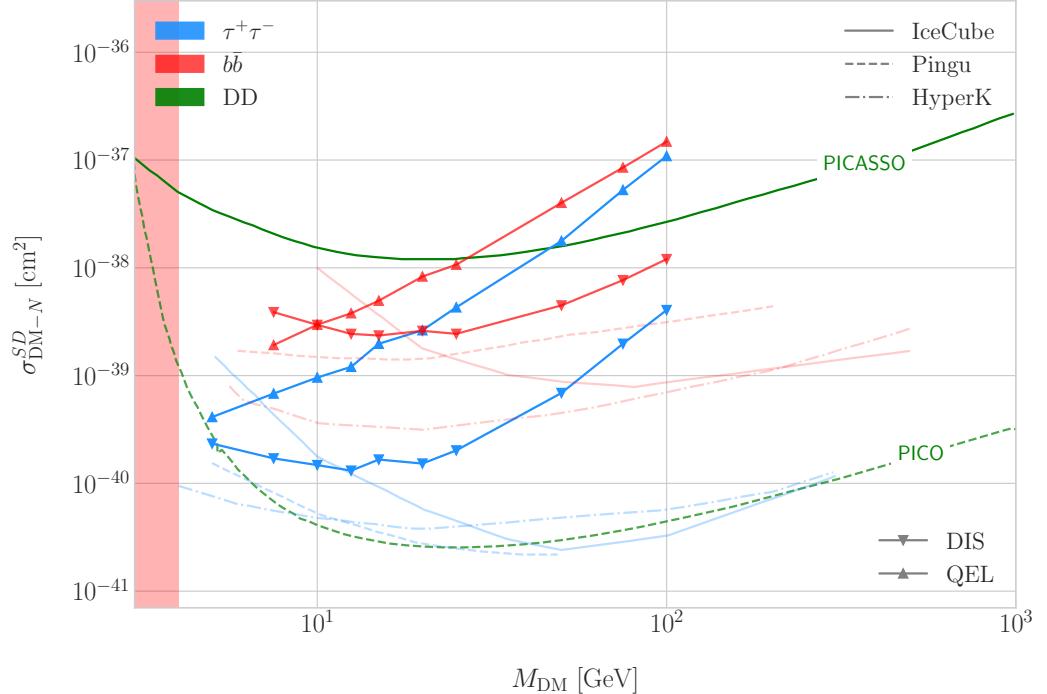


Figure 5.17: Projected 90% confidence level upper limit for DUNE (400 kT yr) on the spin-dependent DM-nucleon scattering cross section as a function of m_{DM} , for the annihilation channels $\tau^+\tau^-$ (blue) and $b\bar{b}$ (red) separated by interaction type (up triangles denote DIS interactions whereas down triangles represent QEL interactions). I also show the previous limits from IceCube [7] (solid lines) and the projected sensitivities for Pingu [8] (dashed lines) and Hyper-Kamiokande [9] (dash-dotted lines), as well as the direct detection limits from PICASSO [10] (solid green line) and PICO-60 C₃F₈ [11] (dashed green line).

2465 5.5.3 Results

2466 In order to estimate the DM-nucleon cross section sensitivities in the present case I need
 2467 again to compute the expected number of background events. As I am now separating
 2468 events by interaction type Eq. (5.25) does not hold anymore, as in that case I integrated
 2469 over the total neutrino-argon cross section. In this instance, the expected background
 2470 events for DIS events is approximately given by:

$$N_B^{DIS} \simeq \eta_B^{DIS} \times (4.655 \times 10^3) \times \left(\frac{\text{exposure}}{400 \text{ kT yr}} \right), \quad (5.38)$$

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2471 whereas for QEL events we have:

$$N_B^{QEL} \simeq \eta_B^{QEL} \times (2.248 \times 10^4) \times \left(\frac{\text{exposure}}{400 \text{ kT yr}} \right). \quad (5.39)$$

2472 Now, using these together with Eqs. (5.26) and (5.27) one can obtain the 90% C.L.
2473 upper limit on the total annihilation rate at equilibrium for both kind of events. Then,
2474 applying the computed DM-nucleons capture rates I can translate these into limits on
2475 the DM-nucleon cross section by means of Eqs. (5.2), (5.5) and (5.6).

2476 Fig. 5.17 shows the obtained limits on the SD DM-nucleon cross section for DUNE,
2477 using the DIS (up triangles) and QEL (down triangles) events both for the $\tau^+\tau^-$ (blue)
2478 and the $b\bar{b}$ (red) samples, for an exposure of 400 kT yr. I also include the corresponding
2479 current limits from IceCube [7] (solid lines), as well as the projected sensitivities of
2480 Pingu [8] (dashed lines) and Hyper-Kamiokande [9] (dash-dotted lines). For comparison,
2481 I also show the reported direct detection limits from PICASSO [10] (solid green line)
2482 and PICO-60 C_3F_8 [11] (dashed green line).

2483 Notice that, for most of the mass range, the limits one can set by using the DIS
2484 events are stronger than those of the QEL interactions, except for the low mass part
2485 of both the $\tau^+\tau^-$ and the $b\bar{b}$ curves where the QEL events dominate. In general, the
2486 expected sensitivity of DUNE for DM masses $\lesssim 25$ GeV surpasses the stronger current
2487 indirect limits. However, experiments like Hyper-Kamiokande are foreseen to have an
2488 overall better sensitivity in this kind of searches, as they have a bigger active volume
2489 and accept a broader energy range.

2490 A pending question is what happens when we add the RES and MEC charged-current
2491 interaction contributions. In that case it would probably be more convenient to split
2492 the samples by final state interaction topologies. Also, another necessary improvement
2493 would be adding a full detector simulation and reconstructions. This will also require
2494 considering the effect of poorly reconstructed events or final states containing neutral
2495 particles such that they mimic the desired topology at the reconstruction level.

5.6. EXAMPLE: LEPTOPHILIC DARK MATTER

2496 5.6 Example: Leptophilic Dark Matter

2497 In general, the capture rate of DM particles by the Sun via interactions with electrons is
2498 several orders of magnitude smaller than the capture via DM-nucleus scattering. Thus,
2499 it would be sub-leading even when nucleon capture is loop suppressed. As I showed in
2500 Fig. 5.2, the capture rate via scattering off electrons only surpasses the capture rates
2501 via DM-nucleons interactions for DM masses $\lesssim 100 - 500$ MeV.

2502 However, if one considers a model where DM-nucleon interactions are forbidden even
2503 at loop level, then electron interactions will be the sole contributor to DM capture in
2504 the Sun. One can describe such scenario where the DM particles couple to leptons but
2505 not to the quark sector using effective operators.

2506 In general, assuming that the DM particle is a Dirac fermion, the dimension six
2507 operators describing the interaction between two DM particles and two leptons can be
2508 written as:

$$\mathcal{L}_{eff} = G \sum_i (\bar{\chi} \Gamma^i \chi) (\bar{\ell} \Gamma^i \ell), \quad (5.40)$$

2509 where $G = 1/\Lambda^2$ is the effective coupling strength, Λ the cut-off of the effective field
2510 theory and ℓ denotes any lepton. In principle, one should consider all the possible
2511 Lorentz structures Γ_f^i in order to have a complete set of effective operators.

2512 However, some combinations will induce interactions with nucleons at loop level.
2513 As we are specifically interested in interactions which forbid any communication with
2514 the quark sector, I will not consider those [140]. In addition, some of the effective
2515 operators give rise to velocity-suppressed scattering cross sections between DM particles
2516 and leptons. I will also neglect those, as the suppression goes with the square of the DM
2517 halo velocity which in units of the speed of light is $\sim 10^{-6}$.

2518 This way, the only Lorentz tensor structure that do not induce interactions with
2519 quarks at loop level and gives a contribution to the scattering cross section that is not
2520 velocity suppress is the axial-axial interaction. The effective Lagrangian is then given

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2521 by:

$$\mathcal{L}_{eff} = \frac{c_A^\chi c_A^\ell}{\Lambda^2} (\bar{\chi} \gamma^\mu \gamma^5 \chi) (\bar{\ell} \gamma_\mu \gamma^5 \ell), \quad (5.41)$$

2522 where c_A^χ and c_A^ℓ are the couplings for the different species. As the DM coupling appears
 2523 as a common factor for any lepton choice, I will redefine the corresponding coupling c_A^ℓ
 2524 to absorb c_A^χ . Also, for simplicity, I will assume that the couplings between the DM
 2525 particles and the leptons are flavour independent, i.e. I have just two couplings, c_A^e for
 2526 charged leptons and c_A^v for neutrinos.

2527 In the case of a scalar DM particle, the lowest order effective interaction with
 2528 leptons happens through a dimension five operator, generating scalar and pseudoscalar
 2529 interactions. However, the former induces interactions with quarks at two loop level
 2530 whereas the latter gives a velocity suppressed scattering cross section.

2531 From the effective Lagrangian in Eq. (5.41) it can be shown that the axial-axial
 2532 contribution to the scattering cross section for the fermionic DM and a charged lepton
 2533 is given by:

$$\sigma_{DM-e}^{AA} = 3 (c_A^e)^2 \frac{m_e^2}{\pi \Lambda^4}. \quad (5.42)$$

2534 If the DM interacts exclusively with fermions, then the only annihilation channels
 2535 that will give us a measurable neutrino flux coming out of the Sun are $\tau^+ \tau^-$ and $\nu \bar{\nu}$. The
 2536 former channel, already explored previously in the more mainstream scenario of the DM
 2537 capture via scattering off nucleons, is open only for $m_{DM} > m_\tau \simeq 1776.86 \pm 0.12$ MeV
 2538 [141], a mass region where the solar DM capture by electrons is at least one order of
 2539 magnitude smaller than the capture via interactions with nucleons. On the contrary, the
 2540 latter allows us to explore a region where the capture rate via scattering off electrons
 2541 dominates over the rest.

2542 One downside of focusing in such low mass range is that it falls below the usual
 2543 limit of $m_{evap} \sim 4$ GeV usually explored in the literature. The pretext to explore this
 2544 region is the result discussed previously reported in Ref. [2], where DM evaporation in
 2545 the Sun for the case of capture via electron scattering could be negligible for masses
 2546 as low as $m_{evap} \sim 200$ MeV. This result is quite sensitive to the high velocity tail of

5.6. EXAMPLE: LEPTOPHILIC DARK MATTER

2547 the DM velocity distribution in equilibrium inside the Sun, and therefore full numerical
 2548 simulations would be needed to asses the impact of this effect. However, this falls out of
 2549 the scope of our work.

2550 In this case, as I have an specific realisation of the interaction between the DM
 2551 and leptons, one can estimate the relic density of our DM for different values of the
 2552 couplings and the effective field theory scale Λ . The first step to do so is compute the
 2553 self-annihilation cross section. Because I consider cold relics, at the freeze-out time our
 2554 DM particles were non-relativistic and so one can expand the annihilation cross section
 2555 in terms of the relative velocity v between two annihilating DM particles as [142]:

$$\sigma_{ann}^{AA}|v| \approx \frac{1}{2\pi\Lambda^4} \sum_{\ell} \left(c_A^{\ell}\right)^2 m_{\chi}^2 \sqrt{1 - \frac{m_{\ell}^2}{m_{\chi}^2} \left[\frac{m_{\ell}^2}{m_{\chi}^2} + \frac{1}{12} \left(2 - \frac{m_{\ell}^2}{m_{\chi}^2}\right) v^2 \right]}, \quad (5.43)$$

2556 where the sum includes all the possible lepton final states with mass m_{ℓ} .

2557 Solving the Boltzmann equation for the evolution of the DM density gives as a
 2558 solution a relic density of:

$$\Omega_{\chi} h^2 \approx \frac{(1.04 \times 10^9) x_F}{M_{Pl} \sqrt{g_*} (a + 3b/x_F)}, \quad (5.44)$$

2559 where $x_F = m_{\chi}/T_F$ being T_F the freeze-out temperature, g_* the number of relativistic
 2560 degrees of freedom at freeze-out and a and b the terms in the annihilation cross section
 2561 expansion $\sigma_{ann}|v| \approx a + bv^2 + \mathcal{O}(v^4)$. Using the current best fit for the relic DM density
 2562 $\Omega_{\chi} h^2 = 0.1198 \pm 0.0012$ [143] one can use these relations to compute the required
 2563 effective theory scale Λ at which the correct density is achieved for any combinations of
 2564 m_{χ} and c_A^{ℓ} .

2565 As discussed before, in the low DM mass region QEL interactions dominate. Moreover,
 2566 if I focus on direct annihilation to neutrinos, the energy of the muon neutrino flux is
 2567 known as it must be equal to the mass of the DM particle, $E_{\nu} = m_{\chi}$. That way, now
 2568 I do not need to use Eq. (5.33) in order to estimate the momentum transfer to the

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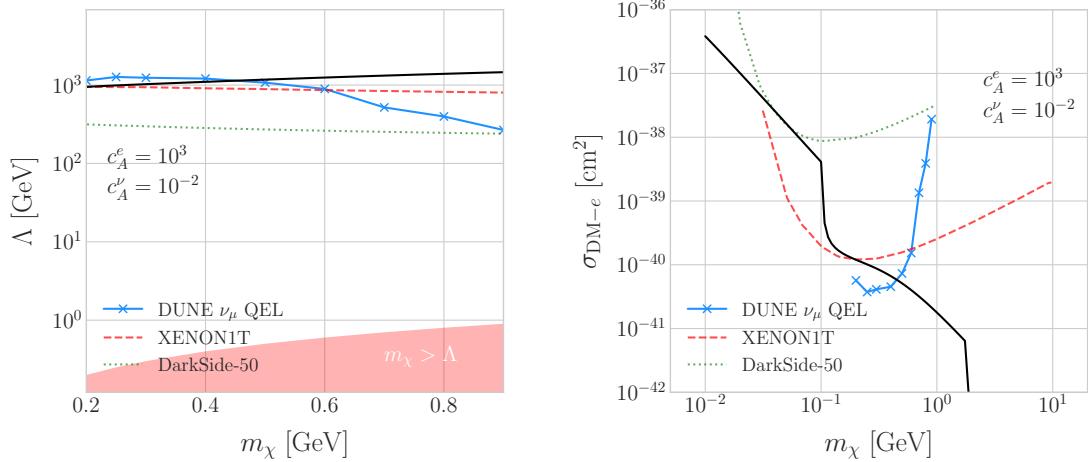


Figure 5.18: Left panel: Projected 90% confidence level sensitivity of DUNE (400 kT yr) to the scale Λ of an EFT containing only leptophilic DM axial-axial interactions (blue line). Right panel: . In both cases the corresponding limits from DarkSide-50 [12] (dotted green line) and XENON1T [13] (dashed red line) are also shown, together with the configurations for which the correct relic density is achieved (black line), all for the coupling values $c_A^e = 10^3$ and $c_A^\nu = 10^{-2}$.

2569 remnant nucleus, I can simply take:

$$\vec{p}_N = \hat{p}_\nu m_\chi - \vec{p}_\mu - \vec{p}_p. \quad (5.45)$$

2570 To estimate the signal efficiency and background rejection for this case I used again
 2571 the MLP classifier from `scikit-learn`, using the same specifications as before. The
 2572 only difference now is that I add also the reconstructed neutrino energy as one of the
 2573 features to train the classifier with, because the characteristic monoenergetic flux for
 2574 each m_χ value will help to distinguish between signal and background events.

2575 In this case, for masses below ~ 500 MeV I obtain a signal efficiency close to unity
 2576 while keeping a background rejection of 99.9%. For bigger values of the mass, the signal
 2577 efficiency drops significantly if I require to keep the background acceptance under 0.01%.
 2578 However, because this kind of search is dominated by the background, sacrificing the
 2579 signal acceptance to keep the background rejection to a minimum enhances the reach
 2580 of the analysis. This way, for DM masses of the order of $m_\chi \sim 1$ GeV I end up with
 2581 efficiencies as low as 1%.

5.7. SYSTEMATIC UNCERTAINTIES

Now, estimating the number of background events using Eq. (5.39) one can go on and apply Eqs. (5.26) and (5.27) together with Eq. (5.42) to derive the sensitivity of DUNE to this kind of model. Fig. 5.18 (left panel) shows the potential reach of DUNE to constrain the EFT scale Λ this model containing only leptophilic DM axial-axial interactions (blue line), for a choice of couplings $c_A^e = 10^3$ and $c_A^\nu = 10^{-2}$. I also included the current limits on the DM-electron scattering cross section from DarkSide-50 [12] (dotted green line) and XENON1T [13] (dashed red line), reworked with Eq. (5.42) to show their implications for the EFT scale. The values of Λ for which the correct DM relic density value is achieved for each mass are also shown (black line). This tells us that, for that specific choice of couplings, DUNE would be sensitive to DM configurations allowed by the relic density constraint up to a mass of $m_\chi \sim 400$ MeV.

In Fig. 5.18 (right panel) I show the same upper limits but for the DM-electron scattering cross section. From this view one can see that DUNE would be able to offer complementary information to the low energy DM-electron interaction searches performed by direct detection experiments, in a slightly higher mass range.

With the present example, although it focuses on a very specific realisation of the DM interactions, I show the potential of DUNE to constrain exotic DM scenarios. Thanks to its low backgrounds and superb angular resolution DUNE will be able to help with the systematic searches for dark sectors physics.

5.7 Systematic uncertainties

The estimation of the DM cross sections using neutrinos from WIMP annihilations inside the Sun is affected by systematic uncertainties from different sources. Surely, the atmospheric background estimation is also affected by systematic uncertainties. There are uncertainties common to both types of events, as well as others specific to each. In this section, I try to provide a comprehensive summary of the main sources of uncertainty for this analysis, which should be taken into account in any future extensions of the same.

CHAPTER 5. DM SEARCHES WITH NEUTRINOS FROM THE SUN

Table 5.1: Systematic uncertainties for the solar WIMP signal events. Table adapted from Ref. [144].

Systematic	Value
Form factor	Does not apply to SD [145]
Solar model	3% [145]
Local DM density	Not relevant for relative interpretations [145, 146]
Dynamics of solar system	Negligible [147]
Velocity distributions	20% at 20 GeV [145, 146]
Oscillation parameters	8% for $\tau^+\tau^-$, 5% for $b\bar{b}$ [148]
Neutrino interactions in the Sun	10%
Matter effects in the Earth	10%

2609 5.7.1 Systematic uncertainties in the solar WIMP signal

2610 The systematic uncertainties affecting the solar WIMP neutrino signal can be divided in
 2611 two categories. On the one hand, we have those affecting the solar WIMP annihilation
 2612 rate. On the other hand, there are the ones which modify the neutrino flux resulting
 2613 from the annihilations reaching our detector.

2614 • **Uncertainties on the annihilation rate.** These include the astrophysical effects
 2615 that affect the normalisation of the solar DM neutrino flux. The main contributions
 2616 are the solar model choice, the form factor uncertainties (only for SI searches), the
 2617 gravitational effect of other planets, the local DM density (not relevant for relative
 2618 comparisons, as it affects direct detection experiments in the same way), and the
 2619 DM halo and dispersion velocities.

2620 • **Uncertainties on the neutrino flux.** These are related to the oscillation effects,
 2621 as well as the absorption and regeneration of neutrinos in the Sun. Matter effects
 2622 inside the Earth also affect the neutrino flux the measured at the detectors.

2623 Table 5.1 summarises the contributions of the different sources of uncertainty for the
 2624 signal events. These are the signal systematic uncertainties that have been taken into
 2625 account in previous solar DM searches with neutrinos [144, 146, 148].

5.7. SYSTEMATIC UNCERTAINTIES

Table 5.2: Systematic uncertainties for the solar WIMP atmospheric background events. Table adapted from Ref. [51].

Systematic	Value
Flux normalisation	25 – 7% for $0.1 < E_\nu \leq 1$ GeV (linear in $\log E_\nu$) 7% up to 10 GeV
$(\nu_\mu + \bar{\nu}_\mu)/(\nu_e + \bar{\nu}_e)$	2% for $E_\nu \leq 1$ GeV 3% for $1 < E_\nu \leq 10$ GeV
$\bar{\nu}_\mu/\nu_\mu$	2% for $E_\nu \leq 1$ GeV 6% for $1 < E_\nu \leq 10$ GeV
K/ π ratio	5% $E_\nu \leq 100$ GeV

2626 5.7.2 Systematic uncertainties in the atmospheric background

2627 For the atmospheric background events, one needs to take into account the systematic
2628 uncertainties affecting the atmospheric ν_μ flux. These have been extensively studied
2629 in the context of atmospheric neutrino oscillation measurements. Among these, the
2630 energy-dependent flux normalisation uncertainty is the in the low energy regime. Other
2631 important contributions to the uncertainty come from the ratios between the muon to
2632 electron neutrino and the muon to anti-muon neutrino components of the flux. Additional
2633 uncertainty is introduced by the errors in the pion and kaon production rates calculated
2634 for the hadronic interactions of cosmic rays in the atmosphere [149].

2635 Table 5.2 shows a summary of the leading contributions to the uncertainty on the
2636 atmospheric muon neutrino flux, in the energy range relevant for this analysis.

2637 5.7.3 Common systematic uncertainties

2638 Finally, there are sources of uncertainty common to both signal and backgrounds. These
2639 have two different origins:

- 2640** • **Uncertainties on the neutrino cross section.** These are introduced by the
2641 modelling of the neutrino-nucleus interactions. In the context of the solar WIMP
2642 analysis, these have been estimated to be 10% for DM masses around 10 GeV
2643 [148].

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- **Uncertainties related to the detector.** They affect the measurement of the neutrino interaction and the final state particles produced. The main detector uncertainties relevant to this analysis are those of the energy and angular resolutions of the DUNE FD. Other effects, like the timing and triggering efficiencies, will also contribute to the uncertainties. The particular values these will take for this analysis need to be worked out in the context of DUNE.

2650

2651

Particle ID in ND-GAr

2652 ND-GAr is a magnetised, high-pressure gaseous argon TPC (HPgTPC), surrounded by
2653 an electromagnetic calorimeter (ECal) and a muon detector (commonly refer to as μ ID).
2654 A detailed discussion on the requirements, design, performance and physics of ND-GAr
2655 can be found in the DUNE ND CDR [91] and the ND-GAr whitepaper (cite).

2656 In DUNE Phase II ND-GAr will fulfill the role of TMS, measuring the momentum
2657 and sign of the charged particles exiting ND-LAr. Additionally, it will be able to measure
2658 neutrino interactions inside the HPgTPC, achieving lower energy thresholds than those
2659 of the ND and FD LArTPCs. By doing so ND-GAr will allow to constrain the relevant
2660 systematic uncertainties for the LBL analysis even further.

2661 The goal of the present chapter is to review the requirements that the physics program
2662 of DUNE impose on ND-GAr, present the current status of its design and describe the
2663 GArSoft package, its simulation and reconstruction software.

2664 As decided during the DUNE Phase II workshop in June 2023 [reference], we want
2665 to build ND-GAr physics case by showing:

- 2666 • That ND-GAr can constrain systematic uncertainties that ND-LAr might miss.
- 2667 • The impact on the neutrino oscillation results if such systematic uncertainties are
2668 missed.
- 2669 • That ND-GAr is necessary to reach DUNE's main physics goals.

2670 This way, the design of ND-GAr will be physics driven.

CHAPTER 6. PARTICLE ID IN ND-GAr

2671 In order to study the effects of final state interactions (FSI) in CC interactions,
2672 ND-GAr should be able to measure the spectrum of protons and charged pions at low
2673 energies. ND-GAr also needs to be able to measure the pion multiplicity, specially for
2674 energies above 100 MeV as at these energies the pions shower in the LAr, to inform the
2675 pion mass correction in the ND and FD LArTPCs.

2676 In order to correctly identify electrons, muons, pions, kaons and protons ND-GAr
2677 can use a combination of: dE/dx measurements in the HPgTPC, E_{ECAL}/p using the
2678 ECAL total energy and the momentum obtained from magnetic spectroscopy in the
2679 HPgTPC and penetration information through the ECAL and muon tagger.

2680 6.1 GArSoft

2681 GArSoft is a software package developed for the simulation and reconstruction of events
2682 in ND-GAr. It is inspired by the LArSoft toolkit used for the simulation of LArTPC
2683 experiments, like the DUNE FD modules. It is based on `art`, the framework for event
2684 processing in particle physics experiments [150]. Other of its main dependencies are
2685 `ROOT`, `NuTools`, `GENIE` and `Geant4`. It allows the user to run all the steps of a generation-
2686 simulation-reconstruction workflow using FHiCL configuration files.

2687 6.1.1 Event generation

2688 The standard generator FHiCLs in GArSoft run the event generation and particle
2689 propagation simulation (i.e. Geant4) in the same job by default. However, it is possible
2690 to split them up if needed. The current version of GArSoft provides five different event
2691 generators, each of them producing `simb::MCTruth` products defined in `NuTools`. The
2692 available modules are:

- 2693 • **SingleGen**: particle gun generator. It produces the specified particles with a given
2694 distribution of momenta, initial positions and angles.
- 2695 • **TextGen**: text file generator. The input file must follow the `hepevt` format¹, the

¹In brief, each event contains at least two lines. The first line contains two entries, the event number

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2696 module simply copies this to `simb::MCTruth` data products.

2697 • **GENIEGen**: GENIE neutrino event generator. The module runs the neutrino-nucleus
2698 interaction generator using the options specified in the driver FHiCL file (flux file,
2699 flavour composition, number of interactions per event, t_0 distribution, ...). Current
2700 default version is v3_04_00.

2701 • **RadioGen**: radiological generator. It produces a set list of particles to model
2702 radiological decays. Not tested.

2703 • **CRYGen**: cosmic ray generator. The module runs the CRY event generator with a
2704 configuration specified in the FHiCL file (latitude and altitude of detector, energy
2705 threshold, ...). Not tested.

2706 The module **GArG4** searches for all the generated `simb::MCTruth` data products, using
2707 them as inputs to the Geant4 simulation with the specified detector geometry. A constant
2708 0.5 T magnetic field along the drift coordinate is assumed. The main outputs of this step
2709 are `simb::MCParticle` objects for the generated Geant4 particles, `gar::EnergyDeposit`
2710 data products for the energy deposits in the HPgTPC and `gar::CaloDeposit` data
2711 products for the energy deposits in the ECal and muon system.

2712 6.1.2 Detector simulation

2713 The standard detector simulation step in GArSoft is all run with a single FHiCL, but
2714 the different modules can be run independently as well. First the `IonizationReadout`
2715 module simulates the charge readout of the HPgTPC, and later the `SiPMReadout` module
2716 runs twice, once for the ECal and then for the muon system, with different configurations.

2717 The `IonizationAndScintillation` module collects all the `gar::EnergyDeposit`
2718 data products, to compute the equivalent number of ionization electrons for each energy

and the number of particles in the event. Each following line contains 15 entries to describe each particle. The entries are: status code, pdg code for the particle, entry of the first mother for this particle, entry of the second mother for this particle, entry of the first daughter for this particle, entry of the second daughter for this particle, x component of the particle momentum, y component of the particle momentum, z component of the particle momentum, energy of the particle, mass of the particle, x component of the particle initial position, y component of the particle initial position, z component of the particle initial position and time of the particle production.

CHAPTER 6. PARTICLE ID IN ND-GAr

deposit. The `ElectronDriftAlg` module simulates the electron diffusion numerically both in the longitudinal and transverse directions and applies an electron lifetime correction factor. The induced charge on the nearest and neighbouring readout pads is modeled using the provided pad response functions. The digitisation of the data is then simulated with the `TPCReadoutSimAlg` module. By default, the ADC sampling rate used is 50.505 MHz. The resulting raw waveforms for each channel are stored with zero-suppression, in order to save memory and CPU time. The algorithms keep blocks of ADC values above a certain threshold, plus some adjustable additional early and late tick counts. The results of these three steps are `gar::raw::RawDigit` data products.

For the ECal and the muon system the `SiPMReadout` module calls either the `ECALReadoutSimStandardAlg` or `MuIDReadoutSimStandardAlg` modules. These take all the `gar::CaloDeposit` data products in the corresponding detector and do the digitisation depending on whether the hit was in a tile or strip layer. They include single photon statistics, electronic noise, SiPM saturation and time smearing. The resulting objects are `gar::raw::CaloRawDigit` data products.

6.1.3 Reconstruction

The reconstruction in GArSoft is also run as a single job by default. It first runs the hit finding, clustering, track fitting and vertex identification in the HPgTPC, followed by the hit finding and clustering in the ECal and muon system. After those it produces the associations between the associations between the tracks and the ECal clusters.

Focusing first on the HPgTPC reconstruction, the `CompressedHitFinder` module takes the zero-suppressed ADCs from the `gar::raw::RawDigit` data products. The reconstructed hits largely correspond to the above threshold blocks, however the hit finder identifies waveforms with more than one maximum, diving them in multiple hits if they dip below a certain threshold. The data products produced are of the form `gar::rec::Hit`. These are the inputs to the clustering of hits in the `TPCHitCluster` module. Hits close in space and time are merged, and the resulting centroids are found. This module outputs `gar::rec::TPCClusters` objects and associations to the input

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2747 hits.

2748 The following step prior to the track fitting is pattern recognition. The module
2749 called `tpcvechitfinder2` uses the `gar::rec::TPCClusters` data products to find track
2750 segments, typically called vector hits. They are identified by performing linear 2D fits
2751 to the positions of the clusters in a 10 cm radius, one fit for each coordinate pair. A
2752 3D fit defines the line segment of the vector hit, using as independent variable the one
2753 whose sum of (absolute value) slopes in the 2D fits is the smallest. The clusters are
2754 merged to a given vector hit if they are less than 2 cm away from the line segment. The
2755 outputs are `gar::rec::VecHit` data products, as well as associations to the clusters. The
2756 `tpcpatrec2` module takes the `gar::rec::VecHit` objects to form the track candidates.
2757 The vector hits are merged together if their direction matches, their centers are within
2758 60 cm and their direction vectors point roughly to their respective centers. Once
2759 the clusters of vector hits are formed they are used to make a first estimation of the
2760 track parameters, simply taking three clusters along the track. The module produces
2761 `gar::rec::Track` data products and associations between these tracks and the clusters
2762 and vector hits.

2763 The track is fitted by means of a Kalman filter in the `tpctrackfit2` module, using
2764 the position along the drift direction as the independent variable. Two different fits are
2765 performed per track, a forward and a backwards fit, each starting from one of the track
2766 ends. The Kalman filter state vector ($y, z, R, \phi, \tan\lambda$) is estimated at each point along
2767 the track using a Bayesian update. The track parameters reported in the forward and
2768 backwards fits are the ones computed at the opposite end where the fit started. The
2769 main outputs of the track fit are the `gar::rec::Track` objects. Additionally, the module
2770 stores the fitted 3D positions along the track in the `gar::rec::TrackTrajectory` data
2771 products and the total charge and step sizes for each point also get stored in the form of
2772 `gar::rec::TrackIonization` objects.

2773 After the tracking step, the `vertexfinder1` module looks at the reconstructed
2774 `gar::rec::Track` products, creating vertex candidates with the track ends that are
2775 within 12 cm of each other. The vertices are then fitted using linear extrapolations from

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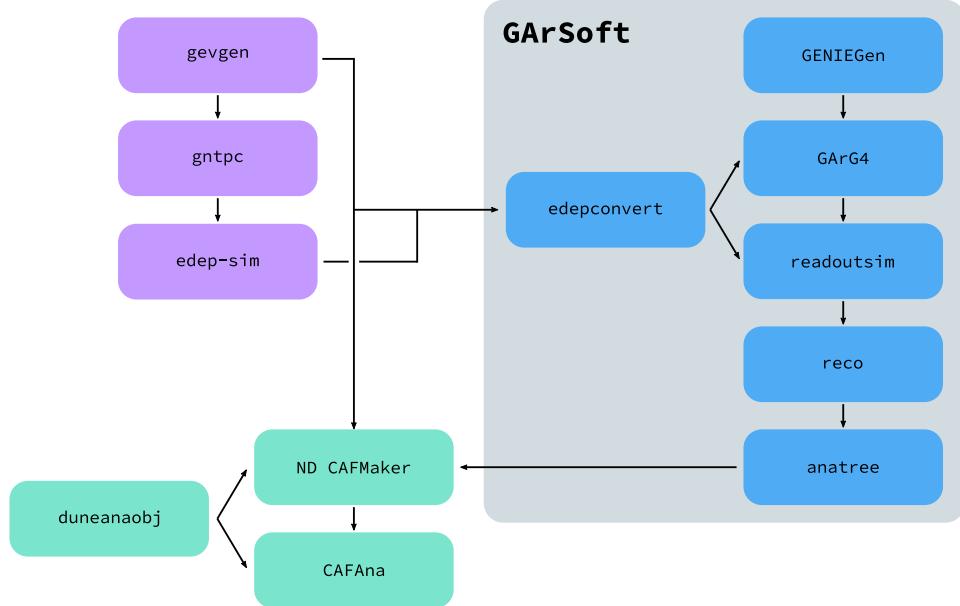


Figure 6.1: Schematic diagram showing the different modules involved in the ND-GAr production.

2776 the different track ends associated. The results are `gar::rec::Vertex` data products,
 2777 and associations to the tracks and corresponding track ends.

2778 For the ECal and muon tagger, the `SiPMHitFinder` module runs twice with different
 2779 configurations, adapted to the particular capabilities of both. The module simply takes
 2780 the `gar::raw::CaloRawDigit` products, applies a calibration factor to convert the ADC
 2781 counts to MeV and for the strip layer hits it calculates the position along the strip using
 2782 the times recorded of both SiPMs. This module produces `gar::rec::CaloHit` data
 2783 products. Next, these objects are used as inputs to the `CaloClustering` module. It
 2784 merges the hits based on a simple nearest neighbours (NN) algorithm. For the resulting
 2785 clusters it also computes the total energy and position of the centroid. The results are
 2786 stored as `gar::rec::Cluster` data products, with associations to the hits.

2787 The last step in the reconstruction is associating the reconstructed tracks in the
 2788 HPgTPC to the clusters formed in the ECal and muon system. The `TPCECALAssociation`
 2789 module checks first the position of the track end points, considering only the points
 2790 that are at least 215 cm away from the cathode or have a radial distance to the center

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2791 greater than 230 cm. The candidates are propagated up to the radial position, in the
2792 case of clusters in the barrel, or the drift coordinate position, for the end cap cluster, of
2793 the different clusters in the collection using the track parameters computed at the end
2794 point. The end point is associated to the cluster if certain proximity criteria are met.
2795 This module creates associations between the tracks, the end points and the clusters.
2796 The criteria for the associations are slightly different for the ECal and the muon tagger.

2797 6.2 dE/dx measurement in the TPC

2798 Among the parameters extracted from the track fitting, ionisation is particularly useful
2799 for particle identification, as it is a function of the particle velocity. Although for the
2800 case of relativistic particles this dependence is not very strong, measuring the track on
2801 a large number of points may allow us to estimate the amount of ionisation accuratel.
2802 This, paired with a measurement of the momentum, may allow us to identify the particle
2803 type.

2804 The first calculation of the energy loss per unit length of relativistic particles using a
2805 quantum-mechanical treatment is due to Bethe [151]. Using this approach, the mean
2806 ionisation rate of a charged particle traveling through a material medium is (using
2807 natural units $G = \hbar = c = 1$):

$$\left\langle \frac{dE}{dx} \right\rangle = \frac{4\pi Ne^4}{m_e \beta^2} z^2 \left(\log \frac{2m_e \beta^2 \gamma^2}{I} - \beta^2 \right), \quad (6.1)$$

2808 where N is the number density of electrons in the medium, e the elementary charge, m_e
2809 is the electron mass, z the charge of the particle in units of e , β is the velocity of the
2810 particle, $\gamma = (1 - \beta^2)^{-1}$ and I denotes the effective ionisation potential averaged over
2811 all electrons. This relation is known as the Bethe-Bloch formula.

2812 From Eq. (6.1) one can see that the ionisation loss does not depend explicitly on
2813 the mass of the charged particle, that for non-relativistic velocities it falls as β^{-2} , then
2814 goes through a minimum and increases as the logarithm of γ . This behaviour at high
2815 velocities is commonly known as the relativistic rise. The physical origin of this effect

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2816 is partly due to the fact that the transverse electromagnetic field of the particle is
2817 proportional to γ , therefore as it increases so does the cross section.

2818 It was later understood that the relativistic rise could not grow indefinitely with γ .
2819 A way to add this feature in the Bethe-Bloch formula is by introducing the so-called
2820 density effect term. It accounts for the polarisation effect of the atoms in the medium,
2821 which effectively shield the electromagnetic field of the charged particle halting any
2822 further increase of the energy loss [152]. Denoting the correction as $\delta(\beta)$, one can rewrite
2823 Eq. (6.1) as:

$$\left\langle \frac{dE}{dx} \right\rangle = \frac{4\pi Ne^4}{m_e \beta^2} z^2 \left(\log \frac{2m_e \beta^2 \gamma^2}{I} - \beta^2 - \frac{\delta(\beta)}{2} \right). \quad (6.2)$$

2824 In general, the form of $\delta(\beta)$ depends on the medium and its state of aggregation,
2825 involving the usage of tabulated parameters and implicit relations [153].

2826 Another standard method to compute the amount of ionisation a charged particle
2827 produces is the so-called photo-absorption ionisation (PAI) model proposed by Allison
2828 and Cobb [154]. Within their approach, the mean ionisation is evaluated using a
2829 semiclassical calculation in which one characterises the continuum material medium by
2830 means of a complex dielectric constant $\epsilon(k, \omega)$. However, in order to model the dielectric
2831 constant they rely on the quantum-mechanical picture of photon absorption and collision.
2832 Therefore, in the PAI model the computation of the ionisation loss involves a numerical
2833 integration of the measured photo-absorption cross-section for the relevant material.

2834 In a particle physics experiment, the typical way of determining the energy loss
2835 per unit length as a function of the particle velocity is studying identified particles
2836 over a range of momenta. Once we have established this relation we can use it for
2837 other, unknown particles. In this sense, it makes sense to have a regular mathematical
2838 expression for this relation that one can use.

2839 It happens that neither the Bethe-Bloch theory nor the PAI model from Allison and
2840 Cobb offer a close mathematical form for the ionisation curve. This is the reason why a
2841 full parametrisation of the ionisation curves can be useful. A parametrisation originally
2842 proposed for the ALEPH TPC [155] and later used by the ALICE TPC [156] group that

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2843 manages to capture the features of the ionisation energy loss is:

$$f(\beta\gamma) = \frac{P_1}{\beta^{P_4}} \left(P_2 - \beta^{P_4} - \log \left[P_3 + \frac{1}{(\beta\gamma)^{P_5}} \right] \right), \quad (6.3)$$

2844 where P_i are five free parameters. Hereafter, we will refer to Eq. (6.3) as the ALEPH
2845 dE/dx parametrisation.

2846 6.2.1 Energy calibration

2847 In order to obtain the amount of energy loss by a charged particle due to ionisation
2848 in our TPC we need to determine the conversion between the charge deposited in our
2849 readout planes and the actual energy depositions. This procedure is known as energy
2850 calibration.

2851 In a general, the first step of the calibration involves a non-uniformity correction,
2852 to make sure that the detector response is uniform throughout the TPC. These are
2853 typically divided into three categories, non-uniformities in the transverse YZ plane,
2854 non-uniformities along the drift direction X and variations of the detector response
2855 over time (would not apply to us as the detector is not built yet). These would correct
2856 for effects such as electron diffusion and attenuation, space charge effects or channel
2857 misconfiguration. However, because at the moment I am only interested in making sure
2858 we recover a sensible result from our simulation, I will not apply uniformity corrections
2859 to our charge deposits.

2860 Other effects, like electron-ion recombination or ADC saturation, lead to a non-linear
2861 relation between the observed charge and the deposited energy in the detector, with the
2862 observed readout charge saturating at high ionisation energies. In this case, because we
2863 are dealing with gaseous argon and therefore recombination is not as important as in
2864 liquid, we do not simulate recombination effects in the TPC. Even so, the simulation of
2865 the electronic response will still introduce charge saturation, and one needs to correct
2866 for it in order to obtain the exact amount of energy loss due to ionisation.

2867 By default, the track fitting algorithm in GArSoft provides a `TrackIonization`

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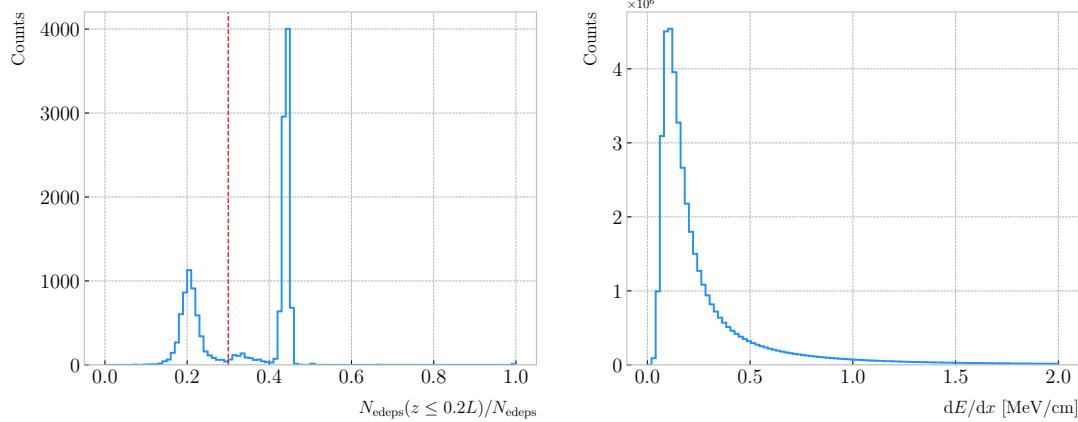


Figure 6.2: Left panel: distribution of the fraction of Geant4-level energy deposits per track with residual range less than 20% of the total track length, for the isotropic proton sample. Right panel: distribution of the ionisation per unit length of the energy deposits in the proton sample after removing the tracks with less than 30% of their energy deposits in the last 20% of the track.

object associated to each reconstructed track. It contains two collections of charge deposits, one for each fitting direction, consisting on pairs of charge values (dQ , in ADC) and step sizes (dx , in cm).

In order to estimate the ionisation loss in the ND-GAr TPC, I have used an MC sample consisting of single, isotropic protons propagating in the TPC. The starting points of the protons were sampled inside a $50 \times 50 \times 25$ cm box centered at $(100, -150, 1250)$, and their momenta are uniformly distributed in the range $0.25 - 1.75$ GeV. I ran the simulated sample through GArSoft's default detector simulation and reconstruction, and then a custom analyser module that extracts the ionisation data together with other reconstructed track information from the Kalman fit.

For studying the energy loss of the protons I select the reconstructed tracks that range out (i.e. slow down to rest) inside the TPC. A characteristic feature of the energy loss profile of any stopping ionising particle is the so-called Bragg peak, a pronounced peak that occurs immediately before the particle comes to rest. From Eq. (6.1) we can see that this behaviour is expected, as the energy loss for non-relativistic particles is inversely proportional to β^2 . In data, a way of identifying the Bragg peak, and thus select the stopping particles, is checking the number of energy deposits towards the

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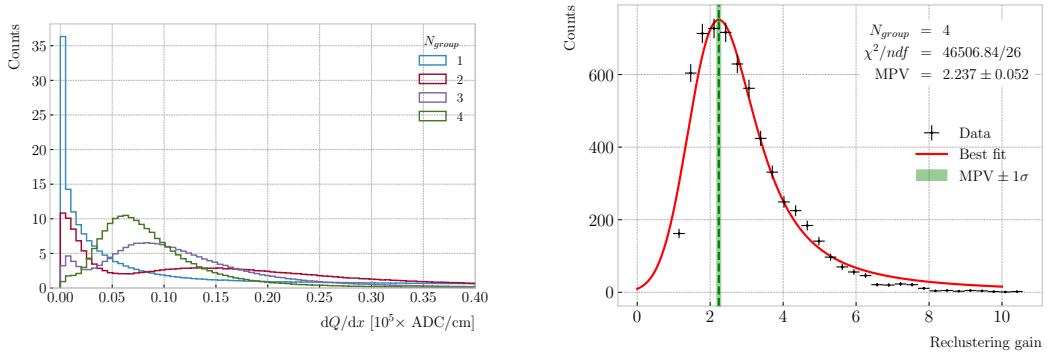


Figure 6.3: Left panel: distribution of the reconstructed ionisation charge per unit length for our MC stopping proton sample. The different colors indicate how many consecutive dQ/dx pairs were grouped together. Right panel: distribution of the median change in dQ/dx per track after $N_{group} = 4$ clusters were reclustered together.

end of the track. In this case, I count the fraction of the Geant4 simulated energy deposits with a residual range value (the distance from a given energy deposit to the last deposit in the track trajectory) less than a 20% of the corresponding track length². The distribution of this fraction of energy deposits for our proton sample is shown in Fig. 6.2 (left panel). We can clearly see two well separated peaks in this distribution, one centered at 0.2 and another, narrower, one centered at a higher value. The first one corresponds to non-stopping protons, as in that case the number of energy deposits towards the end of the track is uniformly distributed due to the absence of the Bragg peak. In that way, I apply a cut in this distribution, requiring that at least 30% of the simulated energy deposits sit in the last 20% of the tracks, to ensure that the Bragg peak is present.

Figure 6.2 (right panel) shows the distribution of the energy loss per unit length for the Geant4 simulated energy deposits of the selected stopping protons. We can see that it follows the expected shape of a Landau distribution, which describes the fluctuations of the ionisation energy losses [157]. This distribution has a characteristic asymmetric PDF, with a long right tail that translates into a high probability for high-energy ionisation losses. The origin of these fluctuations is mainly the possibility of transferring a high

²As we are applying this selection at the Geant4 level we could have simply selected the stopping protons using the `EndProcess` labels from the simulation. However, the Bragg peak identification method displayed here could serve as a starting point for a selection of stopping protons in real data.

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2902 enough energy to an electron, so it becomes a ionising particle itself.

2903 Now, from the point of view of the reconstruction, the objects that we have available
 2904 to extract the ionisation information for the different reconstructed tracks are the
 2905 collections of dQ and dx pairs, as stated before. The dQ values come from adding up
 2906 the amplitude of all the reconstructed hits in a cluster, which is the input object to the
 2907 Kalman fit.

2908 Figure 6.3 (left panel) shows the distribution of the ionisation charge deposits
 2909 per unit length for the track in the stopping proton sample (blue line). As one can
 2910 notice, this distribution does not resemble the expected shape of the Landau PDF. This
 2911 distribution peaks sharply at 0 and has a heavy tailed behaviour. Notice, however, how
 2912 the distribution changes its shape as we group together N_{group} consecutive charge deposit
 2913 pairs (red, purple and green lines). The distribution in the $N_{group} = 4$ case already has
 2914 a shape which resembles that of the Geant4-level ionisation per unit length, so I will
 2915 proceed using this amount of reclustering for the reconstruction-level depositions.

2916 An extra factor I need to account for, when reclustering is applied, is how the overall
 2917 dQ/dx per track changes. To do so, we can look at the ratio between the median dQ/dx
 2918 after and before the reclustering. Figure 6.3 (right panel) shows the median enhancement
 2919 in dQ/dx per track for the stopping proton sample in the case $N_{group} = 4$. Fitting a
 2920 Landau distribution convolved with a Gaussian³, I estimate the most probable value of
 2921 this ratio to be $G_{group} = 2.24 \pm 0.05$.

2922 At this point, I am left with determining the conversion between the charge deposits
 2923 per unit length dQ/dx and the energy deposits per unit length dE/dx . To this end, we
 2924 need a way of comparing the two. I can use the residual range z to get a prediction of
 2925 the most probable dE/dx by using the following empirical parametrisation [158]:

$$\frac{dE}{dx}(z) = \frac{z^{\frac{1}{p}-1}}{p\Lambda^{\frac{1}{p}}}, \quad (6.4)$$

2926 which is quoted in the literature as the Bragg-Kleeman formula. In order to obtain the

³In the literature, this distribution is often referred to as Landau+Gaussian or langau. In the following, I will use LanGauss to refer to such PDF.

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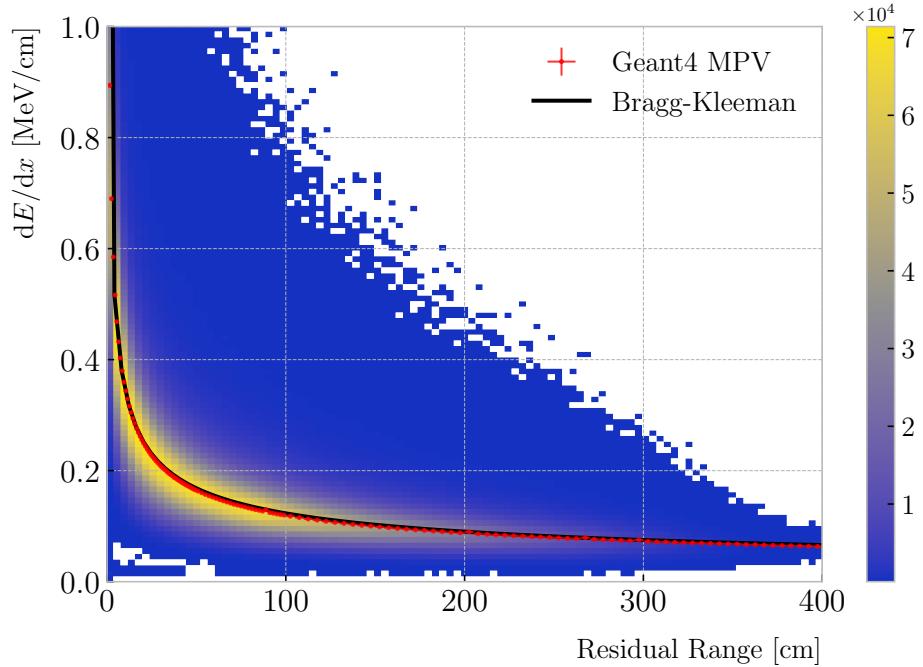


Figure 6.4: Distribution of the Geant4-simulated energy losses per unit length versus residual range for the stopping proton sample. The overlaid points represent the fitted most probable value of the dE/dx distribution in each residual range bin, whereas the curve is their best fit to the Bragg-Kleeman formula from Eq. (6.4).

2927 p and Λ parameters I perform a fit using the energy losses and the residual ranges given
 2928 by the Geant4 stage of our proton sample.

2929 Within our simulation, the residual range is sampled with a maximum size of
 2930 5 mm. Therefore, to perform the fit to the Bragg-Kleeman formula, we can use a
 2931 fine-grained residual range binning. For each of the residual range bins I extract the
 2932 dE/dx distribution and fit it to a LanGauss distribution, to obtain the value of the
 2933 most probable dE/dx in the bin together with a statistical uncertainty. I then fit Eq.
 2934 (6.4) to these most probable values and the centres of the residual range bins. This
 2935 procedure is depicted in Fig. 6.4, where I show the distribution of the energy loss per
 2936 unit length versus the residual range, together with the most probable dE/dx values
 2937 and their uncertainty in each bin (red points) and the curve with the best fit of the
 2938 Bragg-Kleeman relation to those values (black line). The best fit is obtained for the

CHAPTER 6. PARTICLE ID IN ND-GAr

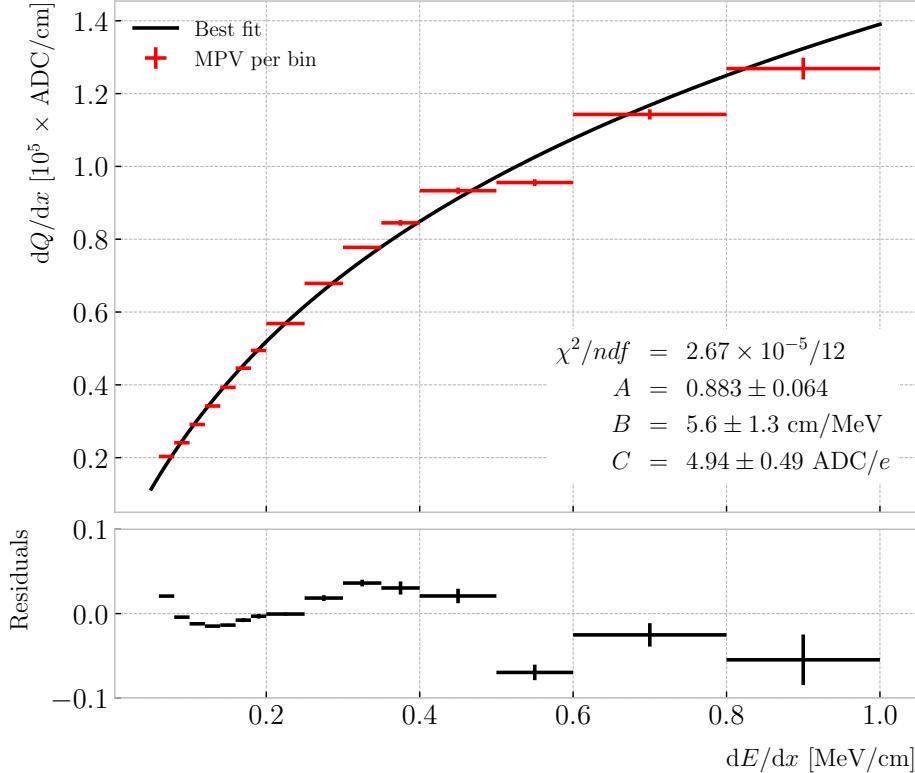


Figure 6.5: Fitted most probable dQ/dx values for each dE/dx bin (red points), obtained from the stopping proton sample. The overlaid curve (black line) represents the best fit to the logarithmic calibration function from Eq. (6.5).

2939 parameter values $p = 1.8192 \pm 0.0005$ and $\Lambda = 0.3497 \pm 0.0008 \text{ cm/MeV}^{p4}$.

2940 Having an analytical expression that relates the residual range to dE/dx , I can take
2941 our reconstruction-level residual ranges from the stopping proton sample and compute
2942 the most probable energy loss associated.

2943 In order to parametrise the charge saturation, we can use the following logarithmic
2944 function inspired by the modified box model for recombination:

$$\frac{dE}{dx} = \frac{e^{\frac{dQ}{dx} B \frac{W_{ion}}{G_{group} C}} - A}{B}, \quad (6.5)$$

2945 where A and B are the calibration parameters we need to determine, W_{ion} is the average
2946 energy to produce an electron-ion pair, G_{group} is the gain from the reclustering discussed

⁴These strange units for Λ come from dimensional analysis, just to keep the Bragg-Kleeman formula (6.4) consistent.

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Table 6.1: Calibration parameters obtained from the fit of the ND-GAr simulated stopping proton sample to the calibration function from Eq. (6.5). The fits were performed for the 10, 12, and 16-bit ADC limits.

	χ^2/ndf	Best fit $\pm 1\sigma$		
		A	B (cm/MeV)	C (ADC/e)
10-bit	$1.83 \times 10^{-6}/12$	-9.3 ± 3.9	270 ± 69	27.1 ± 5.4
12-bit	$2.67 \times 10^{-5}/12$	0.883 ± 0.064	5.6 ± 1.3	4.94 ± 0.49
16-bit	$1.44 \times 10^{-5}/12$	0.949 ± 0.024	3.53 ± 0.58	4.52 ± 0.29

above and C is the calibration constant to convert number of electrons to ADC counts, commonly refer to as gain (also to be obtained in the fit). In this case, I use a value for the electron-ion production energy of $W_{ion} = 26.4$ eV [159]. This value, used in our simulation as well, was measured for gaseous argon in normal conditions, and therefore should be checked in the future to describe correctly the high-pressure argon-CH₄ mixture of ND-GAr.

For the calibration fit I follow a procedure similar to the previous one for Eq. (6.4). Binning the dE/dx range, I fit a LanGauss distribution to the corresponding dQ/dx distribution to obtain the most probable value. The resulting data points (red bars) are shown in Fig. 6.5 (top panel), the horizontal error bars depict the width of the dE/dx bin whereas the vertical bars represent the error associated to the most probable value estimation. A fit to the logarithmic function in Eq. (6.5) is also shown (black line). For this I weighted the data points using the inverse of their relative error, obtaining a reduced chi-square value of $\chi^2/ndf = 2.22 \times 10^{-6}$. The best fit parameters I found from this fit are $A = 0.883 \pm 0.064$, $B = 5.6 \pm 1.3$ cm/MeV and $C = 4.94 \pm 0.49$ ADC/e. Figure 6.5 (bottom panel) shows the residuals between the data points and the fit.

The value for the gain I obtained from the fit is in reasonable agreement with our expectation. This value is set in GArSoft to 5 ADC/e by default.

One interesting thing to check is what induces this non-linear relation between charge and energy. The only effects that modify the amount of electrons reaching the readout planes in the simulation are the transverse diffusion and the finite electron lifetime. Once the electrons reach the readout chambers, the pad response functions are applied,

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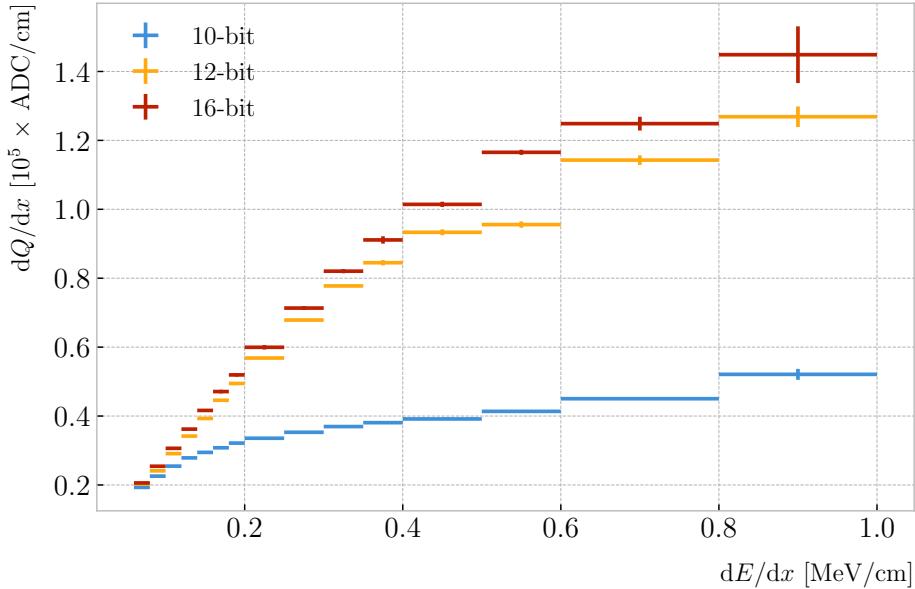


Figure 6.6: Fitted most probable dQ/dx values for each dE/dx bin for three different ADC bit limits, 10 (blue points), 12 (default, yellow points) and 16-bit (red points).

2969 together with an electrons-to-ADC conversion and the ADC saturation limit.

2970 By default, GArSot applies a 12-bit ADC limit, which can be changed in the
 2971 simulation configuration. However, it can only be increased up to 16-bit, as we represent
 2972 the ADC collection as a `std::vector<short>`. This way, I tried to change the saturation
 2973 parameter to see how it affects the relation between reconstructed charge and energy.
 2974 Figure 6.6 shows a comparison between the most probable dQ/dx for 10, 12 and 16-
 2975 bit ADC limits. As expected, the lower the limit is the sooner the charge saturates.
 2976 For higher ADC limits the relation between energy and charge remains linear up to
 2977 higher dE/dx values, but even for the 16-bit limit the saturation is noticeable for values
 2978 $\gtrsim 0.5$ MeV/cm.

2979 Table 6.1 shows the results of fitting the samples with 10 and 16-bits ADC limits to
 2980 the calibration function from Eq. (6.5), using the weights based on their relative error
 2981 as described previously. One interesting feature to notice is how different the best fit
 2982 points look for the 10-bit ADC saturation when compared to the other two, which are
 2983 consistent with each other.

2984 At this point we can compare the dE/dx distribution one gets from Geant4, i.e. the

6.2. dE/dx MEASUREMENT IN THE TPC

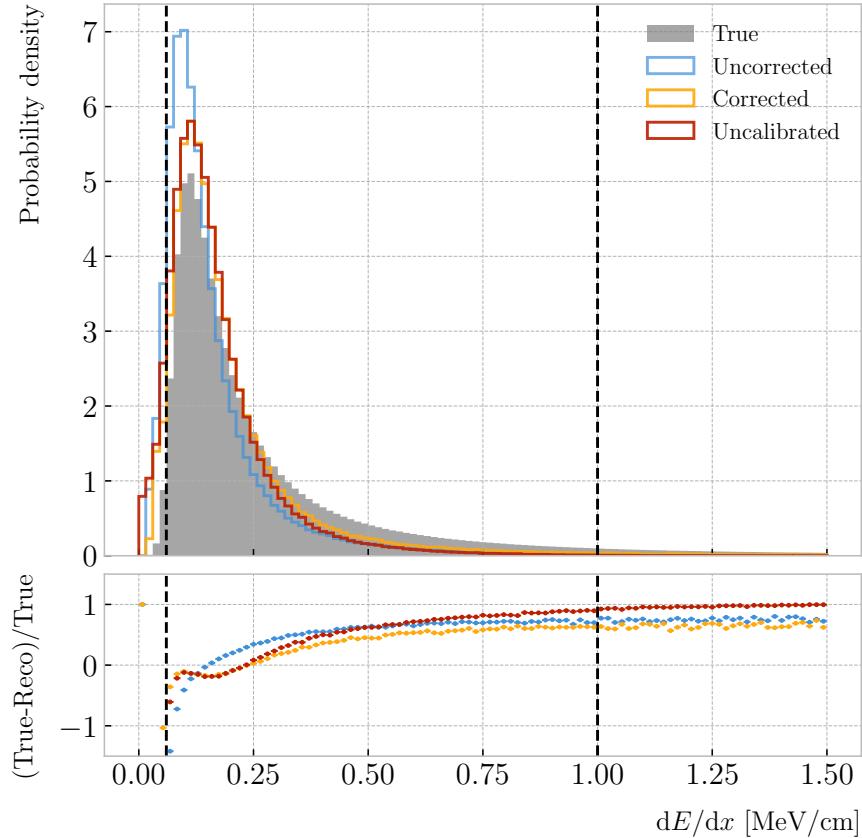


Figure 6.7: Top panel: area normalised dE/dx distributions for the true (solid grey) and the reconstructed energy deposits in the stopping proton sample, both after applying the calibration (blue) and the calibration and the normalisation correction (yellow). Also shown is the distribution obtained by applying a correction factor to the dQ/dx values but not the calibration (red). Bottom panel: fractional residuals for the uncorrected (blue), corrected (yellow) and uncalibrated (red) samples.

2985 true energy loss distribution, and the distribution I found by applying the calibration
 2986 function to our collection of reconstructed dQ/dx values. Figure 6.7 (top panel) shows
 2987 the true (solid grey) and reconstructed (blue, labeled as uncorrected) distributions
 2988 together. The dashed vertical lines indicate the region of validity of the calibration fit, i.e.
 2989 the left and right edges of the first and last dE/dx bin respectively. Notice that these
 2990 histograms are area-normalised, as the total number of true energy deposits is much
 2991 higher than the number of reconstructed charge deposits. This is due to a combination
 2992 of effects, like the finite spatial resolution of the detector, the hit clustering used in the
 2993 track fitting and the reclustering we have applied here.

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2994 The two distributions are significantly different. That can be seen clearly when
2995 looking at the fractional residuals, shown in Fig. 6.7 (bottom panel). In particular,
2996 the position of the peak is off, which could bias the mean energy loss predictions. It
2997 seems like the difference between these may be due to an overall scaling factor. One
2998 possibility is to scale the most probable value of the reconstructed distribution to
2999 the most probable value predicted by Geant4. I do this by fitting both distributions
3000 using a LanGauss function, obtaining $dE/dx_{MPV, true} = 0.1145 \pm 0.0005$ MeV/cm and
3001 $dE/dx_{MPV, reco} = 0.0928 \pm 0.0005$ MeV/cm for the true and reconstructed most probable
3002 values respectively. These can be translated into an scaling factor $S = 0.579 \pm 0.006$.

3003 The result of applying the scaling correction can be seen in Fig. 6.7 (top panel).
3004 The corrected dE/dx distribution (yellow, labeled as corrected) peaks around the same
3005 value the true distribution does, as expected. Moreover, the high energy region is also
3006 slightly better described. For low ionisations, below the lower limit of the calibration
3007 fit, the differences between true and reconstructed are still significant. This low energy
3008 excess may be migration of some events from the peak region. The overall effect of the
3009 correction can be seen in the fractional residual plot in Fig. 6.7 (bottom panel).

3010 One can also check what happens if instead of applying the logarithmic calibration we
3011 simply scale the dQ/dx distribution (post reclustering) to have the same most probable
3012 value as the true dE/dx distribution. In this case, following an analogous procedure to the
3013 one described earlier, I found the scaling factor $S_{uncalibrated} = 0.414 \pm 0.002$ MeV/ADC⁵.
3014 The resulting distribution (red, labeled as uncalibrated) is also shown in in Fig. 6.7 (top
3015 panel). The behaviour of the new distribution is similar to the corrected case at low
3016 energy losses, around the peak of the true distribution, but it is worse at describing the
3017 high energy tail. This is expected, it is in the high ionisation regime where saturation
3018 effects apply and therefore calibration is needed.

6.2. dE/dx MEASUREMENT IN THE TPC

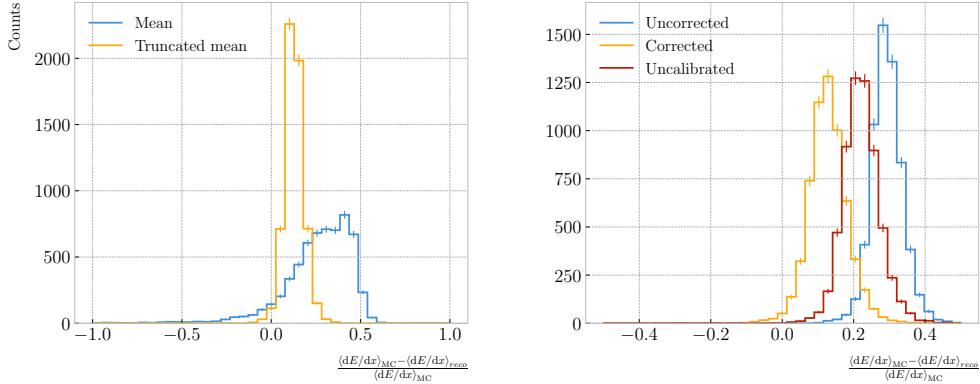


Figure 6.8: Left panel: fractional residuals between the true and the corrected dE/dx means (blue) and the 60% truncated means (yellow), for each event in the stopping proton sample. Right panel: fractional residuals between the true and the uncorrected (blue), corrected (yellow) and uncalibrated (red) dE/dx 60% truncated means, for each event in the stopping proton sample.

6.2.2 Truncated dE/dx mean

Once we have a collection of dE/dx values for each reconstructed track, we can compute the corresponding most probable ionisation loss per unit length of the particle. This is the value predicted by the Bethe-Bloch or the PAI models, and together with a measurement of the momentum it allows for particle identification.

However, estimating the most probable dE/dx value for each reconstructed track is not a trivial task. As mentioned before, the dE/dx distributions follow Landau-like distributions. Therefore, one should perform e.g. a LanGauss fit to correctly estimate the most probable values. Automating this kind of fits is often problematic, as they usually incur in convergence problems. Moreover, the reconstructed dE/dx distributions we obtain tend to have relatively small statistics, which may also produce poor fits. In practice, doing these unsupervised fits may degrade our performance, and a more robust method is preferred.

A possibility could be taking the mean of the reconstructed dE/dx distribution for each particle. The problem with this approach is that the high energy Landau tail, combined with our limited statistics, can induce large fluctuations in the computation

⁵Notice that now the scaling factor is not dimensionless, as it acts more like a conversion factor here.

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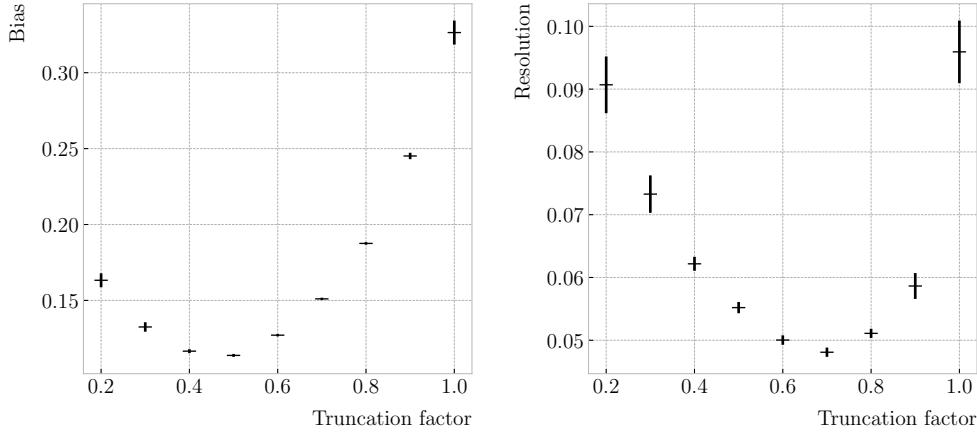


Figure 6.9: Estimated values of the mean dE/dx bias (left panel) and resolution (right panel) obtained using the corrected data from the stopping proton sample, for different values of the truncation factor.

of the mean. Imagine you have two protons with the same kinetic energy, but due to reconstruction problems in one case you did not get as many charge deposits reconstructed in its high ionisation loss region. If you do not remove the tails the computed dE/dx means will be significantly different.

In order to avoid those fluctuations, one can compute the mean of a truncated dE/dx distribution instead. By keeping only a given fraction of the lowest energy deposits we obtain an estimate of the mean energy loss that is more resilient to reconstruction inefficiencies and statistical effects. Figure 6.8 (left panel) shows a comparison between the $\langle dE/dx \rangle$ computed by taking the mean of the full distribution (blue line) and the 60% lowest energy clusters (yellow line), for the stopping proton sample. The fractional residuals are computed for each proton, taking the corresponding means using their collections of true and reconstructed energy deposits. One can see that using the simple mean translates into a high bias and uncertainty in the $\langle dE/dx \rangle$ estimation, whereas applying the truncation reduces both significantly.

Additionally, I performed a comparison between the 60% truncated mean dE/dx obtained using the different calibration methods discussed earlier, namely the uncorrected (blue), corrected (yellow) and uncalibrated (red) distributions. The results are shown in Fig. 6.8 (right panel). While the widths of these distributions are similar, the bias

6.2. dE/dx MEASUREMENT IN THE TPC

3053 obtained for the corrected sample, i.e. calibration function and correction factor applied,
 3054 is a factor of ~ 2 lower than in the uncalibrated case and almost three times smaller
 3055 than for the uncorrected sample.

3056 The next step is to optimise the level of truncation we are going to apply to our
 3057 data. To do so, I used different truncation factors, i.e. the percentage of energy-ordered
 3058 reconstructed energy deposits we keep to compute the mean, on the corrected dE/dx
 3059 sample of the stopping protons. Then, following the same procedure of computing the
 3060 fractional residuals as before, I fitted the resulting histograms using a double Gaussian
 3061 function. This is simply the sum of two Gaussian functions of the type:

$$g(x; \mu, \sigma, A) = A e^{-\frac{(x-\mu)^2}{2\sigma^2}}. \quad (6.6)$$

3062 I do not add the classical normalisation factor of the Gaussian, $1/\sqrt{2\pi}\sigma$, therefore
 3063 the amplitude A simply represents the maximum of the function. One of the two
 3064 Gaussian functions describes the core part of the distribution, while the other captures
 3065 the behaviour of the tails.

3066 For each truncation factor, I look at the bias and the resolution I obtain. I define
 3067 these as the weighted means of the corresponding parameters in the fits:

$$\bar{x} = \frac{A_{core} x_{core} + A_{tail} x_{tail}}{A_{core} + A_{tail}}, \quad (6.7)$$

3068 where A_{core} and A_{tail} are the amplitudes of the core and tail distributions respectively
 3069 and x is either the mean μ or the width σ of said distributions.

3070 Figure 6.9 shows the bias (left panel) and the resolution (right panel) I obtained
 3071 for the stopping proton sample, using different values of the truncation. From these, it
 3072 can be seen that a truncation factor of 50% minimises the bias in the estimation, while
 3073 70% gives the best resolution. That way, I settled on the intermediate value of 60%
 3074 truncation, which yields a $\langle dE/dx \rangle$ resolution of 5.00 ± 0.08 % for stopping protons.

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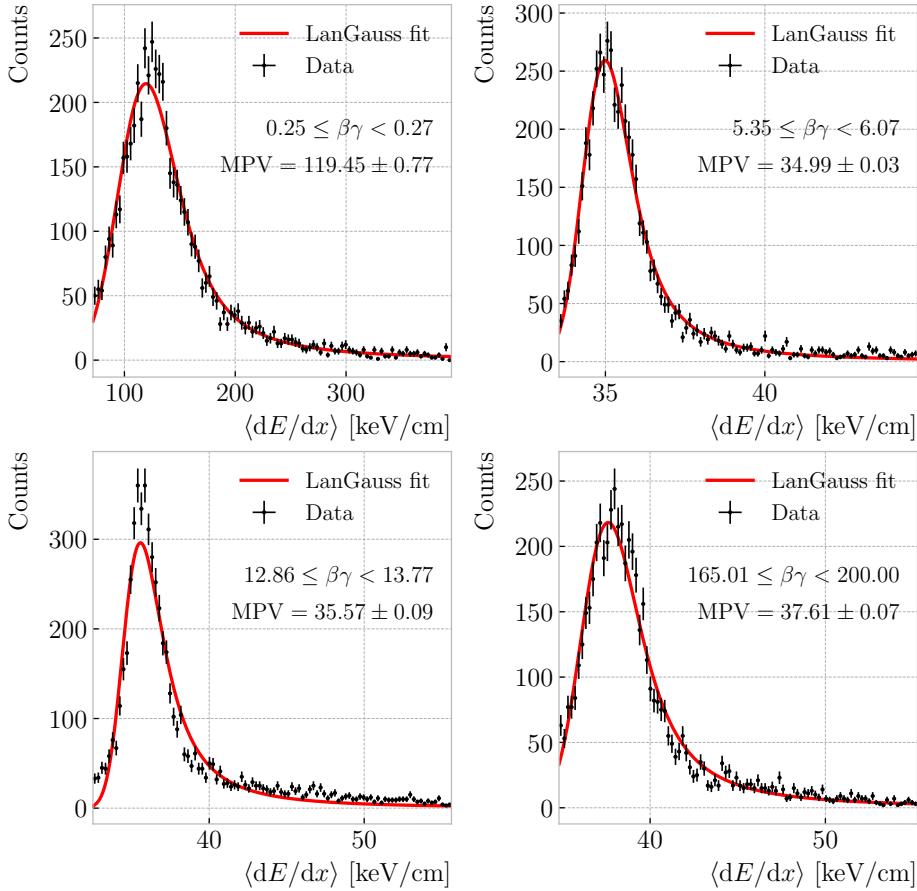


Figure 6.10: Examples of the truncated mean dE/dx LanGauss fits for various $\beta\gamma$ bins, from a simulated FHC neutrino sample.

3075 6.2.3 Mean dE/dx parametrisation

3076 Now that we have a way to estimate the mean energy loss of a particle in the HPgTPC,
 3077 we can determine the value of the free parameters in the ALEPH formula, Eq. (6.3).
 3078 For this, I used a sample of 10^5 reconstructed FHC neutrino events inside ND-GAr. In
 3079 this case I cannot use the stopping proton sample, as we need to cover the full kinematic
 3080 range of interest for the neutrino interactions in our detector.

3081 The original data does not contain an estimation of the velocity of the tracks, instead
 3082 the tracks have a value for the reconstructed momentum and the associated PDG code
 3083 of the Geant4-level particle that created the track. Therefore, one can select some of the
 3084 particles in the data, in this case I selected electrons, muons, pions and protons, and

6.2. dE/dx MEASUREMENT IN THE TPC

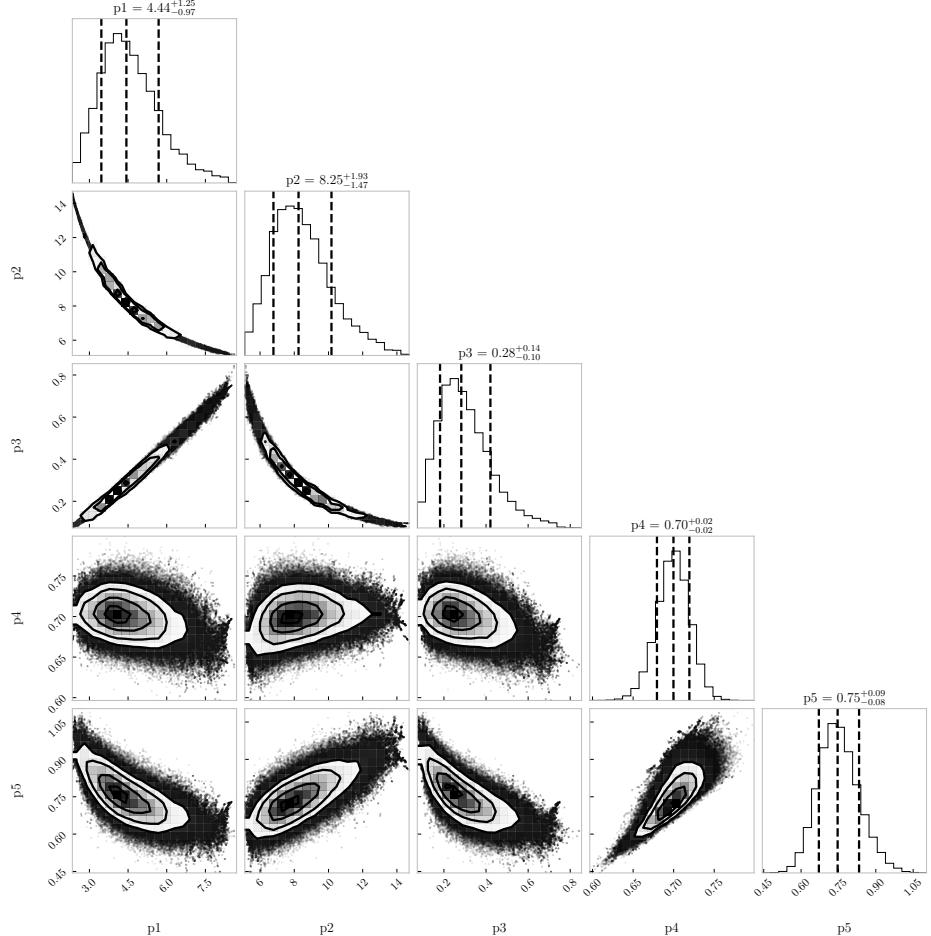


Figure 6.11: Resulting one and two dimensional projections of the posterior probability distributions of the ALEPH $\langle dE/dx \rangle$ parameters obtained by fitting the 60% truncated mean dE/dx values from a FHC neutrino sample in ND-GAr. The vertical dashed lines in the 1D distributions represent the 16th, 50th and 84th percentiles.

3085 compute β and γ using the reconstructed momentum and their mass. In terms of $\beta\gamma$
 3086 the mean dE/dx does not depend on the particle species, so one can consider all the
 3087 dataset as a whole. For this fit, I will express β in terms of the $\beta\gamma$ product as:

$$\beta = \frac{\beta\gamma}{\sqrt{1 + (\beta\gamma)^2}}, \quad (6.8)$$

3088 which can be easily proven from the definition of γ .

3089 Next, I bin the data in $\beta\gamma$. I chose a fine binning so as to capture the different
 3090 features of the ionisation curve. Instead of fixing the bin width, I select them so each one

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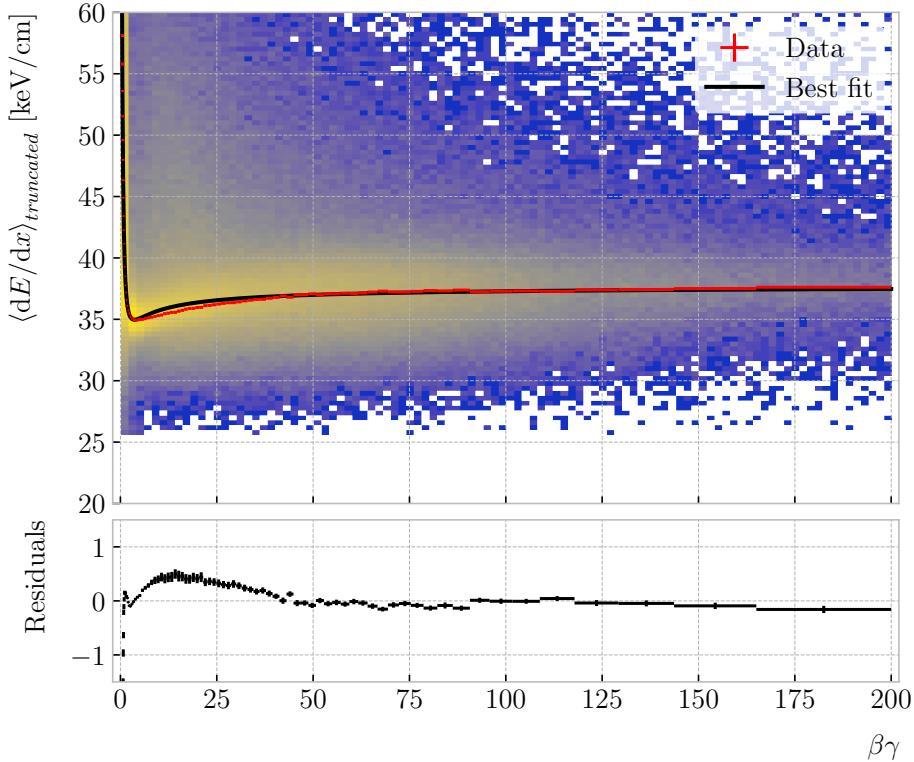


Figure 6.12: Truncated mean dE/dx obtained for the FHC neutrino sample as a function of the $\beta\gamma$ product (upper panel). Also shown are the fitted most probable values for each $\beta\gamma$ bin (red points) and the best fit obtained using the ALEPH parametrisation (black line). The residuals resulting from the fit are shown in the lower panel.

3091 has approximately the same statistics. Then, for each $\beta\gamma$ slice, I compute the median
 3092 and the interquartile range (IQR) of the $\langle dE/dx \rangle$ distribution. Using these, I make a
 3093 histogram in the range [median – IQR, median + 5 IQR], which I fit to a LanGauss
 3094 function in order to extract the MPV. Using this range accounts for the asymmetric
 3095 nature of the distributions, while also helps avoiding a second, lower maximum present
 3096 at low $\beta\gamma$, probably a result of reconstruction failures.

3097 A few examples of these fits are shown in Fig. 6.10. The chosen values of $\beta\gamma$ sit in
 3098 very distinct points along the $\langle dE/dx \rangle$ curve, going from the high ionisation region at
 3099 low velocities (top left panel), to the minimum point (top right panel), the beginning of
 3100 the relativistic rise (bottom left panel), and the plateau produced by the density effect
 3101 (bottom right panel).

6.2. dE/dx MEASUREMENT IN THE TPC

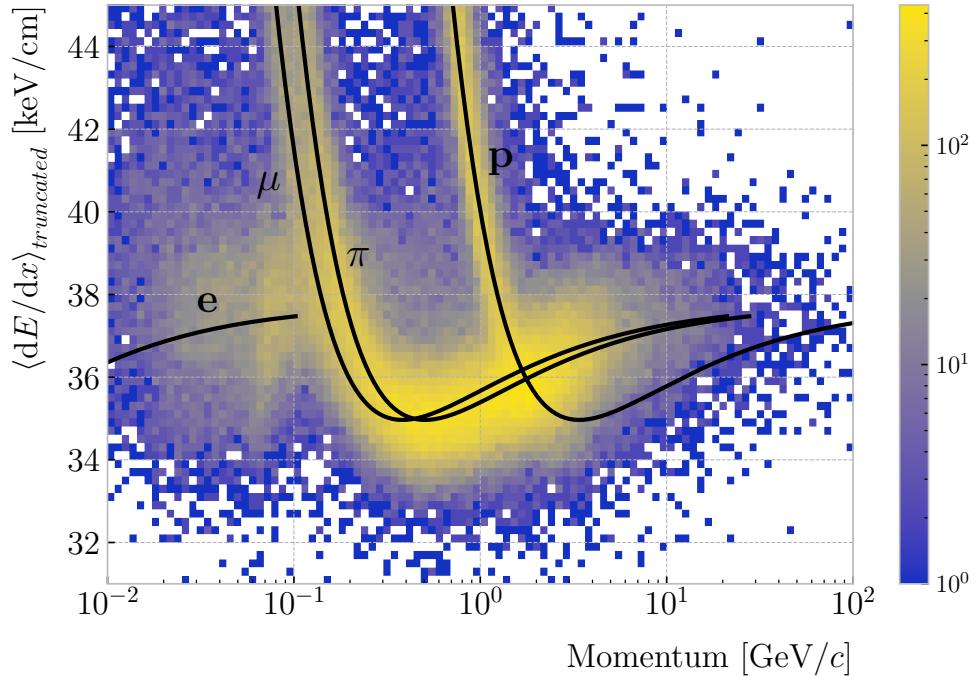


Figure 6.13: Distribution of the 60% truncated mean dE/dx versus reconstructed momentum for the FHC neutrino sample. The black lines indicate the predictions of the ALEPH parametrisation for electrons, muons, charged pions and protons.

3102 I used the resulting most probable $\langle dE/dx \rangle$ values and the centres of the $\beta\gamma$ bins as
 3103 the points to fit to the ALEPH formula. For this particular fit I used the least-squares
 3104 method to get a first estimation of the ALEPH parameters. Applying some uniform
 3105 priors, I then used these values as the starting point of a 100000 steps MCMC. Figure 6.11
 3106 shows the posterior probability distributions I obtain for each parameter. The reported
 3107 best fit points are based on the 16th, 50th, and 84th percentiles in the marginalised
 3108 distributions.

3109 The resulting fit (black line), compared to the data points (red points) and the
 3110 underlying distribution is shown in Fig. 6.12 (top panel). The overall fit is good, with a
 3111 reduced chi-squared of $\chi^2/ndf = 1.02$. However, there are some regions where the fit
 3112 does not describe the data correctly, like the very low $\beta\gamma$ regime, where the fit severely
 3113 underestimates for energy losses $\gtrsim 50$ keV/cm, and the start of the relativistic raise,
 3114 where we have a slight overestimation. This is a result of those points having a larger
 3115 uncertainty when compared to the ones around the dip or the plateau areas. These

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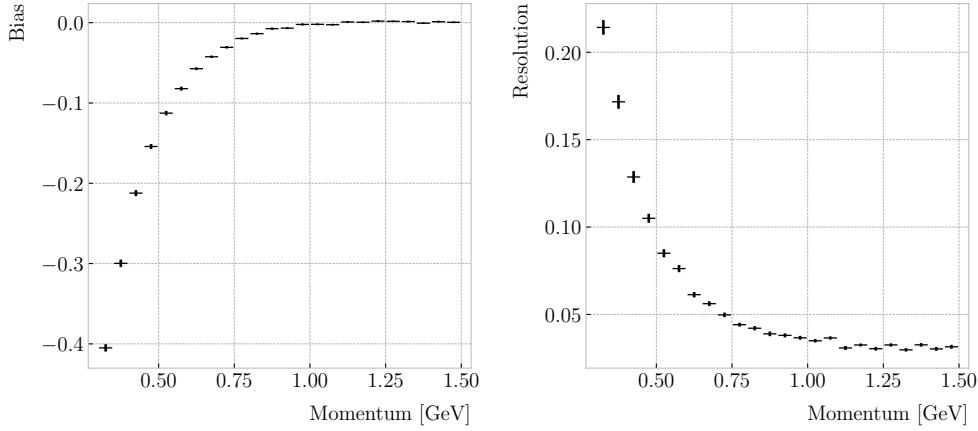


Figure 6.14: Estimated values of the mean dE/dx bias (left panel) and resolution (right panel) obtained for the true protons in a FHC neutrino sample.

3116 differences can be better seen in the residual plot, Fig. 6.12 (bottom panel).

3117 6.2.4 Particle identification

3118 6.3 Muon and pion separation in the ECal and MuID

3119 As it could be seen from Fig. 6.13, it is not possible to separate muons and charged pions
3120 in the HPgTPC using dE/dx for momenta $\gtrsim 300 \text{ MeV}/c$. In ND-GAr, approximately
3121 70% of the interactions in FHC mode will be ν_μ CC (compared to the 47% of $\bar{\nu}_\mu$ CC
3122 interactions when operating in RHC mode), while 24% are neutral currents. Out of
3123 these, around 53% and 47% of them will produce at least one charged pion in the final
3124 state, respectively. Figure 6.15 shows a comparison between the spectra of the primary
3125 muons and the charged pions for ν_μ CC interactions in ND-GAr producing one or more
3126 charged pions. From this, one can see that (i) the majority of muons and charged pions
3127 are not going to be distinguishable with a $\langle dE/dx \rangle$ measurement, and that (ii) particle
3128 identification is necessary both to classify correctly the ν_μ CC events and identify the
3129 primary muon within them.

3130 ND-GAr features two other subdetectors which can provide additional information
3131 for this task, namely the ECal and MuID. The current ECal design, described in (ref
3132 section), consists of 42 layers, made of 5 mm of Pb, 7 mm of plastic scintillator and a

6.3. MUON AND PION SEPARATION IN THE ECAL AND MUID

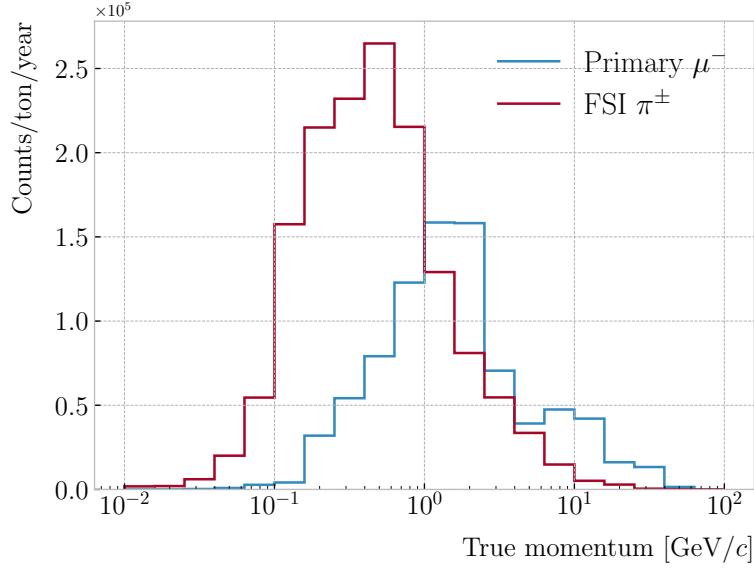


Figure 6.15: True momentum distribution for the primary muon in ν_μ CC $N\pi^\pm$ interactions inside the fiducial volume of ND-GAr (blue line), compared to the post FSI charged pion spectrum (red line).

3133 1 mm PCB board. The total thickness of this calorimeter is 1.66 nuclear interaction
 3134 lengths or 1.39 pion interaction lengths. The Muid design is in a more conceptual
 3135 stage, however it is envisioned to feature layers with 10 cm of Fe and 2 cm of plastic
 3136 scintillator⁶. With its three layers, it will have a thickness of 1.87 or 1.53 nuclear or pion
 3137 interaction lengths, respectively.

3138 Because pion showers are dominated by inelastic nuclear interactions, the signatures
 3139 of these particles in the calorimeter will look significantly different from those of muons.
 3140 Although our ECal is not thick enough to fully contain the hadronic showers of the
 3141 charged pions at their typical energies in FHC neutrino interactions, they can still be
 3142 used to understand whether the original particle was more hadron-like or MIP-like. In
 3143 Fig. 6.16 I show two examples of energy distributions created by a muon (left panel)
 3144 and a charged pion (right panel) of similar momenta interacting in the ECal. These
 3145 figures represent the transverse development of the interactions. For each of them, I
 3146 computed the principal component and centre of mass of the interaction, projecting

⁶It is not mentioned anywhere, but I assume that there should also be another layer of PCB board of 1 mm. However, in this case its contribution to the total thickness of the sampling calorimeter would be negligible.

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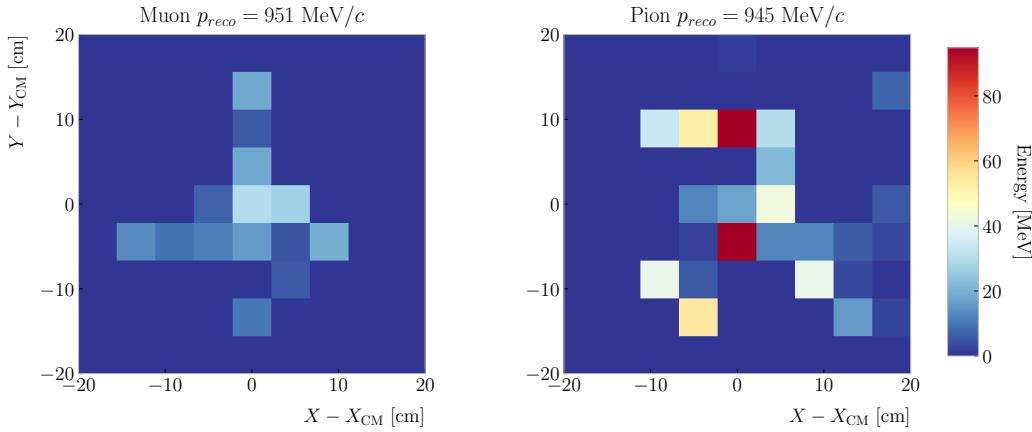


Figure 6.16: Distributions of energy deposits in the ECal for a muon (left panel) and a charged pion (right panel) with similar momenta. The energy is projected onto the plane perpendicular to the principal component of the hits, and the positions are relative to the center of the interaction.

the position of the hits onto the plane perpendicular to that direction, and taking the distances relative to the centre. It can be seen that the muon follows an almost MIP-like behaviour, being the central bin in the histogram the one with the highest deposited energy. On the other hand, the pion not only deposits more energy overall, but also this energy is more spread-out among the different hits. It is this kind of information that would allow us to tell apart muons from pions.

This way, I identify three main action points that need to be addressed if one wants to use these detectors to distinguish between muons and charged pions. These are:

1. the way we make the associations between tracks in the HPgTPC to the activities (what in GArSoft we call clusters) in the ECal and the MuID,

2. what variables or features one can extract from the calorimeters that encapsulate the information we are interested about,

3. and how to carry out the classification problem.

6.3. MUON AND PION SEPARATION IN THE ECAL AND MUID

3160 6.3.1 Track-ECal matching

3161 One of the main players in the muon and pion separation is the way we associate clusters
3162 in the ECal to reconstructed tracks in the TPC. Missing some associations or making
3163 wrong ones can bias the ECal quantities that we can use for classifying particles. The
3164 current algorithm in GArSoft provides precise associations, i.e. most of the associations
3165 that it produces are correct, but it appears to miss an important number of associations
3166 (at least when using the default configuration).

3167 The current TPC track-ECal cluster association algorithm is divided in four parts.
3168 It first checks whether the track end point fulfils certain conditions to be extrapolated.
3169 There are two cut values in this step, one for the drift direction and other radial.

3170 If the point can be extrapolated, the code computes the coordinates of the centre
3171 of curvature using the Kalman fit estimates at the track end (y , z , $1/R$, ϕ , $\tan\lambda$). It
3172 then compares the distance between this and the cluster in the (z, y) plane with R . This
3173 introduces another cut in the perpendicular direction.

3174 The next step is different for clusters in the barrel or in one of the end caps. If it
3175 is a barrel cluster the algorithm extrapolates the track up to the radial distance of the
3176 cluster. There are three possible outcomes, the extrapolated helix can cut the cylinder
3177 of radius r_{clus} two, one or zero times. I get the cut point that is closer to the cluster and
3178 check that it is either in the barrel or the end caps. Computing the difference between
3179 the x coordinates of the cluster and the extrapolated point, the module checks that this
3180 is not greater than a certain cut. If the cluster is in an end cap, I propagate the track
3181 up to the x position of the cluster. Then, the algorithm computes the angle in the (z, y)
3182 plane between the centre of curvature and the cluster, α , and the centre of curvature
3183 and the propagated point, α' . A cut is applied to the quantity $(\alpha - \alpha')R$.

3184 If the cluster contains more than a certain number N of hits, I apply an extra cut to
3185 the dot product of the direction of the track at the propagated x value and the cluster
3186 direction.

3187 The code makes sure to only associate one end of the track (if any) to a cluster.

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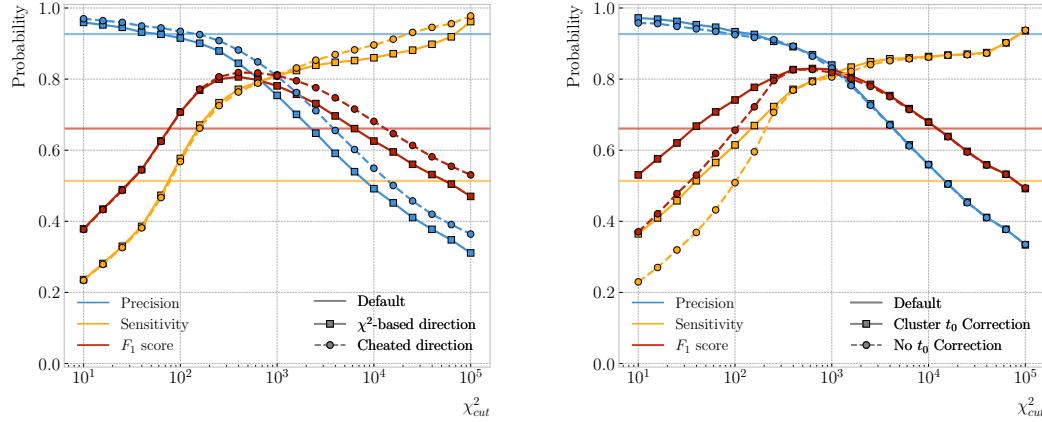


Figure 6.17: Left panel: comparison between the precision (blue), sensitivity (yellow) and F_1 score (red) obtained for the default (horizontal lines) and new algorithms, both with the χ^2 -based direction estimator (squares) and cheating the directions (circles), for different values of the chi^2 cut. Right panel: comparison of the performance of the new algorithm when applying the cluster t_0 correction (squares) and when (circles).

3188 However, it can associate more than one track to the same cluster. This makes sense,
3189 as different particles can contribute to the same cluster in the ECal, but it makes it
3190 difficult to quantify the relative contributions of the tracks to a certain cluster.

3191 As a way of comparing the performance of this algorithm, a new, simpler association
3192 module was written. The goal was to have a simple and robust algorithm, which depends
3193 on as few parameters as possible and that can produce a one-to-one matching between
3194 tracks and ECal clusters.

3195 For each reconstructed track, the new algorithms applies the same procedure to the
3196 forward and the backward fits irrespective of their end point positions. It first gets the
3197 Kalman fit parameters at the corresponding end point together with the X position, x_0 ,
3198 (y_0 , z_0 , $1/R$, ϕ_0 , $\tan\lambda$).

3199 For each ECal cluster, I compute the radial distance to the centre of the TPC and
3200 find the ϕ value in the range $[\phi_0, \phi_0 + \text{sign}(R)\phi_{max}]$ that makes the propagated helix
3201 intersect with the circle defined with such radius. The (x, y, z) position of the helix for
3202 the ϕ value found (if any) is then computed. In case there are two intersections, I keep
3203 the one that minimises the distance between (y, z) and (y_c, z_c) .

3204 I then calculate χ^2 value based on the Euclidean distance between the propagated

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3205 point and the cluster:

$$\chi^2/ndf = \frac{\sum_{n=0}^2 (x^{(n)} - x_c^{(n)})^2}{3}. \quad (6.9)$$

3206 If there was no intersection I store a -1 instead. In the end, for each reconstructed track
3207 in the event one ends up with two collections of χ^2 values, one for each ECal cluster
3208 and fit directions.

3209 The current code only supports having ECal clusters associated to one end of each
3210 track. We have two options to decide what track end to keep. The first one tries to
3211 cheat the selection, looking at the distance between the two track ends and the true
3212 start position of the associated MC particle. The second one keeps the track end with
3213 more χ^2 entries below the cut.

3214 This feature of only considering one track end limits the algorithm, making it not
3215 suitable for reconstructing events with particles originating outside the TPC. However,
3216 as for the moment the main concern of the group is the study of neutrino interactions
3217 off the gaseous argon, this is an acceptable assumption.

3218 In order to associate a cluster to a track, I take all clusters with a χ^2 value in the
3219 range $[0, \chi_{cut}^2]$. If a cluster has been assigned to more than one track we leave it with
3220 the one with the lowest χ^2 .

3221 This default behaviour of the algorithm can be modified to associate more than one
3222 track to each cluster. Not only that, but the χ^2 values can be used to assign relative
3223 weights to the different contributions.

3224 To evaluate the performance of the association method, I use a binary classification
3225 approach. In this case, I check the leading MC Track IDs associated to the reconstructed
3226 tracks and ECal clusters. I count an association as true positive (TP) if both Track
3227 IDs coincide. An association is considered false positive (FP) when the Track IDs are
3228 different. If a cluster has not been associated to any track but it shares the Track ID
3229 with a reconstructed track it is counted as a false negative (FN).

3230 For the testing, I used a sample of 10000 FHC neutrino events inside the HPgTPC.
3231 Figure 6.17 (left panel) shows the precision (blue line), sensitivity (yellow line), and F_1

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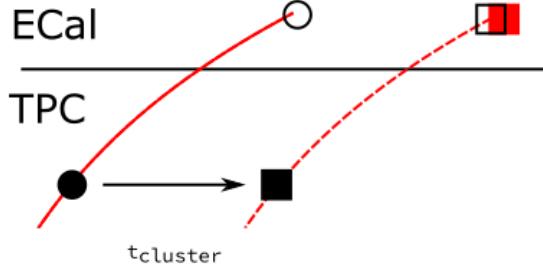


Figure 6.18: Schematics of a possible option to deal with track-ECal associations in non-zero t_0 neutrino interaction events, trying to correct for the drift direction uncertainty in a cluster-by-cluster basis using the cluster time, $t_{cluster}$.

score (red line) I obtained for different values of χ^2_{cut} . For comparison, the same metrics computed for the default algorithm with the current configuration are also shown (dashed lines). In the case of the new algorithm, I used both the χ^2 -based method to estimate the track direction described earlier (square markers) and the cheated direction from the Geant-level information (circle markers). For either of these we achieve similar values of the precision compared to the old code, while having a considerably higher sensitivity. It can be seen that cheating the direction of the tracks only makes a difference at high χ^2_{cut} , past the optimal value of the cut around the F_1 score maximum. Therefore, I set the χ^2 method as the default.

One of the possible weak points of this approach is that it relies on the position along the drift direction to make the decisions. Within the current ND-GAr design implemented in GArSoft, the timing information is provided by the ECal. That effectively means that prior to make the track-ECal associations the reconstructed x positions of the track trajectories differ from the simulated ones by an amount:

$$x_{reco}^{(n)} - x_{sim}^{(n)} = v_{drift} t_0, \quad (6.10)$$

where v_{drift} is the mean drift velocity in our medium and the initial time is in the range $t_0 \in [0, t_{spill}]$ where t_{spill} is the spill length. For a $10 \mu\text{s}$ spill this translates into a maximum 30 cm uncertainty on the drift direction position.

The current default in GArSoft sets $t_0 = 0$, but the functionality to randomly sample

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3250 this within the spill time is in place. Therefore, we need to understand what is the impact
3251 of a non-zero t_0 on the associations algorithm and foresee possible ways of minimising a
3252 loss in performance.

3253 Figure 6.18 represents a possible option to tackle the association problem when
3254 having events with a non-zero initial time t_0 . The black and white circles represent the
3255 original points, whereas the squares indicate the corrected positions. The end points of
3256 the track and the propagated points up to the cluster radius are indicated using filled
3257 and unfilled markers respectively. The red square represents the position of the cluster.

3258 Here I try to correct for the drift coordinate position using the time associated to the
3259 cluster. Assuming that the drift time is much larger than the propagation time, $t_{cluster}$
3260 could be used as a good estimation of the t_0 . An alternative can be using the earliest
3261 time associated to a hit in said cluster. Doing this for each cluster before computing
3262 the χ^2 value could be used as an alternative to knowing the specific value of the t_0 , as
3263 when the association is correct this will provide the right correction but its impact is
3264 small enough to not change the position significantly in the case the cluster does not
3265 correspond to a given track.

3266 I tested the effect of this correction again using a sample of 10000 FHC neutrino
3267 events. Figure 6.17 (right panel) shows the precision (blue line), sensitivity (yellow line),
3268 and F_1 score (red line) for the case the cluster t_0 correction is applied (square markers)
3269 and for the no correction case (circle markers), as a function of χ^2_{cut} . In this case, the
3270 differences are particularly notorious at low values of the cut. It makes sense, as the t_0
3271 effect becomes subdominant when the distance we consider grows large. Overall, the
3272 correction increases the sensitivity while keeping the precision almost unchanged. As a
3273 result, I apply the t_0 correction to the generated samples as the default.

3274 6.3.2 Classification strategy

3275 The problem of the muon and charged pion separation has to be viewed in the broader
3276 context of the particle identification in our detector. Focusing on the beam neutrino
3277 interactions, it is clear that we are going to have muons and pions spanning a broad

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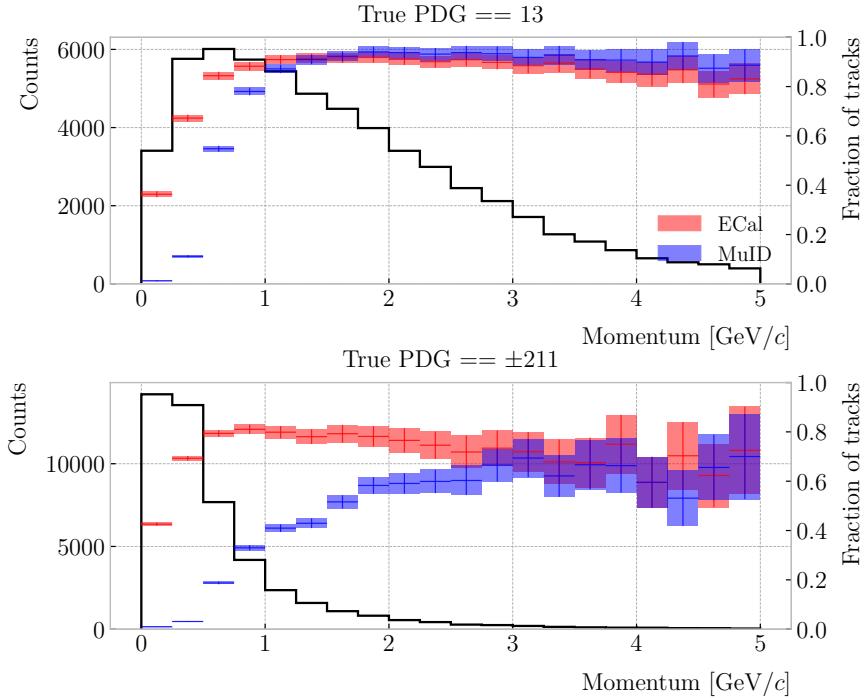


Figure 6.19: Momentum distribution for the reconstructed muons (top panel) and charged pions (bottom panel) in a FHC neutrino sample, together with the fraction of them reaching the ECal (red) and MuID (blue). Each entry corresponds to a reconstructed track, backtracked to a true muon or pion which has not produced any other reconstructed track.

momentum range. Not only that, but we will also have other particles with similar characteristics that will make the classification even more challenging. Therefore, we are presented with a task that will depend heavily on the kinematic range we are looking at each time, as both the available information and the possible impurities of other particle species vary.

For instance, distinguishing muons from pions could be difficult at low momenta, as a great number of them do not reach the ECal. Therefore, we could think of tailoring a version of the classification for that particular case, which could be complemented with a dE/dx measurement. Likewise, for momenta $\gtrsim 1$ GeV muons and pions reach the calorimeters efficiently, but so do protons. Because of this, one can try to train another classifier for this energy range, and rely on other methods to remove as many of the protons as possible.

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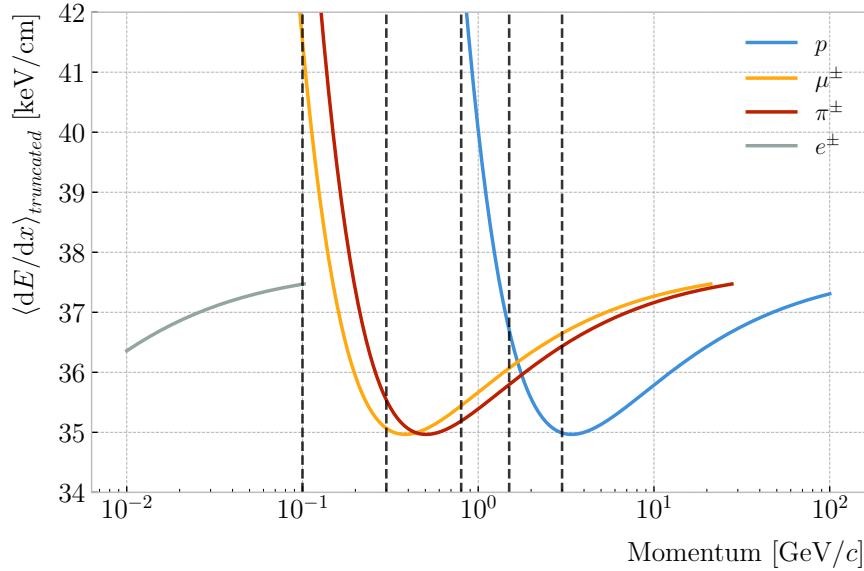


Figure 6.20: Predicted truncated mean dE/dx versus momentum, for electrons, muons, charged pions and protons, obtained using the ALEPH parametrisation. The vertical dashed lines represent the boundaries of the six regions used for the muon and pion classification training.

3290 Figure 6.19 shows the momentum distribution of the reconstructed muons (top) and
 3291 pions (bottom) in a FHC sample. It also contains the fraction of particles reaching the
 3292 ECal (red) and MuID (blue), for the different momentum bins. In Fig. 6.20 I show the
 3293 mean dE/dx of different particles as a function of the momentum, computed using the
 3294 ALEPH parametrisation with the best fit parameters found in Subsec. 6.2.2.

3295 Using these two figures as references, I decided to approach the classification by
 3296 dividing the problem into six different momentum regions. A summary of these can be
 3297 found in Tab. 6.2. The basic idea is to exploit all the information that is available in
 3298 each region and . For the problem at hand, I prepared separated samples of isotropic
 3299 single muons and pions, with momenta uniformly distributed along the corresponding
 3300 momentum range. Each sample contains 50000 events of the corresponding particle
 3301 species. I did not generate samples for the first region, as it is assumed that the separation
 3302 can be achieved using dE/dx only. For the last region, I generated particles up to a
 3303 momentum of 10 GeV/c , as that is well above the typical energies of muons and pions
 3304 from FHC neutrino interactions in ND-GAr.

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Table 6.2: Momentum ranges and description of the PID approach assumed for the muon and pion classification task.

Momentum range	Description
$< 0.1 \text{ GeV}/c$	All tracks can be separated with dE/dx
$[0.1, 0.3) \text{ GeV}/c$	Use ECal for reaching muons and pions, dE/dx for the rest
$[0.3, 0.8) \text{ GeV}/c$	Use ECal for muons and pions, dE/dx for protons
$[0.8, 1.5) \text{ GeV}/c$	Use ECal and MuID for muons and pions, dE/dx for protons
$[1.5, 3.0) \text{ GeV}/c$	Use ECal and MuID for muons and pions, ToF for protons
$\geq 3.0 \text{ GeV}/c$	Use ECal and MuID for muons and pions, dE/dx and ToF for protons

3305 Additionally, I prepared another sample of 100000 FHC neutrino events. For each
 3306 interaction, I select the reconstructed particles which were backtracked to true muons or
 3307 charged pions. I use this dataset to perform validation checks, to see how the models
 3308 trained with the single particle data generalise to a more realistic scenario.

3309 To tackle this classification problem, I make use of Boosted Decision Trees (BDT). A
 3310 decision tree uses a flowchart-like structure to make decisions based on some input data.
 3311 It starts from a root node, which represents the complete dataset, and then it splits
 3312 this based on the variable or feature which gives the best separation between classes,
 3313 creating two new nodes. The process repeats for each node until it reaches a certain
 3314 limit, like a maximum number of splits or some tolerance criteria. The last set of nodes
 3315 are often called leave nodes, and represent the final prediction of the classifier.

3316 Boosting refers to a family of methods to combine the predictions from multiple
 3317 classifiers, following a sequential approach where each new model learns from the errors
 3318 of the previous one. The process starts with a simple decision tree, which is used to
 3319 make predictions on the training data. Then, the data points misclassified by the first
 3320 model are assigned higher weights, and another decision tree is trained on the data with
 3321 adjusted weights. The predictions of the two trees are then combined, and the cycle
 3322 repeats for a predefined number of iterations. Gradient boosting uses the direction of
 3323 the steepest error descent to guide the learning process and improve the accuracy with
 3324 each iteration.

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3325 6.3.3 Feature selection and importance

3326 Using the reconstructed tracks as a starting point, I compute a number of ECal and
3327 MuID variables for each of them. As there can be more than one cluster associated to a
3328 track, what I do is collect all associated clusters and compute these variables from the
3329 complete collection of associated hits. For the MuID, because it only features three layers
3330 and typically there will be less hits, I also allow single hits to be associated with tracks⁷.
3331 I can roughly divide the variables in three types: energy-related, geometry-related and
3332 statistical. In the following, I briefly describe the variables related exclusively to the
3333 ECal:

3334 • Energy-related ECal

- 3335 – ECal total energy (ClusterTotalEnergy): sum of the energy of all the ECal
3336 hits.
- 3337 – Mean ECal hit energy (HitMeanEnergy): mean of the hit energy distribution.
- 3338 – Standard deviation ECal hit energy (HitStdEnergy): standard deviation of
3339 the hit energy distribution.
- 3340 – Maximum ECal hit energy (HitMaxEnergy): maximum of the hit energy
3341 distribution.

3342 • Geometry-related ECal

- 3343 – Mean distance hit-to-cluster (DistHitClusterMean): mean of the distance
3344 distribution between the hits and the corresponding cluster's main axis.
- 3345 – RMS distance hit-to-cluster (DistHitClusterRMS): root mean square of the
3346 distance distribution between the hits and the corresponding cluster's main
3347 axis.

⁷At the reconstruction level what happens is that non-clustered hits are put into single hit clusters, instead of being thrown away. This is necessary to keep the consistency of the track-cluster association code.

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- 3348 – Maximum distance hit-to-centre (DistHitCenterMax): maximum of the
3349 distance distribution between the hits and the centre of the TPC.

3350 – Time-of-Flight velocity (TOFVelocity): slope obtained when fitting a straight
3351 line to the hit time versus hit distance to the centre (i.e. $d = v \times t$).

3352 • Energy and geometry ECal

- 3353 – Radius 90% energy (Radius90E): distance in the hit-to-cluster distribution
3354 for which 90% of the total energy is contained in the hits that are closer to
3355 the axis (i.e. radius that contains 90% of the energy).

3356 • Statistical ECal

- 3357 – Number of hits (NHits): total number of hits associated to the track.

3358 – Number of layers with hits (NLayers): not really a count of all layers with
3359 hits but the difference between the last and the first layer with hits.

3360 Figure 6.21 shows the distributions of three different ECal variables, separating true
3361 muons (blue) and charged pions (red), for the five momentum ranges considered. I chose
3362 to show one feature from each category, namely the mean energy per hit (left column),
3363 the mean distance between the hits and the centre of the cluster (middle column), and
3364 the number of ECal layers with hits (right column). These give an idea of the separating
3365 power of the different features, and how it changes considerably with the energy. In
3366 the number of layers with hits distributions, the peak at 6 is due to the fact that the
3367 first six ECal layers sit inside the pressure vessel⁸. Therefore, some of the particles get
3368 stopped crossing it, never making it to the seventh layer.

3369 In the case of the MuID, because at low momenta a significant fraction of the particles
3370 do not make it past the ECal, I only consider the information coming from this detector
3371 for momenta ≥ 0.8 GeV/c, i.e. for the last three momentum regions. The variables I
3372 extract from it are the following:

⁸Note to self: check this. I thought the ECal barrel had 8 layers of tiles, and that all of them were inside the pressure vessel.

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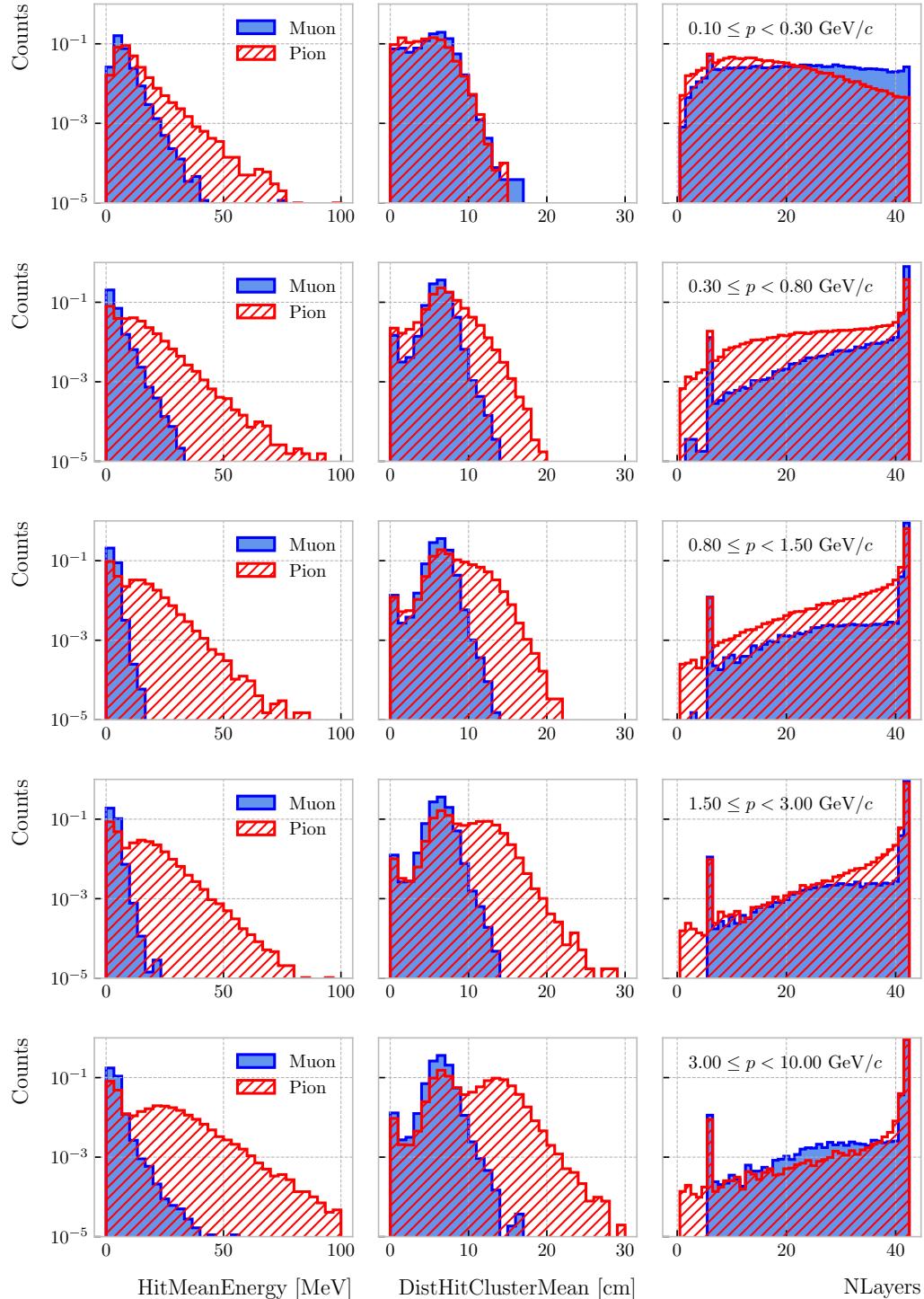


Figure 6.21: Example ECal feature distributions for muons (blue) and charged pions (red) in the five different momentum ranges considered (from top to bottom, in ascending momentum order). From left to right: mean hit energy, mean distance hit-to-cluster, and number of layers with hits.

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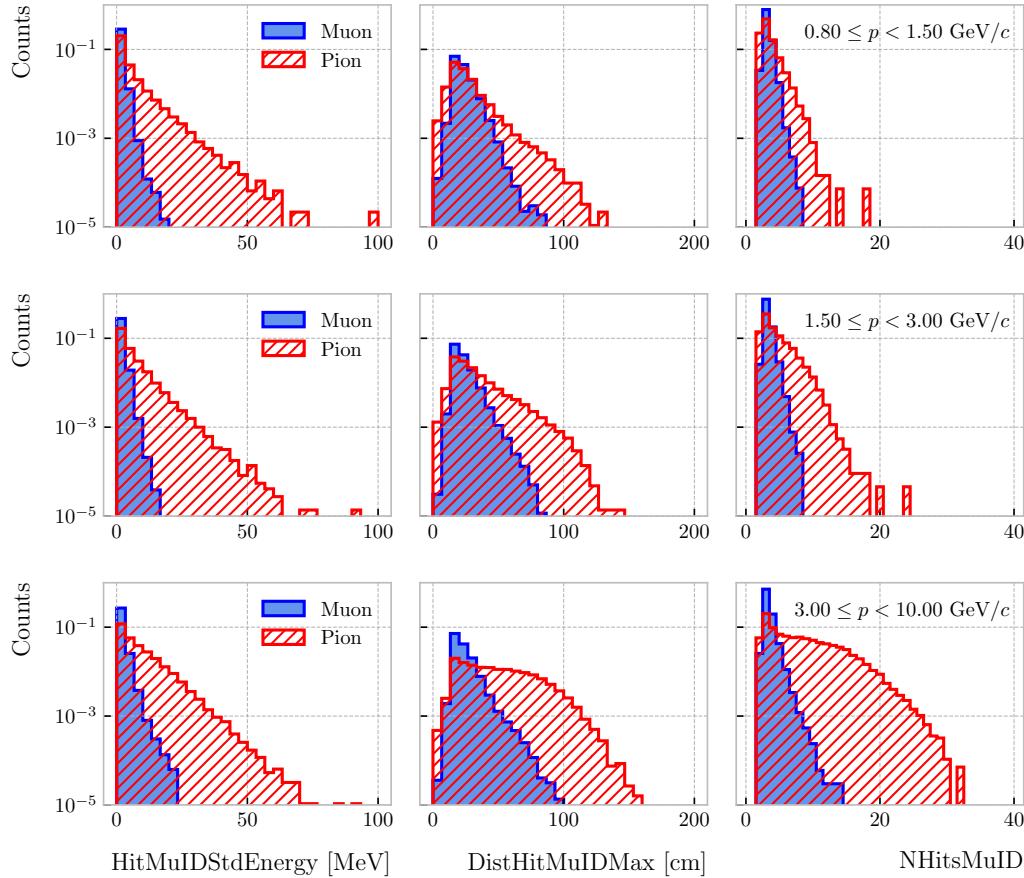


Figure 6.22: Example MuID feature distributions for muons (blue) and charged pions (red) in the three different momentum ranges considered (from top to bottom, in ascending momentum order). From left to right: standard deviation hit energy, maximum distance hit-to-hit, and number of hits.

3373 • Energy-related MuID

- 3374 – MuID total energy (ClusterMuIDTotalEnergy): sum of the energy of all the
- 3375 MuID hits.
- 3376 – Mean MuID hit energy (HitMuIDMeanEnergy): mean of the MuID hit energy
- 3377 distribution.
- 3378 – Standard deviation MuID hit energy (HitMuIDStdEnergy): standard deviation
- 3379 of the MuID hit energy distribution.
- 3380 – Maximum MuID hit energy (HitMuIDMaxEnergy): maximum of the MuID
- 3381 hit energy distribution.

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• Geometry-related MuID

- 3383 – Maximum distance MuID hit-to-hit (DistHitMuIDMax): maximum distance
- 3384 between pairs of MuID hits (not sure this is a good variable, distribution
- 3385 looks nuts).
- 3386 – Maximum distance MuID hit-to-centre (DistHitCenterMuIDMax): maximum
- 3387 of the distance distribution between the MuID hits and the centre of the
- 3388 TPC.

• Statistical MuID

- 3389 – Number of hits (NHitsMuID): total number of MuID hits associated to the
- 3390 track.
- 3392 – Number of layers with hits (NLayersMuID): not really a count of all layers
- 3393 with MuID hits but the difference between the last and the first layer with
- 3394 MuIDhits.

3395 Figure 6.22 shows the distributions of three different MuID variables, separating true
3396 muons (blue) and charged pions (red), for the three momentum ranges which use the
3397 muon tagger information. In this case I decided to standard deviation of the MuID hit
3398 energy distribution (left column), the maximum distance between the MuID hit pairs
3399 (middle column), and the number of MuID hits (right column). These variables are used
3400 together with the ECal features at high momenta, providing additional disambiguation
3401 power.

3402 Once our features have been defined, one can do some exploratory analysis to
3403 understand how well the variables describe the target class, and avoid the black-box
3404 approach by what features are most relevant for the learning process. This way, I
3405 performed a feature analysis for each of the momentum ranges I divided this classification
3406 problem into. It follows three steps: first a principal component analysis (PCA), followed
3407 by a feature importance study using Gini and Shapley values, and finally a feature
3408 permutation importance analysis.

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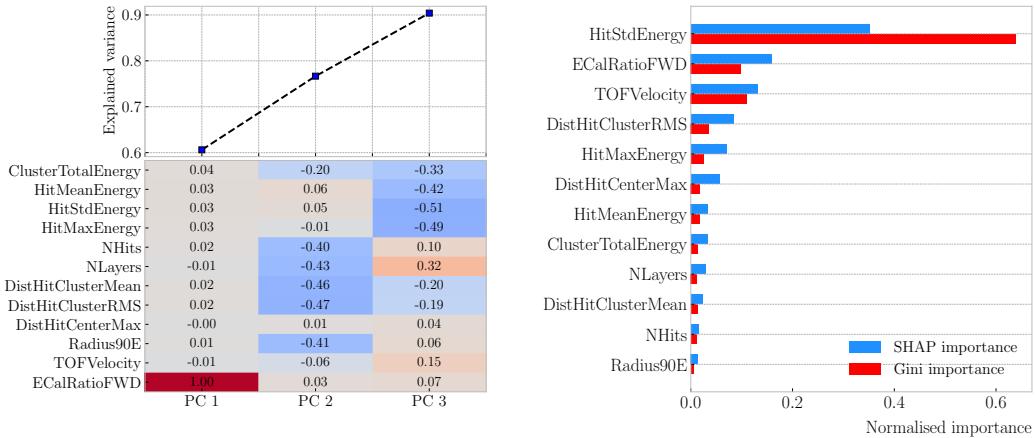


Figure 6.23: Left panel: cumulative explained variance for the first three principal components (top panel) and contribution of the different features to the principal axes in feature space (bottom panel). Right panel: Shapley (blue) and Gini (red) feature importances for the different input features. Both figures correspond to the samples in the momentum range $0.3 \leq p < 0.8 \text{ GeV}/c$.

The PCA is useful to understand the variance of the feature space. It is an unsupervised machine learning technique that allows the user to perform a dimensionality reduction. It uses a singular value decomposition of the input features to project them into a lower dimensional space. The idea is to find the matrix \mathbf{C}_m , whose columns are the first m orthonormal eigenvectors of the input covariance matrix. Consider the $n \times p$ real matrix of input data \mathbf{X} , where n is the number of samples and p the number of features. If \mathbf{X} is centred, i.e. the means of its columns are equal to zero, we can write the covariance matrix of \mathbf{X} as $\mathbf{C} = \mathbf{X}^\top \mathbf{X} / (n - 1)$. This matrix can be diagonalised, yielding:

$$\mathbf{C} = \mathbf{V} \mathbf{L} \mathbf{V}^\top, \quad (6.11)$$

where \mathbf{V} is a matrix of eigenvectors and \mathbf{L} a diagonal matrix with eigenvalues λ_i . Then, performing SVD on \mathbf{X} gives us:

$$\mathbf{X} = \mathbf{U} \mathbf{S} \mathbf{W}^\top, \quad (6.12)$$

where \mathbf{U} is a unitary matrix, whose columns are called left singular vectors, \mathbf{S} is a diagonal matrix of single values s_i , and \mathbf{W} is another unitary matrix, its columns known

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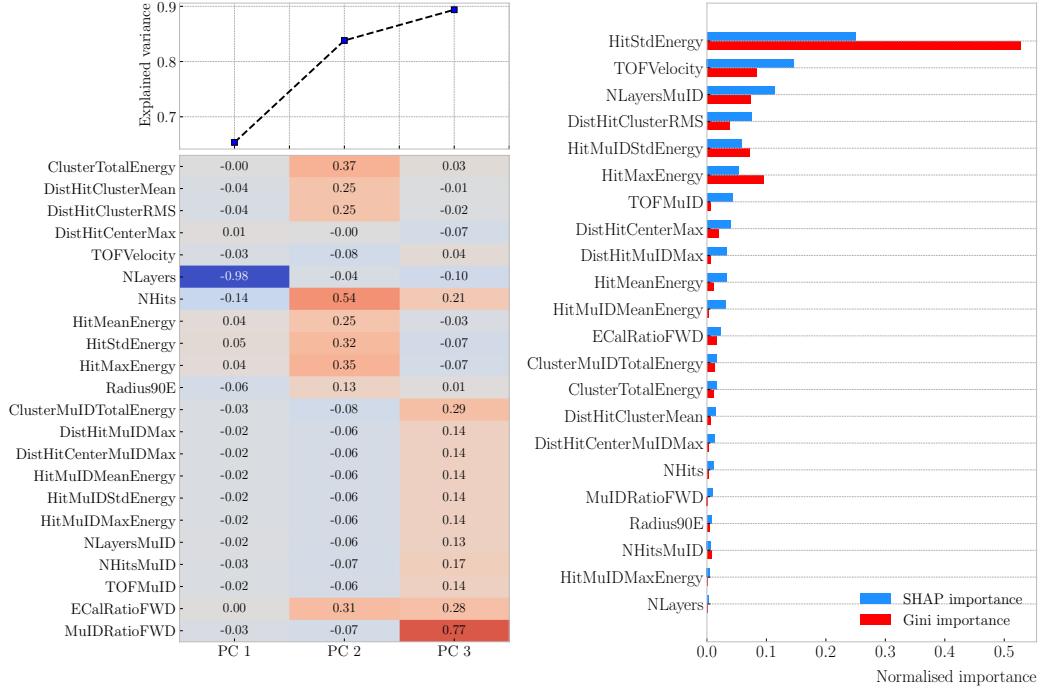


Figure 6.24: Left panel: cumulative explained variance for the first three principal components (top panel) and contribution of the different features to the principal axes in feature space (bottom panel). Right panel: Shapley (blue) and Gini (red) feature importances for the different input features. Both figures correspond to the samples in the momentum range $0.8 \leq p < 1.5$ GeV/c.

as right singular vectors. This way, we can write:

$$\mathbf{C} = \mathbf{W}\mathbf{S}\mathbf{U}^\top\mathbf{U}\mathbf{S}\mathbf{W}^\top/(n-1) = \mathbf{W}\frac{\mathbf{S}^2}{n-1}\mathbf{W}^\top. \quad (6.13)$$

meaning that the right singular vectors are also the eigenvectors of the covariance matrix.

The SVD can be computed numerically following an iterative approach.

This way, taking an input data vector $X \in \mathbb{R}^n$, the resulting feature vector $Y \in \mathbb{R}^m$

is given by:

$$Y = \mathbf{C}_m^\top X. \quad (6.14)$$

The new features capture most of the variance of the original sample, while being lower dimensional, as $m < n$.

Before applying the PCA reduction one needs to centre and scale the input data.

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3429 Centring is necessary when using SVD to obtain the eigenvectors of the covariance
3430 matrix, as only in that case we can do the identification with the right singular vectors
3431 from the input data. Scaling is needed when variables are on different scales, as some
3432 can then dominate the PCA procedure.

3433 I used the PCA module of `scikit-learn`, together with the `RobustScaler`, which
3434 centres the data and scales it based on the interquartile range. In Fig. 6.23 (left panel)
3435 and Fig. 6.24 (left panel) I show the results I obtained from the PCA for the momentum
3436 ranges $0.3 \leq p < 0.8 \text{ GeV}/c$ and $0.8 \leq p < 1.5 \text{ GeV}/c$, respectively. Notice that in
3437 the second case the number of features increases considerably, as this is the first region
3438 which uses the MuID variables. I found that, in all the cases, adding a fourth PC does
3439 not add additional information. As it can be seen in the top panels of the figures, the
3440 cumulative explained variance is already over 80% with three PCs.

3441 The bottom panels show the contribution of the variables to the principal axes. For
3442 the two first momentum regions, I observe a tendency of the energy-related and the
3443 geometry-related ECal variables to be clustered together. For the other ranges, when
3444 I include the MuID variables, there seems to be a division between ECal and MuID
3445 variables. For these, it seems like the number of ECal layers with hits also plays an
3446 important role.

3447 The next step in the analysis is to quantify the importance of the features based on
3448 two additional metrics, namely the Gini and the Shapley values. The Gini importance,
3449 often called mean decrease impurity, is based on how much a feature contributes to the
3450 purity improvement at the splits in each decision tree. The purity is measured in terms
3451 of the Gini impurity index, defined as:

$$I_G = 1 - \sum_i f_i, \quad (6.15)$$

3452 where f_i is the fractional abundance of the i -th class. Then, for each split one can

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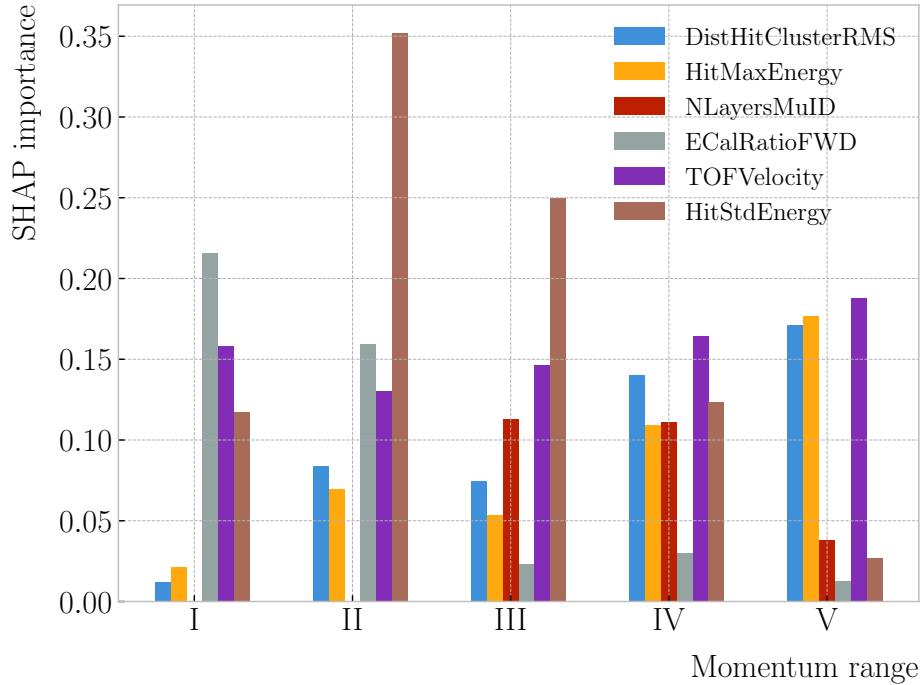


Figure 6.25: Evolution of the SHAP importance for the top six most important features across all five momentum ranges.

3453 compute the weighted decrease in impurity as:

$$\Delta_G = \frac{N_t}{N} \left(I_G - \frac{N_t^R}{N_t} I_G^R - \frac{N_t^L}{N_t} I_G^L \right), \quad (6.16)$$

3454 where N represents the total number of samples, N_t the number of samples at the current
 3455 node, N_t^R and N_t^L the number of samples in the right and left children respectively,
 3456 I_G is the Gini impurity at the current node, and I_G^R and I_G^L the Gini impurities of the
 3457 resulting right and left children.

3458 For each decision tree, one will have a normalised vector with the accumulated
 3459 decrease in Gini impurity for each feature. In the case of a BDT, the feature importances
 3460 are simply the mean for all the estimators in the ensemble⁹.

3461 The concept of Shapley values originated in the context of game theory, and it
 3462 measures the marginal contribution of a feature in enhancing the accuracy of a classifier.

⁹Note to self: this appears not to be the case. If you get the `feature_importance` for each tree in the BDT and take the average, the result is not the same to be one reported in the `feature_importance` attribute of the BDT.

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3463 Take F to be the set of all features in a problem, and $S \subseteq F$ the subset of features. To
 3464 compute the Shapley value of the i -th feature, one has to train a model with that feature
 3465 present, $f_{S \cup \{i\}}$, and another model trained without it, f_S . This has to be repeated for
 3466 all possible combinations of subsets $S \subset F \setminus \{i\}$, and evaluating the models predictions
 3467 on the appropriate sets of data x_S . This way, the Shapley value results:

$$\varphi_i = \sum_{S \subset F \setminus \{i\}} \frac{|S|! (|F| - |S| - 1)!}{|F|!} [f_{S \cup \{i\}}(x_{S \cup \{i\}}) - f_S(x_S)]. \quad (6.17)$$

3468 I trained the `GradientBoostingClassifier` from `scikit-learn` with the default
 3469 configuration in order to evaluate both the Gini and Shapley importances. The Gini
 3470 scores are automatically computed by `scikit-learn`, using the training data. For the
 3471 Shapley importance, I used the implementation from the `SHAP` package, computing
 3472 it using the test sample. The results can be seen in Fig. 6.23 (right panel) and
 3473 Fig. 6.24 (right panel), again for the momentum ranges $0.3 \leq p < 0.8 \text{ GeV}/c$ and
 3474 $0.8 \leq p < 1.5 \text{ GeV}/c$. The length of the bars denote either the SHAP (blue) or the Gini
 3475 (red) importance of the feature. One interesting thing to notice is that, when looking at
 3476 the Gini importance, there is always one feature that dominates over the rest. This is
 3477 not the case for the SHAP importance, where importances tend to be more balanced.

3478 Across all momentum ranges, I observe that the most important features are. For
 3479 the five momentum ranges considered, only six variables sit in the top five at least once.
 3480 Figure 6.25 shows the evolution of the SHAP importance of these six features. It is
 3481 interesting to see that the time-of-flight variable keeps its importance almost unchanged
 3482 for all momenta. Also, it looks like the ECal energy ratio gets less relevant the higher the
 3483 momentum is, but the RMS of the hit-to-cluster distance distribution and the maximum
 3484 ECal hit energy become more important in the last momentum ranges.

3485 The last step in the feature selection analysis is the feature permutation. This
 3486 technique measures the contribution of each feature to the performance of a model by
 3487 randomly shuffling its values and checking how some scores degrade. For the present
 3488 case, I am interested in the precision or purity, and the sensitivity or efficiency, as these

6.3. MUON AND PION SEPARATION IN THE ECAL AND MUID

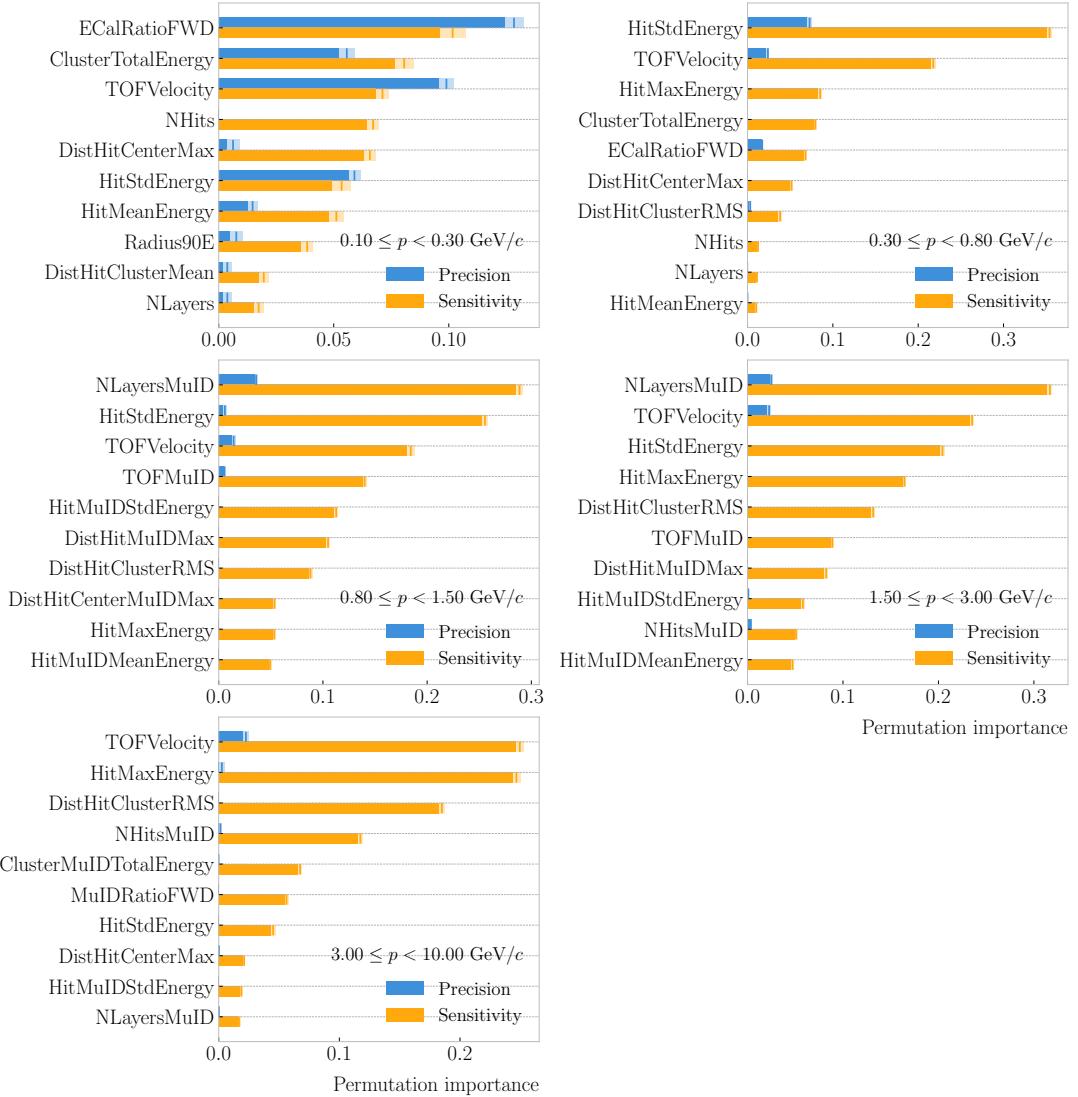


Figure 6.26: Permutation importances for the ten most important features in the different momentum ranges (from left to right, top to bottom, in increasing momentum order). The bars indicate the effect that permutations of each feature have on the purity (blue) and the sensitivity (yellow), the translucent regions representing one standard deviation around the central value.

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3489 two are the most relevant metrics from a physics point of view. The `scikit-learn`
3490 module provides the user with a method to perform the permutation scans.

3491 The results of these are shown in Fig. 6.26. For the different momentum ranges
3492 I show the permutation importances for the ten most important features. For each
3493 of the variables I report the effect the permutations have on the precision (blue) and
3494 sensitivity (yellow) of the models. The bars indicate the importance value, with the
3495 lighter part representing one standard deviation around the mean (hinted as an additional
3496 vertical line). Something to notice is that, in the first momentum region, the feature
3497 permutations have an effect on both the precision and the sensitivity. However, for the
3498 rest the precision is almost unaffected, while the sensitivity changes are considerably
3499 larger.

3500 It is also interesting to see that most of the variables identified as important here
3501 are the same I found when looking at the Shapley values. The behaviour of these across
3502 the momentum ranges is also similar, with the same patterns of some features being
3503 important at low momenta and then dropping in importance for the high momentum
3504 ranges.

3505 Wit this, I conclude the study of the features. I have prepared the training and
3506 testing datasets and understood what features are likely to have the largest impact on
3507 the performance of the classifiers.

3508 6.3.4 Hyperparameter optimisation

3509 Any BDT requires the user to specify a number of parameters that will dictate its
3510 behaviour. They can be divided into two categories: (i) tree-specific parameters, which
3511 affect each individual tree in the model, and (ii) boosting parameters, which control the
3512 boosting operation in the model. The value of these so-called hyperparameters affect the
3513 performance and predictive power of the models. Therefore, one needs to carefully select
3514 their optimal values in order to extract as much information as possible from the data.

3515 From all the parameters used to define a tree in the `scikit-learn` implementation
3516 of the BDT classifier, I only consider a subset of them. This is due to the fact that some

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3517 are mutually exclusive, but also because I noticed that others have little effect on the
3518 problem at hand. Therefore, the parameters I investigate are the following:

- 3519 • `min_samples_split`: defines the minimum number of samples required in a node
3520 to be considered for splitting. Higher values prevent a model from learning relations
3521 which might be highly specific to the particular sample, but may lead to under-fitting
3522 if the value is too low.
- 3523 • `min_samples_leaf`: defines the minimum samples required in a leaf node. For
3524 imbalanced problems it should take a low value, as there will not be many cases
3525 where the minority class dominates.
- 3526 • `max_depth`: maximum depth of a tree. Useful to prevent over-fitting, as higher
3527 depth will allow a model to learn relations specific to the training sample.

3528 In the case of the boosting parameters, the ones I look at are:

- 3529 • `learning_rate`: determines the impact of each tree on the final outcome. Low
3530 values make the model robust to the specific characteristics of a tree, and thus
3531 allow it to generalise well. However, that usually requires a large number of trees
3532 to model the data properly.
- 3533 • `n_estimators`: number of sequential trees to be trained. In general, BDTs are
3534 fairly robust at higher number of trees but it can still overfit at a point.
- 3535 • `subsample`: fraction of observations to be selected for each tree. Values slightly
3536 less than 1 make the model robust by reducing the variance.

3537 In general, hyperparameters depend on each other. Thus, it is not possible to
3538 optimise them independently. In the literature, we find two main strategies to explore
3539 the hyperparameter space. We could use a grid search, in which one discretises a
3540 portion of the space of hyperparameters and evaluates the model at each point. Another
3541 approach is the randomised search, where a certain number of random configurations of
3542 hyperparameters are explored.

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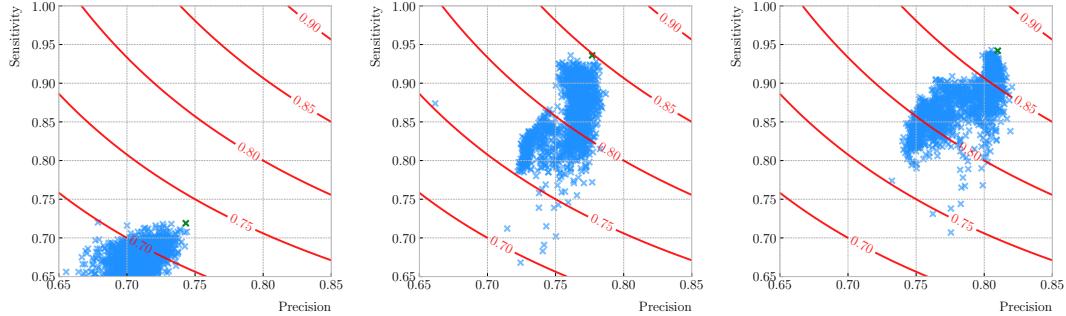


Figure 6.27: Values of the precision and sensitivity obtained for 10000 BDT hyperparameter configurations, for the momentum regions I, III and V. The red contours indicate the curves of equal F_1 -score, while the green crosses are the selected configurations.

3543 In this case, I used the random search to scan the hyperparameter space. Also,
 3544 because it is not guaranteed that a set of hyperparameters can be efficiently applied
 3545 across different datasets, I perform the optimisation for each of the momentum ranges
 3546 considered. Table 6.3 shows the list of hyperparameters considered, and the range within
 3547 which I let them vary. I decided to fix the number of estimators to 400 in all cases, as
 3548 its value is correlated with that of the learning rate.

3549 I evaluate 10000 different hyperparameter configurations for each momentum range.
 3550 For the hyperparameter tuning, I used subsamples containing 10% of the full datasets,
 3551 keeping the original proportions between classes, in order to reduce the computational
 3552 load. The performance of the models was assessed using a stratified 3-fold cross-validation
 3553 with replacement. Cross-validation involves dividing the data in a number of subsets,
 3554 training the model using some of them, and testing it with the rest. In our case, I
 3555 divide the data in 3 equal-sized subsets, maintaining the class proportions of the original
 3556 dataset. Then, for 3 consecutive iterations, I train the models using 2 of the subsets
 3557 while I compute the precision and sensitivity scores with the other. This approach
 3558 provides a more robust estimate of the performance on unseen data.

3559 Figure 6.27 shows the results in the precision versus sensitivity plane, for the
 3560 momentum regions I, III and V (from left to right). The contours represent the curves
 3561 of equal F_1 -score, i.e. the harmonic mean of the precision and the sensitivity. In order

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Table 6.3: Optimal values of the hyperparameters used by the BDT, for each momentum range.

Hyperparameter	Range	Best value				
		I	II	III	IV	V
<code>min_samples_split</code>	[0.001, 1]	0.10	0.06	0.05	0.27	0.06
<code>min_samples_leaf</code>	[0.001, 1]	0.02	0.03	0.01	0.02	0.07
<code>max_depth</code>	{2, 3, ..., 8}	8	2	4	2	7
<code>learning_rate</code>	[0.05, 1]	0.10	0.23	0.07	0.13	0.09
<code>subsample</code>	[0.01, 1]	0.75	0.65	0.79	0.86	0.95

Table 6.4: Performance metrics of the BDTs with optimal hyperparameters, for the different momentum ranges.

Metric	Value $\pm 1\sigma$				
	I	II	III	IV	V
Accuracy	0.779 ± 0.003	0.812 ± 0.003	0.846 ± 0.002	0.861 ± 0.003	0.874 ± 0.002
Precision	0.769 ± 0.003	0.752 ± 0.005	0.788 ± 0.002	0.805 ± 0.003	0.815 ± 0.003
Sensitivity	0.745 ± 0.009	0.921 ± 0.006	0.965 ± 0.002	0.967 ± 0.002	0.976 ± 0.001
F_1 -score	0.757 ± 0.004	0.828 ± 0.003	0.867 ± 0.002	0.879 ± 0.002	0.889 ± 0.002
ROC AUC	0.868 ± 0.003	0.865 ± 0.003	0.899 ± 0.002	0.902 ± 0.002	0.911 ± 0.001

3562 to select the optimal configurations (indicated in the plots with a green cross), I chose
 3563 the point with the highest F_1 -score.

3564 The results for the different momentum ranges are summarised in Tab. 6.3. One
 3565 can see some consistency in hyperparameter choices, with models generally preferring
 3566 small values for the tree-specific parameters, small learning rate, and relatively large
 3567 subsample sizes.

3568 Now that I have obtained the optimal values of the hyperparameters, I can train
 3569 the different BDTs. In this case I use the complete datasets, keeping 20% of the data
 3570 for testing. Table 6.4 shows the values of the different performance metrics obtained
 3571 using the selected hyperparameters and 5-fold cross-validation. The last row indicates
 3572 the value of the area under the receiver operating characteristic (ROC) curve. This
 3573 represents the sensitivity of a model as a function of the false positive rate. I have

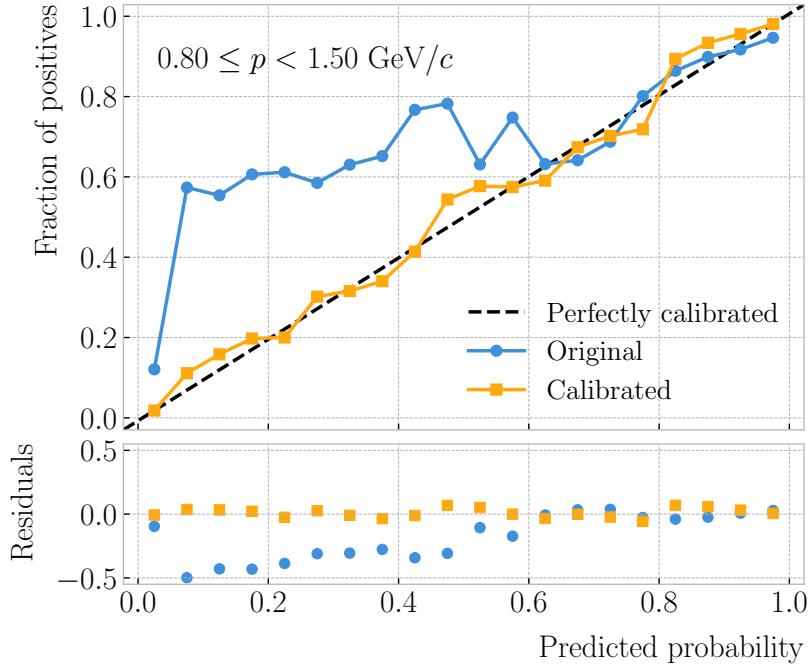


Figure 6.28: Reliability diagrams for the BDT classifier used in the momentum range $0.3 \leq p < 0.8 \text{ GeV}/c$, both for the original (blue circles) and calibrated (yellow squares) responses. For reference, the response of a perfectly calibrated classifier is also shown (black dashed line).

3574 included it here as it is a classic model metric used in the machine learning community.

3575 Overall, there is a clear trend of models performing better at higher momentum.

3576 6.3.5 Probability calibration

3577 So far, the trained BDTs are able to provide predictions of the class labels. Ideally,
 3578 one would like the output of a classifier to give a confidence level about the prediction.
 3579 However, it is not straightforward to interpret the outputs of our BDTs in terms of
 3580 probabilities.

3581 A way to visualise how well the predictions of a classifier are calibrated is using
 3582 reliability diagrams [160]. They represent the probability of the positive label versus the
 3583 probability predicted by the classifier. These can be obtained by binning the predicted
 3584 probabilities, and then compute the conditional probability $P(y_{true} = 1 | y_i \leq y_{pred} <$
 3585 $y_{i+1})$ by checking the fraction of true positive instances in each bin. The reliability

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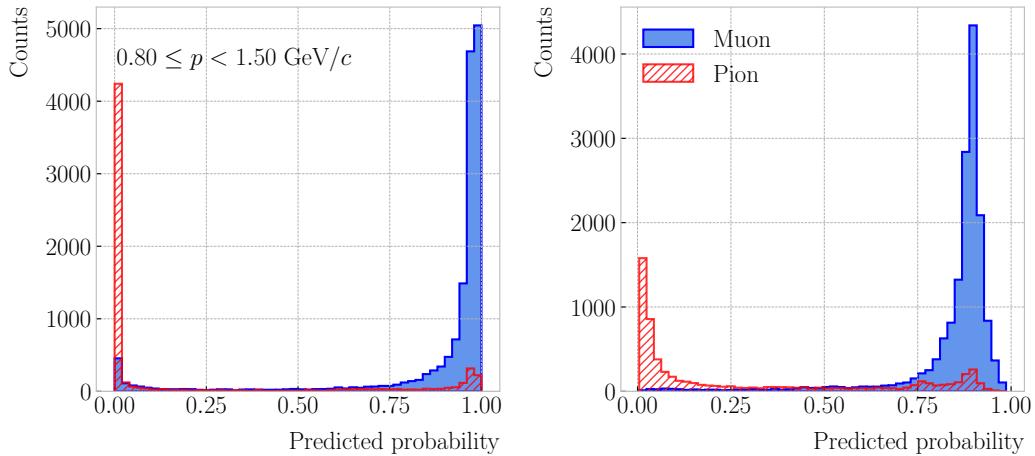


Figure 6.29: Uncalibrated (left panel) and calibrated (right panel) predicted probabilities assigned by the BDT classifiers for true muons (blue) and charged pions (red) in the momentum range $0.3 \leq p < 0.8 \text{ GeV}/c$.

3586 diagram of a perfectly calibrated classifier would be a diagonal line.

3587 In this case, I try to correct the raw response of the classifiers by applying a sigmoid
3588 function:

$$\sigma(x; A, B) = \frac{1}{1 + e^{Ax+B}}, \quad (6.18)$$

3589 where the parameters A and B are real numbers determined using the method of least
3590 squares.

3591 For each classifier, I perform a grid search to obtain the optimal values of A and B .
3592 For any pair, I compute the predicted probabilities as $y_{pred} = \sigma(y_{raw}; A, B)$, where y_{raw}
3593 are the raw predictions of the classifier¹⁰. Then, I calculate the corresponding reliability
3594 curve, and take the sum of the squared residuals between it and the response of the
3595 perfectly calibrated classifier.

3596 Figure 6.28 shows the reliability diagrams for the original (blue) and calibrated
3597 (yellow) probability predictions of the classifier for the III momentum range, $0.3 \leq p <$
3598 $0.8 \text{ GeV}/c$. The original response of the classifier is given by $y_{pred} = \sigma(y_{raw}; -2, 0)$,
3599 which is the transformation applied by `scikit-learn` to produce the probability estimate.
3600 Notice how the calibrated prediction matches the ideal response much better than the

¹⁰In `scikit-learn` these correspond to the outputs of the `decision_function` method.

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3601 original, across all the probability range.

3602 One can also compare the responses of the uncalibrated and calibrated classifiers
3603 broken down by true particle type, as shown in Fig. 6.29. It can be seen that the
3604 distributions for both muons (blue) and charged pions (red) smoothen after calibration,
3605 but still the separating power of the classifier remains unchanged.

3606 At this point, having the trained classifiers and the probability calibration parameters,
3607 I am able to assess the performance of the classification strategy in a physics-relevant
3608 case.

3609 6.3.6 Performance

3610 6.4 ECal time-of-flight

3611 Looking at Fig. 6.20, it is clear that for momentum values in the range $1.0 - 3.0 \text{ GeV}/c$
3612 it is not possible to separate pions and protons using a $\langle dE/dx \rangle$ measurement in the
3613 HPgTPC. However, in the previous section I assumed that protons at those energies
3614 could be identified by other means, and therefore were not an issue for the muon and
3615 pion discrimination.

3616 Some detectors, like ALICE [161] or the ILD concept [162], complement the PID
3617 capabilities of their gaseous trackers with time-of-flight measurements. The use of
3618 fast timing silicon sensors, with hit time resolutions under 100 ps, would allow for the
3619 identification of charged hadrons via a ToF measurement up to $5.0 \text{ GeV}/c$. In the case
3620 of ND-GAr, one could think of using the inner layers of the ECal, the ones consisting of
3621 high-granularity tiles, to obtain a ToF-based PID, with some inputs from the TPC.

3622 Measuring the momentum and the velocity of a charged particle allows for a
3623 determination of the mass through the relativistic momentum formula:

$$m = \frac{p}{\beta} \sqrt{1 - \beta^2}. \quad (6.19)$$

3624 In our case, the momentum is measured in the TPC, using the curvature and the dip

6.4. ECAL TIME-OF-FLIGHT

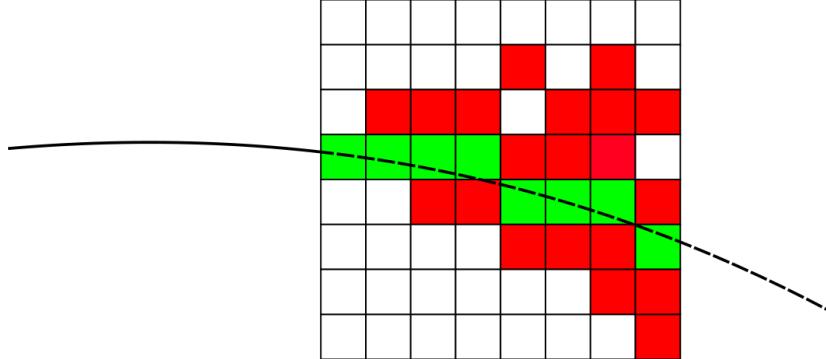


Figure 6.30: Schematic of the hit selection used for the ToF measurement. The grid represents the layers of the inner ECAL, with coloured squares indicating the tiles with hits. Green squares indicate the selected hits.

angle of the helix inside the magnetic field. The velocity of the particle can be written as:

$$\beta = \frac{\ell_{track}}{c\tau}, \quad (6.20)$$

where ℓ_{track} is the length of the track, and τ the arrival time to the ECAL.

In GArSoft, the track length is computed at the Kalman filter stage. It is simply the sum of the line segments along the track, either in the forward or backward fit. In this case, because we are only interested in the particles that make it to the ECAL, I choose the fit direction based on the results of the track-cluster associations.

Additionally, because the last 30 cm of the TPC radius are uninstrumented¹¹, I need to correct for the length of the tracks. Using the track fit parameters to propagate the helix to its entry point in the ECAL, one can write the total track length as:

$$\ell_{track} = \ell + \left| \frac{\phi_{EP} - \phi}{R^{-1}} \right| \sqrt{1 + \tan^2 \lambda}, \quad (6.21)$$

where ϕ_{EP} is the angle of rotation at the entry point to the calorimeter, and ℓ , ϕ , R and λ are the track length, angle of rotation, radius of curvature and dip angle at the last point in the fit, respectively.

To test the idea of performing a ToF measurement with the inner ECAL, I generated

¹¹Note to self: check this number.

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3639 two data samples. Each consists of 10000 single particle events, either charged pions or
3640 protons. Their momenta are uniformly distributed in the range $0.5 - 5.0 \text{ GeV}/c$, and
3641 their directions are isotropic. I process each sample using different values of the time
3642 resolution, from $\Delta\tau = 0$, the perfect time resolution case for comparison, to the current
3643 nominal value of $\Delta\tau = 0.7 \text{ ns}$, and the worse scenario of $\Delta\tau = 1.0 \text{ ns}$.

3644 6.4.1 Arrival time estimations

3645 In the simulation, the limited time resolution of the ECal is taken into account by
3646 applying a Gaussian smearing to the true hit times. Other effects, like the digitisation
3647 of the signals, are not taken into account and fall beyond the scope of this study. After
3648 the track-cluster, one ends up with a collection of ECal hits associated to each particle.
3649 From these, the arrival time of the particle to the ECal can be extracted.

3650 The simplest possibilities are to either take the time of the earliest hit or the hit
3651 closest to the entry point. Because these two coincide, in general, I focused only in
3652 the earliest hit time. However, this needs to be corrected, to account for the distance
3653 travelled from the entry point to the position of the hit:

$$\tau_{earliest} = \tau_{hit} - \frac{d_{EP-hit}}{c}, \quad (6.22)$$

3654 where τ_{hit} is the time of the earliest hit, and d_{EP-hit} is the distance between that hit
3655 and the entry point of the particle to the ECal. This is computed as the arc length
3656 between the entry point and the point of the extrapolated helix up to the layer of the
3657 hit. This way of correcting the time assumes c for the propagation of the particle, which
3658 may lead to biased estimates.

3659 I also tried to estimate the arrival times using information from the rest of the hits.
3660 In order to do this, as a simplifying assumption, I approximate the hadronic shower
3661 considering only its MIP component. For each layer, I keep only the hit in the tile closest
3662 to the point of the extrapolated track up to that layer. Figure 6.30 shows an example of
3663 how this hit selection works. The dashed line represents the extrapolated track, while

6.4. ECAL TIME-OF-FLIGHT

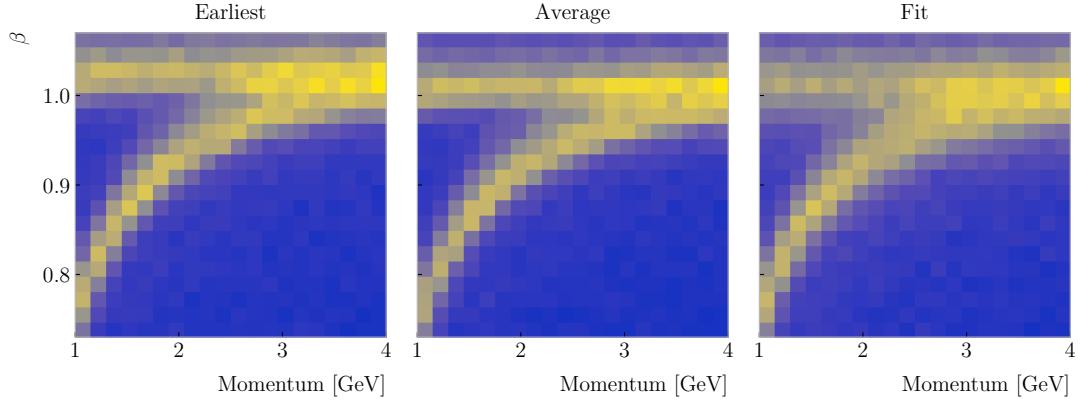


Figure 6.31: Particle velocity versus momentum measured with different ECal arrival time estimations. From left to right: earliest hit time, average hit time, and fitted hit time. In all cases the time resolution is $\Delta\tau = 0.1$ ns.

3664 the coloured squares are the tiles containing hits. Green indicates the tiles closer to the
 3665 track in each layer (in the sketch they correspond to the grid columns).

3666 Now, I can use these collections of hits to estimate the arrival times. A possibility
 3667 is to take the average of the times of the selected hits, denoted $\tau_{average}$. For that to
 3668 work, one needs to correct these times, in a similar way as in Eq. (6.22), before taking
 3669 the average. However, as before, this correction assumes that the particle travels at the
 3670 speed of light inside the ECal. Another option is to perform a linear fit to the hit times
 3671 and the distances to the entry point. In that case, the arrival time would be the fitted
 3672 value of the intercept, τ_{fit} . This method would not assume a speed of light propagation.

3673 Figure 6.31 shows the velocity estimations as a function of the particle momentum,
 3674 for the earliest hit time (left panel), average hit time (middle panel), and fitted hit time
 3675 (right panel). The two bands correspond to the π^\pm and the p particles. $\Delta\tau = 0.1$ ns.
 3676 Notice how, for the earliest hit time method, the velocities are significantly biased
 3677 towards larger values. For the multi-hit methods, the τ_{fit} estimate appears to produce a
 3678 larger variance than when using the $\tau_{average}$ method.

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3679 6.4.2 Proton and pion separation

3680 Once we have the velocities of the particles, one can estimate their masses through
3681 Eq. (6.19). The resulting mass spectra are shown in Fig. 6.32. I computed the masses
3682 for the three arrival time estimates discussed above, and three different values of the
3683 time resolution: $\Delta\tau = 0.00$ (perfect time resolution), $\Delta\tau = 0.10$ ns, and $\Delta\tau = 0.70$ ns.
3684 Although in all cases we have the same number of events, it appears as if the entries
3685 in the histograms decrease as the time resolution increases. Sometimes, the particles
3686 get unphysical values of $\beta > 1$, and in turn they do not contribute to the mass spectra.
3687 This is more likely to happen for higher values of $\Delta\tau$.

3688 As noted before, the average hit time method produces the most robust estimates
3689 when increasing $\Delta\tau$. Intuitively this makes sense, as by taking the mean one averages
3690 out the effect of the Gaussian smearing. Going forward, I will use this arrival time
3691 estimator, as it appears to be the best performing one.

3692 It is possible to use the velocity estimations to select a sample of protons. In this
3693 case, I do so by dividing the relevant momentum range in bins of $0.1 \text{ GeV}/c$. For each
3694 momentum bin, I compute the expected velocity for the protons via the inverse of Eq.
3695 (6.19), and then take the fractional residuals of the measured velocities. Using that
3696 distribution, I choose the cut that maximises the F_1 -score of the proton selection.

3697 The results can be seen in Fig. 6.33, for the case $\Delta\tau = 0.10$ ns. As expected from
3698 Fig. 6.31, the performance of the selection degrades rapidly with increasing momentum.
3699 However, the purity is still around 75% at $3.0 \text{ GeV}/c$. This is likely to be sufficient, as
3700 we do not expect protons or charged pions with higher energies from the beam neutrino
3701 interactions.

3702 Figure 6.34

3703 6.5 Charged pion decay in flight

3704 As discussed previously, in GArSoft the TPC tracks are formed after a pattern recognition
3705 algorithm and a Kalman filter are applied to the TPC clusters. These two steps can

6.5. CHARGED PION DECAY IN FLIGHT

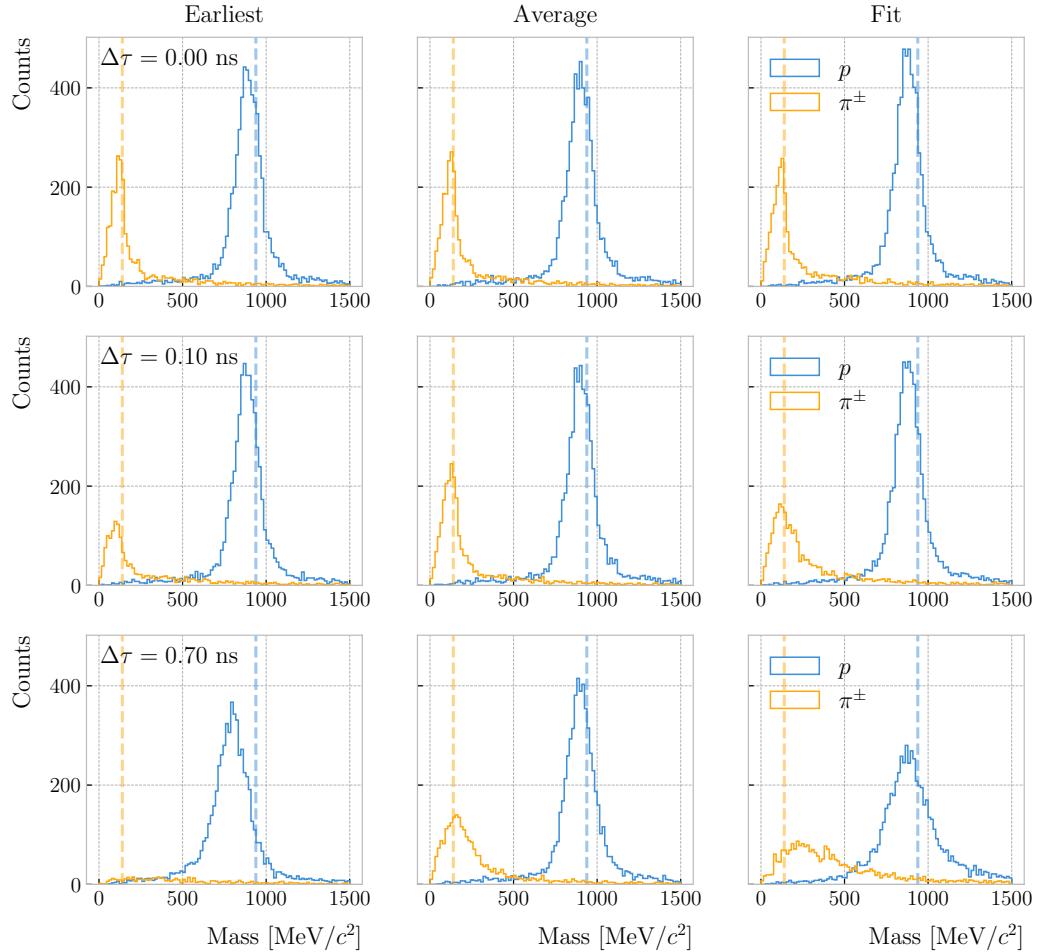


Figure 6.32: Mass spectra for p (blue) and π^\pm (yellow) particles, using different ECal time resolution values (from top to bottom, in ascending order), and arrival time estimates. From left to right: earliest hit time, average hit time, and fitted hit time. The dashed lines indicate the true masses of the particles.

3706 find discontinuities in the track candidates (e.g. due to a particle decay) when these
 3707 so-called breakpoints are large enough. However, for some, more subtle, cases they may
 3708 miss them and form a single reconstructed track. It has been noted in the literature
 3709 that Kalman filters offer, as a by-product, additional information to form test statistics
 3710 to identify these breakpoints [163, 164].

3711 Considering the mean life of the charged pion, $\tau = (2.6033 \pm 0.0005) \times 10^{-8}$ s, one
 3712 can estimate that about 12% of the pions with momentum $p \sim \mathcal{O}(500 \text{ MeV}/c)$ (roughly
 3713 the peak of the pion momentum distribution in ν_μ CC interactions off argon) decay

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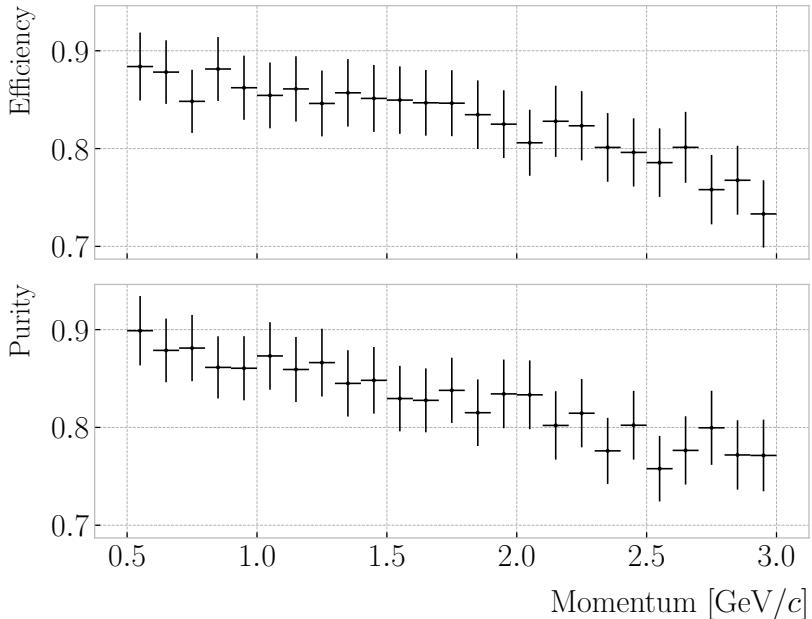


Figure 6.33: Efficiency (top panel) and purity (bottom panel) for the proton selection as a function of the momentum, for $\Delta\tau = 0.10$ ns.

3714 inside the TPC. Figure 6.35 (left panel) shows the amount of charged pions decaying in
 3715 the full TPC and fiducial volumes from an isotropic, monoenergetic sample of 100000
 3716 negatively charged pions with $p = 500$ MeV/ c . We see that about 10% of those decayed,
 3717 with more than half of them decaying inside the TPC fiducial volume.

3718 Figure 6.35 (right panel) shows an example event display of a charged pion (magenta
 3719 line) decays in flight inside the TPC, but because the angle of the muon (blue line) is
 3720 small both were reconstructed as one single track (black line). In this case, the composite
 3721 track reaches the ECal, where it undergoes a muon-like interaction, thus being classified
 3722 as a muon.

3723 A way to understand what decaying pion tracks were totally or partially reconstructed
 3724 together with the daughter muon is looking at the relative energy contributions to the
 3725 reconstructed track. In order to select a sample of such events, I require that a minimum
 3726 50% of the total energy comes from the pion and at least 20% from the muon.

6.5. CHARGED PION DECAY IN FLIGHT

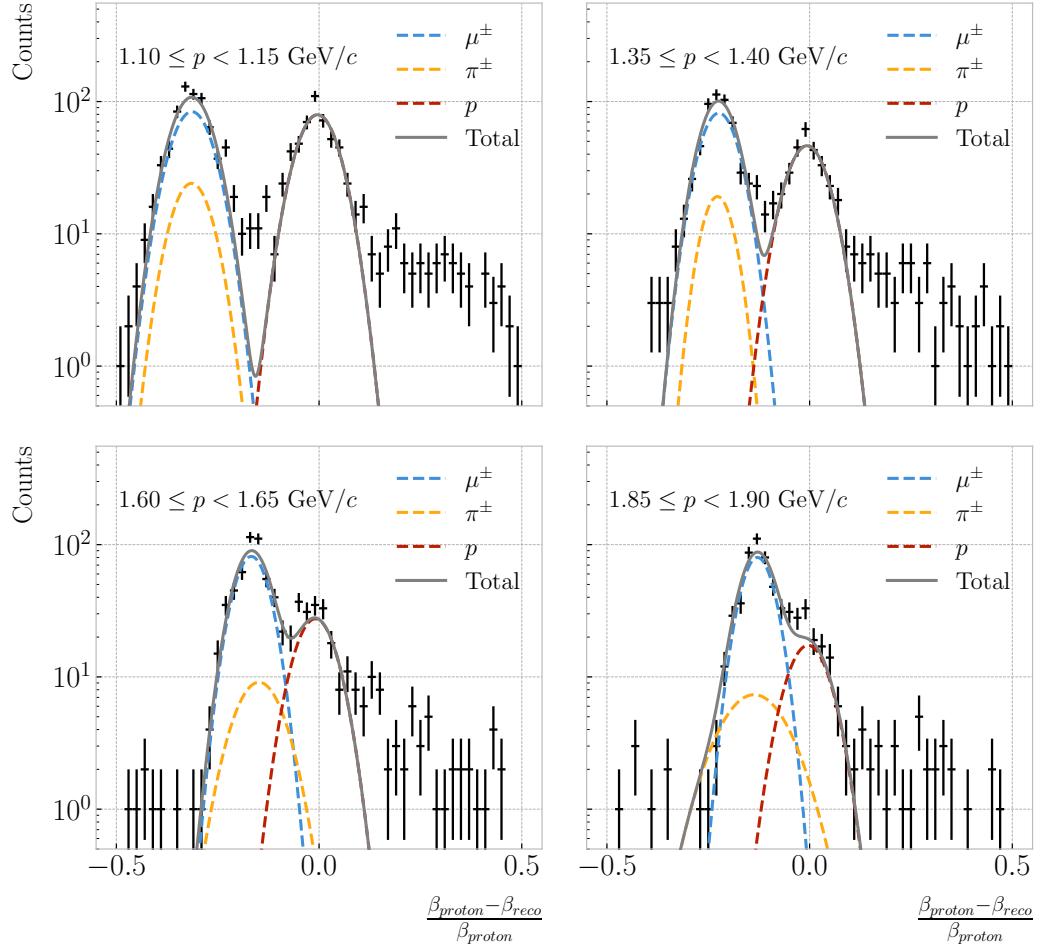


Figure 6.34: Distributions of the velocities measured by ToF with the inner ECal, for different momentum bins, in a FHC neutrino interaction sample. The Gaussian fits are performed around the maxima for each particle species.

3727 6.5.1 Track breakpoints

3728 To identify potential decays we can use the information we obtain from the Kalman
 3729 filter at each step of the fitted track. The simplest test we can think about is computing
 3730 the χ^2 of the mismatch between all the parameters in the forward and the backward fits:

$$\chi_k^{2 (FB)} = (\hat{x}_k^B - \hat{x}_k^F)^T [V^{(\hat{x}_k, B)} + V^{(\hat{x}_k, F)}]^{-1} (\hat{x}_k^B - \hat{x}_k^F), \quad (6.23)$$

3731 where \hat{x}_k^F , \hat{x}_k^B are the Kalman filter state vector estimates at step k in the forward and
 3732 backward fits and $V^{(\hat{x}_k, F)}$, $V^{(\hat{x}_k, B)}$ the covariance matrices of \hat{x}_k^F and \hat{x}_k^B respectively.

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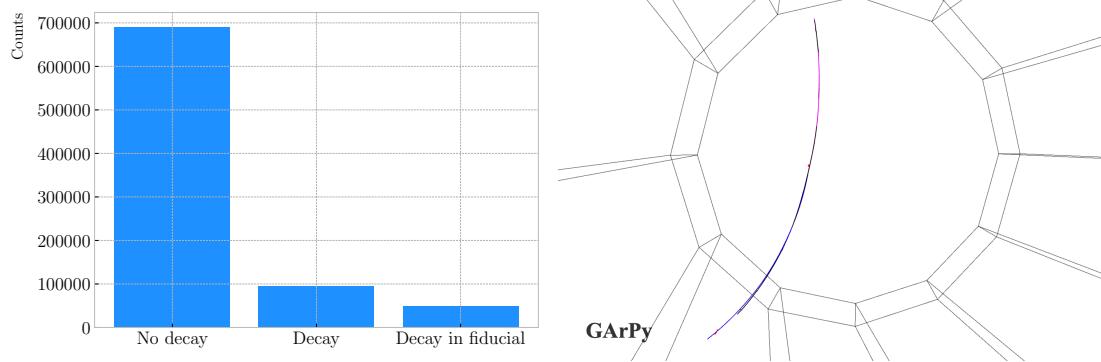


Figure 6.35: Left panel: number of non-decaying, decaying and decaying in the fiducial volume pions for a MC sample of 100000, $p = 500$ MeV/c isotropic positively charged pions inside the TPC. Right panel: event display for a positive pion decaying inside the fiducial volume, with a single reconstructed track for the pion and muon system.

3733 Using the values of the χ^2 at measurement k for the forward and backward fits we can
 3734 compute another χ^2 value that characterises the overall track fit:

$$\chi_{track}^2 = \chi_k^{2(F)} + \chi_k^{2(B)} + \chi_k^{2(FB)}, \quad (6.24)$$

3735 which remains approximately constant for all k .

3736 An alternative approach proposed in the context of the NOMAD experiment was
 3737 using a fit with a more elaborate breakpoint hypothesis, so we can perform a comparison
 3738 of the χ^2 with and without breakpoints. This can be achieved by using some alternative
 3739 parametrisation with extra parameters, which allows some of the track parameters to
 3740 be discontinuous at certain points. A decay changes the momentum magnitude and
 3741 direction, so we can use the new state vector:

$$\alpha = (y, z, 1/R_F, 1/R_B, \phi_F, \phi_B, \tan\lambda_F, \tan\lambda_B)^T. \quad (6.25)$$

3742 As we already have the estimates from the standard Kalman filter and their
 3743 covariance matrices at each point, we do not need to repeat the Kalman fit for the new
 3744 parametrisation. Instead, I can compute the values of α at each point k that minimise

6.5. CHARGED PION DECAY IN FLIGHT

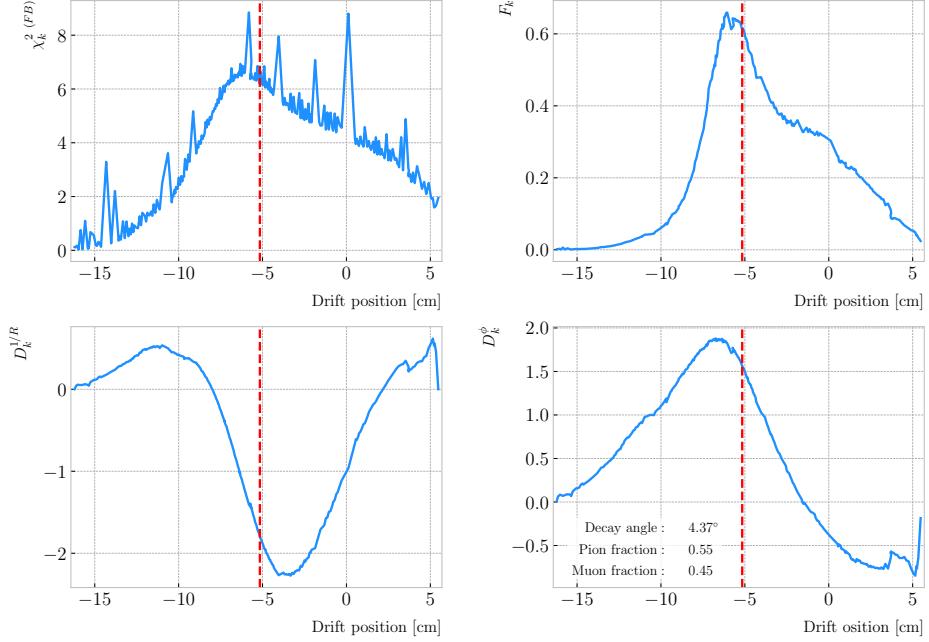


Figure 6.36: Values of $\chi_k^2(FB)$ (top left panel), F_k (top right panel), $D_k^{1/R}$ (bottom left panel) and D_k^ϕ (bottom right panel) versus position along the drift direction for a reconstructed track in a positive pion decay event. The vertical red dashed line indicates the true location of the decay point.

3745 the χ^2 resulting from comparing them to $\{\hat{x}_k^B, \hat{x}_k^F\}$. Introducing the two 5×8 matrices:

$$H^F = \begin{pmatrix} 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \end{pmatrix}, \quad H^B = \begin{pmatrix} 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}, \quad (6.26)$$

3746 we can write this as:

$$\begin{aligned} \chi_k^2(FB)(\alpha) &= (\hat{x}_k^F - H^F \alpha)^T \left[V^{(\hat{x}_k, F)} \right]^{-1} (\hat{x}_k^F - H^F \alpha) \\ &\quad + (\hat{x}_k^B - H^B \alpha)^T \left[V^{(\hat{x}_k, B)} \right]^{-1} (\hat{x}_k^B - H^B \alpha). \end{aligned} \quad (6.27)$$

3747 The minimum of $\chi_k^2(FB)(\alpha)$ is found when the measured new state vector takes the
3748 value:

$$\hat{\alpha}_k = V^{(\hat{\alpha}_k)} H^T (V^{(\hat{x}_k)})^{-1} \hat{X}, \quad (6.28)$$

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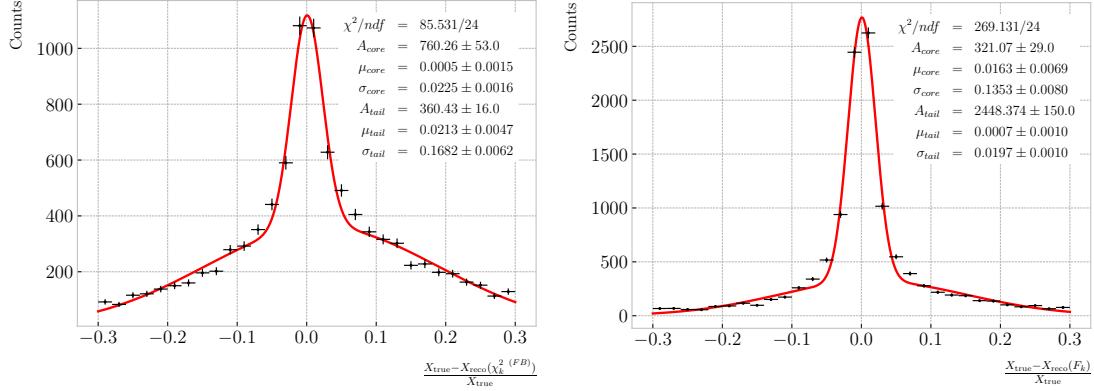


Figure 6.37: Fractional residual distributions of the true and reconstructed decay position along the drift coordinate, using the position of the maximum of $\chi_k^2(FB)$ (left panel) and F_k (right panel) as estimates of the decay position. Also shown are double Gaussian fits to these points (red lines).

3749 where $\hat{X} = \{\hat{x}_k^B, \hat{x}_k^F\}$, $V^{(\hat{x}_k)}$ is the block diagonal matrix formed by $V^{(\hat{x}_k, F)}$ and $V^{(\hat{x}_k, B)}$
 3750 and $V^{(\hat{\alpha}_k)}$ is the covariance matrix of $\hat{\alpha}_k$, given by:

$$V^{(\hat{\alpha}_k)} = \left(H^T (V^{(\hat{x}_k)})^{-1} H \right)^{-1}. \quad (6.29)$$

3751 From these new fit estimates we can compute the F statistic, which tells us whether
 3752 the model with breakpoint provides a statistically significant better fit:

$$F_k = \left(\frac{\chi_{track,k}^2 - \chi_{full,k}^2}{8 - 5} \right) / \left(\frac{\chi_{full,k}^2}{N - 8} \right). \quad (6.30)$$

3753 One can also compute the signed difference of the duplicated variables divided by
 3754 their standard deviation at each point. These represent how significant the discontinuity
 3755 in each variable is. For any variable η we can write it as:

$$D_k^\eta = \frac{\hat{\eta}_k^B - \hat{\eta}_k^F}{\sqrt{\text{Var}[\hat{\eta}_k^F] + \text{Var}[\hat{\eta}_k^B] - 2\text{Cov}[\hat{\eta}_k^F, \hat{\eta}_k^B]}}, \quad (6.31)$$

3756 In our case, the relevant ones to look at are $D_k^{1/R}$ and D_k^ϕ .

3757 Figure 6.36 shows the values of $\chi_k^2(FB)$, F_k , $D_k^{1/R}$ and D_k^ϕ as functions of the position
 3758 along the drift direction, for an example reconstructed track with 55.5% of the energy

6.5. CHARGED PION DECAY IN FLIGHT

3759 coming from the charged pion and 45.5% from the daughter muon. The true position of
 3760 the decay is indicated (dashed red lines). Notice how $\chi_k^{2(FB)}$ and F_k , $D_k^{1/R}$ reach their
 3761 maxima near the decay point. In the former case this indicates a large forward-backward
 3762 difference in the track fit. In the later it represents that the extended state vector
 3763 improves the fit particularly around that point.

3764 I can estimate the decay position finding resolution by computing the difference
 3765 between the X position of the maxima of $\chi_k^{2(FB)}$ and F_k and the X position of the
 3766 true decay. Figure 6.37 represent the the fractional residual distributions for both
 3767 cases, from the sample of tracks containing pion decays. Fitting a double Gaussian to
 3768 the distributions (red lines) I find a resolution of $(3.31 \pm 0.15)\%$ and $(6.94 \pm 0.31)\%$
 3769 respectively.

3770 In principle, the F -statistic should follow a Fisher distribution with $(8 - 5)$ and
 3771 $(N - 8)$ degrees of freedom under the null hypothesis. In most of our cases $N \sim \mathcal{O}(100)$,
 3772 so the probability density functions will look very similar. In this case, it is safe to take
 3773 the limit $N \rightarrow \infty$ in the Fisher PDF:

$$\begin{aligned} \tilde{f}(x; a - b) &= \lim_{N \rightarrow \infty} f(x; a - b, N - a) \\ &= \frac{2^{-\frac{a-b}{2}}}{\Gamma\left(\frac{a-b}{2}\right)} (a - b)^{\frac{a-b}{2}} x^{\frac{a-b}{2}-1} e^{-\frac{a-b}{2}x}. \end{aligned} \quad (6.32)$$

3774 In our case $a - b = 8 - 5 = 3$, so we would obtain a p-value of 0.05 at $x = 2.60$.

3775 Figure 6.38 contains the distributions of the maxima of $\chi_k^{2(FB)}$, F_k and D_k^ϕ and the
 3776 minima of $D_k^{1/R}$ for a sample of non-decaying pion tracks (blue) and another sample of
 3777 reconstructed tracks containing part of the pion and the daughter muon from a decay
 3778 inside the fiducial volume (red). Notice that, even though the values of $F_k^{(max)}$ for the
 3779 decay sample are typically larger than for the non-decaying one, just a small fraction of
 3780 the events go beyond the aforementioned value of $F = 2.60$. Therefore, from a practical
 3781 point of view, it is not the most efficient variable to use for selecting the decay events.

3782 However, looking at the $D_k^{1/R \text{ (min)}}$ distribution we can see there is a big difference
 3783 between non-decaying and decaying events in this variable. One can use a combination

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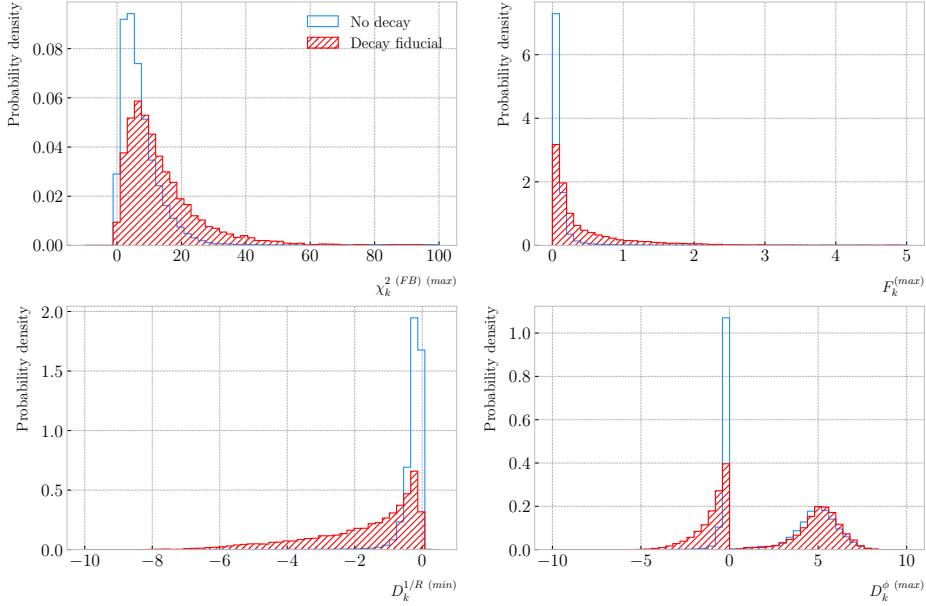


Figure 6.38: Distributions of the extreme values of $\chi_k^2(FB)$ (top left panel), F_k (top right panel), $D_k^{1/R}$ (bottom left panel) and D_k^ϕ (bottom right panel) for non-decaying reconstructed pion tracks (blue) and tracks which include the decay inside the fiducial volume (red).

3784 of these four variables to distinguish between the pion decay events (signal) and the
 3785 non-decaying pions (background).

3786 An approach to this classification could be using a boosted decision tree (BDT). One
 3787 of the advantages of BDTs is that they are easy to interpret and identify the relative
 3788 importance of the different input variables. Training a BDT with 400 estimators and a
 3789 maximum depth of 4 I can obtain an efficient classification without overtraining. Figure
 3790 6.39 (left panel) shows the distribution of probabilities predicted by the BDT for a test
 3791 sample. The signal efficiency as a function of background acceptance, the so-called ROC
 3792 curve, is shown in Fig. 6.39 (right panel). With a relative importance of 0.83, the most
 3793 important variable turned out to be $D_k^{1/R} \text{ (min)}$.

3794 One thing we can check is how the resolution to the decay and the signal efficiency in
 3795 the classification changes with the true decay angle. Using an equal-frequency binning
 3796 for the decay angles, we can repeat the previous steps for each bin.

3797 Figure 6.40 (left panel) shows the dependence on the decay angle of the decay finding

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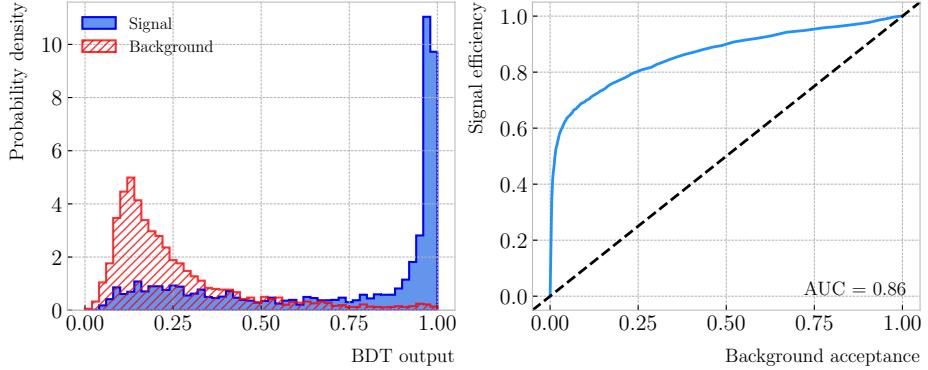


Figure 6.39: Left panel: distributions of the predicted probabilities assigned by the BDT classifier to a test sample of decaying pion+muon tracks (blue) and non-decaying pion tracks (red). Left: signal efficiency versus background acceptance (ROC curve) obtained from the BDT for the test sample.

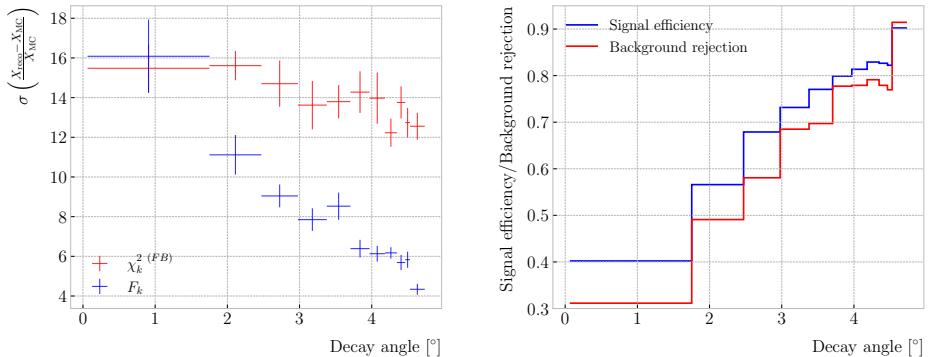


Figure 6.40: Left panel: dependence of the decay position finding resolution on the true value of the decay angle for the $\chi_k^2(FB)$ (red) and F_k (blue) methods. Right panel: signal efficiency (blue line) and background rejection (red line) from the BDT classifier versus true decay angle.

resolution. We can see that for the $\chi_k^2(FB)$ maximum location method the resolution consistently lies between 12 to 16%. However, the $F_k^{(\max)}$ approach gives a significantly better resolution for high angle values, reaching the 4 – 6% range for decay angles $\geq 4^\circ$.

For the classification dependence on the angle, I use the same classifier I trained before but evaluating the test sample for each individual angular bin. I compute the signal efficiency in each bin for a fixed value of the background rejection, in this case 90%. Similarly, for the background rejection estimation I use a fixed signal efficiency value of 90%. Figure 6.40 (right panel) represents the change in signal efficiency (blue)

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3806 and background rejection (red) with the value of the true decay angles.

3807 6.6 Neutral particle identification

3808 6.6.1 ECal clustering

3809 Another important reconstruction item is the clustering algorithm of ECal hits in
3810 GArSoft. The default module features a NN algorithm that treats all hits in the same
3811 way, independently of the layer each hit comes from. However, the current ECal design
3812 of ND-GAr has two very different types of scintillator layers. The inner layers are made
3813 out of tiles, which provide excellent angular and timing resolutions. On the other hand,
3814 the outer layers are cross scintillator strips. That way, an algorithm that treats hits
3815 from both kinds of layers differently may be able to improve the current performance.

3816 Inspired by the reconstruction of T2K’s ND280 downstream ECal [165], the idea
3817 was to put together a clustering module that first builds clusters for the different ECal
3818 views (tiles, strips segmented in the X direction and strips segmented in Y direction),
3819 and then tries to match them together to form the final clusters.

3820 Working on a module-by-module basis, the algorithm first separates the hits depending
3821 on the layer type they come from. Then, it performs a NN clustering for the 3 sets of
3822 hits separately. For the tile hits it clusters together all the hits which are in nearest-
3823 neighbouring tiles and nearest-neighbouring layers, for strip hits it looks at nearest-
3824 neighbouring strips and next-to-nearest-neighbouring layers (as the layers with strips
3825 along the two directions are alternated). For strip clusters an additional cut in the
3826 direction along the strip length is needed.

3827 After this first clustering I then apply a recursive re-clustering for each collection
3828 of strip clusters based on a PCA method. In each case, we loop over the clusters with
3829 $N_{hits} \geq 2$, computing the centre of mass and three principal components. Propagating
3830 these axes up to the layers of the rest of the clusters, we check if the propagated point
3831 and the centre of mass of the second cluster are within next-to-nearest-neighbouring
3832 strips. An additional cut in the direction along the strip length is also needed. Moreover,

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3833 I require that the two closest hits across the two clusters are at most in next-to-nearest-
3834 neighbouring strips. I merge the clusters if these three conditions are satisfied. The
3835 re-clustering is repeated until no more cluster pairs pass the cuts.

3836 The clusters in each strip view are combined if their centres of mass are close enough
3837 and they point in the same direction. An alternative approach for the strip cluster
3838 merging could be to compute the overlap between the ellipsoids defined by the principal
3839 axes of the clusters, and then merge the pair if the overlap exceeds some threshold.
3840 Further study is needed to understand if this change would have an impact in the overall
3841 clustering performance.

3842 To merge the tile clusters to the combined strip clusters I propagate the principal
3843 axis of the strip cluster towards the inner layers, up to the centre of mass layer of the
3844 tile cluster. I merge the clusters if the distance between the propagated point and the
3845 centre of mass is below a certain cut.

3846 The last step is to check if clusters in neighbouring modules should be merged
3847 together, both across two barrel modules, across end cap modules and between barrel
3848 end cap modules. I check the distance between the two closest hits in the pair of clusters
3849 and merge them if it passes this and an additional direction cut.

3850 Figure ?? presents an example of the clustering steps relevant for strip layer hits, from
3851 the input hits (top left panel) to the NN clustering (top right panel) and re-clustering
3852 (bottom left panel) for each strip view and the final merging strip clusters (bottom
3853 right panel). It shows the hits from a single ECal barrel module in a ν_μ CC interaction
3854 event with a neutral pion and a proton in the final state. The two clusters on the left
3855 correspond to the photon pair from the π^0 decay and the one on the upper right corner
3856 is associated to the proton.

3857 This algorithm has a total number of eight free parameters that need to be optimised.
3858 I used a sample of 1000 ν_μ CC interactions in order to obtain the optimal configuration of
3859 clustering parameters. This sample was generated up to the default ECal hit clustering
3860 level, so then I could run the new clustering algorithm each time with a different
3861 configuration of parameters. As the number of parameters is relatively large, I only

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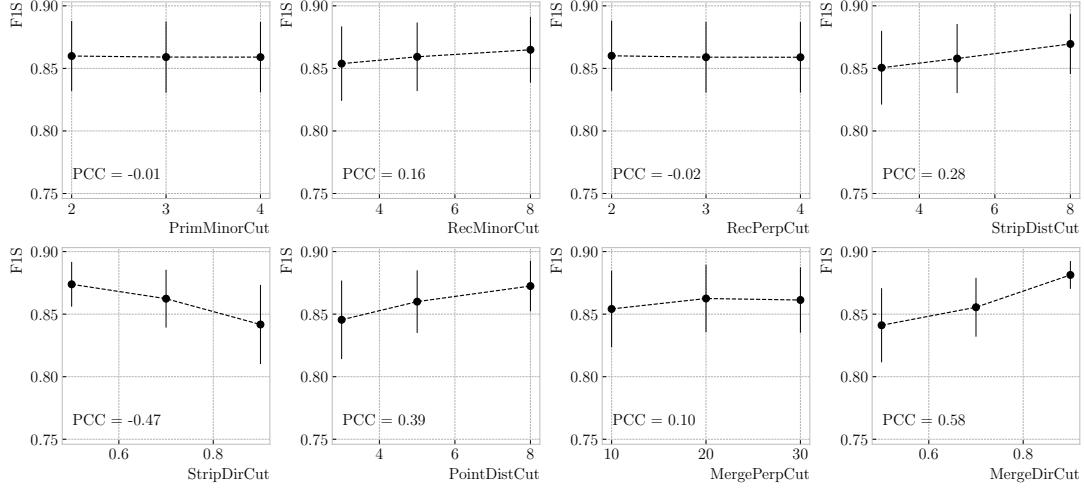


Figure 6.41: Mean values of the F_1 -score marginal distributions for the different free parameters of the new clustering algorithm, with the error bars representing one standard deviation around the mean. The F_1 -score values were computed for the 6561 possible parameter configurations using 1000 ν_μ CC interaction events.

Table 6.5: Summary of parameters and sampled values used in the optimisation of the clustering algorithm.

Name	Units	Sampled values	Description
PrimMinorCut	strips	2, 3, 4	Distance along strip length in NN clustering
RecMinorCut	strips	3, 5, 8	Distance between propagated point and CM along strip length in re-clustering
RecPerpCut	strips	2, 3, 4	Closest hit pair distance in re-clustering
StripDistCut	strips	3, 5, 8	Distance between CMs in strip cluster merging
StripDirCut	cos	0.5, 0.7, 0.9	Main axes direction cut in strip cluster merging
PointDistCut	tiles	3, 5, 8	Distance between propagated point and CM in strip-tile matching
MergePerpCut	cm	10, 20, 30	Closest hit pair distance in module merging
MergeDirCut	cos	0.5, 0.7, 0.9	Main axes direction cut in module merging

3862 performed a coarse-grained scan of the parameter space. Sampling each of the eight
 3863 parameters at three different points each I obtain 6561 different configurations. These
 3864 parameters, together with the used values, are summarised in Tab. 6.5.

3865 In order to measure the performance of the clustering, I use a binary classification
 3866 approach. For each formed cluster, I identify the Geant4 Track ID of the matching MC
 3867 particle and the energy fraction of each hit. Then, I assign to each cluster the Track ID
 3868 with the highest total energy fraction. For each of the different Track IDs associated to

6.6. NEUTRAL PARTICLE IDENTIFICATION

3869 the clusters, I select the cluster with the highest energy (only from the hits with the
3870 same Track ID). I identify such a cluster as the main cluster for that Track ID. I count
3871 as true positives (TPs) the hits with the correct Track ID in each main cluster. False
3872 positives (FPs) are the hits with the incorrect Track ID for the cluster they are in, not
3873 only main clusters. The false negatives (FNs) are the hits with the correct Track ID in
3874 clusters other than the main.

3875 Figure 6.41 shows the computed F_1 -score values for the different cuts. In each case,
3876 the central value represents the mean of the F_1 -score distribution for the specified value
3877 of the corresponding variable and the vertical error bar represents one standard deviation
3878 around the mean. Also shown are the Pearson correlation coefficients of these central
3879 values. We can see that five of the variables have a sizeable effect on the F_1 -score, with
3880 an absolute difference between the last and first values as big as 4%.

3881 The working configuration is obtained as follows. I first select all configurations
3882 with purity $\geq 90\%$. Among those, I choose the combinations that yield the maximum
3883 F_1 -score. If more than one configuration remains I select the one with the highest
3884 sensitivity. Doing so, I end up with a parameter configuration with an efficiency of 88%
3885 and a 90% purity. Compared with the default algorithm, which gives an efficiency of
3886 76% and a purity of 91% for the same sample, I have managed to improve the efficiency
3887 by a factor of 1.16.

3888 6.6.2 π^0 reconstruction

3889 One of the potential applications of the new ECal hit clustering is the reconstruction of
3890 neutral particles, in particular pions. Neutral pions decay promptly after being produced,
3891 through the $\pi^0 \rightarrow \gamma\gamma$ channel ($98.823 \pm 0.034\%$) of the time. The photon pair does
3892 not leave any traces in the HPgTPC (unless one or both of them converts into an
3893 electron-positron pair), but each of them will produce an electromagnetic shower in
3894 the ECal.

3895 To test the potential impact of the new algorithm in π^0 reconstruction, I generated
3896 a MC sample of single, isotropic neutral pions inside the HPgTPC. All pions were

CHAPTER 6. PARTICLE ID IN ND-GAr

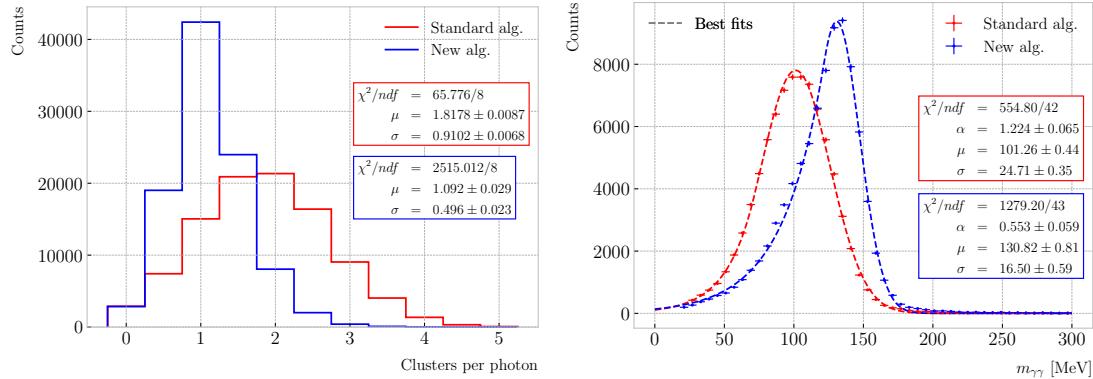


Figure 6.42: Left panel: distributions of the number of ECal clusters per photon from π^0 decays for the standard (red) and new (blue) clustering algorithms. Right panel: reconstructed invariant mass distributions for photon pairs from single π^0 events using the standard (red) and new (blue) ECal clustering algorithms.

3897 generated with a momentum $p = 500$ MeV and their initial positions were uniformly
 3898 sampled inside a $2 \times 2 \times 2$ m box aligned with the centre of the TPC. I ran both the
 3899 default and the new clustering algorithms, using for the latter the optimised configuration
 3900 discussed above.

3901 The first thing to notice is that the number of clusters produced per photon has
 3902 decreased. Figure 6.42 (left panel) shows these distributions for the default (red) and
 3903 new (blue) algorithms. Using a simple Gaussian fit, we see that the mean number of
 3904 ECal clusters per photon went from 1.82 ± 0.01 to 1.09 ± 0.03 . This effectively means that
 3905 with the new algorithm the ECal activity of one true particle is typically reconstructed
 3906 as a single object. From the reconstruction point of view this can be an advantage. As
 3907 now most of the photon energy ends up in a single ECal cluster, I can simply use cluster
 3908 pairs to identify the π^0 decay.

3909 In general, one calculates the invariant mass of the photon pair as:

$$m_{\gamma\gamma} = \sqrt{2E_1E_2(1 - \cos \theta)}, \quad (6.33)$$

3910 where E_i are the energies of the photons and θ the opening angle between them. In this
 3911 case I can use the energies deposited in the ECal and their incident directions. This
 3912 quantity is computed for all possible pairs of clusters, using their position together with

6.7. INTEGRATION IN GArSOFT

3913 the true decay point. In a more realistic scenario, e.g. ν_μ CC interaction, one could use
 3914 the position of the reconstructed primary vertex instead. I also tried to use the principal
 3915 direction of the clusters, but that approach gave considerably worse results. For each
 3916 event I only keep the pair with an invariant mass closer to the true π^0 mass value.

3917 Figure 6.42 (right panel) shows the invariant mass distributions for the photon pairs
 3918 we get using the default (red) and the new (blue) ECal clustering algorithms. For the fit
 3919 I used a modified version of the Crystal Ball function [166], obtained by taking the limit
 3920 where the parameter controlling the power-law tail goes to infinity:

$$f(x; N, \mu, \sigma, \alpha) = N \cdot \begin{cases} e^{\frac{\alpha(2x-2\mu+\alpha\sigma)}{2\sigma}}; & x \leq \mu - \alpha\sigma, \\ e^{-\frac{(x-\mu)^2}{2\sigma^2}}; & x > \mu - \alpha\sigma. \end{cases} \quad (6.34)$$

3921 Comparing the fitted mean and standard deviation values for the Gaussian cores, we
 3922 see that the distribution for the new algorithm is a 67% narrower and also peaks much
 3923 closer to the true m_{π^0} value, going from 101.3 ± 0.4 MeV to 130.8 ± 0.6 MeV.

3924 6.7 Integration in GArSoft

3925 All the additions and improvements to the reconstruction discussed in this Chapter
 3926 had to be integrated in the GArSoft framework. This is necessary both to allow a
 3927 more streamlined path for development, as this makes testing and adding features
 3928 straightforward, as well as make the changes usable in future productions of simulated
 3929 data. In this section, I outline the current status of the integration in GArSoft of the
 3930 reconstruction work presented above.

3931 The new track-cluster association code has been implemented in GArSoft, under
 3932 the name of `TPCECALAssociation2`, and has now become the new default in the
 3933 reconstruction. The structure of the module is similar to the previous implementation,
 3934 and the data products they output are identical in form. Therefore, any existing code
 3935 using the association objects does not need to be modified.

3936 The computation of the truncated mean dE/dx of the tracks, the evaluation of

CHAPTER 6. PARTICLE ID IN ND-GAr

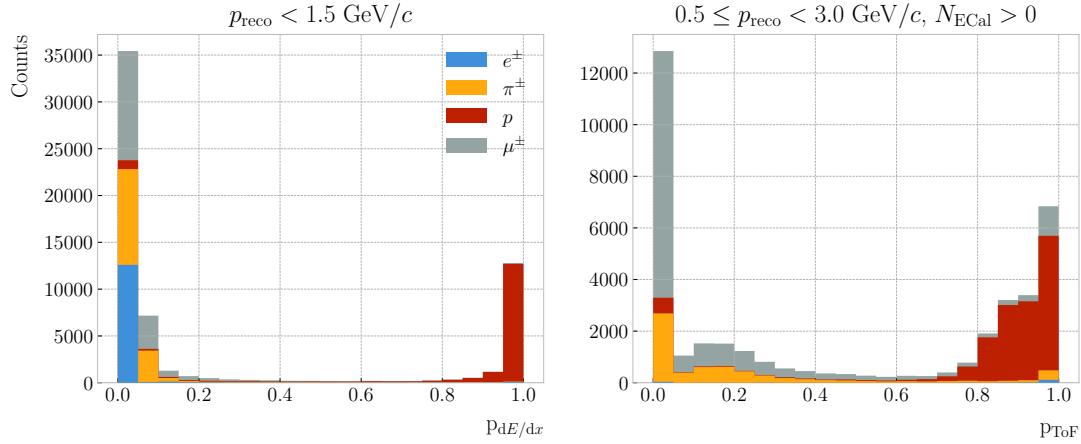


Figure 6.43: Distributions of proton dE/dx (left panel) and ToF (right panel) scores for a sample of 100000 FHC neutrino interactions in the HPgTPC. The distributions are broken down by the true particle type associated to the reconstructed particle.

3937 the muon score for muon and pion separation, and the estimation of the velocity from
 3938 time-of-flight are all orchestrated by the `CreateRecoParticles` module. Each one of
 3939 these is implemented as a separate algorithm, which is then called by the parent module.
 3940 This generates the `gar::rec::RecoParticle` products, a new high-level data object in
 3941 GArSoft. These combine the information from the HPgTPC, ECal, and μ ID to create
 3942 an object useful for analysers. At the moment, these data products are only generated
 3943 for charged particles. However, in the future the module can be extended to incorporate
 3944 other algorithms used for the identification of neutral particles, like neutral pions and
 3945 neutrons.

3946 Additionally, analogous to the muon score, the `gar::rec::RecoParticle` objects
 3947 contain two other scores based on the $\langle dE/dx \rangle$ and ToF estimates which measure the
 3948 “protoness” of a reconstructed particle. These are obtained in a number of momentum
 3949 bins, and are a measure of the distance to the point in the corresponding distribution
 3950 that maximises the F_1 -score for the proton separation. This distance is then transformed
 3951 applying a sigmoid function, which produces a score in the 0 – 1 range, with coefficients
 3952 obtained following a procedure similar to the one used to calibrate the response of
 3953 the muon score. The dE/dx proton score is defined for all particles with momenta
 3954 $p_{\text{reco}} < 1.5 \text{ GeV}/c$, whereas the ToF proton score is available for the particles with at least

6.7. INTEGRATION IN GArSOFT

3955 one associated hit in the inner ECal and momentum in the range $0.5 \leq p_{\text{reco}} < 3.0 \text{ GeV}/c$.
3956 As an example, Fig. 6.43 shows the distributions of the dE/dx (left panel) and ToF
3957 (right panel) proton scores for the reconstructed particles in a 100000 FHC neutrinos
3958 sample.

3959 The calculation of the track breakpoint variables for pion decay identification is
3960 currently implemented as an analysis module in GArSoft. It would be interesting to add
3961 this information to the `gar::rec::RecoParticle` products, possibly calling the code as
3962 an additional algorithm in the `CreateRecoParticles` module. However, the best way
3963 to propagate the information to the high-level objects is still unclear.

3964 About the new ECal clustering algorithm, it is still in a development phase, and
3965 as such it has not replaced the current clustering module. At the moment, its latest
3966 version is integrated in GArSoft as the `CaloClustering2` module. The algorithm used
3967 is implemented separately, and then invoked in the main code. The module can be
3968 run standalone on the outputs of the reconstruction, creating a second instance of the
3969 `gar::rec::Cluster` collection. In the future it may replace the current algorithm as
3970 the default in the reconstruction chain. However, more work is needed in order to
3971 understand its performance in all the different use cases.

Event selection in ND-GAr

3974 7.1 Data sample

3975 In this section I need to make sure to mention:

- 3976 • I need to comment on the versions of the software that were used for the production
3977 of the different samples (if we end up having more than one). The version of GENIE
3978 used was
- 3979 • We use GArG4 instead of `edep-sim` for the particle propagation. Because both
3980 `Geant4` wrappers use different configurations for the simulation, the results obtained
3981 are different. The default `edep-sim` configuration used by the DUNE ND is
3982 appropriate for ND-LAr, where thresholds for particle production are higher. In
3983 the case of ND-GAr, these parameters need to be adjusted accordingly. For the
3984 time being, in these first productions of analysis files, we will use our standalone
3985 `Geant4` implementation. For future iterations these differences will need to be
3986 revisited and understood, so we can use the same simulation workflow as the rest
3987 of the ND.
- 3988 • I need to comment on the sample size. The first sample produced was simply 10^5
3989 events inside the HPgTPC volume. There is also the question of the other sample
3990 we may want to produce for the $\geq 3\pi^\pm$ selection (ask Naseem).
- 3991 • So far we have only simulated single interaction events. Ideally, we should move
3992 to simulate full spills. Of course, we need to understand how many interactions

CHAPTER 7. EVENT SELECTION IN ND-GAR

Table 7.1: Event rates in ND-GAr.

Process	Events/ton/year	
	1.1×10^{21} POT/year	1.9×10^{21} POT/year
All ν_μ -CC	1.60×10^6	2.83×10^6
CC 0π	5.28×10^5	9.35×10^5
CC $1\pi^\pm$	3.02×10^5	5.34×10^5
CC $1\pi^0$	1.65×10^5	2.92×10^5
CC 2π	3.18×10^5	5.63×10^5
CC 3π	1.36×10^5	2.41×10^5
CC other	1.52×10^5	2.69×10^5
All $\bar{\nu}_\mu$ -CC	7.54×10^4	1.33×10^5
All NC	5.50×10^5	9.73×10^5
All ν_e -CC	2.70×10^4	4.78×10^4

3993 we expect in ND-GAr per spill. Also, there is the question of having neutrino
3994 interactions happening in the other detector volumes (ECal, magnet, . . .).

3995 • At some point, we should generate a sample of rock muons making it to ND-GAr.

3996 • I think I should comment on the run plan (at least the part that concerns ND-GAr),
3997 and what it means in terms of generating a full production sample. It will be
3998 good to have an understanding of the POT we need on-axis and at each off-axis
3999 positions (for both FHR and RHC).

4000 7.2 ν_μ CC selection

4001 In a ν_μ CC inclusive selection, the signal topology we look for is a neutrino-induced
4002 muon with or without other final state particles. Here, I also require the neutrino vertex
4003 to be located inside the fiducial volume (FV) of ND-GAr.

4004 The FV is defined as a smaller cylinder within the cylindrical volume of the HPgTPC.

4005 The FV has a radius R_{FV} and a half-length L_{FV} . For a particle position to lie within

7.2. ν_μ CC SELECTION

4006 the FV it must satisfy:

$$\vec{x}_i \in \left\{ \vec{x} \in \mathbb{R}^3 \mid |x_0| \leq L_{\text{FV}} \text{ \& } \sqrt{x_1^2 + x_2^2} \leq R_{\text{FV}} \right\}, \quad (7.1)$$

4007 in the reference frame of the HPgTPC. For convenience, I define:

$$\begin{aligned} \Delta R_{\text{FV}} &= R_{\text{HPgTPC}} - R_{\text{FV}}, \\ \Delta L_{\text{FV}} &= L_{\text{HPgTPC}} - L_{\text{FV}}, \end{aligned} \quad (7.2)$$

4008 where R_{HPgTPC} and L_{HPgTPC} refer to the radius and the half-length of the HPgTPC,
 4009 respectively. Figure 7.1 shows the HPgTPC volume with the FV inside of it. In that
 4010 representation, the FV is defined as $\Delta L_{\text{FV}} = 30.0$ cm and $\Delta R_{\text{FV}} = 30.0$ cm. Also shown
 4011 is the HPgTPC reference frame, with x being the drift direction and z aligned along the
 4012 beam direction.

4013 In some cases, it is interesting to divide the signal events in different categories
 4014 based on their true interaction mode. In this work, I will distinguish between charged-
 4015 current quasi-elastic (CCQE), coherent (CCCOH), resonant (CCRES), and deep-inelastic
 4016 (CCDIS) interactions. I also use a separate category for the interactions not included in
 4017 any of the other categories (CCOther).

4018 Any other events are considered backgrounds. For this selection, I use the following
 4019 categorisation of background events:

- 4020 • Out of FV: if the true neutrino vertex lies outside the defined FV.
- 4021 • NC: if the event is a true neutral-current event.
- 4022 • $\bar{\nu}_\mu$ CC: if the true neutrino candidate is of muon antineutrino flavour.
- 4023 • Other: if the event is not signal nor falls in any of the other background categories.

4024 The key to the CC selection is the identification of a primary muon candidate.
 4025 Typically, this is the longest track in the event. However, sometimes protons and pions
 4026 leave tracks longer than that of the muon. This is particularly important in the GAr

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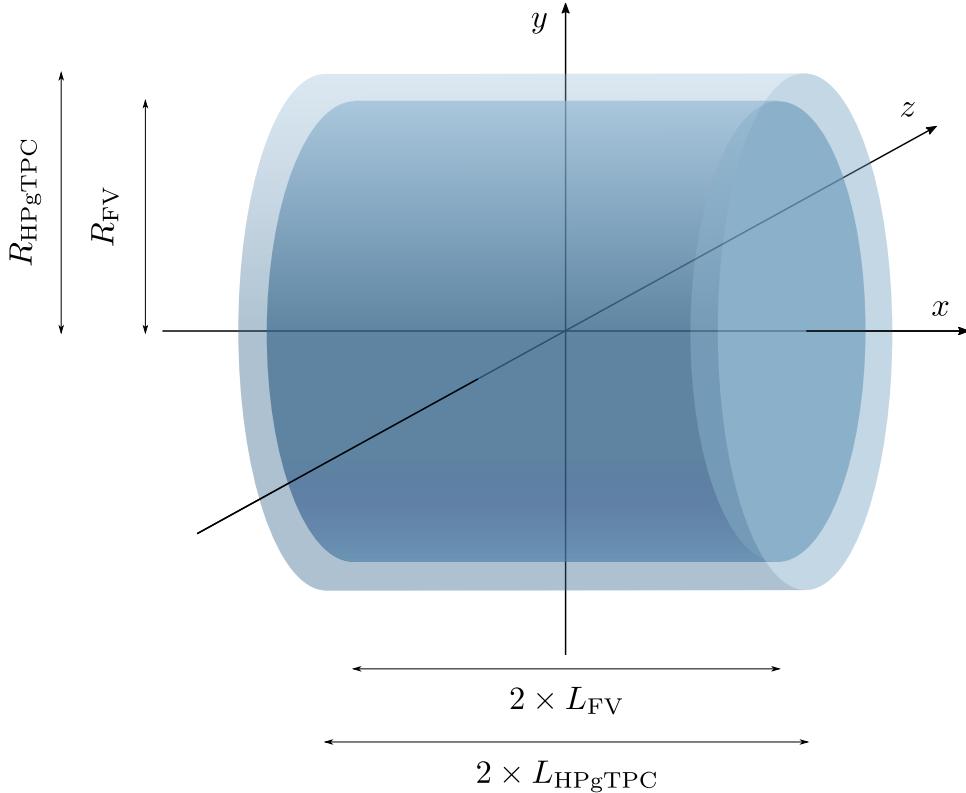


Figure 7.1: Schematic diagram of the HPgTPC including the fiducial volume (FV). In this case the FV is given by $\Delta L_{\text{FV}} = 30.0$ cm and $\Delta R_{\text{FV}} = 30.0$ cm.

4027 medium, considerably less dense than the LAr. For this reason, the muon identification
 4028 in ND-GAr relies heavily on the capabilities of the ECal.

4029 The selection strategy proposed combines the information coming from the three
 4030 main detection systems of ND-GAr: the HPgTPC charge readout, and the ECal and
 4031 μ ID detectors. It consists of five steps:

- 4032 1. Event contains reconstructed particles.
- 4033 2. Select particles with reconstructed negative charge, $q_{\text{reco}} = -1$.
- 4034 3. Select particles passing the muon score cut, $\mu_{\text{score}} \geq \mu_{\text{score}}^{\text{cut}}$.
- 4035 4. Keep reconstructed particle with the highest momentum, $\max [p_{\text{reco}}]$.
- 4036 5. Check that the remaining particle starts within the FV.

7.2. ν_μ CC SELECTION

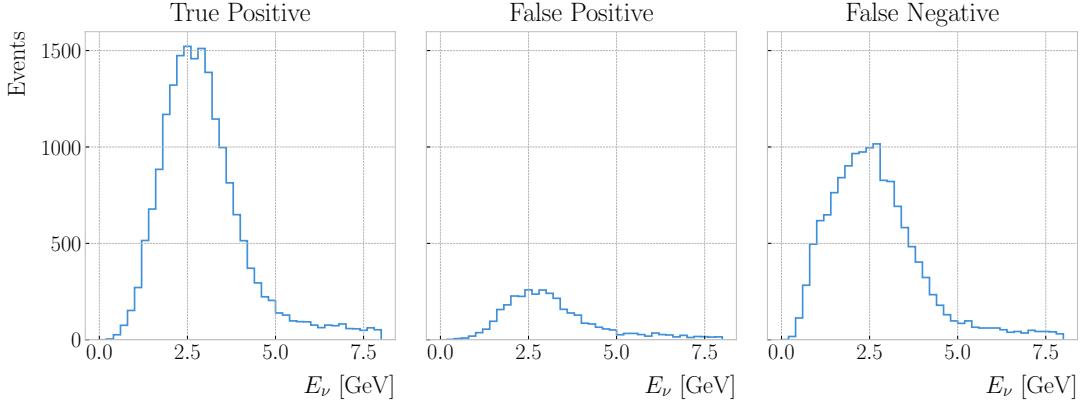


Figure 7.2: True positive (left panel), false positive (middle panel), and false negative (right panel) true neutrino energy distributions for the ν_μ CC selection given by a muon score cut of $\mu_{\text{score}}^{\text{cut}} = 0.75$, and a FV defined as $\Delta L_{\text{FV}} = 30.0$ cm and $\Delta R_{\text{FV}} = 30.0$ cm.

4037 All the events passing these cuts are classified as signal, and the selected particle is
 4038 regarded as the primary muon candidate.

4039 **7.2.1 Selection optimisation**

4040 I performed an optimisation of this selection, comparing the performance of a number of
 4041 configurations. For the muon selection, I varied the value of $\mu_{\text{score}}^{\text{cut}}$ from 0.05 to 0.95,
 4042 using a step size of 0.05. Additionally, to optimise the FV, I systematically explored a
 4043 number of different parameter configurations, moving within the 10.0 – 70.0 cm range for
 4044 ΔL_{FV} and 25.0 – 75.0 cm for ΔR_{FV} , in increments of 10.0 cm and 5.0 cm respectively.

4045 For each parameter configuration, I extract three different true neutrino energy
 4046 distributions. These are built combining the results of the selection described previously,
 4047 which we can refer to as the ‘reco’ selection, and a ‘true’ selection. The later identifies
 4048 the true ν_μ CC events using the GENIE event records, and checks that the true neutrino
 4049 vertices are contained in the FV.

4050 The first distribution consists of the events passing both selections, i.e., these are
 4051 the true ν_μ CC events which pass the ‘reco’ selection. The second distribution contains
 4052 the events passing the ‘reco’ selection but failing the ‘true’ selection. These are
 4053 the background events that the selection misidentifies. Finally, the third distribution

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4054 corresponds to the events picked by the “true” selection but not by the “reco” one. In
 4055 other words, these are the true ν_μ CC events that our selection misses. In analogy to
 4056 the machine learning jargon, I refer to these distributions as the true positive (TP),
 4057 false positive (FP), and false negative (FN) spectra, respectively. Figure 7.2 shows an
 4058 example of these three distributions for the case $\mu_{\text{score}}^{\text{cut}} = 0.75$, $\Delta L_{\text{FV}} = 30.0$ cm, and
 4059 $\Delta R_{\text{FV}} = 30.0$ cm.

4060 By making different combinations of these distributions one can compute a series of
 4061 performance metrics. Using the full information from the spectra allows to obtain the
 4062 scores as a function of the true neutrino energy, whereas the totals can be obtained by
 4063 integrating the histograms. This way, the efficiency of the selection is given by:

$$\begin{aligned} \text{Efficiency} &= \frac{\text{Selected true } \nu_\mu \text{ CC events}}{\text{Total true } \nu_\mu \text{ CC events}} \\ &= \frac{\text{TP}}{\text{TP} + \text{FN}}, \end{aligned} \tag{7.3}$$

4064 while the purity can be written as:

$$\begin{aligned} \text{Purity} &= \frac{\text{Selected true } \nu_\mu \text{ CC events}}{\text{Total selected events}} \\ &= \frac{\text{TP}}{\text{TP} + \text{FP}}. \end{aligned} \tag{7.4}$$

4065 Another scoring metric typically used when quantifying the performance of a selection
 4066 is the significance. It is defined as:

$$\text{Significance} = \frac{S}{\sqrt{S + B}} = \frac{\text{TP}}{\sqrt{\text{TP} + \text{FP}}}. \tag{7.5}$$

4067 The significance measures the relative size of the true signal within the selection, $S = \text{TP}$
 4068 with respect to one standard deviation of the counting experiment. Assuming Poisson
 4069 statistics, the variance is equal to the number of observations, and therefore the standard
 4070 deviation equals to $\sqrt{N} = \sqrt{S + B} = \sqrt{\text{TP} + \text{FP}}$. I use this metric to

4071 Figure 7.3 shows the change in efficiency (blue) and purity (red) of the ν_μ CC
 4072 selection as a function of the different cuts. From left to right, I vary $\mu_{\text{score}}^{\text{cut}}$, ΔL_{FV} ,

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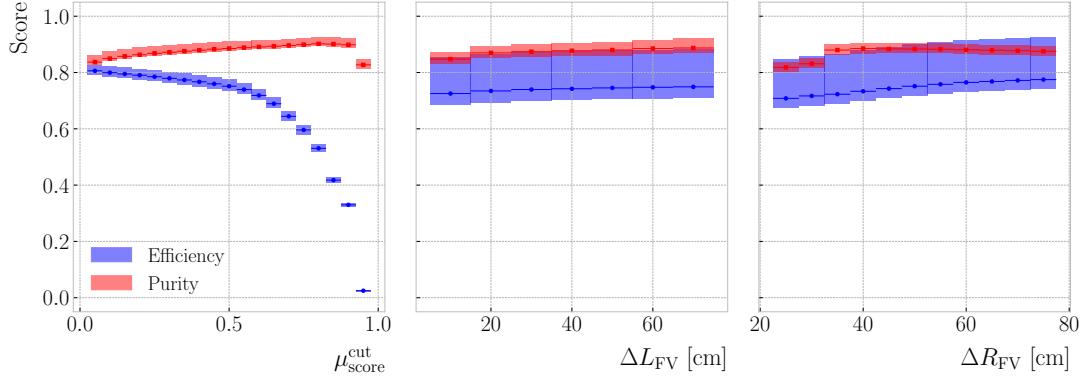


Figure 7.3: Efficiency (blue) and purity (red) for the ν_μ CC selection as a function of the muon score cut (left panel), FV half-length cut (middle panel), and radial cut (right panel). The height of the boxes represents the IQR of the conditional distributions, whereas the horizontal line corresponds to the median.

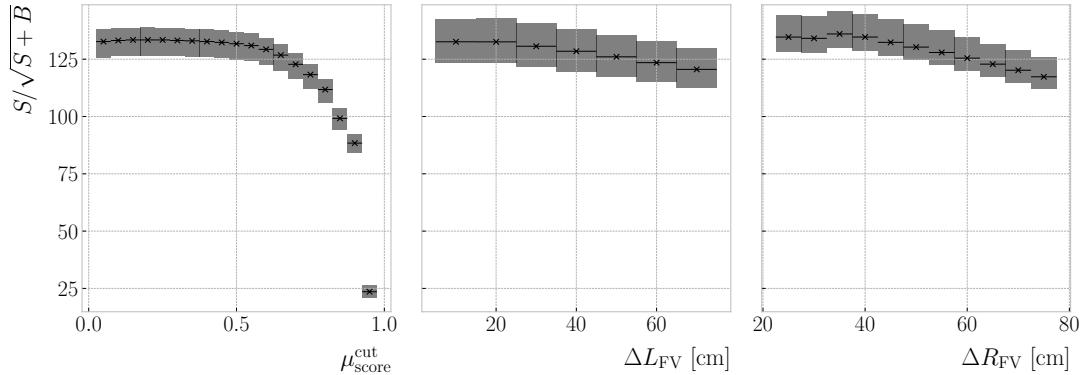


Figure 7.4: Significance for the ν_μ CC selection as a function of the muon score cut (left panel), FV half-length cut (middle panel), and radial cut (right panel). The height of the boxes represents the IQR of the conditional distributions, whereas the horizontal line corresponds to the median.

4073 and ΔR_{FV} . For each value of the cuts, I compute the median and IQR (represented
 4074 by the horizontal lines and the heights of the boxes, respectively) of the corresponding
 4075 conditional distributions of efficiency and purity. This representation is useful to get
 4076 an idea of the general trend the scores follow with the cuts, as well as the spread. It
 4077 is clear that the muon score cut has the biggest impact on the efficiency, which ranges
 4078 between 0.05 to 0.80, whereas the purity remains stable with values around 0.85.

4079 A similar depiction of the significance can be found in Fig. 7.4. In this case, one can
 4080 see that the $S/\sqrt{S+B}$ decreases as the cuts grow tighter. However, there are hints of

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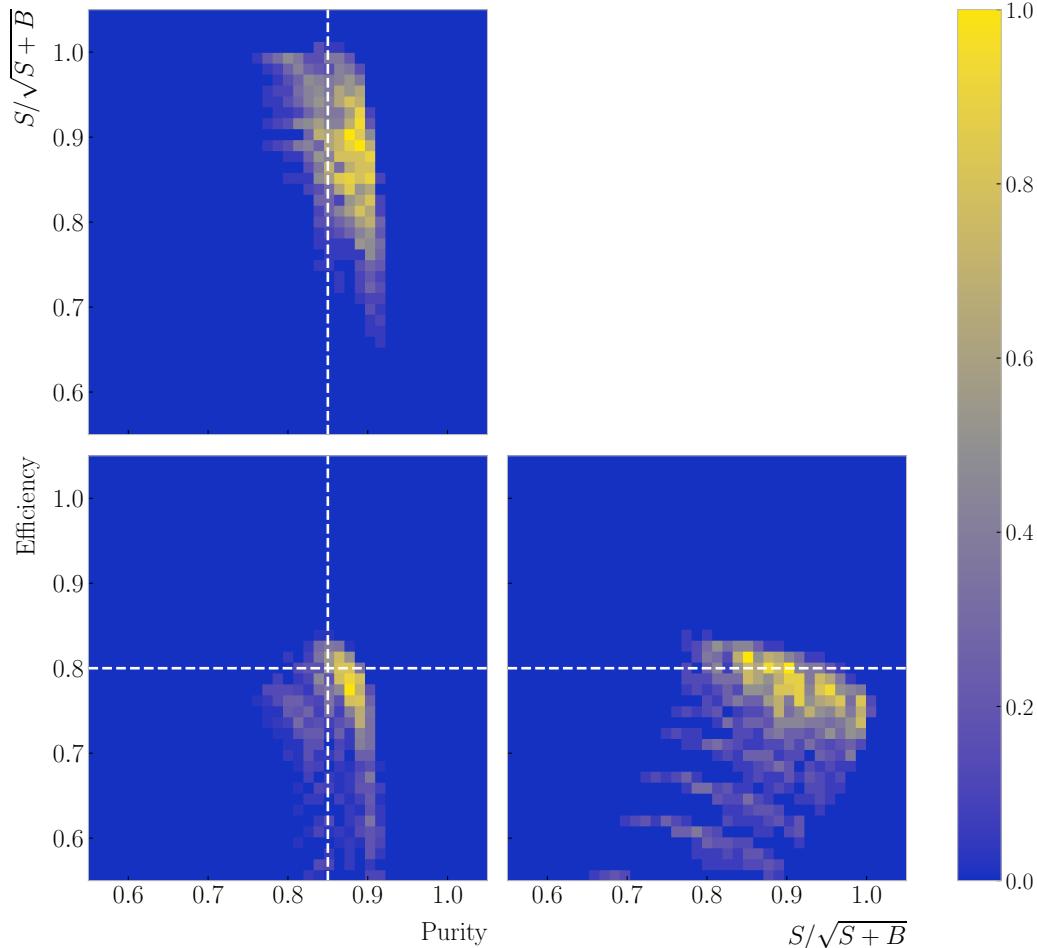


Figure 7.5: Normalised 2D distributions of efficiency, purity and significance for the ν_μ CC selection. The $S/\sqrt{S+B}$ is normalised to the highest value achieved. The vertical dashed line indicates a purity value of 0.85, whereas the horizontal one corresponds to an efficiency of 0.80.

4081 local maxima at intermediate values.

4082 Selecting the cut configuration with the highest significance, 147 ± 11 for the parameter
 4083 values explored here, results in an efficiency and purity of 0.754 ± 0.006 and 0.833 ± 0.007 ,
 4084 respectively. Figure 7.5 shows the 2D distributions resulting when combining pairs of
 4085 efficiency, purity and significance, obtained for the cut configurations explored. The
 4086 significance is normalised to the highest value obtained in the parameter scan. Looking
 4087 at this, it is clear that a selection with highest efficiency and purity can be achieved,
 4088 maintaining a similar significance level.

7.2. ν_μ CC SELECTION

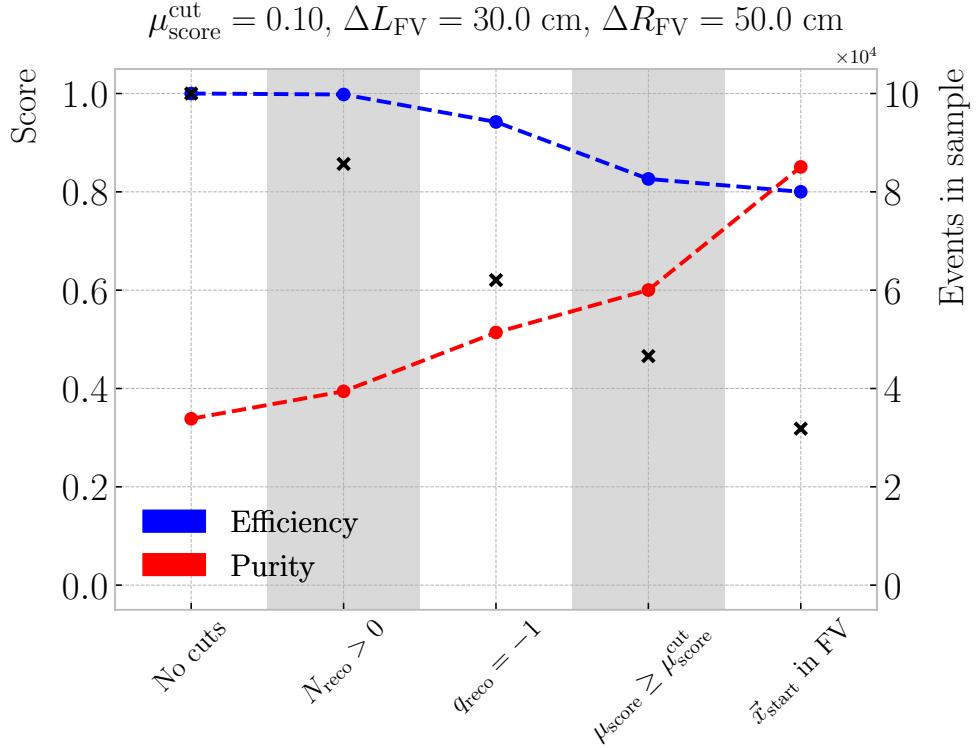


Figure 7.6: Cumulative efficiency (blue) and purity (red) of the ν_μ CC selection. The secondary axis indicates the number of events in the sample after each cut (black crosses).

Table 7.2: Step-by-step ν_μ CC selection cuts and cumulative passing rates. Relative passing rates are indicated in parentheses.

Cut #	Selection cut	Events	Passing rates
0	Total number of events (No cuts)	100000	100.00% (100.00%)
1	At least one reconstructed particle	85680	85.68% (85.68%)
2	Negatively charged particles only	62054	62.05% (72.43%)
3	$\mu_{\text{score}} \geq \mu_{\text{score}}^{\text{cut}}$	46585	46.59% (75.07%)
4	Candidate \vec{x}_{start} in FV	31834	31.83% (68.34%)

4089 Therefore, to get a more refined selection, I first select the configurations with a
 4090 purity and an efficiency higher than 0.85 and 0.80, respectively. After that, I select the
 4091 tuple of cuts yielding the highest significance. The resulting value for the muon score
 4092 cut is $\mu_{\text{score}}^{\text{cut}} = 0.10$, and the FV is given by $\Delta L_{\text{FV}} = 30.0 \text{ cm}$ and $\Delta R_{\text{FV}} = 50.0 \text{ cm}$.
 4093 With these, one obtains a total efficiency of 0.800 ± 0.007 and purity of 0.851 ± 0.008 ,

CHAPTER 7. EVENT SELECTION IN ND-GAR

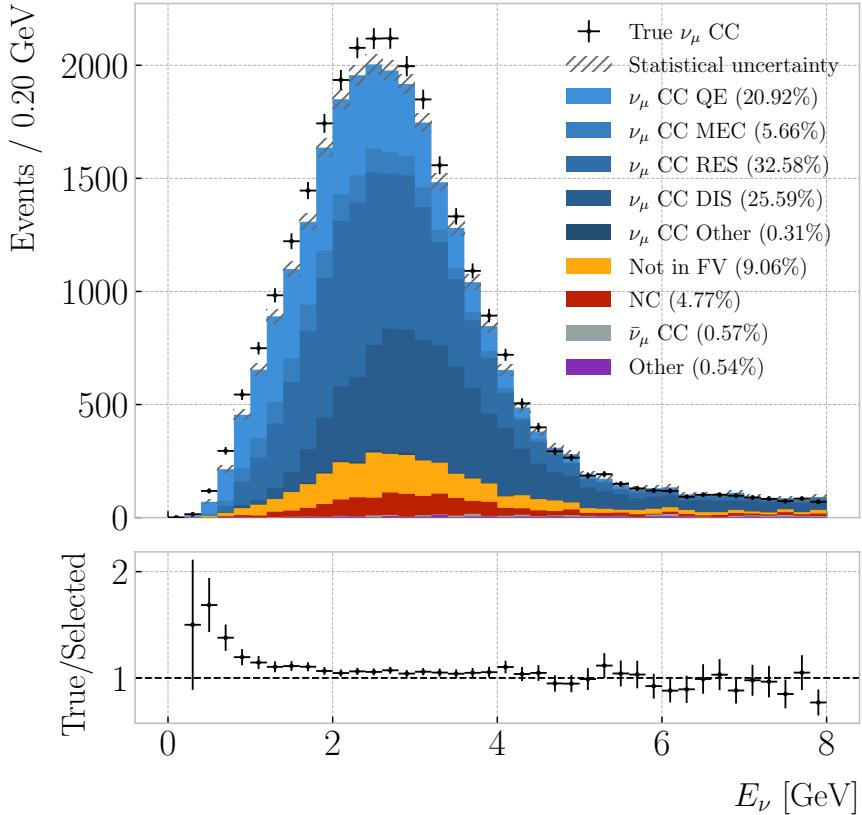


Figure 7.7: True neutrino energy spectra for the ν_μ CC selection. The selected events correspond to the coloured stacked histogram, broken down by signal and background subcategories. The statistical uncertainty is drawn in hatched gray. The true distribution is also shown with the black data points. The bottom panel shows the ratio between the number of true and selected ν_μ CC events per bin.

4094 with a significance of 138 ± 11 . Hereafter, I use this optimised selection cuts, unless
 4095 specified otherwise.

4096 A summary of the selection can be found in Tab. 7.2. It shows the number of
 4097 events in the selected sample after each selection cut, as well as the absolute and relative
 4098 passing rates. Figure 7.6 shows the overall efficiencies (blue) and purities (red) after
 4099 each cut in the event selection is applied. As expected, the efficiency drops while the
 4100 purity increases with the successive cuts.

4101 Notice how, out of the cuts prior to the FV constraint, the sign selection produces
 4102 the highest increase in purity. This is one of the advantages of having a magnetised
 4103 TPC, and can also be used for a $\bar{\nu}_\mu$ CC selection when running in RHC mode.

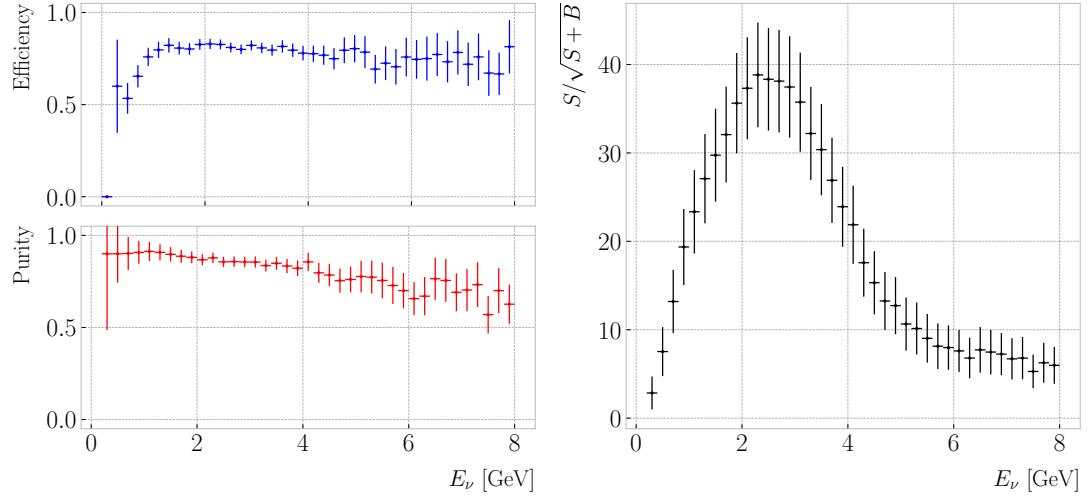


Figure 7.8: Left panel: efficiency (top panel) and purity (bottom panel) for the ν_μ CC selection as a function of the true neutrino energy. Right panel: significance for the ν_μ CC selection as a function of the true neutrino energy

4104 7.2.2 Selection performance

4105 Using the stored spectra discussed above, the true neutrino energy distribution for the
 4106 selected events can be recovered doing TP + FP. Similarly, the combination TP + FN
 4107 gives the true spectrum. Figure 7.7 shows the true (black data points) and selected
 4108 (coloured stacked histogram) E_ν distributions for the optimised ν_μ CC selection. The
 4109 colours in the selected spectrum indicate the different signal categories and backgrounds,
 4110 with the overall statistical uncertainty represented by the gray hatched mess. The ratio
 4111 between the true and selected events is also shown. One can see that it sits around 1 for
 4112 most of the energy range. However, for energies ≤ 1 GeV there is a significant deficit of
 4113 selected events.

4114 These spectra also allow to compute the efficiency and purity of the selection as
 4115 a function of the true neutrino energy, as shown in Fig. 7.8 (left panel). As it could
 4116 be expected from the previous ratio plot, the efficiency is low at low neutrino energies.
 4117 Nonetheless, it raises quickly with the energy, until it stabilises around a value of 0.80.
 4118 Looking at the purity, one may notice that, although it starts at around 0.90, there is a
 4119 significant decrease towards the high end of the spectrum. Figure 7.8 (right panel) also

CHAPTER 7. EVENT SELECTION IN ND-GAR

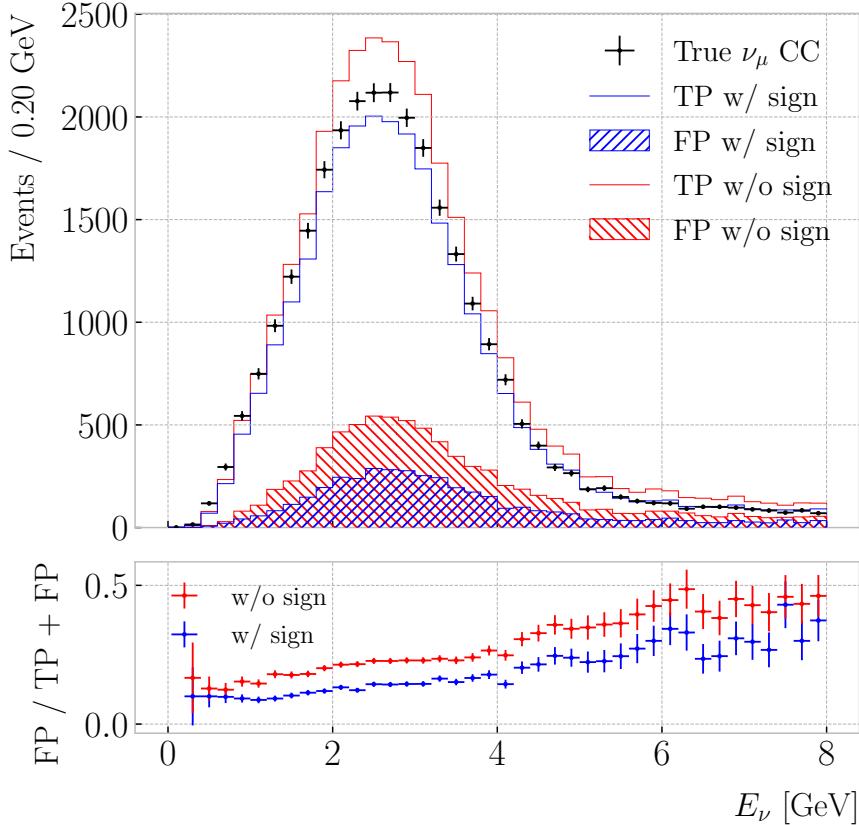


Figure 7.9: True neutrino energy spectra for the ν_μ CC selection with (blue) and without (red) sign selection. The selected events are broken down by true positives (signal) and false positives (background). The true distribution is also shown (black data points). The bottom panel shows the ratios between the number of false positives and total selected events per bin.

4120 shows the significance as a function of the energy. In this case, the highest $S/\sqrt{S+B}$ is
 4121 achieved around the energies where the spectrum peaks.

4122 A variation of the ν_μ CC selection one can try is to apply it without the reconstructed
 4123 charge cut. Figure 7.9 (top panel) shows the E_ν distributions corresponding to the
 4124 selection with (blue stacked histogram) and without (red stacked histogram) the sign
 4125 selection. In the former case, the out of FV contamination amounts to 9.06% of the
 4126 total, while the NC contamination results 4.77% and the wrong-sign contamination
 4127 0.57%. For the later, these backgrounds account for the 10.01%, 10.82%, and 2.18%
 4128 of the selected events, respectively. As expected, removing the positive particles does
 4129 not change the FV-related effects noticeably. However, the sign selection proves its

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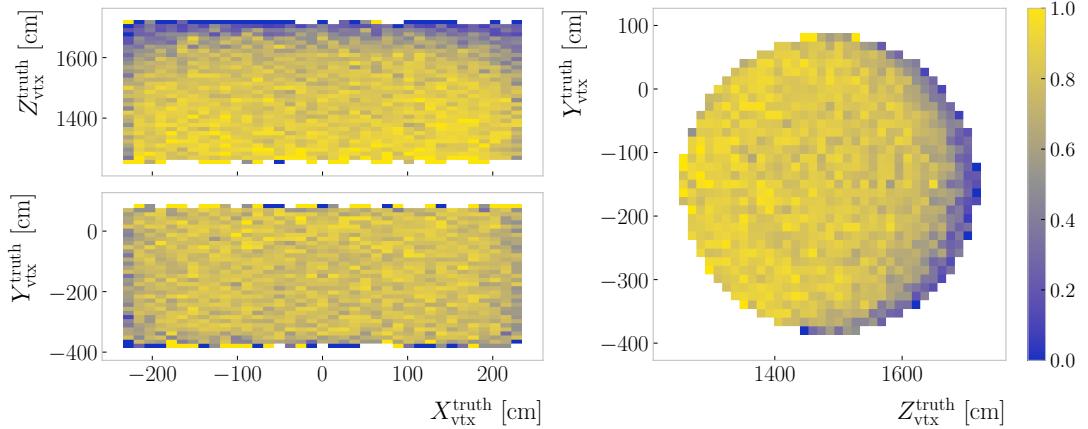


Figure 7.10: Efficiency 2D distributions for the ν_μ CC selection given the true position of the interaction vertex.

worth in the rejection of $\bar{\nu}_\mu$ CC events, which drop almost by one order of magnitude.
 Additionally, the charge selection cuts the NC events in half, as it reduces the chances of misidentifying a positively charged hadron for a muon.
 As an additional check, I explored how the performance of the ν_μ CC selection depends on the position of the neutrino interaction within the HPgTPC. Maps of the selection efficiency for the X, Z (top left panel), X, Y (bottom left panel), and Z, Y (right panel) true vertex position pairs are given in Fig. 7.10. It can be seen that the efficiency remains stable along the drift direction, only slightly degrading close to the edges of the FV. Regarding the radial direction, it is clear that an important number of events with high $Z_{\text{vtx}}^{\text{truth}}$ are not being selected. Intuitively, the muons arising from these interactions will leave short tracks. As their directions are typically aligned with the beam direction, they enter the ECal shortly after production. This is likely to affect the tracking, and therefore their identification. As a result, the regions with the lowest efficiency are the downstream corners of the HPgTPC, i.e. the areas with high $|X_{\text{vtx}}^{\text{truth}}|$ and $Z_{\text{vtx}}^{\text{truth}}$.

7.2.3 Primary muon kinematics

This ν_μ CC selection relies on the identification of the a primary muon, meaning that for each selected event a particle is picked out as the muon candidate. It is because of

CHAPTER 7. EVENT SELECTION IN ND-GAR

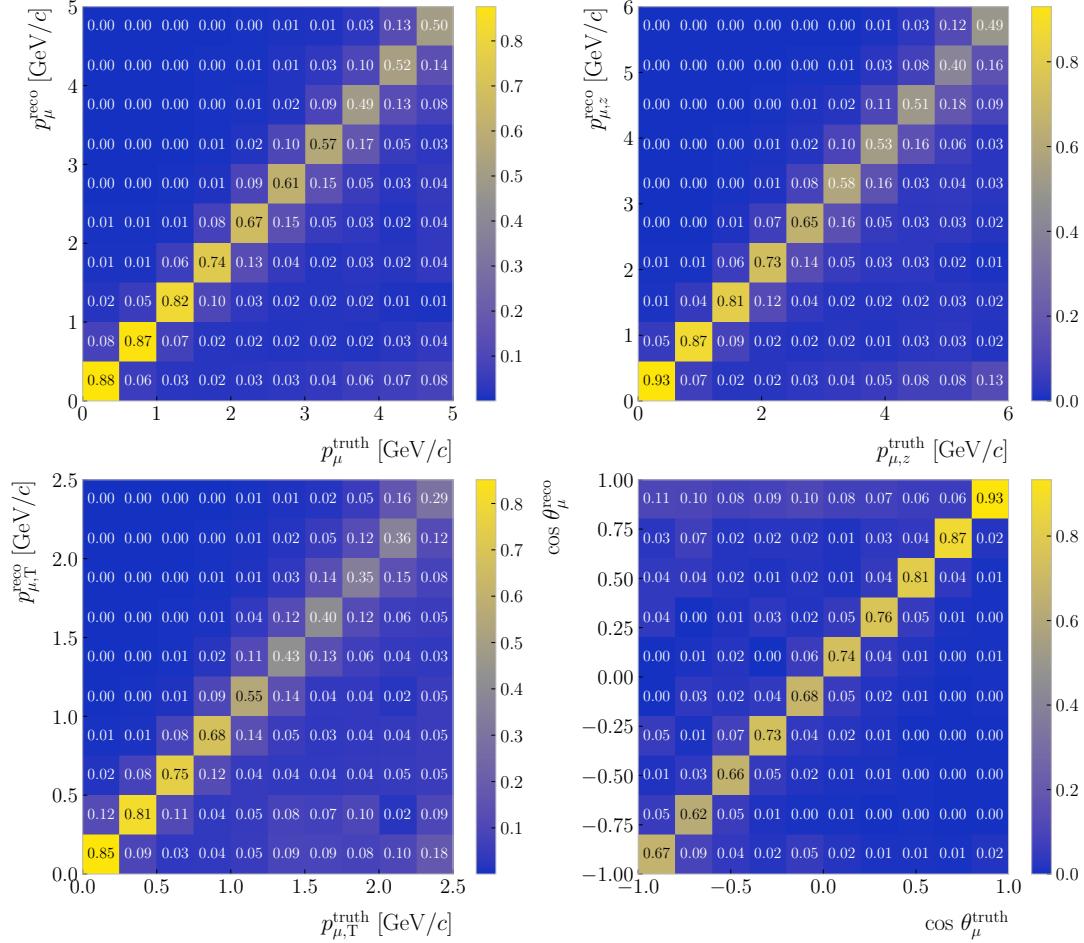


Figure 7.11: Distributions for the reconstructed versus truth generated primary muon momentum (top left panel), longitudinal momentum (top right panel), transverse momentum (bottom left panel), and beam angle (bottom right panel). The reconstructed values correspond to the selected primary muon candidate, whereas the truth values come from the true primary muon in the event.

4148 this that one can study the kinematics of these selected primary muons.

4149 Figure 7.11 shows a comparison between some of the reconstructed and truth primary
 4150 muon kinematic variables. From top to bottom, left to right, we have muon momentum,
 4151 longitudinal momentum, transverse momentum and beam angle. The histograms are
 4152 column-normalised, and so the diagonal entries give an idea of the resolution for the
 4153 different variables. The match between truth and reconstructed values can only be done
 4154 for the selected true ν_{μ} CC events, as the others do not have a primary muon. However,
 4155 for this comparison I do not require the events to start inside the FV.

7.2. ν_μ CC SELECTION

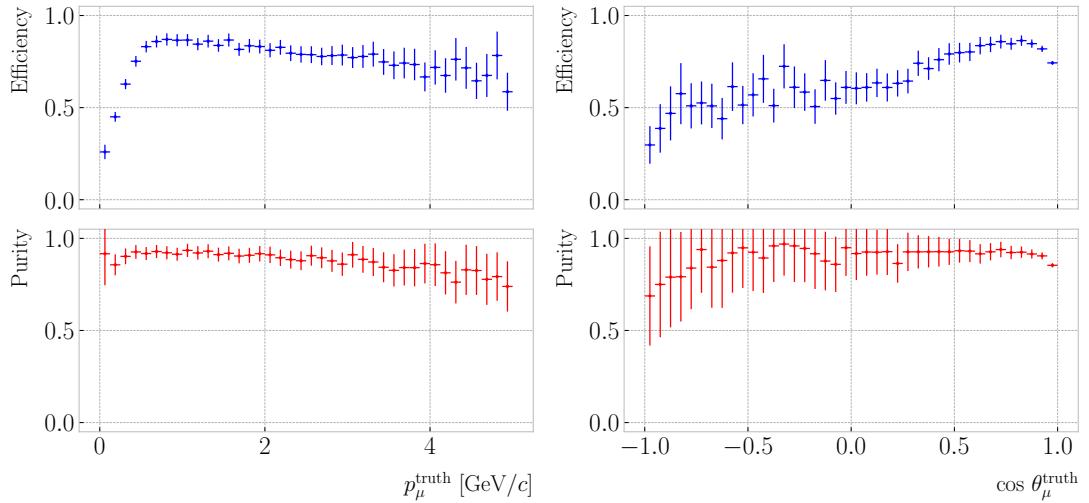


Figure 7.12: Efficiency (blue) and purity (red) of the ν_μ CC selection as a function of the primary muon true momentum (left panel) and beam angle (right panel).

4156 Notice that, for the reconstructed values, the variables do not necessarily come
 4157 from a reconstructed particle that matches the true primary muon. In other words,
 4158 sometimes, even though the event was correctly identified, the primary muon may have
 4159 been confused with another particle. That means that in these distributions include
 4160 both reconstruction and selection deficiencies.

4161 I also studied the performance of the ν_μ CC selection as a function of the kinematic
 4162 variables of the primary muon. As before, these metrics are only possible to compute for
 4163 true ν_μ CC events. The efficiency (top panels) and purity (bottom panels) as a function
 4164 of the truth muon momentum (left) and beam angle (right) are shown in Fig. 7.12. One
 4165 can see that there are some similarities in the behaviour of both metrics between the
 4166 true neutrino energy and the muon momentum cases. This is to be expected, as these
 4167 two variables are highly correlated. For the efficiency, there is a rapid increase at low
 4168 momentum values until it peaks at around 1 GeV/c, after which it starts decreasing
 4169 slowly. The purity remains relatively constant, with a slight drop towards high p_μ^{truth}
 4170 values. In the case of the muon angle, the decrease in efficiency at high $\theta_\mu^{\text{truth}}$ is more
 4171 noticeable. However, note that the number of events with backward-going muons is
 4172 much smaller than those aimed towards the forward direction, as can be seen from the

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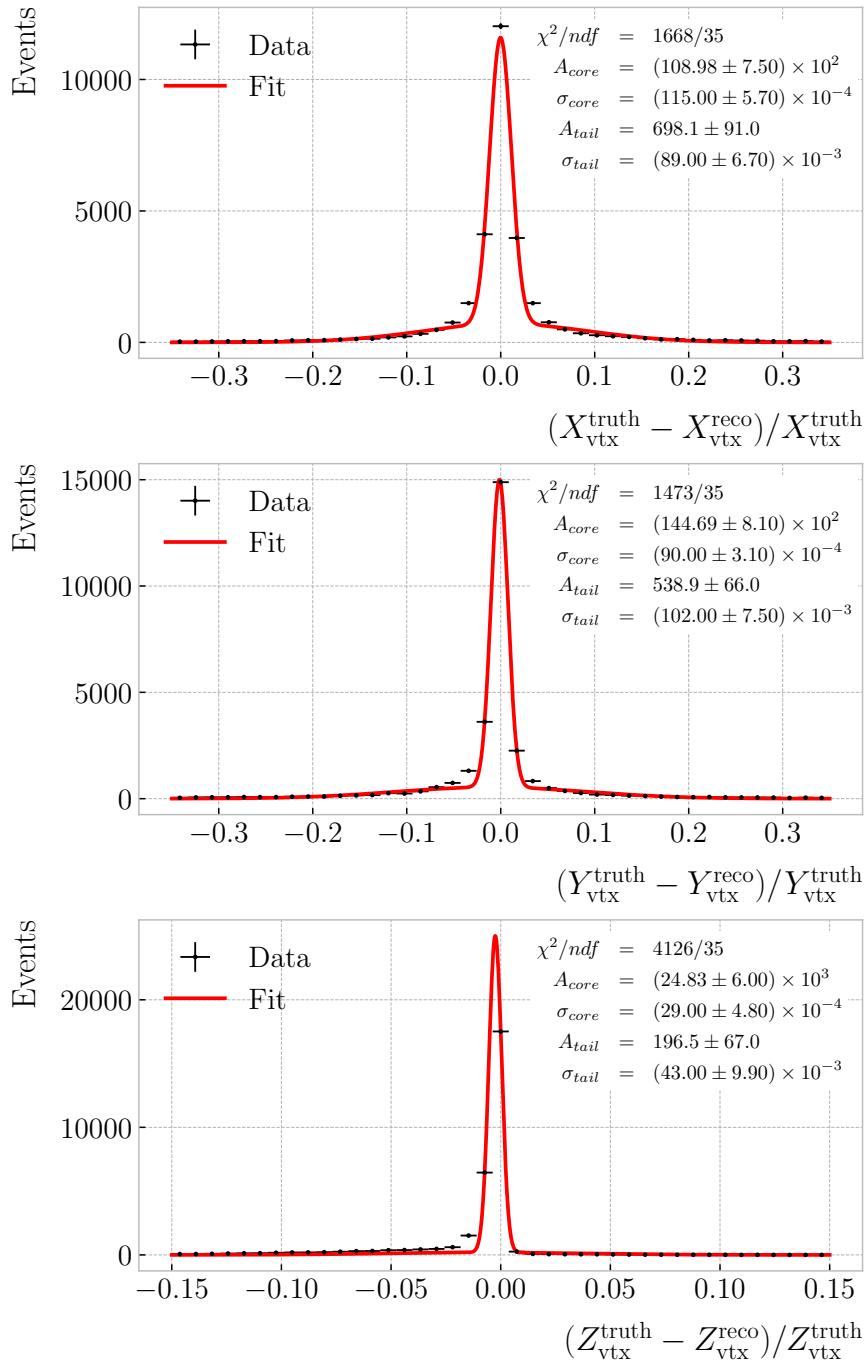


Figure 7.13: Fractional residual distributions for the position of the primary vertex in the ν_μ CC selection. The best fits to a double Gaussian function are also shown (red lines).

7.3. CHARGED PION IDENTIFICATION

4173 size of the vertical error bars. There is also a decline in the purity with the beam angle,
4174 but this effect is much smaller.

4175 A byproduct of selecting the primary lepton in the interaction is the position
4176 of the reconstructed neutrino vertex candidate. Checking how the position of the
4177 selected reconstructed primary vertex and the true vertex position compare is needed to
4178 understand the validity of our method. Figure 7.13 shows the distributions of fractional
4179 residuals between the truth and reconstructed vertex positions in the X (top panel),
4180 Y (middle panel), and Z (bottom panel) directions. Performing a double Gaussian fit
4181 to the distributions (red lines), I estimate the reconstructed vertex resolution achieved
4182 with this method to be $1.62 \pm 0.08\%$, $1.23 \pm 0.05\%$, and $0.32 \pm 0.05\%$ for the X , Y ,
4183 and Z directions, respectively. As expected, the resolution along the drift direction.
4184 However, the significant difference in resolution between the two transverse directions is
4185 worth noting. Not only the resolution is better for the Z direction, but the layout of the
4186 residual distribution is highly asymmetrical. This may be related to the variability in
4187 the selection efficiency along that direction.

4188 7.3 Charged pion identification

4189 Now that I have checked the robustness of the proposed ν_μ CC selection, it can be
4190 used as a starting point for other, more convoluted, selections. One of the priorities
4191 of ND-GAr, as mentioned previously, is the identification of pions. With its lower
4192 tracking thresholds, ND-GAr is expected to do better regarding π^\pm identification than
4193 the traditional LArTPCs, like ND-LAr. Moreover, it can make use of the different
4194 detector subcomponents to tag the charged pions.

4195 The ν_μ CC selection provides a starting point for the pion identification. The first
4196 thing one can do is rule out the selected primary muon candidate. Then, by looking at
4197 the properties of the rest of the reconstructed particles, one can start the counting of
4198 the charged pions.

4199 The two proton scores, the one based on the dE/dx in the HPgTPC and the one

CHAPTER 7. EVENT SELECTION IN ND-GAR

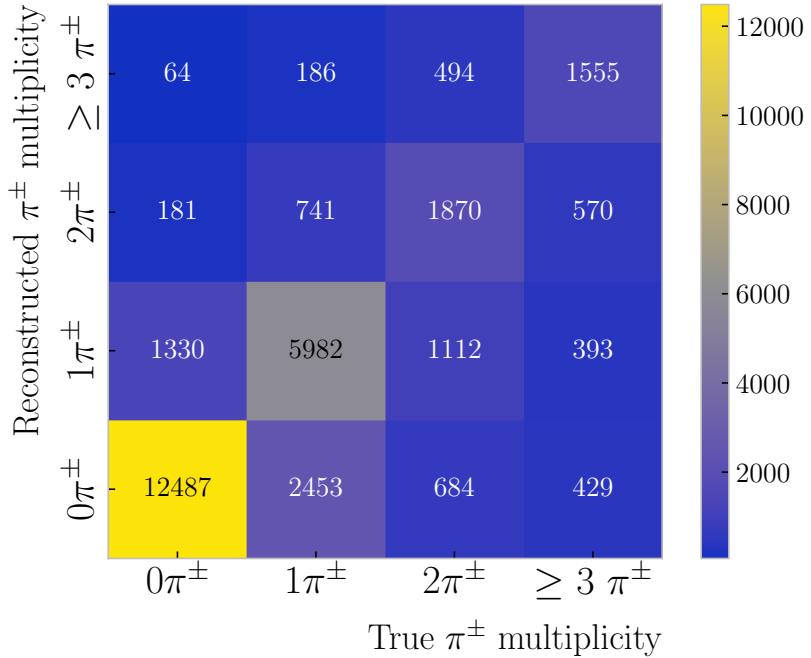


Figure 7.14: Distribution of events given their true and reconstructed π^\pm multiplicity, for the selection given by $p_{dE/dx}^{\text{cut}} = p_{\text{ToF}}^{\text{cut}} = 0.50$, $\Delta_{dE/dx}^{\pi^\pm} = 0.20$, and $d_\mu^{\text{cut}} = 50.0$ cm.

4200 obtained from the ToF measurement in the ECal, can be used to separate the protons
 4201 from the sample of charged pions. By providing appropriate cuts for these, a good
 4202 separation can be achieved.

4203 Another source of information available is the dE/dx of the track associated to the
 4204 reconstructed particle. To select the charged pions, we can require that the measured
 4205 mean dE/dx is compatible with the expectation for a true π^\pm , in other words:

$$\left\langle \frac{dE}{dx} \right\rangle_{\pi^\pm} \left(1 - \Delta_{dE/dx}^{\pi^\pm} \right) \leq \left\langle \frac{dE}{dx} \right\rangle_{\text{meas.}} < \left\langle \frac{dE}{dx} \right\rangle_{\pi^\pm} \left(1 + \Delta_{dE/dx}^{\pi^\pm} \right), \quad (7.6)$$

4206 where the parameter $\Delta_{dE/dx}^{\pi^\pm}$ measures the fractional variation one allows around the
 4207 theoretical expectation. To obtain the expected mean dE/dx of a charged pion with a
 4208 given momentum, I use the ALEPH parametrisation with the parameter values obtained
 4209 previously.

4210 Also, as we are only interested in the primary pions, and because these are by
 4211 definition close to the interaction vertex, one can apply an additional distance cut. Using

7.3. CHARGED PION IDENTIFICATION

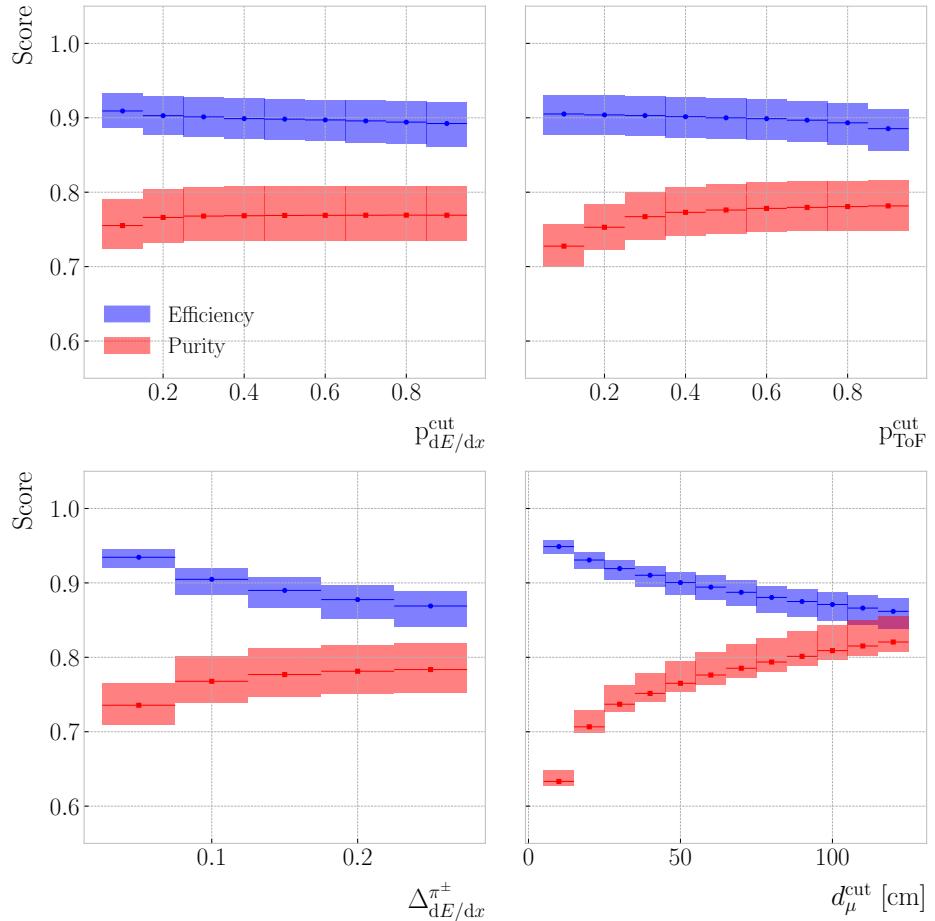


Figure 7.15: Efficiency (blue) and purity (red) for the ν_μ CC $0\pi^\pm$ selection as a function of the proton dE/dx score cut (top left panel), proton ToF score cut (top right panel), pion dE/dx cut (bottom left panel), and distance to muon cut (bottom right panel). The height of the boxes represents the IQR of the conditional distributions, whereas the line corresponds to the median.

4212 the start position of the muon candidate, we can restrict the starting point of pions to a
 4213 certain volume around the vertex.

4214 Combining all these ideas, I propose the following procedure to identify the charged
 4215 pions in an event:

- 4216 1. Apply ν_μ CC selection.
 4217 2. Disregard particle selected as primary muon.
 4218 3. Remove particles with momentum below threshold.

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- 4219 4. Select particles with proton dE/dx score below threshold.
- 4220 5. Select particles with proton ToF score below threshold.
- 4221 6. Select particles with mean dE/dx around the expected value for a pion.
- 4222 7. Remove particles with a distance between the start of the track and the primary
4223 vertex greater than the cut.

4224 The remaining particles after all these cuts are taken to be charged pion candidates.

4225 This counting method depends on four cuts, denoted by $p_{dE/dx}^{\text{cut}}$, $p_{\text{ToF}}^{\text{cut}}$, $\Delta_{dE/dx}^{\pi^\pm}$, and
4226 d_μ^{cut} in order of appearance. The momentum threshold is necessary to compare with
4227 the true multiplicity. For values of the kinetic energy lower than 10 – 20 MeV, we
4228 do not expect to be able to tag individual pions. Such low energy particles just leave
4229 small traces in the TPC which, together with the busy environment of the neutrino
4230 interaction vertex, leaves one with no other option but to only account for their energy
4231 calorimetrically. As such, the true pion counting also features this momentum threshold.

4232 I performed an optimisation of the charged pion counting by scanning the space of
4233 possible cut configurations. For the two proton scores, I let them vary between 0.10 to
4234 0.90, in increments of 0.10. Similarly, the parameter $\Delta_{dE/dx}^{\pi^\pm}$ takes values in the range
4235 0.05 – 0.25, with a step size of 0.05. Finally, the distance cut changes in 10 cm steps,
4236 from 10 to 120 cm.

4237 For each combination of selection cuts, I compare the true charged pion multiplicity
4238 given by GENIE with the number of charged pion candidates I count with this method,
4239 hereafter referred to as the reconstructed π^\pm multiplicity. The result of this comparison
4240 is a matrix, with columns and rows indicating true and reconstructed charged pion
4241 multiplicity, respectively. An example of one of these matrices, obtained for a certain
4242 configuration of cuts, can be seen in Fig. 7.14. From these multiplicity matrices one can
4243 extract performance metrics, like efficiency, purity, and significance.

7.4. NEUTRAL PION IDENTIFICATION

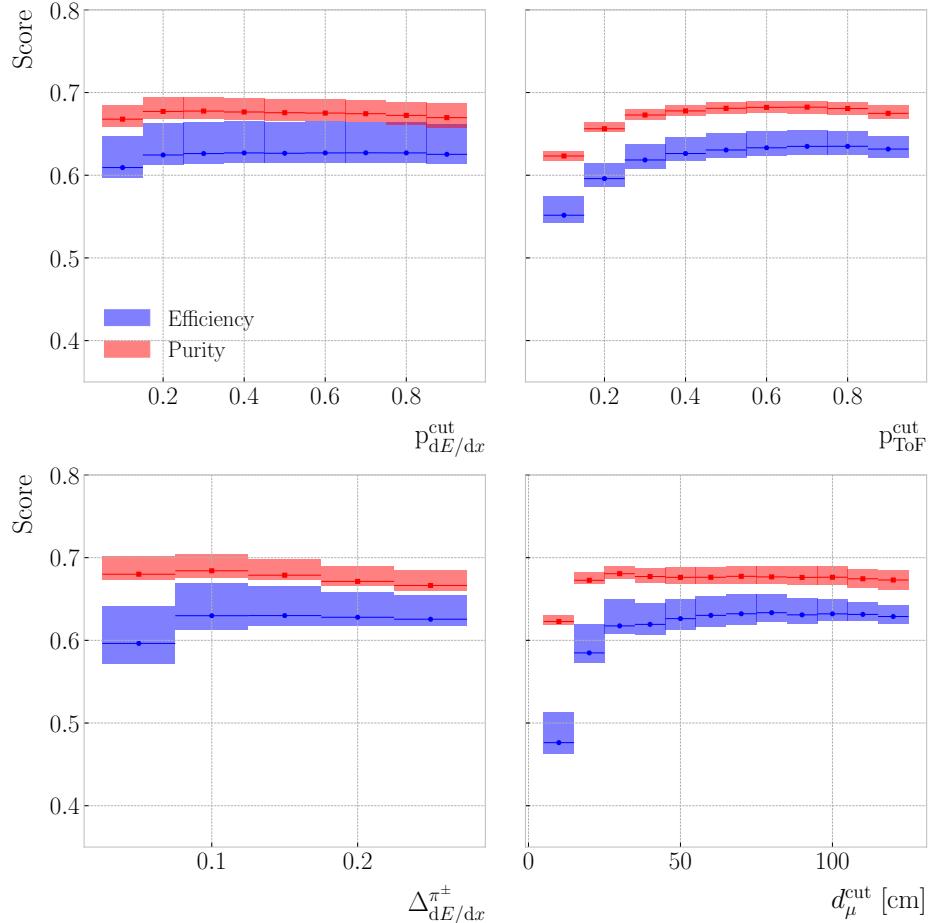


Figure 7.16: Efficiency (blue) and purity (red) for the ν_μ CC $1\pi^\pm$ selection as a function of the proton dE/dx score cut (top left panel), proton ToF score cut (top right panel), pion dE/dx cut (bottom left panel), and distance to muon cut (bottom right panel). The height of the boxes represents the IQR of the conditional distributions, whereas the line corresponds to the median.

4244 7.3.1 ν_μ CC $1\pi^\pm$ selection

4245 7.4 Neutral pion identification

4246 7.5 Systematic uncertainties

4247 7.5.1 Flux uncertainties

4248 The neutrino flux prediction is affected by systematic uncertainties arising from two
 4249 sources: the uncertainties in the production of hadrons in the target and the uncertainties

CHAPTER 7. EVENT SELECTION IN ND-GAR

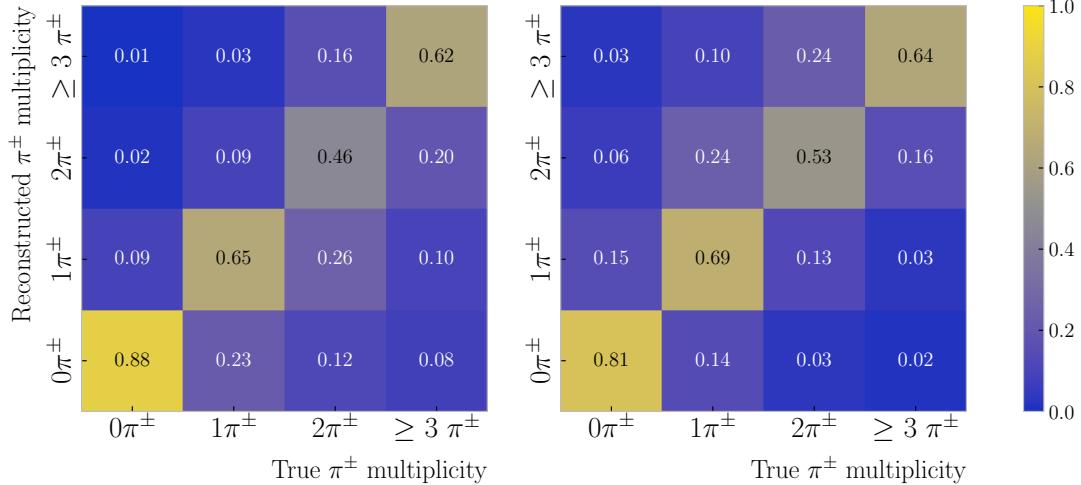


Figure 7.17: Distribution of events given their true and reconstructed π^\pm multiplicity, both column-wise (left panel) and row-wise (right panel) normalised, for the selection that maximises the significance of the ν_μ CC $1\pi^\pm$ selection. The column normalisation yields the efficiency in the diagonal entries, whereas the row normalisation reveals the purity.

in the design parameters of the beamline itself. These fluxes and their uncertainties are generated with the G4LBNF simulation [85], a Geant4 implementation of the LBNF beamline, and the Package to Predict the FluX (PPFX) framework, originally developed for MINERvA [167].

The hadron production uncertainties are associated to the kinematic distributions of the hadrons produced when the protons interact with the carbon target, as well as the possible interactions of the hadrons with the beamline materials. The PPFX package estimates these uncertainties by performing a number of random throws of the production model parameters [168]. This way, different predictions of the LBNF flux are generated, which can be compared to the nominal prediction to build a matrix of the covariances between neutrino energies, flavours and running modes (either FHC or RHC). The resulting hadron production uncertainties are described by the eigenvectors associated to the largest eigenvalues in this matrix, obtained performing a PCA analysis.

The other set of uncertainties affecting the neutrino flux prediction come from the limited precision with which we know the parameters of the different components in the beamline. These include the specifications of the target, the dimensions of the decay

7.5. SYSTEMATIC UNCERTAINTIES

4266 pipe, and the current and alignment of the magnetic horns. The effects on the flux
4267 predictions of these uncertainties are estimated using the G4LBNF simulation. For each
4268 of the parameters, the simulation runs with said parameter shifted by $\pm 1\sigma$ from the
4269 nominal value, and the resulting flux prediction is compared to the nominal one.

4270 7.5.2 Cross section uncertainties

4271 7.5.3 Detector uncertainties

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4272

Conclusion and outlook

4273

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A [REDACTED]

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An appendix

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