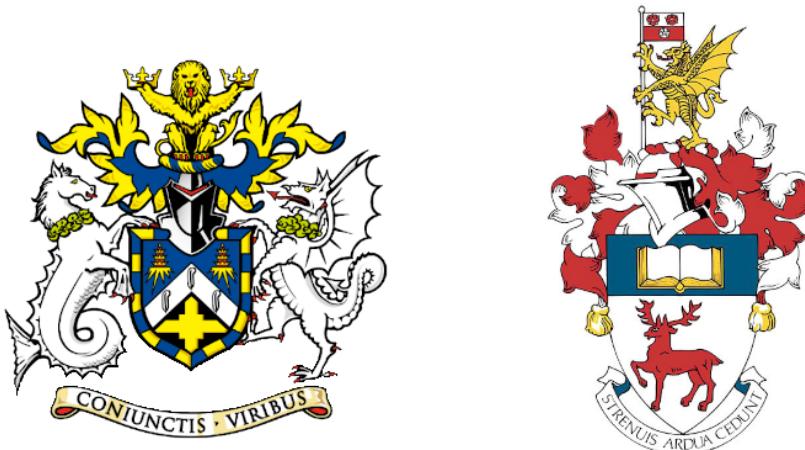


<sup>1</sup> ADVANCING NEUTRINO  
<sup>2</sup> DETECTION AND TRIGGERING IN  
<sup>3</sup> DUNE



<sup>5</sup> Francisco Martínez López

<sup>6</sup> Submitted in partial fulfillment of the requirements  
<sup>7</sup> of the Degree of Doctor of Philosophy

<sup>8</sup> School of Physical and Chemical Sciences  
<sup>9</sup> Queen Mary University of London

<sup>10</sup> School of Physics and Astronomy  
<sup>11</sup> University of Southampton

<sup>12</sup> December 2024



13

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# Abstract

31

32 Work in progress ...



*¡Oh memoria, enemiga mortal de mi descanso!*

---

*El ingenioso hidalgo don Quijote de la Mancha*

MIGUEL DE CERVANTES SAAVEDRA



## Acknowledgements

34 Work in progress ...



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## List of Abbreviations

<b>ADC</b>	Analog to Digital Converter.
<b>ALEPH</b>	Apparatus for LEP PHysics.
<b>ALICE</b>	A Large Ion Collider Experiment.
<b>BDT</b>	Boosted Decision Tree.
<b>CC</b>	Charged Current.
<b>DM</b>	Dark Matter.
<b>DUNE</b>	Deep Underground Neutrino Experiment.
<b>ECal</b>	Electromagnetic Calorimeter.
<b>FD</b>	Far Detector.
<b>FHC</b>	Forward Horn Current.
<b>HPgTPC</b>	High Pressure gaseous Time Projection Chamber.
<b>LBL</b>	Long BaseLine.
<b>MuID</b>	Muon IDentification system.
<b>NC</b>	Neutral Current.
<b>ND</b>	Near Detector.
<b>ND-GAr</b>	Near Detector Gaseous Argon.
<b>ND-LAr</b>	Near Detector Liquid Argon.
<b>PDG</b>	Particle Data Group.
<b>RHC</b>	Reverse Horn Current.



1

592

## Introduction

593



# Neutrino physics

596        *Little particles of inspiration sleet through the universe all the time traveling  
597        through the densest matter in the same way that a neutrino passes through a  
598        candyfloss haystack, and most of them miss.*

599

– Terry Pratchett, *Sourcery*

600        Ever since they were postulated in 1930 by Wolfgang Pauli to explain the continuous  
601         $\beta$  decay spectrum [15] and later found by F. Reines and C. Cowan at the Savannah  
602        River reactor in 1953 [16], neutrinos have had a special place among all other elementary  
603        particles. They provide a unique way to probe a wide range of quite different physics,  
604        from nuclear physics to cosmology, from astrophysics to colliders. Moreover, there is  
605        compelling evidence to believe that the study of neutrinos may be key to unveil different  
606        aspects of physics beyond the SM, difficult to test elsewhere.

607        In this Chapter, I will review the basics of neutrino physics, from its role within the  
608        SM to the main open questions related to the neutrino sector, paying special attention  
609        to the phenomenology of neutrino oscillations.

## 610      2.1 Neutrinos in the SM

611        The SM of fundamental interactions was initially proposed in 1967 by S. Glashow, S.  
612        Weinberg and A. Salam[17–19]. This theoretical framework describes the dynamics  
613        of leptons and quarks, by introducing a collection of mediating gauge vector bosons  
614        and one scalar particle, known as the Higgs boson. It assumes that the local  $SU(3) \times$

## CHAPTER 2. NEUTRINO PHYSICS

615 SU(2)<sub>L</sub> × U(1)<sub>Y</sub> gauge symmetry is an internal symmetry of the system, with SU(3)  
 616 describing quantum chromodynamics, and SU(2)<sub>L</sub> × U(1)<sub>Y</sub> being the gauge groups of  
 617 the electroweak sector. For a detailed overview of the SM of electroweak interactions,  
 618 see Ref. [20].

619 In the SM, neutrinos appear in three flavours, namely  $\nu_e$ ,  $\nu_\mu$ , and  $\nu_\tau$ . These are  
 620 associated with the corresponding charged leptons,  $e$ ,  $\mu$ , and  $\tau$ . Neutrinos exist only  
 621 as left-handed particles, grouped in doublets with the charged leptons, while the later  
 622 come in both chirality states:

$$\begin{pmatrix} \nu_e \\ e_L^- \end{pmatrix}, \quad \begin{pmatrix} \nu_\mu \\ \mu_L^- \end{pmatrix}, \quad \begin{pmatrix} \nu_\tau \\ \tau_L^- \end{pmatrix}, \quad e_R^-, \quad \mu_R^-, \quad \tau_R^-. \quad (2.1)$$

623 Similarly, quarks also exist in both chirality states, and are grouped as:

$$\begin{pmatrix} u_L \\ d_L \end{pmatrix}, \quad \begin{pmatrix} s_L \\ c_L \end{pmatrix}, \quad \begin{pmatrix} t_L \\ b_L \end{pmatrix}, \quad u_R, \quad d_R, \quad s_R, \quad c_R, \quad t_R, \quad b_R. \quad (2.2)$$

624 The fact that there are no right-handed neutrino fields implies that neutrinos are  
 625 strictly massless within the SM. This restriction follows from the experimental observation  
 626 that all neutrinos produced via weak interactions are pure left-handed helicity states  
 627 (and similarly antineutrinos are pure right-handed states). The hypothetical existence  
 628 of right-handed neutrinos could be indirectly inferred from the observation of non-zero  
 629 neutrino masses, nevertheless the existence of neutrino masses is not a sufficient condition  
 630 for the existence of such fields.

631 Left and right-handed fermions transform differently under SU(2)<sub>L</sub> × U(1)<sub>Y</sub> rotations,  
 632 as the right-handed particles are singlets under SU(2)<sub>L</sub>. Applying a local transformation,  
 633 they change as:

$$\begin{aligned} \psi_L &\longrightarrow e^{-iY\beta(x)/2} e^{-iT_a\alpha_a(x)} \psi_L, \\ \psi_R &\longrightarrow e^{-iY\beta(x)/2} \psi_R, \end{aligned} \quad (2.3)$$

634 where  $Y/2$  and  $T_a$  are the generators of SU(2)<sub>L</sub> and U(1)<sub>Y</sub>, respectively, and  $\beta(x)$  and

## 2.1. NEUTRINOS IN THE SM

**Table 2.1:** Values of  $T_3$  and  $Y/2$  assigned to the first generation of fermions.

	$e_L$	$\nu_e$	$e_R$	$u_L$	$d_L$	$u_R$	$d_R$
$T_3$	-1/2	1/2	0	1/2	-1/2	0	0
$Y/2$	-1/2	-1/2	-1	1/6	1/6	2/3	-1/3

635  $\alpha_a(x)$  are the parameters of the rotation.

636 The values of the quantum numbers  $Y/2$  and  $T_3$ , the third component of the weak  
 637 isospin, have to be assigned to the different particles. The values of  $T_3$  follow from the  
 638 commutation relations of the generators of  $SU(2)$ . After the spontaneous symmetry  
 639 breaking  $SU(2)_L \times U(1)_Y \rightarrow U(1)_{EM}$ , one finds the relation which determines the electric  
 640 charge:

$$Q = T_3 + \frac{Y}{2}, \quad (2.4)$$

641 Setting the electric charge to  $-1$  for electrons, we can find the values of the hypercharge  
 642 for the rest of the fermions. The resulting values for the first generation of leptons and  
 643 quarks are shown in Tab. 2.1.

644 It is clear that the free Lagrangian of the theory is not be invariant under the gauge  
 645 transformations, as the kinetic terms contain derivatives. Therefore, to make it invariant,  
 646 one needs to introduce a set of gauge bosons. They appear in the so-called covariant  
 647 derivative, which replaces the common derivative and transforms in the same way as the  
 648 fermion fields under local rotations. This constrain fixes completely the transformations  
 649 of the spin-1 fields. For left and right-handed particles, the covariant derivatives are  
 650 given by:

$$\begin{aligned} D_\mu \psi_L &= \left( \partial_\mu + ig' \frac{Y}{2} B_\mu + ig T_a W_\mu^a \right) \psi_L, \\ D_\mu \psi_R &= \left( \partial_\mu + ig' \frac{Y}{2} B_\mu \right) \psi_R, \end{aligned} \quad (2.5)$$

651 where  $W_\mu^i$ ,  $i = 1, 2, 3$  and  $B_\mu$  are the gauge bosons for the  $SU(2)_L$  and  $U(1)_Y$  factors,  
 652 respectively, and  $g$  and  $g'$  are the corresponding gauge couplings. It can be shown that  
 653 these fields transform in the adjoint representation of the gauge group.

## CHAPTER 2. NEUTRINO PHYSICS

**Table 2.2:** Neutral current couplings.

	$u$	$d$	$\nu_e$	$e$
$2v_f$	$1 - \frac{8}{3}\sin^2\theta_W$	$-1 + \frac{4}{3}\sin^2\theta_W$	1	$-1 + 4\sin^2\theta_W$
$2a_f$	1	-1	1	-1

So far, the theory only contains massless particles, as adding bare mass terms to the Lagrangian would spoil the gauge symmetry. Therefore, the mass terms need to be induced by a spontaneous violation of the symmetries. In the SM, the responsible for this is the Higgs mechanism. The Higgs doublet is coupled to the gauge bosons through the covariant derivative, and to the fermions through the Yukawa couplings. Upon spontaneous symmetry breaking, the vacuum expectation value of the Higgs field generate the mass terms of the particles.

In order to obtain the physical intermediate vector boson states, we need to perform the following redefinitions:

$$\begin{aligned} A_\mu &= \sin \theta_W W_\mu^3 + \cos \theta_W B_\mu, \\ Z_\mu &= \cos \theta_W W_\mu^3 - \sin \theta_W B_\mu, \\ W_\mu^\pm &= \frac{1}{\sqrt{2}} (W_\mu^1 \mp i W_\mu^2), \end{aligned} \tag{2.6}$$

where  $A_\mu$  is the photon field, and  $Z_\mu$  and  $W_\mu^\pm$  are the neutral and the charged weak boson fields, respectively. The Weinberg angle,  $\theta_W$ , relates the weak coupling constants and the electric charge:

$$e = g' \cos \theta_W = g \sin \theta_W. \tag{2.7}$$

At this point, the interacting part of the electroweak Lagrangian can be re-written as the sum of three contributions: the electromagnetic (EM), charged-current (CC) and neutral-current (NC) components:

$$\begin{aligned} \mathcal{L}_{\text{EW}}^{\text{int}} &= \mathcal{L}_{\text{EM}} + \mathcal{L}_{\text{CC}} + \mathcal{L}_{\text{NC}} \\ &= -e A_\mu J_{\text{EM}}^\mu - \frac{g}{2\sqrt{2}} (W_\mu^+ J_{\text{CC}}^\mu + \text{h.c.}) - \frac{g}{2\cos\theta_W} Z_\mu J_{\text{NC}}^\mu, \end{aligned} \tag{2.8}$$

## 2.2. TROUBLE IN THE NEUTRINO SECTOR

669 with the currents defined as:

$$\begin{aligned} J_{\text{EM}}^\mu &= \sum_f Q_f \bar{f} \gamma^\mu f, \\ J_{\text{CC}}^\mu &= \sum_\ell \bar{\nu}_\ell \gamma^\mu (1 - \gamma_5) \ell + \sum_f \bar{u}_f \gamma^\mu (1 - \gamma_5) d_f, \\ J_{\text{NC}}^\mu &= \sum_f \bar{f} \gamma^\mu (v_f - a_f \gamma_5) f, \end{aligned} \quad (2.9)$$

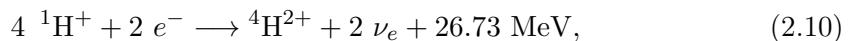
670 where  $f$  denotes any SM fermion,  $\ell$  and  $\nu_\ell$  a charged lepton and a neutrino of any flavour,  
671 and  $u_f$  and  $d_f$  an up-like and a down-like quarks of any flavour. For the NC case, the  
672 values of the  $v_f$  and  $a_f$  couplings are given in Tab. 2.2.

673 As seen in Eq. (5.8), in the electroweak theory neutrinos are coupled to the  $Z$  boson  
674 in a universal way. Therefore, by measuring the so-called invisible decay width of the  $Z$   
675 boson we have an estimate of the number of light (i.e. lighter than the  $Z$  boson) neutrino  
676 flavours. This number was measured by LEP in a combined analysis of  $e^+ e^- \rightarrow \mu^+ \mu^-$   
677 and  $e^+ e^- \rightarrow$  hadrons to be  $N_\nu = 2.9840 \pm 0.0082$  [21].

## 678 2.2 Trouble in the neutrino sector

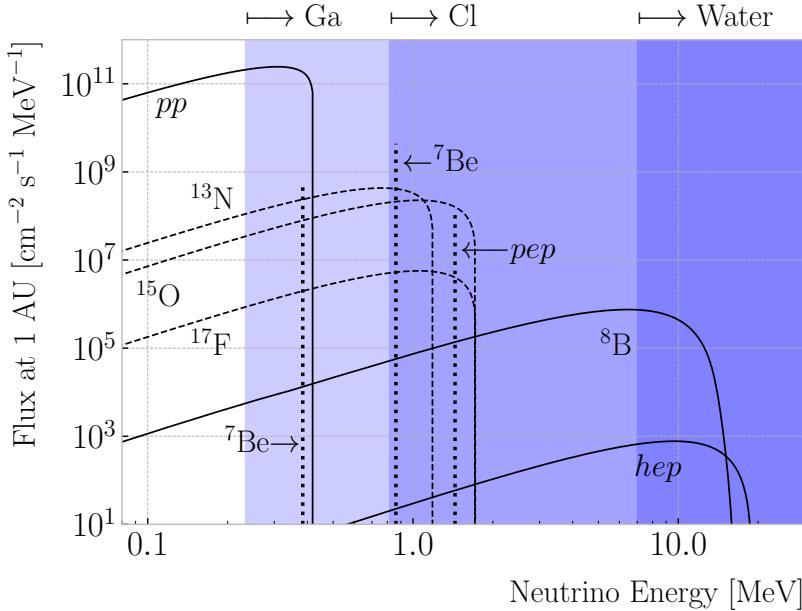
### 679 2.2.1 The solar neutrino problem

680 Neutrinos are produced everywhere in vast amounts. One of the most prominent sources  
681 of neutrinos in our vicinity is our Sun. The Sun is powered mainly by two nuclear fusion  
682 reactions, the p – p chain and the CNO cycle. In both cases, the overall reaction is:



683 where part of the released energy is lost to the neutrinos. The electron neutrinos  
684 produced are often labelled after the processes that generate them. Figure 2.1 shows the  
685 solar neutrino flux as a function of the neutrino energy, broken down by the production  
686 process.

## CHAPTER 2. NEUTRINO PHYSICS



**Figure 2.1:** Solar neutrino fluxes for the solar model BS05(OP). The detection thresholds for Gallium, Chlorine and water-based experiments are also shown. Figure adapted from Ref. [1].

In the late 1960s, the Brookhaven Solar Neutrino Experiment, led by R. Davis, started data taking with the goal of measuring the solar neutrino flux [22]. The experiment used a tank containing  $380 \text{ m}^3$  of tetrachloroethene ( $\text{C}_2\text{Cl}_4$ ), a liquid commonly used in dry-cleaning, located 1.5 km underground in the Homestake mine, in Lead, South Dakota. The incoming neutrinos would get captured following the reaction:

$$\nu_e + {}^{37}\text{Cl} \longrightarrow {}^{37}\text{Ar} + e^-, \quad (2.11)$$

The results of the experiment were compared to the theoretical predictions made by J. Bahcall [23]. During its operation from 1968 to 2002, the experiment observed a solar  $\nu_e$  flux that was approximately a third of the total prediction [24].

In the early 1990s, the SAGE [25] and GALLEX [26] experiments started operations.

## 2.2. TROUBLE IN THE NEUTRINO SECTOR

699 The detection principle used for both experiments was similar to that of the Homestake  
 700 experiment, but using  $^{71}\text{Ga}$  instead of  $\text{C}_2\text{Cl}_4$ . With a detection threshold of 0.233 MeV,  
 701 the Gallium-based experiments were able to observe the  $pp$  neutrino flux. Both  
 702 experiments measured a solar electron neutrino flux that was a factor of two lower  
 703 than the predictions, demonstrating that this deficit was energy-dependent.

704 In the early 2000s, the SNO experiment put an end to the solar neutrino puzzle  
 705 [27, 28]. Thanks to its directionality capabilities, being a Cherenkov light detector, as  
 706 well as to its heavy water target, SNO measured the total solar neutrino flux through  
 707 the NC process:



708 where  $\alpha = e, \mu, \tau$ . This measurement agreed with the solar model predictions. Then,  
 709 measuring the CC reaction:



710 they were able to establish that the  $\nu_\mu$  and  $\nu_\tau$  solar fluxes are in fact non-zero, revealing  
 711 that electron neutrinos were transitioning into different flavours.

### 712 2.2.2 The atmospheric neutrino problem

713 When cosmic-rays interact with the atoms in the upper atmosphere, a plethora of  
 714 hadrons, mainly  $\pi$  and  $K$  mesons, are produced. In particular, for the charged pions,  
 715 we have the following decay chain dominates:

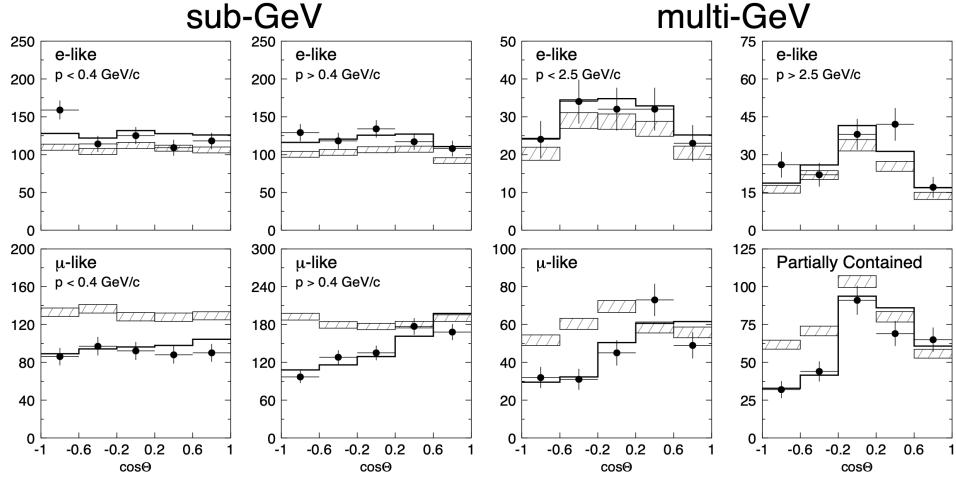


716 and similar for the antiparticles. For neutrino energies  $< 1$  GeV, the ratio:

$$\frac{N(\nu_\mu + \bar{\nu}_\mu)}{N(\nu_e + \bar{\nu}_e)}, \quad (2.15)$$

717 of produced neutrinos and antineutrinos is, in good approximation, equal to two [29].

## CHAPTER 2. NEUTRINO PHYSICS



**Figure 2.2:** Zenith angle distributions for the selected  $\nu_e$  (top row) and  $\nu_\mu$  (bottom row) events in the SK detector. The hatched region corresponds to the expectation in the case of no oscillations, whereas the solid line indicates the best-fit in the case of  $\nu_\mu \rightarrow \nu_\tau$  oscillations. Figure taken from Ref. [34].

718 During the 1980s, several proton decay experiments, like Kamiokande [30], IMB [31],

719 MACRO [32], and Soudan-2 [33], measured the flux of atmospheric neutrinos. This was  
720 an important part of their research programme, as the atmospheric neutrinos constitute  
721 their main background. All these experiments reported an atmospheric neutrino ratio  
722 lower than the predictions.

723 A few years before the SNO discovery, in 1998, Super-Kamiokande (SK) collaboration

724 measured the atmospheric  $\nu_e$  and  $\nu_\mu$  spectra as a function of the zenith angle [34].  
725 Upward-going particles have negative zenith angle,  $\cos \Theta < 0$ , indicating that they  
726 entered from the bottom of the detector. These upward-going neutrinos had to travel  
727 through the Earth in order to reach the detector, allowing SK to probe a broad range  
728 of baselines. Figure 2.2 shows the reported distributions (black dots), compared to the  
729 no oscillations prediction (hatched region). This measurement confirmed that muon  
730 neutrinos transition to other flavours, and that this phenomenon depends both on the  
731 energy and the path length of the neutrino.

732 The SK and SNO findings provided definitive evidence for the existence of neutrino

733 oscillations, and therefore non-zero neutrino masses. This constitutes one of the  
734 groundbreaking discoveries of modern physics and has acted as driving force for beyond

## 2.3. MASSIVE NEUTRINOS

the Standard Model (BSM) physics. The minimal extension of the SM we can do to address these phenomena is introducing different masses for at least two of the neutrinos. This way, we are left with three neutrino mass eigenstates  $\nu_1$ ,  $\nu_2$ , and  $\nu_3$ , with masses  $m_1$ ,  $m_2$ , and  $m_3$  respectively, which in general will not coincide with the flavour eigenstates,  $\nu_e$ ,  $\nu_\mu$ , and  $\nu_\tau$ .

### 2.3 Massive neutrinos

The existence of neutrino oscillations imply that neutrinos are massive particles. However, as we have seen before, within the SM neutrinos are massless, as they do not have a mass term in the Lagrangian. If one wants to give neutrinos a mass, the particle content of the SM needs to be expanded.

A way of generating massive neutrinos while maintaining gauge invariance is by introducing an arbitrary number of sterile neutrinos  $N_i$ ,  $i = 1, \dots, m$ . These allow for two different types of neutrino mass terms:

$$-\mathcal{L}_{M_\nu} = \sum_{i=1}^m \sum_{j=1}^3 M_D^{ij} \bar{N}_i \nu_{Lj} + \frac{1}{2} \sum_{i=1}^m \sum_{j=1}^m M_N^{ij} \bar{N}_i N_j^c + \text{h.c.}, \quad (2.16)$$

where  $M_D$  is a complex  $m \times 3$  matrix and  $M_N$  a complex and symmetric  $m \times m$  matrix. The first term, often referred to as the Dirac mass term, arises from the corresponding Yukawa interaction after the spontaneous electroweak symmetry breaking, similar to the other fermions. The second term, called the Majorana mass term, is allowed in the Lagrangian, as it is a singlet of the gauge group. However, it violates lepton number conservation by two units.

If one imposes lepton number symmetry conservation, the Majorana term must banish,  $M_N = 0$ . In this case, if  $m = 3$  we can identify the sterile neutrinos as the right-handed component of the neutrino field. The Dirac mass matrix can be diagonalised using two unitary matrices,  $V_R^\nu$  and  $V_L^\nu$ , as:

$$M_D = V_R^\nu \text{ diag}(m_1, m_2, m_3) V_L^{\nu\dagger}, \quad (2.17)$$

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758 where  $m_i$ ,  $i = 1, 2, 3$  are the masses of the three neutrino mass eigenstates.

759 The neutrino mass term can be written in term of the resulting eigenstates as:

$$-\mathcal{L}_{M_\nu} = \sum_{i=1}^3 m_i \bar{\nu}_{Di} \nu_{Di}, \quad (2.18)$$

760 with:

$$\nu_{Di} = \left( V_L^{\nu\dagger} \nu_L \right)_i + \left( V_R^{\nu\dagger} N \right)_i. \quad (2.19)$$

761 In this scenario, both the low energy particle budget and the symmetries of the SM  
 762 have to be modified. Moreover, the masses of the neutrinos are generated exclusively  
 763 through the Higgs mechanism, which does not explain why they are much smaller than  
 764 those of the charged leptons.

765 Going back to the general case, we can re-write Eq. (2.16) in matrix form as:

$$-\mathcal{L}_{M_\nu} = \frac{1}{2} \left( \bar{\nu}_L^c, \bar{N} \right) \begin{pmatrix} 0 & M_D^T \\ M_D & M_N \end{pmatrix} \begin{pmatrix} \nu_L \\ N^c \end{pmatrix} + \text{h.c.} = \bar{\nu}^c M_\nu \nu + \text{h.c.}, \quad (2.20)$$

766 with  $\nu = (\nu_L, N^c)^T$  being a  $(3+m)$ -dimensional vector grouping the active and the  
 767 sterile neutrinos. The matrix  $M_\nu$ , which is a complex  $(3+m) \times (3+m)$  symmetric  
 768 matrix, can be diagonalised by means of a unitary matrix  $V^\nu$ , yielding:

$$M_\nu = V^\nu \text{ diag}(m_1, m_2, \dots, m_{3+m}) V^{\nu T}. \quad (2.21)$$

769 Using this eigendecomposition, the neutrino mass term can be expressed as:

$$-\mathcal{L}_{M_\nu} = \frac{1}{2} \sum_{i=1}^{3+m} m_i \bar{\nu}_{Mi} \nu_{Mi}, \quad (2.22)$$

770 where the states  $\nu_{Mi}$ , commonly referred to as Majorana neutrinos, are defined as:

$$\nu_{Mi} = \left( V^{\nu\dagger} \nu \right)_i + \left( V^{\nu\dagger} \nu \right)_i^c, \quad (2.23)$$

771 in such a way that the Majorana condition,  $\nu_M^c = \nu_M$ , holds true.

## 2.4. NEUTRINO OSCILLATION FORMALISM

772 As a consequence of the Majorana condition, the neutrino and the antineutrino states  
 773 can be described in terms of a single field. As opposed to the charged leptons, which  
 774 need to be represented by a four-component or Dirac spinor, the Majorana neutrino is  
 775 described by a two-component or Weyl spinor.

776 If the eigenvalues of the Majorana mass matrix,  $M_N$ , are much larger than the  
 777 electroweak symmetry breaking scale, the diagonalisation of  $M_\nu$  leads to 3 light and  $m$   
 778 heavy neutrino states:

$$-\mathcal{L}_{M_\nu} = \frac{1}{2}\bar{\nu}_l M_l \nu_l + \frac{1}{2}\bar{\nu}_h M_h \nu_h, \quad (2.24)$$

779 where the two mass matrices are given by:

$$\begin{aligned} M_l &\simeq -V_l^T M_D^T M_N^{-1} M_D V_l, \\ M_h &\simeq V_h^T M_N V_h, \end{aligned} \quad (2.25)$$

780 with  $V_l$  and  $V_h$  two unitary matrices.

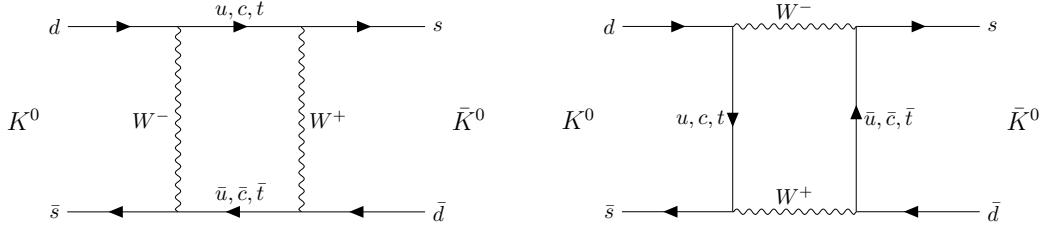
781 This scenario represents the so-called see-saw mechanism [35–39]. The name comes  
 782 from the fact that the masses of the heavy states are proportional to  $M_N$ , whereas for  
 783 the light states they are proportional to  $M_N^{-1}$ . While both the heavy and the light  
 784 neutrinos are Majorana particles, it can be shown that the heavy states are mainly  
 785 right-handed, whereas the light ones are mostly left-handed.

## 786 2.4 Neutrino oscillation formalism

787 Neutrino oscillations were first proposed in 1958 by B. Pontecorvo [40], inspired by the  
 788 neutral kaon oscillation phenomenon [41]. Neutral kaons,  $K^0$  and  $\bar{K}^0$ , have opposite  
 789 strangeness ( $\pm 1$ ) and are produced in strong processes. It was observed that, when  
 790 having a beam initially pure of neutral kaons of one type, these would transition into  
 791 their antiparticles while propagating. Because the weak interaction does not conserve  
 792 strangeness, neutral kaons can change their identity via the processes shown in Fig. 2.3.

793 The mixing considered initially by Pontecorvo was between the neutrino and the

## CHAPTER 2. NEUTRINO PHYSICS



**Figure 2.3:**  $K^0 \rightleftharpoons \bar{K}^0$  mixing through  $W^\pm$  exchange.

794 antineutrino states, as only one neutrino flavour was known at the time. After the  
 795 discovery of the muon neutrino, the mixing between flavours was also explored [42].

796 In the general case, we have 3 active and  $m$  sterile neutrinos, resulting in  $3 + m$   
 797 neutrino mass eigenstates. Working in the mass basis, the leptonic charged-current  
 798 Lagrangian can be written as:

$$-\mathcal{L}_{CC}^{lep} = \frac{g}{\sqrt{2}} (\bar{e}_L, \bar{\mu}_L, \bar{\tau}_L) \gamma^\mu U \begin{pmatrix} \nu_1 \\ \nu_2 \\ \vdots \\ \nu_{3+m} \end{pmatrix} W_\mu^+ + \text{h.c.}, \quad (2.26)$$

799 where  $U$  is a  $3 \times (3 + m)$  matrix which obeys  $UU^\dagger = I_{3 \times 3}$ , but in general will not be  
 800 unitary,  $U^\dagger U \neq I_{(3+m) \times (3+m)}$ .

801 The leptonic mixing matrix,  $U$ , establishes how the neutrino mass states couple to  
 802 the charged leptons. In general, a complex  $n \times n$  matrix can be fully specified by  $2n^2$  real  
 803 parameters. If the matrix is unitary, then the number of independent parameters reduces  
 804 to  $n^2$ , as one has to impose  $n$  normalisation and  $n(n - 1)$  orthogonality constraints.  
 805 In our case, we can further reduce the number of parameters by performing a phase  
 806 redefinition of the charged lepton fields, without affecting the physics. This is not true  
 807 for the neutrinos. As they may be their own antiparticles, one is not allowed to remove  
 808 any physically relevant phases. If we consider  $n$  generations of leptons, the total number  
 809 of parameters in the mixing matrix is  $n^2 - n$ . Out of these, half of them are mixing  
 810 angles, while the other half are complex phase factors.

811 Considering the extended SM without any additional sterile neutrino states, the  
 812 resulting  $3 \times 3$  mixing matrix is unitary. This matrix, often called the Pontecorvo-Maki-

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813 Nakagawa-Sakata (PMNS) matrix [43, 44], relates the set of active neutrinos and the  
814 three mass eigenstates as:

$$|\nu_\alpha\rangle = \sum_{i=1}^3 U_{\alpha i}^* |\nu_i\rangle, \quad (2.27)$$

815 where the Greek index  $\alpha$  denotes the flavour  $\{e, \mu, \tau\}$  and the Latin index  $i$  the mass state  
816  $\{1, 2, 3\}$ . This leptonic mixing matrix may be parametrized in terms of 6 parameters, 3  
817 of which are mixing angles  $\theta_{12}$ ,  $\theta_{13}$  and  $\theta_{23}$ , one CP-violating phase  $\delta_{CP}$  and 2 Majorana  
818 phases  $\alpha$  and  $\beta$ :

$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13} e^{-i\delta_{CP}} \\ 0 & 1 & 0 \\ -s_{13} e^{i\delta_{CP}} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & e^{i\alpha} & 0 \\ 0 & 0 & e^{i\beta} \end{pmatrix}, \quad (2.28)$$

819 where  $c_{ij} \equiv \cos \theta_{ij}$  and  $s_{ij} \equiv \sin \theta_{ij}$ . This matrix is analogous to the Cabibbo-Kobayashi-  
820 Maskawa (CKM) matrix in the quark sector. If neutrinos are Dirac fermions, we can  
821 drop the Majorana phases in the PMNS matrix, as in this case we can perform the  
822 phase redefinitions. However, these phases play no role on the neutrino oscillation  
823 phenomenology.

824 In the case that additional sterile neutrinos states are present, the full leptonic mixing  
825 matrix would not be unitary in general. For instance, in the see-saw scenario, the  $3 \times 3$   
826 submatrix for the three light Majorana neutrinos is not unitary. However, the deviations  
827 from unitarity are of the order  $\mathcal{O}(M_D/M_N)$ , and therefore expected to be negligible.

### 828 2.4.1 Oscillations in vacuum

829 Consider the case where a neutrino of flavour  $\alpha$  is produced at  $t = 0$ , and then it  
830 propagates through vacuum. Such a state will evolve in time according to the relation:

$$|\nu_\alpha(\vec{x}, t)\rangle = \sum_{i=1}^3 U_{\alpha i}^* e^{-i(E_i t - \vec{p}_i \cdot \vec{x})} |\nu_i(\vec{x} = \vec{0}, t = 0)\rangle, \quad (2.29)$$

831 in the plane wave approximation, as the mass eigenstates are also eigenstates of the free  
832 Hamiltonian.

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833 This way, the probability for the neutrino to transition from flavour  $\alpha$  to flavour  $\beta$   
834 will be given by:

$$P(\nu_\alpha \rightarrow \nu_\beta) = |\langle \nu_\beta | \nu_\alpha(\vec{x}, t) \rangle|^2 = \left| \sum_{i=1}^3 \sum_{j=1}^3 U_{\alpha i}^* U_{\beta j} e^{-i(E_i t - \vec{p}_i \cdot \vec{x})} \langle \nu_j | \nu_i \rangle \right|^2 \\ = \left| \sum_{i=1}^3 U_{\alpha i}^* U_{\beta i} e^{-i(E_i t - \vec{p}_i \cdot \vec{x})} \right|^2, \quad (2.30)$$

835 where we have used the orthogonality relation  $\langle \nu_i | \nu_j \rangle = \delta_{ij}$ . A usual approximation to  
836 take at this point is to consider ultra-relativistic neutrinos, i.e.  $p_i \simeq E$ , so we can write  
837 the dispersion relations as:

$$E_i = \sqrt{p_i^2 + m_i^2} \approx E + \frac{m_i^2}{2E}. \quad (2.31)$$

838 In the end, assuming  $t \approx L$  where  $L$  is the distance between the production and the  
839 detection points, the probability for the  $\nu_\alpha \rightarrow \nu_\beta$  transition becomes:

$$P(\nu_\alpha \rightarrow \nu_\beta) = \sum_{i,j} U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j} e^{-i \frac{\Delta m_{ij}^2}{2E} L} \\ = \delta_{\alpha\beta} - 4 \sum_{i < j} \Re e [U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*] \sin^2 \left( \frac{\Delta m_{ij}^2}{4E} L \right) \\ + 2 \sum_{i < j} \Im m [U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*] \sin \left( \frac{\Delta m_{ij}^2}{2E} L \right), \quad (2.32)$$

840 where  $\Delta m_{ij}^2$  is the difference of the squared masses of the  $j$ th and  $i$ th neutrino mass  
841 eigenvalues. At this point, it is usual to write the phase responsible for the oscillations  
842 as:

$$\Delta_{ij} \equiv \frac{\Delta m_{ij}^2}{4E} L \simeq 1.27 \frac{\Delta m_{ij}^2}{(\text{eV}^2)} \frac{L}{(\text{km})} \frac{(\text{GeV})}{E}. \quad (2.33)$$

843 Notice that, in the case of antineutrinos, the only difference would be the sign of the  
844 last term in the oscillation probability. As the process  $\bar{\nu}_\alpha \rightarrow \bar{\nu}_\beta$  is the CP-mirror image  
845 of  $\nu_\alpha \rightarrow \nu_\beta$ , the differences between their oscillation probabilities would be a measure of

## 2.4. NEUTRINO OSCILLATION FORMALISM

846 CP symmetry violation:

$$\begin{aligned} A_{CP}^{\alpha\beta} &= P(\nu_\alpha \rightarrow \nu_\beta) - P(\bar{\nu}_\alpha \rightarrow \bar{\nu}_\beta) \\ &= 4 \sum_{i<j} \Im \left[ U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^* \right] \sin 2\Delta_{ij}. \end{aligned} \quad (2.34)$$

847 Assuming that CPT invariance holds, then the following relation must be true:

$$P(\nu_\alpha \rightarrow \nu_\beta) = P(\bar{\nu}_\beta \rightarrow \bar{\nu}_\alpha), \quad (2.35)$$

848 as these two process are related by the CPT symmetry. From the definition of probability,  
849 we also must have:

$$\sum_{\beta} P(\nu_\alpha \rightarrow \nu_\beta) = \sum_{\beta} P(\bar{\nu}_\alpha \rightarrow \bar{\nu}_\beta) = 1, \quad (2.36)$$

850 where the sum includes all flavours, including  $\alpha$ . From these two constraints, one can  
851 probe that:

$$A_{CP}^{\alpha\beta} = -A_{CP}^{\beta\alpha}, \quad (2.37)$$

852 and in particular:

$$A_{CP}^{\alpha\alpha} = 0. \quad (2.38)$$

853 A direct consequence of this last relation is that there are no observable CP-violating  
854 effects in the so-called disappearance experiments. One needs to perform appearance  
855 experiments, where the flavour detected is different from the original flavour, in order  
856 to measure the CP asymmetry. Neutrino experiments often report the amount of CP-  
857 violation through the Jarlskog invariant. In terms of the parametrisation typically used  
858 to write the PMNS matrix, it is given by:

$$J = \frac{1}{8} \cos \theta_{13} \sin 2\theta_{12} \sin 2\theta_{13} \sin 2\theta_{23} \sin \delta_{CP}. \quad (2.39)$$

859 The Jarlskog invariant can be used to compare the amount of CP-violation in the lepton  
860 and the quark sectors, where  $J = 3.12^{+0.13}_{-0.12} \times 10^{-5}$  in the latter [45].

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### 2.4.2 Oscillations in matter

When neutrinos propagate through matter, their oscillation can be affected in mainly two ways. First, neutrinos can inelastically scatter with nuclei, thus destroying the coherent propagation of their quantum state. Nevertheless, in most cases this effect is negligible (even in very dense mediums like the core of the Sun). Second, neutrinos can also experience coherent or forward scatterings, that can affect their oscillation but not lose the coherent propagation of the state.

The first proposed model to account for neutrino oscillations in matter was proposed by Mikhaev, Smirnov and Wolfenstein (MSW) [46]. It relies on the fact that, as the only charged lepton present in ordinary matter is the electron, electron neutrinos can undergo both charged and neutral-current interactions with matter whereas for muon and tau neutrinos just neutral currents are possible.

An illustrative way to introduce the MSW mechanism is by considering the two flavours case. It can be shown that the evolution of the two flavour eigenstates in vacuum is given by the following time-dependent Schrödinger equation:

$$i \frac{d}{dt} \begin{pmatrix} \nu_e \\ \nu_\mu \end{pmatrix} = H_V \begin{pmatrix} \nu_e \\ \nu_\mu \end{pmatrix}, \quad (2.40)$$

with a vacuum Hamiltonian given by:

$$H_V = \frac{\Delta m^2}{4E} \begin{pmatrix} -\cos 2\theta & \sin 2\theta \\ \sin 2\theta & \cos 2\theta \end{pmatrix}, \quad (2.41)$$

where  $\Delta m^2$  is the mass splitting between the two neutrino states and  $\theta$  the only mixing angle. For simplicity, I omit the terms of the Hamiltonian that are proportional to the identity, as they do not affect the oscillation phenomenology.

The NC contribution to the matter potential is identical for all the flavours, and has the form:

$$V_{NC} = -\frac{G_F}{\sqrt{2}} N_n(x), \quad (2.42)$$

## 2.4. NEUTRINO OSCILLATION FORMALISM

882 where  $G_F$  is the Fermi constant and  $N_n(x)$  the local neutron density. Because it is  
 883 common to all flavours, I do not take it into account in the effective Hamiltonian, as it  
 884 would appear as a term proportional to the identity. The CC component only affects  
 885 the electron neutrino (and antineutrino). It can be written as:

$$V_{\text{CC}} = \pm \sqrt{2} G_F N_e(x), \quad (2.43)$$

886 with  $N_e(x)$  being the local electron density in the material. In the end, the effective  
 887 Hamiltonian which describes the propagation of the flavour eigenstates in matter only  
 888 contains an extra  $\nu_e - \nu_e$  element:

$$H_M = H_V + \begin{pmatrix} V_{\text{CC}} & 0 \\ 0 & 0 \end{pmatrix}. \quad (2.44)$$

889 The solution to the Schrödinger equation greatly simplifies if one considers the case  
 890 of a constant matter density. In that case, the effective Hamiltonian can be diagonalised,  
 891 obtaining the effective neutrino mass eigenstates in matter. It can be re-written in the  
 892 same form as the vacuum Hamiltonian:

$$H_M = \frac{\Delta m_m^2}{4E} \begin{pmatrix} -\cos 2\theta_m & \sin 2\theta_m \\ \sin 2\theta_m & \cos 2\theta_m \end{pmatrix}, \quad (2.45)$$

893 where the effective mass splitting and the effective mixing angle are given by:

$$\begin{aligned} \Delta m_m^2 &= \lambda \Delta m_m^2, \\ \sin 2\theta_m &= \frac{\sin 2\theta_m}{\lambda} \end{aligned} \quad (2.46)$$

894 with:

$$\begin{aligned} \lambda &= \sqrt{(\cos 2\theta - A)^2 + \sin^2 2\theta}, \\ A &= \pm \frac{2\sqrt{2} G_F N_e E}{\Delta m^2}. \end{aligned} \quad (2.47)$$

895 In terms of the effective matter oscillation parameters, the transition probability

## CHAPTER 2. NEUTRINO PHYSICS

896  $\nu_e \rightarrow \nu_\mu$  (in the two flavour approximation) reads:

$$P(\nu_e \rightarrow \nu_\mu) = \sin^2 2\theta_m \sin^2 \left( \frac{\Delta m_m^2}{2E} L \right) \quad (2.48)$$

897 From this last equation one can see that, when  $\cos 2\theta = A > 0$  the oscillations are  
898 greatly enhanced. This effect is known as the MSW resonance. For the neutrinos, this  
899 resonant condition is only satisfied if  $\Delta m^2 > 0$  (the opposite is true for antineutrinos).  
900 This is can be exploited by long baseline experiments, which can gain sensitivity to the  
901 neutrino mass hierarchy through matter effects.

### 902 2.4.3 Current status of neutrino oscillations

903 A wide range of neutrino experiments provide experimental input to the neutrino  
904 oscillation framework, both using natural or synthetic neutrino sources. The results  
905 from one of the neutrino global fit analyses, shown in Tab. 2.3<sup>1</sup>, summarise well our  
906 current understanding of the different oscillation parameters.

907 **Solar neutrino experiments** detect neutrinos produced in thermonuclear reactions  
908 inside the Sun, mainly from the so-called *pp* chain and the CNO cycle. These neutrinos  
909 have a typical energy in the range from 0.1 to 20 MeV. These experiments (Homestake  
910 [47], GALLEX [26], SAGE [25], Borexino [48], Super-Kamiokande [49] and SNO [50])  
911 provide the best sensitivities to  $\theta_{12}$  and  $\Delta m_{21}^2$ .

912 **Atmospheric neutrino experiments** detect the neutrino flux produced when  
913 cosmic rays scatter with particles in Earth's atmosphere. These collisions generate particle  
914 showers that eventually produce electron and muon neutrinos (and antineutrinos). Their  
915 energies range from few MeV to about  $10^9$  GeV. Experiments, like Super-Kamiokande  
916 [51] and IceCube [52] use atmospheric neutrinos to measure oscillations and are specially  
917 sensitive to  $\theta_{23}$  and  $\Delta m_{32}^2$ .

918 **Reactor neutrino experiments** look for the  $\bar{\nu}_e$  spectrum produced by nuclear  
919 reactors, with energies in the MeV scale. Depending on the distance to the source,

<sup>1</sup>These are the results reported during M. Tórtola's talk at Neutrino 2024 (see this link). I need to keep an eye and see if they publish these or other updated results in the near future.

## 2.5. OPEN QUESTIONS IN THE NEUTRINO SECTOR

**Table 2.3:** Summary of neutrino oscillation parameters determined in the Neutrino Global Fit of 2020 [14].

Parameter	Best fit $\pm 1\sigma$	$3\sigma$ range
$\Delta m_{21}^2$ [eV $^2 \times 10^{-5}$ ]	$7.55^{+0.22}_{-0.20}$	6.98 – 8.19
$ \Delta m_{31}^2 $ [eV $^2 \times 10^{-3}$ ] (NO)	$2.51^{+0.02}_{-0.03}$	2.43 – 2.58
$ \Delta m_{31}^2 $ [eV $^2 \times 10^{-3}$ ] (IO)	$2.41^{+0.03}_{-0.02}$	2.34 – 2.49
$\sin^2 \theta_{12}/10^{-1}$	$3.04 \pm 0.16$	2.57 – 3.55
$\sin^2 \theta_{23}/10^{-1}$ (NO)	$5.64^{+0.15}_{-0.21}$	4.23 – 6.04
$\sin^2 \theta_{23}/10^{-1}$ (IO)	$5.64^{+0.15}_{-0.18}$	4.27 – 6.03
$\sin^2 \theta_{13}/10^{-2}$ (NO)	$2.20^{+0.05}_{-0.06}$	2.03 – 2.38
$\sin^2 \theta_{13}/10^{-2}$ (IO)	$2.20^{+0.07}_{-0.04}$	2.04 – 2.38
$\delta_{CP}/\pi$ (NO)	$1.12^{+0.16}_{-0.12}$	0.76 – 2.00
$\delta_{CP}/\pi$ (IO)	$1.50^{+0.13}_{-0.14}$	1.11 – 1.87

long-baseline experiments like KamLAND [53] are sensitive to the solar mass splitting  $\Delta m_{21}^2$  whereas much shorter baseline experiment such as RENO [54] or DayaBay [55] measure  $\theta_{13}$  and  $\Delta m_{31}^2$ .

**Accelerator experiments** measure neutrino fluxes generated in particle accelerators. Usually mesons are produced in the accelerator to be focused into a beam, then some decay to muon neutrinos and the rest are absorbed by a target. Depending on the configuration one can obtain a beam made of mostly neutrinos or antineutrinos. The typical energies of these neutrinos are in the GeV range. Experiments such as NOvA [56], T2K [57], MINOS [58], OPERA [59] and K2K [60] (and in the future DUNE [61]) are primarily sensitive to  $\theta_{13}$ ,  $\theta_{23}$  and  $\Delta m_{32}^2$ . Also, in the coming years DUNE [61] and Hyper-Kamiokande [62] will be sensitive to  $\delta_{CP}$ .

## 2.5 Open questions in the neutrino sector

A crucial question that remains open these days, and is of vital importance for oscillation phenomena, is whether the mass eigenvalue  $\nu_3$  is the heaviest (what we call normal ordering) or the lightest (referred to as inverted ordering) of the mass eigenstates. In

## CHAPTER 2. NEUTRINO PHYSICS

other words, this means that we do not know the sign of  $\Delta m_{32}^2$ , so we can either have  $m_1 < m_2 < m_3$  (NO) or  $m_3 < m_1 < m_2$  (IO).

Another big puzzle is related to the value of  $\delta_{CP}$ . Nowadays it is poorly constrained, with all values between  $\pi$  and  $2\pi$  being consistent with data. A prospective measurement different from  $\delta_{CP} = 0, \pi$  will predict CP-violation in the leptonic sector, and thus contribute along with the one measured in the quark sector to the total amount of CP-violation. Although it is true that these two contributions by themselves are not enough to explain the matter anti-matter asymmetry in our universe, the amount of CP-violation in the leptonic sector can be key to explain such imbalance.

Both of these questions, because of their nature, could be understood thanks to future oscillation experiments.

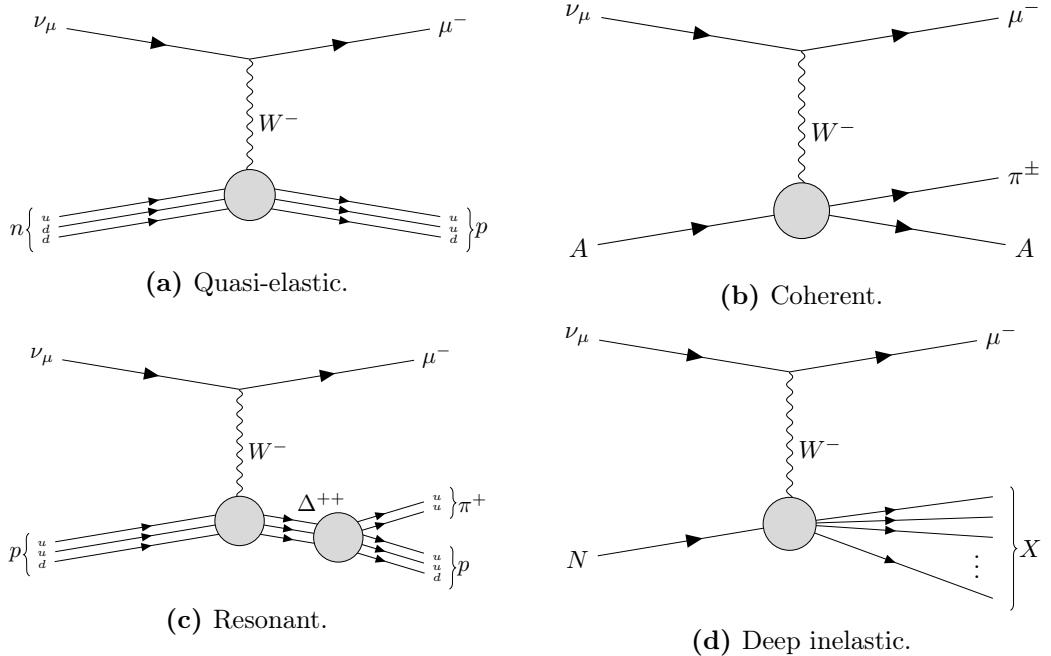
Notwithstanding, there are other mysteries that can not be unveiled just by conducting oscillation experiments, as certain quantities do not influence these phenomena. Among these there is the question of the absolute values of the neutrino masses. Depending on the value of the lightest of the neutrino masses we can have different mass spectra, from hierarchical  $m_1 \ll m_2 < m_3$  (NO) or  $m_3 \ll m_1 < m_2$  (IO) to quasi-degenerate  $m_1 \simeq m_2 \simeq m_3$ .

Other open question concerns the nature itself of the neutrinos. If neutrinos are Dirac particles then their mass term can be generated through the usual Higgs mechanism by adding right-handed neutrino fields. However, if they are Majorana particles and therefore their own antiparticles, there is no need to add extra fields to have the mass term in the Lagrangian. Experiments like SuperNEMO [63], SNO+ [64] and NEXT [65], which search for neutrino-less double beta decay, will be able to determine whether neutrinos are Dirac or Majorana.

## 2.6 Neutrino interactions

The study of neutrino-nucleus interactions is of great importance for long baseline neutrino oscillation experiments. The interaction model provides a mapping between

## 2.6. NEUTRINO INTERACTIONS

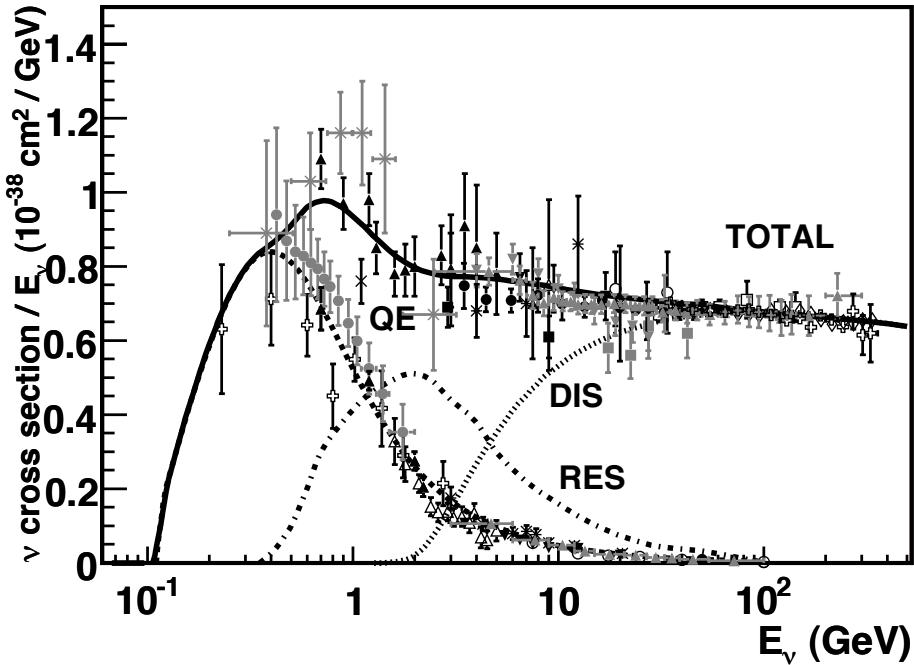


**Figure 2.4:** Feynman diagrams of the four most relevant CC interactions to long baseline neutrino oscillation experiments.

the energy of the incoming neutrino and the final state particles after the interaction.  
 Because in this kind of experiments neutrinos are obtained as secondary decay products of mesons, typically charged pions and kaons, their energies are not known a priori. Not only that, but the kinematics of the interacting nucleon are also unknown. Therefore, we rely on the neutrino interaction models to provide this relation between the observables in the detector and the true kinematics of the neutrino. Interaction modelling is expected to be the one of the leading sources of systematic uncertainties in the next generation of long baseline experiments [66–68].

In the case of neutrino interactions with nuclei, at the energies relevant for long baseline oscillation experiments, around the GeV-scale, the process is dominated by the interaction between the neutrino and a single nucleon within the nuclear medium. Figure 2.4 shows examples of the four most common neutrino CC interactions. In this diagrams  $A$  indicated that the interaction happened with the nucleus as a whole, whereas  $N$  denotes a single nucleon.

At low energies, below 1 GeV, quasi-elastic (QE) interactions dominate. In a CCQE

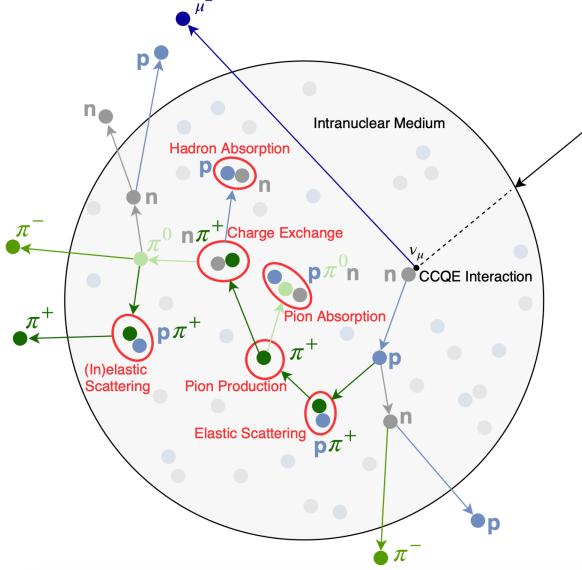


**Figure 2.5:** Total  $\nu_\mu$  CC cross section per nucleon as a function of the neutrino energy. The contributions from the different channels are shown. Figure taken from Ref. [69].

interaction a neutrino (antineutrino) interacts with a neutron (proton), converting it into a proton (neutron) which is then ejected from the nucleus together with the resulting charged lepton. At energies above 1 GeV the neutrino is able to excite the nucleon into a baryonic resonance, which promptly decays into a nucleon and a pion. These are the so-called resonant (RES) interactions. Neutrinos also interact with entire nucleus coherently, in the process known as coherent (COH) interaction. This kind of reactions also produce a single pion in the final state. At high neutrino energies, above 5 GeV, deep inelastic scattering (DIS) takes place. In these processes, the neutrino interacts with a single quark within the nucleon, breaking the nucleon and producing a hadronic shower.

Figure 2.5 shows a compilation of measurements of the total  $\nu_\mu$  CC cross section (see Ref. [69] for the details of the different experimental results). Also shown are the contributions from the different interaction modes. The contribution of the CCCOH interaction is omitted, as it is negligible compared to the others. This shows how the

## 2.6. NEUTRINO INTERACTIONS



**Figure 2.6:** Schematic representation of a  $\nu_\mu$  CCQE interaction with a neutron inside a nucleus. The reaction produces a muon and a proton, which travel through the nuclear medium. The outgoing proton undergoes various kinds of hadronic FSIs on its way out. Figure taken from Ref. [70].

interaction model needs to accurately predict the neutrino-nucleon cross section for the different interaction modes across a broad energy range, to obtain the correct relative contributions.

Nuclear effects alter the neutrino cross section, as well as the multiplicities of the final state particles. Therefore, the interaction models need to account for the effects introduced by the nuclei. There are several models available to describe the initial state of the nucleus, like the relativistic Fermi gas model [71], spectral functions [72] or the random phase approximation [73]. The other main effect that interaction models have to deal with are the so-called final state interactions (FSI). These are the interactions of the particles produced in the neutrino-nucleon scattering as they travel through the nuclear medium. Typically, the lepton exits the nucleus without interacting. However, hadrons tend to get scattered, absorbed or re-emitted. These effects are usually described by means of intra-nuclear cascade models [74]. Figure 2.6 illustrates the effects of FSI on the observable particle content in the detector after a  $\nu_\mu$  CCQE interaction.

There exists a rich experimental programme dedicated to the measurement of neutrino

## CHAPTER 2. NEUTRINO PHYSICS

1006 cross sections. The list of such experiments in the recent years include MiniBooNE  
1007 [75], MINERvA [76], MicroBooNE [77] and SBND [78]. Additionally, thanks to their  
1008 near detectors, long baseline experiments can perform cross section measurements.  
1009 Some recent examples are NOvA [79] or T2K [80]. Future oscillation experiments  
1010 will greatly benefit from these measurements, as the measurement of the oscillation  
1011 parameters depends on the cross section modelling. However, there are alternative  
1012 data-driven approaches to extract the oscillation probabilities without relying on a  
1013 neutrino interaction model, which are planned to be explored in the next generation of  
1014 experiments [81, 82].

1015

1016

1017

# The Deep Underground Neutrino Experiment

1018 The Deep Underground Neutrino Experiment (DUNE) is a next generation long-baseline  
1019 neutrino experiment [83]. It will aim to address several questions in neutrino physics,  
1020 study neutrinos from astrophysical sources and search for beyond the standard model  
1021 physics.

1022 This chapter reviews the main goals of the DUNE experiment, the design of the far  
1023 detector modules and their data acquisition (DAQ) system, and the role that the near  
1024 detector plays in the physics program of DUNE.

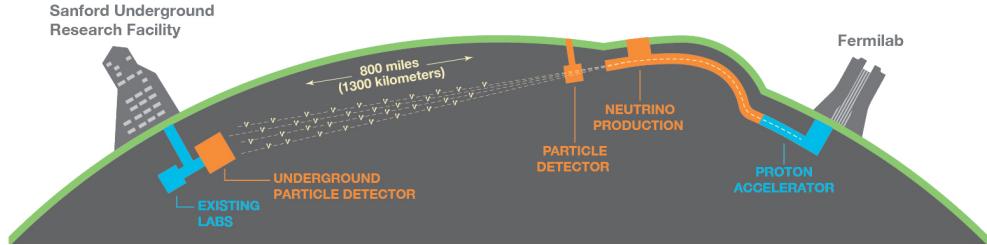
## 1025 3.1 Overview

1026 The main physics goals of DUNE are:

- 1027 • measure the neutrino mass hierarchy, the amount of CP violation in the leptonic  
1028 sector and the  $\theta_{23}$  octant,
- 1029 • detect rare low energy neutrino events, like neutrinos from supernova bursts, and
- 1030 • search for proton decay and other beyond the standard model phenomena.

1031 The design of DUNE has been tailored with these goals in mind. It will consist  
1032 of two neutrino detectors. A near detector (ND) complex will be placed at Fermilab,  
1033 574 m downstream of the neutrino production point, whereas a larger far detector

## CHAPTER 3. THE DEEP UNDERGROUND NEUTRINO EXPERIMENT



**Figure 3.1:** Schematic diagram of the DUNE experiment and the LBNF beamline [83].

1034 (FD) will be built in the Sandford Underground Research Facility (SURF), South  
 1035 Dakota, approximately 1300 km away. Figure 3.1 shows a simplified view of the various  
 1036 components of DUNE (not to scale).

1037 The beam neutrinos will be provided by the Long-Baseline Neutrino Facility (LBNF)  
 1038 beamline, the multi-megawatt wide-band neutrino beam planned for Fermilab. It will  
 1039 produce neutrinos travelling in the direction of SURF, with the capability to switch  
 1040 between neutrino and antineutrino mode.

1041 Before arriving to the FD, the neutrino beam meets the ND complex, which serves  
 1042 as the experiment's control. The design of the DUNE ND is mainly driven by the  
 1043 needs of the oscillation physics program, as its main role is to measure the unoscillated  
 1044 neutrino energy spectra. From these we can predict the unoscillated spectra at the FD,  
 1045 which can be compared to the spectra measured at the FD to extract the oscillation  
 1046 parameters. Additionally, the ND has a physics programme of its own, including cross  
 1047 section measurements and BSM physics searches.

1048 The technology chosen for the FD modules of DUNE is the liquid Argon time  
 1049 projection chamber (LArTPC). Its four modules will record neutrino interactions from  
 1050 the accelerator-produced beam arriving at predictable times. As it also aims at recording  
 1051 rare and low energy events, like supernovae and solar neutrinos, the FD requires trigger  
 1052 schemes which can deal with both kinds of physics, and also maximum uptime.

1053 DUNE is planned to be built using a staged approach consisting on two phases,  
 1054 which are summarised in Tab. 3.1. Phase I consists of a FD with 50% of the total

### 3.2. PHYSICS GOALS OF DUNE

**Table 3.1:** Summary of the two-phased plan for DUNE. Adapted from Ref. [84].

Parameter	Phase I	Phase II	Benefit
FD mass	20 kt fiducial	40 kt fiducial	FD statistics
Beam power	up to 1.2 MW	2.4 MW	FD statistics
ND config.	ND-LAr, TMS, SAND	ND-LAr, ND-GAr, SAND	Systematic constraints

**Table 3.2:** Exposure and time required to achieve the different physics milestones of the two phases. The predictions assume a Phase II staging scenario where FD modules 3 and 4 are deployed in years 4 and 6 and both the beam and ND are upgraded after 6 years. Adapted from Ref. [84].

Stage	Physics milestone	Exposure (kt-MW-years)	Years (staged)
Phase I	$5\sigma$ MO ( $\delta_{CP} = -\pi/2$ )	16	1-2
	$5\sigma$ MO (100% of the $\delta_{CP}$ values)	66	3-5
	$3\sigma$ CPV ( $\delta_{CP} = -\pi/2$ )	100	4-6
Phase II	$5\sigma$ CPV ( $\delta_{CP} = -\pi/2$ )	334	7-8
	$\delta_{CP}$ resolution of 10 degrees ( $\delta_{CP} = 0$ )	400	8-9
	$5\sigma$ CPV (50% of the $\delta_{CP}$ values)	646	11
	$3\sigma$ CPV (75% of the $\delta_{CP}$ values)	936	14
	$\sin^2(2\theta_{13})$ resolution of 0.004	1079	16

1055 fiducial mass, a reduced version of the ND complex and a 1.2 MW proton beam. It will  
 1056 be sufficient to achieve some early physics goals, like the determination of the neutrino  
 1057 mass ordering. For its Phase II, DUNE will feature the full four FD modules, a more  
 1058 capable ND and a 2.4 MW proton beam. The physics milestones for the two phases are  
 1059 given in Tab. 3.2, in a staging scenario which assumes that Phase II is completed after  
 1060 6 years of operation.

1061 A summary of the DUNE science program can be found in the DUNE FD Technical  
 1062 Design Report (TDR) Volume I [83]. For a detailed discussion on the two-phased  
 1063 approach the reader is referred to the DUNE Snowmass 2021 report [84].

### 1064 3.2 Physics goals of DUNE

1065 As noted in the literature (see for instance Ref. [14] for a review), the parameter space of  
 1066 the neutrino oscillation phenomena within the three-flavour picture is quite constrained

### CHAPTER 3. THE DEEP UNDERGROUND NEUTRINO EXPERIMENT

1067 by current experimental data. However, there are still crucial open questions, like the  
1068 mass ordering, the value of  $\delta_{CP}$  or the  $\theta_{23}$  octant. One of the main goals of DUNE is to  
1069 determine precisely the values of these parameters [85].

1070 To address these questions DUNE can look to the subdominant oscillation channel  
1071  $\nu_\mu \rightarrow \nu_e$  ( $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ ) and study the energy dependence of the  $\nu_e$  ( $\bar{\nu}_e$ ) appearance probability.  
1072 When we focus on the antineutrino channel  $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$  there is a change in the sign of  $\delta_{CP}$ ,  
1073 thus introducing CP-violation. Moreover, due to the fact that there are no positrons in  
1074 the composition of Earth, there is a sign difference for the matter effect contribution  
1075 when looking to the antineutrino channel. This asymmetry is proportional to the baseline  
1076 length  $L$  and is sensitive to the sign of  $\Delta m_{31}^2$ , and thus to the neutrino mass ordering.

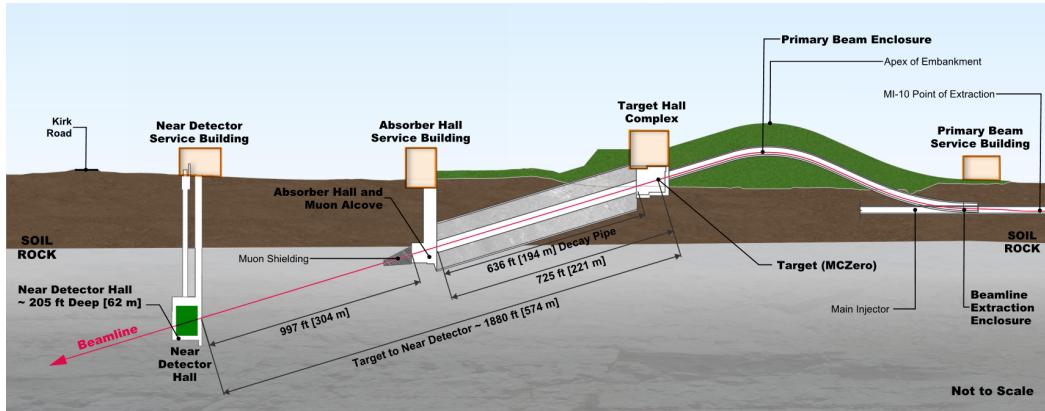
1077 Another of the main physics goals of DUNE is the search for baryon-number violating  
1078 processes. Specifically, it will try to answer the question of whether protons are stable  
1079 or not. There is no symmetry argument that forbids protons from decaying, but its  
1080 apparent stability seems to suggest that baryon number is conserved [86]. However,  
1081 proton decay is a usual feature of grand-unified theories, where electromagnetic, weak  
1082 and strong interactions are unified above a certain energy scale [87].

1083 As the energy deposition scale for this kind of searches is nearly the same as the one  
1084 for long-baseline neutrino oscillations, DUNE will be able to look for them. It has several  
1085 advantages over other experiments, such as excellent imaging and particle identification,  
1086 which can be translated to lower backgrounds.

1087 The last of the main objectives of DUNE is the detection of neutrinos originated in  
1088 supernovae explosions, what is called a supernova neutrino burst (SNB). These neutrinos  
1089 carry with them information about the core-collapse process, from the progenitor to the  
1090 explosion and the remnant; but also may have information about new exotic physics. So  
1091 far, the only neutrino events ever recorded from such a process were a few dozens of  $\bar{\nu}_e$   
1092 events from the 1987A supernova located in the Magellanic Cloud, 50 kpc away from  
1093 Earth [88, 89].

1094 DUNE aims to collect SNB events. Although these are quite rare, as the expected  
1095 supernovae explosion events are about one every few decades for our galaxy and

### 3.3. LBNF BEAMLINE



**Figure 3.2:** Schematic longitudinal section of the LBNF beamline at Fermilab (not to scale). Figure taken from Ref. [90].

1096 Andromeda, the long lifetime of the experiment (around a few decades as well) makes it  
 1097 reasonable to expect some. Nowadays the main sensitivity to SNB of most experiments  
 1098 is to the  $\bar{\nu}_e$  through inverse beta decay. One of the advantages of DUNE is its expected  
 1099 sensitivity to  $\nu_e$ , since the dominant channel will be  $\nu_e$  CC scattering.

1100 Moreover, due to the stringent requirements that the main physics goals set for  
 1101 DUNE, it will allow also to perform searches for all kind of BSM physics. Among  
 1102 others, DUNE will be able to look for: active-sterile neutrino mixing, non-unitarity of  
 1103 the PMNS matrix, non-standard interactions, Lorentz and CPT violations, neutrino  
 1104 trident production, light-mass DM, boosted DM and heavy neutral leptons. The reader  
 1105 is referred to the DUNE FD TDR Volume II [85] for a full discussion of the physics  
 1106 scope of DUNE.

### 1107 3.3 LBNF beamline

1108 The LBNF project is responsible for producing the neutrino beam for the DUNE detectors.  
 1109 A detailed discussion of the LBNF program can be found in the DUNE/LBNF CDR  
 1110 Volume III [90].

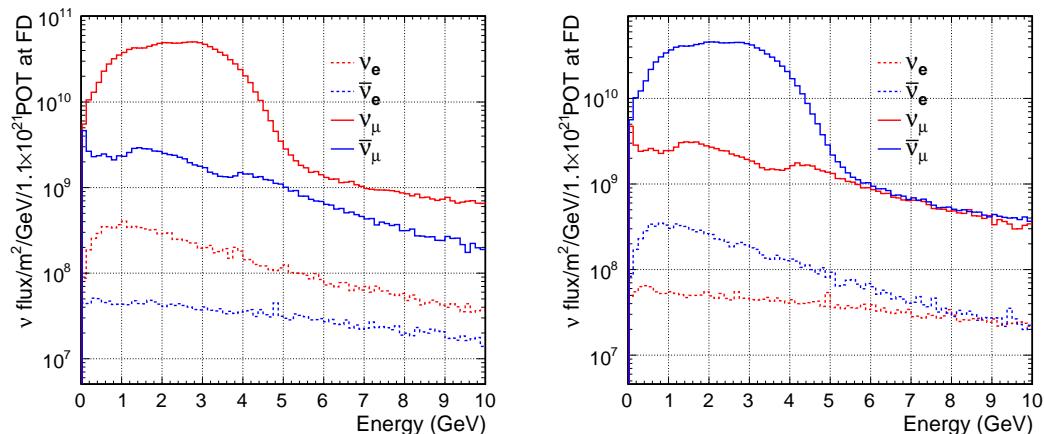
1111 A schematic diagram of the longitudinal section of the LBNF beamline is shown in  
 1112 Fig. 3.2. First, a beam of 60 – 120 GeV protons is extracted from the Fermilab Main  
 1113 Injector. This beam is aimed towards the target area, where it collides with a cylindrical

### CHAPTER 3. THE DEEP UNDERGROUND NEUTRINO EXPERIMENT

graphite target to produce pions and kaons.

The diffuse, secondary beam of particles is focused by a pair of magnetic horns. These select the positively charged particles when operated in Forward Horn Current (FHC) mode, or the negatively charged ones when the current is reversed, also known as Reverse Horn Current (RHC) mode. The focused secondary beam then enters a 194 m decay pipe where the pions and kaons will predominantly produce  $\mu^+\nu_\mu$  pairs when in FHC mode (or  $\mu^-\bar{\nu}_\mu$  in RHC mode).

At the end of the decay pipe a hadron absorber removes the undecayed hadrons and muons from the beam, which reduces the  $\nu_e$  ( $\bar{\nu}_e$ ) and  $\nu_\mu$  ( $\bar{\nu}_\mu$ ) contamination coming from the  $\mu^+$  ( $\mu^-$ ) decays. The resulting neutrino flux at the FD is shown in Fig. 3.3, both for FHC (left) and RHC (right) modes. These predictions show the intrinsic  $\nu_e$  contamination and wrong sign component from wrong sign and neutral meson decays, as well as muons decaying before reaching the absorber.

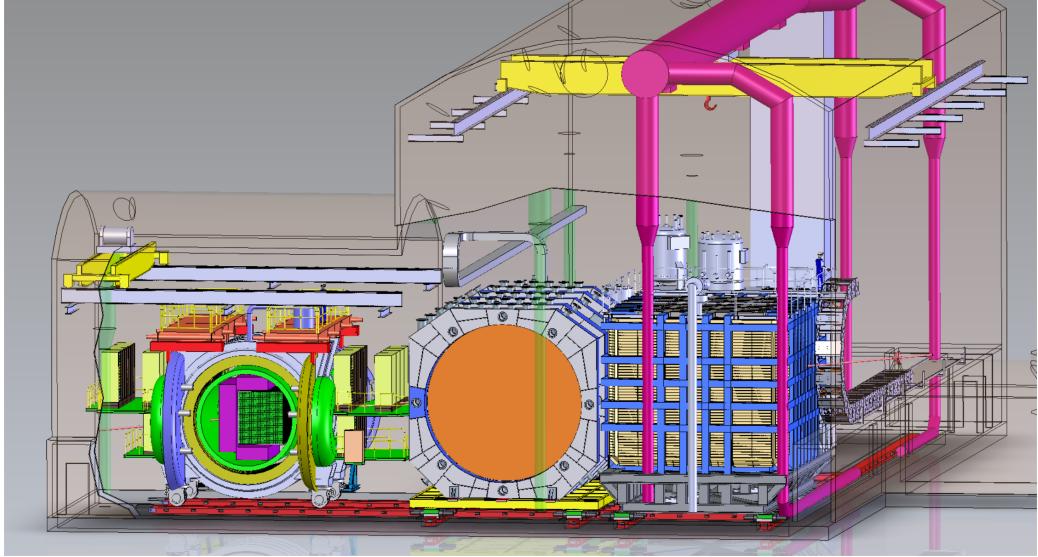


**Figure 3.3:** Predicted neutrino fluxes at the FD in FHC mode (left panel) and RHC mode (right panel). Figures taken from Ref. [85].

### 3.4 Near Detector

To estimate the oscillation parameters we measure the neutrino energy spectra at the FD. This reconstructed energy arises from a convolution of the neutrino flux, cross section, detector response and the oscillation probability. Using theoretical and empirical models

### 3.4. NEAR DETECTOR



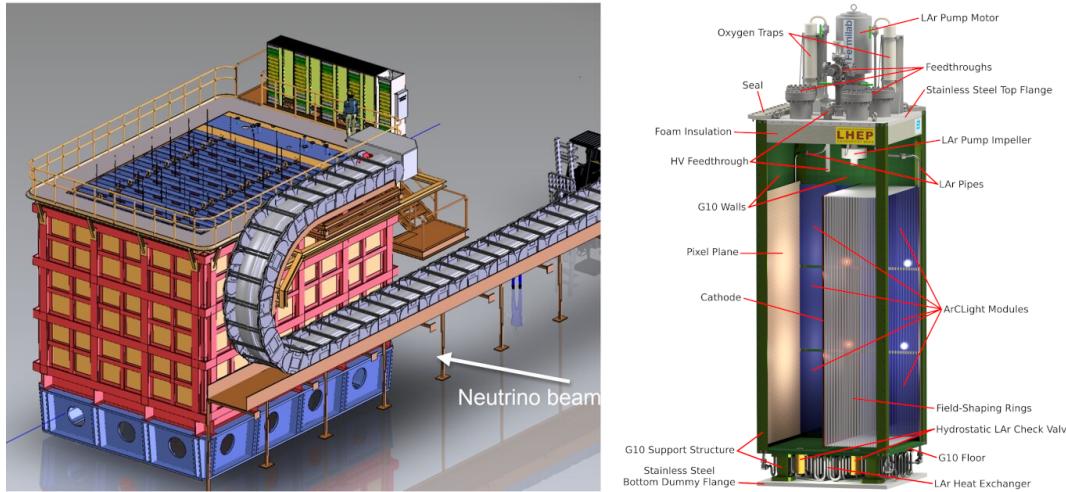
**Figure 3.4:** Representation of the ND hall in Phase II, showing the different subcomponents. From right to left, in the direction of the beam, we have ND-LAr, ND-GAr and SAND. Figure taken from Ref. [91].

to account for the other effects, one can extract the oscillation probability using the measurement. However, these models have associated a number of uncertainties that are then propagated to the oscillation parameters.

One of the main roles of the ND is to measure the neutrino interaction rates before the oscillation effects become relevant, i.e. close to the production point. By measuring the  $\nu_\mu$  and  $\nu_e$  energy spectra, and that of their corresponding antineutrinos, at the ND we can constrain the model uncertainties. A complete cancellation of the uncertainties when taking the ratio between the FD and ND measurements is not possible, as that would require both detectors to have identical designs and the neutrino fluxes to be the same. Because of the distance, the flux probed by the FD will have a different energy and flavour composition than that at the ND, as neutrinos oscillate and the beam spreads. The differences in the flux also determine the design of the detectors, therefore the ND is limited in its capability to match the FD design.

Nevertheless, having a highly capable ND, DUNE can minimise the systematic uncertainties affecting the observed neutrino energy. The ND data can be used to tune the model parameters by comparison with the prediction. Then, one uses the

### CHAPTER 3. THE DEEP UNDERGROUND NEUTRINO EXPERIMENT



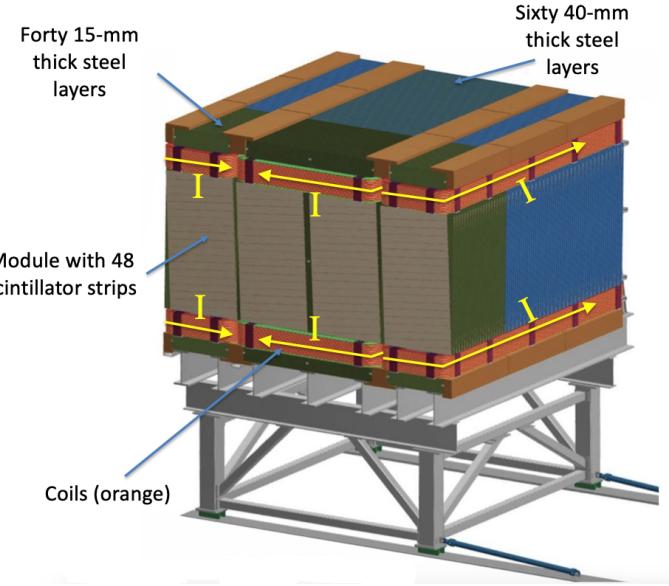
**Figure 3.5:** Schematic representation of the external components of ND-LAr, including the cryostat and the PRISM movable system (left) and detailed drawing of one ArgonCube module (right). Figure adapted from Ref. [83].

1147 tuned model to predict the unoscillated FD spectra. Comparing the prediction with the  
 1148 measured spectra it is possible to extract the oscillation parameters.

1149 Additionally, the ND will have a physics program of its own. In particular, it will  
 1150 measure neutrino cross sections that will then be used to constrain the model used in  
 1151 the long-baseline oscillation analysis. It will also be used to search for BSM phenomena  
 1152 such as heavy neutral leptons, dark photons, millicharged particles, etc.

1153 The DUNE ND can be divided in three main components, a LArTPC known as ND-  
 1154 LAr, a magnetised muon spectrometer, which will be the Temporary Muon Spectrometer  
 1155 (TMS) in Phase I and ND-GAr in Phase II, and the System for on-Axis Neutrino  
 1156 Detection (SAND). The layout of the Phase II DUNE ND can be seen in Fig. 3.4. The  
 1157 first two components of the ND will be able to move off-axis, in what is called the  
 1158 Precision Reaction-Independent Spectrum Measurement (PRISM) concept. More details  
 1159 on the purpose and design of the ND can be found in the DUNE ND Conceptual Design  
 1160 Report (CDR) [91].

### 3.4. NEAR DETECTOR



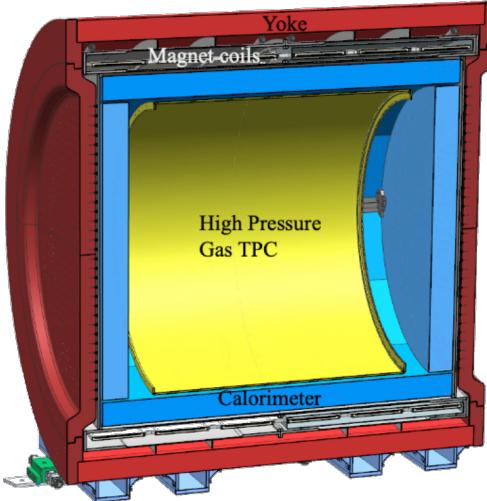
**Figure 3.6:** Schematic view of the TMS detector, highlighting its main parts. Figure adapted from Ref. [83].

#### 3.4.1 ND-LAr

ND-LAr is a LArTPC, as the ND needs a LAr component to reduce cross section and detector systematic uncertainties in the oscillation analysis. However, its design differs significantly from those proposed for the FD modules. Because of the high event rates at the ND, approximately 55 neutrino interaction events per  $10 \mu\text{s}$  spill, ND-LAr will be built in a modular way. Each of the modules, based on the ArgonCube technology, is a fully instrumented, optically isolated TPC with a pixelated readout. The pixelisation allows for a fully 3D reconstruction and the optical isolation reduces the problems due to overlapping interactions. Figure 3.5 shows a representation of the external parts of ND-LAr (left) and a detailed diagram of an ArgonCube module (right).

With a fiducial mass of 67 t and dimensions  $7 \text{ m} (\text{w}) \times 3 \text{ m} (\text{h}) \times 5 \text{ m} (\text{l})$ , ND-LAr will be able to provide high statistics and contain the hadronic systems from the beam neutrino interactions, but muons with a momentum higher than 0.7 GeV will exit the detector.

## CHAPTER 3. THE DEEP UNDERGROUND NEUTRINO EXPERIMENT



**Figure 3.7:** Cross section of the ND-GAr geometry, showing the HPgTPC, ECal and magnet. Figure adapted from Ref. [92].

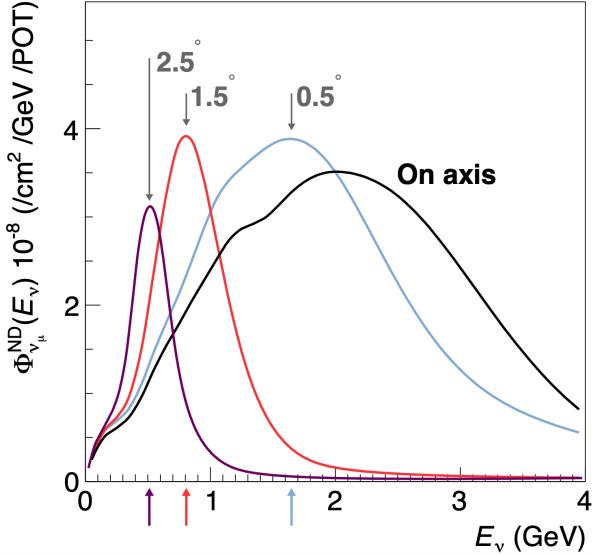
### 1175 3.4.2 TMS/ND-GAr

1176 To accurately estimate the neutrino energy, the momentum of the outgoing muons needs  
 1177 to be determined. That is the reason why a muon spectrometer is needed downstream  
 1178 of ND-LAr.

1179 In Phase I that role will be fulfilled by TMS. It is a magnetised sampling calorimeter,  
 1180 with alternating steel and plastic scintillator layers. Figure 3.6 shows a schematic view  
 1181 of the TMS detector. The magnetic field allows a precise measurement of the sign of the  
 1182 muon, so one can distinguish between neutrino and antineutrino interactions.

1183 After the Phase II upgrade, TMS will be replaced with a more capable near detector.  
 1184 The current technology considered is ND-GAr. This detector is a magnetised, high-  
 1185 pressure GAr TPC (often denoted as HPgTPC) surrounded by an electromagnetic  
 1186 calorimeter (ECal) and a muon tagger. A cross section of its geometry can be seen  
 1187 in Fig. 3.7. ND-GAr will be able to measure the momenta of the outgoing muons  
 1188 while also detect neutrino interactions inside the GAr volume. This allows ND-GAr  
 1189 to constrain the systematic uncertainties even further, as it will be able to accurately  
 1190 measure neutrino interactions at low energies thanks to the lower tracking thresholds of  
 1191 GAr.

### 3.4. NEAR DETECTOR



**Figure 3.8:** Predicted beam muon neutrino flux at the ND location for different off-axis positions. Figure taken from Ref. [91].

#### 3.4.3 PRISM

In general, the observed peak neutrino energy of a neutrino beam decreases as the observation angle with respect to the beam direction increases. This feature has been used in other long-baseline neutrino experiments, like T2K ( $2.5^\circ$  off-axis) and NOvA ( $0.8^\circ$  off-axis), to achieve narrower energy distributions. The DUNE PRISM concept exploits this effect using a movable ND. Within PRISM both ND-LAr and the muon spectrometer (TMS in Phase I and ND-GAr in Phase II) can be moved up to  $3.2^\circ$  off-axis, equivalent to move the detectors 30.5 m laterally through the ND hall.

This allows to record additional data samples with different energy compositions. Figure 3.8 compares the on-axis muon neutrino flux at the ND with the fluxes at different off-axis positions. As the off-axis position increases the neutrino flux becomes closer to a monoenergetic beam with a lower peak energy. These samples can be used to perform a data-driven determination of the relation between true and reconstructed neutrino energy, to reduce the dependence on the interaction model. The off-axis samples are linearly combined to produce a narrow Gaussian energy distribution centered on a target true energy. From the combination coefficients one can build a sample of reconstructed

## CHAPTER 3. THE DEEP UNDERGROUND NEUTRINO EXPERIMENT

1208 neutrino events that will determine the energy mapping.

1209 The PRISM samples will be used to form a flux at the ND location similar in shape  
1210 to the oscillated flux measured by the FD. This method can be used to extract the  
1211 oscillation parameters with minimal input from the neutrino interaction model.

### 1212 3.4.4 SAND

1213 The role of SAND is to monitor the beam stability by measuring the on-axis neutrino  
1214 energy spectra. As the PRISM program requires that ND-LAr and its downstream  
1215 muon spectrometer spend about half of the time in off-axis positions, it is not possible  
1216 to monitor the stability with the movable detectors. Moreover, for the success of PRISM  
1217 it is essential to have a stable beam configuration, or, at least, a quick assessment and  
1218 modeling of the distortions.

1219 The SAND detector is magnetised, and features an inner low density tracker, a LAr  
1220 target with optical readout and surrounding sampling calorimeter.

## 1221 3.5 A More Capable Near Detector

1222 In DUNE Phase II, a more capable near detector is needed to achieve the ultimate physics  
1223 goals of the experiments. The current leading proposal for this detector is ND-GAr.  
1224 As mentioned previously, it will fulfill the role of TMS, measuring the momentum and  
1225 sign of the charged particles exiting ND-LAr. Additionally, it will be able to measure  
1226 neutrino interactions inside the HPgTPC, achieving lower energy thresholds than those  
1227 of the ND and FD LArTPCs. By doing so ND-GAr will allow to constrain the relevant  
1228 systematic uncertainties for the LBL analysis even further. A detailed discussion on the  
1229 requirements, design, performance and physics of ND-GAr can be found in the DUNE  
1230 ND CDR [91] and the ND-GAr white paper [93].

### 3.5. A MORE CAPABLE NEAR DETECTOR

#### 1231 3.5.1 Requirements

1232 The primary requirement for ND-GAr is to measure the momentum and charge of  
1233 muons from  $\nu_\mu$  and  $\bar{\nu}_\mu$  CC interactions in ND-LAr, in order to measure their energy  
1234 spectrum. To achieve the sensitivity to the neutrino oscillation parameters described  
1235 in the DUNE FD TDR Volume II [85], ND-GAr should be able to constrain the muon  
1236 energy within a 1% uncertainty or better. The main constraint will come from the  
1237 calibration of the magnetic field, which will be performed using neutral kaon decays in  
1238 the HPgTPC.

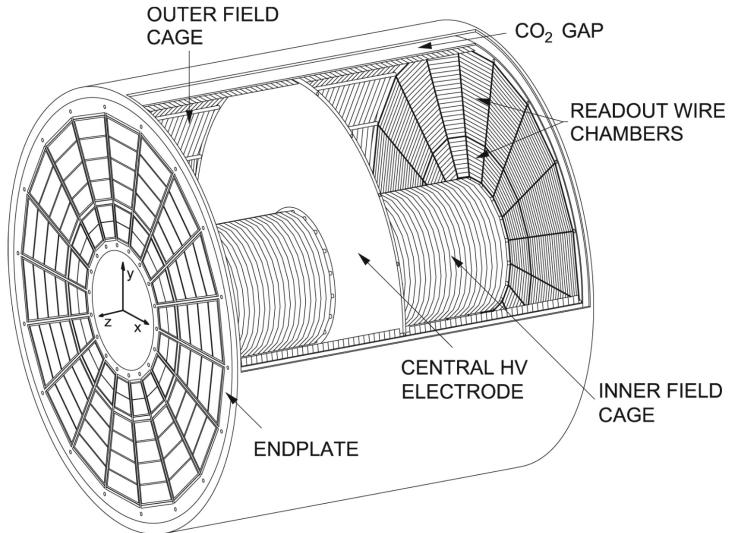
1239 Another requirement for ND-GAr is the precise measurement of neutrino interactions  
1240 on argon for the energies relevant to the neutrino oscillation program. The goal is to  
1241 constrain the cross section systematic uncertainties in the regions of phase space that  
1242 are not accessible to ND-LAr. This requires the kinematic acceptance for muons in  
1243 ND-GAr to exceed that of ND-LAr, being comparable to the one observed in the FD.

1244 ND-GAr should also be able to help establishing the relationship between true and  
1245 reconstructed energy from neutrino interactions on argon with low thresholds, being  
1246 sensitive to particles that are not observed or may be misidentified in ND-LAr. In  
1247 particular, ND-GAr needs to have low tracking thresholds in order to measure the  
1248 spectrum of pions and protons produced in final-state interactions (FSI). It also must  
1249 be able to accurately measure the pion multiplicity in 1, 2 and 3 pions final states, to  
1250 inform the pion mass correction in the LArTPCs.

#### 1251 3.5.2 Reference design

1252 The final design of ND-GAr is still under preparation. However, a preliminary baseline  
1253 design was in place at the time of the ND CDR. This section summarises the main  
1254 features of that design, as it is also the one used for the default geometry in our simulation.  
1255 A DUNE Phase II white paper, discussing the different options under consideration for  
1256 the ND-GAr design, is in progress.

## CHAPTER 3. THE DEEP UNDERGROUND NEUTRINO EXPERIMENT



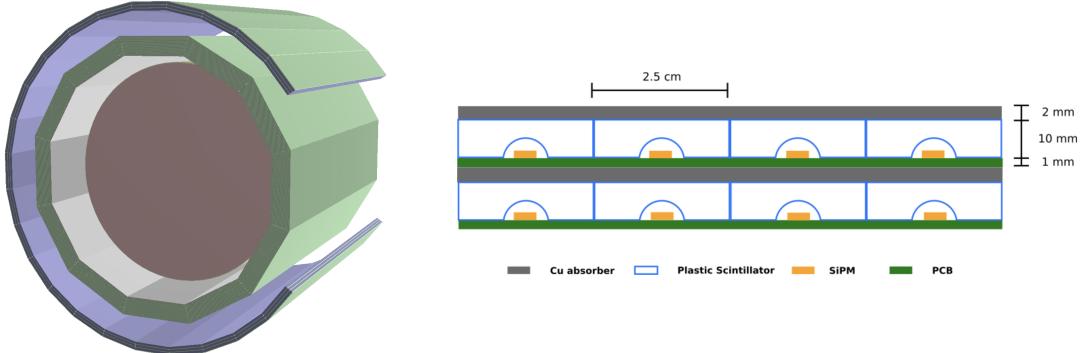
**Figure 3.9:** Diagram of the ALICE TPC, showing the two drift chambers, inner and outer field cages and readout chambers. Figure taken from Ref. [91].

### 1257 HPgTPC

1258 The reference design for the ND-GAr HPgTPC follow closely that of the ALICE TPC.  
 1259 It is a cylinder with a central high-voltage cathode, generating the electric field for  
 1260 the two drift volumes, with a maximum drift distance of 2.5 m each. The anodes will  
 1261 be instrumented with charge readout chambers. The original design repurposed the  
 1262 multi-wire proportional readout chambers (MWPCs) of ALICE, however some of the  
 1263 current R&D efforts focus on a gas electron multiplier (GEM) [94] option instead. Figure  
 1264 3.9 shows a schematic diagram of the ALICE TPC design. The basic ND-GAr geometry  
 1265 will resemble this, except for the inner field cage.

1266 It will use a 90:10 molar fraction Ar:CH<sub>4</sub> mixture at 10 bar. With this baseline gas  
 1267 mixture light collection is not possible, as the quenching gas absorbs most of the VUV  
 1268 photons. Additional R&D efforts are underway, to understand if different mixtures allow  
 1269 for the light signal to be used to provide a  $t_0$  while maintaining stable charge gain.

### 3.5. A MORE CAPABLE NEAR DETECTOR



**Figure 3.10:** View of the 12-sided ECal barrel and outer muon tagger geometries (left) and layout of the ECal tile layers for the 2 mm Cu, 10 mm scintillator option (right). Figure adapted from Ref. [91].

#### 1270    ECal

1271    The main role of the ND-GAr ECal is the calorimetric measurement of the electron  
 1272    energies and the reconstruction of photons, in particular those from neutral pion decays.  
 1273    Also, the ECal is able to provide a  $t_0$  timestamp for neutrino interactions, by associating  
 1274    its activity to the tracks in the HPgTPC. The ECal will also be able to perform  
 1275    neutron reconstruction using time of flight and reject external backgrounds, thanks to  
 1276    its sub-nanosecond time resolution.

1277       The ECal design features three independent subdetectors, two end caps at each side  
 1278    and a barrel surrounding the HPgTPC. Each of the detectors is divided in modules,  
 1279    which combine alternating layers of plastic scintillator and absorber material readout  
 1280    by SiPMs. The inner scintillator layers consist of  $2.5 \times 2.5 \text{ cm}^2$  high-granularity tiles,  
 1281    whereas the outer ones are made out of 4 cm wide cross-strips spanning the whole  
 1282    module length. The current barrel geometry consists of 8 tile layers and 34 strip layers,  
 1283    while the end caps feature 6 and 36 respectively. The thickness of the scintillator layers  
 1284    is 7 mm and 5 mm for the Pb absorber layers. The 12-sided geometry of the ECal barrel  
 1285    (left) and the layout of the tile layers (left)<sup>1</sup> can be seen in Fig. 3.10.

---

<sup>1</sup>The figure shows the layout of the tile layers for a previous design with 2 mm Cu absorber and 10 mm plastic scintillator, as mentioned in the text the current choice is 5 mm Pb absorber and 7 mm scintillator.

## CHAPTER 3. THE DEEP UNDERGROUND NEUTRINO EXPERIMENT

### 1286 Magnet

1287 The ND-GAr magnet design, know as the Solenoid with Partial Yoke (SPY), consists of  
1288 two coupled solenoids with an iron return yoke. The idea behind the design is to have a  
1289 solenoid as thin as possible, as well as a return yoke mass distribution that minimises  
1290 the material budget between ND-LAr and ND-GAr. The magnet needs to provide a  
1291 0.5 T field in the direction perpendicular to the beam, parallel to the drift electric field.  
1292 It needs to host the pressure vessel and the surrounding ECal, which points to a inner  
1293 diameter of  $\sim 6.4$  m.

1294 The solenoid is a single layer coil, based on niobium titanium superconducting  
1295 Rutherford cable. The total length of the coil is 7.5 m. The bobbin will be split in four  
1296 segments grouped in pairs with two identical cryostats, connected in series. The iron  
1297 yoke features an aperture in the upstream side to allow the muons coming from ND-LAr.  
1298 Still, its material will be enough to reduce the magnetic field reaching SAND, and also  
1299 stop the charged pions produced inside the HPgTPC.

### 1300 Muon system

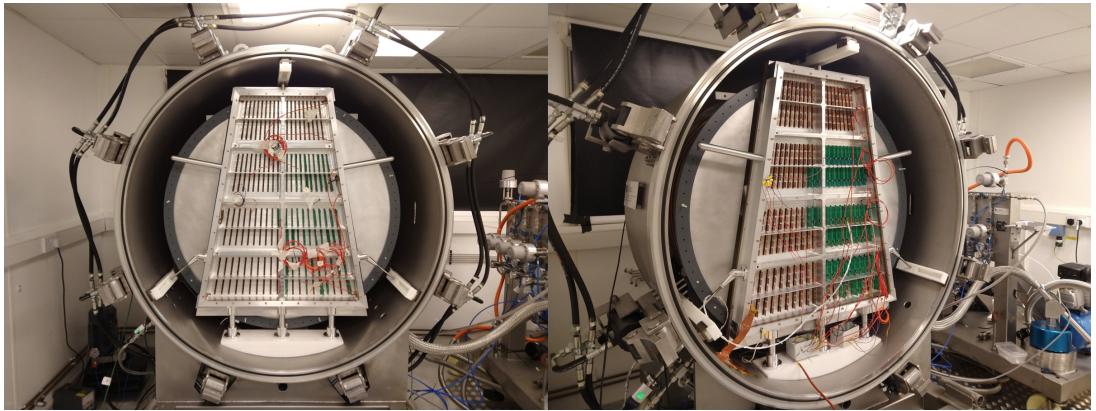
1301 The design of the ND-GAr muon system is still in a preliminary stage. Its role is to  
1302 distinguish between muons and pions punching through the ECal. This is especially  
1303 important for wrong-sign determination, to separate these from neutral current events.

1304 In its current form, the muon system consists of three layers of longitudinal sampling  
1305 structures. It alternates 10 cm Fe absorber slabs with 2 cm plastic scintillator strips.  
1306 The transverse granularity required is still under study.

### 1307 3.5.3 R&D efforts

1308 There are several ND-GAr-related prototypes, mostly focused on the TPC charge  
1309 readout and electronics. The priority is to test the full readout chain, in a high-pressure  
1310 environment, using a gas mixture with high argon fraction. A detailed summary of these  
1311 can be found in the DUNE Phase II white paper [92].

### 3.5. A MORE CAPABLE NEAR DETECTOR



**Figure 3.11:** Photographs of the TOAD pressure vessel at RHUL. The TPC is mounted inside the vessel, and the OROC is supported by an aluminium frame. Figure taken from Ref. [95].

#### 1312 Multi-Wire Proportional Chambers

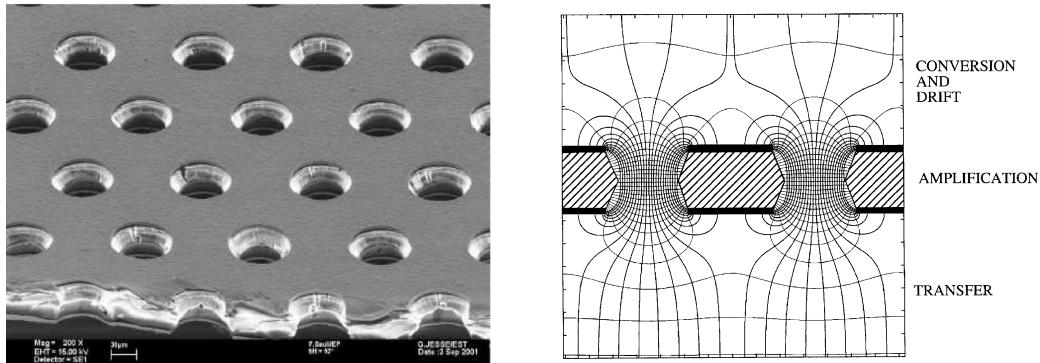
1313 As mentioned before, the original ND-GAr design repurposes the MWPCs of the ALICE  
1314 TPC, which became available after the recent upgrade [96]. These were operated using  
1315 a 90:10:5 Ne:CO<sub>2</sub>:N<sub>2</sub> gas mixture at 1 atm. Therefore, their performance needed to be  
1316 studied in an argon gas environment at high pressure.

1317 The Gas-argon Operation of ALICE TPC (GOAT) test stand tested the ALICE  
1318 readout chambers at high pressure. In particular, it used one of the previously operated  
1319 ALICE inner MWPCs, also known as IROCs, in a pressure vessel rated to 10 atm. It  
1320 measured the gas gain at various pressure points, voltages and gas mixtures.

1321 The Test stand of an Overpressure Argon Detector (TOAD) tested an ALICE outer  
1322 MWPC, also known as OROC, up to 5 atm. During its time at RHUL, it was used to  
1323 study the achievable gas gain of the OROC [95]. At the moment, it is being commissioned  
1324 at Fermilab for a full detector test of the readout electronics and the DAQ.

1325 Figure 3.11 shows the interior of the TOAD pressure vessel. The TPC is mounted  
1326 inside the vessel on three rails. The back of the OROC, supported by an aluminium  
1327 frame, can be seen at the front.

## CHAPTER 3. THE DEEP UNDERGROUND NEUTRINO EXPERIMENT



**Figure 3.12:** Left panel: electron microscope image of a 50  $\mu\text{m}$  thick GEM electrode, with hole pitch and diameter of 140 and 70  $\mu\text{m}$ , respectively. Right panel: Schematics of a GEM electrode cross section, showing the electric field lines around the holes. Figures taken from Ref. [97].

### 1328 Gas Electron Multiplier

1329 An alternative to the MWPC option is the use of GEMs. These are a type of micro-patter  
 1330 detector, where the ionisation electrons passing through the holes in the GEM layers  
 1331 are accelerated by a high intensity electric field. The acceleration causes the electrons  
 1332 to ionise the medium, resulting in an avalanche which increase the signal exponentially  
 1333 [94]. GEMs are used in numerous experiments that need a high spatial resolution, like  
 1334 ALICE [98] and CMS [99] after their upgrades.

1335 Figure 3.12 (left panel) shows an electron microscope picture of a 50  $\mu\text{m}$  thick GEM  
 1336 electrode, with a pitch between neighbouring holes of 140  $\mu\text{m}$  and a hole diameter of  
 1337 70  $\mu\text{m}$ . A schematic representation of the cross section of a GEM layer is shown in Fig.  
 1338 3.12 (left panel).

1339 The Gaseous Argon T0 (GAT0<sup>2</sup>) prototype studies the use of thick GEMs made out  
 1340 of glass to achieve optical imaging of the primary ionisation. Using a 10 atm pressure  
 1341 vessel, the goal is to study different argon-based mixtures that allow for a precise  $t_0$   
 1342 determination.

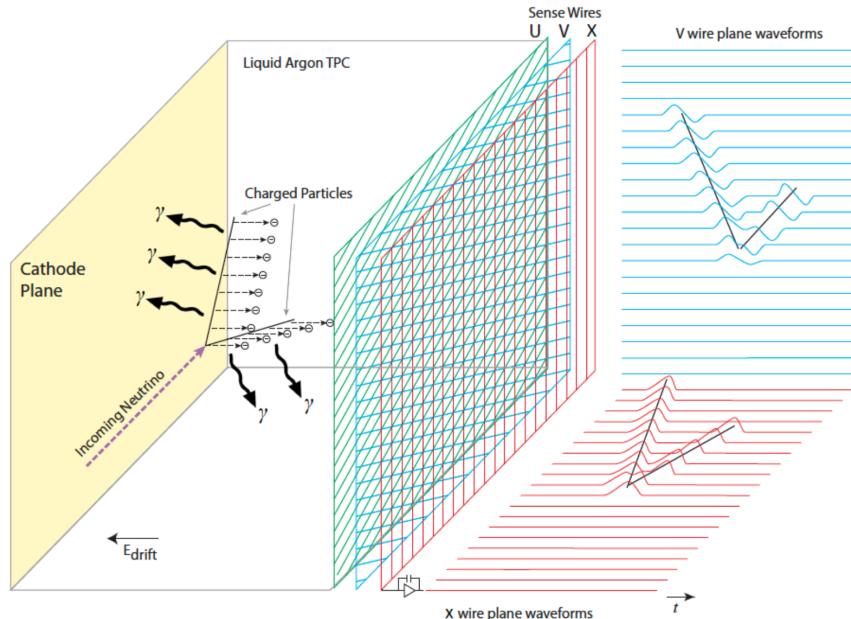
1343 The GEM Over-pressurized with Reference Gases (GORG<sup>3</sup>) test stand is currently  
 1344 testing a GEM-based charge readout, using a triple-GEM stack.

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<sup>2</sup>Spanish for cat.

<sup>3</sup>Persian for wolf.

### 3.6. FAR DETECTOR



**Figure 3.13:** Schematic diagram showing the operating principle of a LArTPC with wire readout. Figure taken from Ref. [83].

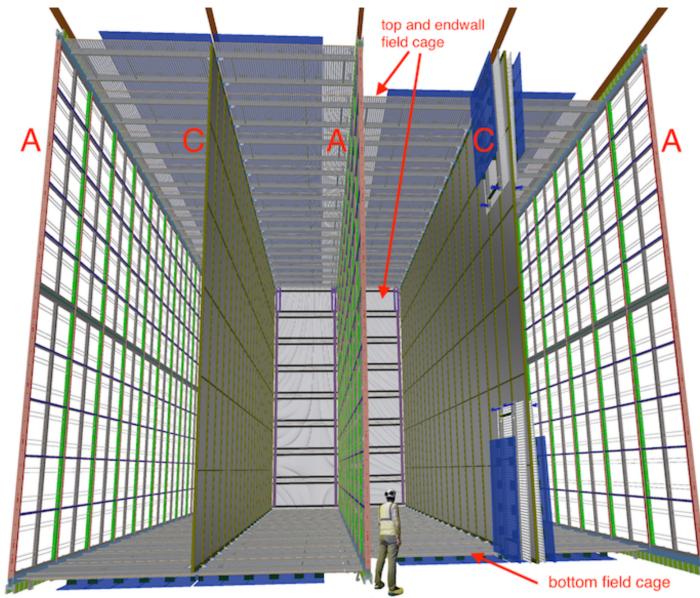
## 1345 3.6 Far Detector

1346 The DUNE FD complex will sit 1300 km away from the beam target and 1.5 km  
 1347 underground at SURF, South Dakota. Two caverns will host the four FD modules, two  
 1348 of them per cavern, each embedded in cryostats of dimensions 18.9 m (w)  $\times$  17.8 m (h)  $\times$   
 1349 65.8 m (l). A central, smaller cavern will host the cryogenic system.

1350 Three out of the four modules will be liquid argon (LAr) time projection chamber  
 1351 detectors, often refer to as LArTPCs, with a LAr fiducial mass of at least 10 kt each.  
 1352 The first and second FD modules, FD-1 and FD-2, will use a Horizontal Drift (HD)  
 1353 technology, whereas the third module, FD-3, will have a Vertical Drift (VD) direction.  
 1354 The technology for the fourth module is still to be decided,

1355 For each event, with energies ranging from a few MeV to several GeV, these detectors  
 1356 collect both the scintillation light and the ionisation electrons created when the charged  
 1357 particles produced in neutrino-nucleus interactions ionise the argon nuclei. In both HD  
 1358 and VD designs the characteristic 128 nm scintillation light of argon is collected by a  
 1359 photon detection system (PDS). This light will indicate the time at which electrons

## CHAPTER 3. THE DEEP UNDERGROUND NEUTRINO EXPERIMENT



**Figure 3.14:** Proposed design for the FD-1 and FD-2 modules following the HD principle. Figure taken from Ref. [83].

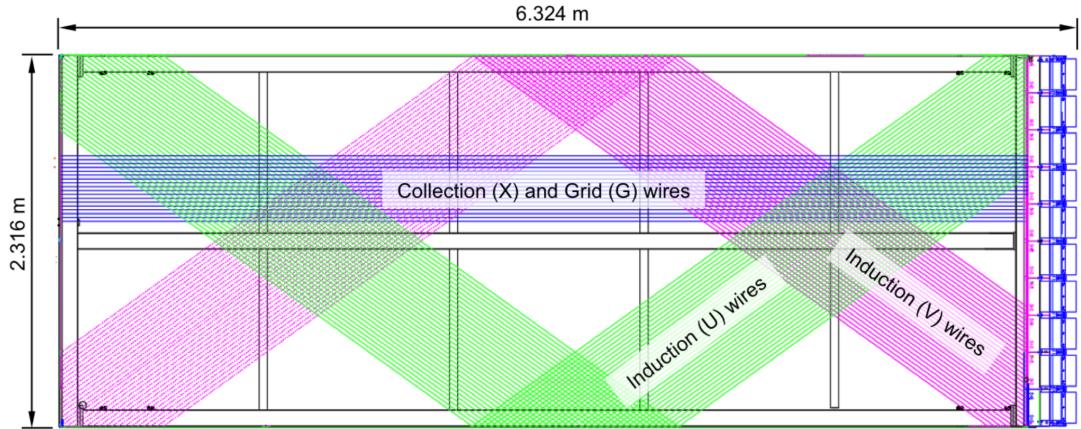
1360 start to drift, thus enabling reconstruction over the drift coordinate when compared  
 1361 to the time when the first ionisation electron arrives to the anode. Reconstruction of  
 1362 the topology in the transverse direction is achieved using the charge readout. Fig. 3.13  
 1363 illustrates the detection principle described, for the case of a HD detector with a wire  
 1364 readout.

### 1365 3.6.1 Horizontal Drift

1366 The HD design the ionisation electrons produced as charged particles traverse the LAr  
 1367 drift horizontally towards the anode planes, due to the effect of an electric field. These  
 1368 anode planes are made out of three layers of wire readout. This design, previously  
 1369 known as single-phase (SP), was tested by the ProtoDUNE-SP detector at CERN. The  
 1370 prototype collected data from a hadron beam and cosmic rays, providing high-quality  
 1371 data sets for calibration and performance studies.

1372 Each FD HD detector module is divided in four drift regions, with a maximum drift  
 1373 length of 3.5 m, by alternating anode and cathode walls. The surrounding field cage  
 1374 ensures the uniformity of the 500 V/cm horizontal electric field across the drift volumes.

### 3.6. FAR DETECTOR



**Figure 3.15:** Schematic representation of an APA. The black lines represent the APA steel frame. The green and magenta lines correspond to the direction of the U and V induction wires respectively. The blue lines indicate the direction of the X collection wires and the wire shielding G. Figure taken from Ref. [83].

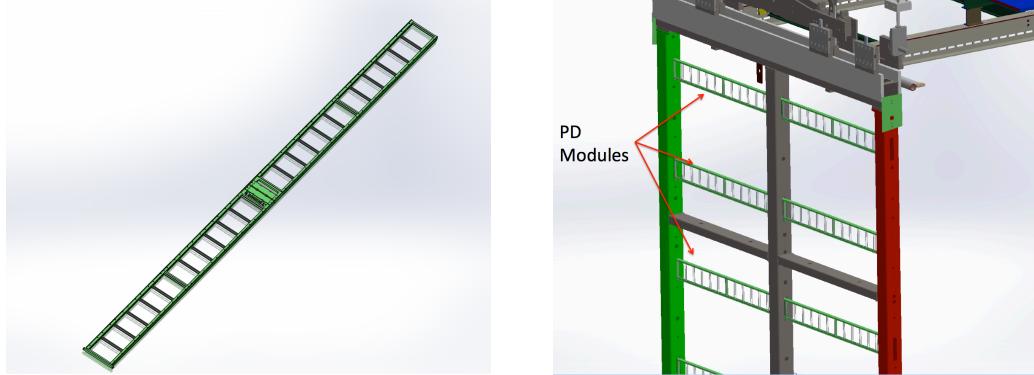
1375 The three anode walls, which constitute the charge readout of the detector, are built by  
 1376 stacking anode plane assemblies (APAs), 2 high times 25 wide. The design of the HD  
 1377 modules is shown in Fig. 3.14.

1378 Each APA is made of 2560 active wires arranged in three layers, plus an extra grid  
 1379 layer, wrapped around a metal frame. The two induction wire planes, U and V, sit at  
 1380  $\pm 35.7^\circ$  to the vertical on each side of the APA. The collection and shielding plane wires,  
 1381 X and G, run parallel to the vertical direction. The ionisation electrons drift past the  
 1382 induction planes, generating bipolar signals on those wires, and are collected by the  
 1383 collection plane, producing a monopolar positive signal. The spacing between the wires  
 1384 is  $\sim 5$  mm, and it defines the spatial resolution of the APA.

1385 The front-end readout electronics, or cold electronics as they are immerse in the LAr,  
 1386 are attached to the top of the up APAs and the bottom of the down APAs. Mounted on  
 1387 the front-end mother boards we have a series of ASICs that digitize the signals from the  
 1388 collection and induction planes. Each wire signal goes to a charge-sensitive amplifier,  
 1389 then there is a pulse-shaping circuit and this is followed by the analogue-to-digital  
 1390 converter. This part of the process happens inside the LAr to minimise the number of  
 1391 cables penetrating the cryostat. The digitised signals come out finally via a series of

## CHAPTER 3. THE DEEP UNDERGROUND NEUTRINO EXPERIMENT

1392 high-speed serial links to the warm interface boards (WIBs), from where the data is sent  
1393 to the back-end DAQ through optical fibers.



**Figure 3.16:** A PDS module containing 24 X-ARAPUCAs (left) and the location of the modules on the APAs (right). Figure taken from Ref. [83].

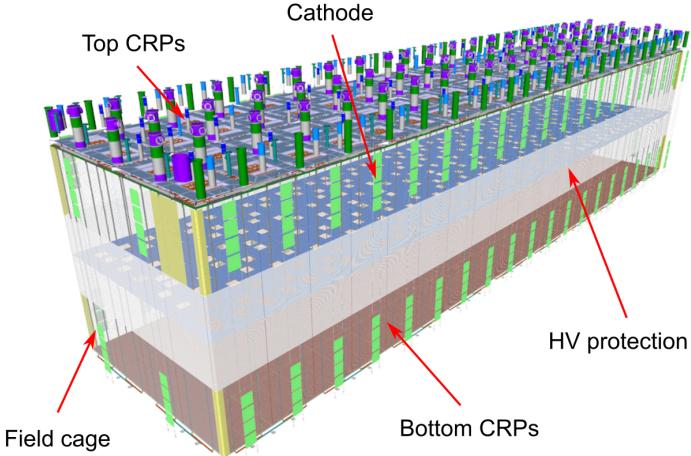
1394 The PDS uses modules of X-ARAPUCA devices, mounted on the APA frames  
1395 between the wire planes. Each X-ARAPUCA consists of layers of dichroic filter and  
1396 wavelength-shifter. They shift the VUV scintillation light into the visible spectrum,  
1397 sending then the visible photons to silicon photomultiplier (SiPM) devices. The PDS  
1398 modules are 209 cm × 12 cm × 2 cm bars, containing 24 X-ARAPUCAs. There are 10  
1399 of these PDS modules per APA. Fig. 3.16 shows a PDS module (left) and the placement  
1400 of the modules on the APAs (right).

### 1401 3.6.2 Vertical Drift

1402 In the VD case the ionisation electrons will drift vertically until they meet a printed  
1403 circuit board-based (PCB) readout plane. It is based on the original dual-phase (DP)  
1404 design deployed at CERN, known as ProtoDUNE-DP, used a vertical drift design with  
1405 an additional amplification of the ionization electrons using a gaseous argon (GAr) layer  
1406 above the liquid phase. The VD module incorporates the positive features of the DP  
1407 design without the complications of having the LAr-GAr interface.

1408 The current design of the FD VD module counts with two drift chambers with a  
1409 maximum drift distance of 6.5 cm. A cathode plane splits the detector volume along the  
1410 drift direction while the two anode planes are connected to the bottom and top walls

### 3.6. FAR DETECTOR



**Figure 3.17:** Proposed design for the FD-3 module following the VD principle. Figure adapted from Ref. [100].

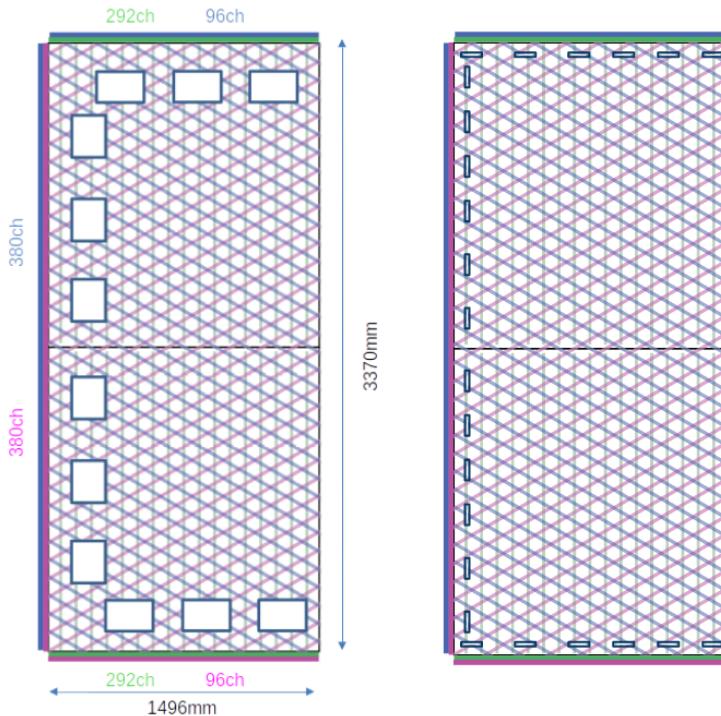
of the detector. The layout of the VD module is shown in Fig. 3.17. Compared with the HD design, the VD option offers a slightly larger instrumented volume and a more cost-effective solution for the charge readout.

As in the HD design, each drift volume features a 500 V/cm electric field and a field cage that ensures its uniformity. The anode planes are arrays of  $3.4\text{ m} \times 3\text{ m}$  charge-readout planes (CRPs). These are formed by a pair of charge-readout units (CRUs), which are built from two double-sided perforated PCBs, with their perforations aligned. The perforations allow the drift electrons to pass between the layers.

The PCB face opposite to the cathode has a copper guard plane which acts as shielding, while its reverse face is etched with electrode strips forming the first induction plane. The outer PCB has electrode strips on both faces, the ones facing the inner PCB form the second induction plane while the outermost ones form the collection plane. Fig. 3.18 shows the layout of the electrode strips for the top (left) and bottom (right) CRUs. The magenta and blue lines represent the first and second induction planes respectively, and the green lines correspond to the collection plane.

The PDS in the VD module will use the same X-ARAPUCA technology developed for the HD design. The plan is to place the PDS modules on the cryostat walls and on

## CHAPTER 3. THE DEEP UNDERGROUND NEUTRINO EXPERIMENT



**Figure 3.18:** Schematic representation of the electrode strip configuration for a top (left) and bottom (right) CRU. Figure taken from Ref. [100].

the cathode, in order to maximise the photon yield.

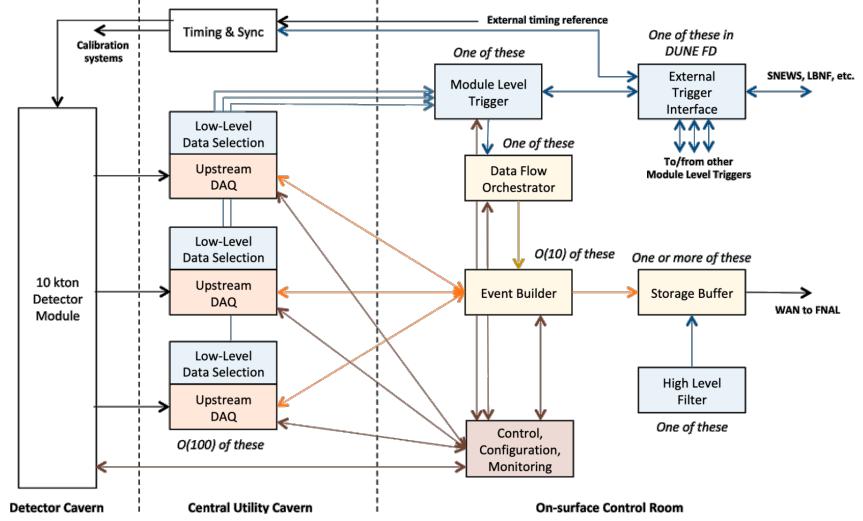
### 3.6.3 FD Data Acquisition System

The data acquisition (DAQ) system receives, processes and stores data from the detector modules. In the case of DUNE the DAQ architecture is designed to work for all FD modules interchangeably, except some aspects of the upstream part which may depend on the specific module technology.

The enormous sample rate and the number of channels in TPC and PD readouts will produce a very large volume of data. These pose really strong requirements and challenges to the DUNE FD DAQ architecture. It will be required to read out data of the order of ten thousand or more channels at rates of a few MHz. To cope with the huge data volume, segmented readouts and compression algorithms are used to reduce the data rate to manageable levels.

The DAQ system of the DUNE FD is composed of five different subsystems. The

### 3.6. FAR DETECTOR



**Figure 3.19:** Detailed diagram of the DUNE FD DAQ system. Figure taken from Ref. [101].

1441 first one is the upstream DAQ, which receives the raw data from the detector, buffers it  
 1442 and perform some low-level pre-processing. The minimally processed data is then fed  
 1443 into a hierarchical data selection system, which then performs a module level trigger  
 1444 decision. In case of a positive decision a trigger command is produced and executed by  
 1445 the data flow orchestrator, located in the back-end (BE) DAQ subsystem. Subsequently  
 1446 the DAQ BE retrieves the relevant data from the buffers located in the upstream DAQ,  
 1447 adds all the data into a cohesive record and saves it to permanent storage. Watching  
 1448 over all the other subsystems we also have the control, configuration and monitoring  
 1449 subsystem and the time and synchronization subsystem. Figure 3.19 shows a schematic  
 1450 diagram of the DAQ system, showing the different subsystems and their relations.

1451 A notorious challenge for the DUNE DAQ system comes from its broad physics  
 1452 goals. We must be prepared to process events spanning a wide range of time windows  
 1453 (from 5 ms in the case of beam and cosmic neutrinos and nucleon decay to 100 s in the  
 1454 case of SNBs) and therefore this requires a continuous readout of the detector modules.  
 1455 Moreover, because of the off-beam measurements we need to ensure the capabilities  
 1456 of online data processing and self-triggering. Having this into account, together with  
 1457 the technical constraints, the DUNE FD DAQ faces a series of challenges: it needs to

### CHAPTER 3. THE DEEP UNDERGROUND NEUTRINO EXPERIMENT

- 1458 be fault tolerant and redundant to reduce downtime, accommodate new components
- 1459 while it keeps serving the operational modules, have large upstream buffers to handle
- 1460 SNB physics, be able to support a wide range of readout windows and last reduce the
- 1461 throughput of data to permanent storage to be at most 30 PB/year.

# 4

1462

1463

## Matched Filter approach to Trigger

1464

## Primitives

### 4.1 Motivation

1465 The filter implemented in the firmware of the upstream DUNE FD DAQ is a 32nd-order  
1466 low-pass finite impulse-response (FIR) filter. The output of such filter for a discrete  
1467 system can be written as:

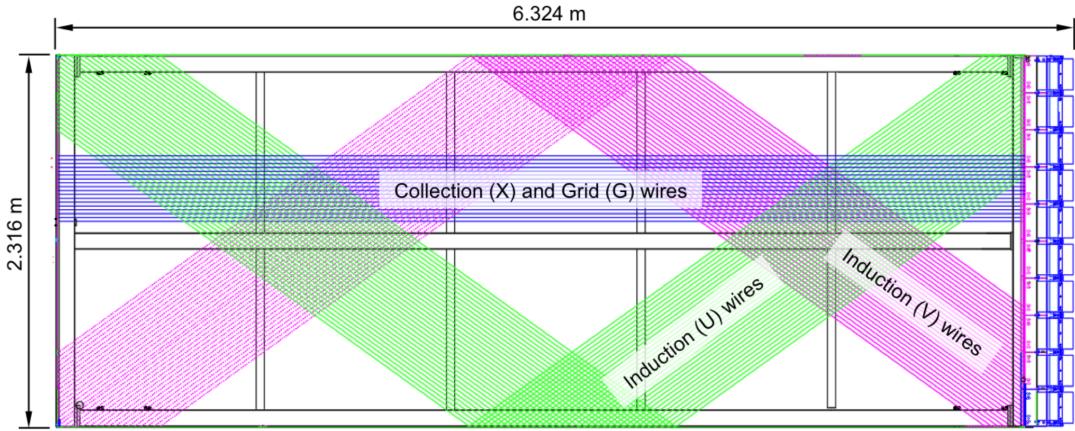
$$y[i] = \sum_{j=0}^N h[j]x[i-j], \quad (4.1)$$

1468 where  $N$  is the order of the filter,  $y$  is the output sequence,  $x$  is the input sequence and  $h$   
1469 is the set of coefficients of the filter. The current implementation within `dtp-firmware`  
1470 [102] uses a set of 16 non-zero integer coefficients.

1471 Filtering is a vital step in the hit finder chain. It helps to suppress the noise and  
1472 enhance the signal peaks with respect to the noiseless baseline. A good filtering strategy  
1473 allows us to use lower thresholds when forming the trigger primitives (TPs) and thus  
1474 increasing the sensitivity of our detector to low energy physics events. In such events,  
1475 the hits produced by the ionisation electrons tend to have lower amplitudes than those  
1476 of interest to the baseline physics programme of the DUNE experiment.

1477 This is particularly important for the induction planes. In general, signal peaks in  
1478 the induction wires have smaller amplitude than the ones in the induction plane. This,  
1479 together with the fact that the pulse shapes are bipolar, reduces our capacity to detect

## CHAPTER 4. MATCHED FILTER APPROACH TO TRIGGER PRIMITIVES



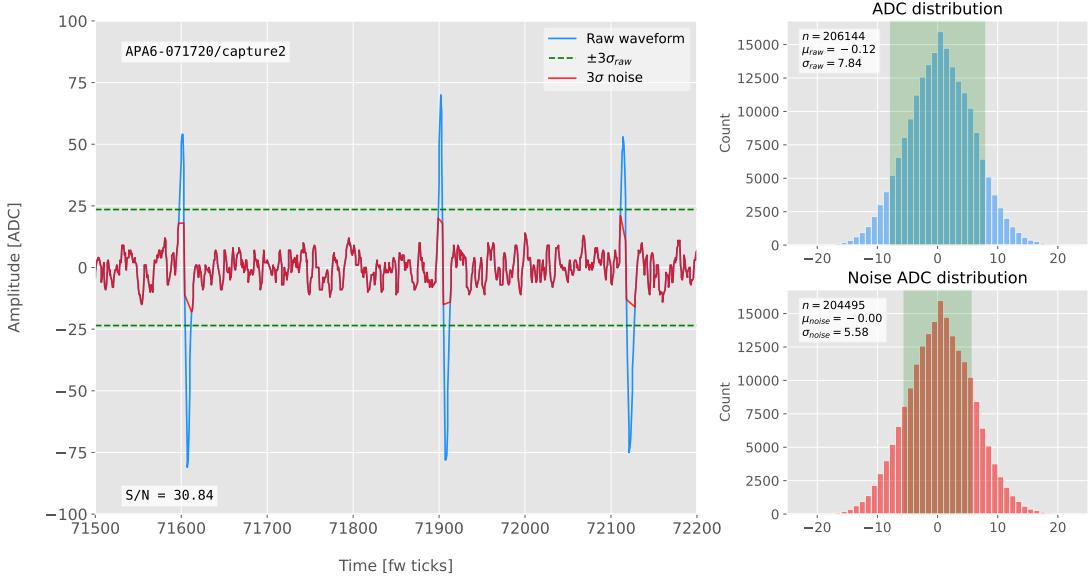
**Figure 4.1:** Schematic representation of an APA. The black lines represent the APA steel frame. The green and magenta lines correspond to the direction of the U and V induction wires respectively. The blue lines indicate the direction of the X collection wires and the wire shielding G.

the hits on these channels. The inefficiency of detecting TPs in the induction planes (denoted as U and V planes) lead trigger algorithms to focus mainly on the TPs from the collection plane (so-called X plane). As a result, the possibility of making trigger decisions based on the coincidence of TPs across the three wire planes remains nowadays unexploited in DUNE. Fig. 4.1 shows a schematic view of an anode plane assembly (APA), with the different wire plane orientations highlighted.

A possible improvement of the current hit finder chain could require optimising the existing or choosing a new filter implementation. A filter strategy which improves the induction signals may be able to enhance the detection efficiency of TPs from the induction planes and ideally make it comparable to that of the collection plane.

The goal is to implement a better finite-impulse response filter design and to evaluate its performance relative to the current filter. To do so, we need to take into account the limitations of the firmware: the FIR filter shall have maximum 32 coefficients (so-called taps) whose values are 12-bit unsigned integers. Although it is technically possible to include non-integer coefficients, it would be a technical challenge as we have 40 FIR instances per APA, as there are 4 FIR per optical link and 10 optical links per APA. With these restrictions, the task is to provide a set of 32 coefficients which yield an

## 4.2. SIGNAL-TO-NOISE RATIO DEFINITION



**Figure 4.2:** Left panel: Zoomed unfiltered waveform corresponding to channel 7840 from the ProtoDUNE-SP raw data capture `felix-2020-07-17-21:31:44` (blue line). The green dashed lines mark the region  $\pm 3\sigma_{\text{raw}}$ . The resulting noise waveform is also shown (red line). Top right panel: ADC distribution for channel 7840, where the green shaded region represents  $\pm \sigma_{\text{raw}}$ . Bottom right panel: noise ADC distribution for channel 7840, where the green shaded region represents  $\pm \sigma_{\text{noise}}$ .

1498 optimal filter performance for the induction wires.

## 1499 4.2 Signal-to-noise ratio definition

1500 I introduce the signal to noise ratio (S/N) as a measure of the FIR filter performance  
1501 and demonstrate how to extract its value for a set of ProtoDUNE-SP data. The S/N  
1502 metrics allow us to compare different filter implementations and serve as a basis for more  
1503 detailed studies presented later in this document. Specifically, I use the ADC capture  
1504 `felix-2020-07-17-21:31:44` (data capture taken for firmware validation purposes). I  
1505 defined S/N as the height of the signal peaks relative to the size of the noise peaks.  
1506 To quantify this quantity channel by channel one first need to estimate the standard  
1507 deviation of the ADC data for each channel,  $\sigma_{\text{ADC}}$ . Then, I define the corresponding  
1508 noise waveform to be the ADC values in the range  $\pm 3\sigma_{\text{ADC}}$ . From this new noise data  
1509 one can estimate again the mean and standard deviation,  $\mu_{\text{noise}}$  and  $\sigma_{\text{noise}}$ , so I can

## CHAPTER 4. MATCHED FILTER APPROACH TO TRIGGER PRIMITIVES

1510 write the S/N for any given channel as:

$$S/N = \frac{\max[ADC] - \mu_{noise}}{\sigma_{noise}}, \quad (4.2)$$

1511 where  $\max[ADC]$  is simply the maximum ADC value found in the corresponding channel.

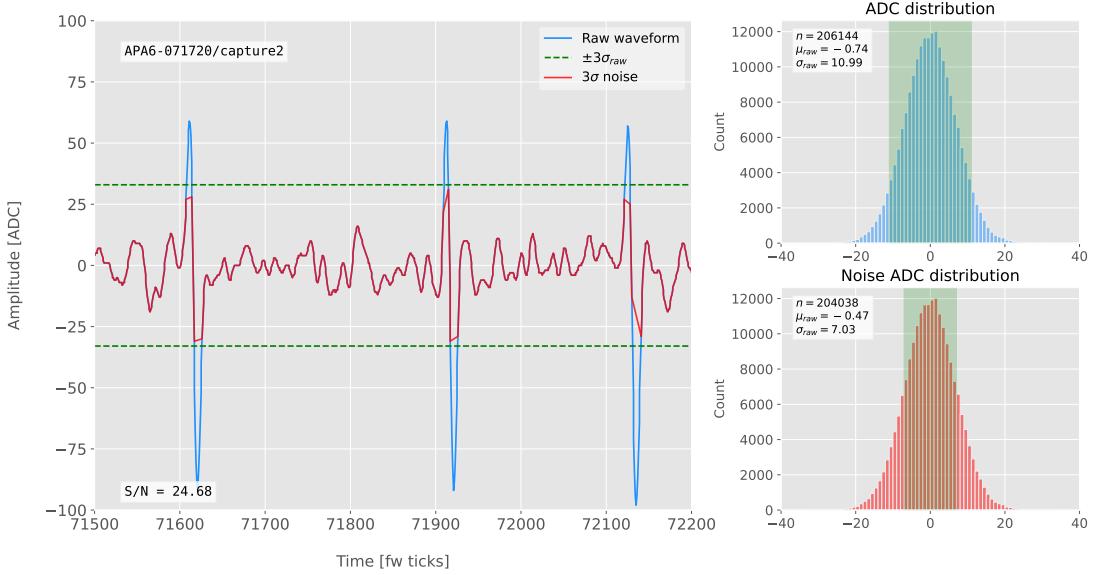
1512 One can apply this definition of the S/N with a waveform from one of the channels  
 1513 of the data capture<sup>1</sup>. Fig. 4.2 shows a zoomed region of the waveform corresponding to  
 1514 channel 7840 (blue line), where one can clearly see three signal peaks and continuous  
 1515 additive noise (we actually see 6 peaks, 3 positive and 3 negative, but, because by design  
 1516 for induction channels the expected signal pulse shapes are bipolar, I treat them as a  
 1517 collection of 3 individual signal peaks). I estimated the standard deviation of this raw  
 1518 waveform to be  $\sigma_{raw} = 7.84$  ADC, so I am able to define the noise waveform (red line)  
 1519 as the ADC values in the range  $\pm 23.52$  ADC. This way one obtains  $\mu_{noise} = 0$  and  
 1520  $\sigma_{noise} = 5.58$  ADC, which gives  $S/N = 30.84$ .

1521 We can repeat this calculation now for the corresponding filtered waveform (using the  
 1522 current firmware FIR filter). In Fig. 4.3 I plotted the same time window for the filtered  
 1523 waveform from channel 7840 (blue line). In this case, the standard deviation of the  
 1524 waveform is larger than before, giving  $\sigma_{raw} = 10.99$  ADC. The resulting noise waveform  
 1525 (red line) results from selection the ADC values in the range  $\pm 32.91$  ADC, giving now  
 1526  $\mu_{noise} = -0.47$  ADC and  $\sigma_{noise} = 7.03$  ADC. Finally, one obtains  $S/N = 24.68$ . Notice  
 1527 that the value of S/N decreases after the filtering. Clearly, one can see that the noise  
 1528 baseline has increased by a factor of 1.35 when we applied the FIR filter and at the same  
 1529 time the amplitude of the signal peaks has remained almost unchanged, leading to this  
 1530 poorer S/N value.

---

<sup>1</sup>All the original work was done within the `dtp-simulation` package [103], which offers a variety of tools to read raw data and emulate the TPG block (pedestal subtraction, filtering and hit finder). However, the results shown in this report were re-worked later using the C++ based `dtpemulator` package [104]. Its main purpose is the emulation of the TPG block and, in the same way as its predecessor, it has been cross-checked against the current firmware implementation.

### 4.3. LOW-PASS FIR FILTER DESIGN



**Figure 4.3:** Left panel: Zoomed filtered waveform corresponding to channel 7840 from the ProtoDUNE-SP raw data capture `felix-2020-07-17-21:31:44` (blue line). The filter used was the current implementation of the low-pass FIR filter in `dtp-firmware`. The green dashed lines mark the region  $\pm 3\sigma_{\text{raw}}$ . The resulting noise waveform is also shown (red line). Top right panel: ADC distribution for channel 7840 after filtering, where the green shaded region represents  $\pm \sigma_{\text{raw}}$ . Bottom right panel: noise ADC distribution for channel 7840 after filtering, where the green shaded region represents  $\pm \sigma_{\text{noise}}$

## 1531 4.3 Low-pass FIR filter design

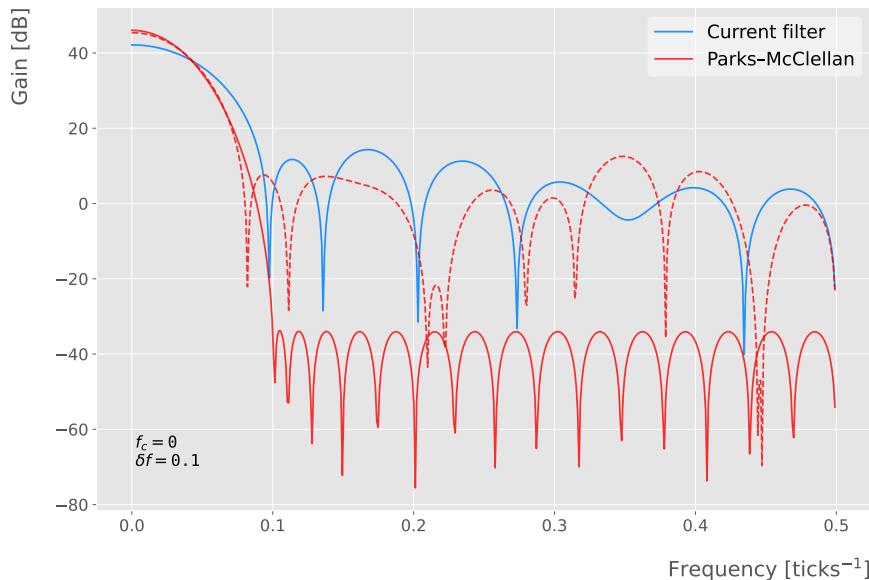
1532 In general, when one uses a method to optimize the frequency response of a digital filter,  
 1533 such as the Parks-McClellan algorithm, one finds a set of  $N$  real coefficients that give  
 1534 the best response for the specified pass-band and order of the filter [105].

1535 In our case, as the sampling frequency is defined as  $1 \text{ ticks}^{-1}$ , the Nyquist frequency  
 1536 will simply be  $1/2 \text{ ticks}^{-1}$ . The current implementation of the filter seems to have as  
 1537 pass-band the range  $[0, 0.1] \text{ ticks}^{-1}$ . This can be seen in Fig. 4.4, where I show the  
 1538 power spectrum, in decibels, of such filter implementation (blue solid line). For instance,  
 1539 the Park-McClellan algorithm finds the optimal Chebyshev FIR filter taking as input  
 1540 the boundaries of the target pass-band and stop-band, which can be written in the form:

$$\left\{ \begin{array}{l} [0, f_c] \\ [f_c + \delta f, f_N] \end{array} \right. , \quad (4.3)$$

## CHAPTER 4. MATCHED FILTER APPROACH TO TRIGGER PRIMITIVES

where  $f_c$  is the cut-off frequency,  $\delta f$  is the transition width and  $f_N$  is the aforementioned Nyquist frequency. A similar behaviour to the one in the current filter can be obtained by setting  $f_c = 0$  and  $\delta f = 0.1 \text{ ticks}^{-1}$ . The response of the resulting filter is also shown in Fig. 4.4 (blue solid line). Notice that the suppression of the stop-band is enhanced for this optimal filter. For comparison I included the power response of the filter obtained by taking the integer part of the coefficients resulting from the Parks-McClellan method (red dashed line). One can see that it does not suppress that much the stop-band, in a similar way to the current implementation of the filter.

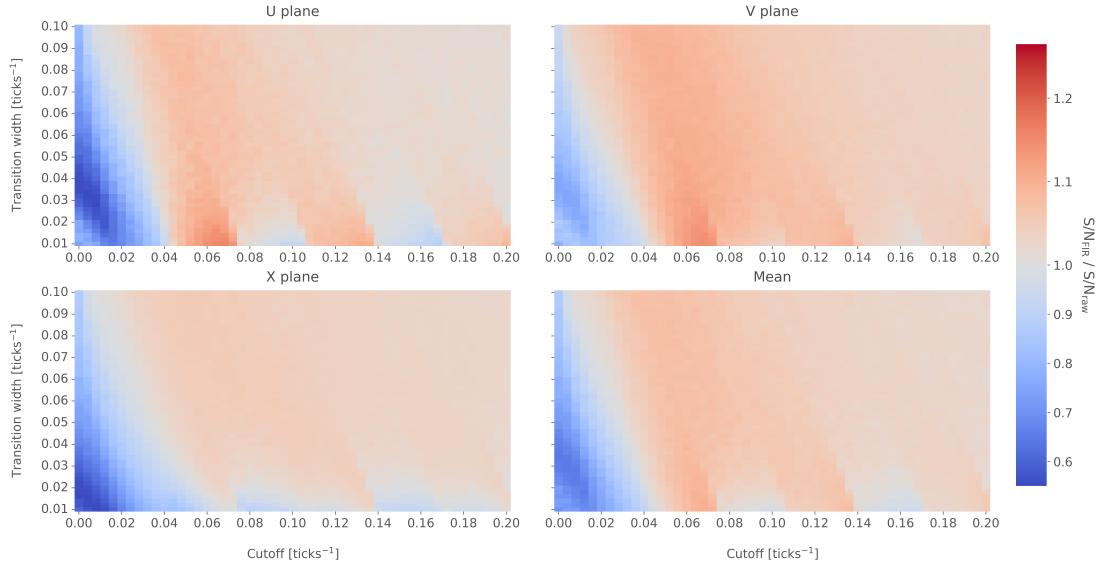


**Figure 4.4:** Power spectrum in decibels for the current implementation of the low-pass FIR filter in `dtp-firmware` (blue line), compared to the response of an optimal filter obtained using the Parks-McClellan algorithm for the same pass-band (red line). Also for comparison I include the spectrum of the optimal filter when taking only the integer part of the coefficients (red dashed line).

At this point, I tried to improve the performance of the FIR filter using the Parks-McClellan method, i.e. maximize the overall S/N, using the available data captures. I did so by varying the values of the two quantities that parametrize the pass-band and stop-band, the cut-off frequency  $f_c$  and the transition width  $\delta f$ .

Fig. 4.5 shows the average relative change in the S/N (i.e. the ratio between the value of the S/N after and before the filtering) for capture `felix-2020-07-17-21:31:44`,

### 4.3. LOW-PASS FIR FILTER DESIGN

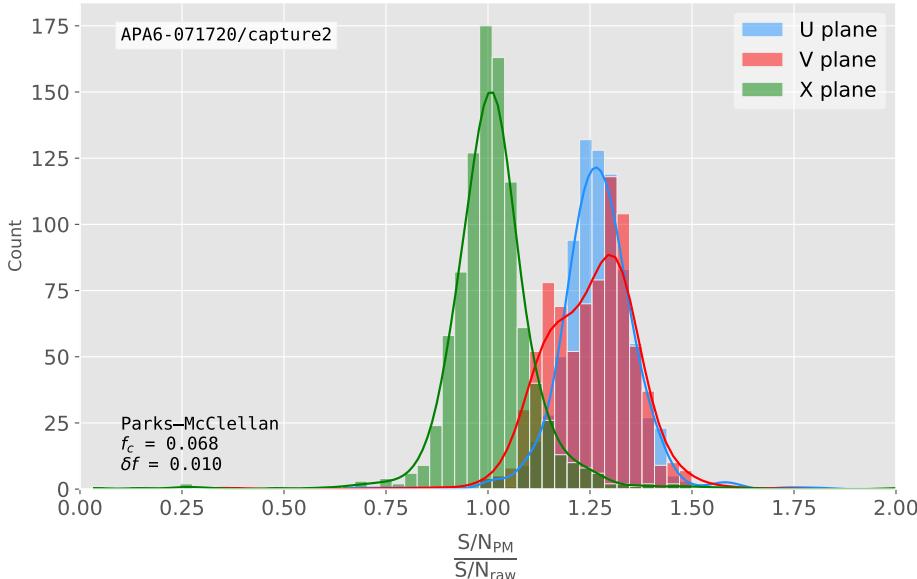


**Figure 4.5:** Relative change in the S/N for the ProtoDUNE-SP raw data capture `felix-2020-07-17-21:31:44`, using different values of the cutoff frequency  $f_c$  and the transition width  $\delta f$ . The optimal Chebyshev filters were applied using just the integer part of the coefficients given by the Parks-McClellan algorithm.

when using filters designed with the Parks-McClellan algorithm for the specified values of the cut-off frequency  $f_c$  and the transition width  $\delta f$ , restricted to integer values for the filter coefficients. One can clearly distinguish different regions where we get an improvement of up to a factor of 1.35 for the U plane. For large values of  $f_c + \delta f$  the ratio tends to 1, as expected (in that limit the width of the stop-band goes to 0, meaning that no frequencies are filtered out and thus the waveform remains the same).

Using the configuration which gives the best mean performance for the three planes (see bottom right panel of Fig. 4.5), i.e.  $f_c = 0.068 \text{ ticks}^{-1}$  and  $\delta f = 0.010 \text{ ticks}^{-1}$ , we can see how such filter affects the different channels. Fig. 4.6 shows the distribution of the S/N improvement values for all the channels in the raw ADC capture `felix-2020-07-17-21:31:44`, separated by wire plane, after the optimal Chebyshev filter was applied. One can see that there is a clear improvement for both U and V induction wire planes, obtaining a mean change of 1.25 and 1.30 for them respectively. However, in the case of the collection plane X the mean of this distribution is roughly 1, meaning that a good fraction of channels in that plane get a slightly worse S/N after the

## CHAPTER 4. MATCHED FILTER APPROACH TO TRIGGER PRIMITIVES



**Figure 4.6:** Distribution of the relative change of the S/N on the different wire planes from the ProtoDUNE-SP raw data capture *felix-2020-07-17-21:31:44* after the optimal Chebyshev filter was applied. The filter was computed with the Parks-McClellan algorithm using a cutoff of  $f_c = 0.068 \text{ ticks}^{-1}$  and a transition width  $\delta f = 0.010 \text{ ticks}^{-1}$ .

filter is applied. In any case, this is not a big issue as the S/N for collection channels is usually much higher than the one for induction channels.

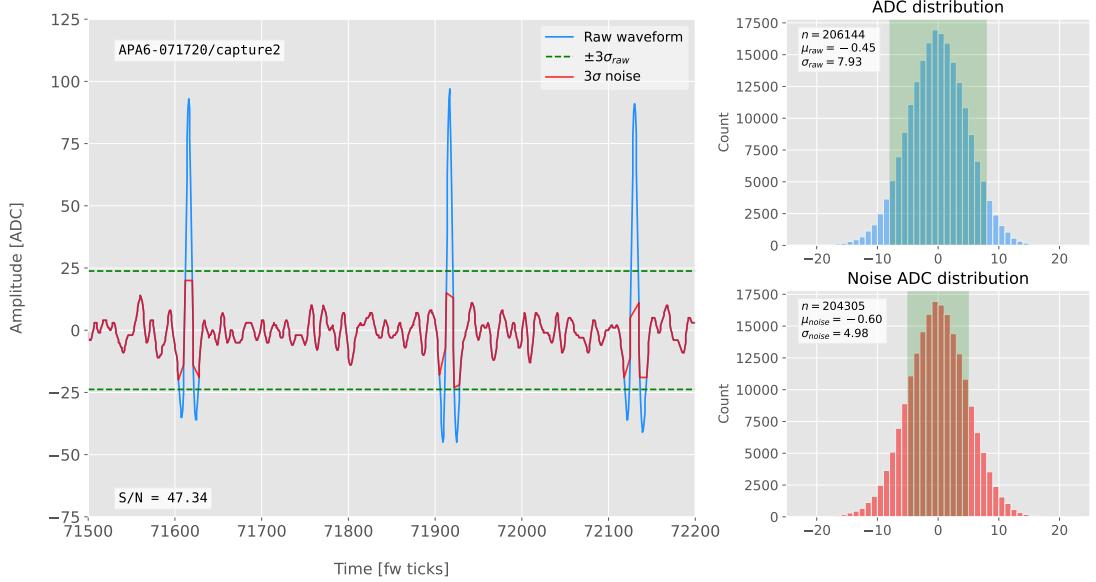
The results I obtained optimising the low pass filter with the Parks-McClellan method are promising. Nonetheless, the improvement found is rather marginal so I wondered if there could be an alternative approach to the filtering problem which yields better outputs. At this point, I found a possible alternative in matched filters. By construction, this kind of filters offer the best improvement on the S/N.

## 4.4 Matched filters

In the context of signal processing, a matched filter is the optimal linear filter for maximising the signal-to-noise ratio (S/N) in the presence of additive noise, obtained by convolving a conjugated time-reversed known template with an unknown signal to detect the presence of the template in the signal [106].

Given a known signal sequence  $s(t)$  and another (a priori unknown) noise sequence

#### 4.4. MATCHED FILTERS



**Figure 4.7:** Left panel: Zoomed match filtered waveform corresponding to channel 7840 from the ProtoDUNE-SP raw data capture felix-2020-07-17-21:31:44 (blue line). The filter used was directly extracted from the data, being the 32 values around the first peak in the original waveform. The green dashed lines mark the region  $\pm 3\sigma_{\text{raw}}$ . The resulting noise waveform is also shown (red line). Top right panel: ADC distribution for channel 7840 after match filtering, where the green shaded region represents  $\pm \sigma_{\text{raw}}$ . Bottom right panel: noise ADC distribution for channel 7840 after match filtering, where the green shaded region represents  $\pm \sigma_{\text{noise}}$

1583  $n(t)$ , the input signal can be written as:

$$x(t) = s(t) + n(t). \quad (4.4)$$

1584 Now, considering a linear time-invariant filter, whose impulse-response function I  
1585 will refer to as  $h(t)$ , one can write the output signal as:

$$\begin{aligned} y(t) &= x(t) * h(t) \\ &= (s(t) + n(t)) * h(t) \\ &= y_s(t) + y_n(t), \end{aligned} \quad (4.5)$$

1586 where  $y_s(t)$  and  $y_n(t)$  are simply the outputs of the filter due to the signal and the noise  
1587 components respectively.

## CHAPTER 4. MATCHED FILTER APPROACH TO TRIGGER PRIMITIVES

1588 The goal of the matched filter is to detect the presence of the signal  $s(t)$  in the input  
 1589 sample  $x(t)$  at a certain time  $t_0$ , which effectively means we need to maximise the S/N.  
 1590 This way, what one wants is to have a filter which gives a much bigger output when the  
 1591 known signal is present than when it is not. Putting it in other words, the instantaneous  
 1592 power of the signal output  $y_s(t)$  should be much larger than the average power of the  
 1593 noise output  $y_n(t)$  at some time  $t_0$ .

1594 For the case of the filtered signal, one can easily re-write it as an inverse Fourier  
 1595 transform:

$$y_s(t) = \frac{1}{2\pi} \int_{-\infty}^{\infty} d\omega H(\omega)S(\omega)e^{i\omega t}, \quad (4.6)$$

1596 where  $H(\omega)$  and  $S(\omega)$  are the Fourier transforms of the impulse-response function (i.e.  
 1597 the transfer function of the filter) and of the input signal, respectively.

1598 Now focusing on the noise, we can use the Wiener-Khinchin theorem [107] to write  
 1599 the mean power of the noise after filtering as:

$$E|y_n(t)|^2 = \frac{1}{2\pi} \int_{-\infty}^{\infty} d\omega |H(\omega)|^2 S_n(\omega), \quad (4.7)$$

1600 where  $S_n(\omega)$  is the power spectral density of the noise.

1601 Having these, one can write the instantaneous S/N at time  $t_0$  as:

$$\begin{aligned} \left( \frac{S}{N} \right)_{t_0} &= \frac{|y_s|^2}{E|y_n(t)|^2} \\ &= \frac{1}{2\pi} \frac{\left| \int_{-\infty}^{\infty} d\omega H(\omega)S(\omega)e^{i\omega t_0} \right|^2}{\int_{-\infty}^{\infty} d\omega |H(\omega)|^2 S_n(\omega)}. \end{aligned} \quad (4.8)$$

1602 Once we have this expression, we need to find the upper limit of it to determine what  
 1603 would be the optimal choice for the transfer function. One can use the Cauchy-Schwarz  
 1604 inequality, which in the present case takes the form:

$$\left| \int_{-\infty}^{\infty} dx f(x)g(x) \right|^2 \leq \int_{-\infty}^{\infty} dx |f(x)|^2 + \int_{-\infty}^{\infty} dx |g(x)|^2, \quad (4.9)$$

#### 4.4. MATCHED FILTERS

1605 for any two analytical functions  $f(x)$  and  $g(x)$ . One can prove that making the choice:

$$\begin{aligned} f(x) &= H(\omega) \sqrt{S_n(\omega)} e^{i\omega t_0}, \\ g(x) &= \frac{S(\omega)}{\sqrt{S_n(\omega)}}, \end{aligned} \quad (4.10)$$

1606 leads to the following upper bound for the S/N:

$$\left( \frac{S}{N} \right)_{t_0} \leq \frac{1}{2\pi} \int_{-\infty}^{\infty} d\omega \frac{|S(\omega)|^2}{S_n(\omega)}. \quad (4.11)$$

1607 From Eqs. (4.8), (4.9) and (4.10) one can also derive the form of the transfer function  
1608 such that the upper bound is exactly reached [108]:

$$H(\omega) \propto \frac{S^*(\omega) e^{-i\omega t_0}}{S_n(\omega)}. \quad (4.12)$$

1609 From this last expression we can clearly see the way the matched filter acts. As the  
1610 transfer function is proportional to the Fourier transform of the signal it will try to only  
1611 pick the frequencies present in the signal [109].

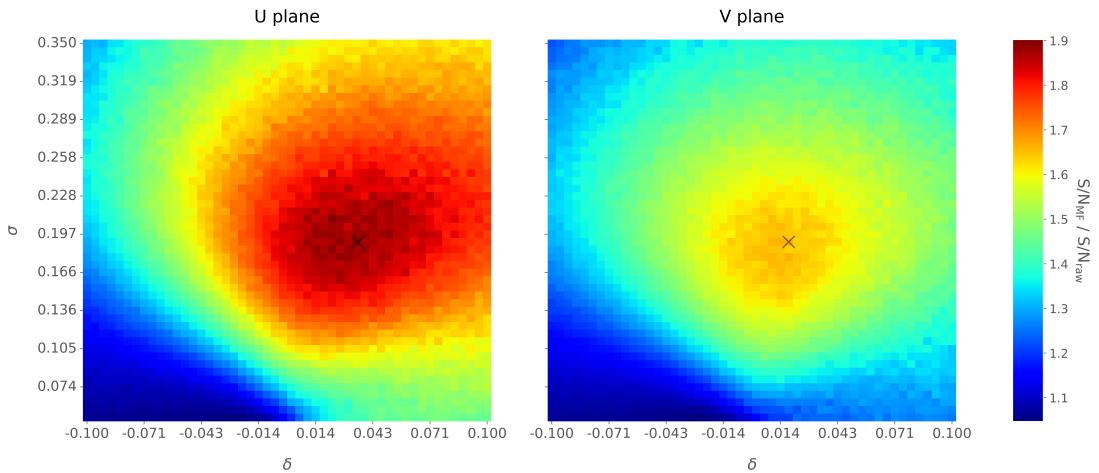
1612 The matched filter transfer function can be greatly simplified if the input noise is  
1613 Gaussian. In that case, the power spectral density of the noise is a constant, so it can be  
1614 re-absorbed in the overall normalisation of the transfer function. Moreover, considering  
1615 that the input signal is a real function, one can simply set  $S^*(\omega) = S(-\omega)$ , which gives:

$$H(\omega) \propto S(-\omega) e^{-i\omega t_0}. \quad (4.13)$$

1616 For a discrete signal, one can think of the input and impulse-response sequences as  
1617 vectors of  $\mathbb{R}^N$ . Then, the matched filter tries to maximise the inner product of the signal  
1618 and the filter while minimising the output due to the noise by choosing a filter vector  
1619 orthogonal to the later. In the case of additive noise, that leads to the impulse-response  
1620 vector:

$$h = \frac{1}{\sqrt{s^\dagger R_n^{-1} s}} R_n^{-1} s, \quad (4.14)$$

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**Figure 4.8:** Relative improvement in the S/N for the raw data capture `felix-2020-07-17-21:31:44`, using the matched filter following the parametrisation in Eq. (4.17). The black crosses in both panels denote the location of the maximum ratio value.

where  $s$  is a reversed signal template sequence of length  $N$  equal to the order of the filter and  $R_n$  is the covariance matrix associated with the noise sequence  $n$ . For the Gaussian noise case, the covariance matrix is simply the unit matrix, so the above expression simplifies again to:

$$h = \frac{s}{|s|}. \quad (4.15)$$

For this first stage of the study, I use a definition of the S/N per channel given by:

$$\text{S/N} = \frac{\max [ADC] - \mu_{noise}}{\sigma_{noise}}, \quad (4.16)$$

where the subscript *noise* refers to a subset of the data obtained by only taking into account waveform values within a  $\pm 3\sigma$  range around the mean of the data and  $\max [ADC]$  is the maximum of the original waveform. This definition is further discussed in App. 4.2, where I also show examples of its application to raw data and to a waveform filtered with the current low-pass FIR filter.

To test whether this choice of filter is appropriate one needs to choose a signal template. As an example of how a matched filter would affect our signal, I simply took the filter coefficients to be the 32 ADC values around a signal peak present in the data.

#### 4.4. MATCHED FILTERS

1634 In Fig. 4.7 (left panel) I plotted a zoomed region for channel 7840 in the raw data capture  
1635 `felix-2020-07-17-21:31:44`, after applying the matched filter described before (blue  
1636 line). When compared to the raw and FIR filtered case (see App. 4.2), after applying  
1637 the match filter the standard deviation of the noise waveform (red line) decreases and at  
1638 the same time the signal peaks are enhanced. This leads to an improvement of the S/N  
1639 by a factor of 1.92 when compared to the raw waveform.

1640 In order to obtain the matched filter that is more suitable for our data, I explored  
1641 different configurations of signal templates. In order to perform this exploration, I  
1642 parametrised the signal using the bipolar function:

$$f(x) = -A(x + \delta) e^{-x^2/\sigma^2}, \quad (4.17)$$

1643 where the parameter  $\delta$  controls the asymmetry between the positive and negative peaks  
1644 and  $\sigma$  controls their width. The amplitude parameter  $A$  is set such that it keeps the  
1645 height of the biggest peak to be less than 200 ADC in absolute value.

1646 As this parametrisation is only adequate for bipolar signals I will focus exclusively  
1647 on the induction channels. Also, the optimal configurations I found for the U and V  
1648 plane will be kept separate, i.e. I will have two sets of coefficients that will be applied to  
1649 either the U and V planes of wires. I do so as I found this was the choice giving the  
1650 best performance. Even so, as I will discuss, the differences are not very pronounced. In  
1651 case it is not technically possible to separate channels in the firmware according to the  
1652 wire plane they come from and use different sets of filter coefficients for them, we can  
1653 just find a common unique set of coefficients. In such case, I do not expect our results  
1654 to change dramatically.

1655 In Fig. 4.8 I present the results of our parameter scan, for channels in the induction  
1656 planes U (left panel) and V (right panel). For each configuration of  $\sigma$  and  $\delta$  the resulting  
1657 matched filter was applied to all channels in the corresponding plane within the data  
1658 capture `felix-2020-07-17-21:31:44`, the S/N improvement was computed with respect  
1659 to the raw waveforms and then the S/N mean value was kept as a score for such filter.

## CHAPTER 4. MATCHED FILTER APPROACH TO TRIGGER PRIMITIVES

1660 One can see that the improvement obtained for the U plane is in general higher than the  
1661 one for the V plane. In any case, I got substantially higher ratios than the ones obtained  
1662 for the low-pass FIR filters. For the optimal configurations I attained improvements up  
1663 to a factor of 1.85 for the U plane and 1.65 for the V plane.

1664 The sets of optimal matched filter coefficients were obtained for the parameters  
1665  $\delta = 0.035$ ,  $\sigma = 0.191$  for the U plane and  $\delta = 0.018$ ,  $\sigma = 0.191$  for the V plane. I  
1666 show these two sets of coefficients in Fig. 4.9 (left panel). Also in Fig. 4.9 (right  
1667 panel) I plot the distribution of the S/N improvement after the optimal match filters  
1668 for the U and V were applied to the corresponding channels in the raw data capture  
1669 `felix-2020-07-17-21:31:44`. As mentioned before, the mean improvement achieved  
1670 for the U plane channels is slightly bigger than the one for the V channels. Note, however,  
1671 that the spread of the distribution for the V plane is also smaller than the one for the U  
1672 plane.

1673 I also performed a similar scan for the case of a low-pass FIR filter using the Parks-  
1674 McClellan algorithm. In that case, the parameters to check were the cutoff frequency  
1675 and the transition width of the filter. A summary of the results is given in App. 4.3.

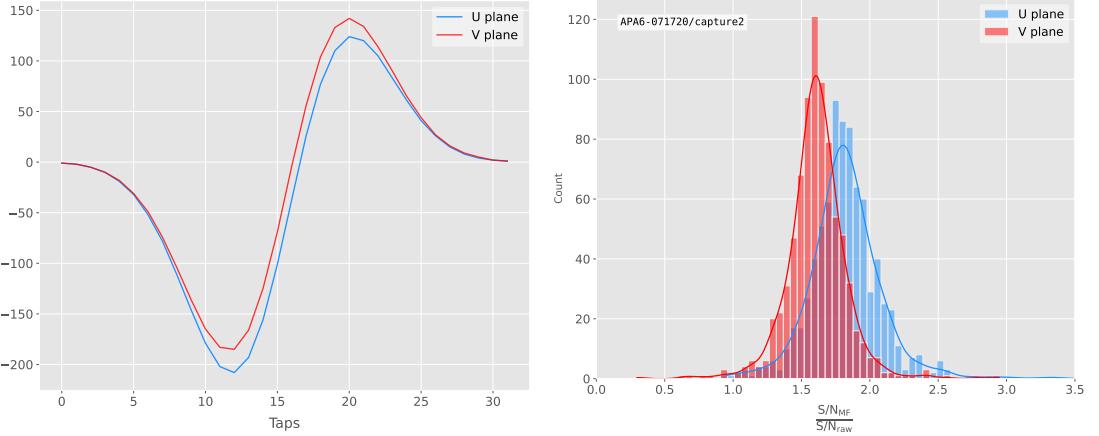
1676 Overall, one can see that the improvements on the S/N are much more significant in  
1677 the case of the matched filter than it is for the low-pass FIR filters. The analysis of this  
1678 and other raw data captures from ProtoDUNE-SP suggest that matched filters increase  
1679 the S/N of induction channels by a factor of 1.5 more than the optimal low-pass FIR  
1680 filters.

1681 Although these results are by themselves great points in favour of the matched  
1682 filter, more studies are needed to completely assess the robustness of this approach. I  
1683 proceeded then to test the matched filter with simulated data samples.

### 1684 4.5 Using simulated samples

1685 In order to further test the matched filter, the next step was to generate and process  
1686 data samples using *LArSoft* [110]. In this way, one can control the particle content of

## 4.5. USING SIMULATED SAMPLES



**Figure 4.9:** Left panel: Optimal matched filter coefficients for the U (blue line) and V (red line) planes. The filters were computed with our parametrisation in Eq. (4.17) for the parameter values  $\delta = 0.035$ ,  $\sigma = 0.191$  and  $\delta = 0.018$ ,  $\sigma = 0.191$  respectively. Right panel: Distribution of the relative change of the S/N on the two induction wire planes from the ProtoDUNE-SP raw data capture *felix-2020-07-17-21:31:44* after their respective optimal matched filters were applied.

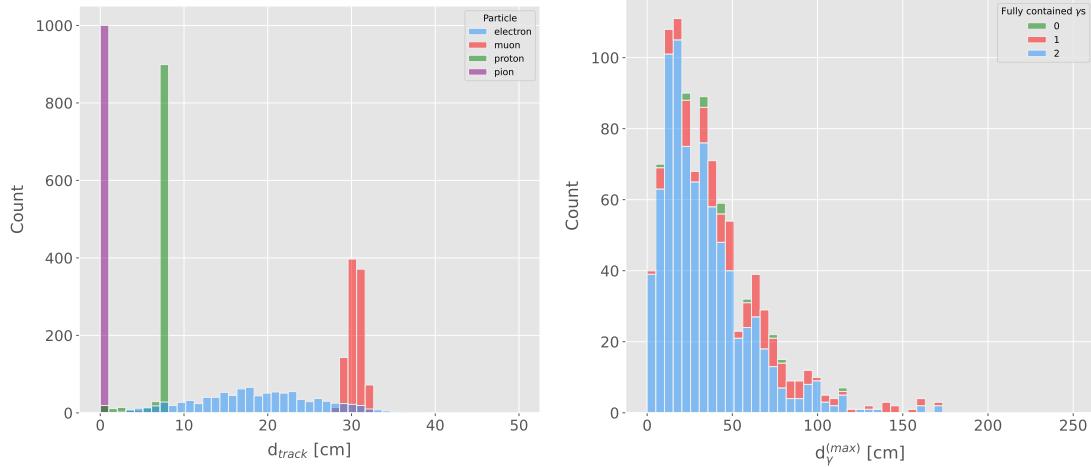
the samples, the orientation of the tracks and their energy, and therefore see how the matched filter behaves in various situations.

To begin with, I prepared different monoenergetic and isotropic samples containing a single particle per event. Each sample contains a different particle species, namely electrons, muons, protons and neutral pions all with a kinetic energy of  $E_k = 100$  MeV. I chose these because of the fairly different topologies they generate in the liquid argon, ranging from shower-like to track-like. The procedure I followed to generate the samples and process them is discussed in detail in App. ??.

These were generated with the single particle gun and the Geant4 stage of the *LArSoft* simulation [110] was performed with the standard configuration for the DUNE FD 10kt module.

For simplicity, I restricted the particles to start drifting in a single TPC volume (in this case TPC 0), so I can focus exclusively on the signals coming from one APA. The chosen kinetic energy for all the particles in my first trial is  $E_k = 100$  MeV, so a necessary check is to see if all our tracks will be typically contained in one TPC volume. Fig. 4.10 (left panel) shows the distributions of the track lengths in the liquid argon

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**Figure 4.10:** Left panel: distributions of the particles track length in the liquid argon for the generated  $E_k = 100$  MeV monoenergetic samples, electrons (blue), muons (red), protons (green) and neutral pions (purple). Right panel: distribution of the length of the longest photon in the neutral pion sample after the decay process  $\pi^0 \rightarrow \gamma\gamma$ .

of all generated particles with  $E_k = 100$  MeV. One can see that, in the case of the track-like particles (i.e. muons and protons), their length distributions are quite sharp and centered at relatively low distances (30 and 8 cm, respectively). For electrons, the distribution is quite broad but it does not extend past  $\sim 30$  cm. The case of neutral pions can be misleading, as they decay promptly the track length associated with the true Monte Carlo particle is always  $< 1$  cm. In Fig. 4.10 (right panel) I show the effective length distribution of the longest photon after the pion decays as  $\pi^0 \rightarrow \gamma\gamma$ , highlighting the number of fully contained photons in the TPC volume per event (either zero, one or both). One can see that the vast majority of events has both photons contained and that just a negligible number of them has none of them contained in the TPC volume. In any case, for the sake of caution, I will only keep the pion events with both photons contained.

Once I have prepared a sample at the Geant4 level, I need to process it through the detector simulation. In order to make adequate estimations of the noise levels and run the filtering and hit finder as I did with the ProtoDUNE data, one needs to turn off the default zero-suppression of the waveforms produced by the simulation. At this first stage I am only concerned with the waveforms with the noise added, so I keep the noise

## 4.5. USING SIMULATED SAMPLES

addition option as true in the configuration. However, for studies related to the hit finder performance one will also need to store the noiseless waveforms in order to retrieve the truth information of the hits. I will discuss this approach next.

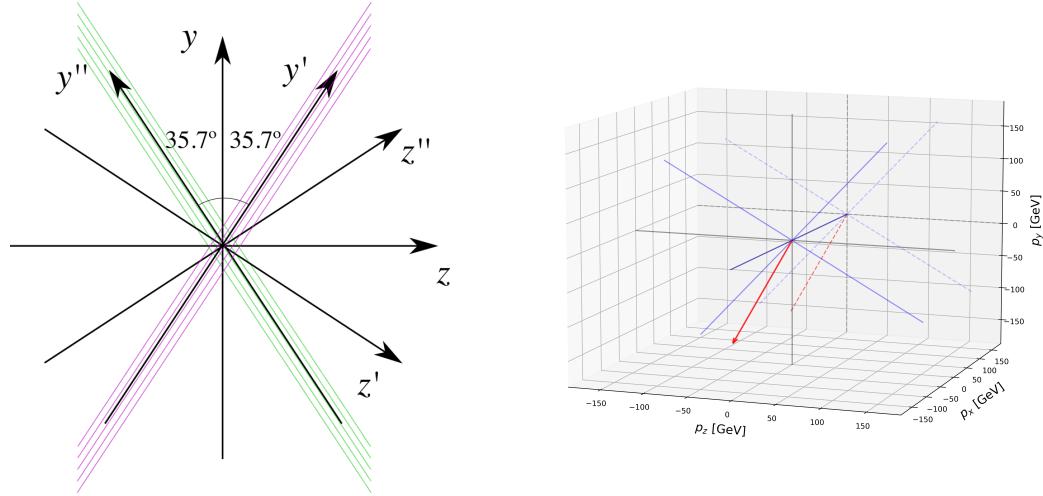
After the detector simulation stage, one needs to extract the no zero-suppressed noisy waveforms, along with their offline channel numbers, and store them in a certain format to be analysed later. To reduce the amount of data that will go for processing, I used the information from the Geant4 step of the simulation to select only the active channels, i.e. the channels where some ionisation electrons arrive. Moreover, as said previously, I only extract the waveforms from APA 0 and exclusively the ones coming from induction channels. The resulting ROOT file contains a tree with two branches, one containing the waveforms for each event and channel and the other with the corresponding offline channel numbers.

Finally, to extract the truth values for the orientation of the tracks and the energies of the particles I used a modified analysis module. This gives a ROOT file with a single tree, containing several branches with different information such as the components of the initial momentum of the particles, initial and final  $xyz$  location, track length, etc.

For the analysis of the resulting waveforms and truth values I used a custom set of Python libraries (available at [??]). Among other functionalities, these enable the user to read the ROOT files, export the raw data as pandas objects, apply the filters and compute the S/N of both the raw and filtered signals. So far, the default configuration for the filtering uses the set of optimal matched filter coefficients that I found using the ProtoDUNE data samples.

Additionally, for the analysis of the samples it was necessary to use two different reference frames, to study separately the signals coming from the U and V induction wire planes. As I am focussing on a single APA, the U and V wires have a different orientation in the  $yz$  plane. In the case of U wires, these are tilted  $35.7^\circ$  clockwise from the vertical ( $y$  direction), whereas the V wires are at the same angle but in the counter clockwise direction. Because of this, the best option is to deal with two new coordinate systems rotated by  $\pm 35.7^\circ$  along the  $x$  axis, so the new  $y'$  and  $y''$  directions are aligned with the

## CHAPTER 4. MATCHED FILTER APPROACH TO TRIGGER PRIMITIVES

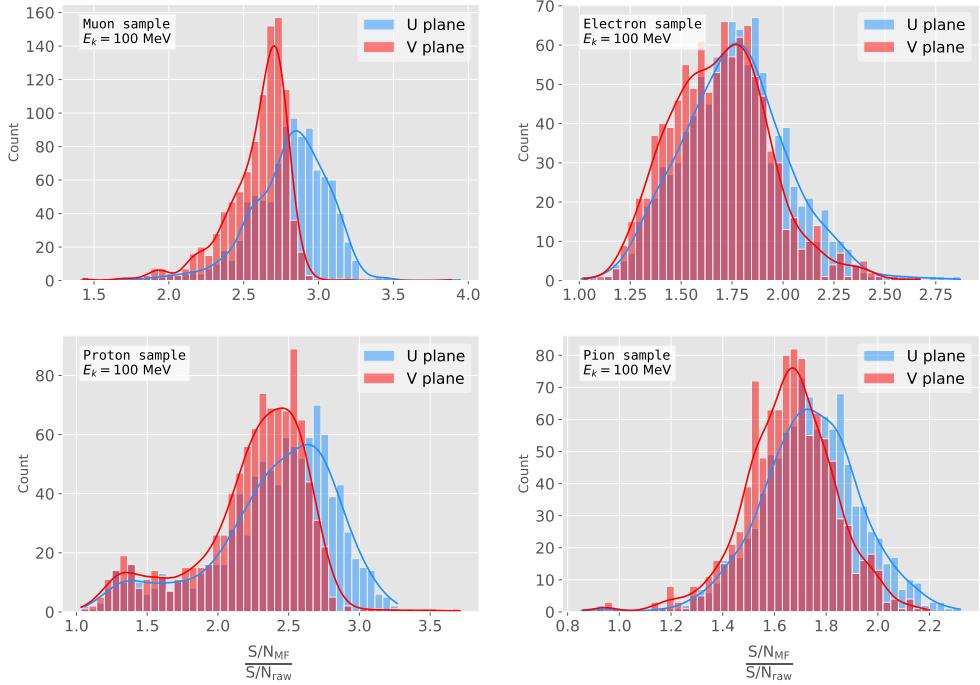


**Figure 4.11:** Left panel: schematic representation of the two new rotated reference frames used in this analysis (denoted as prime and double prime), viewed from the  $yz$  plane. The magenta stack of lines represent the wires in the  $U$  plane, whereas the green lines correspond to the wires in the  $V$  plane. Right panel: 3D representation of the momentum of one of the generated monoenergetic muons (red arrow) in the original reference frame (black lines), along with the new reference frame used for the  $U$  plane waveforms (blue lines). In the  $yz$  plane I added the projection of these three.

1749 U and V induction wires. Fig. 4.11 (left panel) shows a schematic representation of  
 1750 the original reference frame together with the two rotated ones (denoted by primed and  
 1751 double primed). This way, one can easily understand how parallel was a track to the  
 1752 wires in the two induction planes. Fig. 4.11 (right panel) shows a 3D representation of  
 1753 the momentum of a track (red arrow) in the original reference frame (black lines), along  
 1754 with the new reference frame for  $U$  wires (blue lines). I added the projection in the  $yz$   
 1755 plane of this three, to show the usefulness of the new reference frame to tell whether a  
 1756 track is parallel or normal to the wires in the induction plane.

1757 Fig. 4.12 shows the distribution of the average S/N improvement per event when one  
 1758 applies the optimal matched filters. I produced separate distributions for the channels  
 1759 in the  $U$  (red) and  $V$  (blue) induction wire planes. Notice that the S/N distributions  
 1760 for the track-like particles, i.e. muons (top left panel) and protons (bottom left panel),  
 1761 have significantly larger mean values than the distributions of the shower like particles,  
 1762 i.e. electrons (top right panel) and neutral pions (bottom right panel). An important

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**Figure 4.12:** Distributions of the mean  $S/N$  improvement per event for the corresponding sample after applying the matched filters. Here I separated the change in the U plane (blue) and the V plane (red) channels. From top left to the right: muon, electron, proton and neutral pion. All the events have a fixed kinetic energy of  $E_k = 100$  MeV.

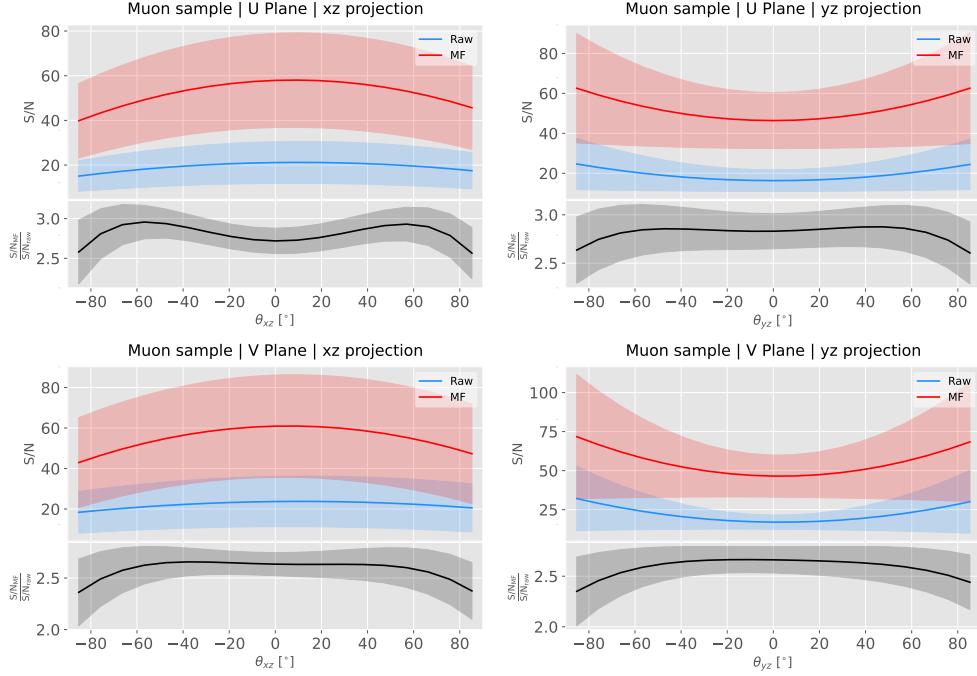
difference between these results and the ones seen before for ProtoDUNE data is that, overall, the improvements that I get for simulated data are bigger. This could be due either to the default noise model used in the *LArSoft* simulation or to the simulated hits having higher energy than the ones in the recorded data. Nonetheless, the concluding message is that the previously optimised matched filters give an overall significant improvement of the S/N for the different samples.

About the convention I followed for the plots and results, in the case of the raw and filtered S/N of each event in the sample I simply took the average of the quantities over all the active channels in the event. That is, if a certain event has  $N_{chan}$  active channels these two quantities are computed as:

$$(S/N_{fir})_{event} = \frac{\sum_{i=0}^{N_{chan}} (S/N_{fir})_i}{N_{chan}}, \quad (4.18)$$

$$(S/N_{raw})_{event} = \frac{\sum_{i=0}^{N_{chan}} (S/N_{raw})_i}{N_{chan}}.$$

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**Figure 4.13:** Angular dependence of the mean S/N and the S/N improvement, for the different monoenergetic samples considered (from top to bottom: electrons, muons, protons and neutral pions). The two columns on the left represent the values for the U plane waveforms. The top subplots show the mean S/N for raw (green) and filtered (red) waveforms whereas the bottom subplots depict the averaged S/N improvement (black).

1773 However, for the ratio of the raw and filtered S/N (what I called the S/N improvement)  
 1774 per event I am not just taking the ratio of the previous two quantities but computing  
 1775 the average of the individual ratios per channel in the event:

$$\left( \frac{S/N_{fir}}{S/N_{raw}} \right)_{event} = \frac{\sum_{i=0}^{N_{chan}} \left( \frac{S/N_{fir}}{S/N_{raw}} \right)_i}{N_{chan}}, \quad (4.19)$$

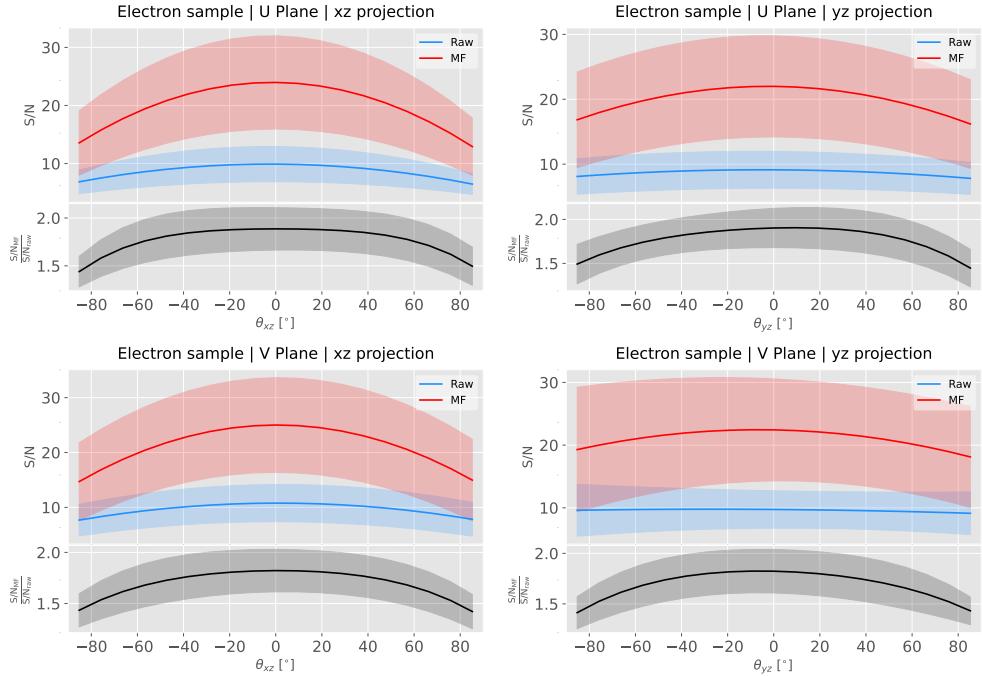
1776 and so:

$$\left( \frac{S/N_{fir}}{S/N_{raw}} \right)_{event} \neq \frac{(S/N_{fir})_{event}}{(S/N_{raw})_{event}}. \quad (4.20)$$

### 1777 4.5.1 Angular dependence

1778 Having these monoenergetic samples, one can also study the angular dependence of the  
 1779 performance of the matched filter. This is an important point, as it is a well established

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**Figure 4.14:** Angular dependence of the mean S/N and the S/N improvement, for the different monoenergetic samples considered (from top to bottom: electrons, muons, protons and neutral pions). The two columns on the left represent the values for the U plane waveforms. The top subplots show the mean S/N for raw (green) and filtered (red) waveforms whereas the bottom subplots depict the averaged S/N improvement (black).

fact that for certain configurations (an extreme case configuration being signals normal to the wire plane and perpendicular to the induction wires at the same time) the S/N is much lower than average as the corresponding waveforms are severely distorted. In this sense, I am interested to see how the matched filter behaves for these cases and how the S/N improvement on those compare to the average.

Fig. 4.13 shows the angular dependence of the S/N for the monoenergetic  $E_k = 100$  MeV isotropic muons, for the different induction wire planes and projections. The angles for each event are given by the components of the initial value of the momentum of the particles, taking the angles of the projections on the  $xz$  and  $yz$  planes with respect to the  $z$  axis (more accurately, one needs to compute these angles twice for each event, a pair for the  $xy'z'$  coordinate system and the other for the  $xy''z''$ ). The top row shows the dependence on the angles corresponding to the U plane, i.e.  $\theta_{xz'}$  and  $\theta_{y'z'}$ , whereas the bottom row shows the angular dependence viewed from the V plane,  $\theta_{xz''}$  and  $\theta_{y''z''}$ . In

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each plot, the top subplot represents the mean values of the S/N for the raw (blue) and matched filtered (red) signals, and the bottom subplot the averaged S/N improvement (black). The solid lines represent the mean value obtained for the corresponding angular value, whereas the semitransparent bands represent one standard deviation around the mean at each point.

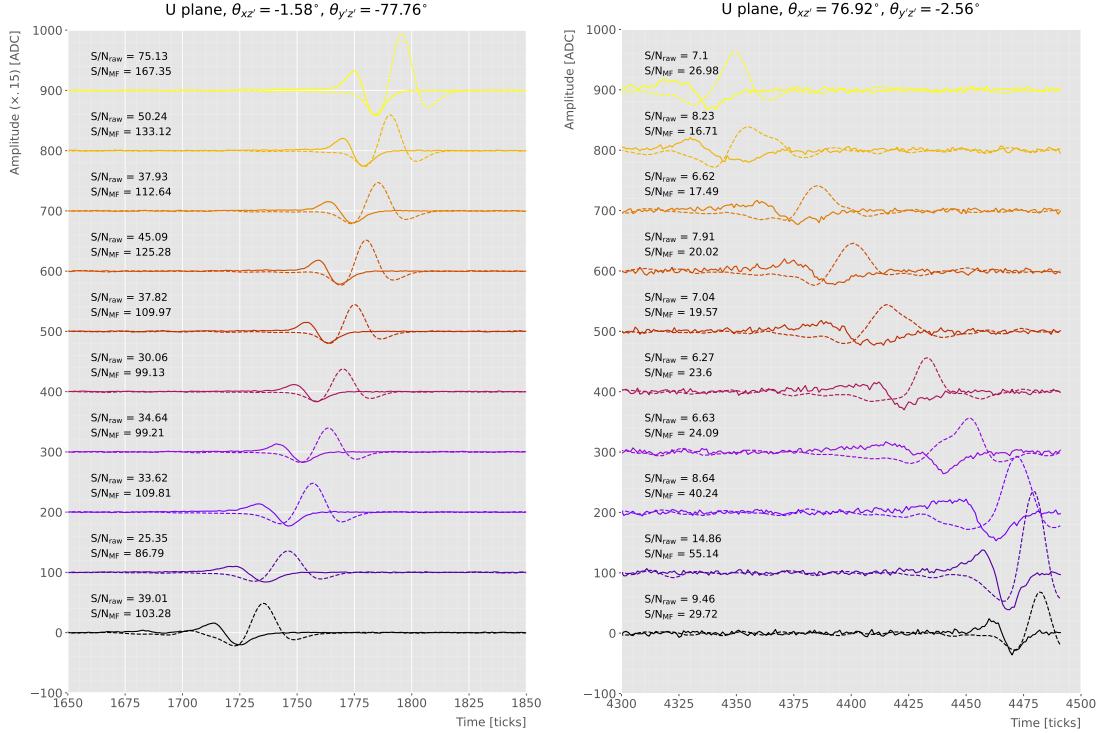
As expected, the S/N is in general higher when tracks are parallel to the APA (i.e.  $\theta_{xz} \sim 0$ ) and lower when it is normal to the plane ( $\theta_{xz} \sim \pm 90^\circ$ ). In the same way, tracks parallel to the wires ( $\theta_{yz} \sim \pm 90^\circ$ ) tend to have higher S/N than those perpendicular to these ( $\theta_{yz} \sim \pm 0$ ).

Fig. 4.14 shows the corresponding angular dependence information for the  $E_k = 100$  MeV electrons sample. Notice that, in this case, the S/N behaviour discussed above does not hold. A possible explanation can be that, because most hits in these events are produced by the secondary particles generated in the EM shower, the signal peaks whose S/N ratios were computed do not correspond to the directional information of the primary electron.

### 4.5.2 Distortion and peak asymmetry

As a little case of study, I selected two of the simulated  $E_k = 100$  MeV monoenergetic muon events. With respect to the U induction plane, one is parallel to the APA (low  $\theta_{xz'}$ ) and to the wires (high  $\theta_{y'z'}$ ) and the other is normal to the APA plane (high  $\theta_{xz'}$ ) and perpendicular to the wires (low  $\theta_{y'z'}$ ). As expected from the results on the angular dependence discussed above, the former has a higher S/N (before and after the filtering) when compared to the latter. An interesting thing to notice about these two samples is that, even though one has a much bigger S/N than the other, it is the one with the smallest S/N the one that got the biggest averaged S/N improvement. In Table 4.1 I included all the relevant parameters of these two  $E_k = 100$  MeV muon events I am considering, namely, the angles with respect to the  $xy'z'$  reference frame, the values of the S/N, the S/N improvement and also the so-called peak asymmetry  $\Delta_{peak}$  that I will discuss next.

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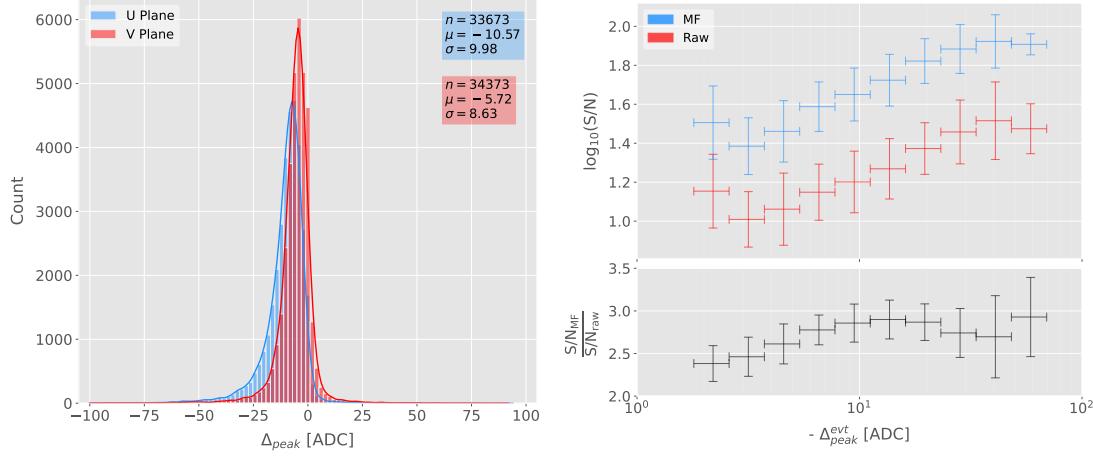
**Figure 4.15:** Selected consecutive waveforms corresponding to two monoenergetic  $E_k = 100$  MeV muon events, one is parallel to the APA and to the wires in the U plane (left panel) and the other is normal to the APA plane and perpendicular to the U plane wires (right panel). The solid lines represent the raw waveforms whereas the dashed lines correspond to the waveforms after the matched filter was applied. The waveforms on the left panel have been scaled by a factor of 0.15 to have similar amplitude to the ones on the right panel.

**Table 4.1:** Characteristic parameters of the two monoenergetic muon events selected, relative to the U plane: projected angles in the  $xz'$  and  $yz'$  planes, S/N values for the raw and filtered waveforms, mean improvement of the S/N and peak asymmetry.

	$\theta_{xz'} (\circ)$	$\theta_{yz'} (\circ)$	$S/N_{\text{raw}}$	$S/N_{\text{MF}}$	$\frac{S/N_{\text{MF}}}{S/N_{\text{raw}}}$	$\Delta_{\text{peak}} (\text{ADC})$
High ("parallel")	-1.58	-77.76	41.65	112.44	2.83	-35.73
Low ("normal")	76.92	-2.56	8.07	25.46	3.12	-10.38

1821 One can try to understand better what is going on with these two events by looking  
 1822 at the raw and filtered data from some of their active channels. Fig. 4.15 shows a  
 1823 selection of consecutive raw and filtered U plane waveforms from the event with high S/N  
 1824 (left panel) and the one with low S/N (right panel). Notice that to show both collections  
 1825 of waveforms at a similar scale I had to apply a factor of 0.15 to the waveforms with  
 1826 high S/N. Additionally, next to each waveform I included the values of the raw and

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**Figure 4.16:** Left panel: peak asymmetry distribution for the case of the monoenergetic  $E_k = 100$  MeV muon sample. Each value corresponds to a single bipolar signal peak from a channel in any event. The blue distribution represents the peaks on U plane channels, whereas the red corresponds to signal peaks in V wires. Right panel: relation between the mean peak asymmetry per event with the S/N for U channel waveforms from the  $E_k = 100$  MeV muon sample. The top subplot shows the decimal logarithm of the mean S/N for the raw (red) and the matched filtered (blue) waveforms. The bottom subplot contains the mean S/N improvement ratio after the matched filter was applied.

1827 matched filtered S/N for the corresponding channel. The first thing to notice in this plot  
 1828 is that the amplitude of the signal peaks from the normal track have a much smaller  
 1829 amplitude, and also appear quite distorted when compared to the others. On the other  
 1830 hand, although the matched filtered S/N is still smaller, the relative improvement is  
 1831 bigger than in the parallel case.

1832 A way I found to quantify the difference between the shapes within these two events  
 1833 is their different peak asymmetry. One can define the peak asymmetry as the (signed)  
 1834 difference between the positive and the negative peaks of the bipolar shape, i.e.:

$$\Delta_{peak} \equiv h_+ - h_-, \quad (4.21)$$

1835 where both heights  $h_+$  and  $h_-$  are positive defined. Fig. 4.16 (left panel) shows the  
 1836 distribution of this peak asymmetry for all the waveforms corresponding to channels  
 1837 in the U (blue) and V (red) planes for the monoenergetic muon sample. One can  
 1838 see that these distributions are clearly shifted to negative values (with mean values

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1839  $\mu_{\Delta}^U = -10.57$  ADC and  $\mu_{\Delta}^V = -5.72$  ADC respectively). It is interesting to notice  
1840 that the peak asymmetry value of the sample with high S/N sits at the left tail of the  
1841 distribution whereas the corresponding value of the sample with low S/N lies around  
1842 the mean.

1843 Now, one can try to correlate the peak asymmetry with the S/N and the S/N change  
1844 per event. Fig. 4.16 (right panel) shows the result of comparing (minus) the mean  
1845 peak asymmetry per event to the averaged raw (red) and matched filtered (blue) S/N  
1846 per event (top subplot). The horizontal lines sit at the mean value obtained in the fit  
1847 and represent the width of the  $-\Delta_{peak}$  bins used, while the vertical lines indicate one  
1848 standard deviation around that mean value. Notice that, when taking decimal logarithm  
1849 on both, there is an approximate linear relation between these quantities, except for  
1850 peak asymmetry values bigger than  $-5$  ADC where the S/N remains constant.

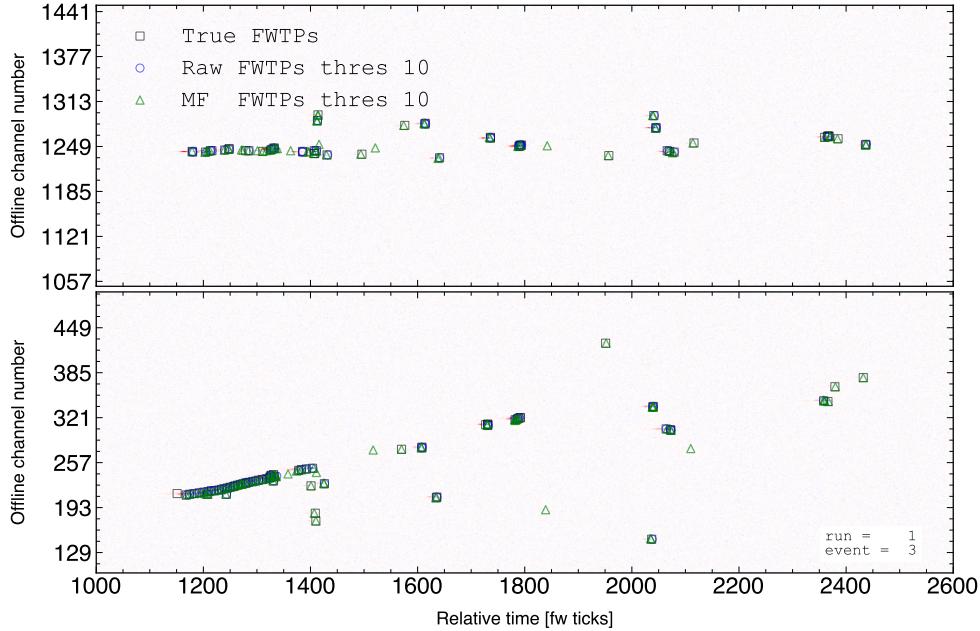
1851 Also, in the bottom subplot of Fig. 4.16 (right panel) I show the relation between  
1852 the peak asymmetry and the mean S/N improvement. In this case, one see that there is  
1853 a maximum at  $\Delta_{peak} \sim -10$  ADC. As mentioned previously, this is also the value of the  
1854 mean of the peak asymmetry distribution. In fact, it is expected that our filter favours  
1855 the signal peaks with the most common values of the peak asymmetry, as this was one  
1856 of the features I target in our filter coefficient optimisation through the parameter  $\delta$ .

1857 These results suggest that events with poorer values of the mean S/N, usually  
1858 associated to non-favourable track orientations, tend to have smaller values of the mean  
1859 peak asymmetry (in absolute value). Nonetheless, because our matched filters have  
1860 been optimised to account for these asymmetries, the improvement on the S/N for these  
1861 events is sizeable if not better than the one for events which already had a high S/N.

### 1862 4.5.3 Hit sensitivity

1863 One of the advantages of the matched filter, directly related to increasing the S/N, is  
1864 the capability of picking hits that before fell below the threshold. For instance, Fig. 4.17  
1865 shows the raw ADC data from an example event (electron,  $E_k = 100$  MeV) with the  
1866 produced true hits superimposed (black boxes), together with the hits produced by the

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**Figure 4.17:** Raw data display in the plane time (in firmware ticks) vs. offline channel number for an  $E_k = 100$  MeV electron event. The produced true hits are superimposed (black boxes) as well as the hits coming from the standard hit finder chain (blue circles) and the hit finder using the matched filter (green triangles).

standard hit finder chain (blue circles), i.e. using the current FIR filter, and the hits obtained using the matched filters (green triangles). Both the standard and the matched filter hit finders were run with a threshold of 10 ADC. Notice that the standard hits match well the true ones at the initial part of the event (where we have a track-like object), but they miss most of the hits produced by the EM shower at later times. On the other hand, the hits produced with the matched filter have a better agreement with the true hits even for the more diffuse shower activity.

Notwithstanding that now I get more hits with this combination of matched filter and low threshold as a results of the enhancement of the signal peaks relative to the noise level, it is also true that I pick some spurious hits not related to any real activity if one lowers the thresholds too much. Therefore, some optimisation of the threshold is needed. Basically one will need to make a trade-off between precision and sensitivity.

Having this in mind, I tried to compare the produced hits one gets from the standard hit finder and the ones resulting from applying the matched filter with the true hits.

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1881 By running the hit finders on our samples with different values of the threshold one  
1882 can understand, for instance, how low one can set the threshold without getting mostly  
1883 spurious hits and then evaluate the gains obtained from this.

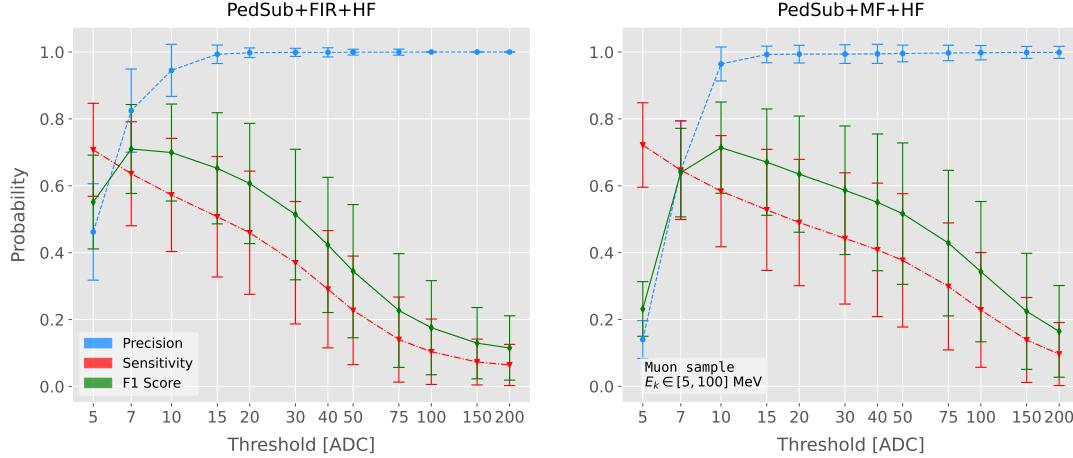
1884 Because now I am also interested in seeing how the hit sensitivity changes with the  
1885 energy, I prepared new isotropic samples with the same types of particles as before  
1886 (muons, electrons, protons and neutral pions) but with a flat kinetic energy distribution  
1887 ranging from 5 to 100 MeV.

1888 In order to estimate the hit sensitivity, given a certain sample, one needs to recover  
1889 the set of true hits to be able to compare these with the ones produced. To do so,  
1890 a modification in the procedure I was using to extract the raw waveforms is needed.  
1891 For this kind of study I run the detector simulation in two steps, first I produce the  
1892 waveforms without noise and extract them in the same format I used for the raw data,  
1893 then the noise is added and the noisy waveforms are then written to a file as well.

1894 To have a better comparison between the true hits and the ones produced from  
1895 the raw waveforms after applying the two filters, I applied also the FIR filter and the  
1896 matched filters to the noiseless waveforms and then I run the hit finder with a minimal  
1897 threshold (in this case I used 1 ADC) on these noiseless filtered waveforms. In this way  
1898 I generated two sets of true hits, I will refer to them as standard true hits (with the  
1899 current/default FIR filter) and matched filter true hits respectively. This allows a more  
1900 precise matching between the different groups of hits produced, as it will account for  
1901 any delays and distortions introduced by the FIR and the matched filters.

1902 In the case of the raw waveforms (with noise), I run the hit finder on them, with  
1903 different values of the threshold, after applying either the FIR or the matched filters. I  
1904 will name them simply standard hits and matched filter hits respectively. Then, I match  
1905 the generated hits to the true hits (the standard hits with the standard true hits and  
1906 the matched filter hits with the matched filter true hits). The matching is performed by  
1907 comparing the channel number and the timestamp of the hits. To count as a match,  
1908 I require that all hits with the same channel number and timestamp have overlapping  
1909 hit windows, i.e. the time windows between their hit end and hit start times need to

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**Figure 4.18:** Dependence of the precision (blue), sensitivity (red) and  $F_1$  (green) scores on the threshold values used in the hit finder, for the FIR (left panel) and matched filter (right panel) cases. The results were obtained after matching the hits to the true hits in the case of the isotropic muon sample with kinetic energy in the range 5 to 100 MeV, taking only into account the induction plane channels. The points represent the mean value while the error bars indicate one standard deviation around that mean value.

overlap. If more than one hit in one of the groups have hit overlap with the same hit in the other group I only count the hit with closer hit peak time value.

The generation of the samples, the procedure to produce the standard hits (with the default FIR filter) and matched filter hits and the matching of these with the true hits is described in detail in App. ??.

To quantify the performance of the two hit finder approaches, I use a classical method from statistical classification known as confusion matrix [111]. This is basically a way of sorting the outputs of a binary classifier, considering the true values of the classification and the predicted values. It divides the outputs in four categories: true positive (TP, both true and predicted values are 1), false negative (FN, true value is 1 but predicted is 0), false positive (FP, true value is 0 but predicted is 1) and true negative (TN, both true and predicted values are 0)).

The contents of the confusion matrix allow us to compute other derived scores to judge the performance of our classifiers. In this study, I will make use of three of these

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1924 metrics, namely the precision or positive predictive value:

$$\text{PPV} = \frac{\text{TP}}{\text{TP} + \text{FP}}, \quad (4.22)$$

1925 the sensitivity or true positive rate:

$$\text{TPR} = \frac{\text{TP}}{\text{TP} + \text{FN}}, \quad (4.23)$$

1926 and the  $F_1$  score [112]:

$$F_1 = \frac{2\text{TP}}{2\text{TP} + \text{FP} + \text{FN}}, \quad (4.24)$$

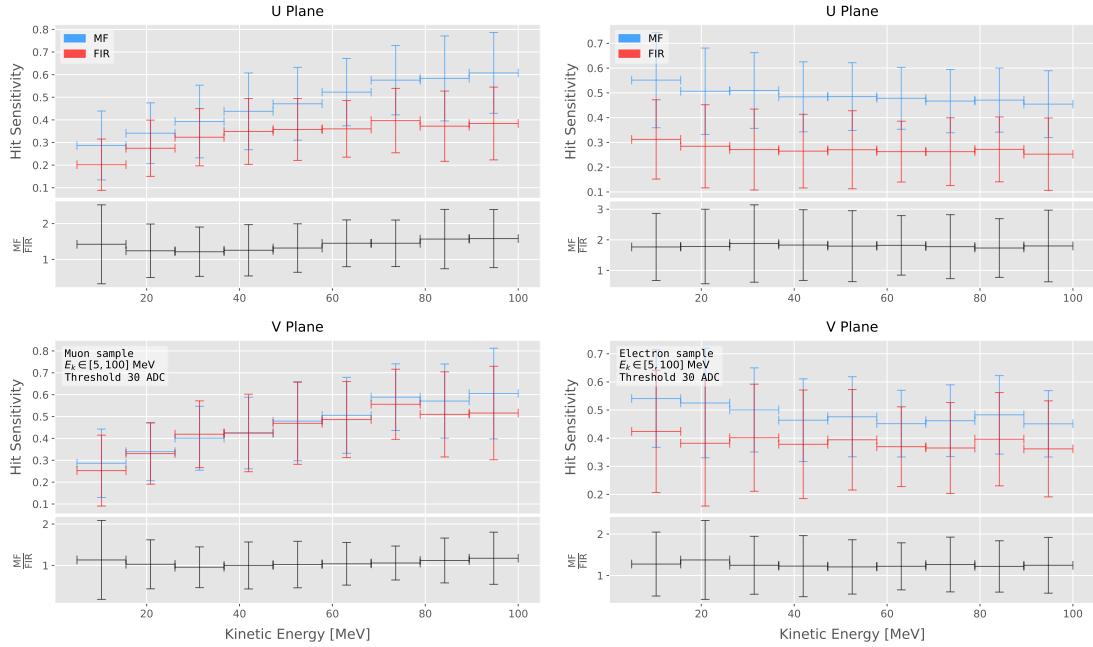
1927 which is the harmonic mean of the precision and the sensitivity.

1928 In our specific case I am not going to make use of the true negative value, as its  
1929 definition in this context can be ambiguous because one does not have clear instances in  
1930 the classification process. This way, I will only count the number of true positives as the  
1931 total amount of hits I can match between true and raw populations, the number of false  
1932 negatives will be the number of missing true hits and the false positive the number of  
1933 hits which do not match any true hit.

1934 In Fig. 4.18 I show the precision (blue), sensitivity (red) and  $F_1$  (green) scores I  
1935 obtained for different values of the threshold used in the hit finder for the case of the  
1936 muon sample. Because the matched filters are only applied to induction channels, I only  
1937 consider here hits coming from the U and V planes. The panel on the left corresponds  
1938 to the scores I got when I ran the hit finder on the FIR filtered waveforms, whereas the  
1939 right panel contains the scores for the matched filter case. The points are centered at  
1940 the threshold value used and represent the mean value obtained for each score using all  
1941 the generated events, while the error bars indicate one standard deviation around the  
1942 mean value.

1943 One can see that the precision for the matched filter case is lower when the thresholds  
1944 are very low, as the noise baseline is slightly amplified, but then rises to high values  
1945 quicker than for the FIR case. The other difference one can spot is that the sensitivity

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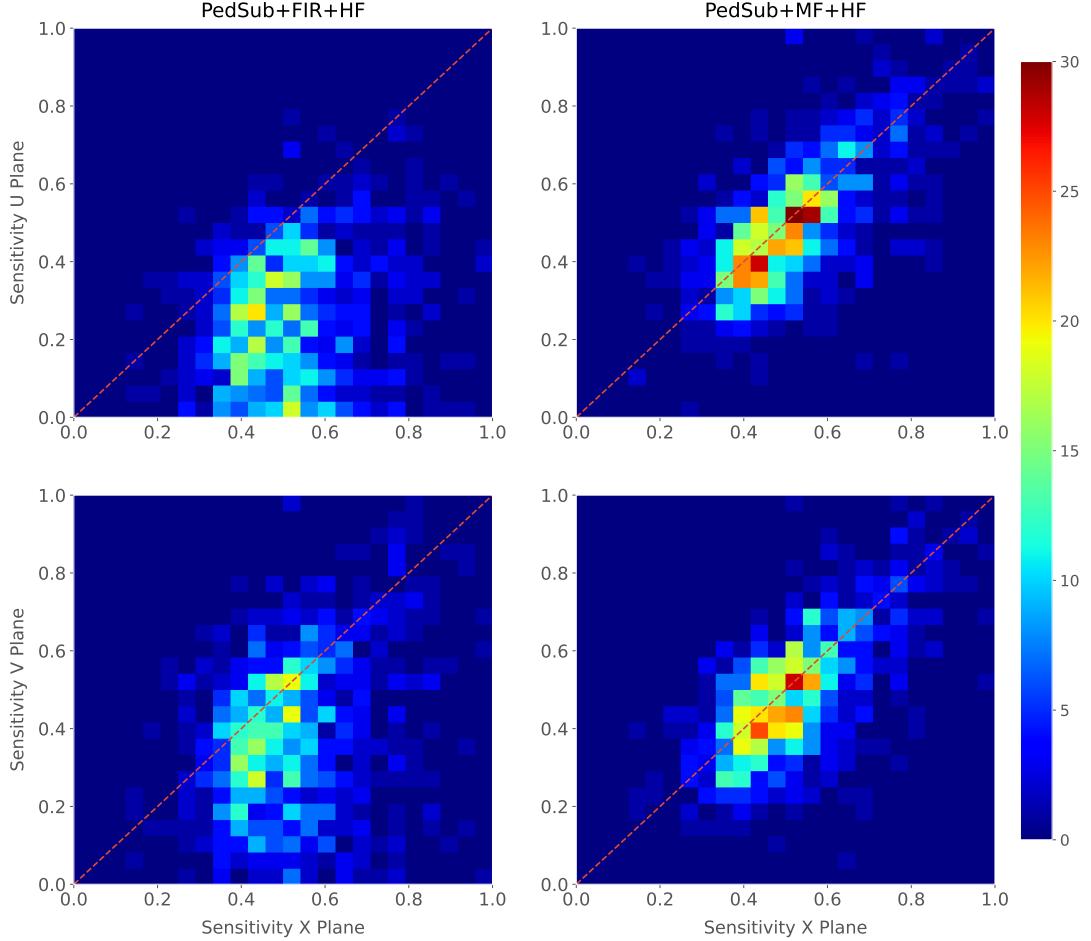


**Figure 4.19:** Dependence of the averaged hit sensitivity on the kinetic energy of the events for the matched filter (blue) and standard (red) hits, for the case of the muon (left panel) and electron (right panel) samples, separated between U (top plots) and V (bottom plots) induction wire planes. The top subplots contain the hit sensitivities for the two hit finder alternatives, while the bottom subplots show the ratio between the two. The horizontal lines sit at the mean value and represent the size of the energy bins, while the vertical error bars indicate one standard deviation around that mean value.

in the FIR case starts dropping faster at around the same threshold values where the precision stabilizes around 1, while in contrast for the matched filter this rapid decrease starts at higher threshold values. A similar scan for the same thresholds was performed for the electron sample in the same energy range, yielding similar results.

In Fig. 4.19 I show the averaged hit sensitivity versus the kinetic energy of the events, both for the matched filter hits (blue) and the standard hits (red). The left panel corresponds to the muon sample, whereas the one on the right corresponds to the electron sample, both with kinetic energies between 5 and 100 MeV. In each panel the top plot corresponds to hits in the U plane, while the bottom plot contains the same information for the V plane. Each plot contains two subplots, the one on the top shows the hit sensitivity values for the matched filter and standard hits separate, while the bottom subplot depicts the ratio between the matched filter and standard sensitivities.

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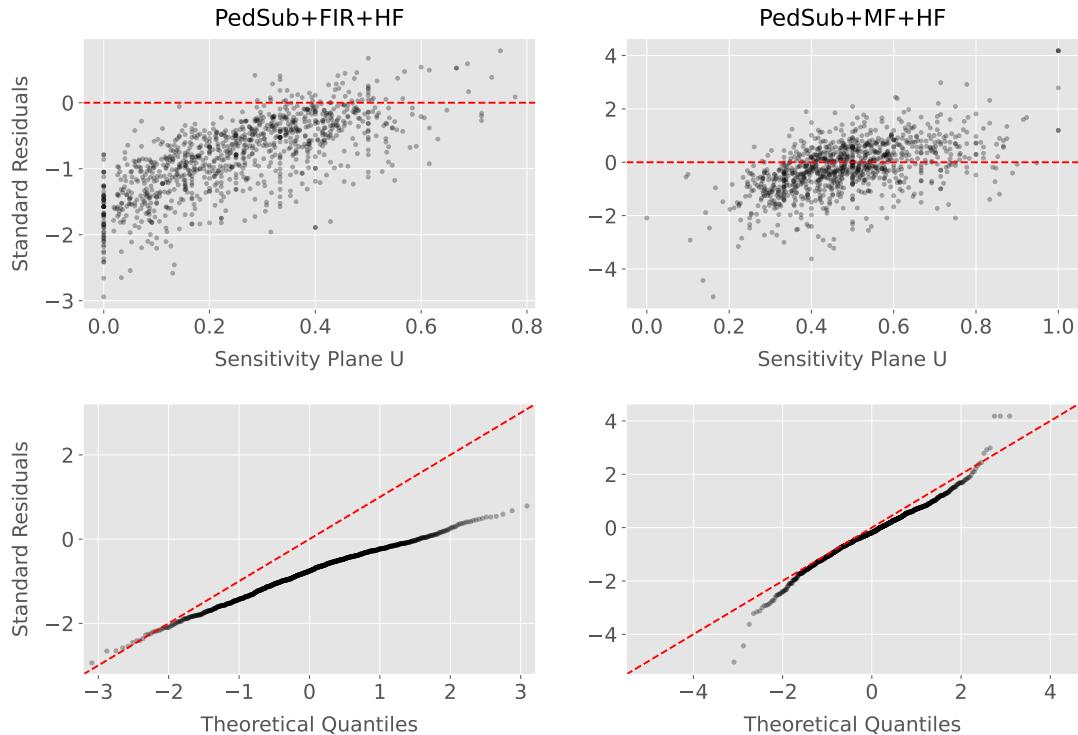


**Figure 4.20:** Distributions of the hit sensitivity in the  $U$  (top panels) and  $V$  (bottom panels) planes versus the hit sensitivity in the  $X$  plane, both for the standard hits (left panels) and the matched filter hits (right panels), in the case of the electron sample and a threshold of 30 ADC.

1958 The horizontal lines are placed at the mean value obtained in the fit and represent the  
 1959 width of the  $E_k$  bins used, while the vertical error bars indicate one standard deviation  
 1960 around that mean value. In both cases the threshold used was 30 ADC, as I required  
 1961 the precision to be higher than 0.99 for both matched filter and standard cases.

1962 One can see that, in general, the improvements are better for the  $U$  than for the  $V$   
 1963 plane. While for the  $U$  channels I achieved a mean improvement of 50% and 80% for  
 1964 muons and electrons respectively, the improvement in the  $V$  plane is stalled at 10% and  
 1965 25%. Nevertheless, if I look at the sensitivities for the matched filter hits in both planes  
 1966 one can see these have similar mean values for each energy bin, while on the contrary

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**Figure 4.21:** Top panels: standard residual plots of the hit sensitivities between the  $X$  and  $U$  planes. Bottom panels: quantile-quantile plots of the hit sensitivity standard residuals between the  $X$  and  $U$  planes. In all cases, the left panel corresponds to the standard hits while the right panel represents the matched filter case, all from the electron sample with a 30 ADC threshold.

for the standard hits the sensitivity remains relatively high for the  $V$  plane. This way, it looks there was a less significant gain because the hit sensitivity was already high.

Another interesting observation is the different behaviors for muons and electrons. While hit sensitivity for muons grows significantly with energy, in the case of electrons this slightly decreases the higher the kinetic energy of the event is. In any case, when it comes to the improvement on the sensitivities, this remains almost constant in all cases.

Furthermore, we can look at how the concurrence of hits between the different wire planes has changed. For any given event, I expect to have a similar number of hits in the three planes. As the ionisation electrons need to cross the  $U$  and  $V$  planes prior to reach the collection plane  $X$  they will induce current in those wire planes. A way to check the concurrence of hits across planes is looking at the relation between the hit sensitivities for each individual event. One cannot expect the sensitivities to be exactly equal across

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1979 planes, but ideally they should be normally distributed around the diagonal.

1980 Fig. 4.20 shows the hit sensitivity in the U (top panels) and V (bottom panels)  
1981 planes versus the hit sensitivity in the X plane, for the case of the standard hits (left  
1982 panels) and the matched filter hits (right panels). All plots were generated for the  
1983 electron sample and a threshold of 30 ADC. From these one can see a clear trend,  
1984 when I use the standard hit finder chain the sensitivities in the induction planes are  
1985 systematically lower than the hit sensitivity in the X plane, i.e. most of the points sit  
1986 below the diagonal (red dashed line). In contrast, when the matched filters are applied,  
1987 the majority of the events are distributed around the diagonal. This points out that the  
1988 concurrence of hits across planes has improved.

1989 To exemplify the improvement I obtained, one can consider the residuals of the hit  
1990 sensitivities for the X and U planes. Assuming the diagonal hypothesis, i.e. given a  
1991 dataset of the form  $(x, y)$  for any  $x$  I take the predicted  $y$  value to be equal to the value  
1992 of  $x$ , I can compute the standard residuals for the hit sensitivities in U given the ones for  
1993 X. In Fig. 4.21 (top panels) I show these standard residuals against the corresponding  
1994 values of the hit sensitivity in the U plane, for our electron sample with kinetic energy  
1995 between 5 and 100 MeV. If I compare the scatter points in the case of the standard  
1996 hits (left panel) and the matched filter hits (right panel), I see that the residuals of the  
1997 standard hit finder case follow a certain pattern and their mean deviates from 0.

1998 To see clearly if the residuals are normally distributed, in Fig. 4.21 (bottom panels)  
1999 I plot the corresponding quantile-quantile plot for both the standard (left panel) and  
2000 matched filter (right panel) standard residuals. One can clearly see that the points for  
2001 the standard case follow a strongly non-linear pattern, suggesting that the residuals  
2002 do not follow a normal distribution. In contrast, for the matched filter hits the points  
2003 conform to a roughly linear path, implying that in this case the normality condition is  
2004 fulfilled.

2005 All these results hint at the fact that the concurrence of hits across the wire planes  
2006 can be strengthened by applying the matched filters.



## 2008 DM searches with neutrinos from the Sun

2009 The idea of detecting neutrino signals coming from the Sun's core to probe DM is not  
2010 new. The main focus of these searches has usually been high-energy neutrinos originated  
2011 from DM annihilations into heavy particles [113–116], although recent studies have  
2012 proposed to look at the low-energy neutrino flux arising from the decay of light mesons  
2013 at rest in the Sun [117–120] previously thought undetectable.

2014 In this Chapter I try to demonstrate the capability of DUNE to constrain different  
2015 DM scenarios. I used the neutrino fluxes arising from DM annihilations in the core  
2016 of the Sun to compute the projected limits that DUNE would be able to set on the  
2017 annihilation rates in the Sun and the DM scattering cross sections.

### 2018 5.1 Gravitational capture of DM by the Sun

2019 The Sun and the centre of the Earth are possible sources of DM annihilations, specially  
2020 interesting because of their proximity. Their gravitational attraction ensured the capture  
2021 of DM from the local halo through repeated scatterings of DM particles crossing them.  
2022 Only neutrinos produced from DM annihilations can escape the dense interior of these  
2023 objects. Therefore, neutrino telescopes are the most useful experimental layouts to  
2024 pursue DM searches from their cores.

2025 The neutrino flux from DM annihilations inside the Sun depends on the DM capture  
2026 rate, which is proportional to the DM scattering cross section, and the annihilation rate,  
2027 which is proportional to the velocity-averaged DM annihilation cross-section. The total

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2028 number of DM particles inside the Sun follows the Boltzmann equation [117]:

$$\frac{dN_{DM}}{dt} = C_{\odot} - A_{\odot} N_{DM}^2, \quad (5.1)$$

2029 where  $C_{\odot}$  and  $A_{\odot}$  are the total Sun DM capture and annihilation rates respectively.  
 2030 In this expression I neglected the evaporation term, proportional to  $N_{DM}$ , which only  
 2031 contribute for  $m_{DM} \lesssim 4$  GeV [121]. As the current threshold of neutrino telescopes  
 2032 is a few GeV, this region falls below the probed range but can be important in future  
 2033 low-energy projects.

2034 This equation has an equilibrium solution:

$$N_{DM}^{eq} = \sqrt{\frac{C_{\odot}}{A_{\odot}}}, \quad (5.2)$$

2035 which represents the amount of DM inside the Sun if the capture and annihilation have  
 2036 reached equilibrium. As the Sun is approximately 4.6 Gyr old, it is usually assumed that  
 2037 equilibrium has been achieved. Therefore, the anomalous neutrino flux from the Sun  
 2038 would only depend on the DM scattering cross section, enabling us to set limits on this  
 2039 quantity. If one does not assume equilibrium, some assumptions on the DM annihilation  
 2040 cross section are necessary to extract predictions from neutrino signals.

2041 Here, I am going to consider three possible scenarios for the DM interactions: DM  
 2042 scattering off electrons, spin-dependent (SD) and spin-independent interactions off nuclei.  
 2043 For the case of these last two, the cross sections will be given in terms of the SD and  
 2044 SI elastic scattering DM cross section off protons (assuming that DM interactions off  
 2045 protons and neutrons are identical),  $\sigma_p^{\text{SD}}$  and  $\sigma_p^{\text{SI}}$ , as [2, 117]:

$$\sigma_i^{\text{SD}} = \left( \frac{\tilde{\mu}_{A_i}}{\tilde{\mu}_p} \right)^2 \frac{4(J_i + 1)}{3J_i} |\langle S_{p,i} \rangle + \langle S_{n,i} \rangle|^2 \sigma_p^{\text{SD}}, \quad (5.3)$$

$$\sigma_i^{\text{SI}} = \left( \frac{\tilde{\mu}_{A_i}}{\tilde{\mu}_p} \right)^2 A_i^2 \sigma_p^{\text{SI}}, \quad (5.4)$$

2046 where  $\tilde{\mu}_{A_i}$  is the reduced mass of the DM-nucleus  $i$  system,  $\tilde{\mu}_p$  is the reduced mass of

## 5.1. GRAVITATIONAL CAPTURE OF DM BY THE SUN

2047 the DM-proton system,  $A_i$  and  $J_i$  the mass number and total angular momentum of  
 2048 nucleus  $i$  and  $\langle S_{p,i} \rangle$  and  $\langle S_{n,i} \rangle$  the expectation value of the spins of protons and neutrons  
 2049 averaged over all nucleons, respectively (see Ref. [122] for a review on spin expectation  
 2050 values).

2051 Since the Sun is mainly composed of Hydrogen, the capture of DM from the halo  
 2052 is expected to occur mainly through spin-dependent scattering. However, since the  
 2053 spin-independent cross section is proportional to the square of the atomic mass, heavy  
 2054 elements can contribute to the capture rate (even though they constitute less than 2%  
 2055 of the mass of the Sun). Heavy elements can also contribute to the spin-dependent cross  
 2056 section if the DM has also momentum-dependent interactions.

2057 DM particles can get captured by the Sun if after repeated scatterings off solar  
 2058 targets their final velocity is lower than the escape velocity of the Sun. In the limit of  
 2059 weak cross sections, this capture rate can be approximately written as [2]:

$$C_{\odot}^{\text{weak}} = \sum_i \int_0^{R_{\odot}} dr 4\pi r^2 \int_0^{\infty} du_{\chi} \frac{\rho_{\chi}}{m_{\chi}} \frac{f_{v_{\odot}}(u_{\chi})}{u_{\chi}} \omega(r) \int_0^{v_e(r)} dv R_i^-(\omega \rightarrow v) |F_i(q)|^2, \quad (5.5)$$

2060 where the summation extends over all possible nuclear targets. In this expression,  $R_{\odot}$   
 2061 is the radius of the Sun,  $\rho_{\chi}$  is the local DM density,  $m_{\chi}$  the mass of the DM particle,  
 2062  $f_{v_{\odot}}(u_{\chi})$  the DM velocity distribution seen from the Sun's reference frame,  $R_i^-(\omega \rightarrow v)$   
 2063 is the differential rate at which a DM particle with velocity  $v$  scatters a solar target of  
 2064 mass  $m_i$  to end up with a velocity  $\omega$  and  $|F_i(q)|$  is the nuclear form factor of target  $i$ .

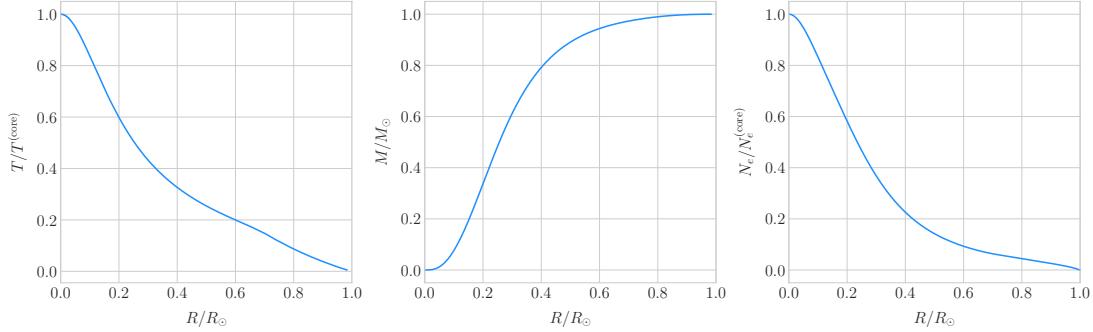
2065 The differential scattering rate takes a rather simple form when considering velocity-  
 2066 independent and isotropic cross sections. In that case, this quantity is given by [2, 123]:

$$R_i^-(\omega \rightarrow v) = \frac{2}{\sqrt{\pi}} \frac{\mu_{i,+}^2}{\mu_i} \frac{v}{\omega} n_i(r) \sigma_i \left[ \chi(-\alpha_-, \alpha_+) + \chi(-\beta_-, \beta_+) e^{\mu_i(\omega^2 - v^2)/u_i^2(r)} \right], \quad (5.6)$$

2067 where  $\mu_i$  is the ratio between the DM mass and the mass of target  $i$ ,  $\mu_{i,\pm}$  is defined as:

$$\mu_{i,\pm} \equiv \frac{\mu_i \pm 1}{2}, \quad (5.7)$$

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**Figure 5.1:** Input solar parameters used in our capture rate computation as functions of the Sun's radius, from left to right: temperature (with respect to the temperature at the core), mass (in solar masses) and electron number density (with respect to the electron density at the core). All quantities shown correspond to the standard solar model BS2005-OP [1].

2068  $n_i(r)$  is the density profile of target  $i$  in the solar medium,  $u_i(r)$  is the most probable  
2069 velocity of target  $i$  given by:

$$u_i(r) = \sqrt{\frac{2T_\odot(r)}{m_i}}, \quad (5.8)$$

2070 where  $T_\odot(r)$  is the temperature of the Sun, the quantities  $\alpha_\pm$  and  $\beta_\pm$  are defined as:

$$\alpha_\pm \equiv \frac{\mu_{i,+}v \pm \mu_{i,-}\omega}{u_i(r)}, \quad (5.9)$$

$$\beta_\pm \equiv \frac{\mu_{i,-}v \pm \mu_{i,+}\omega}{u_i(r)}, \quad (5.10)$$

2071 and the function  $\chi(a, b)$  is a Gaussian integral of the form:

$$\chi(a, b) \equiv \int_a^b dx e^{-x^2}. \quad (5.11)$$

2072 Finally, if one assumes the DM halo velocity distribution in the galactic rest frame  
2073 to be a Maxwell-Boltzmann distribution, one can write the halo velocity distribution for  
2074 an observer moving at the speed of the Sun with respect to the DM rest frame as:

$$f_{v_\odot}(u_\chi) = \sqrt{\frac{3}{2\pi}} \frac{u_\chi}{v_\odot v_d} \left( e^{-\frac{3(u_\chi - v_\odot)^2}{2v_d^2}} - e^{-\frac{3(u_\chi + v_\odot)^2}{2v_d^2}} \right), \quad (5.12)$$

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2075 where:

$$\omega^2 = u_\chi + v_e(r)^2, \quad (5.13)$$

2076 is the DM velocity squared,  $v_\odot$  the relative velocity of the Sun from the DM rest frame  
 2077 and  $v_d \simeq \sqrt{3/2}v_\odot$  the velocity dispersion.

2078 For the case of strong scattering cross section, Eq. (5.5) ceases to be valid, as it  
 2079 escalates indefinitely with the cross section. In that limit, the capture rate saturates to  
 2080 the case where the probability of interaction is equal to one, which can be written as:

$$C_\odot^{\text{geom}} = \pi R_\odot^2 \left( \frac{\rho_\chi}{m_\chi} \right) \langle v \rangle \left( 1 + \frac{3}{2} \frac{v_e^2(R_\odot)}{v_d^2} \right) \xi(v_\odot, v_d), \quad (5.14)$$

2081 where  $v_d = \sqrt{8/3\pi}v_d$  is the mean velocity in the DM rest frame and the factor  $\xi(v_\odot, v_d)$   
 2082 accounts for the suppression due to the motion of the Sun:

$$\xi(v_\odot, v_d) = \frac{v_d^2 e^{-\frac{3v_\odot^2}{2v_d^2}} + \sqrt{\frac{\pi}{6}} \frac{v_d}{v_\odot} (v_d^2 + 3v_e^2(R_\odot) + 3v_\odot^2) \operatorname{Erf} \left( \sqrt{\frac{3}{2}} \frac{v_\odot}{v_d} \right)}{2v_d^2 + 3v_e^2(R_\odot)}. \quad (5.15)$$

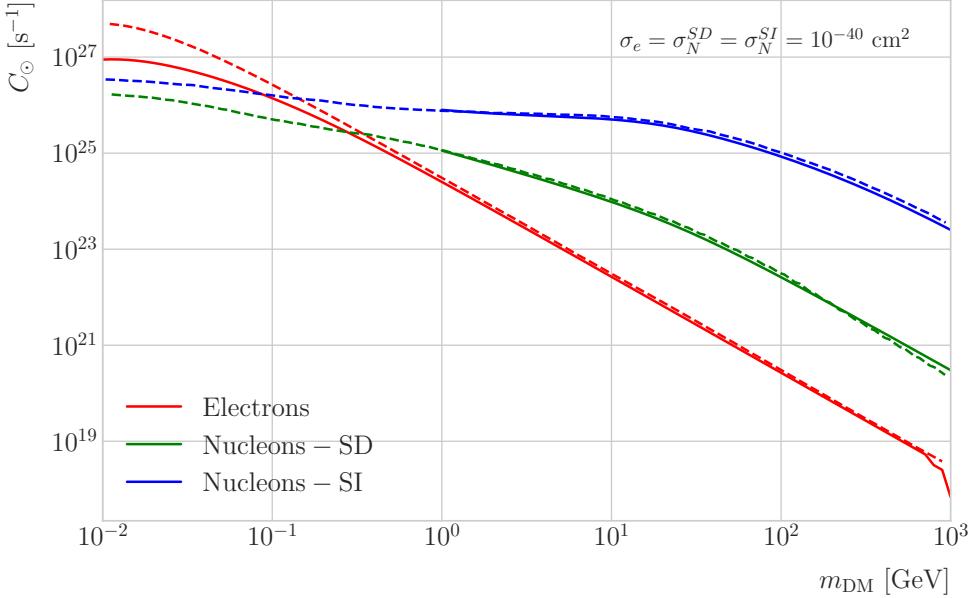
2083 Having these into account, one can write the total capture rate as a combination of  
 2084 both contributions, allowing a smooth transition between the two, as:

$$C_\odot = C_\odot^{\text{weak}} \left( 1 - e^{C_\odot^{\text{geom}} / C_\odot^{\text{weak}}} \right). \quad (5.16)$$

2085 I computed the capture rate from Eq. (5.16) in the case of interactions with  
 2086 electrons. To do so, I used the standard solar model BS2005-OP [1]. Fig. 5.1 shows the  
 2087 three parameters from the solar model that are needed for the computation, the solar  
 2088 temperature (left panel), mass (central panel) and electron density (right panel) profiles.

2089 For the case of the interactions off nuclei, the computations are more convoluted  
 2090 as one needs to add up the contributions of the different most abundant nuclei in  
 2091 the Sun. Also, in contrast to the electron scenario where the form factor is trivially  
 2092  $|F_e(q)|^2 = 1$ , for any nucleus  $i$  one would need to consider some appropriate nuclear  
 2093 density distribution (either a Gaussian approximation, a Woods-Saxon distribution, etc)

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**Figure 5.2:** Capture rates as a function of the DM mass for the DM-electron interactions (red lines), SD DM-nucleons interactions (green lines) and SI DM-nucleons interactions (blue lines). Solid lines represent the values computed in this work while the dashed lines are the one given in Ref. [2]. All the rates are shown for a choice of scattering cross section of  $\sigma_i = 10^{-40} \text{ cm}^2$ .

which would complicate the calculations even further.

That is the reason why, at this stage of our study, I decided to take an alternative approach to the computation of the DM-nucleus capture rates. I used the **DarkSUSY** software, that allows us to compute these quantities performing a full numerical integration over the momentum transfer of the form factors. The default standard solar model used by **DarkSUSY** is BP2000<sup>1</sup> [124].

In Fig. 5.2 I show the results I obtained for the capture rates, for the case of interactions off electrons (red solid line), SD (green solid line) and SI (blue solid line) interactions of nucleons. In all cases I used a value of the scattering cross sections of  $\sigma_i = 10^{-40} \text{ cm}^2$ . Note here one of the limitations of the **DarkSUSY** approach, one can not extend the computation below  $m_{\text{DM}} = 1 \text{ GeV}$ . Nevertheless, this is not something to worry about in this case, as I will discuss next. As a comparison, I added also the

<sup>1</sup>This is what they say in their manual, but I fear it is somewhat outdated. It appears to me this model is relatively old and do not see why they are not using others like [1]. Maybe one can double-check in the code to make sure.

## 5.1. GRAVITATIONAL CAPTURE OF DM BY THE SUN

values computed in Ref. [2] (same color scheme, dashed lines). One can see there is good agreement between these and the **DarkSUSY** computation of the SD and SI interactions for  $m_{\text{DM}} \geq 1$  GeV. In this regime their computations also matches quite well our result for the electron capture rate. However, these start to differ significantly below  $m_{\text{DM}} = 1$  GeV, being their estimate up to a factor of 5 bigger than ours for low masses.

Let us comment briefly about the assumption I made before about not including an evaporation term in the Boltzmann equation. If I include this term in the equation (which will be proportional to the number of DM particles) the equilibrium solution takes the form:

$$N_{\text{DM}}^{\text{eq}} = \sqrt{\frac{C_{\odot}}{A_{\odot}}} \frac{1}{\kappa + \frac{1}{2} E_{\odot} \tau_{\text{eq}}}, \quad (5.17)$$

where  $E_{\odot}$  is the total evaporation rate,  $\tau_{\text{eq}}$  is the equilibrium time in the absence of evaporation:

$$\tau_{\text{eq}} = \frac{1}{\sqrt{C_{\odot} A_{\odot}}}, \quad (5.18)$$

and  $\kappa$  is defined as:

$$\kappa \equiv \sqrt{1 + \left( \frac{E_{\odot} \tau_{\text{eq}}}{2} \right)^2}. \quad (5.19)$$

Now, it is easy to proof that in case evaporation dominates  $\kappa \gg 1$  and therefore:

$$N_{\text{DM}}^{\text{eq}} \simeq \frac{C_{\odot}}{E_{\odot}}. \quad (5.20)$$

In contrast, if evaporation is irrelevant  $\kappa \simeq 1$  and one recovers Eq. (5.2).

In this way, one can define the evaporation mass as the mass for which the number of DM particles in equilibrium approaches Eq. (5.20) at 10% level:

$$\left| N_{\text{DM}}^{\text{eq}}(m_{\text{evap}}) - \frac{C_{\odot}(m_{\text{evap}})}{E_{\odot}(m_{\text{evap}})} \right| = 0.1 N_{\text{DM}}^{\text{eq}}(m_{\text{evap}}). \quad (5.21)$$

This can be regarded as the minimum testable mass one can reach using the annihilation products of the DM in the Sun.

It was reported in Ref. [2] that, in the case of both SD and SI DM interactions

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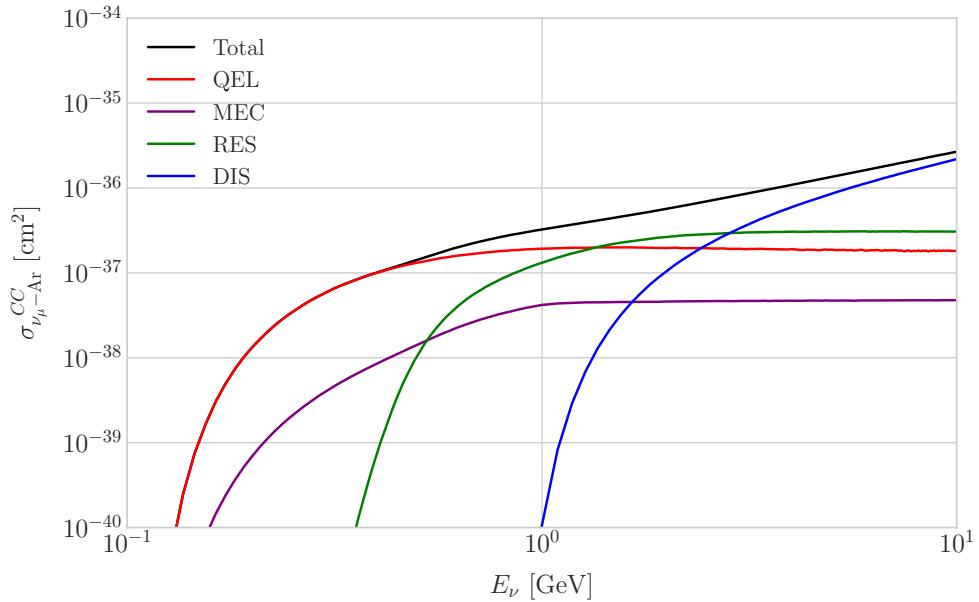
off nuclei, this value ranges from 2 to 4 GeV depending on the specific scattering cross section value, compatible with the usual assumptions in the literature. What is interesting is the case of the electron capture. It was found that, when one applies a cutoff in the velocity distribution of the DM trapped in the Sun slightly below the escape velocity, the evaporation mass for the DM-electron interaction decreases remarkably. For a moderate choice of  $v_c(r) = 0.9v_e(r)$  one gets an evaporation mass of around 200 to 600 MeV. This possibility opens a region of the parameter space that could be tested with neutrino detectors.

## 5.2 Neutrino flux from DM annihilations

When WIMPs annihilate inside the Sun a flux of high-energy neutrinos is expected from heavy quarks, gauge bosons and  $\tau^+\tau^-$  final states, which decay before losing energy in the dense solar medium, as they will produce a continuum spectra up to  $E_\nu \sim m_\chi$  (in the case of direct annihilation to neutrinos one would have a line at  $E_\nu = m_\chi$ ) [118]. This kind of signal has been extensively studied in the literature, allowing to put strong limits on the SD WIMP-proton cross section for large  $m_\chi$ . However, the number of high-energy neutrinos per WIMP annihilation is small and the spectrum depends on the unknown final state. Moreover, background rejection is easier for large  $m_\chi$  but neutrinos with  $E_\nu \gtrsim 100$  GeV are significantly attenuated by interactions in the Sun.

Nevertheless, most WIMP annihilation final states eventually produce a low-energy neutrino spectrum. In this case one does not just consider the more massive final states but also annihilations into  $e^+e^-$ ,  $\mu^+\mu^-$  and light quarks [117]. In particular, light mesons would be produced and stopped in the dense medium, thus decaying at rest and producing a monoenergetic neutrino signal. The decay-at-rest of kaons will produce a  $E_\nu = 236$  MeV  $\nu_\mu$  while in the case of pions one would have a  $E_\nu = 29.8$  MeV  $\nu_\mu$ . In practice only  $K^+$  and  $\pi^+$  contribute to these signals, as  $K^-$  and  $\pi^-$  are usually Coulomb-captured in an atomic orbit and get absorbed by the nucleus. There is also a low-energy neutrino signal coming from muon decays, which are produced in kaon or

### 5.3. COMPUTING LIMITS FROM SOLAR NEUTRINO FLUXES



**Figure 5.3:** *NuWro* computed  $\nu_\mu - {}^{40}\text{Ar}$  charged-current scattering cross section as a function of the neutrino energy  $E_\mu$ . The black line shows to the total cross section, whereas the others correspond to the different contributions (in red quasi-elastic scattering, in green resonant pion exchange, in blue deep inelastic scattering and in purple meson exchange current).

2152 pion decays, leptonic decays of other hadrons and heavy leptons or even directly from  
 2153 WIMP annihilations, which can decay at rest and contribute to the previous low-energy  
 2154 neutrino flux with a well known spectrum below 52.8 MeV.

2155 These monoenergetic MeV neutrinos were previously considered undetectable but,  
 2156 due to the large yield, the known spectra and the modern advances in the detector  
 2157 technology, these low-energy neutrino flux can be a good probe of the SD WIMP-proton  
 2158 cross-section in standard solar WIMP capture scenario, as it is sensitive to low WIMP  
 2159 masses and insensitive to the particular final state. A good place to look for these signals  
 2160 are next-generation neutrino experiments such as DUNE.

### 2161 5.3 Computing limits from solar neutrino fluxes

2162 In order to use the neutrino fluxes from DM annihilations in the Sun, the first thing I  
 2163 need to do is to determine the expected number of atmospheric background events, for

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2164 a given exposure, after directionality selection has been applied. I can write this number

2165 as:

$$N_B = \eta_B \int d\Omega \int_{E_{min}}^{E_{max}} dE_\nu \frac{d^2\Phi_{atm}^\mu}{dE_\nu d\Omega} \times \left( A_{eff}^{(\mu)}(E_\nu) T \right), \quad (5.22)$$

2166 where  $\eta_B$  is the background efficiency,  $E_{min}$  and  $E_{max}$  the minimum and maximum

2167 energies to integrate over,  $d^2\Phi_{atm}^\mu/dE_\nu d\Omega$  the differential flux of atmospheric muon

2168 neutrinos,  $A_{eff}^{(\mu)}$  is the effective area of DUNE to muon neutrinos and  $T$  is the exposure

2169 time. The effective area can be expressed as the product of the neutrino-nucleus scattering

2170 cross section and the number of nuclei in the fiducial volume of the detector. This way

2171 for DUNE I can write:

$$A_{eff}^{(\mu)}(E_\nu) = (6.0 \times 10^{-10} \text{ m}^2) \left( \frac{\sigma_{\nu-\text{Ar}}^{(\mu)}(E_\nu)}{10^{-38} \text{ cm}^2} \right) \left( \frac{M_{target}}{40 \text{ kT}} \right), \quad (5.23)$$

2172 where  $\sigma_{\nu-\text{Ar}}^{(\mu)}$  is the  $\nu_\mu - {}^{40}\text{Ar}$  charged-current scattering cross section. In Fig. 5.3 I

2173 show the computed value of this cross section as a function of the neutrino energy  $E_\nu$ ,

2174 in the range of interest both for the atmospheric background and signal events. It was

2175 computed using the NuWro Monte Carlo neutrino event generator [125], including the

2176 charged-current contributions of the quasi-elastic scattering (red line), resonant pion

2177 exchange (green line), deep inelastic scattering (blue line) and meson exchange current

2178 (purple line).

2179 The background rejection will depend on the resolution of the detector and the

2180 selection one applies on the events. A geometry argument can be used to estimate

2181 the maximum background rejection one can achieve in this case, considering one can

2182 efficiently discriminate all events coming from a direction different from that of the

2183 Sun. In that case, the optimal background efficiency will simply be the relative angular

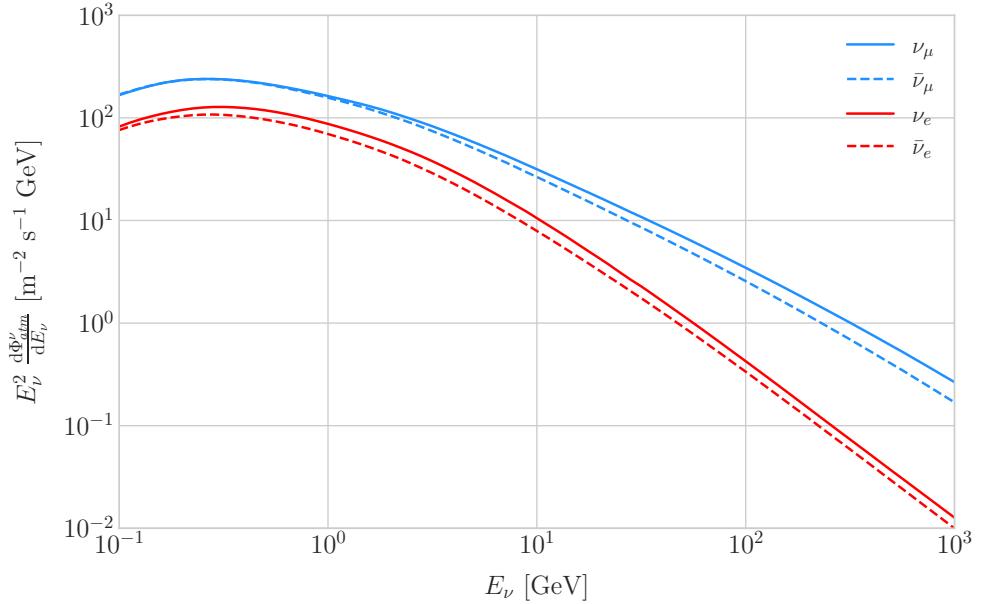
2184 coverage of the Sun. Taking the angular diameter of the Sun as seen from the Earth to

2185 be  $0.5^\circ$ , I have:

$$\eta_B^{(opt)} \approx \frac{\pi \left( \frac{0.5}{2} \right)^2}{360 \times 180} \simeq 3.03 \times 10^{-6}. \quad (5.24)$$

2186 This value will give a very optimistic estimate of the number of background events.

### 5.3. COMPUTING LIMITS FROM SOLAR NEUTRINO FLUXES



**Figure 5.4:** Expected atmospheric neutrino flux as a function of the neutrino energy  $E_\nu$  at Homestake at solar minimum, taken from Ref. [3]. The blue solid (dashed) line correspond to muon neutrinos (antineutrinos) and the red solid (dashed) line correspond to electron neutrinos (antineutrinos).

2187 However, it can be regarded as an lower limit, as it represents the best case scenario.

2188 In Fig. 5.4 I show the fluxes of atmospheric neutrinos at the Homestake mine during  
 2189 solar minimum, taken from Ref. [3]. The values are averaged over the two angular  
 2190 directions. In blue I have the flux of muon neutrinos while in red I indicate the flux  
 2191 of electron neutrinos. Additionally, the dashed lines correspond to both antineutrino  
 2192 species.

2193 Using these values for the muon neutrino and the corresponding total CC cross  
 2194 section, one can compute the number of expected background events by integrating over  
 2195 the given energy range (as in this case the angular integral is trivial). As for the energy  
 2196 range to integrate over, I choose the range for DUNE specified in [85],  $E_{min} = 10^{-1}$  GeV  
 2197 and  $E_{max} = 10$  GeV. Taking all these into account, I found the number of background  
 2198 events to be:

$$N_B \simeq \eta_B \times (3.827 \times 10^4) \times \left( \frac{\text{exposure}}{400 \text{ kT yr}} \right). \quad (5.25)$$

2199 In order to estimate the sensitivity of DUNE to this kind signal, one can consider a

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2200 hypothetical data set where the number of observed neutrinos is taken to be the expected  
 2201 number of background events rounded to the nearest integer,  $N_{obs} = \text{round}(N_B)$  [126].  
 2202 Now, if I assume that the number of signal and background events seen by DUNE are  
 2203 given by Poisson distributions with means equal to the expected number of signal and  
 2204 background events,  $N_S$  and  $N_B$ , one can denote by  $N_S^{90}$  to the number of expected  
 2205 signal events such that the probability of having an experimental run with a number of  
 2206 events greater than  $N_{obs}$  is 90%. This number can be obtained as the numerical solution  
 2207 to the equation:

$$1 - \frac{\Gamma(N_{obs} + 1, N_S^{90} + N_B)}{N_{obs}!} = 0.9, \quad (5.26)$$

2208 where  $\Gamma(x, y)$  is the upper incomplete gamma function.

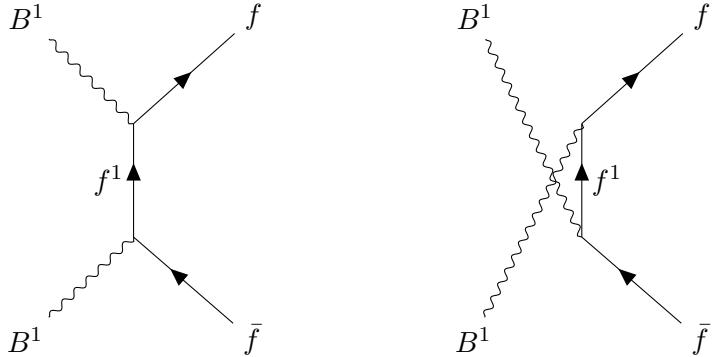
2209 The number of signal events is related to the neutrino flux from DM annihilations in  
 2210 a similar way as the background events to the atmospheric neutrino flux. In this case I  
 2211 have:

$$N_S = \eta_S \Gamma_A^{eq} \int_{z_{min}}^{z_{max}} dz \frac{dN_\nu}{dAdN_A dz} \times \left( A_{eff}^\mu(z) T \right), \quad (5.27)$$

2212 where  $\eta_S$  is the signal efficiency,  $\Gamma_A^{eq}$  is the total annihilation rate of DM particles at  
 2213 equilibrium,  $\Gamma_A^{eq} = A_\odot (N_{DM}^{eq})^2$ ,  $z_{min}$  and  $z_{max}$  the minimum and maximum relative  
 2214 energies to integrate over (in such a way that  $z_{min,max} \leq E_{min,max}/m_{DM}$  for each  $m_{DM}$ )  
 2215 and  $dN_\nu/dAdN_A dz$  the muon neutrino flux per DM annihilation in the Sun.

2216 Knowing  $N_S^{90}$  one can use the relation in Eq. (5.27) to obtain  $\Gamma_A^{eq,90}$  for different  
 2217 values of the DM mass. From there I can directly translate those values into the  
 2218 upper limits for DUNE on the DM scattering cross sections, for a given exposure. The  
 2219 relation between the annihilation rate and the DM-nucleon cross section comes from the  
 2220 equilibrium condition through the solar DM capture rate. The details of the evolution  
 2221 of the number of DM particles inside the Sun and the computation of the capture rates  
 2222 are discussed in App. 5.1.

## 5.4. EXAMPLE: KALUZA-KLEIN DARK MATTER



**Figure 5.5:** Feynman diagrams for  $B^1 B^1$  annihilation into SM fermions.

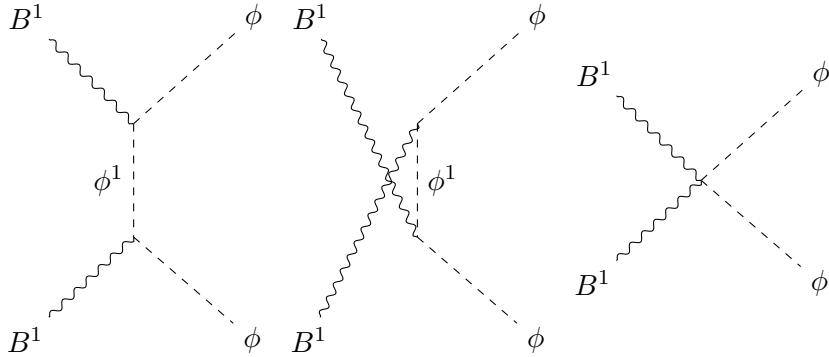
### **2223 5.4 Example: Kaluza-Klein Dark Matter**

2224 Even though there are plenty of BSM theories which provide viable dark matter  
 2225 candidates, Kaluza-Klein type of models [127, 128] within the universal extra dimensions  
 2226 (UED) paradigm naturally predict the existence of a massive, stable particle that can  
 2227 play the role of the dark matter. In the UED scenario all the SM fields can propagate  
 2228 in one or more compact extra dimensions [129], as opposed to the idea of brane worlds  
 2229 [130, 131], where just gravity can propagate in the bulk while SM particles live at fixed  
 2230 points.

2231 Furthermore, in UED there is no violation of the translational invariance along the  
 2232 extra dimensions, thus leading to degenerate KK modes masses and also the conservation  
 2233 of the KK number in the effective four dimensional theory. At loop level, radiative  
 2234 corrections and boundary terms shift the masses of the KK modes and break KK  
 2235 number conservation into a KK parity. As a result, this theory only contains interactions  
 2236 between an even number of odd KK modes and therefore the lightest among the first KK  
 2237 excitations will be stable. This particle is usually denoted as the lightest Kaluza-Klein  
 2238 particle (LKP) and its mass is proportional to  $1/R$ , being  $R$  the size of the extra  
 2239 dimension.

2240 A viable DM candidate needs to be electrically neutral and non-baryonic, therefore  
 2241 good candidates among the first Kaluza-Klein excitations would be the KK neutral

## CHAPTER 5. DM SEARCHES WITH NEUTRINOS FROM THE SUN



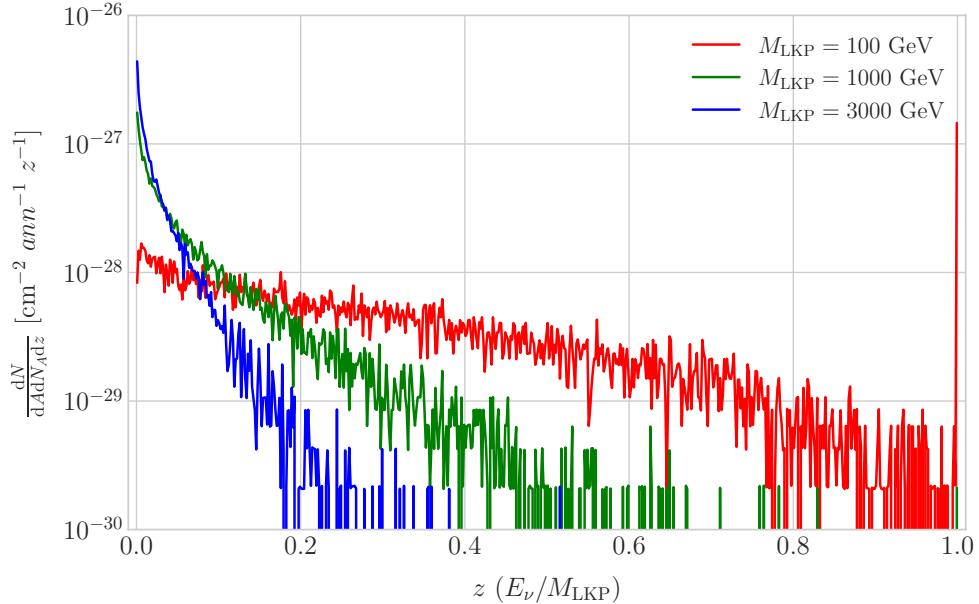
**Figure 5.6:** Feynman diagrams for  $B^1B^1$  annihilation into a Higgs boson pair.

gauge bosons and the KK neutrinos [132]. Another possible candidate is the first KK excitation of the graviton, which receives negligible radiative contributions and therefore has a mass almost equal to  $1/R$ , but it has been shown that the lightest eigenstate from the mixing of the gauge mass states  $(B^1, W_3^1)$  would be lighter, as  $B^1$  and  $W_3^1$  receive negative radiative corrections [133]. It is also understood that, when these corrections become sizeable, the eigenstates become approximately pure  $B^1$  and  $W_3^1$  states as the Weinberg mixing angle grows small with the KK number [133]. In that case, the LKP can be well-approximated as being entirely  $B^1$ .

I need to compute the neutrino flux produced by the annihilations of the LKP in the core of the Sun, taking into account their propagation in the solar medium, as well as neutrino oscillations. To this end I used `WimpSim` [134, 135] to generate one million annihilation events in the Sun over a time span of four years and propagate them to the DUNE FD location ( $44^\circ 20' \text{ N}, 103^\circ 45' \text{ W}$ ), for different values of  $M_{\text{LKP}}$ . In Fig. 5.7 I show the obtained muon neutrino spectra arriving to the detector from LKP annihilations in the Sun, per unit area and per annihilation, plotted in relative energy units for different values of the mass. As one could expect the spectra get steeper the higher is the mass, due to the absorption of high-energy neutrinos in the solar medium. Also, one can see the peak at  $z = 1$  due to the direct annihilation into neutrinos  $\chi\chi \rightarrow \nu\bar{\nu}$ .

Now, one can estimate the sensitivity of DUNE to this particular model by using

#### 5.4. EXAMPLE: KALUZA-KLEIN DARK MATTER



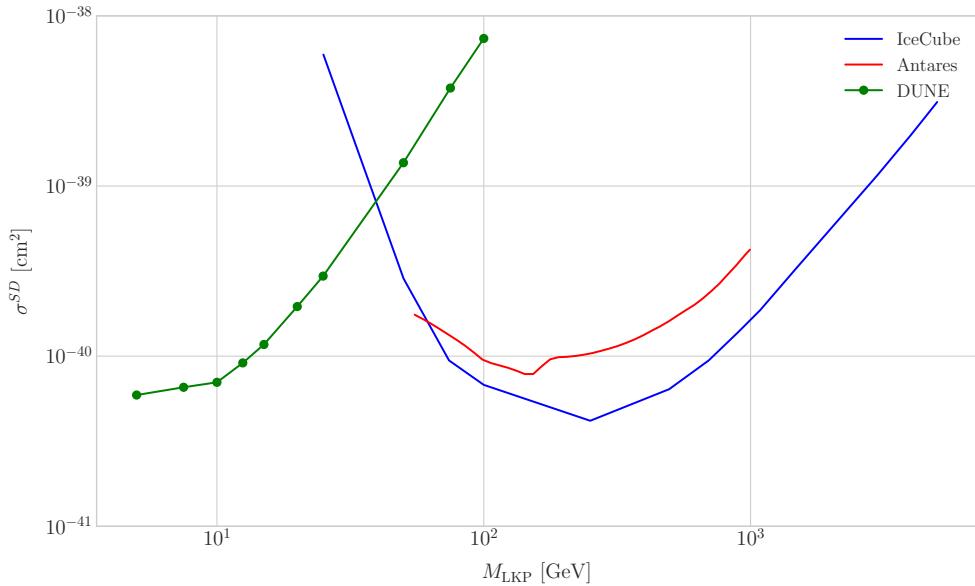
**Figure 5.7:** Computed spectra of muon neutrinos at the DUNE FD site from  $B^1$  annihilations in the Sun for three different values of  $M_{\text{LKP}}$ , plotted in relative energy units for legibility.

the methods I previously discussed. To begin with, I will use the optimistic estimation  
 of the background efficiency in Eq. (5.24) to get our upper bound. Using it, one can  
 directly compute the number of expected background events to be  $N_B = 0.1101$  for an  
 exposure of 400 kT yr. Then, Eq. (5.26) give us a value of  $N_S^{90} = 2.20$  for the 90%  
 exclusion number of expected signal events. By using the NuWro generated cross sections  
 and the computed neutrino fluxes from  $B^1$  annihilations in the Sun I can estimate the  
 limits on the SD and SI DM-nucleus cross section using the relation in Eq. (5.2) and  
 the capture rates I computed with DarkSUSY.

In Fig. 5.8 I show the projected sensitive for DUNE on the spin-dependent  $B^1$ -proton  
 scattering cross section versus the mass of the DM particle, for a exposure of 400 kT yr  
 (green dots). I also include the previous results from IceCube [4] (blue line) and Antares  
 [5] (red line). The shaded area represents the disfavoured region from combined searches  
 for UED by ATLAS and CMS [6].

From the experimental point of view, this estimation lacked a detailed simulation of  
 the detector response and thus this must be consider as a mere optimistic sensitivity

## CHAPTER 5. DM SEARCHES WITH NEUTRINOS FROM THE SUN



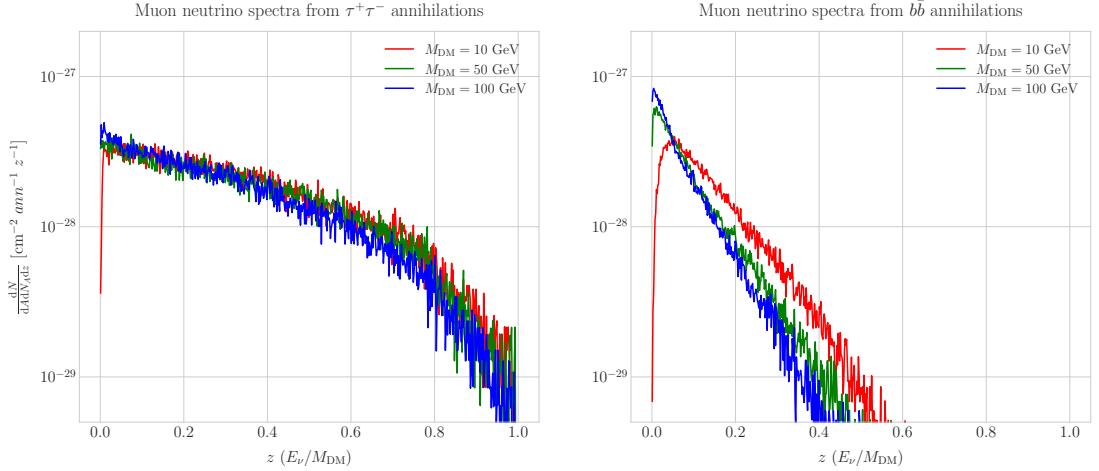
**Figure 5.8:** Projected 90% confidence level upper limit for DUNE (400 kT yr) on the spin-dependent  $B^1$ -proton scattering cross section as a function of  $M_{LKP}$  (green dots). I also show the previous limits from IceCube [4] (blue line) and Antares [5] (red line) on the LKP cross section. The shaded area represents the disfavoured region (at 95% confidence level) on the mass of the LKP from LHC data [6].

computation. However, it shows the potential of DUNE to constrain this kind of exotic scenarios, showing the region where it will be in a position to compete with other neutrino telescopes. A more detailed analysis is needed if I am to make a realistic estimation. Even though the region of the parameter space where DUNE would be sensitive to this particular model is quite constrained by collider searches [6] and other rare decay measurements [136, 137], it still constitutes an alternative indirect probe.

## 5.5 High energy DM neutrino signals

To have better estimates on the capability of the DUNE FD to constrain the parameter space of DM using solar neutrino fluxes, I need to start accounting for the detector resolution effects and the topologies of the different signatures. As a starting point, I will focus on specific annihilation channels. For the case of DUNE, the relevant ones are mainly the hard channels  $\tau^+\tau^-$  and  $\nu\bar{\nu}$  and the soft channel  $b\bar{b}$ . These are the open annihilation channels for relatively low mass WIMPs that will actually give neutrino

## 5.5. HIGH ENERGY DM NEUTRINO SIGNALS



**Figure 5.9:** Computed spectra of muon neutrinos at the DUNE FD site from  $\tau^+\tau^-$  (left panel) and  $b\bar{b}$  (right panel) annihilations in the Sun for the DM masses  $m_{\text{DM}} = 10 \text{ GeV}$  (red line),  $50 \text{ GeV}$  (green line) and  $100 \text{ GeV}$  (blue line), plotted in relative energy units.

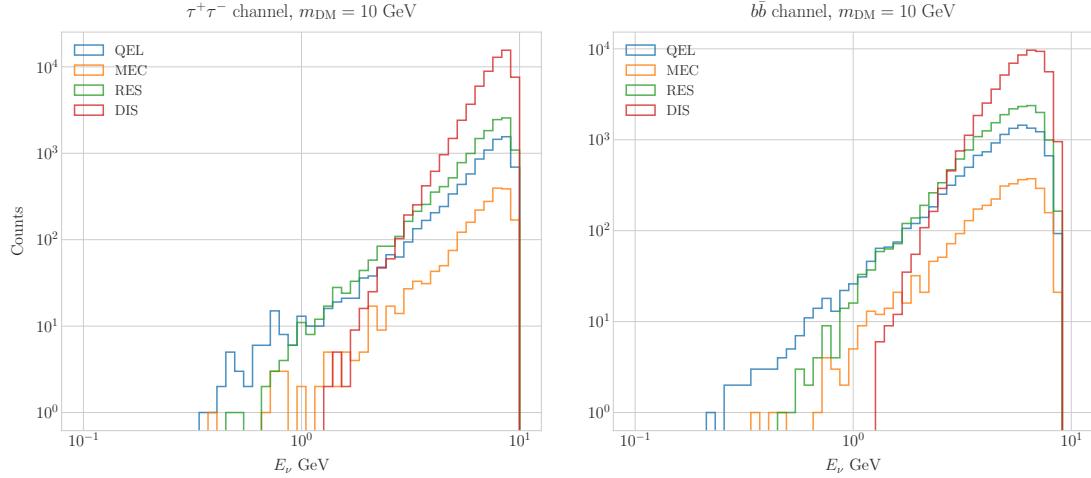
2290 fluxes. Other channels, like  $W^+W^-$  and  $ZZ$ , are open for more massive WIMPs, but  
 2291 those will produce usually a higher energy neutrino flux that will be out of reach for  
 2292 DUNE (usually the maximum neutrino energy is taken to be  $E_{\max} = 10 \text{ GeV}$ ).

2293 In Fig. 5.9 I show the `WimpSim` [134, 135] generated muon neutrino spectra at the  
 2294 DUNE FD location ( $44^\circ 20' \text{ N}, 103^\circ 45' \text{ W}$ ) from  $\tau^+\tau^-$  (left panel) and  $b\bar{b}$  (right panel)  
 2295 annihilations in the core of the Sun, for different DM masses. Here, one can clearly see  
 2296 the meaning of the previous distinction between hard and soft channels. For the same  
 2297 DM mass value, the muon neutrino spectrum from the  $\tau^+\tau^-$  channel is more flat and  
 2298 reaches higher energies than the one from the  $b\bar{b}$  channel, which drops faster.

2299 In this case, I prepared two sets of files, one for  $\tau^+\tau^-$  and the other for  $b\bar{b}$ , for DM  
 2300 masses in the range from 5 to 100 GeV (actually for  $b\bar{b}$  the first mass point I took is  
 2301 7.5 GeV, as a WIMP with  $m_{\text{DM}} = 5 \text{ GeV}$  can not kinematically self annihilate into  $b\bar{b}$ ).  
 2302 Then, I prepared the `WimpSim` output fluxes in a specific way to use them as inputs to  
 2303 `NuWro`, which simulates the neutrino interaction with the argon.

2304 Because `WimpSim` outputs an event list together with the fluxes, I can use the former  
 2305 to generate the events. The direction of these is given in terms of the azimuth and  
 2306 altitude angles viewed from the specified location, so first I need to convert these into the

## CHAPTER 5. DM SEARCHES WITH NEUTRINOS FROM THE SUN



**Figure 5.10:** Distribution of the muon neutrino energies from the  $\tau^+\tau^-$  (left panel) and  $b\bar{b}$  (right panel) annihilation channels, for  $m_{\text{DM}} = 10$  GeV, separated by CC interaction type: QEL (blue), MEC (orange), RES (green) and DIS (red).

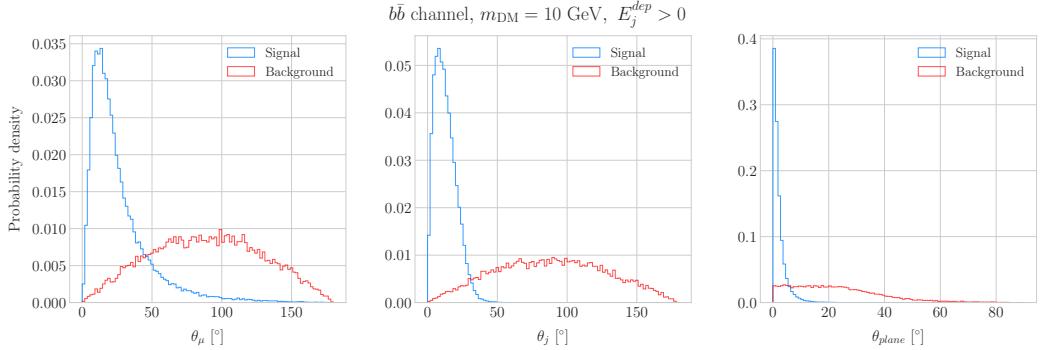
2307 DUNE FD coordinates. Once I have done it, each event can be processed with `NuWro`.  
 2308 To increase the number of samples and optimise the computation time, I generate 100  
 2309 interactions (i.e. `NuWro` events) for each `WimpSim` event<sup>2</sup>. I restrict the event generation  
 2310 to charged current interactions, but I allow all the different contributions to the CC  
 2311 cross section, i.e. quasielastic scattering (QEL), meson exchange current process (MEC),  
 2312 resonant pion production (RES) and deep inelastic scattering (DIS). I just take into  
 2313 account the CC contribution because I am only interested in final states with charged  
 2314 leptons, as we have better chances of reconstructing the kinematics of CC events.

2315 For the atmospheric fluxes I follow a similar procedure, only that this time I do not  
 2316 have a set of events but the fluxes binned in azimuth and altitude angles. This way, I  
 2317 transform these to DUNE coordinates and process the fluxes for each bin separated with  
 2318 `NuWro`.

2319 At this point, I have two sets of events with different energies and final states.  
 2320 In Fig. 5.10 one can see the distribution of the muon neutrino energies for the case  
 2321  $m_{\text{DM}} = 10$  GeV, both for the  $\tau^+\tau^-$  (left panel) and  $b\bar{b}$  (right panel) channels, separated

<sup>2</sup>This also solves a problem related with the generation of the neutrino interactions in `NuWro`, as if you only produce one event each time you launch `NuWro` it will always produce an interaction of the dominant interaction type for that particular energy.

## 5.5. HIGH ENERGY DM NEUTRINO SIGNALS



**Figure 5.11:** Distributions of  $\theta_\mu$  (left panel),  $\theta_j$  (central panel) and  $\theta_{\text{plane}}$  (right panel) for the  $b\bar{b}$  sample with  $m_{\text{DM}} = 10$  GeV (blue) and the atmospheric background (red).

by interaction. One can clearly see that there are different energy regimes where the primary interaction type is different. This leads to a plurality of event topologies, therefore making it difficult to implement a general approach to the selection of events in detriment of the background. As a way to proceed, I decided to split our samples, based on the different interaction modes and contents of the final state, into a CC DIS sample and a single proton CC QEL sample.

### 5.5.1 DIS events

To begin with, I consider the high energy part of the spectrum. In this region DIS events dominate, i.e. interactions of the form  $\nu_\mu + q_d(\bar{q}_u) \rightarrow \mu^- + q_u(\bar{q}_d)$ . Therefore, our final states will contain a muon and a hadronic jet from the fragmentation of the outgoing quark. As all these events have  $E_\nu \gtrsim 1$  GeV the momentum transfer to the remnant nucleus is negligible, for this reason the neutrino energy can be effectively reconstructed just taking into account the momenta of the muon and the jet. This technique was successfully used in Ref. [138] to select monoenergetic DM solar neutrino events from  $\nu\bar{\nu}$  annihilation channels.

Using momentum conservation one sees that the plane generated by the momenta of the muon and the jet needs to also contain the momentum of the neutrino. As we are interested in neutrinos coming from the Sun, the momentum of the neutrino can be regarded as known beforehand. This will allow us to define the angle of the outgoing

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2341 muon and jet with respect to the incoming neutrino. Moreover, one can also use that  
 2342 information to reject poorly reconstructed jets, checking for deviations of these from the  
 2343 momentum conservation plane.

2344 To account for the limited angular resolution of the detector, I smeared the momenta  
 2345 of the muons and hadrons. In a liquid argon TPC muons are expected to be tracked with  
 2346 high precision, therefore I take the associated angular resolution to be  $1^\circ$ . In the case of  
 2347 jets, it is expected that for the hadrons dominating the cascade a detector like DUNE  
 2348 has an angular resolution between  $1^\circ$  to  $5^\circ$  [85], so I take the latter, more conservative,  
 2349 estimate.

2350 As a first selection step, I will just take into account particles with kinetic energies  
 2351 above the detection threshold of DUNE. For muons and photons the specified threshold  
 2352 energy is 30 MeV, for charged pions 100 MeV and for other hadrons 50 MeV [85]. This  
 2353 way, if the outgoing muon in a certain event has an energy lower than the required  
 2354 threshold I will drop such event. For the case of hadrons and photons, I will only require  
 2355 to have at least one particle above the energy threshold, so then one can compute the  
 2356 jet momentum using the (smeared) momenta of the  $N$  particles above threshold as:

$$\vec{p}_j = \sum_{i=1}^N \vec{p}_i. \quad (5.28)$$

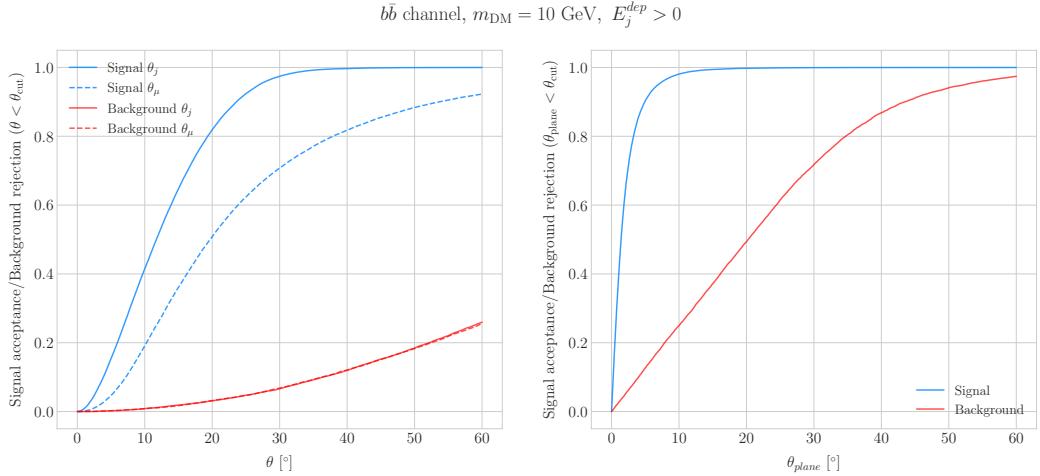
2357 Additionally, I will also define an estimation of the deposited hadronic energy as:

$$E_j^{dep} = m_{^{39}\text{Ar}} - m_{^{40}\text{Ar}} + \sum_{i=1}^N \sqrt{|\vec{p}_i|^2 + m_i^2}. \quad (5.29)$$

2358 This quantity is useful to select events with enough hadronic visible energy in the  
 2359 detector. For events where most of the hadronic energy is scattered across plenty of  
 2360 hadrons with individual energies below the detection threshold, this estimation will  
 2361 give  $E_j^{dep} \leq 0$ . In these cases it could be expected that the jet momentum is poorly  
 2362 reconstructed, and therefore I require events to pass the cut  $E_j^{dep} > 0$ .

2363 For the events I can compute the angles for the muon and jet with respect to the

## 5.5. HIGH ENERGY DM NEUTRINO SIGNALS



**Figure 5.12:** Left panel: signal efficiencies (blue lines) and background rejections (red lines) for events passing the cuts  $\theta < \theta_{cut}$  for the jet (solid lines) and muon (dashed lines) angles. Right panel: signal efficiency (blue line) and background rejection (red line) for events passing the cut  $\theta_{plane} < \theta_{cut}$  for the momentum conservation plane deviation.

2364 incoming neutrino as:

$$\cos \theta_\mu = \hat{p}_\nu \cdot \hat{p}_\mu, \quad (5.30)$$

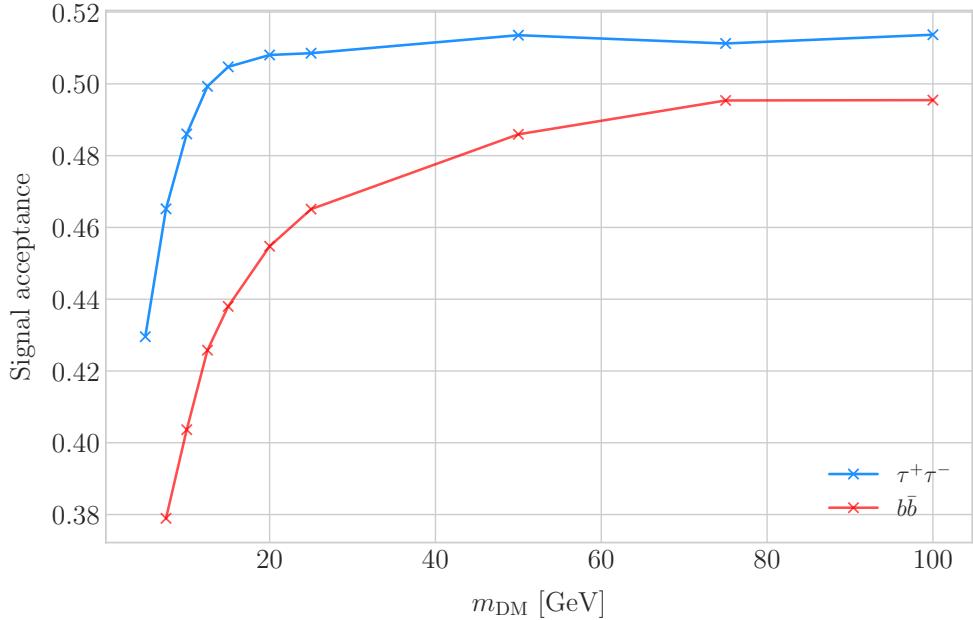
$$\cos \theta_j = \hat{p}_\nu \cdot \hat{p}_j, \quad (5.31)$$

2365 and the deviation from the momentum conservation plane as:

$$\sin \theta_{plane} = \left| \frac{\hat{p}_\mu \times \hat{p}_\nu}{|\hat{p}_\mu \times \hat{p}_\nu|} \cdot \hat{p}_j \right|. \quad (5.32)$$

2366 In Fig. 5.11 I show some distributions of these quantities for the case of the  $b\bar{b}$  sample  
 2367 with  $m_{DM} = 10$  GeV (blue histograms) and for the atmospheric backgrounds (red).  
 2368 In order to select the atmospheric events I followed the same criteria as for the signal  
 2369 events. However, because in the signal case I used the true direction of the neutrino  
 2370 as input, as it should be that of the Sun at that time and therefore known, in the  
 2371 atmospheric case I used a set of solar positions as our ansatz for the neutrino direction.  
 2372 From the distributions, one can see that the muon and the jet for the signal events are  
 2373 predominantly forward and also that the deviations from the momentum conservation

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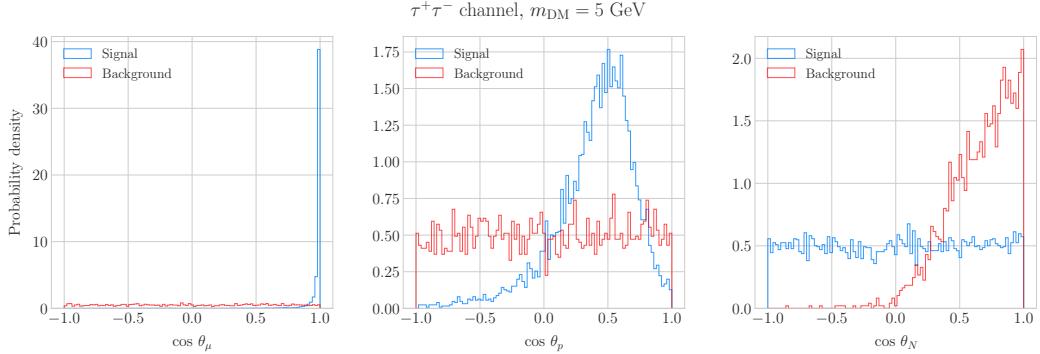
**Figure 5.13:** Signal efficiencies for the  $\tau^+\tau^-$  (blue line) and  $b\bar{b}$  (red line) DIS samples as functions of the DM mass,  $m_{\text{DM}}$ , obtained by applying the optimal angular cuts  $\theta_\mu < 27^\circ$ ,  $4^\circ < \theta_j < 26^\circ$  and  $\theta_{\text{plane}} < 3.5^\circ$ .

2374 plane are peaked at zero, as one should expect.

2375 Now, I can start applying cuts to maximise our signal selection efficiency while at  
 2376 the same time I try to minimise the amount of atmospheric background events passing  
 2377 the selection. To this end, I will need to find some lower and upper cuts for  $\theta_j$  and  
 2378  $\theta_\mu$  and an upper bound for  $\theta_{\text{plane}}$ . In Fig. 5.12 I show how upper bound cuts in the  
 2379 different angular variables affect the signal efficiency (blue lines) and the background  
 2380 rejection (red lines). Notice that the signal efficiency behaves in a quite different way  
 2381 when I apply cuts in the jet and the muon angles. On the contrary, the cuts on both  
 2382 variables have a similar effect on the background rejection.

2383 In order to obtain the optimal set of cuts, I perform a multidimensional scan. I  
 2384 do this separately for the  $\tau^+\tau^-$  and the  $b\bar{b}$  samples. For each case, I scan the possible  
 2385 cuts for each mass point and then I take the mean value of the signal efficiency for  
 2386 each configuration, to get the mean efficiency for each set of cuts. I do a similar scan  
 2387 for the atmospheric sample independently. Then, I take the sets of cuts such that  
 2388 the background rejection achieved is greater than 99.8% and search for the one which

## 5.5. HIGH ENERGY DM NEUTRINO SIGNALS



**Figure 5.14:** Distributions of  $\cos \theta_\mu$  (left panel),  $\cos \theta_p$  (central panel) and  $\cos \theta_N$  (right panel) for the  $\tau^+\tau^-$  QEL sample with  $m_{\text{DM}} = 5 \text{ GeV}$  (blue) and the atmospheric background (red).

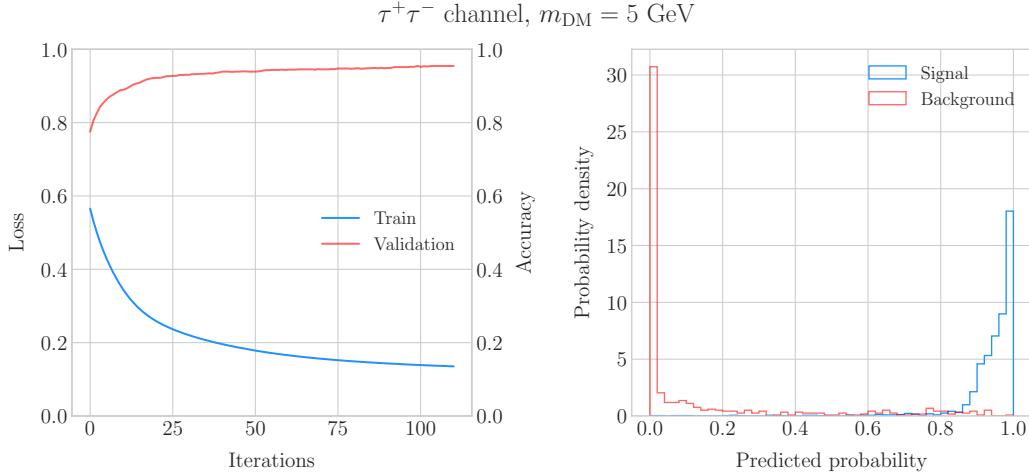
2389 maximises the  $\tau^+\tau^-$  and  $b\bar{b}$  sample mean efficiencies. I found that with the cuts  $\theta_\mu < 27^\circ$ ,  
 2390  $4^\circ < \theta_j < 26^\circ$  and  $\theta_{\text{plane}} < 3.5^\circ$  I get a background rejection of 99.80% while achieving  
 2391 a 49.40% and 44.92% mean signal efficiencies for the  $\tau^+\tau^-$  and  $b\bar{b}$  signals respectively.

2392 In Fig. 5.13 I show the signal efficiencies as a function of the DM mass for the  $\tau^+\tau^-$   
 2393 (blue line) and the  $b\bar{b}$  (red line) DIS events, after applying the cuts discussed above, as  
 2394 well as the energy threshold and hadronic visible energy selections. One can see that  
 2395 the efficiency grows with the mass, as annihilations of more massive DM particles will  
 2396 produce a neutrino spectrum centered at higher energies, where DIS events dominate.  
 2397 Notice also that the efficiency is higher for the  $\tau^+\tau^-$  case at every mass point, as in  
 2398 general this channel produces neutrinos at higher energies than the corresponding  $b\bar{b}$   
 2399 channel.

### 2400 5.5.2 Single proton QEL events

2401 Now, one can try to explore the low energy tail of the neutrino energy distributions. This  
 2402 regime is dominated by the QEL interactions, i.e. events of the type  $\nu_\mu + n \rightarrow \mu^- + p$ .  
 2403 In this case, as the typical energies are  $E_\nu \lesssim 1 \text{ GeV}$ , the momentum transfer to the  
 2404 remnant nucleus is sizeable. Therefore, I can not make the approximation I did before  
 2405 and assume that the momentum of the muon and the proton will give an adequate  
 2406 estimation of the reconstructed neutrino energy.

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**Figure 5.15:** Left panel: value of the loss function for the training sample (blue line) and accuracy for the validation sample (red line) versus the number of iterations for the MLP classifier training. Right panel: distributions of the predicted probabilities assigned by the MLP classifier to the test sample for the  $\tau^+\tau^-$  QEL signal with  $m_{\text{DM}} = 5 \text{ GeV}$  (blue) and the atmospheric background (red).

2407 In any case, as before, I can take the direction of the incoming neutrino as known.  
 2408 That way, one can estimate the energy of the neutrino as:

$$E_\nu^{\text{reco}} = E_\mu + E_p + m_{^{39}\text{Ar}} - m_{^{40}\text{Ar}}, \quad (5.33)$$

2409 and using momentum conservation I can write the momentum of the remnant nucleus  
 2410 as:

$$\vec{p}_N = \hat{p}_\nu (E_\mu + E_p + m_{^{39}\text{Ar}} - m_{^{40}\text{Ar}}) - \vec{p}_\mu - \vec{p}_p. \quad (5.34)$$

2411 As in the previous case, I need to drop the events where the muon or the proton fall  
 2412 below the kinetic energy detection threshold [85]. Also, I again apply a smearing to the  
 2413 momenta of the particles, a 1% for muons and 5% for protons.

2414 Having done that, one can compute the following angular variables for our selected  
 2415 events:

$$\cos \theta_\mu = \hat{p}_\nu \cdot \hat{p}_\mu, \quad (5.35)$$

$$\cos \theta_p = \hat{p}_\nu \cdot \hat{p}_p, \quad (5.36)$$

## 5.5. HIGH ENERGY DM NEUTRINO SIGNALS

$$\cos \theta_N = \hat{p}_\nu \cdot \hat{p}_N. \quad (5.37)$$

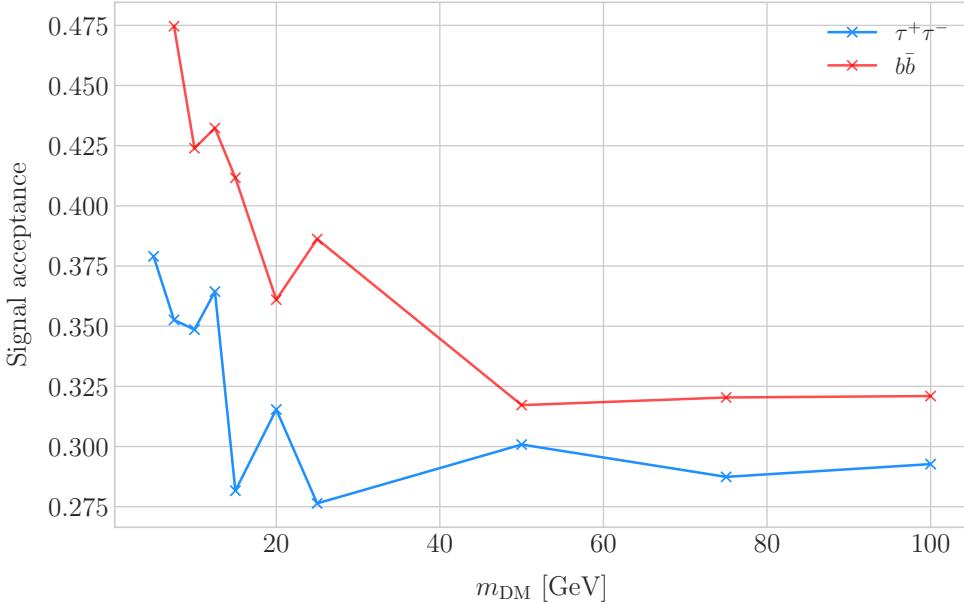
2416 Fig. 5.14 shows the distributions of these angular variables for the  $\tau^+\tau^-$  QEL  
 2417 sample with  $m_{\text{DM}} = 5$  GeV (blue) and the atmospheric background (red). Again, for  
 2418 the atmospheric events I used a random solar position as the ansatz for the incoming  
 2419 neutrino direction. Notice that now, opposed to the DIS case where the signal had very  
 2420 sharp distributions for the variables considered, the shapes of the angular distributions  
 2421 for signal and background are not that much different.

2422 This effectively means that the usual approach of applying simple angular cuts would  
 2423 not work as well as in the previous situation. Therefore, as a possible solution, I tried to  
 2424 use a multilayer perceptron (MLP) classifier to separate between signal and background  
 2425 events. Thus, the power of the hypothesis test will serve as an estimate of the signal  
 2426 efficiency, and in the same way one can take the size of the test to be our background  
 2427 rejection.

2428 For each DM mass value and channel, as well as for the background sample, I divide  
 2429 our events into training, validation and test samples. The input variables for the classifier  
 2430 were the reconstructed neutrino energy from Eq. (5.33) and the angular variables defined  
 2431 in Eqs. (5.35 - 5.37). I used the MLP classifier implemented in `scikit-learn` [139], with  
 2432 a total of five hidden layers, the rectified linear unit activation function and adaptive  
 2433 learning rate. In order to account for fluctuations due to artifacts in the training process I  
 2434 repeated the training a thousand times for each sample, redefining each time the training,  
 2435 validation and test subsets, so one can take as our signal efficiency and background  
 2436 rejection the mean values of the powers and sizes of the tests.

2437 The results of one of these training processes for the  $\tau^+\tau^-$  QEL signal with  $m_{\text{DM}} =$   
 2438 5 GeV is shown in Fig. 5.15. On the left panel I show the loss function values (blue) and  
 2439 accuracy (red) at each iteration for the training and the validation samples respectively.  
 2440 The training stops either when the maximum number of iterations is reached (1000 in  
 2441 this case) or when the accuracy for the validation sample reaches a certain tolerance  
 2442 (I chose  $10^{-4}$  as our tolerance). On the right panel I have the distributions for the

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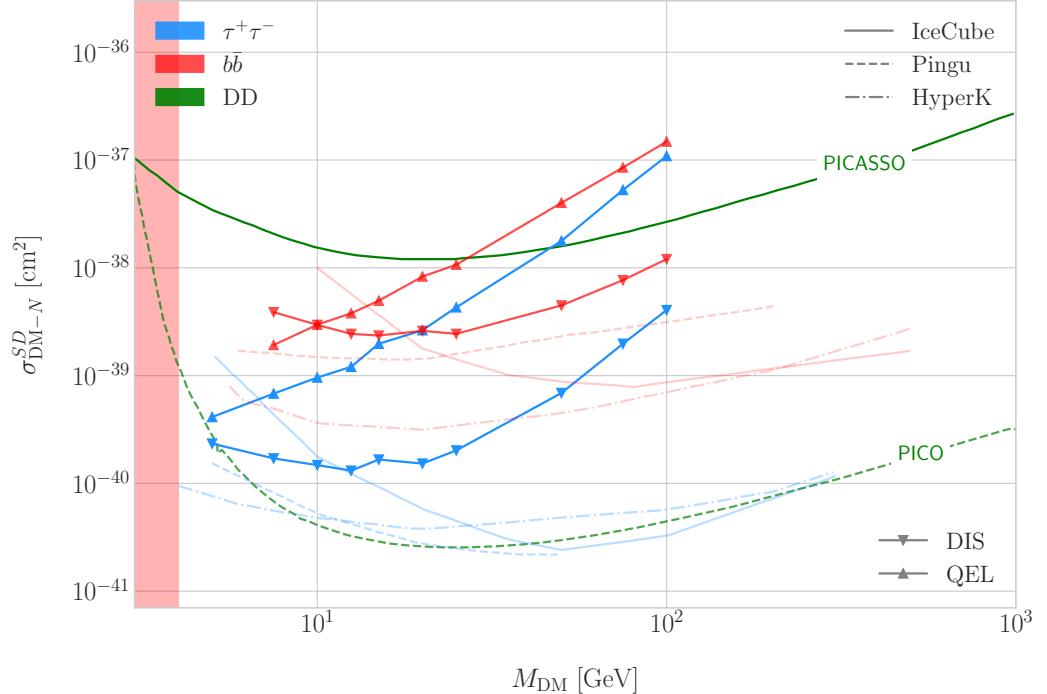


**Figure 5.16:** Signal efficiencies for the  $\tau^+\tau^-$  (blue line) and  $b\bar{b}$  (red line) single proton QEL samples as functions of the DM mass,  $m_{\text{DM}}$ , obtained by requiring a minimum predicted probability from the MLP classifier of 0.97 in order to achieve a background rejection greater than 99.8%.

predicted probability by the model, separated in true signal (blue) and background (red) events, for the test sample. One can see that both populations are well separated, obtaining a power of 44.97% and a size of 0.17% when I require a predicted probability greater than 0.97.

Applying this criteria for each sample, I obtain the mean signal efficiencies shown in Fig. 5.16. Notice that the efficiencies for the channel  $\tau^+\tau^-$  (blue line) are consistently lower than the ones for the  $b\bar{b}$  channel (red line). This can be due to the fact that, for each DM mass point, the neutrino spectrum coming from the  $b\bar{b}$  annihilation channel is centered at lower energies when compared to the  $\tau^+\tau^-$  spectrum. This directly translates into more low energy neutrinos undergoing QEL interactions, which give signals that can be easily separated from the atmospheric background. This explanation also help us understand why in both cases the signal acceptance drops when the DM mass increases. In all cases, the background rejection took values between 99.8% to 99.9%. I will assume a 99.8% background rejection value in all cases to keep our estimation conservative.

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**Figure 5.17:** Projected 90% confidence level upper limit for DUNE (400 kT yr) on the spin-dependent DM-nucleon scattering cross section as a function of  $m_{\text{DM}}$ , for the annihilation channels  $\tau^+\tau^-$  (blue) and  $b\bar{b}$  (red) separated by interaction type (up triangles denote DIS interactions whereas down triangles represent QEL interactions). I also show the previous limits from IceCube [7] (solid lines) and the projected sensitivities for Pingu [8] (dashed lines) and Hyper-Kamiokande [9] (dash-dotted lines), as well as the direct detection limits from PICASSO [10] (solid green line) and PICO-60 C<sub>3</sub>F<sub>8</sub> [11] (dashed green line).

### 2457 5.5.3 Results

2458 In order to estimate the DM-nucleon cross section sensitivities in the present case I need  
 2459 again to compute the expected number of background events. As I am now separating  
 2460 events by interaction type Eq. (5.25) does not hold anymore, as in that case I integrated  
 2461 over the total neutrino-argon cross section. In this instance, the expected background  
 2462 events for DIS events is approximately given by:

$$N_B^{DIS} \simeq \eta_B^{DIS} \times (4.655 \times 10^3) \times \left( \frac{\text{exposure}}{400 \text{ kT yr}} \right), \quad (5.38)$$

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2463 whereas for QEL events we have:

$$N_B^{QEL} \simeq \eta_B^{QEL} \times (2.248 \times 10^4) \times \left( \frac{\text{exposure}}{400 \text{ kT yr}} \right). \quad (5.39)$$

2464 Now, using these together with Eqs. (5.26) and (5.27) one can obtain the 90% C.L.  
2465 upper limit on the total annihilation rate at equilibrium for both kind of events. Then,  
2466 applying the computed DM-nucleons capture rates I can translate these into limits on  
2467 the DM-nucleon cross section by means of Eqs. (5.2), (5.5) and (5.6).

2468 Fig. 5.17 shows the obtained limits on the SD DM-nucleon cross section for DUNE,  
2469 using the DIS (up triangles) and QEL (down triangles) events both for the  $\tau^+\tau^-$  (blue)  
2470 and the  $b\bar{b}$  (red) samples, for an exposure of 400 kT yr. I also include the corresponding  
2471 current limits from IceCube [7] (solid lines), as well as the projected sensitivities of  
2472 Pingu [8] (dashed lines) and Hyper-Kamiokande [9] (dash-dotted lines). For comparison,  
2473 I also show the reported direct detection limits from PICASSO [10] (solid green line)  
2474 and PICO-60  $C_3F_8$  [11] (dashed green line).

2475 Notice that, for most of the mass range, the limits one can set by using the DIS  
2476 events are stronger than those of the QEL interactions, except for the low mass part  
2477 of both the  $\tau^+\tau^-$  and the  $b\bar{b}$  curves where the QEL events dominate. In general, the  
2478 expected sensitivity of DUNE for DM masses  $\lesssim 25$  GeV surpasses the stronger current  
2479 indirect limits. However, experiments like Hyper-Kamiokande are foreseen to have an  
2480 overall better sensitivity in this kind of searches, as they have a bigger active volume  
2481 and accept a broader energy range.

2482 A pending question is what happens when we add the RES and MEC charged-current  
2483 interaction contributions. In that case it would probably be more convenient to split  
2484 the samples by final state interaction topologies. Also, another necessary improvement  
2485 would be adding a full detector simulation and reconstructions. This will also require  
2486 considering the effect of poorly reconstructed events or final states containing neutral  
2487 particles such that they mimic the desired topology at the reconstruction level.

## 5.6. EXAMPLE: LEPTOPHILIC DARK MATTER

### **2488 5.6 Example: Leptophilic Dark Matter**

**2489** In general, the capture rate of DM particles by the Sun via interactions with electrons is  
**2490** several orders of magnitude smaller than the capture via DM-nucleus scattering. Thus,  
**2491** it would be sub-leading even when nucleon capture is loop suppressed. As I showed in  
**2492** Fig. 5.2, the capture rate via scattering off electrons only surpasses the capture rates  
**2493** via DM-nucleons interactions for DM masses  $\lesssim 100 - 500$  MeV.

**2494** However, if one considers a model where DM-nucleon interactions are forbidden even  
**2495** at loop level, then electron interactions will be the sole contributor to DM capture in  
**2496** the Sun. One can describe such scenario where the DM particles couple to leptons but  
**2497** not to the quark sector using effective operators.

**2498** In general, assuming that the DM particle is a Dirac fermion, the dimension six  
**2499** operators describing the interaction between two DM particles and two leptons can be  
**2500** written as:

$$\mathcal{L}_{eff} = G \sum_i (\bar{\chi} \Gamma^i \chi) (\bar{\ell} \Gamma^i \ell), \quad (5.40)$$

**2501** where  $G = 1/\Lambda^2$  is the effective coupling strength,  $\Lambda$  the cut-off of the effective field  
**2502** theory and  $\ell$  denotes any lepton. In principle, one should consider all the possible  
**2503** Lorentz structures  $\Gamma_f^i$  in order to have a complete set of effective operators.

**2504** However, some combinations will induce interactions with nucleons at loop level.  
**2505** As we are specifically interested in interactions which forbid any communication with  
**2506** the quark sector, I will not consider those [140]. In addition, some of the effective  
**2507** operators give rise to velocity-suppressed scattering cross sections between DM particles  
**2508** and leptons. I will also neglect those, as the suppression goes with the square of the DM  
**2509** halo velocity which in units of the speed of light is  $\sim 10^{-6}$ .

**2510** This way, the only Lorentz tensor structure that do not induce interactions with  
**2511** quarks at loop level and gives a contribution to the scattering cross section that is not  
**2512** velocity suppress is the axial-axial interaction. The effective Lagrangian is then given

## CHAPTER 5. DM SEARCHES WITH NEUTRINOS FROM THE SUN

2513 by:

$$\mathcal{L}_{eff} = \frac{c_A^\chi c_A^\ell}{\Lambda^2} (\bar{\chi} \gamma^\mu \gamma^5 \chi) (\bar{\ell} \gamma_\mu \gamma^5 \ell), \quad (5.41)$$

2514 where  $c_A^\chi$  and  $c_A^\ell$  are the couplings for the different species. As the DM coupling appears  
 2515 as a common factor for any lepton choice, I will redefine the corresponding coupling  $c_A^\ell$   
 2516 to absorb  $c_A^\chi$ . Also, for simplicity, I will assume that the couplings between the DM  
 2517 particles and the leptons are flavour independent, i.e. I have just two couplings,  $c_A^e$  for  
 2518 charged leptons and  $c_A^v$  for neutrinos.

2519 In the case of a scalar DM particle, the lowest order effective interaction with  
 2520 leptons happens through a dimension five operator, generating scalar and pseudoscalar  
 2521 interactions. However, the former induces interactions with quarks at two loop level  
 2522 whereas the latter gives a velocity suppressed scattering cross section.

2523 From the effective Lagrangian in Eq. (5.41) it can be shown that the axial-axial  
 2524 contribution to the scattering cross section for the fermionic DM and a charged lepton  
 2525 is given by:

$$\sigma_{DM-e}^{AA} = 3 (c_A^e)^2 \frac{m_e^2}{\pi \Lambda^4}. \quad (5.42)$$

2526 If the DM interacts exclusively with fermions, then the only annihilation channels  
 2527 that will give us a measurable neutrino flux coming out of the Sun are  $\tau^+ \tau^-$  and  $\nu \bar{\nu}$ . The  
 2528 former channel, already explored previously in the more mainstream scenario of the DM  
 2529 capture via scattering off nucleons, is open only for  $m_{DM} > m_\tau \simeq 1776.86 \pm 0.12$  MeV  
 2530 [141], a mass region where the solar DM capture by electrons is at least one order of  
 2531 magnitude smaller than the capture via interactions with nucleons. On the contrary, the  
 2532 latter allows us to explore a region where the capture rate via scattering off electrons  
 2533 dominates over the rest.

2534 One downside of focusing in such low mass range is that it falls below the usual  
 2535 limit of  $m_{evap} \sim 4$  GeV usually explored in the literature. The pretext to explore this  
 2536 region is the result discussed previously reported in Ref. [2], where DM evaporation in  
 2537 the Sun for the case of capture via electron scattering could be negligible for masses  
 2538 as low as  $m_{evap} \sim 200$  MeV. This result is quite sensitive to the high velocity tail of

## 5.6. EXAMPLE: LEPTOPHILIC DARK MATTER

2539 the DM velocity distribution in equilibrium inside the Sun, and therefore full numerical  
 2540 simulations would be needed to asses the impact of this effect. However, this falls out of  
 2541 the scope of our work.

2542 In this case, as I have an specific realisation of the interaction between the DM  
 2543 and leptons, one can estimate the relic density of our DM for different values of the  
 2544 couplings and the effective field theory scale  $\Lambda$ . The first step to do so is compute the  
 2545 self-annihilation cross section. Because I consider cold relics, at the freeze-out time our  
 2546 DM particles were non-relativistic and so one can expand the annihilation cross section  
 2547 in terms of the relative velocity  $v$  between two annihilating DM particles as [142]:

$$\sigma_{ann}^{AA}|v| \approx \frac{1}{2\pi\Lambda^4} \sum_{\ell} \left(c_A^{\ell}\right)^2 m_{\chi}^2 \sqrt{1 - \frac{m_{\ell}^2}{m_{\chi}^2} \left[ \frac{m_{\ell}^2}{m_{\chi}^2} + \frac{1}{12} \left(2 - \frac{m_{\ell}^2}{m_{\chi}^2}\right) v^2 \right]}, \quad (5.43)$$

2548 where the sum includes all the possible lepton final states with mass  $m_{\ell}$ .

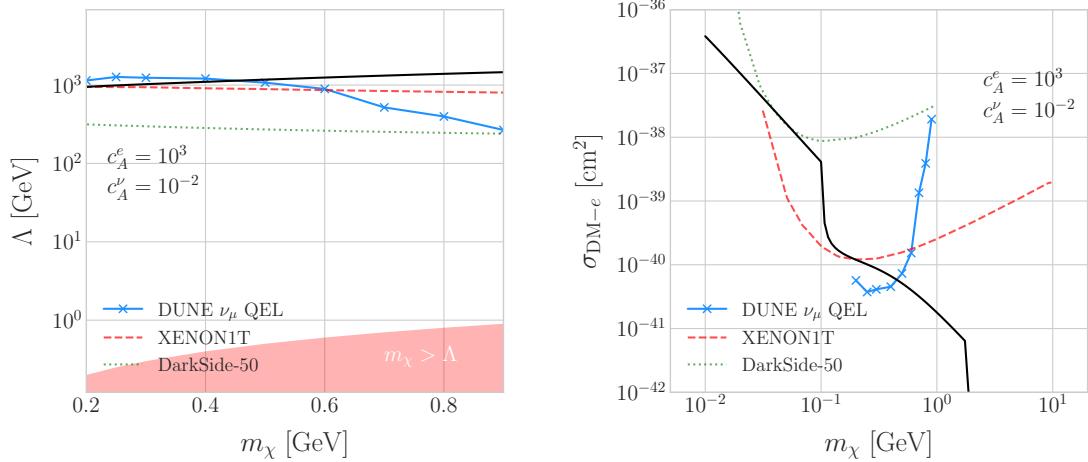
2549 Solving the Boltzmann equation for the evolution of the DM density gives as a  
 2550 solution a relic density of:

$$\Omega_{\chi} h^2 \approx \frac{(1.04 \times 10^9) x_F}{M_{Pl} \sqrt{g_*} (a + 3b/x_F)}, \quad (5.44)$$

2551 where  $x_F = m_{\chi}/T_F$  being  $T_F$  the freeze-out temperature,  $g_*$  the number of relativistic  
 2552 degrees of freedom at freeze-out and  $a$  and  $b$  the terms in the annihilation cross section  
 2553 expansion  $\sigma_{ann}|v| \approx a + bv^2 + \mathcal{O}(v^4)$ . Using the current best fit for the relic DM density  
 2554  $\Omega_{\chi} h^2 = 0.1198 \pm 0.0012$  [143] one can use these relations to compute the required  
 2555 effective theory scale  $\Lambda$  at which the correct density is achieved for any combinations of  
 2556  $m_{\chi}$  and  $c_A^{\ell}$ .

2557 As discussed before, in the low DM mass region QEL interactions dominate. Moreover,  
 2558 if I focus on direct annihilation to neutrinos, the energy of the muon neutrino flux is  
 2559 known as it must be equal to the mass of the DM particle,  $E_{\nu} = m_{\chi}$ . That way, now  
 2560 I do not need to use Eq. (5.33) in order to estimate the momentum transfer to the

## CHAPTER 5. DM SEARCHES WITH NEUTRINOS FROM THE SUN



**Figure 5.18:** Left panel: Projected 90% confidence level sensitivity of DUNE (400 kT yr) to the scale  $\Lambda$  of an EFT containing only leptophilic DM axial-axial interactions (blue line). Right panel: In both cases the corresponding limits from DarkSide-50 [12] (dotted green line) and XENON1T [13] (dashed red line) are also shown, together with the configurations for which the correct relic density is achieved (black line), all for the coupling values  $c_A^e = 10^3$  and  $c_A^\nu = 10^{-2}$ .

2561 remnant nucleus, I can simply take:

$$\vec{p}_N = \hat{p}_\nu m_\chi - \vec{p}_\mu - \vec{p}_p. \quad (5.45)$$

2562 To estimate the signal efficiency and background rejection for this case I used again  
 2563 the MLP classifier from `scikit-learn`, using the same specifications as before. The  
 2564 only difference now is that I add also the reconstructed neutrino energy as one of the  
 2565 features to train the classifier with, because the characteristic monoenergetic flux for  
 2566 each  $m_\chi$  value will help to distinguish between signal and background events.

2567 In this case, for masses below  $\sim 500$  MeV I obtain a signal efficiency close to unity  
 2568 while keeping a background rejection of 99.9%. For bigger values of the mass, the signal  
 2569 efficiency drops significantly if I require to keep the background acceptance under 0.01%.  
 2570 However, because this kind of search is dominated by the background, sacrificing the  
 2571 signal acceptance to keep the background rejection to a minimum enhances the reach  
 2572 of the analysis. This way, for DM masses of the order of  $m_\chi \sim 1$  GeV I end up with  
 2573 efficiencies as low as 1%.

## 5.7. SYSTEMATIC UNCERTAINTIES

Now, estimating the number of background events using Eq. (5.39) one can go on and apply Eqs. (5.26) and (5.27) together with Eq. (5.42) to derive the sensitivity of DUNE to this kind of model. Fig. 5.18 (left panel) shows the potential reach of DUNE to constrain the EFT scale  $\Lambda$  this model containing only leptophilic DM axial-axial interactions (blue line), for a choice of couplings  $c_A^e = 10^3$  and  $c_A^\nu = 10^{-2}$ . I also included the current limits on the DM-electron scattering cross section from DarkSide-50 [12] (dotted green line) and XENON1T [13] (dashed red line), reworked with Eq. (5.42) to show their implications for the EFT scale. The values of  $\Lambda$  for which the correct DM relic density value is achieved for each mass are also shown (black line). This tells us that, for that specific choice of couplings, DUNE would be sensitive to DM configurations allowed by the relic density constraint up to a mass of  $m_\chi \sim 400$  MeV.

In Fig. 5.18 (right panel) I show the same upper limits but for the DM-electron scattering cross section. From this view one can see that DUNE would be able to offer complementary information to the low energy DM-electron interaction searches performed by direct detection experiments, in a slightly higher mass range.

With the present example, although it focuses on a very specific realisation of the DM interactions, I show the potential of DUNE to constrain exotic DM scenarios. Thanks to its low backgrounds and superb angular resolution DUNE will be able to help with the systematic searches for dark sectors physics.

## 5.7 Systematic uncertainties

The estimation of the DM cross sections using neutrinos from WIMP annihilations inside the Sun is affected by systematic uncertainties from different sources. Surely, the atmospheric background estimation is also affected by systematic uncertainties. There are uncertainties common to both types of events, as well as others specific to each. In this section, I try to provide a comprehensive summary of the main sources of uncertainty for this analysis, which should be taken into account in any future extensions of the same.

## CHAPTER 5. DM SEARCHES WITH NEUTRINOS FROM THE SUN

**Table 5.1:** Systematic uncertainties for the solar WIMP signal events. Table adapted from Ref. [144].

Systematic	Value
Form factor	Does not apply to SD [145]
Solar model	3% [145]
Local DM density	Not relevant for relative interpretations [145, 146]
Dynamics of solar system	Negligible [147]
Velocity distributions	20% at 20 GeV [145, 146]
Oscillation parameters	8% for $\tau^+\tau^-$ , 5% for $b\bar{b}$ [148]
Neutrino interactions in the Sun	10%
Matter effects in the Earth	10%

### 2601 5.7.1 Systematic uncertainties in the solar WIMP signal

2602 The systematic uncertainties affecting the solar WIMP neutrino signal can be divided in  
 2603 two categories. On the one hand, we have those affecting the solar WIMP annihilation  
 2604 rate. On the other hand, there are the ones which modify the neutrino flux resulting  
 2605 from the annihilations reaching our detector.

2606 • **Uncertainties on the annihilation rate.** These include the astrophysical effects  
 2607 that affect the normalisation of the solar DM neutrino flux. The main contributions  
 2608 are the solar model choice, the form factor uncertainties (only for SI searches), the  
 2609 gravitational effect of other planets, the local DM density (not relevant for relative  
 2610 comparisons, as it affects direct detection experiments in the same way), and the  
 2611 DM halo and dispersion velocities.

2612 • **Uncertainties on the neutrino flux.** These are related to the oscillation effects,  
 2613 as well as the absorption and regeneration of neutrinos in the Sun. Matter effects  
 2614 inside the Earth also affect the neutrino flux the measured at the detectors.

2615 Table 5.1 summarises the contributions of the different sources of uncertainty for the  
 2616 signal events. These are the signal systematic uncertainties that have been taken into  
 2617 account in previous solar DM searches with neutrinos [144, 146, 148].

## 5.7. SYSTEMATIC UNCERTAINTIES

**Table 5.2:** Systematic uncertainties for the solar WIMP atmospheric background events. Table adapted from Ref. [51].

Systematic	Value
Flux normalisation	25 – 7% for $0.1 < E_\nu \leq 1$ GeV (linear in $\log E_\nu$ ) 7% up to 10 GeV
$(\nu_\mu + \bar{\nu}_\mu)/(\nu_e + \bar{\nu}_e)$	2% for $E_\nu \leq 1$ GeV 3% for $1 < E_\nu \leq 10$ GeV
$\bar{\nu}_\mu/\nu_\mu$	2% for $E_\nu \leq 1$ GeV 6% for $1 < E_\nu \leq 10$ GeV
K/ $\pi$ ratio	5% $E_\nu \leq 100$ GeV

### 2618 5.7.2 Systematic uncertainties in the atmospheric background

2619 For the atmospheric background events, one needs to take into account the systematic  
 2620 uncertainties affecting the atmospheric  $\nu_\mu$  flux. These have been extensively studied  
 2621 in the context of atmospheric neutrino oscillation measurements. Among these, the  
 2622 energy-dependent flux normalisation uncertainty is the in the low energy regime. Other  
 2623 important contributions to the uncertainty come from the ratios between the muon to  
 2624 electron neutrino and the muon to anti-muon neutrino components of the flux. Additional  
 2625 uncertainty is introduced by the errors in the pion and kaon production rates calculated  
 2626 for the hadronic interactions of cosmic rays in the atmosphere [149].

2627 Table 5.2 shows a summary of the leading contributions to the uncertainty on the  
 2628 atmospheric muon neutrino flux, in the energy range relevant for this analysis.

### 2629 5.7.3 Common systematic uncertainties

2630 Finally, there are sources of uncertainty common to both signal and backgrounds. These  
 2631 have two different origins:

- 2632 • **Uncertainties on the neutrino cross section.** These are introduced by the  
 2633 modelling of the neutrino-nucleus interactions. In the context of the solar WIMP  
 2634 analysis, these have been estimated to be 10% for DM masses around 10 GeV  
 2635 [148].

## CHAPTER 5. DM SEARCHES WITH NEUTRINOS FROM THE SUN

- 2636     • **Uncertainties related to the detector.** They affect the measurement of the  
2637       neutrino interaction and the final state particles produced. The main detector  
2638       uncertainties relevant to this analysis are those of the energy and angular resolutions  
2639       of the DUNE FD. Other effects, like the timing and triggering efficiencies, will  
2640       also contribute to the uncertainties. The particular values these will take for this  
2641       analysis need to be worked out in the context of DUNE.

2642

2643

## Particle ID in ND-GAr

2644 ND-GAr is a magnetised, high-pressure gaseous argon TPC (HPgTPC), surrounded by  
2645 an electromagnetic calorimeter (ECal) and a muon detector (commonly refer to as  $\mu$ ID).  
2646 A detailed discussion on the requirements, design, performance and physics of ND-GAr  
2647 can be found in the DUNE ND CDR [91] and the ND-GAr whitepaper (cite).

2648 In DUNE Phase II ND-GAr will fulfill the role of TMS, measuring the momentum  
2649 and sign of the charged particles exiting ND-LAr. Additionally, it will be able to measure  
2650 neutrino interactions inside the HPgTPC, achieving lower energy thresholds than those  
2651 of the ND and FD LArTPCs. By doing so ND-GAr will allow to constrain the relevant  
2652 systematic uncertainties for the LBL analysis even further.

2653 The goal of the present chapter is to review the requirements that the physics program  
2654 of DUNE impose on ND-GAr, present the current status of its design and describe the  
2655 GArSoft package, its simulation and reconstruction software.

2656 As decided during the DUNE Phase II workshop in June 2023 [reference], we want  
2657 to build ND-GAr physics case by showing:

- 2658 • That ND-GAr can constrain systematic uncertainties that ND-LAr might miss.
- 2659 • The impact on the neutrino oscillation results if such systematic uncertainties are  
2660 missed.
- 2661 • That ND-GAr is necessary to reach DUNE's main physics goals.

2662 This way, the design of ND-GAr will be physics driven.

## CHAPTER 6. PARTICLE ID IN ND-GAr

2663 In order to study the effects of final state interactions (FSI) in CC interactions,  
2664 ND-GAr should be able to measure the spectrum of protons and charged pions at low  
2665 energies. ND-GAr also needs to be able to measure the pion multiplicity, specially for  
2666 energies above 100 MeV as at these energies the pions shower in the LAr, to inform the  
2667 pion mass correction in the ND and FD LArTPCs.

2668 In order to correctly identify electrons, muons, pions, kaons and protons ND-GAr  
2669 can use a combination of:  $dE/dx$  measurements in the HPgTPC,  $E_{ECAL}/p$  using the  
2670 ECAL total energy and the momentum obtained from magnetic spectroscopy in the  
2671 HPgTPC and penetration information through the ECAL and muon tagger.

### 2672 6.1 GArSoft

2673 GArSoft is a software package developed for the simulation and reconstruction of events  
2674 in ND-GAr. It is inspired by the LArSoft toolkit used for the simulation of LArTPC  
2675 experiments, like the DUNE FD modules. It is based on `art`, the framework for event  
2676 processing in particle physics experiments [150]. Other of its main dependencies are  
2677 `ROOT`, `NuTools`, `GENIE` and `Geant4`. It allows the user to run all the steps of a generation-  
2678 simulation-reconstruction workflow using FHiCL configuration files.

#### 2679 6.1.1 Event generation

2680 The standard generator FHiCLs in GArSoft run the event generation and particle  
2681 propagation simulation (i.e. Geant4) in the same job by default. However, it is possible  
2682 to split them up if needed. The current version of GArSoft provides five different event  
2683 generators, each of them producing `simb::MCTruth` products defined in `NuTools`. The  
2684 available modules are:

- 2685 • **SingleGen**: particle gun generator. It produces the specified particles with a given  
2686 distribution of momenta, initial positions and angles.
- 2687 • **TextGen**: text file generator. The input file must follow the `hepevt` format<sup>1</sup>, the

---

<sup>1</sup>In brief, each event contains at least two lines. The first line contains two entries, the event number

## 6.1. GARSOFT

2688 module simply copies this to `simb::MCTruth` data products.

2689 • **GENIEGen**: GENIE neutrino event generator. The module runs the neutrino-nucleus  
2690 interaction generator using the options specified in the driver FHiCL file (flux file,  
2691 flavour composition, number of interactions per event,  $t_0$  distribution, ...). Current  
2692 default version is v3\_04\_00.

2693 • **RadioGen**: radiological generator. It produces a set list of particles to model  
2694 radiological decays. Not tested.

2695 • **CRYGen**: cosmic ray generator. The module runs the CRY event generator with a  
2696 configuration specified in the FHiCL file (latitude and altitude of detector, energy  
2697 threshold, ...). Not tested.

2698 The module **GArG4** searches for all the generated `simb::MCTruth` data products, using  
2699 them as inputs to the Geant4 simulation with the specified detector geometry. A constant  
2700 0.5 T magnetic field along the drift coordinate is assumed. The main outputs of this step  
2701 are `simb::MCParticle` objects for the generated Geant4 particles, `gar::EnergyDeposit`  
2702 data products for the energy deposits in the HPgTPC and `gar::CaloDeposit` data  
2703 products for the energy deposits in the ECal and muon system.

### 2704 6.1.2 Detector simulation

2705 The standard detector simulation step in GArSoft is all run with a single FHiCL, but  
2706 the different modules can be run independently as well. First the `IonizationReadout`  
2707 module simulates the charge readout of the HPgTPC, and later the `SiPMReadout` module  
2708 runs twice, once for the ECal and then for the muon system, with different configurations.

2709 The `IonizationAndScintillation` module collects all the `gar::EnergyDeposit`  
2710 data products, to compute the equivalent number of ionization electrons for each energy

---

and the number of particles in the event. Each following line contains 15 entries to describe each particle. The entries are: status code, pdg code for the particle, entry of the first mother for this particle, entry of the second mother for this particle, entry of the first daughter for this particle, entry of the second daughter for this particle, x component of the particle momentum, y component of the particle momentum, z component of the particle momentum, energy of the particle, mass of the particle, x component of the particle initial position, y component of the particle initial position, z component of the particle initial position and time of the particle production.

## CHAPTER 6. PARTICLE ID IN ND-GAr

deposit. The `ElectronDriftAlg` module simulates the electron diffusion numerically both in the longitudinal and transverse directions and applies an electron lifetime correction factor. The induced charge on the nearest and neighbouring readout pads is modeled using the provided pad response functions. The digitisation of the data is then simulated with the `TPCReadoutSimAlg` module. By default, the ADC sampling rate used is 50.505 MHz. The resulting raw waveforms for each channel are stored with zero-suppression, in order to save memory and CPU time. The algorithms keep blocks of ADC values above a certain threshold, plus some adjustable additional early and late tick counts. The results of these three steps are `gar::raw::RawDigit` data products.

For the ECal and the muon system the `SiPMReadout` module calls either the `ECALReadoutSimStandardAlg` or `MuIDReadoutSimStandardAlg` modules. These take all the `gar::CaloDeposit` data products in the corresponding detector and do the digitisation depending on whether the hit was in a tile or strip layer. They include single photon statistics, electronic noise, SiPM saturation and time smearing. The resulting objects are `gar::raw::CaloRawDigit` data products.

### 6.1.3 Reconstruction

The reconstruction in GArSoft is also run as a single job by default. It first runs the hit finding, clustering, track fitting and vertex identification in the HPgTPC, followed by the hit finding and clustering in the ECal and muon system. After those it produces the associations between the associations between the tracks and the ECal clusters.

Focusing first on the HPgTPC reconstruction, the `CompressedHitFinder` module takes the zero-suppressed ADCs from the `gar::raw::RawDigit` data products. The reconstructed hits largely correspond to the above threshold blocks, however the hit finder identifies waveforms with more than one maximum, diving them in multiple hits if they dip below a certain threshold. The data products produced are of the form `gar::rec::Hit`. These are the inputs to the clustering of hits in the `TPCHitCluster` module. Hits close in space and time are merged, and the resulting centroids are found. This module outputs `gar::rec::TPCClusters` objects and associations to the input

## 6.1. GARSOFT

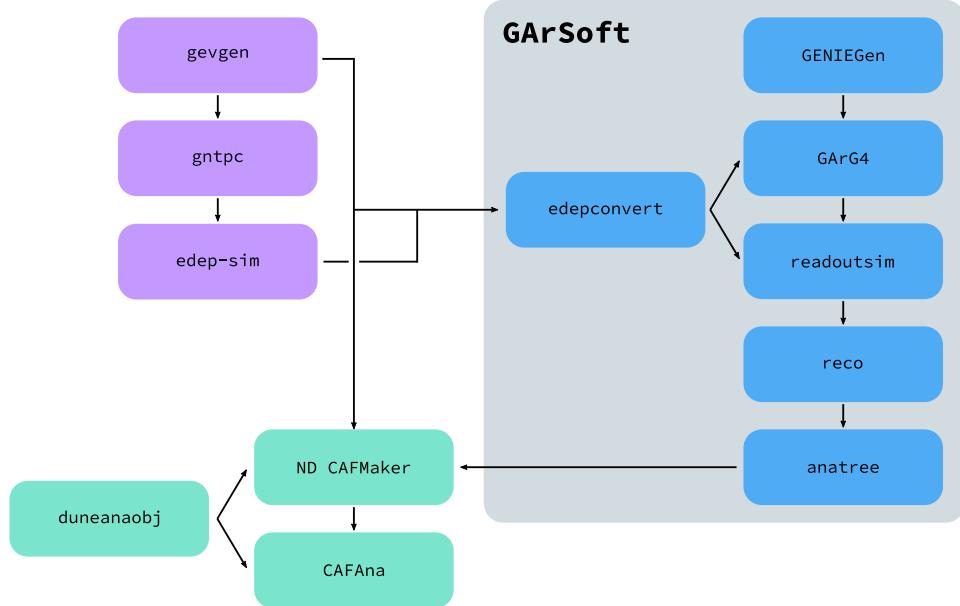
2739 hits.

2740 The following step prior to the track fitting is pattern recognition. The module  
2741 called `tpcvechitfinder2` uses the `gar::rec::TPCClusters` data products to find track  
2742 segments, typically called vector hits. They are identified by performing linear 2D fits  
2743 to the positions of the clusters in a 10 cm radius, one fit for each coordinate pair. A  
2744 3D fit defines the line segment of the vector hit, using as independent variable the one  
2745 whose sum of (absolute value) slopes in the 2D fits is the smallest. The clusters are  
2746 merged to a given vector hit if they are less than 2 cm away from the line segment. The  
2747 outputs are `gar::rec::VecHit` data products, as well as associations to the clusters. The  
2748 `tpcpatrec2` module takes the `gar::rec::VecHit` objects to form the track candidates.  
2749 The vector hits are merged together if their direction matches, their centers are within  
2750 60 cm and their direction vectors point roughly to their respective centers. Once  
2751 the clusters of vector hits are formed they are used to make a first estimation of the  
2752 track parameters, simply taking three clusters along the track. The module produces  
2753 `gar::rec::Track` data products and associations between these tracks and the clusters  
2754 and vector hits.

2755 The track is fitted by means of a Kalman filter in the `tpctrackfit2` module, using  
2756 the position along the drift direction as the independent variable. Two different fits are  
2757 performed per track, a forward and a backwards fit, each starting from one of the track  
2758 ends. The Kalman filter state vector ( $y, z, R, \phi, \tan\lambda$ ) is estimated at each point along  
2759 the track using a Bayesian update. The track parameters reported in the forward and  
2760 backwards fits are the ones computed at the opposite end where the fit started. The  
2761 main outputs of the track fit are the `gar::rec::Track` objects. Additionally, the module  
2762 stores the fitted 3D positions along the track in the `gar::rec::TrackTrajectory` data  
2763 products and the total charge and step sizes for each point also get stored in the form of  
2764 `gar::rec::TrackIonization` objects.

2765 After the tracking step, the `vertexfinder1` module looks at the reconstructed  
2766 `gar::rec::Track` products, creating vertex candidates with the track ends that are  
2767 within 12 cm of each other. The vertices are then fitted using linear extrapolations from

## CHAPTER 6. PARTICLE ID IN ND-GAr



**Figure 6.1:** Schematic diagram showing the different modules involved in the ND-GAr production.

2768 the different track ends associated. The results are `gar::rec::Vertex` data products,  
 2769 and associations to the tracks and corresponding track ends.

2770 For the ECal and muon tagger, the `SiPMHitFinder` module runs twice with different  
 2771 configurations, adapted to the particular capabilities of both. The module simply takes  
 2772 the `gar::raw::CaloRawDigit` products, applies a calibration factor to convert the ADC  
 2773 counts to MeV and for the strip layer hits it calculates the position along the strip using  
 2774 the times recorded of both SiPMs. This module produces `gar::rec::CaloHit` data  
 2775 products. Next, these objects are used as inputs to the `CaloClustering` module. It  
 2776 merges the hits based on a simple nearest neighbours (NN) algorithm. For the resulting  
 2777 clusters it also computes the total energy and position of the centroid. The results are  
 2778 stored as `gar::rec::Cluster` data products, with associations to the hits.

2779 The last step in the reconstruction is associating the reconstructed tracks in the  
 2780 HPgTPC to the clusters formed in the ECal and muon system. The `TPCECALAssociation`  
 2781 module checks first the position of the track end points, considering only the points  
 2782 that are at least 215 cm away from the cathode or have a radial distance to the center

## 6.2. $dE/dx$ MEASUREMENT IN THE TPC

2783 greater than 230 cm. The candidates are propagated up to the radial position, in the  
2784 case of clusters in the barrel, or the drift coordinate position, for the end cap cluster, of  
2785 the different clusters in the collection using the track parameters computed at the end  
2786 point. The end point is associated to the cluster if certain proximity criteria are met.  
2787 This module creates associations between the tracks, the end points and the clusters.  
2788 The criteria for the associations are slightly different for the ECal and the muon tagger.

### 2789 6.2 $dE/dx$ measurement in the TPC

2790 Among the parameters extracted from the track fitting, ionisation is particularly useful  
2791 for particle identification, as it is a function of the particle velocity. Although for the  
2792 case of relativistic particles this dependence is not very strong, measuring the track on  
2793 a large number of points may allow us to estimate the amount of ionisation accuratel.  
2794 This, paired with a measurement of the momentum, may allow us to identify the particle  
2795 type.

2796 The first calculation of the energy loss per unit length of relativistic particles using a  
2797 quantum-mechanical treatment is due to Bethe [151]. Using this approach, the mean  
2798 ionisation rate of a charged particle traveling through a material medium is (using  
2799 natural units  $G = \hbar = c = 1$ ):

$$\left\langle \frac{dE}{dx} \right\rangle = \frac{4\pi Ne^4}{m_e \beta^2} z^2 \left( \log \frac{2m_e \beta^2 \gamma^2}{I} - \beta^2 \right), \quad (6.1)$$

2800 where  $N$  is the number density of electrons in the medium,  $e$  the elementary charge,  $m_e$   
2801 is the electron mass,  $z$  the charge of the particle in units of  $e$ ,  $\beta$  is the velocity of the  
2802 particle,  $\gamma = (1 - \beta^2)^{-1}$  and  $I$  denotes the effective ionisation potential averaged over  
2803 all electrons. This relation is known as the Bethe-Bloch formula.

2804 From Eq. (6.1) one can see that the ionisation loss does not depend explicitly on  
2805 the mass of the charged particle, that for non-relativistic velocities it falls as  $\beta^{-2}$ , then  
2806 goes through a minimum and increases as the logarithm of  $\gamma$ . This behaviour at high  
2807 velocities is commonly known as the relativistic rise. The physical origin of this effect

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2808 is partly due to the fact that the transverse electromagnetic field of the particle is  
2809 proportional to  $\gamma$ , therefore as it increases so does the cross section.

2810 It was later understood that the relativistic rise could not grow indefinitely with  $\gamma$ .  
2811 A way to add this feature in the Bethe-Bloch formula is by introducing the so-called  
2812 density effect term. It accounts for the polarisation effect of the atoms in the medium,  
2813 which effectively shield the electromagnetic field of the charged particle halting any  
2814 further increase of the energy loss [152]. Denoting the correction as  $\delta(\beta)$ , one can rewrite  
2815 Eq. (6.1) as:

$$\left\langle \frac{dE}{dx} \right\rangle = \frac{4\pi Ne^4}{m_e \beta^2} z^2 \left( \log \frac{2m_e \beta^2 \gamma^2}{I} - \beta^2 - \frac{\delta(\beta)}{2} \right). \quad (6.2)$$

2816 In general, the form of  $\delta(\beta)$  depends on the medium and its state of aggregation,  
2817 involving the usage of tabulated parameters and implicit relations [153].

2818 Another standard method to compute the amount of ionisation a charged particle  
2819 produces is the so-called photo-absorption ionisation (PAI) model proposed by Allison  
2820 and Cobb [154]. Within their approach, the mean ionisation is evaluated using a  
2821 semiclassical calculation in which one characterises the continuum material medium by  
2822 means of a complex dielectric constant  $\varepsilon(k, \omega)$ . However, in order to model the dielectric  
2823 constant they rely on the quantum-mechanical picture of photon absorption and collision.  
2824 Therefore, in the PAI model the computation of the ionisation loss involves a numerical  
2825 integration of the measured photo-absorption cross-section for the relevant material.

2826 In a particle physics experiment, the typical way of determining the energy loss  
2827 per unit length as a function of the particle velocity is studying identified particles  
2828 over a range of momenta. Once we have established this relation we can use it for  
2829 other, unknown particles. In this sense, it makes sense to have a regular mathematical  
2830 expression for this relation that one can use.

2831 It happens that neither the Bethe-Bloch theory nor the PAI model from Allison and  
2832 Cobb offer a close mathematical form for the ionisation curve. This is the reason why a  
2833 full parametrisation of the ionisation curves can be useful. A parametrisation originally  
2834 proposed for the ALEPH TPC [155] and later used by the ALICE TPC [156] group that

## 6.2. dE/dx MEASUREMENT IN THE TPC

2835 manages to capture the features of the ionisation energy loss is:

$$f(\beta\gamma) = \frac{P_1}{\beta^{P_4}} \left( P_2 - \beta^{P_4} - \log \left[ P_3 + \frac{1}{(\beta\gamma)^{P_5}} \right] \right), \quad (6.3)$$

2836 where  $P_i$  are five free parameters. Hereafter, we will refer to Eq. (6.3) as the ALEPH

2837 dE/dx parametrisation.

### 2838 6.2.1 Energy calibration

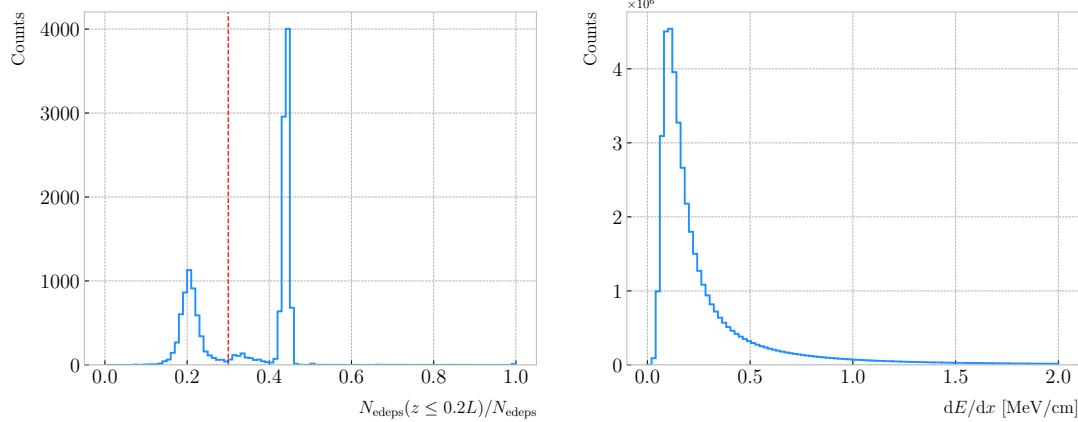
2839 In order to obtain the amount of energy loss by a charged particle due to ionisation  
2840 in our TPC we need to determine the conversion between the charge deposited in our  
2841 readout planes and the actual energy depositions. This procedure is known as energy  
2842 calibration.

2843 In a general, the first step of the calibration involves a non-uniformity correction,  
2844 to make sure that the detector response is uniform throughout the TPC. These are  
2845 typically divided into three categories, non-uniformities in the transverse  $YZ$  plane,  
2846 non-uniformities along the drift direction  $X$  and variations of the detector response  
2847 over time (would not apply to us as the detector is not built yet). These would correct  
2848 for effects such as electron diffusion and attenuation, space charge effects or channel  
2849 misconfiguration. However, because at the moment I am only interested in making sure  
2850 we recover a sensible result from our simulation, I will not apply uniformity corrections  
2851 to our charge deposits.

2852 Other effects, like electron-ion recombination or ADC saturation, lead to a non-linear  
2853 relation between the observed charge and the deposited energy in the detector, with the  
2854 observed readout charge saturating at high ionisation energies. In this case, because we  
2855 are dealing with gaseous argon and therefore recombination is not as important as in  
2856 liquid, we do not simulate recombination effects in the TPC. Even so, the simulation of  
2857 the electronic response will still introduce charge saturation, and one needs to correct  
2858 for it in order to obtain the exact amount of energy loss due to ionisation.

2859 By default, the track fitting algorithm in GArSoft provides a `TrackIonization`

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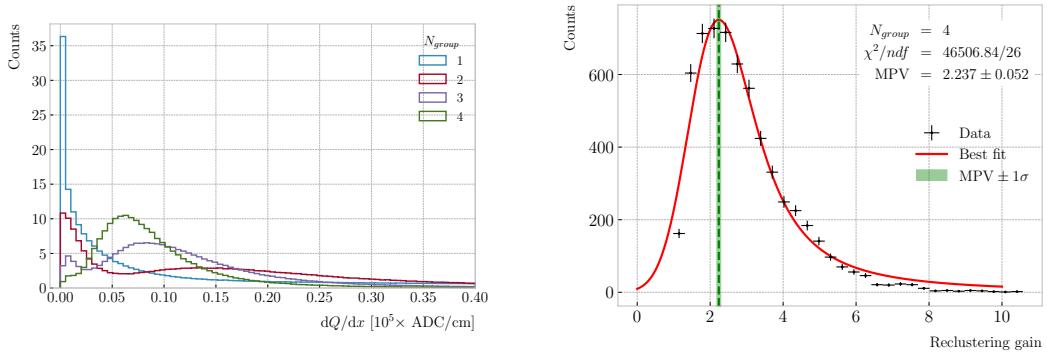
**Figure 6.2:** Left panel: distribution of the fraction of Geant4-level energy deposits per track with residual range less than 20% of the total track length, for the isotropic proton sample. Right panel: distribution of the ionisation per unit length of the energy deposits in the proton sample after removing the tracks with less than 30% of their energy deposits in the last 20% of the track.

object associated to each reconstructed track. It contains two collections of charge deposits, one for each fitting direction, consisting on pairs of charge values ( $dQ$ , in ADC) and step sizes ( $dx$ , in cm).

In order to estimate the ionisation loss in the ND-GAr TPC, I have used an MC sample consisting of single, isotropic protons propagating in the TPC. The starting points of the protons were sampled inside a  $50 \times 50 \times 25$  cm box centered at  $(100, -150, 1250)$ , and their momenta are uniformly distributed in the range  $0.25 - 1.75$  GeV. I ran the simulated sample through GArSoft's default detector simulation and reconstruction, and then a custom analyser module that extracts the ionisation data together with other reconstructed track information from the Kalman fit.

For studying the energy loss of the protons I select the reconstructed tracks that range out (i.e. slow down to rest) inside the TPC. A characteristic feature of the energy loss profile of any stopping ionising particle is the so-called Bragg peak, a pronounced peak that occurs immediately before the particle comes to rest. From Eq. (6.1) we can see that this behaviour is expected, as the energy loss for non-relativistic particles is inversely proportional to  $\beta^2$ . In data, a way of identifying the Bragg peak, and thus select the stopping particles, is checking the number of energy deposits towards the

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**Figure 6.3:** Left panel: distribution of the reconstructed ionisation charge per unit length for our MC stopping proton sample. The different colors indicate how many consecutive  $dQ/dx$  pairs were grouped together. Right panel: distribution of the median change in  $dQ/dx$  per track after  $N_{group} = 4$  clusters were reclustered together.

2877 end of the track. In this case, I count the fraction of the Geant4 simulated energy  
 2878 deposits with a residual range value (the distance from a given energy deposit to the  
 2879 last deposit in the track trajectory) less than a 20% of the corresponding track length<sup>2</sup>.  
 2880 The distribution of this fraction of energy deposits for our proton sample is shown in  
 2881 Fig. 6.2 (left panel). We can clearly see two well separated peaks in this distribution,  
 2882 one centered at 0.2 and another, narrower, one centered at a higher value. The first  
 2883 one corresponds to non-stopping protons, as in that case the number of energy deposits  
 2884 towards the end of the track is uniformly distributed due to the absence of the Bragg  
 2885 peak. In that way, I apply a cut in this distribution, requiring that at least 30% of the  
 2886 simulated energy deposits sit in the last 20% of the tracks, to ensure that the Bragg  
 2887 peak is present.

2888 Figure 6.2 (right panel) shows the distribution of the energy loss per unit length for  
 2889 the Geant4 simulated energy deposits of the selected stopping protons. We can see that  
 2890 it follows the expected shape of a Landau distribution, which describes the fluctuations of  
 2891 the ionisation energy losses [157]. This distribution has a characteristic asymmetric PDF,  
 2892 with a long right tail that translates into a high probability for high-energy ionisation  
 2893 losses. The origin of these fluctuations is mainly the possibility of transferring a high

<sup>2</sup>As we are applying this selection at the Geant4 level we could have simply selected the stopping protons using the `EndProcess` labels from the simulation. However, the Bragg peak identification method displayed here could serve as a starting point for a selection of stopping protons in real data.

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2894 enough energy to an electron, so it becomes a ionising particle itself.

2895 Now, from the point of view of the reconstruction, the objects that we have available  
 2896 to extract the ionisation information for the different reconstructed tracks are the  
 2897 collections of  $dQ$  and  $dx$  pairs, as stated before. The  $dQ$  values come from adding up  
 2898 the amplitude of all the reconstructed hits in a cluster, which is the input object to the  
 2899 Kalman fit.

2900 Figure 6.3 (left panel) shows the distribution of the ionisation charge deposits  
 2901 per unit length for the track in the stopping proton sample (blue line). As one can  
 2902 notice, this distribution does not resemble the expected shape of the Landau PDF. This  
 2903 distribution peaks sharply at 0 and has a heavy tailed behaviour. Notice, however, how  
 2904 the distribution changes its shape as we group together  $N_{group}$  consecutive charge deposit  
 2905 pairs (red, purple and green lines). The distribution in the  $N_{group} = 4$  case already has  
 2906 a shape which resembles that of the Geant4-level ionisation per unit length, so I will  
 2907 proceed using this amount of reclustering for the reconstruction-level depositions.

2908 An extra factor I need to account for, when reclustering is applied, is how the overall  
 2909  $dQ/dx$  per track changes. To do so, we can look at the ratio between the median  $dQ/dx$   
 2910 after and before the reclustering. Figure 6.3 (right panel) shows the median enhancement  
 2911 in  $dQ/dx$  per track for the stopping proton sample in the case  $N_{group} = 4$ . Fitting a  
 2912 Landau distribution convolved with a Gaussian<sup>3</sup>, I estimate the most probable value of  
 2913 this ratio to be  $G_{group} = 2.24 \pm 0.05$ .

2914 At this point, I am left with determining the conversion between the charge deposits  
 2915 per unit length  $dQ/dx$  and the energy deposits per unit length  $dE/dx$ . To this end, we  
 2916 need a way of comparing the two. I can use the residual range  $z$  to get a prediction of  
 2917 the most probable  $dE/dx$  by using the following empirical parametrisation [158]:

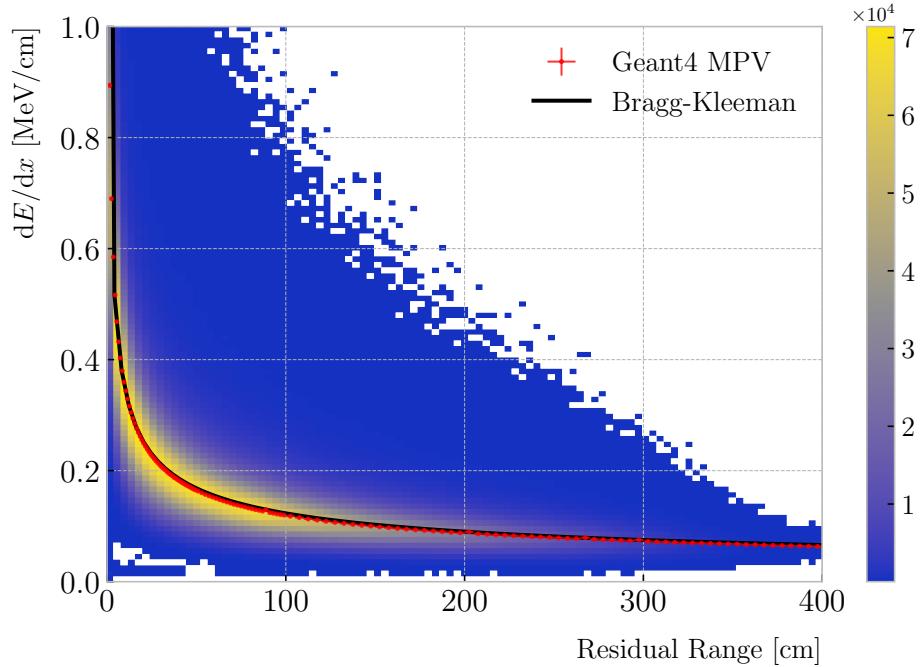
$$\frac{dE}{dx}(z) = \frac{z^{\frac{1}{p}-1}}{p\Lambda^{\frac{1}{p}}}, \quad (6.4)$$

2918 which is quoted in the literature as the Bragg-Kleeman formula. In order to obtain the

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<sup>3</sup>In the literature, this distribution is often referred to as Landau+Gaussian or langau. In the following, I will use LanGauss to refer to such PDF.

## 6.2. $dE/dx$ MEASUREMENT IN THE TPC

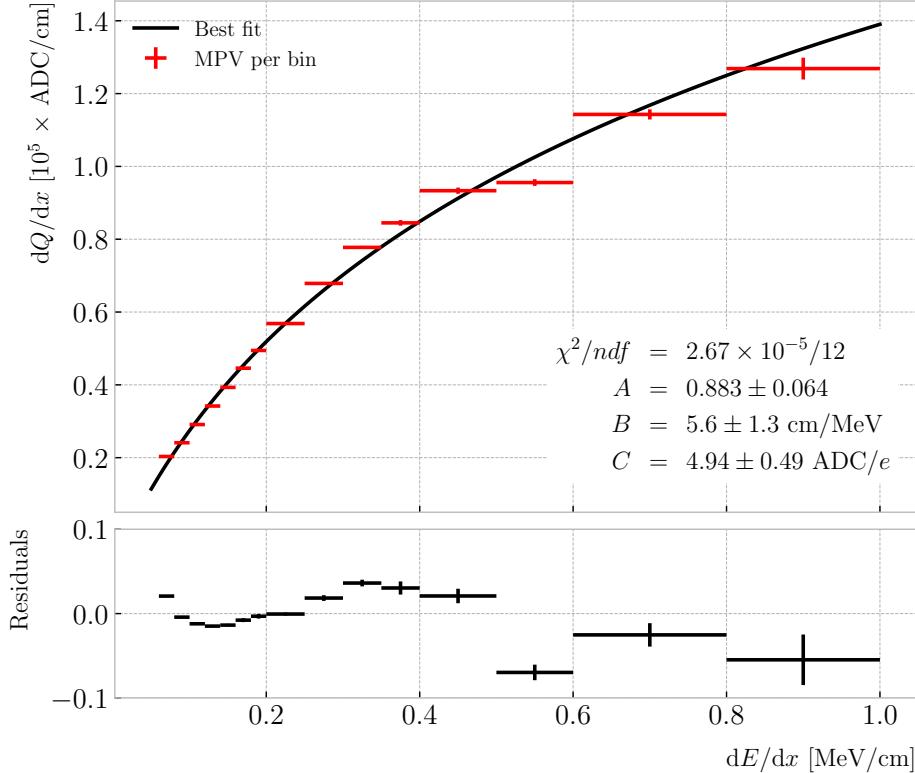


**Figure 6.4:** Distribution of the Geant4-simulated energy losses per unit length versus residual range for the stopping proton sample. The overlaid points represent the fitted most probable value of the  $dE/dx$  distribution in each residual range bin, whereas the curve is their best fit to the Bragg-Kleeman formula from Eq. (6.4).

2919  $p$  and  $\Lambda$  parameters I perform a fit using the energy losses and the residual ranges given  
 2920 by the Geant4 stage of our proton sample.

2921 Within our simulation, the residual range is sampled with a maximum size of  
 2922 5 mm. Therefore, to perform the fit to the Bragg-Kleeman formula, we can use a  
 2923 fine-grained residual range binning. For each of the residual range bins I extract the  
 2924  $dE/dx$  distribution and fit it to a LanGauss distribution, to obtain the value of the  
 2925 most probable  $dE/dx$  in the bin together with a statistical uncertainty. I then fit Eq.  
 2926 (6.4) to these most probable values and the centres of the residual range bins. This  
 2927 procedure is depicted in Fig. 6.4, where I show the distribution of the energy loss per  
 2928 unit length versus the residual range, together with the most probable  $dE/dx$  values  
 2929 and their uncertainty in each bin (red points) and the curve with the best fit of the  
 2930 Bragg-Kleeman relation to those values (black line). The best fit is obtained for the

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**Figure 6.5:** Fitted most probable  $dQ/dx$  values for each  $dE/dx$  bin (red points), obtained from the stopping proton sample. The overlaid curve (black line) represents the best fit to the logarithmic calibration function from Eq. (6.5).

2931 parameter values  $p = 1.8192 \pm 0.0005$  and  $\Lambda = 0.3497 \pm 0.0008 \text{ cm}/\text{MeV}^{p4}$ .

2932 Having an analytical expression that relates the residual range to  $dE/dx$ , I can take  
 2933 our reconstruction-level residual ranges from the stopping proton sample and compute  
 2934 the most probable energy loss associated.

2935 In order to parametrise the charge saturation, we can use the following logarithmic  
 2936 function inspired by the modified box model for recombination:

$$\frac{dE}{dx} = \frac{e^{\frac{dQ}{dx} B \frac{W_{ion}}{G_{group} C}} - A}{B}, \quad (6.5)$$

2937 where  $A$  and  $B$  are the calibration parameters we need to determine,  $W_{ion}$  is the average  
 2938 energy to produce an electron-ion pair,  $G_{group}$  is the gain from the reclustering discussed

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<sup>4</sup>These strange units for  $\Lambda$  come from dimensional analysis, just to keep the Bragg-Kleeman formula (6.4) consistent.

## 6.2. $dE/dx$ MEASUREMENT IN THE TPC

**Table 6.1:** Calibration parameters obtained from the fit of the ND-GAr simulated stopping proton sample to the calibration function from Eq. (6.5). The fits were performed for the 10, 12, and 16-bit ADC limits.

	$\chi^2/ndf$	Best fit $\pm 1\sigma$		
		$A$	$B$ (cm/MeV)	$C$ (ADC/e)
10-bit	$1.83 \times 10^{-6}/12$	$-9.3 \pm 3.9$	$270 \pm 69$	$27.1 \pm 5.4$
12-bit	$2.67 \times 10^{-5}/12$	$0.883 \pm 0.064$	$5.6 \pm 1.3$	$4.94 \pm 0.49$
16-bit	$1.44 \times 10^{-5}/12$	$0.949 \pm 0.024$	$3.53 \pm 0.58$	$4.52 \pm 0.29$

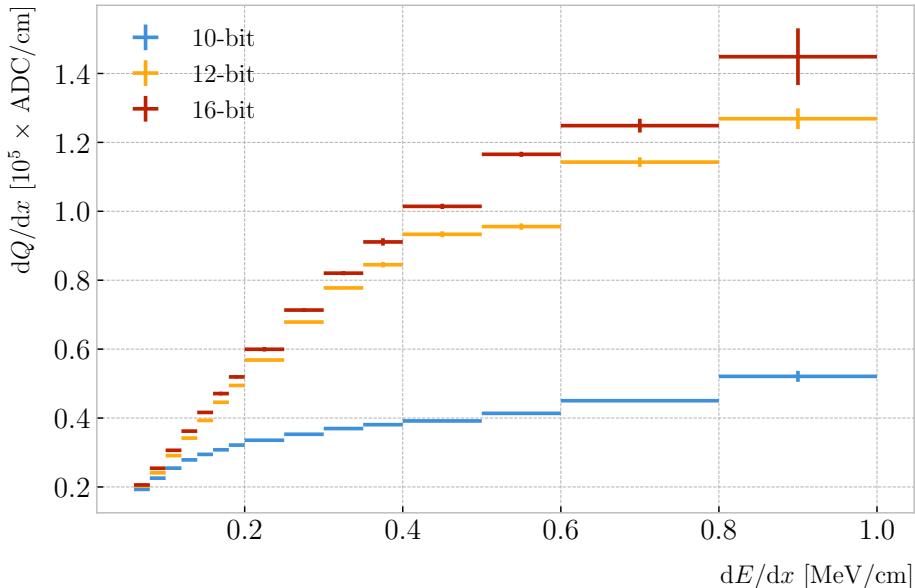
above and  $C$  is the calibration constant to convert number of electrons to ADC counts, commonly refer to as gain (also to be obtained in the fit). In this case, I use a value for the electron-ion production energy of  $W_{ion} = 26.4$  eV [159]. This value, used in our simulation as well, was measured for gaseous argon in normal conditions, and therefore should be checked in the future to describe correctly the high-pressure argon-CH<sub>4</sub> mixture of ND-GAr.

For the calibration fit I follow a procedure similar to the previous one for Eq. (6.4). Binning the  $dE/dx$  range, I fit a LanGauss distribution to the corresponding  $dQ/dx$  distribution to obtain the most probable value. The resulting data points (red bars) are shown in Fig. 6.5 (top panel), the horizontal error bars depict the width of the  $dE/dx$  bin whereas the vertical bars represent the error associated to the most probable value estimation. A fit to the logarithmic function in Eq. (6.5) is also shown (black line). For this I weighted the data points using the inverse of their relative error, obtaining a reduced chi-square value of  $\chi^2/ndf = 2.22 \times 10^{-6}$ . The best fit parameters I found from this fit are  $A = 0.883 \pm 0.064$ ,  $B = 5.6 \pm 1.3$  cm/MeV and  $C = 4.94 \pm 0.49$  ADC/e. Figure 6.5 (bottom panel) shows the residuals between the data points and the fit.

The value for the gain I obtained from the fit is in reasonable agreement with our expectation. This value is set in GArSoft to 5 ADC/e by default.

One interesting thing to check is what induces this non-linear relation between charge and energy. The only effects that modify the amount of electrons reaching the readout planes in the simulation are the transverse diffusion and the finite electron lifetime. Once the electrons reach the readout chambers, the pad response functions are applied,

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**Figure 6.6:** Fitted most probable  $dQ/dx$  values for each  $dE/dx$  bin for three different ADC bit limits, 10 (blue points), 12 (default, yellow points) and 16-bit (red points).

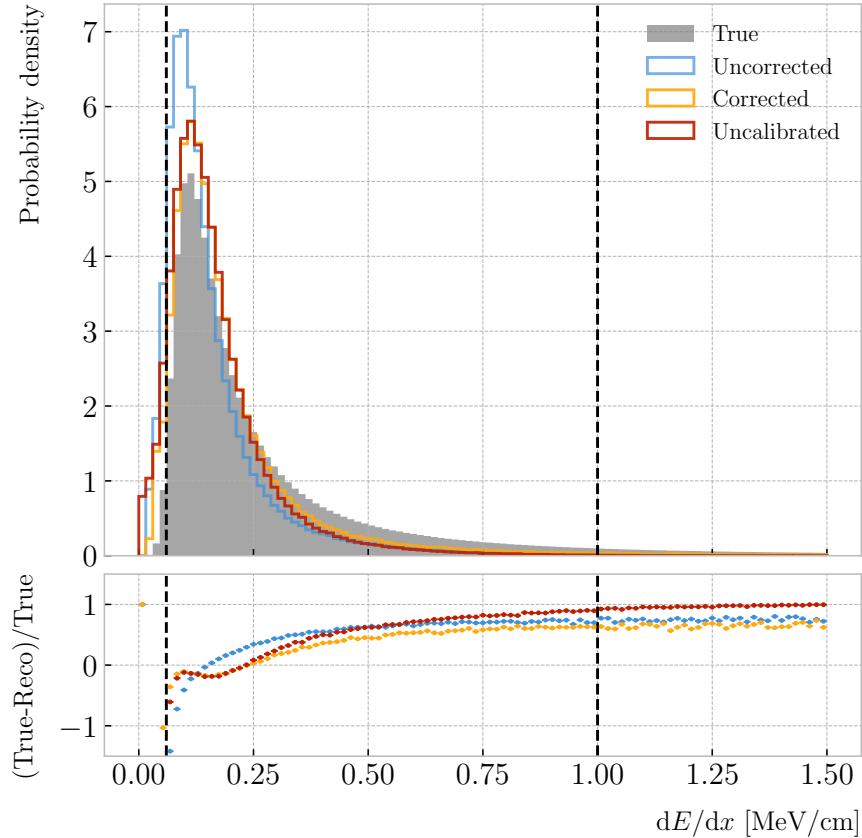
2961 together with an electrons-to-ADC conversion and the ADC saturation limit.

2962 By default, GArSot applies a 12-bit ADC limit, which can be changed in the  
 2963 simulation configuration. However, it can only be increased up to 16-bit, as we represent  
 2964 the ADC collection as a `std::vector<short>`. This way, I tried to change the saturation  
 2965 parameter to see how it affects the relation between reconstructed charge and energy.  
 2966 Figure 6.6 shows a comparison between the most probable  $dQ/dx$  for 10, 12 and 16-  
 2967 bit ADC limits. As expected, the lower the limit is the sooner the charge saturates.  
 2968 For higher ADC limits the relation between energy and charge remains linear up to  
 2969 higher  $dE/dx$  values, but even for the 16-bit limit the saturation is noticeable for values  
 2970  $\gtrsim 0.5$  MeV/cm.

2971 Table 6.1 shows the results of fitting the samples with 10 and 16-bits ADC limits to  
 2972 the calibration function from Eq. (6.5), using the weights based on their relative error  
 2973 as described previously. One interesting feature to notice is how different the best fit  
 2974 points look for the 10-bit ADC saturation when compared to the other two, which are  
 2975 consistent with each other.

2976 At this point we can compare the  $dE/dx$  distribution one gets from Geant4, i.e. the

## 6.2. $dE/dx$ MEASUREMENT IN THE TPC



**Figure 6.7:** Top panel: area normalised  $dE/dx$  distributions for the true (solid grey) and the reconstructed energy deposits in the stopping proton sample, both after applying the calibration (blue) and the calibration and the normalisation correction (yellow). Also shown is the distribution obtained by applying a correction factor to the  $dQ/dx$  values but not the calibration (red). Bottom panel: fractional residuals for the uncorrected (blue), corrected (yellow) and uncalibrated (red) samples.

2977 true energy loss distribution, and the distribution I found by applying the calibration  
 2978 function to our collection of reconstructed  $dQ/dx$  values. Figure 6.7 (top panel) shows  
 2979 the true (solid grey) and reconstructed (blue, labeled as uncorrected) distributions  
 2980 together. The dashed vertical lines indicate the region of validity of the calibration fit, i.e.  
 2981 the left and right edges of the first and last  $dE/dx$  bin respectively. Notice that these  
 2982 histograms are area-normalised, as the total number of true energy deposits is much  
 2983 higher than the number of reconstructed charge deposits. This is due to a combination  
 2984 of effects, like the finite spatial resolution of the detector, the hit clustering used in the  
 2985 track fitting and the reclustering we have applied here.

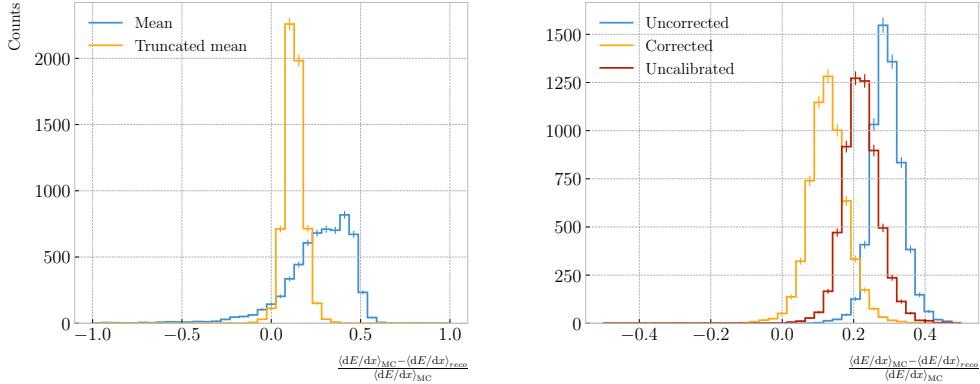
## CHAPTER 6. PARTICLE ID IN ND-GAr

2986        The two distributions are significantly different. That can be seen clearly when  
2987        looking at the fractional residuals, shown in Fig. 6.7 (bottom panel). In particular,  
2988        the position of the peak is off, which could bias the mean energy loss predictions. It  
2989        seems like the difference between these may be due to an overall scaling factor. One  
2990        possibility is to scale the most probable value of the reconstructed distribution to  
2991        the most probable value predicted by Geant4. I do this by fitting both distributions  
2992        using a LanGauss function, obtaining  $dE/dx_{MPV, true} = 0.1145 \pm 0.0005$  MeV/cm and  
2993         $dE/dx_{MPV, reco} = 0.0928 \pm 0.0005$  MeV/cm for the true and reconstructed most probable  
2994        values respectively. These can be translated into an scaling factor  $S = 0.579 \pm 0.006$ .

2995        The result of applying the scaling correction can be seen in Fig. 6.7 (top panel).  
2996        The corrected  $dE/dx$  distribution (yellow, labeled as corrected) peaks around the same  
2997        value the true distribution does, as expected. Moreover, the high energy region is also  
2998        slightly better described. For low ionisations, below the lower limit of the calibration  
2999        fit, the differences between true and reconstructed are still significant. This low energy  
3000        excess may be migration of some events from the peak region. The overall effect of the  
3001        correction can be seen in the fractional residual plot in Fig. 6.7 (bottom panel).

3002        One can also check what happens if instead of applying the logarithmic calibration we  
3003        simply scale the  $dQ/dx$  distribution (post reclustering) to have the same most probable  
3004        value as the true  $dE/dx$  distribution. In this case, following an analogous procedure to the  
3005        one described earlier, I found the scaling factor  $S_{uncalibrated} = 0.414 \pm 0.002$  MeV/ADC<sup>5</sup>.  
3006        The resulting distribution (red, labeled as uncalibrated) is also shown in in Fig. 6.7 (top  
3007        panel). The behaviour of the new distribution is similar to the corrected case at low  
3008        energy losses, around the peak of the true distribution, but it is worse at describing the  
3009        high energy tail. This is expected, it is in the high ionisation regime where saturation  
3010        effects apply and therefore calibration is needed.

## 6.2. $dE/dx$ MEASUREMENT IN THE TPC



**Figure 6.8:** Left panel: fractional residuals between the true and the corrected  $dE/dx$  means (blue) and the 60% truncated means (yellow), for each event in the stopping proton sample. Right panel: fractional residuals between the true and the uncorrected (blue), corrected (yellow) and uncalibrated (red)  $dE/dx$  60% truncated means, for each event in the stopping proton sample.

### 3011 6.2.2 Truncated $dE/dx$ mean

3012 Once we have a collection of  $dE/dx$  values for each reconstructed track, we can compute  
 3013 the corresponding most probable ionisation loss per unit length of the particle. This  
 3014 is the value predicted by the Bethe-Bloch or the PAI models, and together with a  
 3015 measurement of the momentum it allows for particle identification.

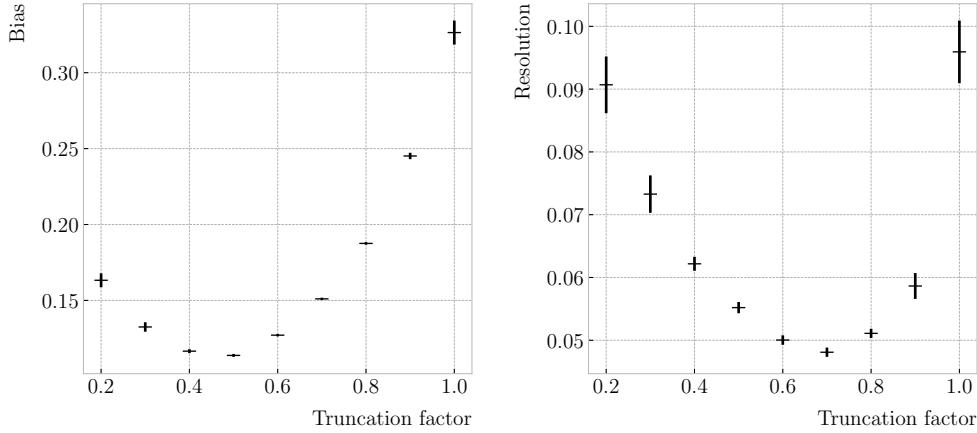
3016 However, estimating the most probable  $dE/dx$  value for each reconstructed track  
 3017 is not a trivial task. As mentioned before, the  $dE/dx$  distributions follow Landau-like  
 3018 distributions. Therefore, one should perform e.g. a LanGauss fit to correctly estimate  
 3019 the most probable values. Automating this kind of fits is often problematic, as they  
 3020 usually incur in convergence problems. Moreover, the reconstructed  $dE/dx$  distributions  
 3021 we obtain tend to have relatively small statistics, which may also produce poor fits. In  
 3022 practice, doing these unsupervised fits may degrade our performance, and a more robust  
 3023 method is preferred.

3024 A possibility could be taking the mean of the reconstructed  $dE/dx$  distribution for  
 3025 each particle. The problem with this approach is that the high energy Landau tail,  
 3026 combined with our limited statistics, can induce large fluctuations in the computation

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<sup>5</sup>Notice that now the scaling factor is not dimensionless, as it acts more like a conversion factor here.

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**Figure 6.9:** Estimated values of the mean  $dE/dx$  bias (left panel) and resolution (right panel) obtained using the corrected data from the stopping proton sample, for different values of the truncation factor.

of the mean. Imagine you have two protons with the same kinetic energy, but due to reconstruction problems in one case you did not get as many charge deposits reconstructed in its high ionisation loss region. If you do not remove the tails the computed  $dE/dx$  means will be significantly different.

In order to avoid those fluctuations, one can compute the mean of a truncated  $dE/dx$  distribution instead. By keeping only a given fraction of the lowest energy deposits we obtain an estimate of the mean energy loss that is more resilient to reconstruction inefficiencies and statistical effects. Figure 6.8 (left panel) shows a comparison between the  $\langle dE/dx \rangle$  computed by taking the mean of the full distribution (blue line) and the 60% lowest energy clusters (yellow line), for the stopping proton sample. The fractional residuals are computed for each proton, taking the corresponding means using their collections of true and reconstructed energy deposits. One can see that using the simple mean translates into a high bias and uncertainty in the  $\langle dE/dx \rangle$  estimation, whereas applying the truncation reduces both significantly.

Additionally, I performed a comparison between the 60% truncated mean  $dE/dx$  obtained using the different calibration methods discussed earlier, namely the uncorrected (blue), corrected (yellow) and uncalibrated (red) distributions. The results are shown in Fig. 6.8 (right panel). While the widths of these distributions are similar, the bias

## 6.2. $dE/dx$ MEASUREMENT IN THE TPC

3045 obtained for the corrected sample, i.e. calibration function and correction factor applied,  
 3046 is a factor of  $\sim 2$  lower than in the uncalibrated case and almost three times smaller  
 3047 than for the uncorrected sample.

3048 The next step is to optimise the level of truncation we are going to apply to our  
 3049 data. To do so, I used different truncation factors, i.e. the percentage of energy-ordered  
 3050 reconstructed energy deposits we keep to compute the mean, on the corrected  $dE/dx$   
 3051 sample of the stopping protons. Then, following the same procedure of computing the  
 3052 fractional residuals as before, I fitted the resulting histograms using a double Gaussian  
 3053 function. This is simply the sum of two Gaussian functions of the type:

$$g(x; \mu, \sigma, A) = A e^{-\frac{(x-\mu)^2}{2\sigma^2}}. \quad (6.6)$$

3054 I do not add the classical normalisation factor of the Gaussian,  $1/\sqrt{2\pi}\sigma$ , therefore  
 3055 the amplitude  $A$  simply represents the maximum of the function. One of the two  
 3056 Gaussian functions describes the core part of the distribution, while the other captures  
 3057 the behaviour of the tails.

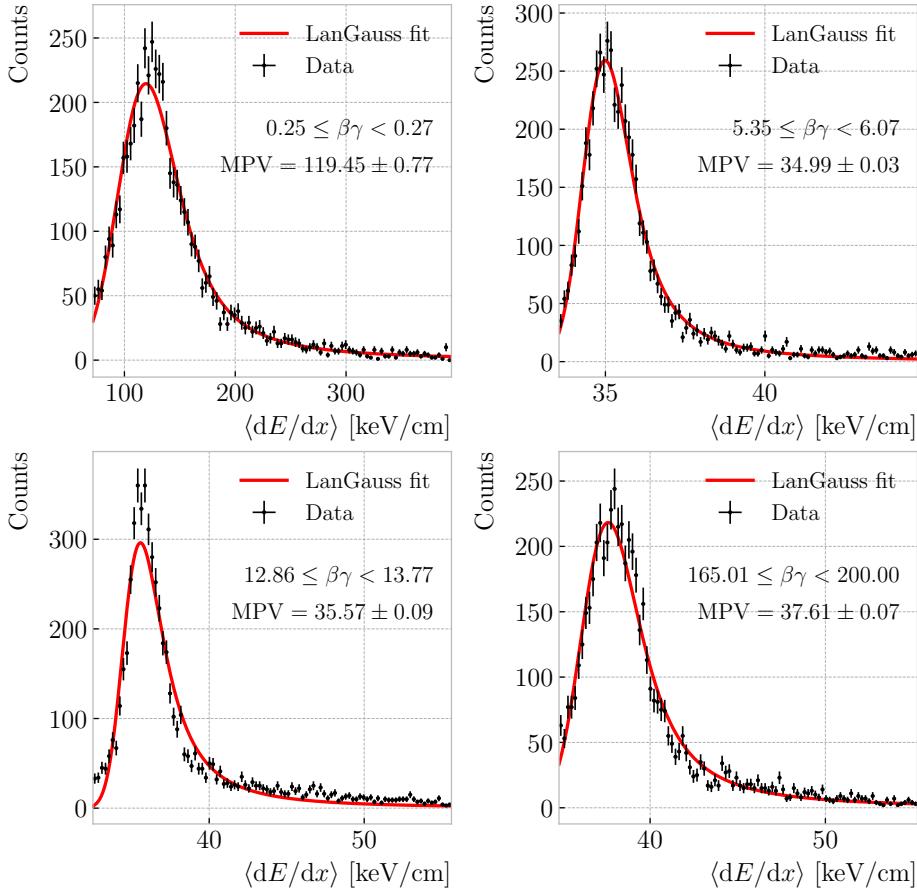
3058 For each truncation factor, I look at the bias and the resolution I obtain. I define  
 3059 these as the weighted means of the corresponding parameters in the fits:

$$\bar{x} = \frac{A_{core} x_{core} + A_{tail} x_{tail}}{A_{core} + A_{tail}}, \quad (6.7)$$

3060 where  $A_{core}$  and  $A_{tail}$  are the amplitudes of the core and tail distributions respectively  
 3061 and  $x$  is either the mean  $\mu$  or the width  $\sigma$  of said distributions.

3062 Figure 6.9 shows the bias (left panel) and the resolution (right panel) I obtained  
 3063 for the stopping proton sample, using different values of the truncation. From these, it  
 3064 can be seen that a truncation factor of 50% minimises the bias in the estimation, while  
 3065 70% gives the best resolution. That way, I settled on the intermediate value of 60%  
 3066 truncation, which yields a  $\langle dE/dx \rangle$  resolution of  $5.00 \pm 0.08$  % for stopping protons.

## CHAPTER 6. PARTICLE ID IN ND-GAr



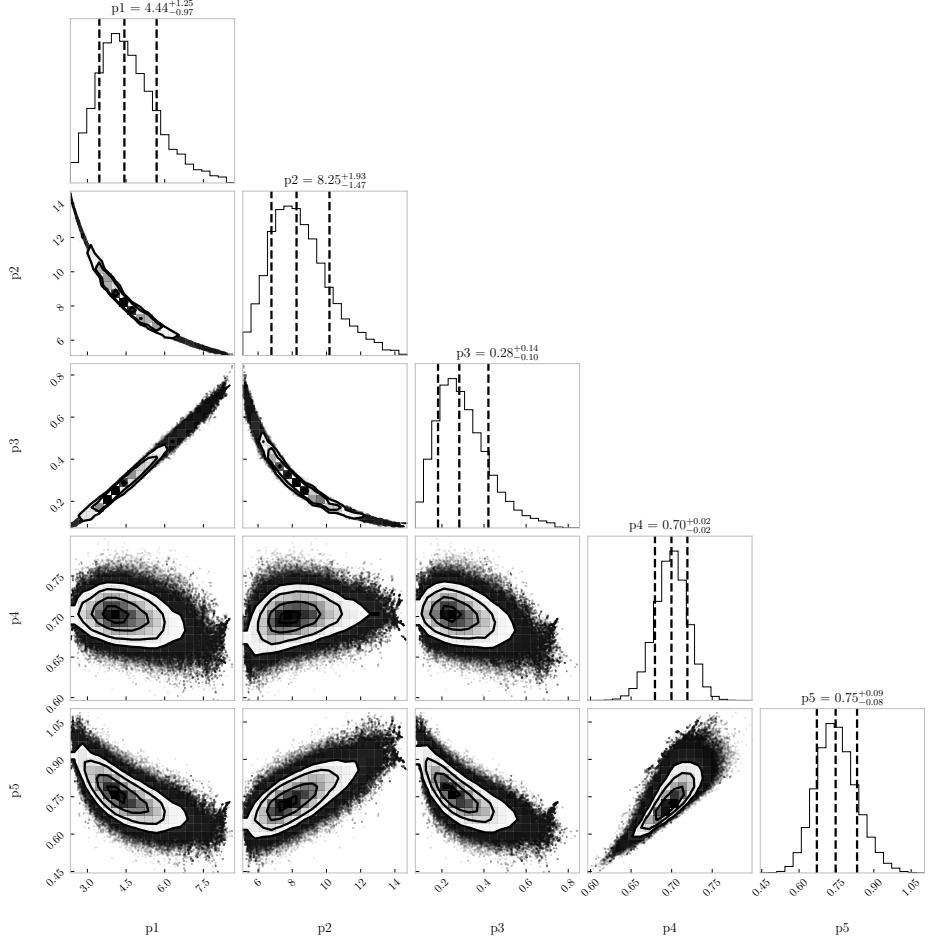
**Figure 6.10:** Examples of the truncated mean  $dE/dx$  LanGauss fits for various  $\beta\gamma$  bins, from a simulated FHC neutrino sample.

### 3067 6.2.3 Mean $dE/dx$ parametrisation

3068 Now that we have a way to estimate the mean energy loss of a particle in the HPgTPC,  
 3069 we can determine the value of the free parameters in the ALEPH formula, Eq. (6.3).  
 3070 For this, I used a sample of  $10^5$  reconstructed FHC neutrino events inside ND-GAr. In  
 3071 this case I cannot use the stopping proton sample, as we need to cover the full kinematic  
 3072 range of interest for the neutrino interactions in our detector.

3073 The original data does not contain an estimation of the velocity of the tracks, instead  
 3074 the tracks have a value for the reconstructed momentum and the associated PDG code  
 3075 of the Geant4-level particle that created the track. Therefore, one can select some of the  
 3076 particles in the data, in this case I selected electrons, muons, pions and protons, and

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**Figure 6.11:** Resulting one and two dimensional projections of the posterior probability distributions of the ALEPH  $\langle dE/dx \rangle$  parameters obtained by fitting the 60% truncated mean  $dE/dx$  values from a FHC neutrino sample in ND-GAr. The vertical dashed lines in the 1D distributions represent the 16th, 50th and 84th percentiles.

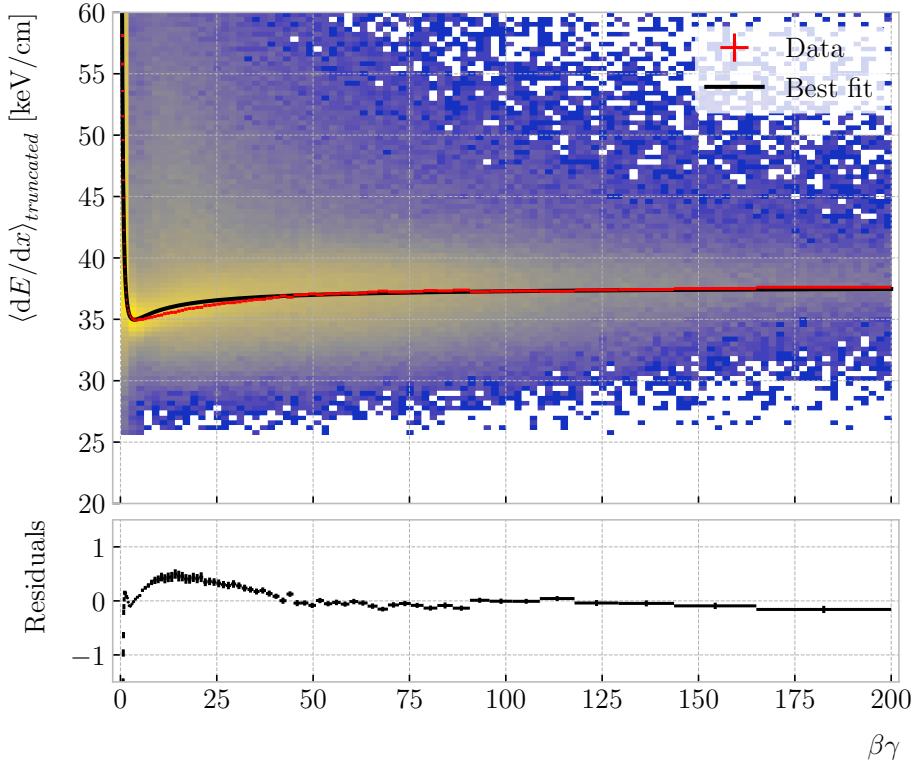
3077 compute  $\beta$  and  $\gamma$  using the reconstructed momentum and their mass. In terms of  $\beta\gamma$   
 3078 the mean  $dE/dx$  does not depend on the particle species, so one can consider all the  
 3079 dataset as a whole. For this fit, I will express  $\beta$  in terms of the  $\beta\gamma$  product as:

$$\beta = \frac{\beta\gamma}{\sqrt{1 + (\beta\gamma)^2}}, \quad (6.8)$$

3080 which can be easily proven from the definition of  $\gamma$ .

3081 Next, I bin the data in  $\beta\gamma$ . I chose a fine binning so as to capture the different  
 3082 features of the ionisation curve. Instead of fixing the bin width, I select them so each one

## CHAPTER 6. PARTICLE ID IN ND-GAr

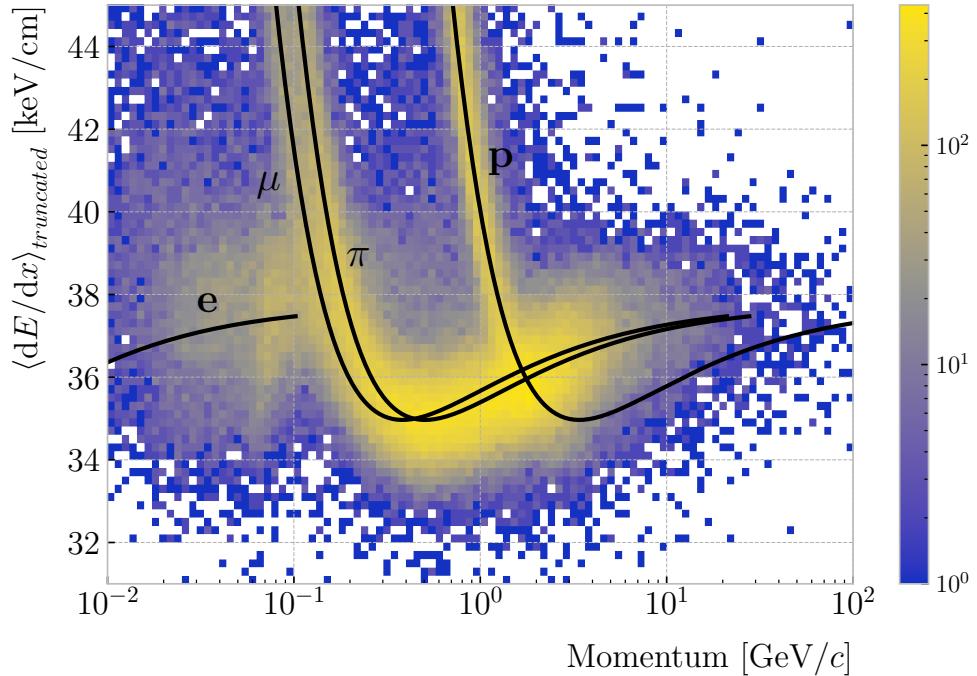


**Figure 6.12:** Truncated mean  $dE/dx$  obtained for the FHC neutrino sample as a function of the  $\beta\gamma$  product (upper panel). Also shown are the fitted most probable values for each  $\beta\gamma$  bin (red points) and the best fit obtained using the ALEPH parametrisation (black line). The residuals resulting from the fit are shown in the lower panel.

3083 has approximately the same statistics. Then, for each  $\beta\gamma$  slice, I compute the median  
 3084 and the interquartile range (IQR) of the  $\langle dE/dx \rangle$  distribution. Using these, I make a  
 3085 histogram in the range [median – IQR, median + 5 IQR], which I fit to a LanGauss  
 3086 function in order to extract the MPV. Using this range accounts for the asymmetric  
 3087 nature of the distributions, while also helps avoiding a second, lower maximum present  
 3088 at low  $\beta\gamma$ , probably a result of reconstruction failures.

3089 A few examples of these fits are shown in Fig. 6.10. The chosen values of  $\beta\gamma$  sit in  
 3090 very distinct points along the  $\langle dE/dx \rangle$  curve, going from the high ionisation region at  
 3091 low velocities (top left panel), to the minimum point (top right panel), the beginning of  
 3092 the relativistic rise (bottom left panel), and the plateau produced by the density effect  
 3093 (bottom right panel).

## 6.2. $dE/dx$ MEASUREMENT IN THE TPC

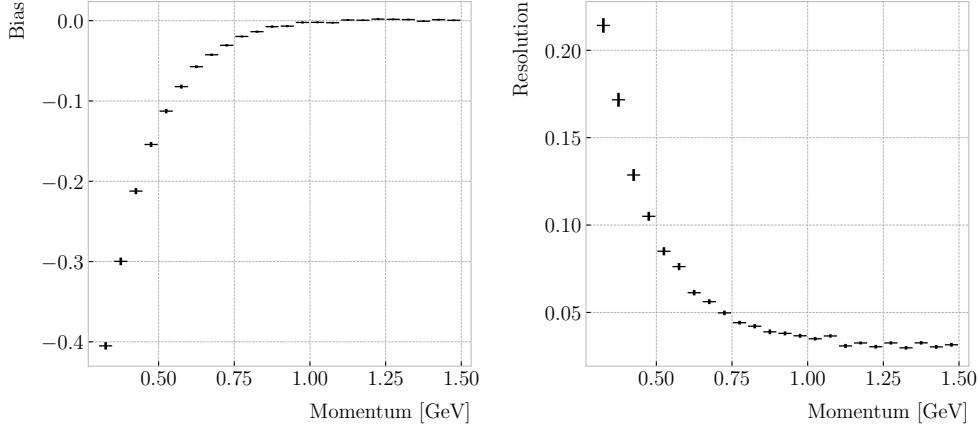


**Figure 6.13:** Distribution of the 60% truncated mean  $dE/dx$  versus reconstructed momentum for the FHC neutrino sample. The black lines indicate the predictions of the ALEPH parametrisation for electrons, muons, charged pions and protons.

3094 I used the resulting most probable  $\langle dE/dx \rangle$  values and the centres of the  $\beta\gamma$  bins as  
 3095 the points to fit to the ALEPH formula. For this particular fit I used the least-squares  
 3096 method to get a first estimation of the ALEPH parameters. Applying some uniform  
 3097 priors, I then used these values as the starting point of a 100000 steps MCMC. Figure 6.11  
 3098 shows the posterior probability distributions I obtain for each parameter. The reported  
 3099 best fit points are based on the 16th, 50th, and 84th percentiles in the marginalised  
 3100 distributions.

3101 The resulting fit (black line), compared to the data points (red points) and the  
 3102 underlying distribution is shown in Fig. 6.12 (top panel). The overall fit is good, with a  
 3103 reduced chi-squared of  $\chi^2/ndf = 1.02$ . However, there are some regions where the fit  
 3104 does not describe the data correctly, like the very low  $\beta\gamma$  regime, where the fit severely  
 3105 underestimates for energy losses  $\gtrsim 50$  keV/cm, and the start of the relativistic raise,  
 3106 where we have a slight overestimation. This is a result of those points having a larger  
 3107 uncertainty when compared to the ones around the dip or the plateau areas. These

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**Figure 6.14:** Estimated values of the mean  $dE/dx$  bias (left panel) and resolution (right panel) obtained for the true protons in a FHC neutrino sample.

3108 differences can be better seen in the residual plot, Fig. 6.12 (bottom panel).

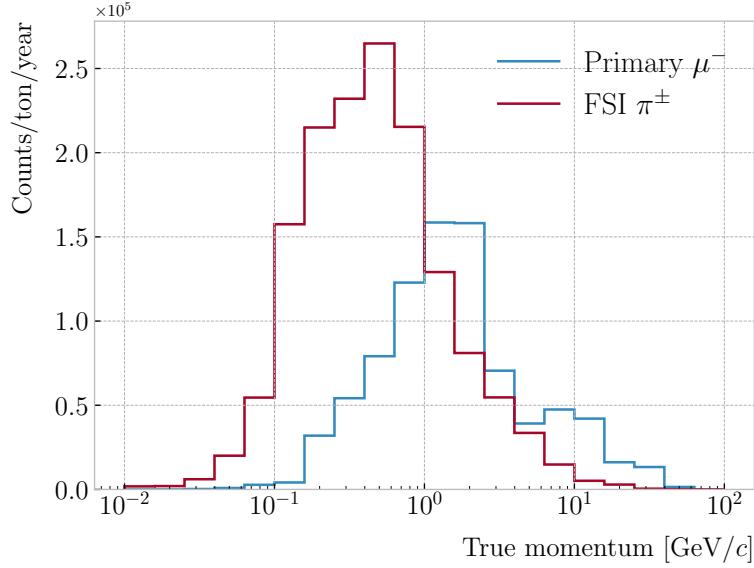
3109 **6.2.4 Particle identification**

3110 **6.3 Muon and pion separation in the ECal and MuID**

3111 As it could be seen from Fig. 6.13, it is not possible to separate muons and charged pions  
3112 in the HPgTPC using  $dE/dx$  for momenta  $\gtrsim 300 \text{ MeV}/c$ . In ND-GAr, approximately  
3113 70% of the interactions in FHC mode will be  $\nu_\mu$  CC (compared to the 47% of  $\bar{\nu}_\mu$  CC  
3114 interactions when operating in RHC mode), while 24% are neutral currents. Out of  
3115 these, around 53% and 47% of them will produce at least one charged pion in the final  
3116 state, respectively. Figure 6.15 shows a comparison between the spectra of the primary  
3117 muons and the charged pions for  $\nu_\mu$  CC interactions in ND-GAr producing one or more  
3118 charged pions. From this, one can see that (i) the majority of muons and charged pions  
3119 are not going to be distinguishable with a  $\langle dE/dx \rangle$  measurement, and that (ii) particle  
3120 identification is necessary both to classify correctly the  $\nu_\mu$  CC events and identify the  
3121 primary muon within them.

3122 ND-GAr features two other subdetectors which can provide additional information  
3123 for this task, namely the ECal and MuID. The current ECal design, described in (ref  
3124 section), consists of 42 layers, made of 5 mm of Pb, 7 mm of plastic scintillator and a

### 6.3. MUON AND PION SEPARATION IN THE ECAL AND MUID



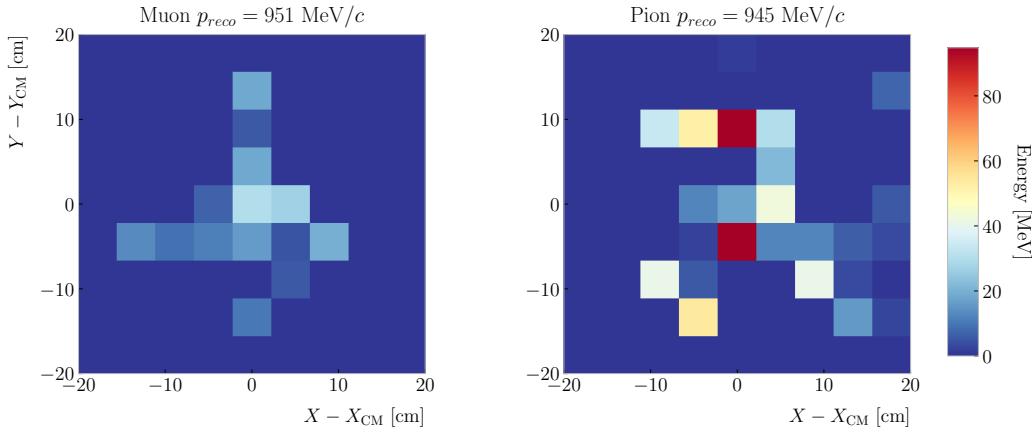
**Figure 6.15:** True momentum distribution for the primary muon in  $\nu_\mu$  CC  $N\pi^\pm$  interactions inside the fiducial volume of ND-GAr (blue line), compared to the post FSI charged pion spectrum (red line).

3125 1 mm PCB board. The total thickness of this calorimeter is 1.66 nuclear interaction  
 3126 lengths or 1.39 pion interaction lengths. The Muid design is in a more conceptual  
 3127 stage, however it is envisioned to feature layers with 10 cm of Fe and 2 cm of plastic  
 3128 scintillator<sup>6</sup>. With its three layers, it will have a thickness of 1.87 or 1.53 nuclear or pion  
 3129 interaction lengths, respectively.

3130 Because pion showers are dominated by inelastic nuclear interactions, the signatures  
 3131 of these particles in the calorimeter will look significantly different from those of muons.  
 3132 Although our ECal is not thick enough to fully contain the hadronic showers of the  
 3133 charged pions at their typical energies in FHC neutrino interactions, they can still be  
 3134 used to understand whether the original particle was more hadron-like or MIP-like. In  
 3135 Fig. 6.16 I show two examples of energy distributions created by a muon (left panel)  
 3136 and a charged pion (right panel) of similar momenta interacting in the ECal. These  
 3137 figures represent the transverse development of the interactions. For each of them, I  
 3138 computed the principal component and centre of mass of the interaction, projecting

<sup>6</sup>It is not mentioned anywhere, but I assume that there should also be another layer of PCB board of 1 mm. However, in this case its contribution to the total thickness of the sampling calorimeter would be negligible.

## CHAPTER 6. PARTICLE ID IN ND-GAr



**Figure 6.16:** Distributions of energy deposits in the ECal for a muon (left panel) and a charged pion (right panel) with similar momenta. The energy is projected onto the plane perpendicular to the principal component of the hits, and the positions are relative to the center of the interaction.

the position of the hits onto the plane perpendicular to that direction, and taking the distances relative to the centre. It can be seen that the muon follows an almost MIP-like behaviour, being the central bin in the histogram the one with the highest deposited energy. On the other hand, the pion not only deposits more energy overall, but also this energy is more spread-out among the different hits. It is this kind of information that would allow us to tell apart muons from pions.

This way, I identify three main action points that need to be addressed if one wants to use these detectors to distinguish between muons and charged pions. These are:

1. the way we make the associations between tracks in the HPgTPC to the activities (what in GArSoft we call clusters) in the ECal and the MuID,

2. what variables or features one can extract from the calorimeters that encapsulate the information we are interested about,

3. and how to carry out the classification problem.

### 6.3. MUON AND PION SEPARATION IN THE ECAL AND MUID

#### 3152 6.3.1 Track-ECal matching

3153 One of the main players in the muon and pion separation is the way we associate clusters  
3154 in the ECal to reconstructed tracks in the TPC. Missing some associations or making  
3155 wrong ones can bias the ECal quantities that we can use for classifying particles. The  
3156 current algorithm in GArSoft provides precise associations, i.e. most of the associations  
3157 that it produces are correct, but it appears to miss an important number of associations  
3158 (at least when using the default configuration).

3159 The current TPC track-ECal cluster association algorithm is divided in four parts.  
3160 It first checks whether the track end point fulfils certain conditions to be extrapolated.  
3161 There are two cut values in this step, one for the drift direction and other radial.

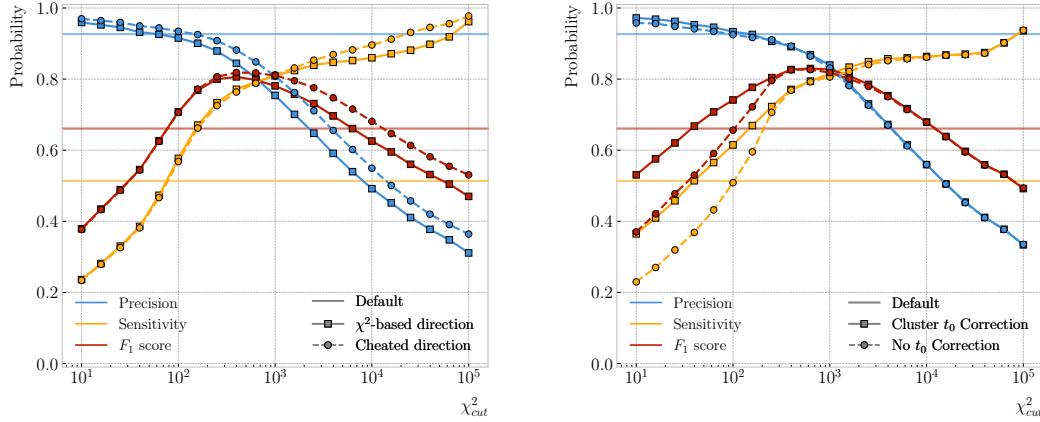
3162 If the point can be extrapolated, the code computes the coordinates of the centre  
3163 of curvature using the Kalman fit estimates at the track end ( $y$ ,  $z$ ,  $1/R$ ,  $\phi$ ,  $\tan\lambda$ ). It  
3164 then compares the distance between this and the cluster in the  $(z, y)$  plane with  $R$ . This  
3165 introduces another cut in the perpendicular direction.

3166 The next step is different for clusters in the barrel or in one of the end caps. If it  
3167 is a barrel cluster the algorithm extrapolates the track up to the radial distance of the  
3168 cluster. There are three possible outcomes, the extrapolated helix can cut the cylinder  
3169 of radius  $r_{clus}$  two, one or zero times. I get the cut point that is closer to the cluster and  
3170 check that it is either in the barrel or the end caps. Computing the difference between  
3171 the  $x$  coordinates of the cluster and the extrapolated point, the module checks that this  
3172 is not greater than a certain cut. If the cluster is in an end cap, I propagate the track  
3173 up to the  $x$  position of the cluster. Then, the algorithm computes the angle in the  $(z, y)$   
3174 plane between the centre of curvature and the cluster,  $\alpha$ , and the centre of curvature  
3175 and the propagated point,  $\alpha'$ . A cut is applied to the quantity  $(\alpha - \alpha')R$ .

3176 If the cluster contains more than a certain number  $N$  of hits, I apply an extra cut to  
3177 the dot product of the direction of the track at the propagated  $x$  value and the cluster  
3178 direction.

3179 The code makes sure to only associate one end of the track (if any) to a cluster.

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**Figure 6.17:** Left panel: comparison between the precision (blue), sensitivity (yellow) and  $F_1$  score (red) obtained for the default (horizontal lines) and new algorithms, both with the  $\chi^2$ -based direction estimator (squares) and cheating the directions (circles), for different values of the  $chi^2$  cut. Right panel: comparison of the performance of the new algorithm when applying the cluster  $t_0$  correction (squares) and when (circles).

3180 However, it can associate more than one track to the same cluster. This makes sense,  
3181 as different particles can contribute to the same cluster in the ECal, but it makes it  
3182 difficult to quantify the relative contributions of the tracks to a certain cluster.

3183 As a way of comparing the performance of this algorithm, a new, simpler association  
3184 module was written. The goal was to have a simple and robust algorithm, which depends  
3185 on as few parameters as possible and that can produce a one-to-one matching between  
3186 tracks and ECal clusters.

3187 For each reconstructed track, the new algorithms applies the same procedure to the  
3188 forward and the backward fits irrespective of their end point positions. It first gets the  
3189 Kalman fit parameters at the corresponding end point together with the  $X$  position,  $x_0$ ,  
3190 ( $y_0$ ,  $z_0$ ,  $1/R$ ,  $\phi_0$ ,  $\tan\lambda$ ).

3191 For each ECal cluster, I compute the radial distance to the centre of the TPC and  
3192 find the  $\phi$  value in the range  $[\phi_0, \phi_0 + \text{sign}(R)\phi_{max}]$  that makes the propagated helix  
3193 intersect with the circle defined with such radius. The  $(x, y, z)$  position of the helix for  
3194 the  $\phi$  value found (if any) is then computed. In case there are two intersections, I keep  
3195 the one that minimises the distance between  $(y, z)$  and  $(y_c, z_c)$ .

3196 I then calculate  $\chi^2$  value based on the Euclidean distance between the propagated

### 6.3. MUON AND PION SEPARATION IN THE ECAL AND MUID

3197 point and the cluster:

$$\chi^2/ndf = \frac{\sum_{n=0}^2 (x^{(n)} - x_c^{(n)})^2}{3}. \quad (6.9)$$

3198 If there was no intersection I store a  $-1$  instead. In the end, for each reconstructed track  
3199 in the event one ends up with two collections of  $\chi^2$  values, one for each ECal cluster  
3200 and fit directions.

3201 The current code only supports having ECal clusters associated to one end of each  
3202 track. We have two options to decide what track end to keep. The first one tries to  
3203 cheat the selection, looking at the distance between the two track ends and the true  
3204 start position of the associated MC particle. The second one keeps the track end with  
3205 more  $\chi^2$  entries below the cut.

3206 This feature of only considering one track end limits the algorithm, making it not  
3207 suitable for reconstructing events with particles originating outside the TPC. However,  
3208 as for the moment the main concern of the group is the study of neutrino interactions  
3209 off the gaseous argon, this is an acceptable assumption.

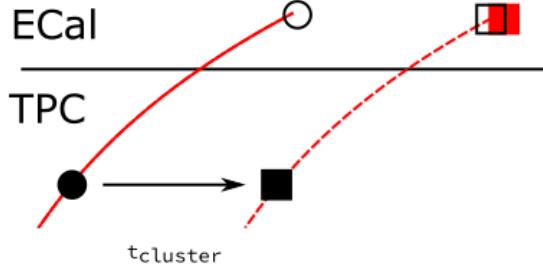
3210 In order to associate a cluster to a track, I take all clusters with a  $\chi^2$  value in the  
3211 range  $[0, \chi_{cut}^2]$ . If a cluster has been assigned to more than one track we leave it with  
3212 the one with the lowest  $\chi^2$ .

3213 This default behaviour of the algorithm can be modified to associate more than one  
3214 track to each cluster. Not only that, but the  $\chi^2$  values can be used to assign relative  
3215 weights to the different contributions.

3216 To evaluate the performance of the association method, I use a binary classification  
3217 approach. In this case, I check the leading MC Track IDs associated to the reconstructed  
3218 tracks and ECal clusters. I count an association as true positive (TP) if both Track  
3219 IDs coincide. An association is considered false positive (FP) when the Track IDs are  
3220 different. If a cluster has not been associated to any track but it shares the Track ID  
3221 with a reconstructed track it is counted as a false negative (FN).

3222 For the testing, I used a sample of 10000 FHC neutrino events inside the HPgTPC.  
3223 Figure 6.17 (left panel) shows the precision (blue line), sensitivity (yellow line), and  $F_1$

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**Figure 6.18:** Schematics of a possible option to deal with track-ECal associations in non-zero  $t_0$  neutrino interaction events, trying to correct for the drift direction uncertainty in a cluster-by-cluster basis using the cluster time,  $t_{cluster}$ .

score (red line) I obtained for different values of  $\chi^2_{cut}$ . For comparison, the same metrics computed for the default algorithm with the current configuration are also shown (dashed lines). In the case of the new algorithm, I used both the  $\chi^2$ -based method to estimate the track direction described earlier (square markers) and the cheated direction from the Geant-level information (circle markers). For either of these we achieve similar values of the precision compared to the old code, while having a considerably higher sensitivity. It can be seen that cheating the direction of the tracks only makes a difference at high  $\chi^2_{cut}$ , past the optimal value of the cut around the  $F_1$  score maximum. Therefore, I set the  $\chi^2$  method as the default.

One of the possible weak points of this approach is that it relies on the position along the drift direction to make the decisions. Within the current ND-GAr design implemented in GArSoft, the timing information is provided by the ECal. That effectively means that prior to make the track-ECal associations the reconstructed  $x$  positions of the track trajectories differ from the simulated ones by an amount:

$$x_{reco}^{(n)} - x_{sim}^{(n)} = v_{drift} t_0, \quad (6.10)$$

where  $v_{drift}$  is the mean drift velocity in our medium and the initial time is in the range  $t_0 \in [0, t_{spill}]$  where  $t_{spill}$  is the spill length. For a  $10 \mu\text{s}$  spill this translates into a maximum 30 cm uncertainty on the drift direction position.

The current default in GArSoft sets  $t_0 = 0$ , but the functionality to randomly sample

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3242 this within the spill time is in place. Therefore, we need to understand what is the impact  
3243 of a non-zero  $t_0$  on the associations algorithm and foresee possible ways of minimising a  
3244 loss in performance.

3245 Figure 6.18 represents a possible option to tackle the association problem when  
3246 having events with a non-zero initial time  $t_0$ . The black and white circles represent the  
3247 original points, whereas the squares indicate the corrected positions. The end points of  
3248 the track and the propagated points up to the cluster radius are indicated using filled  
3249 and unfilled markers respectively. The red square represents the position of the cluster.

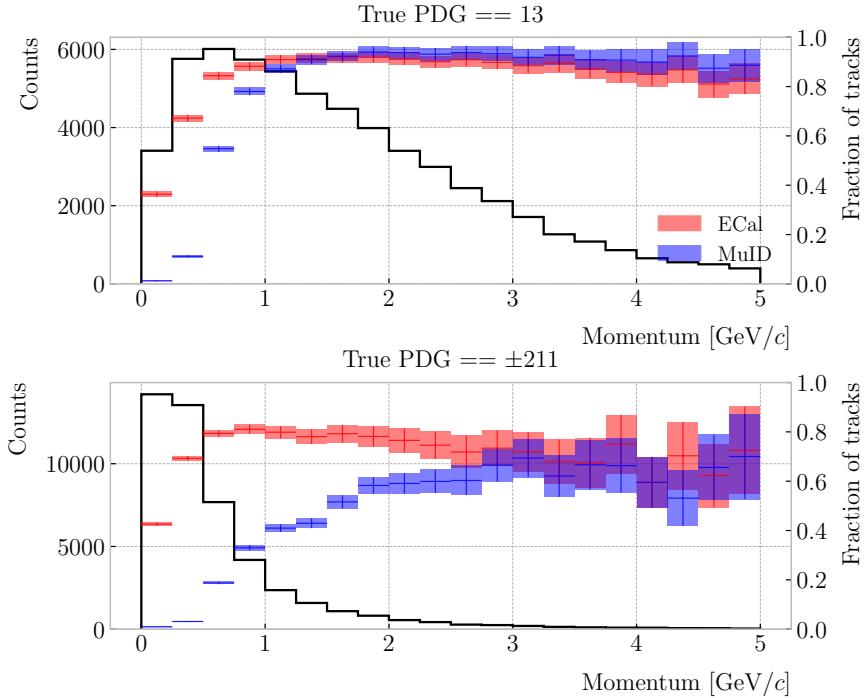
3250 Here I try to correct for the drift coordinate position using the time associated to the  
3251 cluster. Assuming that the drift time is much larger than the propagation time,  $t_{cluster}$   
3252 could be used as a good estimation of the  $t_0$ . An alternative can be using the earliest  
3253 time associated to a hit in said cluster. Doing this for each cluster before computing  
3254 the  $\chi^2$  value could be used as an alternative to knowing the specific value of the  $t_0$ , as  
3255 when the association is correct this will provide the right correction but its impact is  
3256 small enough to not change the position significantly in the case the cluster does not  
3257 correspond to a given track.

3258 I tested the effect of this correction again using a sample of 10000 FHC neutrino  
3259 events. Figure 6.17 (right panel) shows the precision (blue line), sensitivity (yellow line),  
3260 and  $F_1$  score (red line) for the case the cluster  $t_0$  correction is applied (square markers)  
3261 and for the no correction case (circle markers), as a function of  $\chi^2_{cut}$ . In this case, the  
3262 differences are particularly notorious at low values of the cut. It makes sense, as the  $t_0$   
3263 effect becomes subdominant when the distance we consider grows large. Overall, the  
3264 correction increases the sensitivity while keeping the precision almost unchanged. As a  
3265 result, I apply the  $t_0$  correction to the generated samples as the default.

#### 3266 6.3.2 Classification strategy

3267 The problem of the muon and charged pion separation has to be viewed in the broader  
3268 context of the particle identification in our detector. Focusing on the beam neutrino  
3269 interactions, it is clear that we are going to have muons and pions spanning a broad

## CHAPTER 6. PARTICLE ID IN ND-GAr

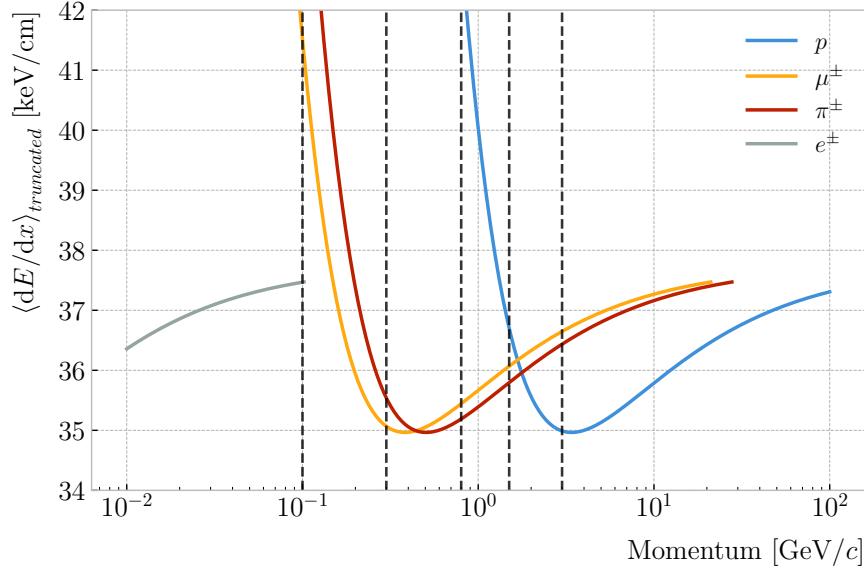


**Figure 6.19:** Momentum distribution for the reconstructed muons (top panel) and charged pions (bottom panel) in a FHC neutrino sample, together with the fraction of them reaching the ECal (red) and MuID (blue). Each entry corresponds to a reconstructed track, backtracked to a true muon or pion which has not produced any other reconstructed track.

3270 momentum range. Not only that, but we will also have other particles with similar  
 3271 characteristics that will make the classification even more challenging. Therefore, we are  
 3272 presented with a task that will depend heavily on the kinematic range we are looking at  
 3273 each time, as both the available information and the possible impurities of other particle  
 3274 species vary.

3275 For instance, distinguishing muons from pions could be difficult at low momenta, as  
 3276 a great number of them do not reach the ECal. Therefore, we could think of tailoring a  
 3277 version of the classification for that particular case, which could be complemented with  
 3278 a  $dE/dx$  measurement. Likewise, for momenta  $\gtrsim 1$  GeV muons and pions reach the  
 3279 calorimeters efficiently, but so do protons. Because of this, one can try to train another  
 3280 classifier for this energy range, and rely on other methods to remove as many of the  
 3281 protons as possible.

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**Figure 6.20:** Predicted truncated mean  $dE/dx$  versus momentum, for electrons, muons, charged pions and protons, obtained using the ALEPH parametrisation. The vertical dashed lines represent the boundaries of the six regions used for the muon and pion classification training.

3282     Figure 6.19 shows the momentum distribution of the reconstructed muons (top) and  
 3283     pions (bottom) in a FHC sample. It also contains the fraction of particles reaching the  
 3284     ECal (red) and MuID (blue), for the different momentum bins. In Fig. 6.20 I show the  
 3285     mean  $dE/dx$  of different particles as a function of the momentum, computed using the  
 3286     ALEPH parametrisation with the best fit parameters found in Subsec. 6.2.2.

3287     Using these two figures as references, I decided to approach the classification by  
 3288     dividing the problem into six different momentum regions. A summary of these can be  
 3289     found in Tab. 6.2. The basic idea is to exploit all the information that is available in  
 3290     each region and . For the problem at hand, I prepared separated samples of isotropic  
 3291     single muons and pions, with momenta uniformly distributed along the corresponding  
 3292     momentum range. Each sample contains 50000 events of the corresponding particle  
 3293     species. I did not generate samples for the first region, as it is assumed that the separation  
 3294     can be achieved using  $dE/dx$  only. For the last region, I generated particles up to a  
 3295     momentum of 10  $\text{GeV}/c$ , as that is well above the typical energies of muons and pions  
 3296     from FHC neutrino interactions in ND-GAr.

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**Table 6.2:** Momentum ranges and description of the PID approach assumed for the muon and pion classification task.

Momentum range	Description
$< 0.1 \text{ GeV}/c$	All tracks can be separated with $dE/dx$
$[0.1, 0.3) \text{ GeV}/c$	Use ECal for reaching muons and pions, $dE/dx$ for the rest
$[0.3, 0.8) \text{ GeV}/c$	Use ECal for muons and pions, $dE/dx$ for protons
$[0.8, 1.5) \text{ GeV}/c$	Use ECal and MuID for muons and pions, $dE/dx$ for protons
$[1.5, 3.0) \text{ GeV}/c$	Use ECal and MuID for muons and pions, ToF for protons
$\geq 3.0 \text{ GeV}/c$	Use ECal and MuID for muons and pions, $dE/dx$ and ToF for protons

3297     Additionally, I prepared another sample of 100000 FHC neutrino events. For each  
 3298    interaction, I select the reconstructed particles which were backtracked to true muons or  
 3299    charged pions. I use this dataset to perform validation checks, to see how the models  
 3300    trained with the single particle data generalise to a more realistic scenario.

3301     To tackle this classification problem, I make use of Boosted Decision Trees (BDT). A  
 3302    decision tree uses a flowchart-like structure to make decisions based on some input data.  
 3303    It starts from a root node, which represents the complete dataset, and then it splits  
 3304    this based on the variable or feature which gives the best separation between classes,  
 3305    creating two new nodes. The process repeats for each node until it reaches a certain  
 3306    limit, like a maximum number of splits or some tolerance criteria. The last set of nodes  
 3307    are often called leave nodes, and represent the final prediction of the classifier.

3308     Boosting refers to a family of methods to combine the predictions from multiple  
 3309    classifiers, following a sequential approach where each new model learns from the errors  
 3310    of the previous one. The process starts with a simple decision tree, which is used to  
 3311    make predictions on the training data. Then, the data points misclassified by the first  
 3312    model are assigned higher weights, and another decision tree is trained on the data with  
 3313    adjusted weights. The predictions of the two trees are then combined, and the cycle  
 3314    repeats for a predefined number of iterations. Gradient boosting uses the direction of  
 3315    the steepest error descent to guide the learning process and improve the accuracy with  
 3316    each iteration.

### 6.3. MUON AND PION SEPARATION IN THE ECal AND MuID

#### 3317 6.3.3 Feature selection and importance

3318 Using the reconstructed tracks as a starting point, I compute a number of ECal and  
3319 MuID variables for each of them. As there can be more than one cluster associated to a  
3320 track, what I do is collect all associated clusters and compute these variables from the  
3321 complete collection of associated hits. For the MuID, because it only features three layers  
3322 and typically there will be less hits, I also allow single hits to be associated with tracks<sup>7</sup>.  
3323 I can roughly divide the variables in three types: energy-related, geometry-related and  
3324 statistical. In the following, I briefly describe the variables related exclusively to the  
3325 ECal:

3326 • Energy-related ECal

- 3327 – ECal total energy (ClusterTotalEnergy): sum of the energy of all the ECal  
3328 hits.
- 3329 – Mean ECal hit energy (HitMeanEnergy): mean of the hit energy distribution.
- 3330 – Standard deviation ECal hit energy (HitStdEnergy): standard deviation of  
3331 the hit energy distribution.
- 3332 – Maximum ECal hit energy (HitMaxEnergy): maximum of the hit energy  
3333 distribution.

3334 • Geometry-related ECal

- 3335 – Mean distance hit-to-cluster (DistHitClusterMean): mean of the distance  
3336 distribution between the hits and the corresponding cluster's main axis.
- 3337 – RMS distance hit-to-cluster (DistHitClusterRMS): root mean square of the  
3338 distance distribution between the hits and the corresponding cluster's main  
3339 axis.

---

<sup>7</sup>At the reconstruction level what happens is that non-clustered hits are put into single hit clusters, instead of being thrown away. This is necessary to keep the consistency of the track-cluster association code.

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- 3340        – Maximum distance hit-to-centre (DistHitCenterMax): maximum of the  
3341                  distance distribution between the hits and the centre of the TPC.  
  
3342        – Time-of-Flight velocity (TOFVelocity): slope obtained when fitting a straight  
3343                  line to the hit time versus hit distance to the centre (i.e.  $d = v \times t$ ).

### 3344        • Energy and geometry ECal

- 3345        – Radius 90% energy (Radius90E): distance in the hit-to-cluster distribution  
3346                  for which 90% of the total energy is contained in the hits that are closer to  
3347                  the axis (i.e. radius that contains 90% of the energy).

### 3348        • Statistical ECal

- 3349        – Number of hits (NHits): total number of hits associated to the track.  
3350        – Number of layers with hits (NLayers): not really a count of all layers with  
3351                  hits but the difference between the last and the first layer with hits.

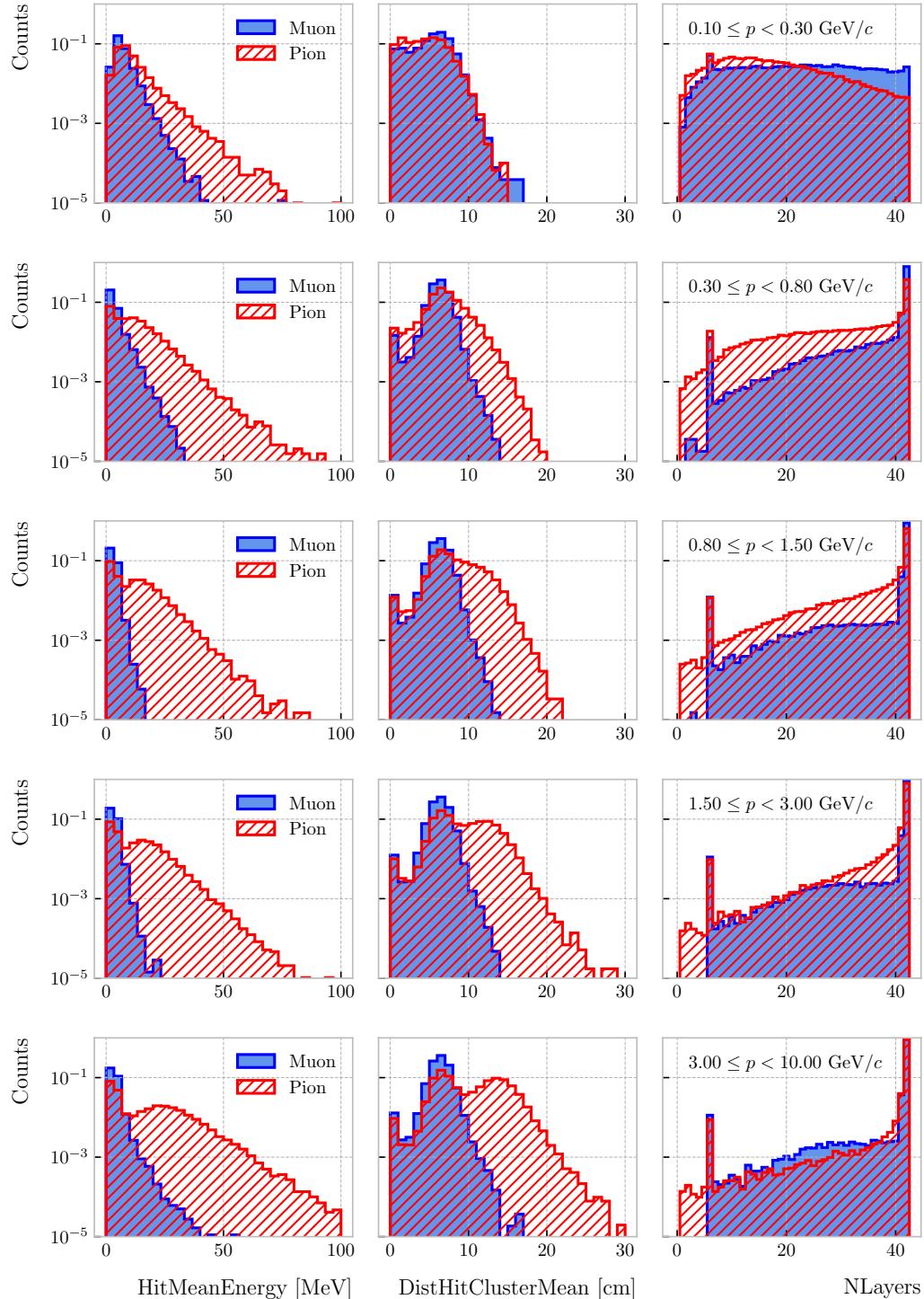
3352        Figure 6.21 shows the distributions of three different ECal variables, separating true  
3353                  muons (blue) and charged pions (red), for the five momentum ranges considered. I chose  
3354                  to show one feature from each category, namely the mean energy per hit (left column),  
3355                  the mean distance between the hits and the centre of the cluster (middle column), and  
3356                  the number of ECal layers with hits (right column). These give an idea of the separating  
3357                  power of the different features, and how it changes considerably with the energy. In  
3358                  the number of layers with hits distributions, the peak at 6 is due to the fact that the  
3359                  first six ECal layers sit inside the pressure vessel<sup>8</sup>. Therefore, some of the particles get  
3360                  stopped crossing it, never making it to the seventh layer.

3361        In the case of the MuID, because at low momenta a significant fraction of the particles  
3362                  do not make it past the ECal, I only consider the information coming from this detector  
3363                  for momenta  $\geq 0.8$  GeV/c, i.e. for the last three momentum regions. The variables I  
3364                  extract from it are the following:

---

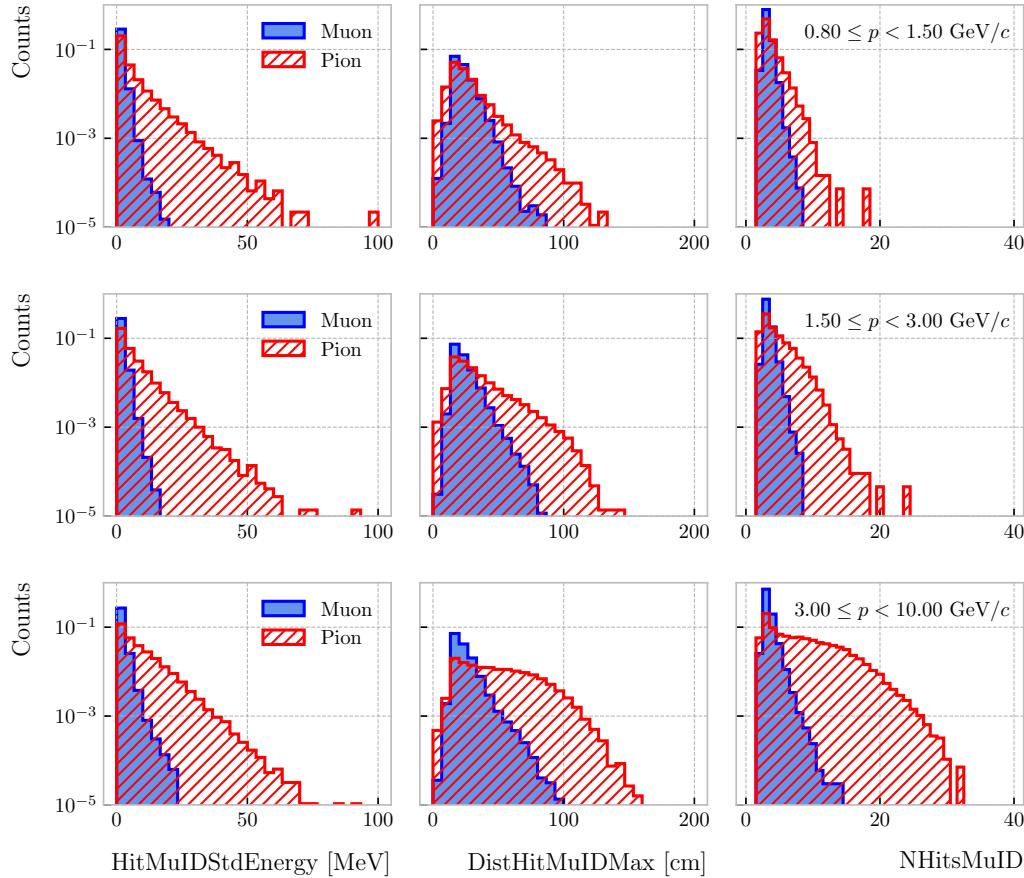
<sup>8</sup>Note to self: check this. I thought the ECal barrel had 8 layers of tiles, and that all of them were inside the pressure vessel.

### 6.3. MUON AND PION SEPARATION IN THE ECAL AND MUID



**Figure 6.21:** Example ECal feature distributions for muons (blue) and charged pions (red) in the five different momentum ranges considered (from top to bottom, in ascending momentum order). From left to right: mean hit energy, mean distance hit-to-cluster, and number of layers with hits.

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**Figure 6.22:** Example MuID feature distributions for muons (blue) and charged pions (red) in the three different momentum ranges considered (from top to bottom, in ascending momentum order). From left to right: standard deviation hit energy, maximum distance hit-to-hit, and number of hits.

3365

- Energy-related MuID

3366

- MuID total energy (ClusterMuIDTotalEnergy): sum of the energy of all the MuID hits.

3367

- Mean MuID hit energy (HitMuIDMeanEnergy): mean of the MuID hit energy distribution.

3368

- Standard deviation MuID hit energy (HitMuIDStdEnergy): standard deviation of the MuID hit energy distribution.

3369

- Maximum MuID hit energy (HitMuIDMaxEnergy): maximum of the MuID hit energy distribution.

3370

3371

### 6.3. MUON AND PION SEPARATION IN THE ECAL AND MUID

3374        • **Geometry-related MuID**

- 3375            – Maximum distance MuID hit-to-hit (DistHitMuIDMax): maximum distance  
3376              between pairs of MuID hits (not sure this is a good variable, distribution  
3377              looks nuts).
- 3378            – Maximum distance MuID hit-to-centre (DistHitCenterMuIDMax): maximum  
3379              of the distance distribution between the MuID hits and the centre of the  
3380              TPC.

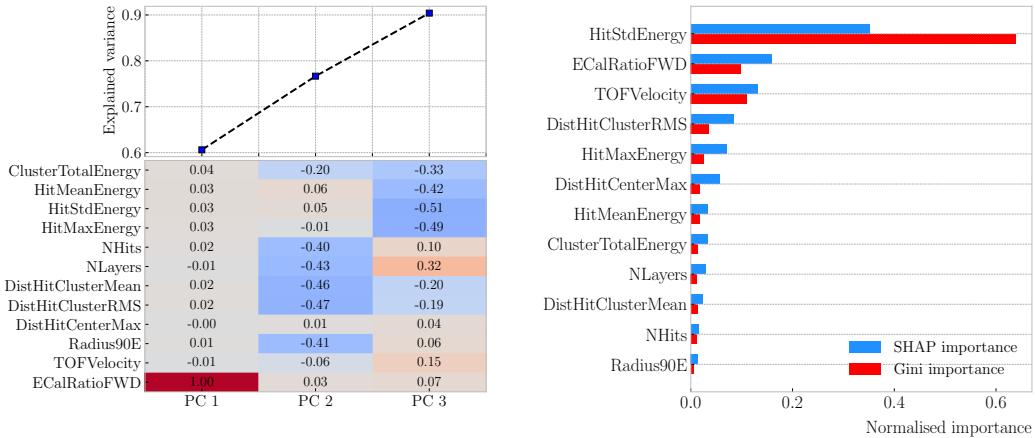
3381        • **Statistical MuID**

- 3382            – Number of hits (NHitsMuID): total number of MuID hits associated to the  
3383              track.
- 3384            – Number of layers with hits (NLayersMuID): not really a count of all layers  
3385              with MuID hits but the difference between the last and the first layer with  
3386              MuIDhits.

3387        Figure 6.22 shows the distributions of three different MuID variables, separating true  
3388        muons (blue) and charged pions (red), for the three momentum ranges which use the  
3389        muon tagger information. In this case I decided to standard deviation of the MuID hit  
3390        energy distribution (left column), the maximum distance between the MuID hit pairs  
3391        (middle column), and the number of MuID hits (right column). These variables are used  
3392        together with the ECal features at high momenta, providing additional disambiguation  
3393        power.

3394        Once our features have been defined, one can do some exploratory analysis to  
3395        understand how well the variables describe the target class, and avoid the black-box  
3396        approach by what features are most relevant for the learning process. This way, I  
3397        performed a feature analysis for each of the momentum ranges I divided this classification  
3398        problem into. It follows three steps: first a principal component analysis (PCA), followed  
3399        by a feature importance study using Gini and Shapley values, and finally a feature  
3400        permutation importance analysis.

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**Figure 6.23:** Left panel: cumulative explained variance for the first three principal components (top panel) and contribution of the different features to the principal axes in feature space (bottom panel). Right panel: Shapley (blue) and Gini (red) feature importances for the different input features. Both figures correspond to the samples in the momentum range  $0.3 \leq p < 0.8 \text{ GeV}/c$ .

The PCA is useful to understand the variance of the feature space. It is an unsupervised machine learning technique that allows the user to perform a dimensionality reduction. It uses a singular value decomposition of the input features to project them into a lower dimensional space. The idea is to find the matrix  $\mathbf{C}_m$ , whose columns are the first  $m$  orthonormal eigenvectors of the input covariance matrix. Consider the  $n \times p$  real matrix of input data  $\mathbf{X}$ , where  $n$  is the number of samples and  $p$  the number of features. If  $\mathbf{X}$  is centred, i.e. the means of its columns are equal to zero, we can write the covariance matrix of  $\mathbf{X}$  as  $\mathbf{C} = \mathbf{X}^\top \mathbf{X} / (n - 1)$ . This matrix can be diagonalised, yielding:

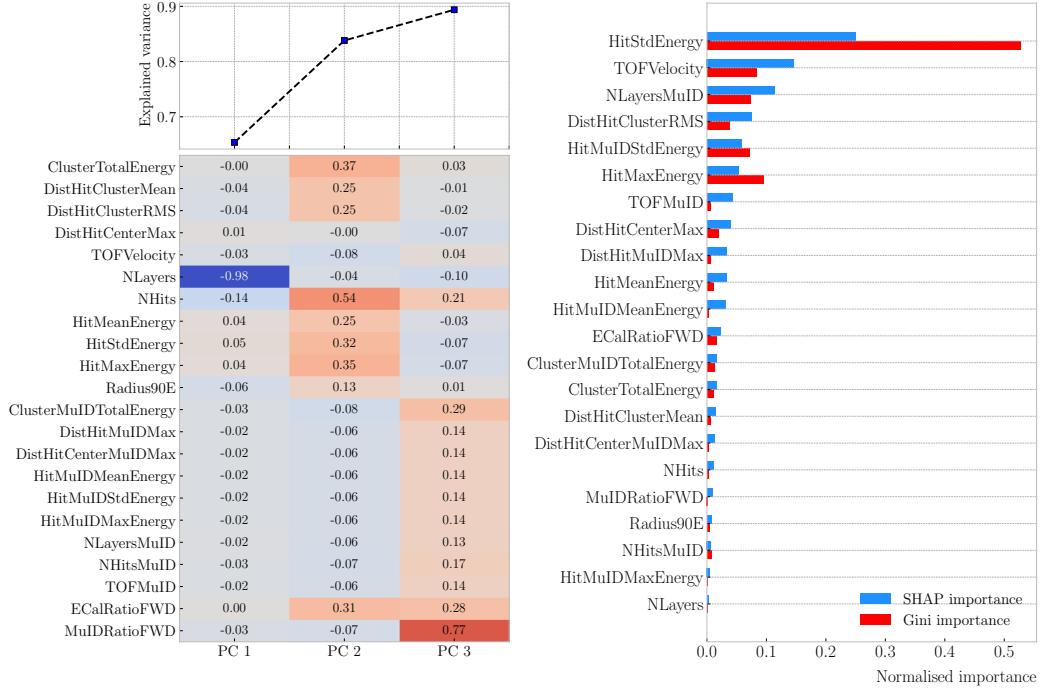
$$\mathbf{C} = \mathbf{V} \mathbf{L} \mathbf{V}^\top, \quad (6.11)$$

where  $\mathbf{V}$  is a matrix of eigenvectors and  $\mathbf{L}$  a diagonal matrix with eigenvalues  $\lambda_i$ . Then, performing SVD on  $\mathbf{X}$  gives us:

$$\mathbf{X} = \mathbf{U} \mathbf{S} \mathbf{W}^\top, \quad (6.12)$$

where  $\mathbf{U}$  is a unitary matrix, whose columns are called left singular vectors,  $\mathbf{S}$  is a diagonal matrix of single values  $s_i$ , and  $\mathbf{W}$  is another unitary matrix, its columns known

### 6.3. MUON AND PION SEPARATION IN THE ECAL AND MUID



**Figure 6.24:** Left panel: cumulative explained variance for the first three principal components (top panel) and contribution of the different features to the principal axes in feature space (bottom panel). Right panel: Shapley (blue) and Gini (red) feature importances for the different input features. Both figures correspond to the samples in the momentum range  $0.8 \leq p < 1.5$  GeV/c.

as right singular vectors. This way, we can write:

$$\mathbf{C} = \mathbf{W}\mathbf{S}\mathbf{U}^\top\mathbf{U}\mathbf{S}\mathbf{W}^\top/(n-1) = \mathbf{W}\frac{\mathbf{S}^2}{n-1}\mathbf{W}^\top. \quad (6.13)$$

meaning that the right singular vectors are also the eigenvectors of the covariance matrix.

The SVD can be computed numerically following an iterative approach.

This way, taking an input data vector  $X \in \mathbb{R}^n$ , the resulting feature vector  $Y \in \mathbb{R}^m$

is given by:

$$Y = \mathbf{C}_m^\top X. \quad (6.14)$$

The new features capture most of the variance of the original sample, while being lower

dimensional, as  $m < n$ .

Before applying the PCA reduction one needs to centre and scale the input data.

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3421 Centring is necessary when using SVD to obtain the eigenvectors of the covariance  
3422 matrix, as only in that case we can do the identification with the right singular vectors  
3423 from the input data. Scaling is needed when variables are on different scales, as some  
3424 can then dominate the PCA procedure.

3425 I used the PCA module of `scikit-learn`, together with the `RobustScaler`, which  
3426 centres the data and scales it based on the interquartile range. In Fig. 6.23 (left panel)  
3427 and Fig. 6.24 (left panel) I show the results I obtained from the PCA for the momentum  
3428 ranges  $0.3 \leq p < 0.8 \text{ GeV}/c$  and  $0.8 \leq p < 1.5 \text{ GeV}/c$ , respectively. Notice that in  
3429 the second case the number of features increases considerably, as this is the first region  
3430 which uses the MuID variables. I found that, in all the cases, adding a fourth PC does  
3431 not add additional information. As it can be seen in the top panels of the figures, the  
3432 cumulative explained variance is already over 80% with three PCs.

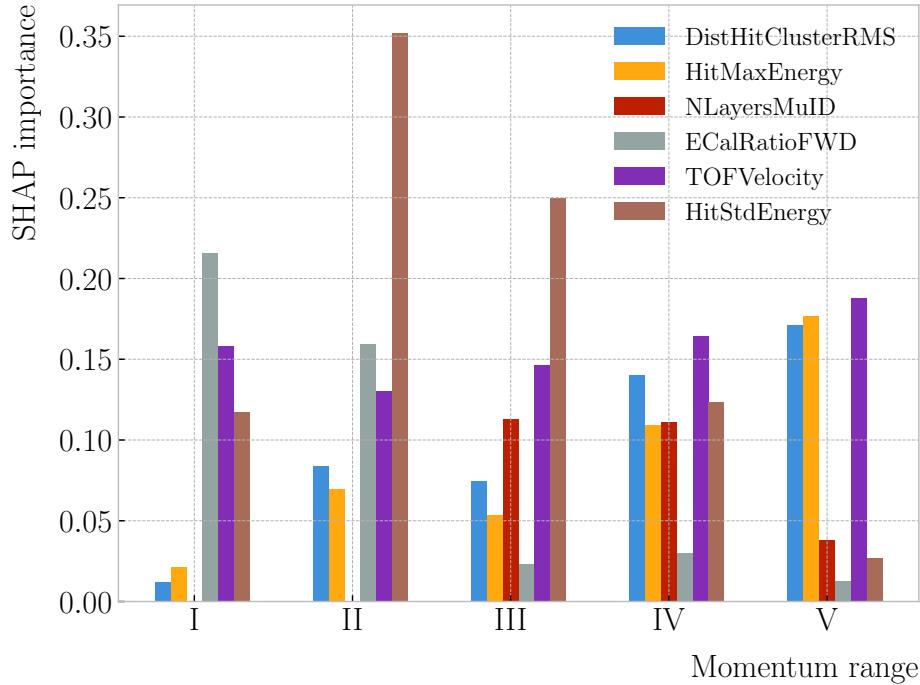
3433 The bottom panels show the contribution of the variables to the principal axes. For  
3434 the two first momentum regions, I observe a tendency of the energy-related and the  
3435 geometry-related ECal variables to be clustered together. For the other ranges, when  
3436 I include the MuID variables, there seems to be a division between ECal and MuID  
3437 variables. For these, it seems like the number of ECal layers with hits also plays an  
3438 important role.

3439 The next step in the analysis is to quantify the importance of the features based on  
3440 two additional metrics, namely the Gini and the Shapley values. The Gini importance,  
3441 often called mean decrease impurity, is based on how much a feature contributes to the  
3442 purity improvement at the splits in each decision tree. The purity is measured in terms  
3443 of the Gini impurity index, defined as:

$$I_G = 1 - \sum_i f_i, \quad (6.15)$$

3444 where  $f_i$  is the fractional abundance of the  $i$ -th class. Then, for each split one can

### 6.3. MUON AND PION SEPARATION IN THE ECAL AND MUID



**Figure 6.25:** Evolution of the SHAP importance for the top six most important features across all five momentum ranges.

3445 compute the weighted decrease in impurity as:

$$\Delta_G = \frac{N_t}{N} \left( I_G - \frac{N_t^R}{N_t} I_G^R - \frac{N_t^L}{N_t} I_G^L \right), \quad (6.16)$$

3446 where  $N$  represents the total number of samples,  $N_t$  the number of samples at the current  
 3447 node,  $N_t^R$  and  $N_t^L$  the number of samples in the right and left children respectively,  
 3448  $I_G$  is the Gini impurity at the current node, and  $I_G^R$  and  $I_G^L$  the Gini impurities of the  
 3449 resulting right and left children.

3450 For each decision tree, one will have a normalised vector with the accumulated  
 3451 decrease in Gini impurity for each feature. In the case of a BDT, the feature importances  
 3452 are simply the mean for all the estimators in the ensemble<sup>9</sup>.

3453 The concept of Shapley values originated in the context of game theory, and it  
 3454 measures the marginal contribution of a feature in enhancing the accuracy of a classifier.

---

<sup>9</sup>Note to self: this appears not to be the case. If you get the `feature_importance` for each tree in the BDT and take the average, the result is not the same to be one reported in the `feature_importance` attribute of the BDT.

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3455 Take  $F$  to be the set of all features in a problem, and  $S \subseteq F$  the subset of features. To  
 3456 compute the Shapley value of the  $i$ -th feature, one has to train a model with that feature  
 3457 present,  $f_{S \cup \{i\}}$ , and another model trained without it,  $f_S$ . This has to be repeated for  
 3458 all possible combinations of subsets  $S \subset F \setminus \{i\}$ , and evaluating the models predictions  
 3459 on the appropriate sets of data  $x_S$ . This way, the Shapley value results:

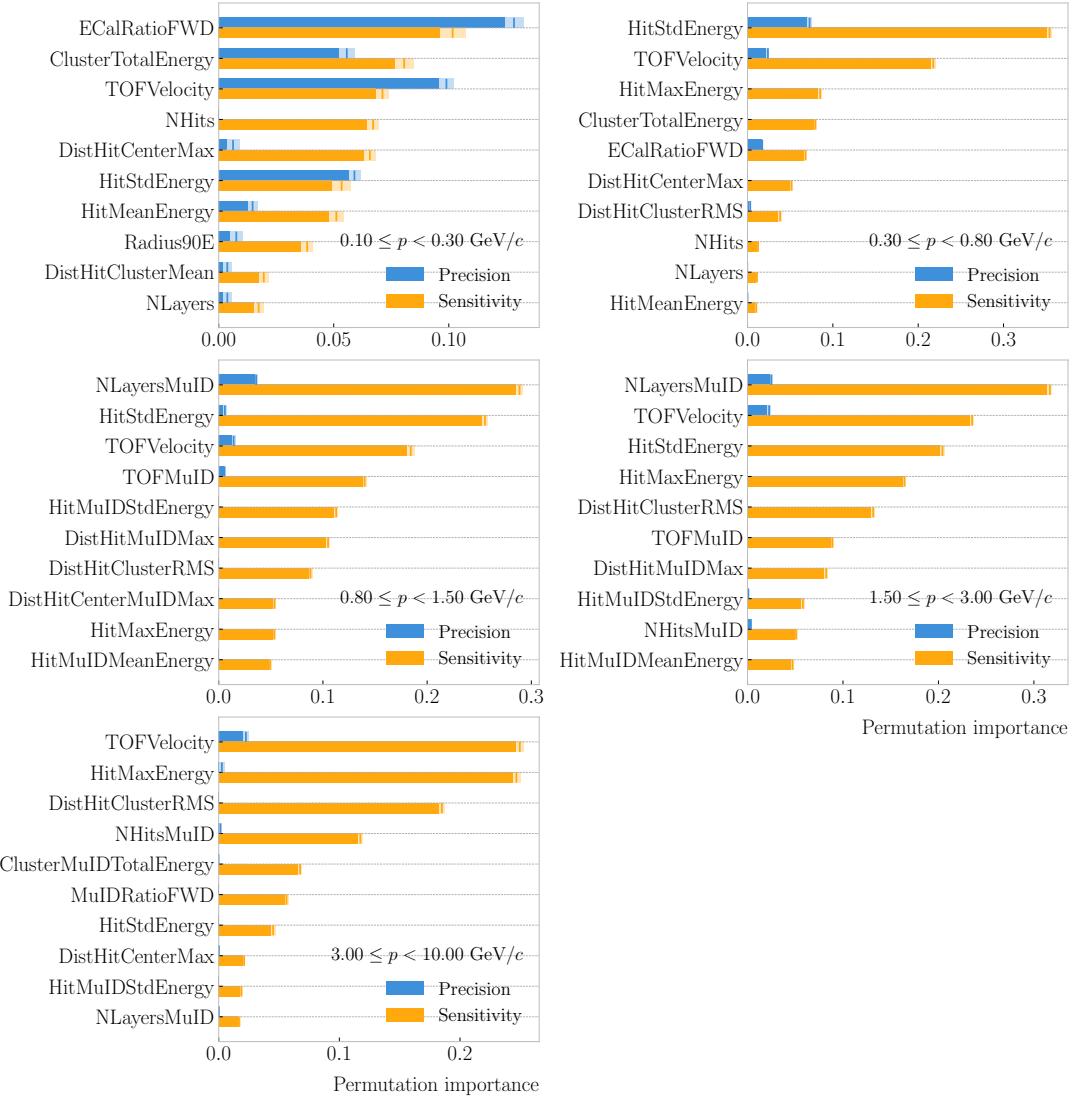
$$\varphi_i = \sum_{S \subset F \setminus \{i\}} \frac{|S|! (|F| - |S| - 1)!}{|F|!} [f_{S \cup \{i\}}(x_{S \cup \{i\}}) - f_S(x_S)]. \quad (6.17)$$

3460 I trained the `GradientBoostingClassifier` from `scikit-learn` with the default  
 3461 configuration in order to evaluate both the Gini and Shapley importances. The Gini  
 3462 scores are automatically computed by `scikit-learn`, using the training data. For the  
 3463 Shapley importance, I used the implementation from the `SHAP` package, computing  
 3464 it using the test sample. The results can be seen in Fig. 6.23 (right panel) and  
 3465 Fig. 6.24 (right panel), again for the momentum ranges  $0.3 \leq p < 0.8 \text{ GeV}/c$  and  
 3466  $0.8 \leq p < 1.5 \text{ GeV}/c$ . The length of the bars denote either the SHAP (blue) or the Gini  
 3467 (red) importance of the feature. One interesting thing to notice is that, when looking at  
 3468 the Gini importance, there is always one feature that dominates over the rest. This is  
 3469 not the case for the SHAP importance, where importances tend to be more balanced.

3470 Across all momentum ranges, I observe that the most important features are. For  
 3471 the five momentum ranges considered, only six variables sit in the top five at least once.  
 3472 Figure 6.25 shows the evolution of the SHAP importance of these six features. It is  
 3473 interesting to see that the time-of-flight variable keeps its importance almost unchanged  
 3474 for all momenta. Also, it looks like the ECal energy ratio gets less relevant the higher the  
 3475 momentum is, but the RMS of the hit-to-cluster distance distribution and the maximum  
 3476 ECal hit energy become more important in the last momentum ranges.

3477 The last step in the feature selection analysis is the feature permutation. This  
 3478 technique measures the contribution of each feature to the performance of a model by  
 3479 randomly shuffling its values and checking how some scores degrade. For the present  
 3480 case, I am interested in the precision or purity, and the sensitivity or efficiency, as these

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**Figure 6.26:** Permutation importances for the ten most important features in the different momentum ranges (from left to right, top to bottom, in increasing momentum order). The bars indicate the effect that permutations of each feature have on the purity (blue) and the sensitivity (yellow), the translucent regions representing one standard deviation around the central value.

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3481 two are the most relevant metrics from a physics point of view. The `scikit-learn`  
3482 module provides the user with a method to perform the permutation scans.

3483 The results of these are shown in Fig. 6.26. For the different momentum ranges  
3484 I show the permutation importances for the ten most important features. For each  
3485 of the variables I report the effect the permutations have on the precision (blue) and  
3486 sensitivity (yellow) of the models. The bars indicate the importance value, with the  
3487 lighter part representing one standard deviation around the mean (hinted as an additional  
3488 vertical line). Something to notice is that, in the first momentum region, the feature  
3489 permutations have an effect on both the precision and the sensitivity. However, for the  
3490 rest the precision is almost unaffected, while the sensitivity changes are considerably  
3491 larger.

3492 It is also interesting to see that most of the variables identified as important here  
3493 are the same I found when looking at the Shapley values. The behaviour of these across  
3494 the momentum ranges is also similar, with the same patterns of some features being  
3495 important at low momenta and then dropping in importance for the high momentum  
3496 ranges.

3497 Wit this, I conclude the study of the features. I have prepared the training and  
3498 testing datasets and understood what features are likely to have the largest impact on  
3499 the performance of the classifiers.

### 3500 6.3.4 Hyperparameter optimisation

3501 Any BDT requires the user to specify a number of parameters that will dictate its  
3502 behaviour. They can be divided into two categories: (i) tree-specific parameters, which  
3503 affect each individual tree in the model, and (ii) boosting parameters, which control the  
3504 boosting operation in the model. The value of these so-called hyperparameters affect the  
3505 performance and predictive power of the models. Therefore, one needs to carefully select  
3506 their optimal values in order to extract as much information as possible from the data.

3507 From all the parameters used to define a tree in the `scikit-learn` implementation  
3508 of the BDT classifier, I only consider a subset of them. This is due to the fact that some

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3509 are mutually exclusive, but also because I noticed that others have little effect on the  
3510 problem at hand. Therefore, the parameters I investigate are the following:

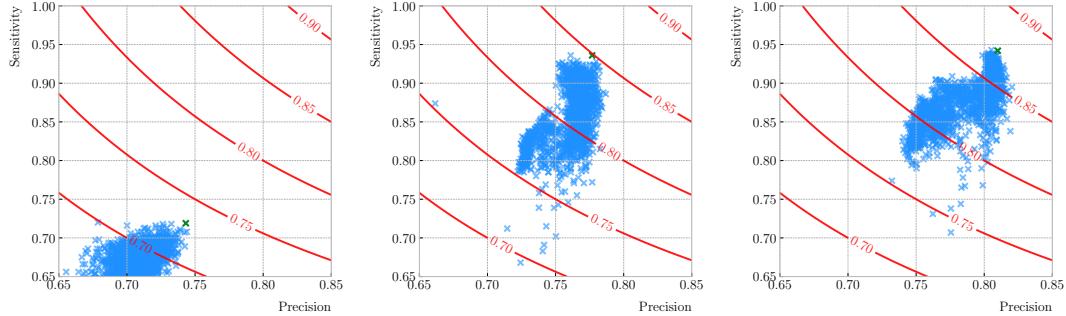
- 3511     • `min_samples_split`: defines the minimum number of samples required in a node  
3512         to be considered for splitting. Higher values prevent a model from learning relations  
3513         which might be highly specific to the particular sample, but may lead to under-fitting  
3514         if the value is too low.
- 3515     • `min_samples_leaf`: defines the minimum samples required in a leaf node. For  
3516         imbalanced problems it should take a low value, as there will not be many cases  
3517         where the minority class dominates.
- 3518     • `max_depth`: maximum depth of a tree. Useful to prevent over-fitting, as higher  
3519         depth will allow a model to learn relations specific to the training sample.

3520 In the case of the boosting parameters, the ones I look at are:

- 3521     • `learning_rate`: determines the impact of each tree on the final outcome. Low  
3522         values make the model robust to the specific characteristics of a tree, and thus  
3523         allow it to generalise well. However, that usually requires a large number of trees  
3524         to model the data properly.
- 3525     • `n_estimators`: number of sequential trees to be trained. In general, BDTs are  
3526         fairly robust at higher number of trees but it can still overfit at a point.
- 3527     • `subsample`: fraction of observations to be selected for each tree. Values slightly  
3528         less than 1 make the model robust by reducing the variance.

3529 In general, hyperparameters depend on each other. Thus, it is not possible to  
3530 optimise them independently. In the literature, we find two main strategies to explore  
3531 the hyperparameter space. We could use a grid search, in which one discretises a  
3532 portion of the space of hyperparameters and evaluates the model at each point. Another  
3533 approach is the randomised search, where a certain number of random configurations of  
3534 hyperparameters are explored.

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**Figure 6.27:** Values of the precision and sensitivity obtained for 10000 BDT hyperparameter configurations, for the momentum regions I, III and V. The red contours indicate the curves of equal  $F_1$ -score, while the green crosses are the selected configurations.

3535 In this case, I used the random search to scan the hyperparameter space. Also,  
 3536 because it is not guaranteed that a set of hyperparameters can be efficiently applied  
 3537 across different datasets, I perform the optimisation for each of the momentum ranges  
 3538 considered. Table 6.3 shows the list of hyperparameters considered, and the range within  
 3539 which I let them vary. I decided to fix the number of estimators to 400 in all cases, as  
 3540 its value is correlated with that of the learning rate.

3541 I evaluate 10000 different hyperparameter configurations for each momentum range.  
 3542 For the hyperparameter tuning, I used subsamples containing 10% of the full datasets,  
 3543 keeping the original proportions between classes, in order to reduce the computational  
 3544 load. The performance of the models was assessed using a stratified 3-fold cross-validation  
 3545 with replacement. Cross-validation involves dividing the data in a number of subsets,  
 3546 training the model using some of them, and testing it with the rest. In our case, I  
 3547 divide the data in 3 equal-sized subsets, maintaining the class proportions of the original  
 3548 dataset. Then, for 3 consecutive iterations, I train the models using 2 of the subsets  
 3549 while I compute the precision and sensitivity scores with the other. This approach  
 3550 provides a more robust estimate of the performance on unseen data.

3551 Figure 6.27 shows the results in the precision versus sensitivity plane, for the  
 3552 momentum regions I, III and V (from left to right). The contours represent the curves  
 3553 of equal  $F_1$ -score, i.e. the harmonic mean of the precision and the sensitivity. In order

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**Table 6.3:** Optimal values of the hyperparameters used by the BDT, for each momentum range.

Hyperparameter	Range	Best value				
		I	II	III	IV	V
<code>min_samples_split</code>	[0.001, 1]	0.10	0.06	0.05	0.27	0.06
<code>min_samples_leaf</code>	[0.001, 1]	0.02	0.03	0.01	0.02	0.07
<code>max_depth</code>	{2, 3, ..., 8}	8	2	4	2	7
<code>learning_rate</code>	[0.05, 1]	0.10	0.23	0.07	0.13	0.09
<code>subsample</code>	[0.01, 1]	0.75	0.65	0.79	0.86	0.95

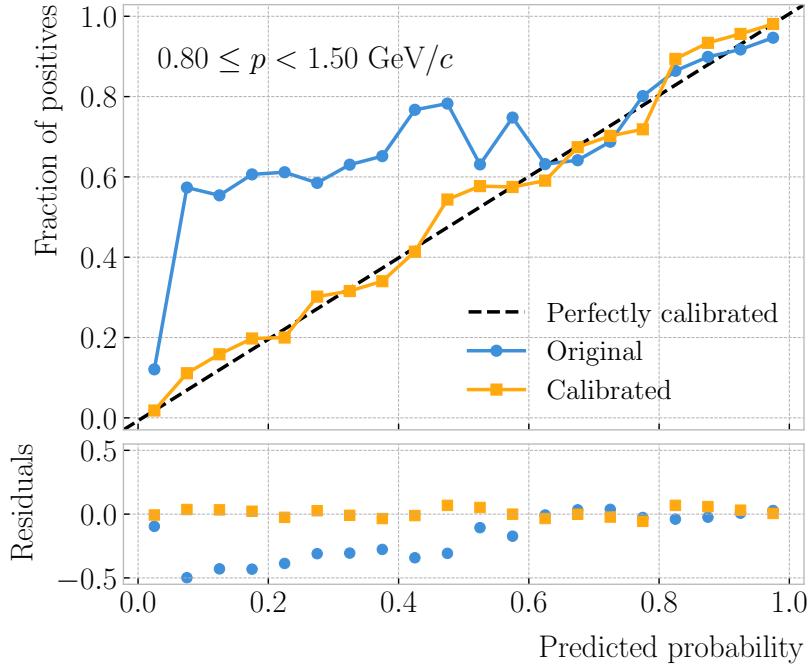
**Table 6.4:** Performance metrics of the BDTs with optimal hyperparameters, for the different momentum ranges.

Metric	Value $\pm 1\sigma$				
	I	II	III	IV	V
Accuracy	$0.779 \pm 0.003$	$0.812 \pm 0.003$	$0.846 \pm 0.002$	$0.861 \pm 0.003$	$0.874 \pm 0.002$
Precision	$0.769 \pm 0.003$	$0.752 \pm 0.005$	$0.788 \pm 0.002$	$0.805 \pm 0.003$	$0.815 \pm 0.003$
Sensitivity	$0.745 \pm 0.009$	$0.921 \pm 0.006$	$0.965 \pm 0.002$	$0.967 \pm 0.002$	$0.976 \pm 0.001$
$F_1$ -score	$0.757 \pm 0.004$	$0.828 \pm 0.003$	$0.867 \pm 0.002$	$0.879 \pm 0.002$	$0.889 \pm 0.002$
ROC AUC	$0.868 \pm 0.003$	$0.865 \pm 0.003$	$0.899 \pm 0.002$	$0.902 \pm 0.002$	$0.911 \pm 0.001$

3554 to select the optimal configurations (indicated in the plots with a green cross), I chose  
 3555 the point with the highest  $F_1$ -score.

3556 The results for the different momentum ranges are summarised in Tab. 6.3. One  
 3557 can see some consistency in hyperparameter choices, with models generally preferring  
 3558 small values for the tree-specific parameters, small learning rate, and relatively large  
 3559 subsample sizes.

3560 Now that I have obtained the optimal values of the hyperparameters, I can train  
 3561 the different BDTs. In this case I use the complete datasets, keeping 20% of the data  
 3562 for testing. Table 6.4 shows the values of the different performance metrics obtained  
 3563 using the selected hyperparameters and 5-fold cross-validation. The last row indicates  
 3564 the value of the area under the receiver operating characteristic (ROC) curve. This  
 3565 represents the sensitivity of a model as a function of the false positive rate. I have



**Figure 6.28:** Reliability diagrams for the BDT classifier used in the momentum range  $0.3 \leq p < 0.8 \text{ GeV}/c$ , both for the original (blue circles) and calibrated (yellow squares) responses. For reference, the response of a perfectly calibrated classifier is also shown (black dashed line).

3566 included it here as it is a classic model metric used in the machine learning community.

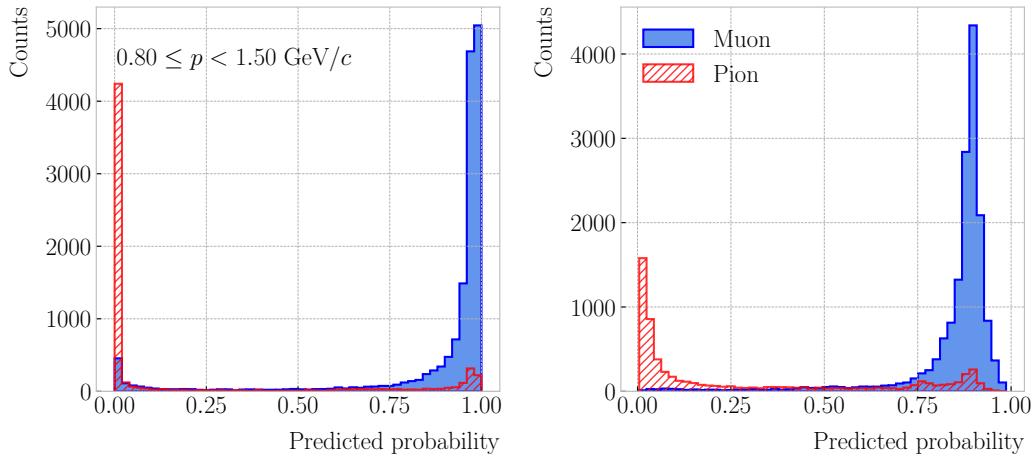
3567 Overall, there is a clear trend of models performing better at higher momentum.

### 3568 6.3.5 Probability calibration

3569 So far, the trained BDTs are able to provide predictions of the class labels. Ideally,  
3570 one would like the output of a classifier to give a confidence level about the prediction.  
3571 However, it is not straightforward to interpret the outputs of our BDTs in terms of  
3572 probabilities.

3573 A way to visualise how well the predictions of a classifier are calibrated is using  
3574 reliability diagrams [160]. They represent the probability of the positive label versus the  
3575 probability predicted by the classifier. These can be obtained by binning the predicted  
3576 probabilities, and then compute the conditional probability  $P(y_{true} = 1 | y_i \leq y_{pred} <$   
3577  $y_{i+1})$  by checking the fraction of true positive instances in each bin. The reliability

### 6.3. MUON AND PION SEPARATION IN THE ECAL AND MUID



**Figure 6.29:** Uncalibrated (left panel) and calibrated (right panel) predicted probabilities assigned by the BDT classifiers for true muons (blue) and charged pions (red) in the momentum range  $0.3 \leq p < 0.8 \text{ GeV}/c$ .

3578 diagram of a perfectly calibrated classifier would be a diagonal line.

3579 In this case, I try to correct the raw response of the classifiers by applying a sigmoid  
3580 function:

$$\sigma(x; A, B) = \frac{1}{1 + e^{Ax+B}}, \quad (6.18)$$

3581 where the parameters  $A$  and  $B$  are real numbers determined using the method of least  
3582 squares.

3583 For each classifier, I perform a grid search to obtain the optimal values of  $A$  and  $B$ .  
3584 For any pair, I compute the predicted probabilities as  $y_{pred} = \sigma(y_{raw}; A, B)$ , where  $y_{raw}$   
3585 are the raw predictions of the classifier<sup>10</sup>. Then, I calculate the corresponding reliability  
3586 curve, and take the sum of the squared residuals between it and the response of the  
3587 perfectly calibrated classifier.

3588 Figure 6.28 shows the reliability diagrams for the original (blue) and calibrated  
3589 (yellow) probability predictions of the classifier for the III momentum range,  $0.3 \leq p <$   
3590  $0.8 \text{ GeV}/c$ . The original response of the classifier is given by  $y_{pred} = \sigma(y_{raw}; -2, 0)$ ,  
3591 which is the transformation applied by `scikit-learn` to produce the probability estimate.  
3592 Notice how the calibrated prediction matches the ideal response much better than the

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<sup>10</sup>In `scikit-learn` these correspond to the outputs of the `decision_function` method.

## CHAPTER 6. PARTICLE ID IN ND-GAr

3593 original, across all the probability range.

3594 One can also compare the responses of the uncalibrated and calibrated classifiers  
3595 broken down by true particle type, as shown in Fig. 6.29. It can be seen that the  
3596 distributions for both muons (blue) and charged pions (red) smoothen after calibration,  
3597 but still the separating power of the classifier remains unchanged.

3598 At this point, having the trained classifiers and the probability calibration parameters,  
3599 I am able to assess the performance of the classification strategy in a physics-relevant  
3600 case.

### 3601 6.3.6 Performance

## 3602 6.4 ECal time-of-flight

3603 Looking at Fig. 6.20, it is clear that for momentum values in the range  $1.0 - 3.0 \text{ GeV}/c$   
3604 it is not possible to separate pions and protons using a  $\langle dE/dx \rangle$  measurement in the  
3605 HPgTPC. However, in the previous section I assumed that protons at those energies  
3606 could be identified by other means, and therefore were not an issue for the muon and  
3607 pion discrimination.

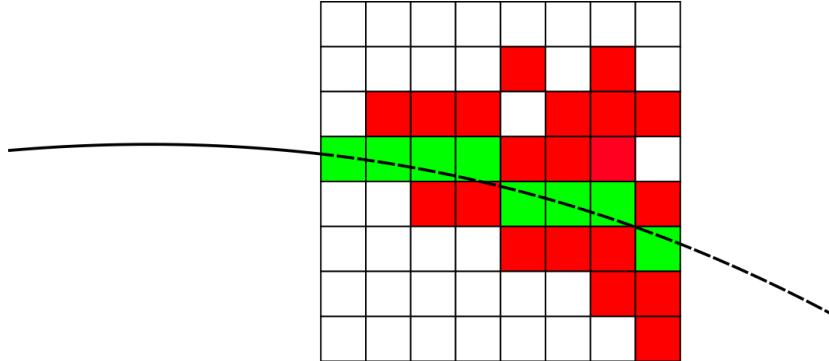
3608 Some detectors, like ALICE [161] or the ILD concept [162], complement the PID  
3609 capabilities of their gaseous trackers with time-of-flight measurements. The use of  
3610 fast timing silicon sensors, with hit time resolutions under 100 ps, would allow for the  
3611 identification of charged hadrons via a ToF measurement up to  $5.0 \text{ GeV}/c$ . In the case  
3612 of ND-GAr, one could think of using the inner layers of the ECal, the ones consisting of  
3613 high-granularity tiles, to obtain a ToF-based PID, with some inputs from the TPC.

3614 Measuring the momentum and the velocity of a charged particle allows for a  
3615 determination of the mass through the relativistic momentum formula:

$$m = \frac{p}{\beta} \sqrt{1 - \beta^2}. \quad (6.19)$$

3616 In our case, the momentum is measured in the TPC, using the curvature and the dip

## 6.4. ECAL TIME-OF-FLIGHT



**Figure 6.30:** Schematic of the hit selection used for the ToF measurement. The grid represents the layers of the inner ECAL, with coloured squares indicating the tiles with hits. Green squares indicate the selected hits.

angle of the helix inside the magnetic field. The velocity of the particle can be written as:

$$\beta = \frac{\ell_{track}}{c\tau}, \quad (6.20)$$

where  $\ell_{track}$  is the length of the track, and  $\tau$  the arrival time to the ECAL.

In GArSoft, the track length is computed at the Kalman filter stage. It is simply the sum of the line segments along the track, either in the forward or backward fit. In this case, because we are only interested in the particles that make it to the ECAL, I choose the fit direction based on the results of the track-cluster associations.

Additionally, because the last 30 cm of the TPC radius are uninstrumented<sup>11</sup>, I need to correct for the length of the tracks. Using the track fit parameters to propagate the helix to its entry point in the ECAL, one can write the total track length as:

$$\ell_{track} = \ell + \left| \frac{\phi_{EP} - \phi}{R^{-1}} \right| \sqrt{1 + \tan^2 \lambda}, \quad (6.21)$$

where  $\phi_{EP}$  is the angle of rotation at the entry point to the calorimeter, and  $\ell$ ,  $\phi$ ,  $R$  and  $\lambda$  are the track length, angle of rotation, radius of curvature and dip angle at the last point in the fit, respectively.

To test the idea of performing a ToF measurement with the inner ECAL, I generated

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<sup>11</sup>Note to self: check this number.

## CHAPTER 6. PARTICLE ID IN ND-GAr

3631 two data samples. Each consists of 10000 single particle events, either charged pions or  
3632 protons. Their momenta are uniformly distributed in the range  $0.5 - 5.0 \text{ GeV}/c$ , and  
3633 their directions are isotropic. I process each sample using different values of the time  
3634 resolution, from  $\Delta\tau = 0$ , the perfect time resolution case for comparison, to the current  
3635 nominal value of  $\Delta\tau = 0.7 \text{ ns}$ , and the worse scenario of  $\Delta\tau = 1.0 \text{ ns}$ .

### 3636 6.4.1 Arrival time estimations

3637 In the simulation, the limited time resolution of the ECal is taken into account by  
3638 applying a Gaussian smearing to the true hit times. Other effects, like the digitisation  
3639 of the signals, are not taken into account and fall beyond the scope of this study. After  
3640 the track-cluster, one ends up with a collection of ECal hits associated to each particle.  
3641 From these, the arrival time of the particle to the ECal can be extracted.

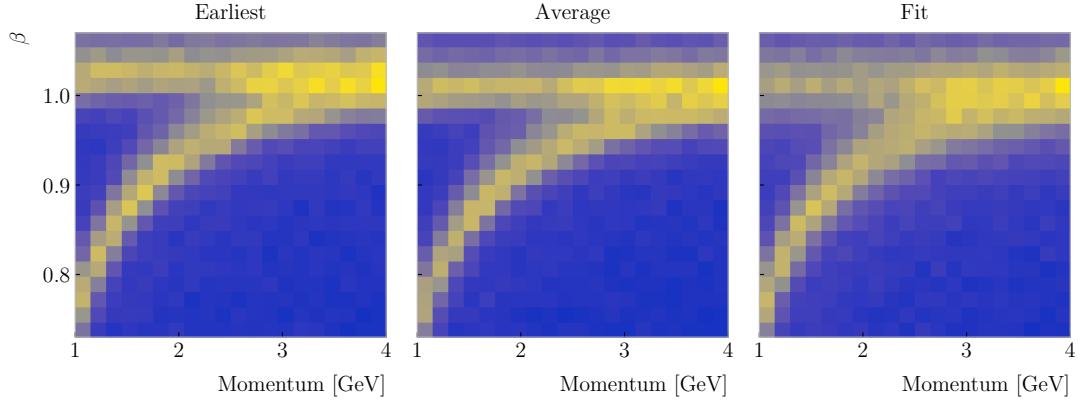
3642 The simplest possibilities are to either take the time of the earliest hit or the hit  
3643 closest to the entry point. Because these two coincide, in general, I focused only in  
3644 the earliest hit time. However, this needs to be corrected, to account for the distance  
3645 travelled from the entry point to the position of the hit:

$$\tau_{earliest} = \tau_{hit} - \frac{d_{EP-hit}}{c}, \quad (6.22)$$

3646 where  $\tau_{hit}$  is the time of the earliest hit, and  $d_{EP-hit}$  is the distance between that hit  
3647 and the entry point of the particle to the ECal. This is computed as the arc length  
3648 between the entry point and the point of the extrapolated helix up to the layer of the  
3649 hit. This way of correcting the time assumes  $c$  for the propagation of the particle, which  
3650 may lead to biased estimates.

3651 I also tried to estimate the arrival times using information from the rest of the hits.  
3652 In order to do this, as a simplifying assumption, I approximate the hadronic shower  
3653 considering only its MIP component. For each layer, I keep only the hit in the tile closest  
3654 to the point of the extrapolated track up to that layer. Figure 6.30 shows an example of  
3655 how this hit selection works. The dashed line represents the extrapolated track, while

## 6.4. ECAL TIME-OF-FLIGHT



**Figure 6.31:** Particle velocity versus momentum measured with different ECal arrival time estimations. From left to right: earliest hit time, average hit time, and fitted hit time. In all cases the time resolution is  $\Delta\tau = 0.1$  ns.

the coloured squares are the tiles containing hits. Green indicates the tiles closer to the track in each layer (in the sketch they correspond to the grid columns).

Now, I can use these collections of hits to estimate the arrival times. A possibility is to take the average of the times of the selected hits, denoted  $\tau_{average}$ . For that to work, one needs to correct these times, in a similar way as in Eq. (6.22), before taking the average. However, as before, this correction assumes that the particle travels at the speed of light inside the ECal. Another option is to perform a linear fit to the hit times and the distances to the entry point. In that case, the arrival time would be the fitted value of the intercept,  $\tau_{fit}$ . This method would not assume a speed of light propagation.

Figure 6.31 shows the velocity estimations as a function of the particle momentum, for the earliest hit time (left panel), average hit time (middle panel), and fitted hit time (right panel). The two bands correspond to the  $\pi^\pm$  and the  $p$  particles.  $\Delta\tau = 0.1$  ns. Notice how, for the earliest hit time method, the velocities are significantly biased towards larger values. For the multi-hit methods, the  $\tau_{fit}$  estimate appears to produce a larger variance than when using the  $\tau_{average}$  method.

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### 3671 6.4.2 Proton and pion separation

3672 Once we have the velocities of the particles, one can estimate their masses through  
3673 Eq. (6.19). The resulting mass spectra are shown in Fig. 6.32. I computed the masses  
3674 for the three arrival time estimates discussed above, and three different values of the  
3675 time resolution:  $\Delta\tau = 0.00$  (perfect time resolution),  $\Delta\tau = 0.10$  ns, and  $\Delta\tau = 0.70$  ns.  
3676 Although in all cases we have the same number of events, it appears as if the entries  
3677 in the histograms decrease as the time resolution increases. Sometimes, the particles  
3678 get unphysical values of  $\beta > 1$ , and in turn they do not contribute to the mass spectra.  
3679 This is more likely to happen for higher values of  $\Delta\tau$ .

3680 As noted before, the average hit time method produces the most robust estimates  
3681 when increasing  $\Delta\tau$ . Intuitively this makes sense, as by taking the mean one averages  
3682 out the effect of the Gaussian smearing. Going forward, I will use this arrival time  
3683 estimator, as it appears to be the best performing one.

3684 It is possible to use the velocity estimations to select a sample of protons. In this  
3685 case, I do so by dividing the relevant momentum range in bins of  $0.1 \text{ GeV}/c$ . For each  
3686 momentum bin, I compute the expected velocity for the protons via the inverse of Eq.  
3687 (6.19), and then take the fractional residuals of the measured velocities. Using that  
3688 distribution, I choose the cut that maximises the  $F_1$ -score of the proton selection.

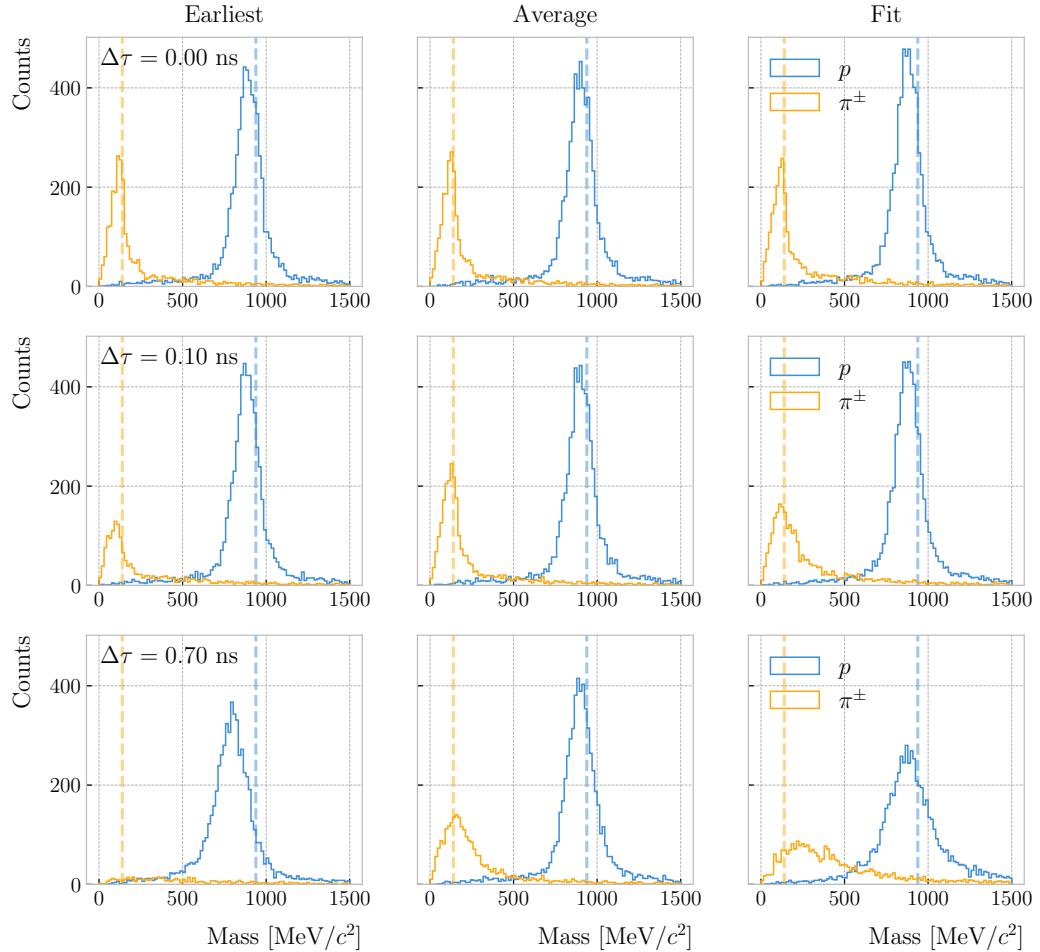
3689 The results can be seen in Fig. 6.33, for the case  $\Delta\tau = 0.10$  ns. As expected from  
3690 Fig. 6.31, the performance of the selection degrades rapidly with increasing momentum.  
3691 However, the purity is still around 75% at  $3.0 \text{ GeV}/c$ . This is likely to be sufficient, as  
3692 we do not expect protons or charged pions with higher energies from the beam neutrino  
3693 interactions.

3694 Figure 6.34

### 3695 6.5 Charged pion decay in flight

3696 As discussed previously, in GArSoft the TPC tracks are formed after a pattern recognition  
3697 algorithm and a Kalman filter are applied to the TPC clusters. These two steps can

## 6.5. CHARGED PION DECAY IN FLIGHT

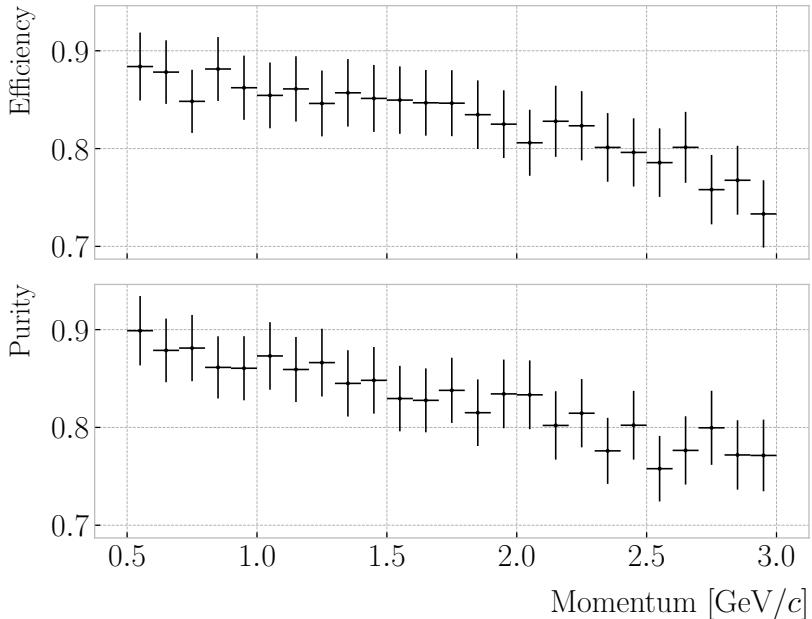


**Figure 6.32:** Mass spectra for  $p$  (blue) and  $\pi^\pm$  (yellow) particles, using different ECal time resolution values (from top to bottom, in ascending order), and arrival time estimates. From left to right: earliest hit time, average hit time, and fitted hit time. The dashed lines indicate the true masses of the particles.

3698 find discontinuities in the track candidates (e.g. due to a particle decay) when these  
 3699 so-called breakpoints are large enough. However, for some, more subtle, cases they may  
 3700 miss them and form a single reconstructed track. It has been noted in the literature  
 3701 that Kalman filters offer, as a by-product, additional information to form test statistics  
 3702 to identify these breakpoints [163, 164].

3703 Considering the mean life of the charged pion,  $\tau = (2.6033 \pm 0.0005) \times 10^{-8}$  s, one  
 3704 can estimate that about 12% of the pions with momentum  $p \sim \mathcal{O}(500 \text{ MeV}/c)$  (roughly  
 3705 the peak of the pion momentum distribution in  $\nu_\mu$  CC interactions off argon) decay

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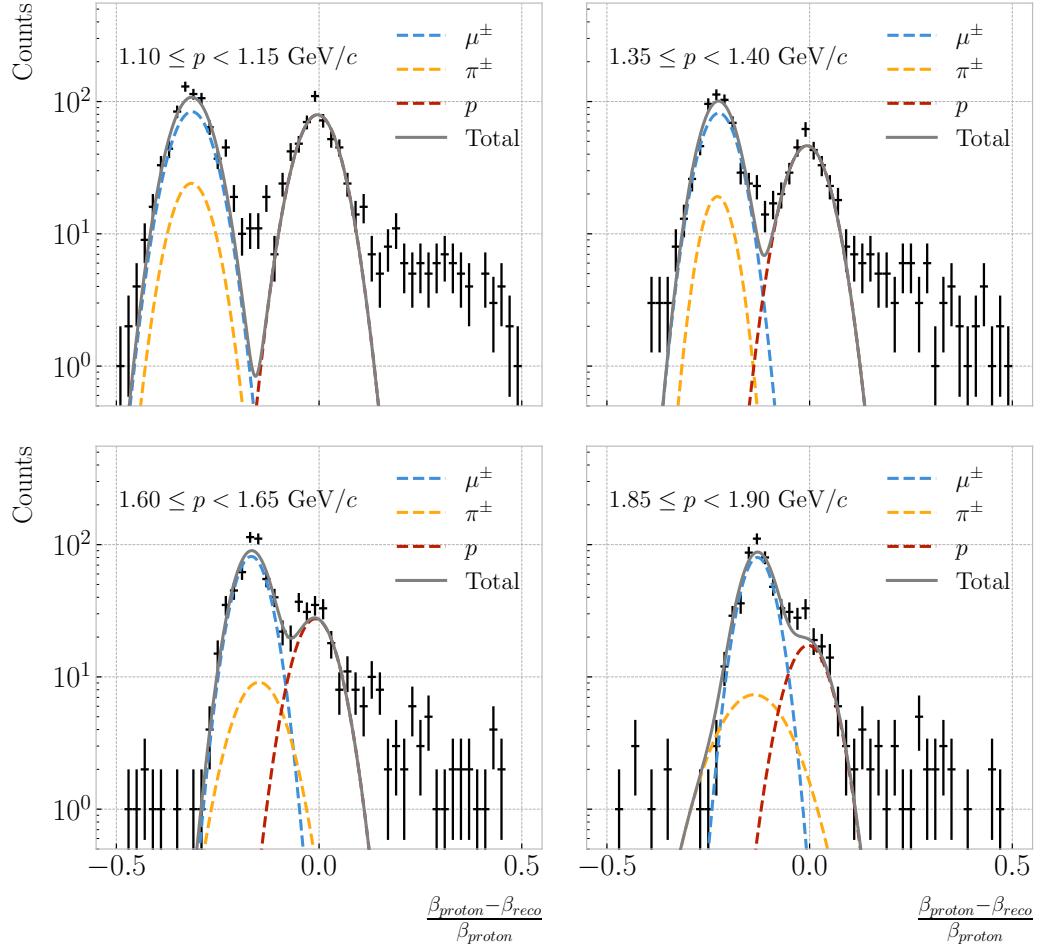
**Figure 6.33:** Efficiency (top panel) and purity (bottom panel) for the proton selection as a function of the momentum, for  $\Delta\tau = 0.10$  ns.

3706 inside the TPC. Figure 6.35 (left panel) shows the amount of charged pions decaying in  
 3707 the full TPC and fiducial volumes from an isotropic, monoenergetic sample of 100000  
 3708 negatively charged pions with  $p = 500$  MeV/ $c$ . We see that about 10% of those decayed,  
 3709 with more than half of them decaying inside the TPC fiducial volume.

3710 Figure 6.35 (right panel) shows an example event display of a charged pion (magenta  
 3711 line) decays in flight inside the TPC, but because the angle of the muon (blue line) is  
 3712 small both were reconstructed as one single track (black line). In this case, the composite  
 3713 track reaches the ECal, where it undergoes a muon-like interaction, thus being classified  
 3714 as a muon.

3715 A way to understand what decaying pion tracks were totally or partially reconstructed  
 3716 together with the daughter muon is looking at the relative energy contributions to the  
 3717 reconstructed track. In order to select a sample of such events, I require that a minimum  
 3718 50% of the total energy comes from the pion and at least 20% from the muon.

## 6.5. CHARGED PION DECAY IN FLIGHT



**Figure 6.34:** Distributions of the velocities measured by ToF with the inner ECal, for different momentum bins, in a FHC neutrino interaction sample. The Gaussian fits are performed around the maxima for each particle species.

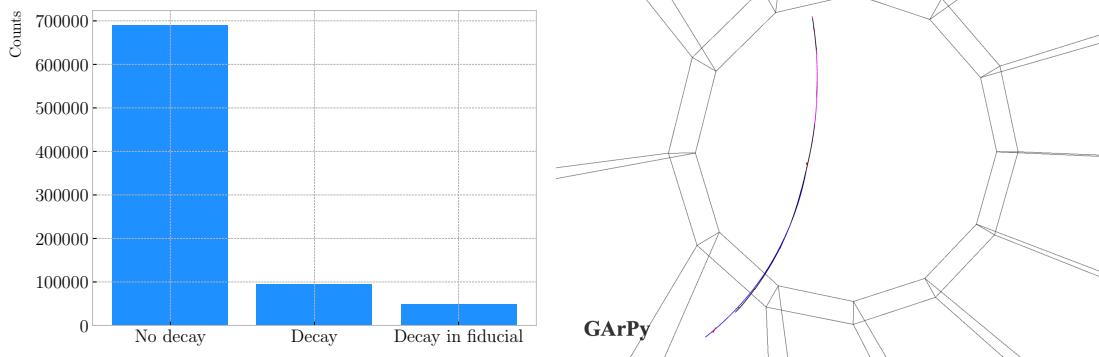
### 3719 6.5.1 Track breakpoints

3720 To identify potential decays we can use the information we obtain from the Kalman  
 3721 filter at each step of the fitted track. The simplest test we can think about is computing  
 3722 the  $\chi^2$  of the mismatch between all the parameters in the forward and the backward fits:

$$\chi_k^{2 (FB)} = (\hat{x}_k^B - \hat{x}_k^F)^T [V^{(\hat{x}_k, B)} + V^{(\hat{x}_k, F)}]^{-1} (\hat{x}_k^B - \hat{x}_k^F), \quad (6.23)$$

3723 where  $\hat{x}_k^F$ ,  $\hat{x}_k^B$  are the Kalman filter state vector estimates at step  $k$  in the forward and  
 3724 backward fits and  $V^{(\hat{x}_k, F)}$ ,  $V^{(\hat{x}_k, B)}$  the covariance matrices of  $\hat{x}_k^F$  and  $\hat{x}_k^B$  respectively.

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**Figure 6.35:** Left panel: number of non-decaying, decaying and decaying in the fiducial volume pions for a MC sample of 100000,  $p = 500$  MeV/c isotropic positively charged pions inside the TPC. Right panel: event display for a positive pion decaying inside the fiducial volume, with a single reconstructed track for the pion and muon system.

3725 Using the values of the  $\chi^2$  at measurement  $k$  for the forward and backward fits we can  
 3726 compute another  $\chi^2$  value that characterises the overall track fit:

$$\chi_{track}^2 = \chi_k^{2(F)} + \chi_k^{2(B)} + \chi_k^{2(FB)}, \quad (6.24)$$

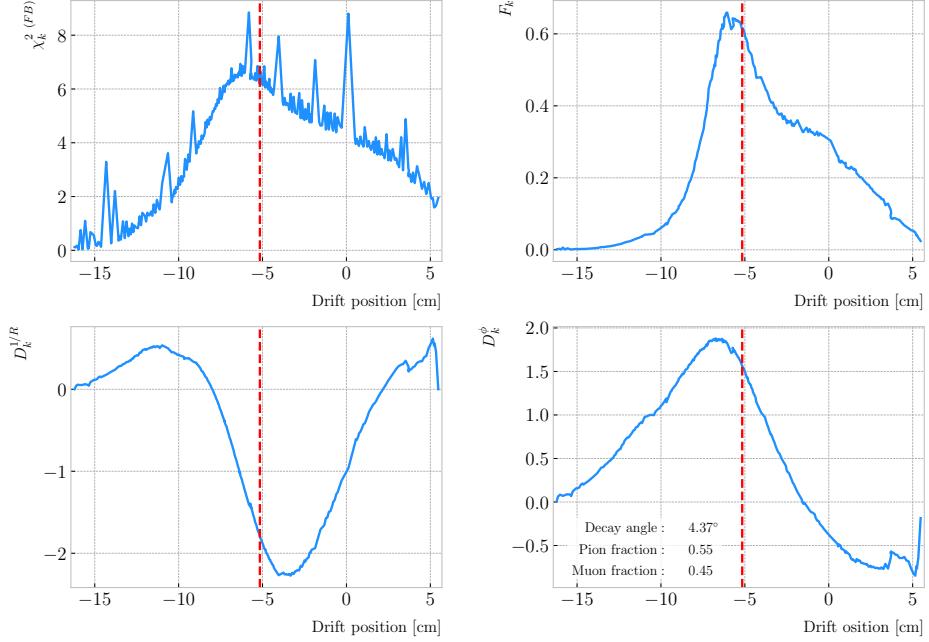
3727 which remains approximately constant for all  $k$ .

3728 An alternative approach proposed in the context of the NOMAD experiment was  
 3729 using a fit with a more elaborate breakpoint hypothesis, so we can perform a comparison  
 3730 of the  $\chi^2$  with and without breakpoints. This can be achieved by using some alternative  
 3731 parametrisation with extra parameters, which allows some of the track parameters to  
 3732 be discontinuous at certain points. A decay changes the momentum magnitude and  
 3733 direction, so we can use the new state vector:

$$\alpha = (y, z, 1/R_F, 1/R_B, \phi_F, \phi_B, \tan\lambda_F, \tan\lambda_B)^T. \quad (6.25)$$

3734 As we already have the estimates from the standard Kalman filter and their  
 3735 covariance matrices at each point, we do not need to repeat the Kalman fit for the new  
 3736 parametrisation. Instead, I can compute the values of  $\alpha$  at each point  $k$  that minimise

## 6.5. CHARGED PION DECAY IN FLIGHT



**Figure 6.36:** Values of  $\chi_k^2(FB)$  (top left panel),  $F_k$  (top right panel),  $D_k^{1/R}$  (bottom left panel) and  $D_k^\phi$  (bottom right panel) versus position along the drift direction for a reconstructed track in a positive pion decay event. The vertical red dashed line indicates the true location of the decay point.

3737 the  $\chi^2$  resulting from comparing them to  $\{\hat{x}_k^B, \hat{x}_k^F\}$ . Introducing the two  $5 \times 8$  matrices:

$$H^F = \begin{pmatrix} 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \end{pmatrix}, \quad H^B = \begin{pmatrix} 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}, \quad (6.26)$$

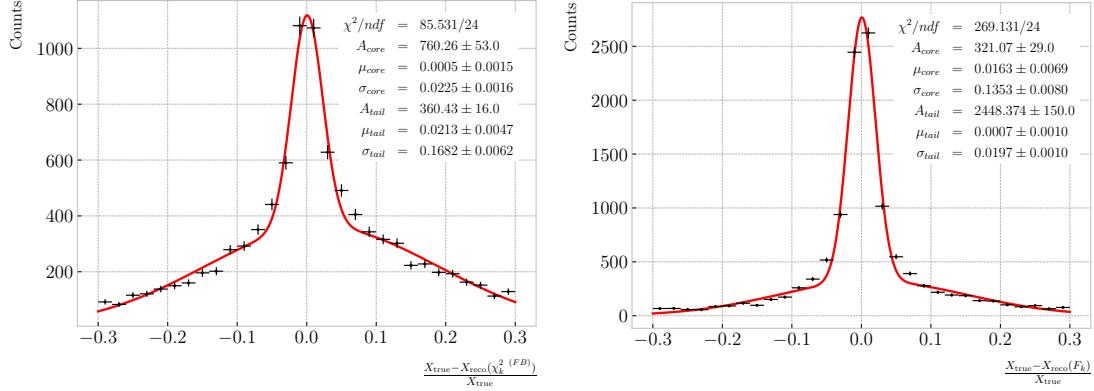
3738 we can write this as:

$$\begin{aligned} \chi_k^2(FB)(\alpha) &= (\hat{x}_k^F - H^F \alpha)^T \left[ V^{(\hat{x}_k, F)} \right]^{-1} (\hat{x}_k^F - H^F \alpha) \\ &\quad + (\hat{x}_k^B - H^B \alpha)^T \left[ V^{(\hat{x}_k, B)} \right]^{-1} (\hat{x}_k^B - H^B \alpha). \end{aligned} \quad (6.27)$$

3739 The minimum of  $\chi_k^2(FB)(\alpha)$  is found when the measured new state vector takes the  
3740 value:

$$\hat{\alpha}_k = V^{(\hat{\alpha}_k)} H^T (V^{(\hat{x}_k)})^{-1} \hat{X}, \quad (6.28)$$

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**Figure 6.37:** Fractional residual distributions of the true and reconstructed decay position along the drift coordinate, using the position of the maximum of  $\chi_k^2(FB)$  (left panel) and  $F_k$  (right panel) as estimates of the decay position. Also shown are double Gaussian fits to these points (red lines).

3741 where  $\hat{X} = \{\hat{x}_k^B, \hat{x}_k^F\}$ ,  $V^{(\hat{x}_k)}$  is the block diagonal matrix formed by  $V^{(\hat{x}_k, F)}$  and  $V^{(\hat{x}_k, B)}$   
 3742 and  $V^{(\hat{\alpha}_k)}$  is the covariance matrix of  $\hat{\alpha}_k$ , given by:

$$V^{(\hat{\alpha}_k)} = \left( H^T (V^{(\hat{x}_k)})^{-1} H \right)^{-1}. \quad (6.29)$$

3743 From these new fit estimates we can compute the  $F$  statistic, which tells us whether  
 3744 the model with breakpoint provides a statistically significant better fit:

$$F_k = \left( \frac{\chi_{track,k}^2 - \chi_{full,k}^2}{8 - 5} \right) / \left( \frac{\chi_{full,k}^2}{N - 8} \right). \quad (6.30)$$

3745 One can also compute the signed difference of the duplicated variables divided by  
 3746 their standard deviation at each point. These represent how significant the discontinuity  
 3747 in each variable is. For any variable  $\eta$  we can write it as:

$$D_k^\eta = \frac{\hat{\eta}_k^B - \hat{\eta}_k^F}{\sqrt{\text{Var}[\hat{\eta}_k^F] + \text{Var}[\hat{\eta}_k^B] - 2\text{Cov}[\hat{\eta}_k^F, \hat{\eta}_k^B]}}, \quad (6.31)$$

3748 In our case, the relevant ones to look at are  $D_k^{1/R}$  and  $D_k^\phi$ .

3749 Figure 6.36 shows the values of  $\chi_k^2(FB)$ ,  $F_k$ ,  $D_k^{1/R}$  and  $D_k^\phi$  as functions of the position  
 3750 along the drift direction, for an example reconstructed track with 55.5% of the energy

## 6.5. CHARGED PION DECAY IN FLIGHT

3751 coming from the charged pion and 45.5% from the daughter muon. The true position of  
 3752 the decay is indicated (dashed red lines). Notice how  $\chi_k^{2(FB)}$  and  $F_k$ ,  $D_k^{1/R}$  reach their  
 3753 maxima near the decay point. In the former case this indicates a large forward-backward  
 3754 difference in the track fit. In the later it represents that the extended state vector  
 3755 improves the fit particularly around that point.

3756 I can estimate the decay position finding resolution by computing the difference  
 3757 between the  $X$  position of the maxima of  $\chi_k^{2(FB)}$  and  $F_k$  and the  $X$  position of the  
 3758 true decay. Figure 6.37 represent the the fractional residual distributions for both  
 3759 cases, from the sample of tracks containing pion decays. Fitting a double Gaussian to  
 3760 the distributions (red lines) I find a resolution of  $(3.31 \pm 0.15)\%$  and  $(6.94 \pm 0.31)\%$   
 3761 respectively.

3762 In principle, the  $F$ -statistic should follow a Fisher distribution with  $(8 - 5)$  and  
 3763  $(N - 8)$  degrees of freedom under the null hypothesis. In most of our cases  $N \sim \mathcal{O}(100)$ ,  
 3764 so the probability density functions will look very similar. In this case, it is safe to take  
 3765 the limit  $N \rightarrow \infty$  in the Fisher PDF:

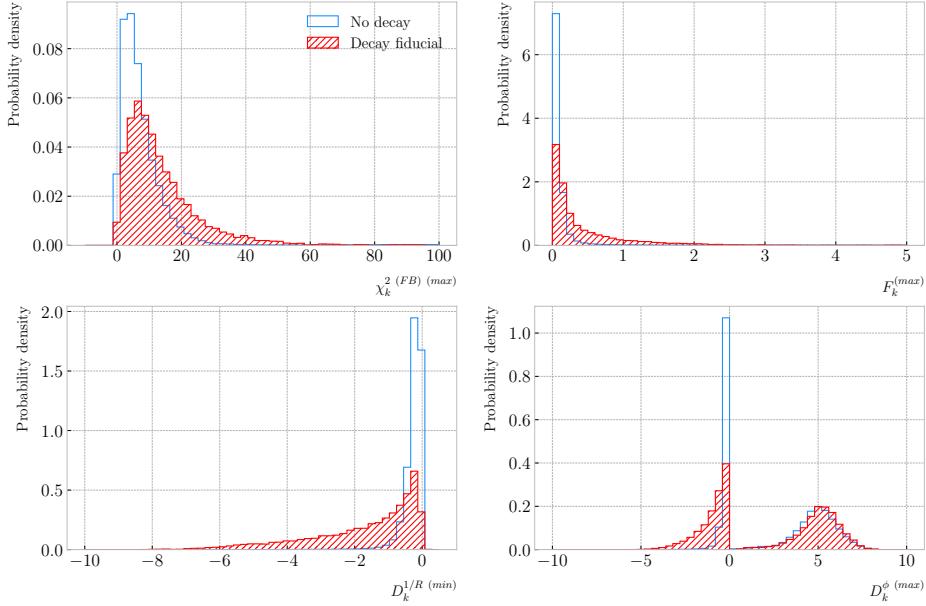
$$\begin{aligned}\tilde{f}(x; a - b) &= \lim_{N \rightarrow \infty} f(x; a - b, N - a) \\ &= \frac{2^{-\frac{a-b}{2}}}{\Gamma\left(\frac{a-b}{2}\right)} (a - b)^{\frac{a-b}{2}} x^{\frac{a-b}{2}-1} e^{-\frac{a-b}{2}x}.\end{aligned}\tag{6.32}$$

3766 In our case  $a - b = 8 - 5 = 3$ , so we would obtain a p-value of 0.05 at  $x = 2.60$ .

3767 Figure 6.38 contains the distributions of the maxima of  $\chi_k^{2(FB)}$ ,  $F_k$  and  $D_k^\phi$  and the  
 3768 minima of  $D_k^{1/R}$  for a sample of non-decaying pion tracks (blue) and another sample of  
 3769 reconstructed tracks containing part of the pion and the daughter muon from a decay  
 3770 inside the fiducial volume (red). Notice that, even though the values of  $F_k^{(max)}$  for the  
 3771 decay sample are typically larger than for the non-decaying one, just a small fraction of  
 3772 the events go beyond the aforementioned value of  $F = 2.60$ . Therefore, from a practical  
 3773 point of view, it is not the most efficient variable to use for selecting the decay events.

3774 However, looking at the  $D_k^{1/R \text{ (min)}}$  distribution we can see there is a big difference  
 3775 between non-decaying and decaying events in this variable. One can use a combination

## CHAPTER 6. PARTICLE ID IN ND-GAr



**Figure 6.38:** Distributions of the extreme values of  $\chi_k^2(FB)$  (top left panel),  $F_k$  (top right panel),  $D_k^{1/R}$  (bottom left panel) and  $D_k^\phi$  (bottom right panel) for non-decaying reconstructed pion tracks (blue) and tracks which include the decay inside the fiducial volume (red).

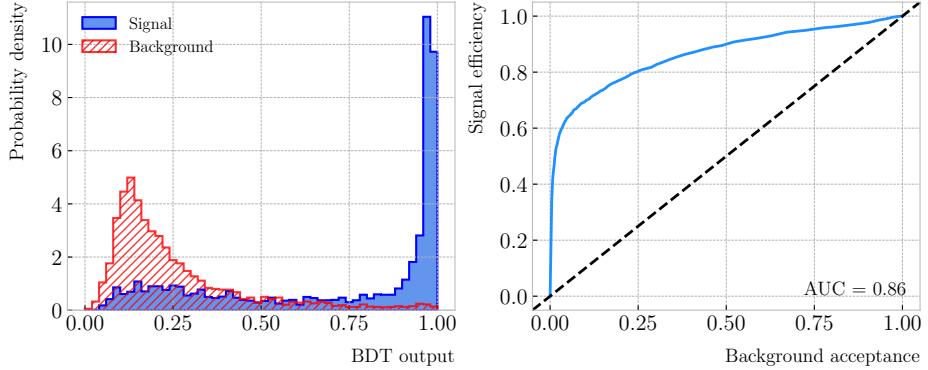
3776 of these four variables to distinguish between the pion decay events (signal) and the  
 3777 non-decaying pions (background).

3778 An approach to this classification could be using a boosted decision tree (BDT). One  
 3779 of the advantages of BDTs is that they are easy to interpret and identify the relative  
 3780 importance of the different input variables. Training a BDT with 400 estimators and a  
 3781 maximum depth of 4 I can obtain an efficient classification without overtraining. Figure  
 3782 6.39 (left panel) shows the distribution of probabilities predicted by the BDT for a test  
 3783 sample. The signal efficiency as a function of background acceptance, the so-called ROC  
 3784 curve, is shown in Fig. 6.39 (right panel). With a relative importance of 0.83, the most  
 3785 important variable turned out to be  $D_k^{1/R} \text{ (min)}$ .

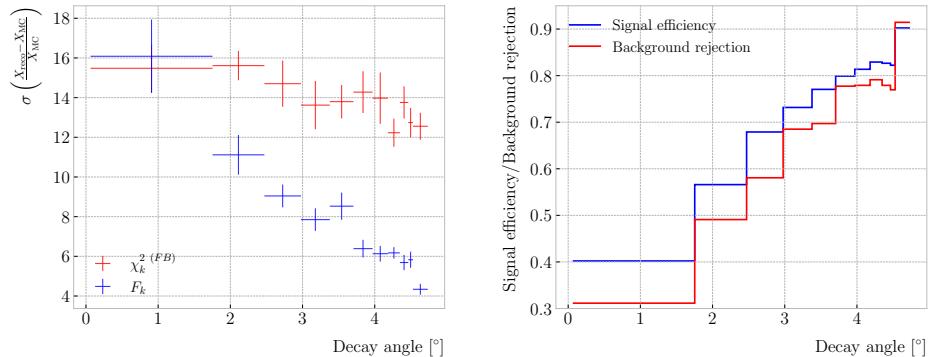
3786 One thing we can check is how the resolution to the decay and the signal efficiency in  
 3787 the classification changes with the true decay angle. Using an equal-frequency binning  
 3788 for the decay angles, we can repeat the previous steps for each bin.

3789 Figure 6.40 (left panel) shows the dependence on the decay angle of the decay finding

## 6.5. CHARGED PION DECAY IN FLIGHT



**Figure 6.39:** Left panel: distributions of the predicted probabilities assigned by the BDT classifier to a test sample of decaying pion+muon tracks (blue) and non-decaying pion tracks (red). Left: signal efficiency versus background acceptance (ROC curve) obtained from the BDT for the test sample.



**Figure 6.40:** Left panel: dependence of the decay position finding resolution on the true value of the decay angle for the  $\chi_k^2(FB)$  (red) and  $F_k$  (blue) methods. Right panel: signal efficiency (blue line) and background rejection (red line) from the BDT classifier versus true decay angle.

resolution. We can see that for the  $\chi_k^2(FB)$  maximum location method the resolution consistently lies between 12 to 16%. However, the  $F_k^{(\max)}$  approach gives a significantly better resolution for high angle values, reaching the 4 – 6% range for decay angles  $\geq 4^\circ$ .

For the classification dependence on the angle, I use the same classifier I trained before but evaluating the test sample for each individual angular bin. I compute the signal efficiency in each bin for a fixed value of the background rejection, in this case 90%. Similarly, for the background rejection estimation I use a fixed signal efficiency value of 90%. Figure 6.40 (right panel) represents the change in signal efficiency (blue)

## CHAPTER 6. PARTICLE ID IN ND-GAr

3798 and background rejection (red) with the value of the true decay angles.

## 3799 6.6 Neutral particle identification

### 3800 6.6.1 ECal clustering

3801 Another important reconstruction item is the clustering algorithm of ECal hits in  
3802 GArSoft. The default module features a NN algorithm that treats all hits in the same  
3803 way, independently of the layer each hit comes from. However, the current ECal design  
3804 of ND-GAr has two very different types of scintillator layers. The inner layers are made  
3805 out of tiles, which provide excellent angular and timing resolutions. On the other hand,  
3806 the outer layers are cross scintillator strips. That way, an algorithm that treats hits  
3807 from both kinds of layers differently may be able to improve the current performance.

3808 Inspired by the reconstruction of T2K’s ND280 downstream ECal [165], the idea  
3809 was to put together a clustering module that first builds clusters for the different ECal  
3810 views (tiles, strips segmented in the  $X$  direction and strips segmented in  $Y$  direction),  
3811 and then tries to match them together to form the final clusters.

3812 Working on a module-by-module basis, the algorithm first separates the hits depending  
3813 on the layer type they come from. Then, it performs a NN clustering for the 3 sets of  
3814 hits separately. For the tile hits it clusters together all the hits which are in nearest-  
3815 neighbouring tiles and nearest-neighbouring layers, for strip hits it looks at nearest-  
3816 neighbouring strips and next-to-nearest-neighbouring layers (as the layers with strips  
3817 along the two directions are alternated). For strip clusters an additional cut in the  
3818 direction along the strip length is needed.

3819 After this first clustering I then apply a recursive re-clustering for each collection  
3820 of strip clusters based on a PCA method. In each case, we loop over the clusters with  
3821  $N_{hits} \geq 2$ , computing the centre of mass and three principal components. Propagating  
3822 these axes up to the layers of the rest of the clusters, we check if the propagated point  
3823 and the centre of mass of the second cluster are within next-to-nearest-neighbouring  
3824 strips. An additional cut in the direction along the strip length is also needed. Moreover,

## 6.6. NEUTRAL PARTICLE IDENTIFICATION

3825 I require that the two closest hits across the two clusters are at most in next-to-nearest-  
3826 neighbouring strips. I merge the clusters if these three conditions are satisfied. The  
3827 re-clustering is repeated until no more cluster pairs pass the cuts.

3828 The clusters in each strip view are combined if their centres of mass are close enough  
3829 and they point in the same direction. An alternative approach for the strip cluster  
3830 merging could be to compute the overlap between the ellipsoids defined by the principal  
3831 axes of the clusters, and then merge the pair if the overlap exceeds some threshold.  
3832 Further study is needed to understand if this change would have an impact in the overall  
3833 clustering performance.

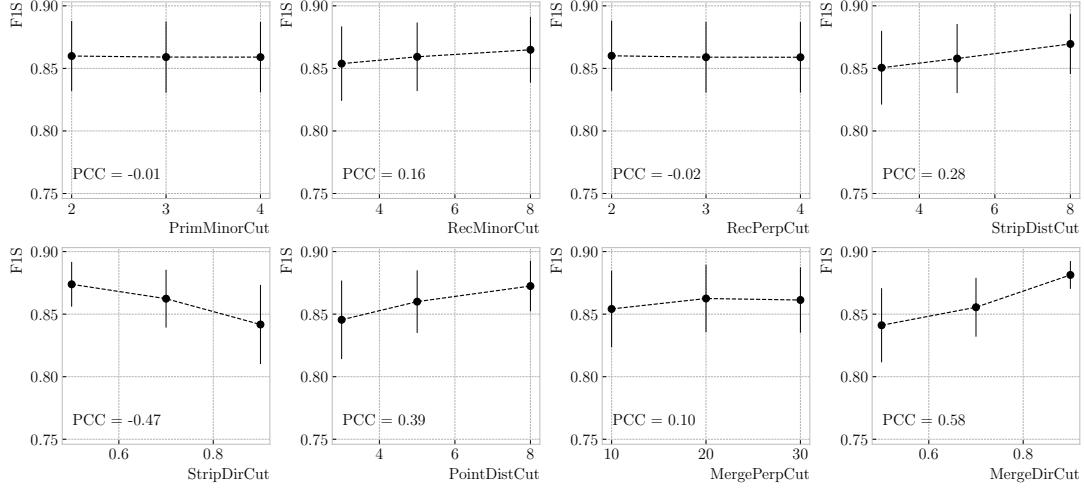
3834 To merge the tile clusters to the combined strip clusters I propagate the principal  
3835 axis of the strip cluster towards the inner layers, up to the centre of mass layer of the  
3836 tile cluster. I merge the clusters if the distance between the propagated point and the  
3837 centre of mass is below a certain cut.

3838 The last step is to check if clusters in neighbouring modules should be merged  
3839 together, both across two barrel modules, across end cap modules and between barrel  
3840 end cap modules. I check the distance between the two closest hits in the pair of clusters  
3841 and merge them if it passes this and an additional direction cut.

3842 Figure ?? presents an example of the clustering steps relevant for strip layer hits, from  
3843 the input hits (top left panel) to the NN clustering (top right panel) and re-clustering  
3844 (bottom left panel) for each strip view and the final merging strip clusters (bottom  
3845 right panel). It shows the hits from a single ECal barrel module in a  $\nu_\mu$  CC interaction  
3846 event with a neutral pion and a proton in the final state. The two clusters on the left  
3847 correspond to the photon pair from the  $\pi^0$  decay and the one on the upper right corner  
3848 is associated to the proton.

3849 This algorithm has a total number of eight free parameters that need to be optimised.  
3850 I used a sample of 1000  $\nu_\mu$  CC interactions in order to obtain the optimal configuration of  
3851 clustering parameters. This sample was generated up to the default ECal hit clustering  
3852 level, so then I could run the new clustering algorithm each time with a different  
3853 configuration of parameters. As the number of parameters is relatively large, I only

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**Figure 6.41:** Mean values of the  $F_1$ -score marginal distributions for the different free parameters of the new clustering algorithm, with the error bars representing one standard deviation around the mean. The  $F_1$ -score values were computed for the 6561 possible parameter configurations using 1000  $\nu_\mu$  CC interaction events.

**Table 6.5:** Summary of parameters and sampled values used in the optimisation of the clustering algorithm.

Name	Units	Sampled values	Description
PrimMinorCut	strips	2, 3, 4	Distance along strip length in NN clustering
RecMinorCut	strips	3, 5, 8	Distance between propagated point and CM along strip length in re-clustering
RecPerpCut	strips	2, 3, 4	Closest hit pair distance in re-clustering
StripDistCut	strips	3, 5, 8	Distance between CMs in strip cluster merging
StripDirCut	cos	0.5, 0.7, 0.9	Main axes direction cut in strip cluster merging
PointDistCut	tiles	3, 5, 8	Distance between propagated point and CM in strip-tile matching
MergePerpCut	cm	10, 20, 30	Closest hit pair distance in module merging
MergeDirCut	cos	0.5, 0.7, 0.9	Main axes direction cut in module merging

3854 performed a coarse-grained scan of the parameter space. Sampling each of the eight  
 3855 parameters at three different points each I obtain 6561 different configurations. These  
 3856 parameters, together with the used values, are summarised in Tab. 6.5.

3857 In order to measure the performance of the clustering, I use a binary classification  
 3858 approach. For each formed cluster, I identify the Geant4 Track ID of the matching MC  
 3859 particle and the energy fraction of each hit. Then, I assign to each cluster the Track ID  
 3860 with the highest total energy fraction. For each of the different Track IDs associated to

## 6.6. NEUTRAL PARTICLE IDENTIFICATION

3861 the clusters, I select the cluster with the highest energy (only from the hits with the  
3862 same Track ID). I identify such a cluster as the main cluster for that Track ID. I count  
3863 as true positives (TPs) the hits with the correct Track ID in each main cluster. False  
3864 positives (FPs) are the hits with the incorrect Track ID for the cluster they are in, not  
3865 only main clusters. The false negatives (FNs) are the hits with the correct Track ID in  
3866 clusters other than the main.

3867 Figure 6.41 shows the computed  $F_1$ -score values for the different cuts. In each case,  
3868 the central value represents the mean of the  $F_1$ -score distribution for the specified value  
3869 of the corresponding variable and the vertical error bar represents one standard deviation  
3870 around the mean. Also shown are the Pearson correlation coefficients of these central  
3871 values. We can see that five of the variables have a sizeable effect on the  $F_1$ -score, with  
3872 an absolute difference between the last and first values as big as 4%.

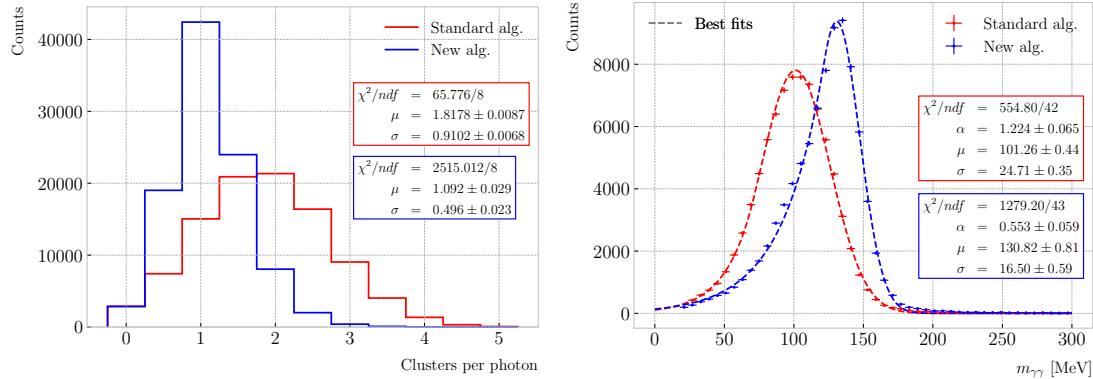
3873 The working configuration is obtained as follows. I first select all configurations  
3874 with purity  $\geq 90\%$ . Among those, I choose the combinations that yield the maximum  
3875  $F_1$ -score. If more than one configuration remains I select the one with the highest  
3876 sensitivity. Doing so, I end up with a parameter configuration with an efficiency of 88%  
3877 and a 90% purity. Compared with the default algorithm, which gives an efficiency of  
3878 76% and a purity of 91% for the same sample, I have managed to improve the efficiency  
3879 by a factor of 1.16.

### 3880 6.6.2 $\pi^0$ reconstruction

3881 One of the potential applications of the new ECal hit clustering is the reconstruction of  
3882 neutral particles, in particular pions. Neutral pions decay promptly after being produced,  
3883 through the  $\pi^0 \rightarrow \gamma\gamma$  channel ( $98.823 \pm 0.034\%$ ) of the time. The photon pair does  
3884 not leave any traces in the HPgTPC (unless one or both of them converts into an  
3885 electron-positron pair), but each of them will produce an electromagnetic shower in  
3886 the ECal.

3887 To test the potential impact of the new algorithm in  $\pi^0$  reconstruction, I generated  
3888 a MC sample of single, isotropic neutral pions inside the HPgTPC. All pions were

## CHAPTER 6. PARTICLE ID IN ND-GAr



**Figure 6.42:** Left panel: distributions of the number of ECal clusters per photon from  $\pi^0$  decays for the standard (red) and new (blue) clustering algorithms. Right panel: reconstructed invariant mass distributions for photon pairs from single  $\pi^0$  events using the standard (red) and new (blue) ECal clustering algorithms.

3889 generated with a momentum  $p = 500$  MeV and their initial positions were uniformly  
 3890 sampled inside a  $2 \times 2 \times 2$  m box aligned with the centre of the TPC. I ran both the  
 3891 default and the new clustering algorithms, using for the latter the optimised configuration  
 3892 discussed above.

3893 The first thing to notice is that the number of clusters produced per photon has  
 3894 decreased. Figure 6.42 (left panel) shows these distributions for the default (red) and  
 3895 new (blue) algorithms. Using a simple Gaussian fit, we see that the mean number of  
 3896 ECal clusters per photon went from  $1.82 \pm 0.01$  to  $1.09 \pm 0.03$ . This effectively means that  
 3897 with the new algorithm the ECal activity of one true particle is typically reconstructed  
 3898 as a single object. From the reconstruction point of view this can be an advantage. As  
 3899 now most of the photon energy ends up in a single ECal cluster, I can simply use cluster  
 3900 pairs to identify the  $\pi^0$  decay.

3901 In general, one calculates the invariant mass of the photon pair as:

$$m_{\gamma\gamma} = \sqrt{2E_1E_2(1 - \cos \theta)}, \quad (6.33)$$

3902 where  $E_i$  are the energies of the photons and  $\theta$  the opening angle between them. In this  
 3903 case I can use the energies deposited in the ECal and their incident directions. This  
 3904 quantity is computed for all possible pairs of clusters, using their position together with

## 6.7. INTEGRATION IN GArSOFT

3905 the true decay point. In a more realistic scenario, e.g.  $\nu_\mu$  CC interaction, one could use  
 3906 the position of the reconstructed primary vertex instead. I also tried to use the principal  
 3907 direction of the clusters, but that approach gave considerably worse results. For each  
 3908 event I only keep the pair with an invariant mass closer to the true  $\pi^0$  mass value.

3909 Figure 6.42 (right panel) shows the invariant mass distributions for the photon pairs  
 3910 we get using the default (red) and the new (blue) ECal clustering algorithms. For the fit  
 3911 I used a modified version of the Crystal Ball function [166], obtained by taking the limit  
 3912 where the parameter controlling the power-law tail goes to infinity:

$$f(x; N, \mu, \sigma, \alpha) = N \cdot \begin{cases} e^{\frac{\alpha(2x-2\mu+\alpha\sigma)}{2\sigma}}; & x \leq \mu - \alpha\sigma, \\ e^{-\frac{(x-\mu)^2}{2\sigma^2}}; & x > \mu - \alpha\sigma. \end{cases} \quad (6.34)$$

3913 Comparing the fitted mean and standard deviation values for the Gaussian cores, we  
 3914 see that the distribution for the new algorithm is a 67% narrower and also peaks much  
 3915 closer to the true  $m_{\pi^0}$  value, going from  $101.3 \pm 0.4$  MeV to  $130.8 \pm 0.6$  MeV.

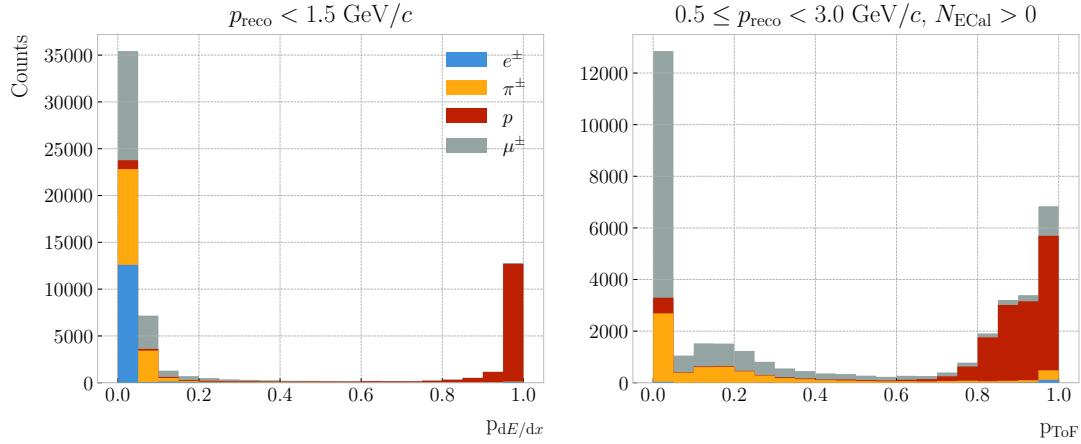
## 3916 6.7 Integration in GArSoft

3917 All the additions and improvements to the reconstruction discussed in this Chapter  
 3918 had to be integrated in the GArSoft framework. This is necessary both to allow a  
 3919 more streamlined path for development, as this makes testing and adding features  
 3920 straightforward, as well as make the changes usable in future productions of simulated  
 3921 data. In this section, I outline the current status of the integration in GArSoft of the  
 3922 reconstruction work presented above.

3923 The new track-cluster association code has been implemented in GArSoft, under  
 3924 the name of `TPCECALAssociation2`, and has now become the new default in the  
 3925 reconstruction. The structure of the module is similar to the previous implementation,  
 3926 and the data products they output are identical in form. Therefore, any existing code  
 3927 using the association objects does not need to be modified.

3928 The computation of the truncated mean  $dE/dx$  of the tracks, the evaluation of

## CHAPTER 6. PARTICLE ID IN ND-GAr



**Figure 6.43:** Distributions of proton  $dE/dx$  (left panel) and ToF (right panel) scores for a sample of 100000 FHC neutrino interactions in the HPgTPC. The distributions are broken down by the true particle type associated to the reconstructed particle.

3929 the muon score for muon and pion separation, and the estimation of the velocity from  
 3930 time-of-flight are all orchestrated by the `CreateRecoParticles` module. Each one of  
 3931 these is implemented as a separate algorithm, which is then called by the parent module.  
 3932 This generates the `gar::rec::RecoParticle` products, a new high-level data object in  
 3933 GArSoft. These combine the information from the HPgTPC, ECal, and  $\mu$ ID to create  
 3934 an object useful for analysers. At the moment, these data products are only generated  
 3935 for charged particles. However, in the future the module can be extended to incorporate  
 3936 other algorithms used for the identification of neutral particles, like neutral pions and  
 3937 neutrons.

3938 Additionally, analogous to the muon score, the `gar::rec::RecoParticle` objects  
 3939 contain two other scores based on the  $\langle dE/dx \rangle$  and ToF estimates which measure the  
 3940 “protoness” of a reconstructed particle. These are obtained in a number of momentum  
 3941 bins, and are a measure of the distance to the point in the corresponding distribution  
 3942 that maximises the  $F_1$ -score for the proton separation. This distance is then transformed  
 3943 applying a sigmoid function, which produces a score in the 0 – 1 range, with coefficients  
 3944 obtained following a procedure similar to the one used to calibrate the response of  
 3945 the muon score. The  $dE/dx$  proton score is defined for all particles with momenta  
 3946  $p_{\text{reco}} < 1.5 \text{ GeV}/c$ , whereas the ToF proton score is available for the particles with at least

## 6.7. INTEGRATION IN GArSOFT

3947 one associated hit in the inner ECal and momentum in the range  $0.5 \leq p_{\text{reco}} < 3.0 \text{ GeV}/c$ .  
3948 As an example, Fig. 6.43 shows the distributions of the  $dE/dx$  (left panel) and ToF  
3949 (right panel) proton scores for the reconstructed particles in a 100000 FHC neutrinos  
3950 sample.

3951 The calculation of the track breakpoint variables for pion decay identification is  
3952 currently implemented as an analysis module in GArSoft. It would be interesting to add  
3953 this information to the `gar::rec::RecoParticle` products, possibly calling the code as  
3954 an additional algorithm in the `CreateRecoParticles` module. However, the best way  
3955 to propagate the information to the high-level objects is still unclear.

3956 About the new ECal clustering algorithm, it is still in a development phase, and  
3957 as such it has not replaced the current clustering module. At the moment, its latest  
3958 version is integrated in GArSoft as the `CaloClustering2` module. The algorithm used  
3959 is implemented separately, and then invoked in the main code. The module can be  
3960 run standalone on the outputs of the reconstruction, creating a second instance of the  
3961 `gar::rec::Cluster` collection. In the future it may replace the current algorithm as  
3962 the default in the reconstruction chain. However, more work is needed in order to  
3963 understand its performance in all the different use cases.



3964

3965

# Event selection in ND-GAr

## 7.1 Data sample

3967 In this section I need to make sure to mention:

- 3968 • I need to comment on the versions of the software that were used for the production  
3969 of the different samples (if we end up having more than one). The version of GENIE  
3970 used was
- 3971 • We use GArG4 instead of `edep-sim` for the particle propagation. Because both  
3972 `Geant4` wrappers use different configurations for the simulation, the results obtained  
3973 are different. The default `edep-sim` configuration used by the DUNE ND is  
3974 appropriate for ND-LAr, where thresholds for particle production are higher. In  
3975 the case of ND-GAr, these parameters need to be adjusted accordingly. For the  
3976 time being, in these first productions of analysis files, we will use our standalone  
3977 `Geant4` implementation. For future iterations these differences will need to be  
3978 revisited and understood, so we can use the same simulation workflow as the rest  
3979 of the ND.
- 3980 • I need to comment on the sample size. The first sample produced was simply  $10^5$   
3981 events inside the HPgTPC volume. There is also the question of the other sample  
3982 we may want to produce for the  $\geq 3\pi^\pm$  selection (ask Naseem).
- 3983 • So far we have only simulated single interaction events. Ideally, we should move  
3984 to simulate full spills. Of course, we need to understand how many interactions

## CHAPTER 7. EVENT SELECTION IN ND-GAR

**Table 7.1:** Event rates in ND-GAr.

Process	Events/ton/year	
	$1.1 \times 10^{21}$ POT/year	$1.9 \times 10^{21}$ POT/year
All $\nu_\mu$ -CC	$1.60 \times 10^6$	$2.83 \times 10^6$
CC $0\pi$	$5.28 \times 10^5$	$9.35 \times 10^5$
CC $1\pi^\pm$	$3.02 \times 10^5$	$5.34 \times 10^5$
CC $1\pi^0$	$1.65 \times 10^5$	$2.92 \times 10^5$
CC $2\pi$	$3.18 \times 10^5$	$5.63 \times 10^5$
CC $3\pi$	$1.36 \times 10^5$	$2.41 \times 10^5$
CC other	$1.52 \times 10^5$	$2.69 \times 10^5$
All $\bar{\nu}_\mu$ -CC	$7.54 \times 10^4$	$1.33 \times 10^5$
All NC	$5.50 \times 10^5$	$9.73 \times 10^5$
All $\nu_e$ -CC	$2.70 \times 10^4$	$4.78 \times 10^4$

3985 we expect in ND-GAr per spill. Also, there is the question of having neutrino  
3986 interactions happening in the other detector volumes (ECal, magnet, . . . ).

- 3987 • At some point, we should generate a sample of rock muons making it to ND-GAr.  
3988 • I think I should comment on the run plan (at least the part that concerns ND-GAr),  
3989 and what it means in terms of generating a full production sample. It will be  
3990 good to have an understanding of the POT we need on-axis and at each off-axis  
3991 positions (for both FHR and RHC).

## 3992 7.2 $\nu_\mu$ CC selection

3993 In a  $\nu_\mu$  CC inclusive selection, the signal topology we look for is a neutrino-induced  
3994 muon with or without other final state particles. Here, I also require the neutrino vertex  
3995 to be located inside the fiducial volume (FV) of ND-GAr.

3996 The FV is defined as a smaller cylinder within the cylindrical volume of the HPgTPC.  
3997 The FV has a radius  $R_{\text{FV}}$  and a half-length  $L_{\text{FV}}$ . For a particle position to lie within

## 7.2. $\nu_\mu$ CC SELECTION

3998 the FV it must satisfy:

$$\vec{x}_i \in \left\{ \vec{x} \in \mathbb{R}^3 \mid |x_0| \leq L_{\text{FV}} \text{ \& } \sqrt{x_1^2 + x_2^2} \leq R_{\text{FV}} \right\}, \quad (7.1)$$

3999 in the reference frame of the HPgTPC. For convenience, I define:

$$\begin{aligned} \Delta R_{\text{FV}} &= R_{\text{HPgTPC}} - R_{\text{FV}}, \\ \Delta L_{\text{FV}} &= L_{\text{HPgTPC}} - L_{\text{FV}}, \end{aligned} \quad (7.2)$$

4000 where  $R_{\text{HPgTPC}}$  and  $L_{\text{HPgTPC}}$  refer to the radius and the half-length of the HPgTPC,  
4001 respectively. Figure 7.1 shows the HPgTPC volume with the FV inside of it. In that  
4002 representation, the FV is defined as  $\Delta L_{\text{FV}} = 30.0$  cm and  $\Delta R_{\text{FV}} = 30.0$  cm. Also shown  
4003 is the HPgTPC reference frame, with  $x$  being the drift direction and  $z$  aligned along the  
4004 beam direction.

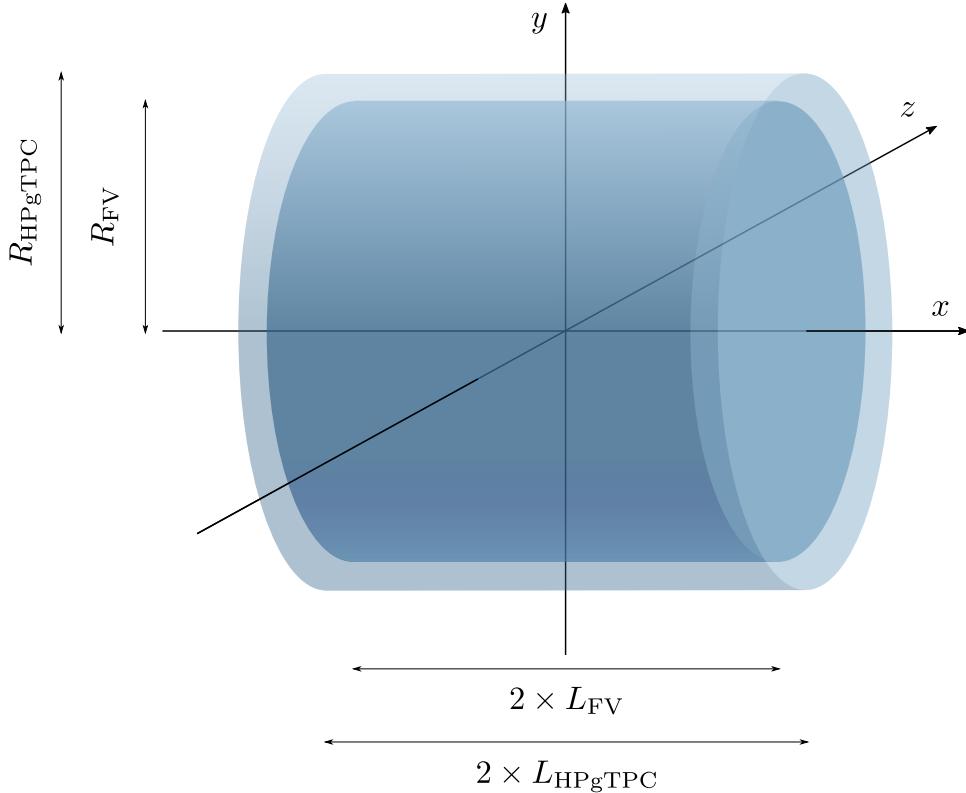
4005 In some cases, it is interesting to divide the signal events in different categories  
4006 based on their true interaction mode. In this work, I will distinguish between charged-  
4007 current quasi-elastic (CCQE), coherent (CCCOH), resonant (CCRES), and deep-inelastic  
4008 (CCDIS) interactions. I also use a separate category for the interactions not included in  
4009 any of the other categories (CCOther).

4010 Any other events are considered backgrounds. For this selection, I use the following  
4011 categorisation of background events:

- 4012 • Out of FV: if the true neutrino vertex lies outside the defined FV.
- 4013 • NC: if the event is a true neutral-current event.
- 4014 •  $\bar{\nu}_\mu$  CC: if the true neutrino candidate is of muon antineutrino flavour.
- 4015 • Other: if the event is not signal nor falls in any of the other background categories.

4016 The key to the CC selection is the identification of a primary muon candidate.  
4017 Typically, this is the longest track in the event. However, sometimes protons and pions  
4018 leave tracks longer than that of the muon. This is particularly important in the GAr

## CHAPTER 7. EVENT SELECTION IN ND-GAR



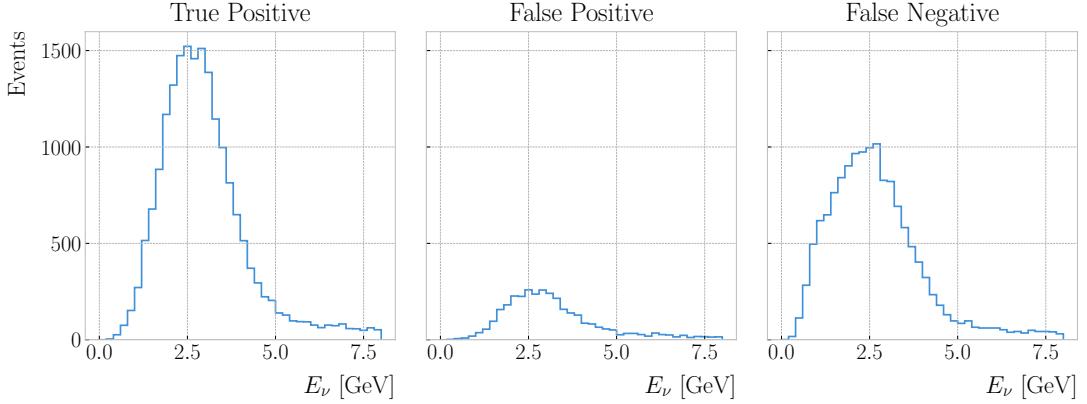
**Figure 7.1:** Schematic diagram of the HPgTPC including the fiducial volume (FV). In this case the FV is given by  $\Delta L_{\text{FV}} = 30.0$  cm and  $\Delta R_{\text{FV}} = 30.0$  cm.

4019 medium, considerably less dense than the LAr. For this reason, the muon identification  
 4020 in ND-GAr relies heavily on the capabilities of the ECal.

4021 The selection strategy proposed combines the information coming from the three  
 4022 main detection systems of ND-GAr: the HPgTPC charge readout, and the ECal and  
 4023  $\mu$ ID detectors. It consists of five steps:

- 4024 1. Event contains reconstructed particles.
- 4025 2. Select particles with reconstructed negative charge,  $q_{\text{reco}} = -1$ .
- 4026 3. Select particles passing the muon score cut,  $\mu_{\text{score}} \geq \mu_{\text{score}}^{\text{cut}}$ .
- 4027 4. Keep reconstructed particle with the highest momentum,  $\max [p_{\text{reco}}]$ .
- 4028 5. Check that the remaining particle starts within the FV.

## 7.2. $\nu_\mu$ CC SELECTION



**Figure 7.2:** True positive (left panel), false positive (middle panel), and false negative (right panel) true neutrino energy distributions for the  $\nu_\mu$  CC selection given by a muon score cut of  $\mu_{\text{score}}^{\text{cut}} = 0.75$ , and a FV defined as  $\Delta L_{\text{FV}} = 30.0$  cm and  $\Delta R_{\text{FV}} = 30.0$  cm.

4029 All the events passing these cuts are classified as signal, and the selected particle is  
 4030 regarded as the primary muon candidate.

4031 **7.2.1 Selection optimisation**

4032 I performed an optimisation of this selection, comparing the performance of a number of  
 4033 configurations. For the muon selection, I varied the value of  $\mu_{\text{score}}^{\text{cut}}$  from 0.05 to 0.95,  
 4034 using a step size of 0.05. Additionally, to optimise the FV, I systematically explored a  
 4035 number of different parameter configurations, moving within the 10.0 – 70.0 cm range for  
 4036  $\Delta L_{\text{FV}}$  and 25.0 – 75.0 cm for  $\Delta R_{\text{FV}}$ , in increments of 10.0 cm and 5.0 cm respectively.

4037 For each parameter configuration, I extract three different true neutrino energy  
 4038 distributions. These are built combining the results of the selection described previously,  
 4039 which we can refer to as the ‘reco’ selection, and a ‘true’ selection. The later identifies  
 4040 the true  $\nu_\mu$  CC events using the GENIE event records, and checks that the true neutrino  
 4041 vertices are contained in the FV.

4042 The first distribution consists of the events passing both selections, i.e., these are  
 4043 the true  $\nu_\mu$  CC events which pass the ‘reco’ selection. The second distribution contains  
 4044 the events passing the ‘reco’ selection but failing the ‘true’ selection. These are  
 4045 the background events that the selection misidentifies. Finally, the third distribution

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4046 corresponds to the events picked by the “true” selection but not by the “reco” one. In  
 4047 other words, these are the true  $\nu_\mu$  CC events that our selection misses. In analogy to  
 4048 the machine learning jargon, I refer to these distributions as the true positive (TP),  
 4049 false positive (FP), and false negative (FN) spectra, respectively. Figure 7.2 shows an  
 4050 example of these three distributions for the case  $\mu_{\text{score}}^{\text{cut}} = 0.75$ ,  $\Delta L_{\text{FV}} = 30.0$  cm, and  
 4051  $\Delta R_{\text{FV}} = 30.0$  cm.

4052 By making different combinations of these distributions one can compute a series of  
 4053 performance metrics. Using the full information from the spectra allows to obtain the  
 4054 scores as a function of the true neutrino energy, whereas the totals can be obtained by  
 4055 integrating the histograms. This way, the efficiency of the selection is given by:

$$\begin{aligned} \text{Efficiency} &= \frac{\text{Selected true } \nu_\mu \text{ CC events}}{\text{Total true } \nu_\mu \text{ CC events}} \\ &= \frac{\text{TP}}{\text{TP} + \text{FN}}, \end{aligned} \tag{7.3}$$

4056 while the purity can be written as:

$$\begin{aligned} \text{Purity} &= \frac{\text{Selected true } \nu_\mu \text{ CC events}}{\text{Total selected events}} \\ &= \frac{\text{TP}}{\text{TP} + \text{FP}}. \end{aligned} \tag{7.4}$$

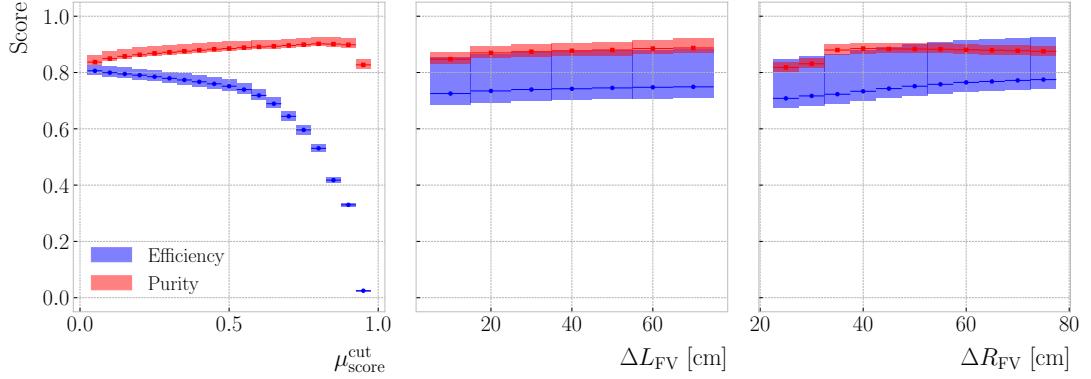
4057 Another scoring metric typically used when quantifying the performance of a selection  
 4058 is the significance. It is defined as:

$$\text{Significance} = \frac{S}{\sqrt{S + B}} = \frac{\text{TP}}{\sqrt{\text{TP} + \text{FP}}}. \tag{7.5}$$

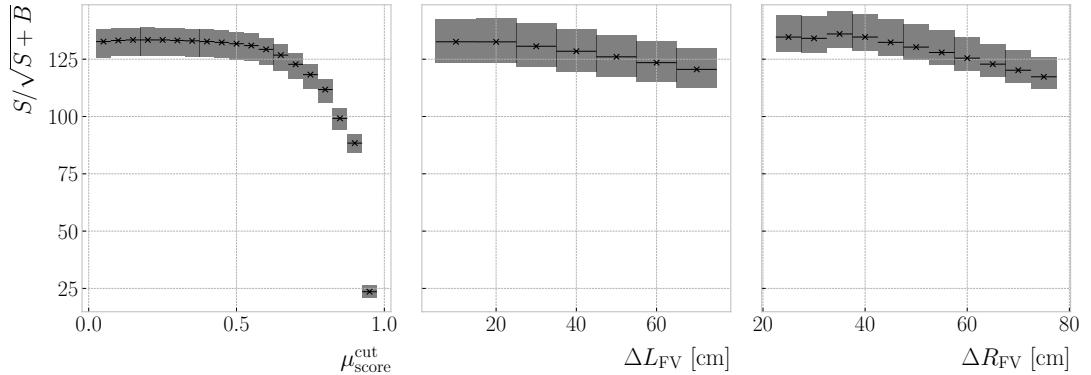
4059 The significance measures the relative size of the true signal within the selection,  $S = \text{TP}$   
 4060 with respect to one standard deviation of the counting experiment. Assuming Poisson  
 4061 statistics, the variance is equal to the number of observations, and therefore the standard  
 4062 deviation equals to  $\sqrt{N} = \sqrt{S + B} = \sqrt{\text{TP} + \text{FP}}$ . I use this metric to

4063 Figure 7.3 shows the change in efficiency (blue) and purity (red) of the  $\nu_\mu$  CC  
 4064 selection as a function of the different cuts. From left to right, I vary  $\mu_{\text{score}}^{\text{cut}}$ ,  $\Delta L_{\text{FV}}$ ,

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**Figure 7.3:** Efficiency (blue) and purity (red) for the  $\nu_\mu$  CC selection as a function of the muon score cut (left panel), FV half-length cut (middle panel), and radial cut (right panel). The height of the boxes represents the IQR of the conditional distributions, whereas the horizontal line corresponds to the mean.

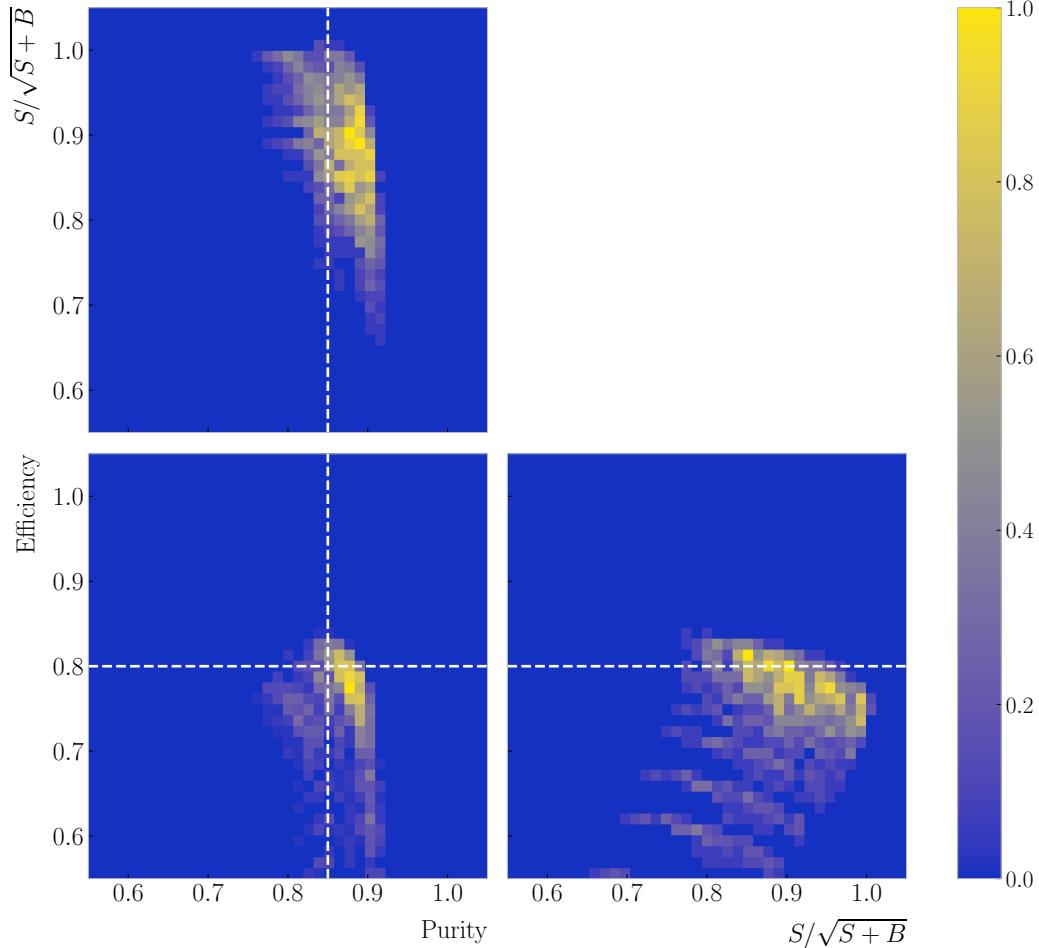


**Figure 7.4:** Significance for the  $\nu_\mu$  CC selection as a function of the muon score cut (left panel), FV half-length cut (middle panel), and radial cut (right panel). The height of the boxes represents the IQR of the conditional distributions, whereas the horizontal line corresponds to the mean.

and  $\Delta R_{\text{FV}}$ . For each value of the cuts, I compute the median and IQR (represented by the horizontal lines and the heights of the boxes, respectively) of the corresponding conditional distributions of efficiency and purity. This representation is useful to get an idea of the general trend the scores follow with the cuts, as well as the spread. It is clear that the muon score cut has the biggest impact on the efficiency, which ranges between 0.05 to 0.80, whereas the purity remains stable with values around 0.85.

A similar depiction of the significance can be found in Fig. 7.4. In this case, one can see that the  $S/\sqrt{S+B}$  decreases as the cuts grow tighter. However, there are hints of

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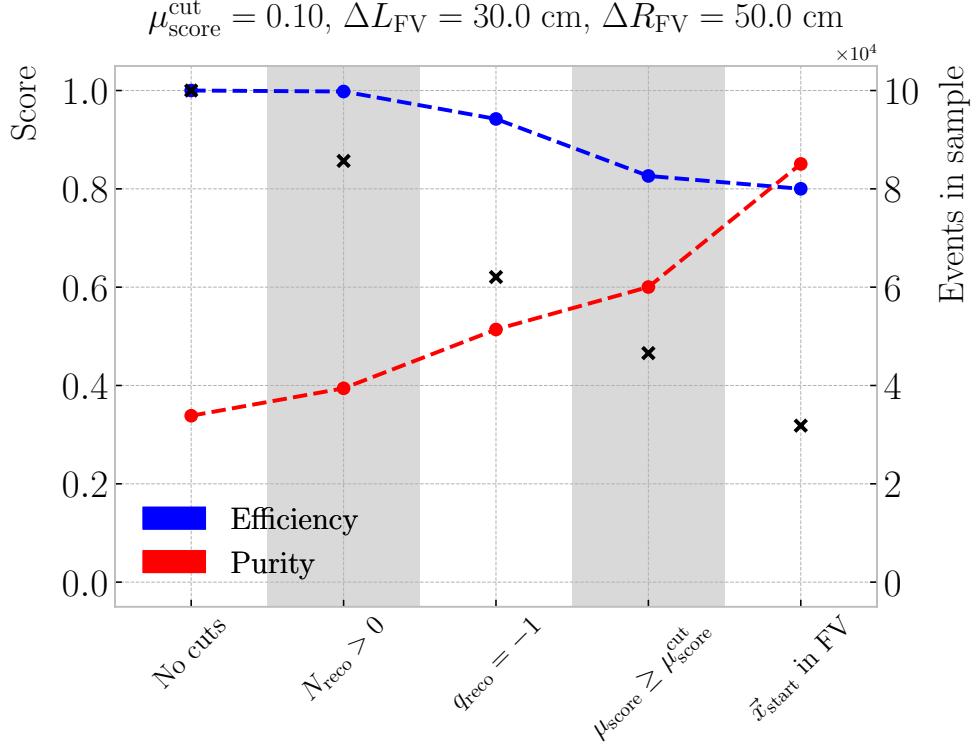


**Figure 7.5:** Normalised 2D distributions of efficiency, purity and significance for the  $\nu_\mu$  CC selection. The  $S/\sqrt{S+B}$  is normalised to the highest value achieved. The vertical dashed line indicates a purity value of 0.85, whereas the horizontal one corresponds to an efficiency of 0.80.

4073 local maxima at intermediate values.

4074 Selecting the cut configuration with the highest significance,  $147 \pm 11$  for the parameter  
 4075 values explored here, results in an efficiency and purity of  $0.754 \pm 0.006$  and  $0.833 \pm 0.007$ ,  
 4076 respectively. Figure 7.5 shows the 2D distributions resulting when combining pairs of  
 4077 efficiency, purity and significance, obtained for the cut configurations explored. The  
 4078 significance is normalised to the highest value obtained in the parameter scan. Looking  
 4079 at this, it is clear that a selection with highest efficiency and purity can be achieved,  
 4080 maintaining a similar significance level.

## 7.2. $\nu_\mu$ CC SELECTION



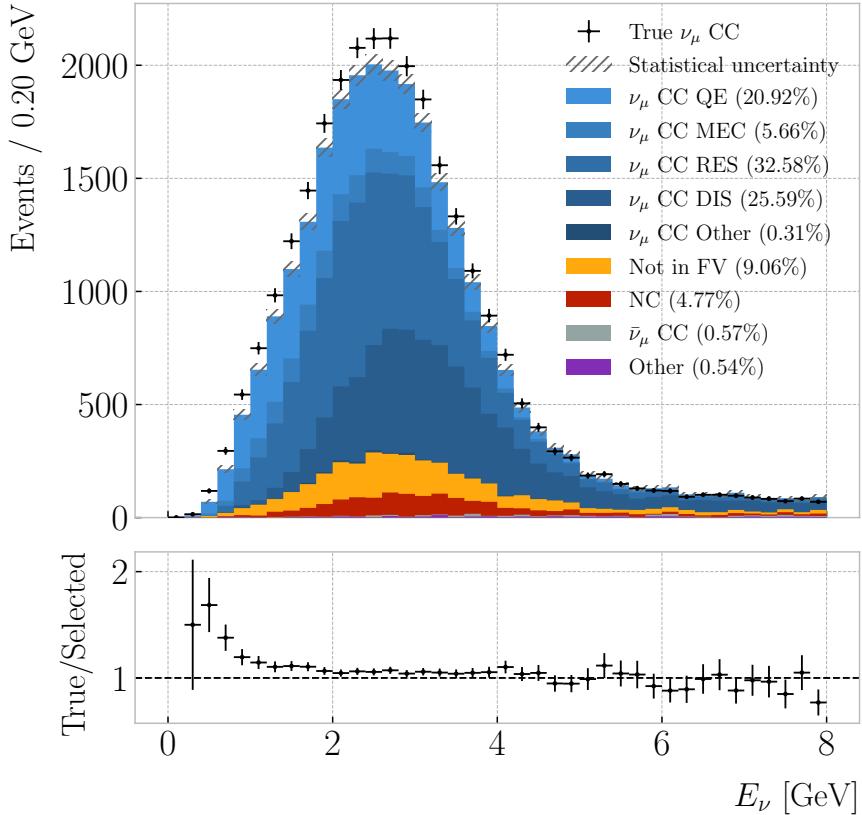
**Figure 7.6:** Cumulative efficiency (blue) and purity (red) of the  $\nu_\mu$  CC selection. The secondary axis indicates the number of events in the sample after each cut (black crosses).

**Table 7.2:** Step-by-step  $\nu_\mu$  CC selection cuts and cumulative passing rates. Relative passing rates are indicated in parentheses.

Cut #	Selection cut	Events	Passing rates
0	Total number of events (No cuts)	100000	100.00% (100.00%)
1	At least one reconstructed particle	85680	85.68% (85.68%)
2	Negatively charged particles only	62054	62.05% (72.43%)
3	$\mu_{\text{score}} \geq \mu_{\text{score}}^{\text{cut}}$	46585	46.59% (75.07%)
4	Candidate $\vec{x}_{\text{start}}$ in FV	31834	31.83% (68.34%)

4081 Therefore, to get a more refined selection, I first select the configurations with a  
 4082 purity and an efficiency higher than 0.85 and 0.80, respectively. After that, I select the  
 4083 tuple of cuts yielding the highest significance. The resulting value for the muon score  
 4084 cut is  $\mu_{\text{score}}^{\text{cut}} = 0.10$ , and the FV is given by  $\Delta L_{\text{FV}} = 30.0 \text{ cm}$  and  $\Delta R_{\text{FV}} = 50.0 \text{ cm}$ .  
 4085 With these, one obtains a total efficiency of  $0.800 \pm 0.007$  and purity of  $0.851 \pm 0.008$ ,

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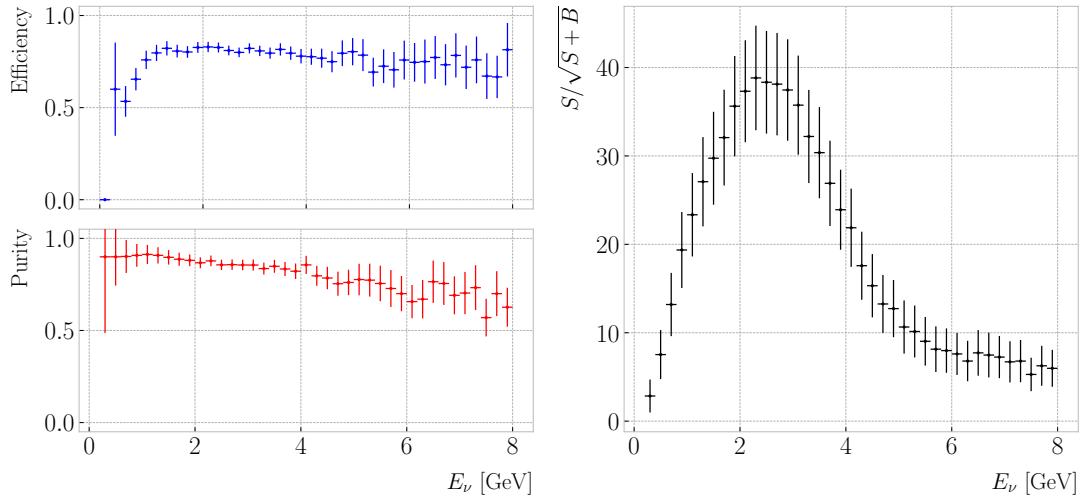


**Figure 7.7:** True neutrino energy spectra for the  $\nu_\mu$  CC selection. The selected events correspond to the coloured stacked histogram, broken down by signal and background subcategories. The statistical uncertainty is drawn in hatched gray. The true distribution is also shown with the black data points. The bottom panel shows the ratio between the number of true and selected  $\nu_\mu$  CC events per bin.

4086 with a significance of  $138 \pm 11$ . Hereafter, I use this optimised selection cuts, unless  
 4087 specified otherwise.

4088 A summary of the selection can be found in Tab. 7.2. It shows the number of  
 4089 events in the selected sample after each selection cut, as well as the absolute and relative  
 4090 passing rates. Figure 7.6 shows the overall efficiencies (blue) and purities (red) after  
 4091 each cut in the event selection is applied. As expected, the efficiency drops while the  
 4092 purity increases with the successive cuts.

4093 Notice how, out of the cuts prior to the FV constraint, the sign selection produces  
 4094 the highest increase in purity. This is one of the advantages of having a magnetised  
 4095 TPC, and can also be used for a  $\bar{\nu}_\mu$  CC selection when running in RHC mode.



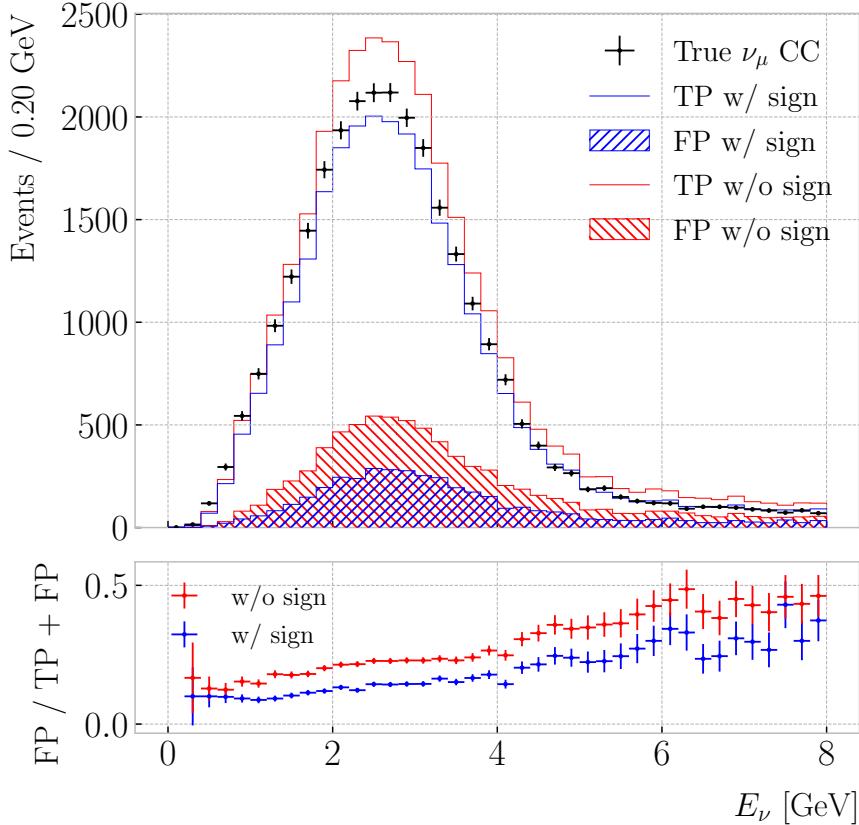
**Figure 7.8:** Left panel: efficiency (top panel) and purity (bottom panel) for the  $\nu_\mu$  CC selection as a function of the true neutrino energy. Right panel: significance for the  $\nu_\mu$  CC selection as a function of the true neutrino energy

#### 4096 7.2.2 Selection performance

4097 Using the stored spectra discussed above, the true neutrino energy distribution for the  
 4098 selected events can be recovered doing TP + FP. Similarly, the combination TP + FN  
 4099 gives the true spectrum. Figure 7.7 shows the true (black data points) and selected  
 4100 (coloured stacked histogram)  $E_\nu$  distributions for the optimised  $\nu_\mu$  CC selection. The  
 4101 colours in the selected spectrum indicate the different signal categories and backgrounds,  
 4102 with the overall statistical uncertainty represented by the gray hatched mess. The ratio  
 4103 between the true and selected events is also shown. One can see that it sits around 1 for  
 4104 most of the energy range. However, for energies  $\leq 1$  GeV there is a significant deficit of  
 4105 selected events.

4106 These spectra also allow to compute the efficiency and purity of the selection as  
 4107 a function of the true neutrino energy, as shown in Fig. 7.8 (left panel). As it could  
 4108 be expected from the previous ratio plot, the efficiency is low at low neutrino energies.  
 4109 Nonetheless, it raises quickly with the energy, until it stabilises around a value of 0.80.  
 4110 Looking at the purity, one may notice that, although it starts at around 0.90, there is a  
 4111 significant decrease towards the high end of the spectrum. Figure 7.8 (right panel) also

## CHAPTER 7. EVENT SELECTION IN ND-GAR

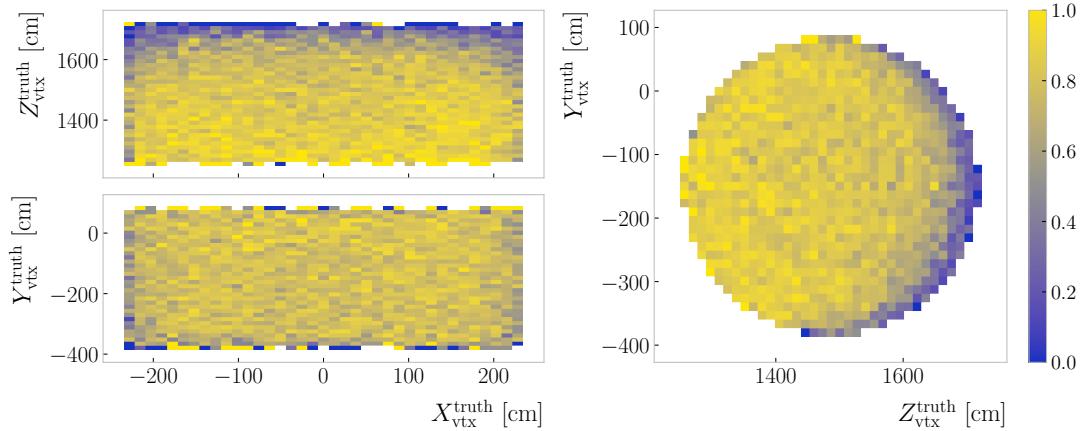


**Figure 7.9:** True neutrino energy spectra for the  $\nu_\mu$  CC selection with (blue) and without (red) sign selection. The selected events are broken down by true positives (signal) and false positives (background). The true distribution is also shown (black data points). The bottom panel shows the ratios between the number of false positives and total selected events per bin.

4112 shows the significance as a function of the energy. In this case, the highest  $S/\sqrt{S+B}$  is  
 4113 achieved around the energies where the spectrum peaks.

4114 A variation of the  $\nu_\mu$  CC selection one can try is to apply it without the reconstructed  
 4115 charge cut. Figure 7.9 (top panel) shows the  $E_\nu$  distributions corresponding to the  
 4116 selection with (blue stacked histogram) and without (red stacked histogram) the sign  
 4117 selection. In the former case, the out of FV contamination amounts to 9.06% of the  
 4118 total, while the NC contamination results 4.77% and the wrong-sign contamination  
 4119 0.57%. For the later, these backgrounds account for the 10.01%, 10.82%, and 2.18%  
 4120 of the selected events, respectively. As expected, removing the positive particles does  
 4121 not change the FV-related effects noticeably. However, the sign selection proves its

## 7.2. $\nu_\mu$ CC SELECTION



**Figure 7.10:** Efficiency 2D distributions for the  $\nu_\mu$  CC selection given the true position of the interaction vertex.

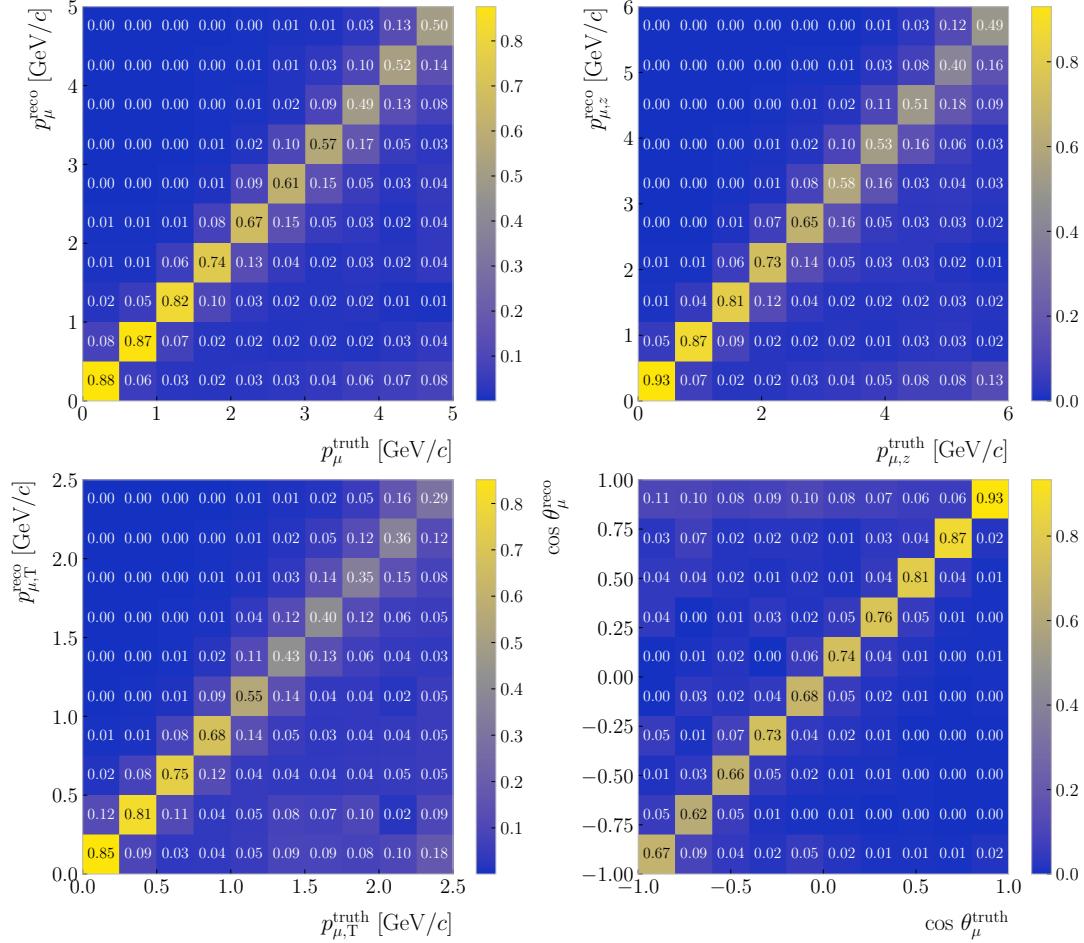
worth in the rejection of  $\bar{\nu}_\mu$  CC events, which drop almost by one order of magnitude.  
 Additionally, the charge selection cuts the NC events in half, as it reduces the chances of misidentifying a positively charged hadron for a muon.

As an additional check, I explored how the performance of the  $\nu_\mu$  CC selection depends on the position of the neutrino interaction within the HPgTPC. Maps of the selection efficiency for the  $X, Z$  (top left panel),  $X, Y$  (bottom left panel), and  $Z, Y$  (right panel) true vertex position pairs are given in Fig. 7.10. It can be seen that the efficiency remains stable along the drift direction, only slightly degrading close to the edges of the FV. Regarding the radial direction, it is clear that an important number of events with high  $Z_{\text{vtx}}^{\text{truth}}$  are not being selected. Intuitively, the muons arising from these interactions will leave short tracks. As their directions are typically aligned with the beam direction, they enter the ECal shortly after production. This is likely to affect the tracking, and therefore their identification. As a result, the regions with the lowest efficiency are the downstream corners of the HPgTPC, i.e. the areas with high  $|X_{\text{vtx}}^{\text{truth}}|$  and  $Z_{\text{vtx}}^{\text{truth}}$ .

### 7.2.3 Primary muon kinematics

This  $\nu_\mu$  CC selection relies on the identification of the a primary muon, meaning that for each selected event a particle is picked out as the muon candidate. It is because of

## CHAPTER 7. EVENT SELECTION IN ND-GAR

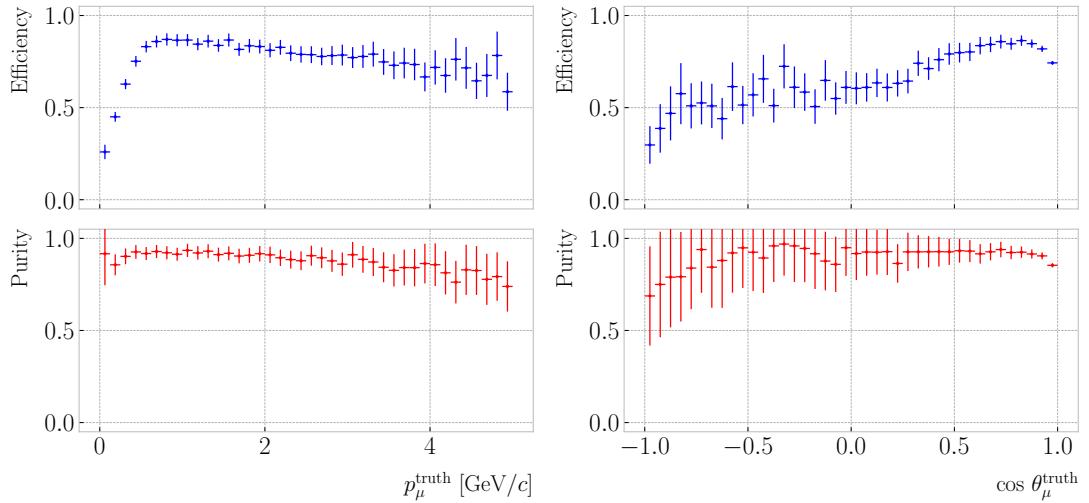


**Figure 7.11:** Distributions for the reconstructed versus truth generated primary muon momentum (top left panel), longitudinal momentum (top right panel), transverse momentum (bottom left panel), and beam angle (bottom right panel). The reconstructed values correspond to the selected primary muon candidate, whereas the truth values come from the true primary muon in the event.

4140 this that one can study the kinematics of these selected primary muons.

4141 Figure 7.11 shows a comparison between some of the reconstructed and truth primary  
 4142 muon kinematic variables. From top to bottom, left to right, we have muon momentum,  
 4143 longitudinal momentum, transverse momentum and beam angle. The histograms are  
 4144 column-normalised, and so the diagonal entries give an idea of the resolution for the  
 4145 different variables. The match between truth and reconstructed values can only be done  
 4146 for the selected true  $\nu_{\mu}$  CC events, as the others do not have a primary muon. However,  
 4147 for this comparison I do not require the events to start inside the FV.

## 7.2. $\nu_\mu$ CC SELECTION

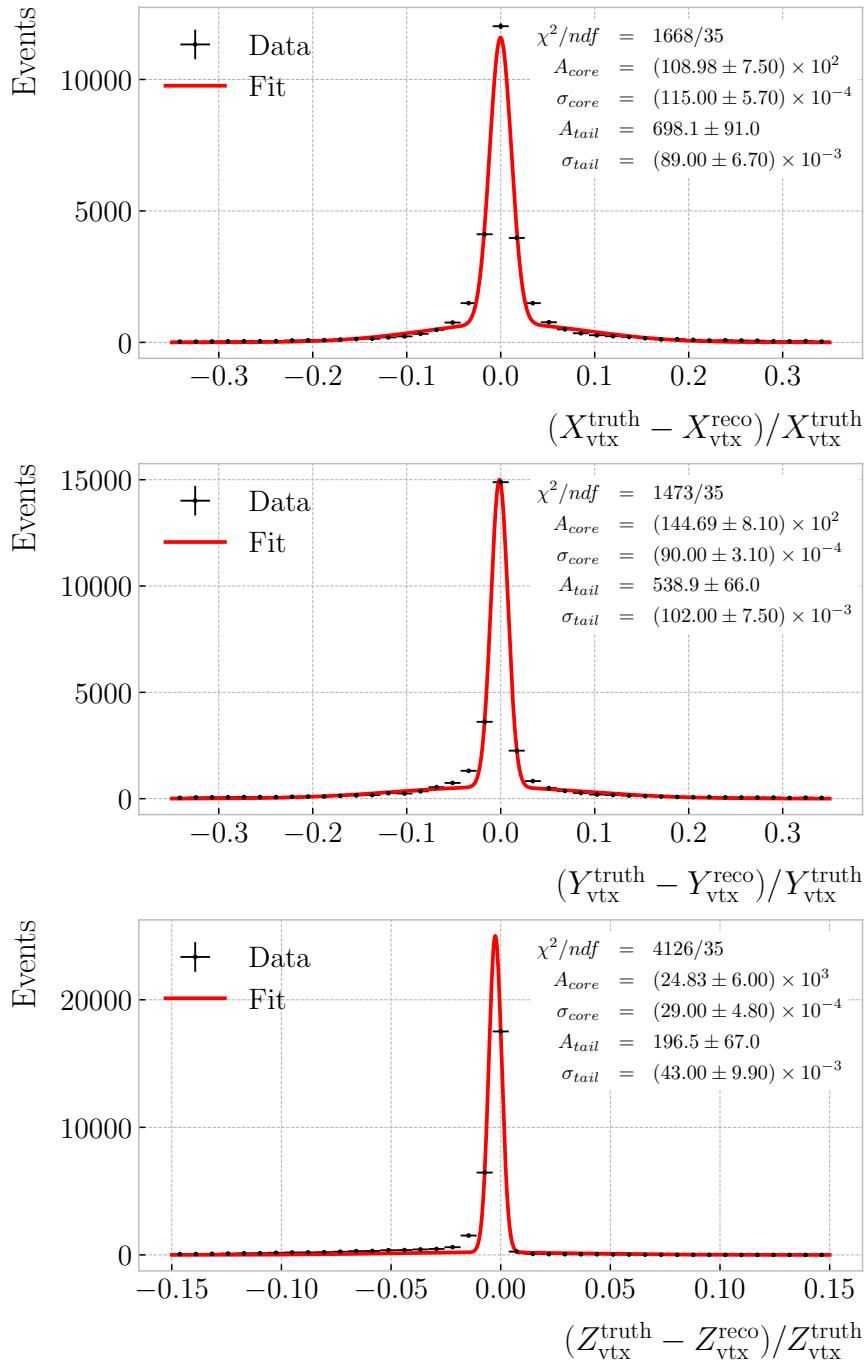


**Figure 7.12:** Efficiency (blue) and purity (red) of the  $\nu_\mu$  CC selection as a function of the primary muon true momentum (left panel) and beam angle (right panel).

4148 Notice that, for the reconstructed values, the variables do not necessarily come  
 4149 from a reconstructed particle that matches the true primary muon. In other words,  
 4150 sometimes, even though the event was correctly identified, the primary muon may have  
 4151 been confused with another particle. That means that in these distributions include  
 4152 both reconstruction and selection deficiencies.

4153 I also studied the performance of the  $\nu_\mu$  CC selection as a function of the kinematic  
 4154 variables of the primary muon. As before, these metrics are only possible to compute for  
 4155 true  $\nu_\mu$  CC events. The efficiency (top panels) and purity (bottom panels) as a function  
 4156 of the truth muon momentum (left) and beam angle (right) are shown in Fig. 7.12. One  
 4157 can see that there are some similarities in the behaviour of both metrics between the  
 4158 true neutrino energy and the muon momentum cases. This is to be expected, as these  
 4159 two variables are highly correlated. For the efficiency, there is a rapid increase at low  
 4160 momentum values until it peaks at around 1 GeV/c, after which it starts decreasing  
 4161 slowly. The purity remains relatively constant, with a slight drop towards high  $p_\mu^{\text{truth}}$   
 4162 values. In the case of the muon angle, the decrease in efficiency at high  $\theta_\mu^{\text{truth}}$  is more  
 4163 noticeable. However, note that the number of events with backward-going muons is  
 4164 much smaller than those aimed towards the forward direction, as can be seen from the

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**Figure 7.13:** Fractional residual distributions for the position of the primary vertex in the  $\nu_\mu$  CC selection. The best fits to a double Gaussian function are also shown (red lines).

### 7.3. CHARGED PION IDENTIFICATION

4165 size of the vertical error bars. There is also a decline in the purity with the beam angle,  
4166 but this effect is much smaller.

4167 A byproduct of selecting the primary lepton in the interaction is the position  
4168 of the reconstructed neutrino vertex candidate. Checking how the position of the  
4169 selected reconstructed primary vertex and the true vertex position compare is needed to  
4170 understand the validity of our method. Figure 7.13 shows the distributions of fractional  
4171 residuals between the truth and reconstructed vertex positions in the  $X$  (top panel),  
4172  $Y$  (middle panel), and  $Z$  (bottom panel) directions. Performing a double Gaussian fit  
4173 to the distributions (red lines), I estimate the reconstructed vertex resolution achieved  
4174 with this method to be  $1.62 \pm 0.08\%$ ,  $1.23 \pm 0.05\%$ , and  $0.32 \pm 0.05\%$  for the  $X$ ,  $Y$ ,  
4175 and  $Z$  directions, respectively. As expected, the resolution along the drift direction.  
4176 However, the significant difference in resolution between the two transverse directions is  
4177 worth noting. Not only the resolution is better for the  $Z$  direction, but the layout of the  
4178 residual distribution is highly asymmetrical. This may be related to the variability in  
4179 the selection efficiency along that direction.

## 4180 7.3 Charged pion identification

4181 Now that I have checked the robustness of the proposed  $\nu_\mu$  CC selection, it can be  
4182 used as a starting point for other, more convoluted, selections. One of the priorities of  
4183 ND-GAr, as mentioned previously, is the identification of pions. In a

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4184 7.3.1  $\nu_\mu$  CC  $1\pi^\pm$  selection

4185 7.4 Neutral pion identification

4186 7.5 Systematic uncertainties

4187 7.5.1 Flux uncertainties

4188 7.5.2 Cross section uncertainties

4189 7.5.3 Detector uncertainties

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## Conclusion and outlook



4192

A [REDACTED]

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An appendix



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