

Vector network analyzer.

Define settings.

Index of the measurement k , number of frequency points N_F , bandwidth $B = f_1 - f_0$, frequency step $\Delta f = \frac{f_1 - f_0}{N_F}$, number of measurements N .

Transmission coefficient in the frequency domain $S_{21,k}$.

Add $N_{\text{Left}} = \frac{f_0}{\Delta f}$ zeroes to the left side of $S_{21,k}$.

Determine the maximum unambiguous range $d_{\text{max}} = \frac{c}{2\Delta f}$. Calculate distance vector $d_{\text{VNA}} = [0, \Delta d, 2 \cdot \Delta d, \dots, d_{\text{max}}]$. $\Delta d = \frac{d_{\text{max}}}{N_F + N_{\text{Left}}}$

Optional: multiply $S_{21,k}$ with window function.

Choose total number of samples N_{total} with $N_{\text{total}} > N_F + N_{\text{Left}}$.

Calculate new distance vector $d_{\text{VNA,New}}$.
 $d_{\text{VNA,new}} = [0, \Delta d_{\text{New}}, 2 \cdot \Delta d_{\text{New}}, \dots, d_{\text{max}}]$, $\Delta d_{\text{New}} = \frac{d_{\text{max}}}{N_{\text{total}}}$

Apply zero-padding to the right side of the spectrum in the frequency domain. The number of zeros is $N_{\text{total}} - N_{\text{Left}} - N_F$.

Subtract d_{Offset} of each value in $d_{\text{VNA,New}}$ so that the distance value 0 m equals a distance of 0 m in the image.

Calculate the IFFT of the padded frequency domain signal $S_{21,\text{padded},k}$ to get the time domain response of each measurement.
 $R_k(d_{\text{Radar,New}}) = \text{IFFT}(S_{21,\text{padded},k})$.

Create a function $I_{k,\text{Interpol,VNA}}(d_{\text{VNA,New}})$ that can be called with any distance value between $\min(d_{\text{VNA,New}})$ and $\max(d_{\text{VNA,New}})$.

Frequency modulated continuous wave radar.

Define settings.

Index of the measurement k , bandwidth $B = f_1 - f_0$, ramp duration T , number of measurements N .

IF signal in the time domain $s_{\text{IF},k}$.

Calculate IF frequency vector f_{IF} from time vector t .
 $f_{\text{IF}} = [0, \Delta f, 2 \cdot \Delta f, \dots, f_s]$, $\Delta f = \frac{1}{T}$,
 $f_s = \frac{1}{t[1] - t[0]}$, number of samples $N_{\text{Samples}} = T \cdot f_s$.
 Calculate distance vector d_{Radar} from IF frequency vector.
 $d_{\text{Radar}} = [0, \Delta d, 2 \cdot \Delta d, \dots, d_{\text{max}}]$. $\Delta d = \frac{\Delta f \cdot c \cdot T}{2 \cdot B}$, $d_{\text{max}} = \frac{f_s \cdot c \cdot T}{2 \cdot B}$.

Optional: multiply $s_{\text{IF},k}$ with window function.

Choose total number of samples N_{total} with $N_{\text{total}} > N_{\text{Samples}}$.

Calculate new distance vector $d_{\text{Radar,New}}$.
 $d_{\text{Radar,new}} = [0, \Delta d_{\text{New}}, 2 \cdot \Delta d_{\text{New}}, \dots, d_{\text{max}}]$, $\Delta d_{\text{New}} = \frac{d_{\text{max}}}{N_{\text{total}}}$

Apply zero-padding to the right side of the signal in the time domain. The number of zeros is $N_{\text{total}} - N_{\text{Samples}}$.

Subtract d_{Offset} of each value in $d_{\text{Radar,new}}$ so that the distance value 0 m equals a distance of 0 m in the image.

Calculate the FFT of the padded time domain signal $s_{\text{IF,padded},k}$ to get the range FFT $R_k(d_{\text{Radar,New}})$ of each measurement.
 $R_k(d_{\text{Radar,New}}) = \text{FFT}(s_{\text{IF,padded},k})$.

Multiply $R_k(d_{\text{Radar,New}})$ with the phase compensation term $\exp\left(-j2\pi f_0 \cdot \frac{2(d_{\text{Air}} + d_{\text{Offset}})}{c}\right)$ to calculate I_k .

Create a function $I_{k,\text{Interpol,Radar}}(d_{\text{Radar,New}})$ that can be called with any distance value between $\min(d_{\text{Radar,New}})$ and $\max(d_{\text{Radar,New}})$.