

**2.6 Problem 13:** Determine a particular solution  $\psi(t)$  of  $my'' + cy' + ky = F_0 \cos \omega t$  of the form  $\psi(t) = A \cos(\omega t - \phi)$ . Show that the amplitude  $A$  is a maximum when  $\omega^2 = \omega_0^2 - \frac{1}{2}(c/m)^2$ . This value of  $\omega$  is called the *resonant frequency* of the system. What happens when  $\omega_0^2 < \frac{1}{2}(c/m)^2$ ?

**2.10 Problem 20:** Solve the following initial-value problem by the method of Laplace Transforms.

$$y'' + y = t \sin t, \quad y(0) = 1, \quad y'(0) = 2$$

**2.12 Problem 1:** Let  $a$  be a fixed constant. Show that every solution of the differential equation  $\frac{d^2y}{dt^2} + 2\alpha\frac{dy}{dt} + \alpha^2y = 0$  can be written in the form

$$y(t) = [c_1 + c_2(t - a)]e^{-\alpha(t-a)}$$

**2.13 Problem 17:** Use Theorem 9 to find a solution  $y(t)$  to the following equation.

$$y'(t) = 2y + \int_0^t y(u)e^{-(t-u)}du, \quad y(0) = 0$$