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Task	MATLAB/Octave	Python NumPy	R	Julia	Task
<b>CREATING MATRICES</b>					
<b>Creating Matrices</b> (here: 3x3 matrix)	<pre>M&gt; A = [1 2 3; 4 5 6; 7 8 9] A =      1     2     3      4     5     6      7     8     9</pre>	<pre>P&gt; A = np.array([ [1,2,3], [4,5,6],                   [7,8,9] ]) P&gt; A array([[1, 2, 3],        [4, 5, 6],        [7, 8, 9]])</pre>	<pre>R&gt; A = matrix(c(1,2,3,4,5,6,7,8,9),nrow=3,byrow=T) # equivalent to # A = matrix(1:9,nrow=3,byrow=T) R&gt; A [,1] [,2] [,3] [1,] 1 2 3 [2,] 4 5 6 [3,] 7 8 9</pre>	<pre>J&gt; A=[1 2 3; 4 5 6; 7 8 9] 3x3 Array{Int64,2}:  1 2 3  4 5 6  7 8 9</pre>	<b>Creating Matrices</b> (here: 3x3 matrix)
<b>Creating an 1D column vector</b>	<pre>M&gt; a = [1; 2; 3] a =      1      2      3</pre>	<pre>P&gt; a = np.array([1,2,3]).reshape(1,3) P&gt; b.shape (1, 3)</pre>	<pre>R&gt; a = matrix(c(1,2,3), nrow=3, byrow=T) R&gt; a [,1] [1,] 1 [2,] 2 [3,] 3</pre>	<pre>J&gt; a=[1; 2; 3] 3-element Array{Int64,1}:  1  2  3</pre>	<b>Creating an 1D column vec</b>
<b>Creating an 1D row vector</b>	<pre>M&gt; b = [1 2 3] b =      1     2     3</pre>	<pre>P&gt; b = np.array([1,2,3]) P&gt; b array([1, 2, 3]) # note that numpy doesn't have # explicit "row-vectors", but 1-D # arrays P&gt; b.shape</pre>	<pre>R&gt; b = matrix(c(1,2,3), ncol=3) R&gt; b [,1] [,2] [,3] [1,] 1 2 3</pre>	<pre>J&gt; b=[1 2 3] 1x3 Array{Int64,2}:  1 2 3 # note that this is a 2D array. # vectors in Julia are columns</pre>	<b>Creating an 1D row vector</b>

### Creating a random m x n matrix

```
M> rand(3,2)

ans =

    0.21977    0.10220

    0.38959    0.69911

    0.15624    0.65637
```

```
(3,)
P> np.random.rand(3,2)

array([[ 0.29347865,  0.17920462],
       [ 0.51615758,  0.64593471],
       [ 0.01067605,  0.09692771]])
```

```
R> matrix(runif(3*2), ncol=2)

[,1] [,2]

[1,] 0.5675127 0.7751204

[2,] 0.3439412 0.5261893

[3,] 0.2273177 0.223438
```

```
J> rand(3,2)

3x2 Array{Float64,2}:

0.36882 0.267725

0.571856 0.601524

0.848084 0.858935
```

### Creating a random m x n matrix

### Creating a zero m x n matrix

```
M> zeros(3,2)

ans =

    0    0

    0    0

    0    0
```

```
P> np.zeros((3,2))

array([[ 0.,  0.],
       [ 0.,  0.],
       [ 0.,  0.]])
```

```
R> mat.or.vec(3, 2)

[,1] [,2]

[1,] 0 0

[2,] 0 0

[3,] 0 0
```

```
J> zeros(3,2)

3x2 Array{Float64,2}:

0.0 0.0

0.0 0.0

0.0 0.0
```

### Creating a zero m x n matrix

### Creating an m x n matrix of ones

```
M> ones(3,2)

ans =

    1    1

    1    1

    1    1
```

```
P> np.ones((3,2))

array([[ 1.,  1.],
       [ 1.,  1.],
       [ 1.,  1.]])
```

```
R> matrix(1L, 3, 2)

[,1] [,2]

[1,] 1 1

[2,] 1 1

[3,] 1 1
```

```
J> ones(3,2)

3x2 Array{Float64,2}:

1.0 1.0

1.0 1.0

1.0 1.0
```

### Creating an m x n matrix of ones

### Creating an identity matrix

```
M> eye(3)

ans =

Diagonal Matrix

    1    0    0

    0    1    0

    0    0    1
```

```
P> np.eye(3)

array([[ 1.,  0.,  0.],
       [ 0.,  1.,  0.],
       [ 0.,  0.,  1.]])
```

```
R> diag(3)

[,1] [,2] [,3]

[1,] 1 0 0

[2,] 0 1 0

[3,] 0 0 1
```

```
J> eye(3)

3x3 Array{Float64,2}:

1.0 0.0 0.0

0.0 1.0 0.0

0.0 0.0 1.0
```

### Creating an identity matrix

### Creating a diagonal matrix

```
M> a = [1 2 3]

M> diag(a)

ans =

Diagonal Matrix

    1    0    0

    0    2    0

    0    0    0
```

```
P> a = np.array([1,2,3])

P> np.diag(a)

array([[1, 0, 0],
       [0, 2, 0],
       [0, 0, 3]])
```

```
R> diag(1:3)

[,1] [,2] [,3]

[1,] 1 0 0

[2,] 0 2 0

[3,] 0 0 3
```

```
J> a=[1, 2, 3]

# added commas because julia
# vectors are columnar

J> diagm(a)

3x3 Array{Int64,2}:
```

### Creating a diagonal matrix

```
0 0 3
```

```
1 0 0
```

```
0 2 0
```

```
0 0 3
```

## ACCESSING MATRIX ELEMENTS

Getting the dimension  
of a matrix  
(here: 2D, rows x cols)

```
M> A = [1 2 3; 4 5 6]
```

```
A =
```

```
1 2 3
```

```
4 5 6
```

```
M> size(A)
```

```
ans =
```

```
2 3
```

Selecting rows

```
M> A = [1 2 3; 4 5 6; 7 8 9]
```

```
% 1st row
```

```
M> A(1,:)
```

```
ans =
```

```
1 2 3
```

```
% 1st 2 rows
```

```
M> A(1:2,:)
```

```
ans =
```

```
1 2 3
```

```
4 5 6
```

Selecting columns

```
M> A = [1 2 3; 4 5 6; 7 8 9]
```

```
% 1st column
```

```
M> A(:,1)
```

```
P> A = np.array([ [1,2,3], [4,5,6] ])
```

```
P> A
```

```
array([[1, 2, 3],
       [4, 5, 6]])
```

```
P> A.shape
```

```
(2, 3)
```

```
P> A = np.array([ [1,2,3], [4,5,6],
                  [7,8,9] ])
# 1st row
```

```
P> A[0,:]
```

```
array([1, 2, 3])
```

```
# 1st 2 rows
```

```
P> A[0:2,:]
```

```
array([[1, 2, 3], [4, 5, 6]])
```

```
P> A = np.array([ [1,2,3], [4,5,6],
                  [7,8,9] ])
# 1st column (as row vector)
```

```
P> A[:,0]
```

```
R> A = matrix(1:6,nrow=2,byrow=T)
```

```
R> A
```

```
[,1] [,2] [,3]
```

```
[1,] 1 2 3
```

```
[2,] 4 5 6
```

```
R> dim(A)
```

```
[1] 2 3
```

```
R> A = matrix(1:9,nrow=3,byrow=T)
```

```
# 1st row
```

```
R> A[1,]
```

```
[1] 1 2 3
```

```
# 1st 2 rows
```

```
R> A[1:2,]
```

```
[,1] [,2] [,3]
```

```
[1,] 1 2 3
```

```
[2,] 4 5 6
```

```
R> A = matrix(1:9,nrow=3,byrow=T)
```

```
# 1st column as row vector
```

```
R> t(A[,1])
```

```
J> A=[1 2 3; 4 5 6]
```

```
2x3 Array{Int64,2}:
```

```
1 2 3
```

```
4 5 6
```

```
J> size(A)
```

```
(2,3)
```

```
J> A=[1 2 3; 4 5 6; 7 8 9];
```

```
#semicolon suppresses output
```

```
#1st row
```

```
J> A[1,:]
```

```
1x3 Array{Int64,2}:
```

```
1 2 3
```

```
#1st 2 rows
```

```
J> A[1:2,:]
```

```
2x3 Array{Int64,2}:
```

```
1 2 3
```

```
4 5 6
```

```
J> A=[1 2 3; 4 5 6; 7 8 9];
```

```
#1st column
```

```
J> A[:,1]
```

Getting the dimension  
of a matrix  
(here: 2D, rows x cols)

Selecting rows

Selecting columns

	<pre>ans =     1     4     7  % 1st 2 columns M&gt; A(:,1:2) ans =     1     2     4     5     7     8</pre>	<pre>array([1, 4, 7])  # 1st column (as column vector) P&gt; A[:,0] array([[1],        [4],        [7]])  # 1st 2 columns P&gt; A[:,0:2] array([[1, 2],        [4, 5],        [7, 8]])</pre>	<pre>[,1] [,2] [,3] [1,] 1 4 7  # 1st column as column vector R&gt; A[,1] [1] 1 4 7  # 1st 2 columns R&gt; A[:,1:2] [,1] [,2] [1,] 1 2 [2,] 4 5 [3,] 7 8</pre>	<pre>3-element Array{Int64,1}:  1  4  7  #1st 2 columns J&gt; A[:,1:2] 3x2 Array{Int64,2}:  1 2  4 5  7 8</pre>	
<b>Extracting rows and columns by criteria</b>  <b>(here: get rows that have value 9 in column 3)</b>	<pre>M&gt; A = [1 2 3; 4 5 9; 7 8 9] A =     1     2     3     4     5     9     7     8     9  M&gt; A(A(:,3) == 9,:) ans =     4     5     9     7     8     9</pre>	<pre>P&gt; A = np.array([ [1,2,3], [4,5,9], [7,8,9] ]) P&gt; A array([[1, 2, 3],        [4, 5, 9],        [7, 8, 9]])  P&gt; A[A[:,2] == 9] array([[4, 5, 9],        [7, 8, 9]])</pre>	<pre>R&gt; A = matrix(1:9,nrow=3,byrow=T) R&gt; A [,1] [,2] [,3] [1,] 1 2 3 [2,] 4 5 9 [3,] 7 8 9  R&gt; A[A[,3]==9,] [1] 7 8 9</pre>	<pre>J&gt; A=[1 2 3; 4 5 9; 7 8 9] 3x3 Array{Int64,2}:  1 2 3  4 5 9  7 8 9  # use '==' for # element-wise check J&gt; A[ A[:,3] .==9, :] 2x3 Array{Int64,2}:  4 5 9  7 8 9</pre>	<b>Extracting rows and column</b>  <b>(here: get rows that have value 9 in column 3)</b>
<b>Accessing elements</b>  <b>(here: 1st element)</b>	<pre>M&gt; A = [1 2 3; 4 5 6; 7 8 9] M&gt; A(1,1) ans = 1</pre>	<pre>P&gt; A = np.array([ [1,2,3], [4,5,6], [7,8,9] ]) P&gt; A array([[1, 2, 3],        [4, 5, 6],        [7, 8, 9]])  P&gt; A[0,0] 1</pre>	<pre>R&gt; A = matrix(c(1,2,3,4,5,9,7,8,9),nrow=3,byrow=T) R&gt; A [,1] [,2] [,3] [1,] 1 2 3 [2,] 4 5 9 [3,] 7 8 9  R&gt; A[1,1] [1] 1</pre>	<pre>J&gt; A=[1 2 3; 4 5 6; 7 8 9]; J&gt; A[1,1] 1</pre>	<b>Accessing elements</b>  <b>(here: 1st element)</b>

## MANIPULATING SHAPE AND DIMENSIONS

### Converting a matrix into a row vector (by column)

```
M> A = [1 2 3; 4 5 6; 7 8 9]
```

```
M> A(:)
```

```
ans =
```

```
P> A = np.array([[1,2,3],[4,5,6],[7,8,9]]) R> A = matrix(1:9,nrow=3,byrow=T)
```

```
P> A.flatten(1) # returns a copy
```

```
array([1, 4, 7, 2, 5, 8, 3, 6, 9])
```

```
1 # alternatively A.ravel()
```

```
4 # ravel() returns a view
```

```
7
```

```
2
```

```
5
```

```
8
```

```
3
```

```
6
```

```
9
```

```
R> as.vector(A)
```

```
[1] 1 4 7 2 5 8 3 6 9
```

```
J> A=[1 2 3; 4 5 6; 7 8 9]
```

```
J> vec(A)
```

```
9-element Array{Int64,1}:
```

### Converting a matrix into a row vector (

### Converting row to column vectors

```
M> b = [1 2 3]
```

```
M> b = b'
```

```
b =
```

```
1
```

```
2
```

```
3
```

```
P> b = np.array([1, 2, 3])
```

```
P> b = b[np.newaxis].T
```

```
# alternatively
```

```
# b = b[:,np.newaxis]
```

```
P> b
```

```
array([[1],
```

```
      [2],
```

```
      [3]])
```

```
R> b = matrix(c(1,2,3), ncol=3)
```

```
R> t(b)
```

```
 [,1]
```

```
[1,] 1
```

```
[2,] 2
```

```
[3,] 3
```

```
J> b=vec([1 2 3])
```

```
3-element Array{Int64,1}:
```

```
1
```

```
2
```

```
3
```

### Converting row to column vectors

### Reshaping Matrices

(here: 3x3 matrix to row vector)

```
M> A = [1 2 3; 4 5 6; 7 8 9]
```

```
A =
```

```
1 2 3
```

```
4 5 6
```

```
7 8 9
```

```
P> A = np.array([[1,2,3],[4,5,6],[7,8,9]]) R> A = matrix(1:9,nrow=3,byrow=T)
```

```
P> A
```

```
array([[1, 2, 3],
```

```
      [4, 5, 9],
```

```
      [7, 8, 9]])
```

```
R> A
```

```
 [,1] [,2] [,3]
```

```
[1,] 1 2 3
```

```
[2,] 4 5 6
```

```
[3,] 7 8 9
```

```
J> A=[1 2 3; 4 5 6; 7 8 9]
```

```
3x3 Array{Int64,2}:
```

```
1 2 3
```

```
4 5 6
```

```
7 8 9
```

```
M> total_elements = numel(A)
```

```
P> total_elements = np.prod(A.shape)
```

```
M> B = reshape(A,1,total_elements)
```

```
% or reshape(A,1,9)
```

```
P> B = A.reshape(1, total_elements)
```

```
B =
```

```
1 4 7 2 5 8 3 6 9 # alternative shortcut:
```

```
R> total_elements = dim(A)[1] * dim(A)[2]
```

```
R> B = matrix(A, ncol=total_elements)
```

```
J> total_elements=length(A)
```

```
9
```

```
J> B=reshape(A,1,total_elements)
```

```
1x9 Array{Int64,2}:
```

```
1 4 7 2 5 8 3 6 9
```

### Reshaping Matrices

(here: 3x3 matrix to row ve

## Concatenating matrices

```
M> A = [1 2 3; 4 5 6]
```

```
M> B = [7 8 9; 10 11 12]
```

```
M> C = [A; B]
```

```
1  2  3
4  5  6
7  8  9
10 11 12
```

Stacking  
vectors and matrices

```
M> a = [1 2 3]
```

```
M> b = [4 5 6]
```

```
M> c = [a' b']
```

```
c =
1  4
2  5
3  6
```

```
M> c = [a; b]
```

```
c =
1  2  3
4  5  6
```

```
# A.reshape(1,-1)
```

```
P> B
```

```
array([[1, 2, 3, 4, 5, 6, 7, 8, 9]])
```

```
P> A = np.array([[1, 2, 3], [4, 5, 6]])
```

```
P> B = np.array([[7, 8, 9],[10,11,12]])
```

```
P> C = np.concatenate( (A, B), axis=0)
```

```
P> C
```

```
array([[1, 2, 3],
       [4, 5, 6],
       [7, 8, 9],
       [10, 11, 12]])
```

```
P> a = np.array([1,2,3])
```

```
P> b = np.array([4,5,6])
```

```
P> np.column_stack([a,b])
```

```
array([[1, 4],
       [2, 5],
       [3, 6]])
```

```
P> np.row_stack([a,b])
```

```
array([[1, 2, 3],
       [4, 5, 6]])
```

```
R> B
```

```
[,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9]
```

```
[1,] 1 4 7 2 5 8 3 6 9
```

```
R> A = matrix(1:6,nrow=2,byrow=T)
```

```
R> B = matrix(7:12,nrow=2,byrow=T)
```

```
R> C = rbind(A,B)
```

```
R> C
```

```
[,1] [,2] [,3]
[1,] 1 2 3
[2,] 4 5 6
[3,] 7 8 9
[4,] 10 11 12
```

```
R> a = matrix(1:3, ncol=3)
```

```
R> b = matrix(4:6, ncol=3)
```

```
R> matrix(rbind(A, B), ncol=2)
```

```
[,1] [,2]
[1,] 1 5
[2,] 4 3
```

```
R> rbind(A,B)
```

```
[,1] [,2] [,3]
[1,] 1 2 3
[2,] 4 5 6
```

```
J> A=[1 2 3; 4 5 6];
```

```
J> B=[7 8 9; 10 11 12];
```

```
J> C=[A; B]
```

```
4x3 Array{Int64,2}:
1 2 3
4 5 6
7 8 9
10 11 12
```

```
J> a=[1 2 3];
```

```
J> b=[4 5 6];
```

```
J> c=[a' b']
```

```
3x2 Array{Int64,2}:
1 4
2 5
3 6
```

```
J> c=[a; b]
```

```
2x3 Array{Int64,2}:
1 2 3
4 5 6
```

## Concatenating matrices

Stacking  
vectors and matrices

## BASIC MATRIX OPERATIONS

**Matrix-scalar  
operations****M>** A = [1 2 3; 4 5 6; 7 8 9]**M>** A \* 2  
ans =  
2 4 6  
8 10 12  
14 16 18**M>** A + 2**M>** A - 2**M>** A / 2**Matrix-matrix  
multiplication****M>** A = [1 2 3; 4 5 6; 7 8 9]**M>** A \* A  
ans =  
30 36 42  
66 81 96  
102 126 150**Matrix-vector  
multiplication****M>** A = [1 2 3; 4 5 6; 7 8 9]**M>** b = [1; 2; 3]**M>** A \* b  
ans =  
14  
32  
50**Element-wise  
matrix-matrix operations****M>** A = [1 2 3; 4 5 6; 7 8 9]**M>** A .\* A**P>** A = np.array([ [1,2,3], [4,5,6],  
[7,8,9] ])**P>** A \* 2  
array([[ 2, 4, 6],  
[ 8, 10, 12],  
[14, 16, 18]])**P>** A + 2**P>** A - 2**P>** A / 2# Note that NumPy was optimized for  
# in-place assignments  
# e.g., A += A instead of  
# A = A + A**P>** A = np.array([ [1,2,3], [4,5,6],  
[7,8,9] ])**P>** np.dot(A,A) # or A.dot(A)  
array([[ 30, 36, 42],  
[ 66, 81, 96],  
[102, 126, 150]])**P>** A = np.array([ [1,2,3], [4,5,6],  
[7,8,9] ])**P>** b = np.array([ [1], [2], [3] ])**P>** np.dot(A,b) # or A.dot(b)  
array([[14], [32], [50]])**P>** A = np.array([ [1,2,3], [4,5,6],  
[7,8,9] ])**P>** A \* A**R>** A = matrix(1:9, nrow=3, byrow=T)**R>** A \* 2  
[,1] [,2] [,3]  
[1,] 2 4 6  
[2,] 8 10 12  
[3,] 14 16 18**R>** A + 2**R>** A - 2**R>** A / 2**R>** A = matrix(1:9, nrow=3, byrow=T)**R>** A %\*% A  
[,1] [,2] [,3]  
[1,] 30 36 42  
[2,] 66 81 96  
[3,] 102 126 150**R>** A = matrix(1:9, ncol=3)**R>** b = matrix(1:3, nrow=3)**R>** t(b %\*% A)  
[,1]  
[1,] 14  
[2,] 32  
[3,] 50**R>** A = matrix(1:9, nrow=3, byrow=T)**R>** A \* A**J>** A=[1 2 3; 4 5 6; 7 8 9];

# elementwise operator

**J>** A .\* 2  
3x3 Array{Int64,2}:  
2 4 6  
8 10 12  
14 16 18**J>** A .+ 2;**J>** A .- 2;**J>** A ./ 2;**J>** A=[1 2 3; 4 5 6; 7 8 9];**J>** A \* A  
3x3 Array{Int64,2}:  
30 36 42  
66 81 96  
102 126 150**J>** A=[1 2 3; 4 5 6; 7 8 9];**J>** b=[1; 2; 3];**J>** A\*b  
3-element Array{Int64,1}:  
14  
32  
50**J>** A=[1 2 3; 4 5 6; 7 8 9];**J>** A .\* A**Matrix-scalar  
operations****Matrix-matrix  
multiplication****Matrix-vector  
multiplication****Element-wise  
matrix-matrix operations**

	<pre>ans =   1   4   9  16  25  36  49  64  81</pre>	<pre>array([[ 1,  4,  9],        [16, 25, 36],        [49, 64, 81]])</pre>	<pre>[,1] [,2] [,3] [1,] 1 4 9 [2,] 16 25 36 [3,] 49 64 81</pre>	<pre>3x3 Array{Int64,2}:  1 4 9 16 25 36 49 64 81</pre>	
	<pre>M&gt; A .+ A</pre>	<pre>P&gt; A + A</pre>	<pre>R&gt; A + A</pre>	<pre>J&gt; A .+ A;</pre>	
	<pre>M&gt; A .- A</pre>	<pre>P&gt; A - A</pre>	<pre>R&gt; A - A</pre>	<pre>J&gt; A .- A;</pre>	
	<pre>M&gt; A ./ A</pre>	<pre>P&gt; A / A</pre>	<pre>R&gt; A / A</pre>	<pre>J&gt; A ./ A;</pre>	
		<pre># Note that NumPy was optimized for # in-place assignments # e.g., A += A instead of # A = A + A</pre>			
Matrix elements to power n	<pre>M&gt; A = [1 2 3; 4 5 6; 7 8 9]</pre>	<pre>P&gt; A = np.array([ [1,2,3], [4,5,6],                   [7,8,9] ])</pre>	<pre>R&gt; A = matrix(1:9, nrow=3, byrow=T)</pre>	<pre>J&gt; A=[1 2 3; 4 5 6; 7 8 9];</pre>	Matrix elements to power n
(here: individual elements squared)	<pre>M&gt; A.^2</pre>	<pre>P&gt; np.power(A,2)</pre>	<pre>R&gt; A ^ 2</pre>	<pre>J&gt; A .^ 2</pre>	(here: individual elements :
	<pre>ans =   1   4   9  16  25  36  49  64  81</pre>	<pre>array([[ 1,  4,  9],        [16, 25, 36],        [49, 64, 81]])</pre>	<pre>[,1] [,2] [,3] [1,] 1 4 9 [2,] 16 25 36 [3,] 49 64 81</pre>	<pre>3x3 Array{Int64,2}:  1 4 9 16 25 36 49 64 81</pre>	
Matrix to power n	<pre>M&gt; A = [1 2 3; 4 5 6; 7 8 9]</pre>	<pre>P&gt; A = np.array([ [1,2,3], [4,5,6],                   [7,8,9] ])</pre>	<pre>R&gt; A = matrix(1:9, ncol=3)</pre>	<pre>J&gt; A=[1 2 3; 4 5 6; 7 8 9];</pre>	Matrix to power n
(here: matrix-matrix multiplication with itself)	<pre>M&gt; A ^ 2</pre>	<pre>P&gt; np.linalg.matrix_power(A,2)</pre>	<pre># requires the 'expm' package</pre>	<pre>J&gt; A ^ 2</pre>	(here: matrix-matrix multip
	<pre>ans =   30   36   42   66   81   96  102  126  150</pre>	<pre>array([[ 30,  36,  42],        [ 66,  81,  96],        [102, 126, 150]])</pre>	<pre>R&gt; install.packages('expm')  R&gt; library(expm)  R&gt; A %^% 2 [,1] [,2] [,3] [1,] 30 66 102 [2,] 36 81 126 [3,] 42 96 150</pre>	<pre>3x3 Array{Int64,2}:  30 36 42  66 81 96 102 126 150</pre>	
Matrix transpose	<pre>M&gt; A = [1 2 3; 4 5 6; 7 8 9]</pre>	<pre>P&gt; A = np.array([ [1,2,3], [4,5,6],                   [7,8,9] ])</pre>	<pre>R&gt; A = matrix(1:9, nrow=3, byrow=T)</pre>	<pre>J&gt; A=[1 2 3; 4 5 6; 7 8 9]</pre>	Matrix transpose
	<pre>M&gt; A'</pre>	<pre>P&gt; A.T</pre>	<pre>R&gt; t(A)</pre>	<pre>3x3 Array{Int64,2}:  1 2 3  4 5 6</pre>	
	<pre>ans =</pre>	<pre>array([[1, 4, 7],</pre>	<pre>[,1] [,2] [,3]</pre>		



**Determinant of a matrix:****A -> |A|**

```
1  4  7
2  5  8
3  6  9
```

```
M> A = [6 1 1; 4 -2 5; 2 8 7]
```

```
A =
```

```
6  1  1
4 -2  5
2  8  7
```

```
M> det(A)
```

```
ans = -306
```

**Inverse of a matrix**

```
M> A = [4 7; 2 6]
```

```
A =
```

```
4  7
2  6
```

```
M> A_inv = inv(A)
```

```
A_inv =
```

```
0.60000  -0.70000
-0.20000  0.40000
```

```
[2, 5, 8],
[3, 6, 9]])
```

```
P> A = np.array([[6,1,1],[4,-2,5],
[2,8,7]])
```

```
P> A
```

```
array([[ 6,  1,  1],
       [ 4, -2,  5],
       [ 2,  8,  7]])
```

```
P> np.linalg.det(A)
```

```
-306
```

```
P> A = np.array([[4, 7], [2, 6]])
```

```
P> A
```

```
array([[4, 7],
       [2, 6]])
```

```
P> A_inverse = np.linalg.inv(A)
```

```
P> A_inverse
```

```
array([[ 0.6, -0.7],
       [-0.2,  0.4]])
```

```
[1,] 1 4 7
[2,] 2 5 8
[3,] 3 6 9
```

```
R> A = matrix(c(6,1,1,4,-2,5,2,8,7), nrow=3,
byrow=T)
```

```
R> A
```

```
[,1] [,2] [,3]
[1,] 6 1 1
[2,] 4 -2 5
[3,] 2 8 7
```

```
R> det(A)
```

```
[1] -306
```

```
R> A = matrix(c(4,7,2,6), nrow=2, byrow=T)
```

```
R> A
```

```
[,1] [,2]
[1,] 4 7
[2,] 2 6
```

```
R> solve(A)
```

```
[,1] [,2]
[1,] 0.6 -0.7
[2,] -0.2 0.4
```

```
7 8 9
```

```
J> A'
```

```
3x3 Array{Int64,2}:
```

```
1 4 7
2 5 8
3 6 9
```

```
J> A=[6 1 1; 4 -2 5; 2 8 7]
```

```
3x3 Array{Int64,2}:
```

```
6 1 1
4 -2 5
2 8 7
```

```
J> det(A)
```

```
-306
```

```
J> A=[4 7; 2 6]
```

```
2x2 Array{Int64,2}:
```

```
4 7
2 6
```

```
J> A_inv=inv(A)
```

```
2x2 Array{Float64,2}:
```

```
0.6 -0.7
-0.2 0.4
```

**Determinant of a matrix:****A -> |A|****Inverse of a matrix****ADVANCED MATRIX OPERATIONS**

Calculating the covariance matrix of 3 random variables	<pre>M&gt; x1 = [4.0000 4.2000 3.9000 4.3000 4.1000]'</pre>	Calculating the covariance of 3 random variables
	<pre>P&gt; x1 = np.array([ 4, 4.2, 3.9, 4.3, 4.1])</pre>	
(here: covariances of the means	<pre>R&gt; x1 = matrix(c(4, 4.2, 3.9, 4.3, 4.1), ncol=5)</pre>	(here: covariances of the m
of x1, x2, and x3)	<pre>J&gt; x1=[4.0 4.2 3.9 4.3 4.1]';</pre>	of x1, x2, and x3)
	<pre>M&gt; x2 = [2.0000 2.1000 2.0000 2.1000 2.2000]'</pre>	
	<pre>P&gt; x2 = np.array([ 2, 2.1, 2, 2.1, 2.2])</pre>	
	<pre>R&gt; x2 = matrix(c(2, 2.1, 2, 2.1, 2.2), ncol=5)</pre>	
	<pre>J&gt; x2=[2. 2.1 2. 2.1 2.2]';</pre>	
	<pre>M&gt; cov( [x1,x2,x3] )</pre>	
	<pre>P&gt; np.cov([x1, x2, x3])</pre>	
	<pre>R&gt; cov(matrix(c(x1, x2, x3), ncol=3))</pre>	
	<pre>J&gt; cov([x1 x2 x3])</pre>	
	<pre>ans =</pre>	
	<pre>Array([[ 0.025 , 0.0075 , 0.00175],</pre>	
	<pre>[ 0.0075 , 0.007 , 0.00135],</pre>	
	<pre>[ 0.00175, 0.00135, 0.00043]]</pre>	
	<pre>2.5000e-02 7.5000e-03 1.7500e-03</pre>	
	<pre>7.5000e-03 7.0000e-03 1.3500e-03</pre>	
	<pre>1.7500e-03 1.3500e-03 4.3000e-04</pre>	
Calculating eigenvectors and eigenvalues	<pre>M&gt; A = [3 1; 1 3]</pre>	Calculating eigenvectors and eigenvali
	<pre>P&gt; A = np.array([[3, 1], [1, 3]])</pre>	
	<pre>R&gt; A = matrix(c(3,1,1,3), ncol=2)</pre>	
	<pre>J&gt; A=[3 1; 1 3]</pre>	
	<pre>P&gt; A</pre>	
	<pre>R&gt; A</pre>	
	<pre>J&gt; (eig_vec,eig_val)=eig(a)</pre>	
	<pre>P&gt; eig_val, eig_vec = np.linalg.eig(A)</pre>	
	<pre>R&gt; eigen(A)</pre>	
	<pre>J&gt; (eig_vec,eig_val)=eig(a)</pre>	
	<pre>P&gt; eig_val</pre>	
	<pre>R&gt; eigen(A)</pre>	
	<pre>J&gt; (eig_vec,eig_val)=eig(a)</pre>	
	<pre>P&gt; eig_val</pre>	
	<pre>R&gt; eigen(A)</pre>	
	<pre>J&gt; (eig_vec,eig_val)=eig(a)</pre>	
	<pre>P&gt; eig_val</pre>	
	<pre>R&gt; eigen(A)</pre>	
	<pre>J&gt; (eig_vec,eig_val)=eig(a)</pre>	
	<pre>P&gt; eig_val</pre>	
	<pre>R&gt; eigen(A)</pre>	
	<pre>J&gt; (eig_vec,eig_val)=eig(a)</pre>	
	<pre>P&gt; eig_val</pre>	
	<pre>R&gt; eigen(A)</pre>	
	<pre>J&gt; (eig_vec,eig_val)=eig(a)</pre>	
	<pre>P&gt; eig_val</pre>	
	<pre>R&gt; eigen(A)</pre>	
	<pre>J&gt; (eig_vec,eig_val)=eig(a)</pre>	
	<pre>P&gt; eig_val</pre>	
	<pre>R&gt; eigen(A)</pre>	
	<pre>J&gt; (eig_vec,eig_val)=eig(a)</pre>	
	<pre>P&gt; eig_val</pre>	
	<pre>R&gt; eigen(A)</pre>	
	<pre>J&gt; (eig_vec,eig_val)=eig(a)</pre>	
	<pre>P&gt; eig_val</pre>	
	<pre>R&gt; eigen(A)</pre>	
	<pre>J&gt; (eig_vec,eig_val)=eig(a)</pre>	
	<pre>P&gt; eig_val</pre>	
	<pre>R&gt; eigen(A)</pre>	
	<pre>J&gt; (eig_vec,eig_val)=eig(a)</pre>	
	<pre>P&gt; eig_val</pre>	
	<pre>R&gt; eigen(A)</pre>	
	<pre>J&gt; (eig_vec,eig_val)=eig(a)</pre>	
	<pre>P&gt; eig_val</pre>	
	<pre>R&gt; eigen(A)</pre>	
	<pre>J&gt; (eig_vec,eig_val)=eig(a)</pre>	
	<pre>P&gt; eig_val</pre>	
	<pre>R&gt; eigen(A)</pre>	
	<pre>J&gt; (eig_vec,eig_val)=eig(a)</pre>	
	<pre>P&gt; eig_val</pre>	
	<pre>R&gt; eigen(A)</pre>	
	<pre>J&gt; (eig_vec,eig_val)=eig(a)</pre>	
	<pre>P&gt; eig_val</pre>	
	<pre>R&gt; eigen(A)</pre>	
	<pre>J&gt; (eig_vec,eig_val)=eig(a)</pre>	
	<pre>P&gt; eig_val</pre>	
	<pre>R&gt; eigen(A)</pre>	
	<pre>J&gt; (eig_vec,eig_val)=eig(a)</pre>	
	<pre>P&gt; eig_val</pre>	
	<pre>R&gt; eigen(A)</pre>	
	<pre>J&gt; (eig_vec,eig_val)=eig(a)</pre>	
	<pre>P&gt; eig_val</pre>	
	<pre>R&gt; eigen(A)</pre>	
	<pre>J&gt; (eig_vec,eig_val)=eig(a)</pre>	
	<pre>P&gt; eig_val</pre>	
	<pre>R&gt; eigen(A)</pre>	
	<pre>J&gt; (eig_vec,eig_val)=eig(a)</pre>	
	<pre>P&gt; eig_val</pre>	
	<pre>R&gt; eigen(A)</pre>	
	<pre>J&gt; (eig_vec,eig_val)=eig(a)</pre>	
	<pre>P&gt; eig_val</pre>	
	<pre>R&gt; eigen(A)</pre>	
	<pre>J&gt; (eig_vec,eig_val)=eig(a)</pre>	
	<pre>P&gt; eig_val</pre>	
	<pre>R&gt; eigen(A)</pre>	
	<pre>J&gt; (eig_vec,eig_val)=eig(a)</pre>	
	<pre>P&gt; eig_val</pre>	
	<pre>R&gt; eigen(A)</pre>	
	<pre>J&gt; (eig_vec,eig_val)=eig(a)</pre>	
	<pre>P&gt; eig_val</pre>	
	<pre>R&gt; eigen(A)</pre>	
	<pre>J&gt; (eig_vec,eig_val)=eig(a)</pre>	
	<pre>P&gt; eig_val</pre>	
	<pre>R&gt; eigen(A)</pre>	
	<pre>J&gt; (eig_vec,eig_val)=eig(a)</pre>	
	<pre>P&gt; eig_val</pre>	
	<pre>R&gt; eigen(A)</pre>	
	<pre>J&gt; (eig_vec,eig_val)=eig(a)</pre>	
	<pre>P&gt; eig_val</pre>	
	<pre>R&gt; eigen(A)</pre>	
	<pre>J&gt; (eig_vec,eig_val)=eig(a)</pre>	
	<pre>P&gt; eig_val</pre>	
	<pre>R&gt; eigen(A)</pre>	
	<pre>J&gt; (eig_vec,eig_val)=eig(a)</pre>	
	<pre>P&gt; eig_val</pre>	
	<pre>R&gt; eigen(A)</pre>	
	<pre>J&gt; (eig_vec,eig_val)=eig(a)</pre>	
	<pre>P&gt; eig_val</pre>	
	<pre>R&gt; eigen(A)</pre>	
	<pre>J&gt; (eig_vec,eig_val)=eig(a)</pre>	
	<pre>P&gt; eig_val</pre>	
	<pre>R&gt; eigen(A)</pre>	
	<pre>J&gt; (eig_vec,eig_val)=eig(a)</pre>	
	<pre>P&gt; eig_val</pre>	
	<pre>R&gt; eigen(A)</pre>	
	<pre>J&gt; (eig_vec,eig_val)=eig(a)</pre>	

creating random vectors from the multivariate normal distribution given mean and covariance matrix

(here: 5 random vectors with mean 0, covariance = 0, variance = 2)

```
% download the package from:
% http://octave.sourceforge.net/packages.php
% pkg install
% ~/Desktop/io-2.0.2.tar.gz
% pkg install
% ~/Desktop/statistics-1.2.3.tar.gz
M> pkg load statistics

M> mean = [0 0]

M> cov = [2 0; 0 2]
cov =
    2    0
    0    2

M> mvnrnd(mean,cov,5)

    2.480150   -0.559906
   -2.933047    0.560212
    0.098206    3.055316
   -0.985215   -0.990936
    1.122528    0.686977
```

```
P> cov = np.array([[2,0],[0,2]])
```

```
P> np.random.multivariate_normal(mean, cov, 5)
```

```
Array([[ 1.55432624, -1.17972629],
       [-2.01185294,  1.96081908],
       [-2.11810813,  1.45784216],
       [-2.93207591, -0.07369322],
       [-1.37031244, -1.18408792]])
```

```
R> install.packages('MASS')
```

```
R> library(MASS)
```

```
R> mvrnorm(n=10, mean, cov)
```

```
[,1] [,2]
[1,] -0.8407830 -0.1882706
[2,]  0.8496822 -0.7889329
[3,] -0.1564171  0.8422177
[4,] -0.6288779  1.0618688
[5,] -0.5103879  0.1303697
[6,]  0.8413189 -0.1623758
[7,] -1.0495466 -0.4161082
[8,] -1.3236339  0.7755572
[9,]  0.2771013  1.4900494
[10,] -1.3536268  0.2338913
```

```
J> using Distributions
```

```
J> mean=[0., 0.]
```

```
2-element Array{Float64,1}:
```

```
0
```

```
0
```

```
J> cov=[2. 0.; 0. 2.]
```

```
2x2 Array{Float64,2}:
```

```
2.0 0.0
```

```
0.0 2.0
```

```
J> rand( MvNormal(mean, cov), 5)
```

```
2x5 Array{Float64,2}:
```

```
-0.527634  0.370725 -0.761928
-3.91747  1.47516
-0.448821  2.21904  2.24561
0.692063  0.390495
```

creating random vectors from the multivariate normal distribution given mean and covariance matrix

(here: 5 random vectors with mean 0, covariance = 0, variance = 2)