

$$\overline{X} = \frac{\sum_{i=1}^n X_i}{n}; S^2 = \frac{\sum_{i=1}^n (X_i - \overline{X})^2}{n-1} = \frac{\sum_{i=1}^n X_i^2 - n\overline{X}^2}{n-1}; S_p^2 = \frac{\sum_{i=1}^n (n_i - 1)S_i^2}{\sum_{i=1}^n (n_i - 1)}; P(Z > z_{\alpha/2}) = P(T > t_{\alpha/2}) = P(T^* > t_{\alpha/2}^*) = \alpha/2; Z \sim N(0,1); T \sim t_{n-1}; T^* \sim t_{n_1+n_2-2}$$

Intervalo de confiança a 1 - α % de confiança

$$\left[\overline{X} \pm z_{\alpha/2} \frac{\sigma}{\sqrt{n}} \right]; \left[\overline{X} \pm t_{\alpha/2, n-1} \frac{s}{\sqrt{n}} \right]; \left[\hat{p} \pm z_{\alpha/2} \sqrt{\frac{\hat{p}(1-\hat{p})}{n}} \right]; \left[\frac{(n-1)S^2}{\chi^2_{1-\alpha/2, n-1}}; \frac{(n-1)S^2}{\chi^2_{\alpha/2, n-1}} \right]; \left[\overline{X}_1 - \overline{X}_2 \pm z_{\alpha/2} \sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}} \right]; \left[\overline{X}_1 - \overline{X}_2 \pm t_{\alpha/2} \sqrt{\frac{S_p^2}{n_1} + \frac{S_p^2}{n_2}} \right]; \left[\hat{p}_1 - \hat{p}_2 \pm z_{\alpha/2} \sqrt{\frac{\hat{p}_1(1-\hat{p}_1)}{n_1} + \frac{\hat{p}_2(1-\hat{p}_2)}{n_2}} \right]$$

H_0	H_1	Regra de decisão (H_0 é falsa se)	H_0	H_1	Regra de decisão (H_0 é falsa se)
$\mu \neq \mu_0$	$\mu > \mu_0$	$\overline{X}_{obs} \notin \left[\mu_0 \pm z_{\alpha/2} \frac{\sigma}{\sqrt{n}} \right]$ ou $Z_{obs} \notin [-z_{\alpha/2}; z_{\alpha/2}]$; $P(Z > z_{\alpha/2}) = \alpha/2$	$p \neq p_0$	$p > p_0$	$\hat{p}_{obs} \notin \left[p_0 \pm z_{\alpha/2} \sqrt{\frac{p_0(1-p_0)}{n}} \right]$ ou $Z_{obs} \notin [-z_{\alpha/2}; z_{\alpha/2}]$; $P(Z > z_{\alpha/2}) = \alpha/2$
$\mu = \mu_0$	$\mu < \mu_0$	$\overline{X}_{obs} \in \left[\mu_0 + z_{\alpha} \frac{\sigma}{\sqrt{n}}; \infty \right)$ ou $Z_{obs} \in [z_{\alpha}; \infty]$; $Z_{obs} = \frac{\overline{X}_{obs} - \mu_0}{\frac{\sigma}{\sqrt{n}}}$	$p = p_0$	$p < p_0$	$\hat{p}_{obs} \in \left[p_0 + z_{\alpha} \sqrt{\frac{p_0(1-p_0)}{n}}; \infty \right)$ ou $Z_{obs} \in [z_{\alpha}; \infty]$; $Z_{obs} = \frac{\hat{p} - p_0}{\sqrt{\frac{p_0(1-p_0)}{n}}}$
		$\overline{X}_{obs} \in [-\infty; \mu_0 - z_{\alpha} \frac{\sigma}{\sqrt{n}}]$ ou $Z_{obs} \in [-\infty; -z_{\alpha}]$; $Z \sim N(0;1)$			$\hat{p}_{obs} \in [-\infty; p_0 - z_{\alpha} \sqrt{\frac{p_0(1-p_0)}{n}}]$ ou $Z_{obs} \in [-\infty; -z_{\alpha}]$; $Z \sim N(0;1)$
$\mu \neq \mu_0$	$\mu > \mu_0$	$\overline{X}_{obs} \notin \left[\mu_0 \pm t_{\alpha/2} \frac{s}{\sqrt{n}} \right]$ ou $t_{obs} \notin [-t_{\alpha/2}; t_{\alpha/2}]$; $P(T > t_{\alpha/2}) = \alpha/2$	$\sigma^2 \neq \sigma_0^2$	$\sigma^2 > \sigma_0^2$	$S^2 \notin \left[\frac{\sigma_0^2 \chi^2_{\alpha/2}}{n-1}; \frac{\sigma_0^2 \chi^2_{1-\alpha/2}}{n-1} \right]$ ou $\chi^2_{obs} \notin [\chi^2_{\alpha/2}; \chi^2_{1-\alpha/2}]$; $P(\chi^2 < \chi^2_{\alpha/2}) = \alpha/2$
$\mu = \mu_0$	$\mu < \mu_0$	$\overline{X}_{obs} \in \left[\mu_0 + t_{\alpha} \frac{s}{\sqrt{n}}; \infty \right)$ ou $t_{obs} \in [t_{\alpha}; \infty]$; $t_{obs} = \frac{\overline{X}_{obs} - \mu_0}{s/\sqrt{n}}$	$\sigma^2 = \sigma_0^2$	$\sigma^2 < \sigma_0^2$	$S^2 \in \left[\frac{\sigma_0^2 \chi^2_{1-\alpha/2}}{n-1}; \infty \right)$ ou $\chi^2_{obs} \in [\chi^2_{1-\alpha/2}; \infty]$; $\chi^2_{obs} = \frac{(n-1)S^2}{\sigma_0^2}$
		$\overline{X}_{obs} \in [-\infty; \mu_0 - t_{\alpha} \frac{s}{\sqrt{n}}]$ ou $t_{obs} \in [-\infty; -t_{\alpha}]$; $T \sim t_{n-1}$			$S^2 \in \left[0; \frac{\sigma_0^2 \chi^2_{\alpha/2}}{n-1} \right]$ ou $\chi^2_{obs} \in]0; \chi^2_{\alpha/2}]$; $\chi^2 \sim \chi^2_{n-1}$

H_0	H_1	Regra de decisão (H_0 é falsa se)	H_0	H_1	Regra de decisão (H_0 é falsa se)
$\mu_1 \neq \mu_2$	$\mu_1 > \mu_2$	$\overline{X}_1 - \overline{X}_2 \notin \left[\pm z_{\alpha/2} \sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}} \right]$ ou $Z_{obs} \notin [\pm z_{\alpha/2}]$; $P(Z > z_{\alpha/2}) = \alpha/2$	$p_1 \neq p_2$	$p_1 > p_2$	$\hat{p}_1 - \hat{p}_2 \notin \left[\pm z_{\alpha/2} \sqrt{\frac{\hat{p}(1-\hat{p})}{n_1} + \frac{\hat{p}(1-\hat{p})}{n_2}} \right]$ ou $Z_{obs} \notin [\pm z_{\alpha/2}]$; $P(Z > z_{\alpha/2}) = \alpha/2$
$\mu_1 = \mu_2$	$\mu_1 < \mu_2$	$\overline{X}_1 - \overline{X}_2 \in \left[z_{\alpha} \sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}; \infty \right)$ ou $Z_{obs} \in [z_{\alpha}; \infty]$; $Z_{obs} = \frac{\overline{X}_1 - \overline{X}_2}{\sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}}$	$p_1 = p_2$	$p_1 < p_2$	$\hat{p}_1 - \hat{p}_2 \in \left[z_{\alpha} \sqrt{\frac{\hat{p}(1-\hat{p})}{n_1} + \frac{\hat{p}(1-\hat{p})}{n_2}}; \infty \right)$ ou $Z_{obs} \in [z_{\alpha}; \infty]$; $Z_{obs} = \frac{\hat{p}_1 - \hat{p}_2}{\sqrt{\frac{\hat{p}(1-\hat{p})}{n_1} + \frac{\hat{p}(1-\hat{p})}{n_2}}}$
		$\overline{X}_1 - \overline{X}_2 \in \left[-\infty; -z_{\alpha} \sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}} \right]$ ou $Z_{obs} \in [-\infty; -z_{\alpha}]$; $Z \sim N(0;1)$			$\hat{p}_1 - \hat{p}_2 \in \left[-\infty; z_{\alpha} \sqrt{\frac{\hat{p}(1-\hat{p})}{n_1} + \frac{\hat{p}(1-\hat{p})}{n_2}} \right]$ ou $Z_{obs} \in [-\infty; -z_{\alpha}]$; $\hat{p} = \frac{n_1 \hat{p}_1 + n_2 \hat{p}_2}{n_2 + n_2}$
$\mu_1 \neq \mu_2$	$\mu_1 > \mu_2$	$\overline{X}_1 - \overline{X}_2 \notin \left[\pm t_{\alpha/2} \sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}} \right]$ ou $t_{obs} \notin [\pm t_{\alpha/2}]$; $P(T > t_{\alpha/2}) = \alpha/2$	$\sigma_1^2 \neq \sigma_2^2$	$\sigma_1^2 > \sigma_2^2$	$\frac{S_1^2}{S_2^2} \notin [F_{\alpha/2, n_1-1, n_2-1}; F_{1-\alpha/2, n_1-1, n_2-1}]$; $P(F > F_{\alpha/2}) = \alpha/2$
$\mu_1 = \mu_2$	$\mu_1 < \mu_2$	$\overline{X}_1 - \overline{X}_2 \in \left[+t_{\alpha} \sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}; \infty \right)$ ou $t_{obs} \in [t_{\alpha}; \infty]$; $t_{obs} = \frac{\overline{X}_1 - \overline{X}_2}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}}$	$\sigma_1^2 = \sigma_2^2$	$\sigma_1^2 < \sigma_2^2$	$\frac{S_1^2}{S_2^2} \in [F_{1-\alpha, n_1-1, n_2-1}, \infty]$
		$\overline{X}_1 - \overline{X}_2 \in \left[-\infty; -t_{\alpha} \sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}} \right]$ ou $t_{obs} \in [-\infty; -t_{\alpha}]$; $T \sim t_{n_1+n_2-2}$			$\frac{S_1^2}{S_2^2} \in]0; F_{\alpha, n_1-1, n_2-1}]$; $F \sim F_{n-1, n-2}$

Dados Emparelhados: $\overline{D} = \frac{\sum_{i=1}^n D_i}{n}; D_i = X_i - Y_i; S_D^2 = \frac{\sum_{i=1}^n (D_i - \overline{D})^2}{n-1}; t_{obs} = \overline{D} / \sqrt{S_D^2/n}; P(T > t_{\alpha/2}) = \alpha/2; T \sim t_{n-1}$

$H_0: \mu_x = \mu_y$	$H_1: \mu_x \neq \mu_y$	$H_1: \mu_x > \mu_y$	$H_1: \mu_x < \mu_y$
H_0 é falsa se	$\overline{D} \notin [\pm t_{\alpha/2} \sqrt{S_D^2/n}]$ ou $t_{obs} \notin [\pm t_{\alpha/2}]$	$\overline{D} \in [t_{\alpha} \sqrt{S_D^2/n}, \infty]$ ou $t_{obs} \in [t_{\alpha/2}, \infty]$	$\overline{D} \in [-\infty, -t_{\alpha} \sqrt{S_D^2/n}]$ ou $t_{obs} \in [-\infty, -t_{\alpha}]$

ANOVA 1 fator Modelo $X_{ij} = \mu + \alpha_i + \epsilon_{ij}; i = 1, \dots, k; j = 1, \dots, n_i$

FV	SQ	gl	QM	F_{obs}
Entre	$\sum_{i=1}^k n_i (\overline{X}_i - \overline{X})^2$	$k - 1$	$S_e^2 = \frac{SQ_{Entre}}{k-1}$	$\frac{F_{obs}}{S_e^2}$
Dentro	$\sum_{i=1}^k \sum_{j=1}^{n_i} (X_{ij} - \overline{X}_i)^2$	$\sum_{i=1}^k (n_i - 1)$	$S_p^2 = \frac{SQ_{Dentro}}{\sum_{i=1}^k (n_i - 1)}$	
Total	$\sum_{i=1}^k \sum_{j=1}^{n_i} (X_{ij} - \overline{X})^2$	$\sum_{i=1}^k n_i - 1$		

$H_0: \alpha_1 = \dots = \alpha_k = 0; H_0$ é falsa se $F_{obs} > F_{\alpha, k-1, \sum_{i=1}^k (n_i - 1)}$

ANOVA 2 fatores sem réplica

Modelo $X_{ij} = \mu + \alpha_i + \beta_j + \epsilon_{ij}, i = 1, \dots, a; j = 1, \dots, b$

FV	SQ	gl	QM	F_{obs}
A	$\sum_{i=1}^a b (\overline{X}_i - \overline{X})^2$	$a - 1$	$S_A^2 = \frac{SQA}{a-1}$	$F_a = \frac{S_A^2}{S_p^2}$
B	$\sum_{j=1}^b a (\overline{X}_j - \overline{X})^2$	$b - 1$	$S_B^2 = \frac{SQB}{b-1}$	$F_b = \frac{S_B^2}{S_p^2}$
Resíduos	$SQT - SQA - SQB$	$(a-1)(b-1)$	$S_r^2 = \frac{SQRes}{(a-1)(b-1)}$	
Total	$\sum_{i=1}^a \sum_{j=1}^b (X_{ij} - \overline{X})^2$	$a \times b - 1$		

$H_{01}: \alpha_1 = \dots = \alpha_a = 0; H_{01}$ é falsa se $F_a > F_{\alpha, a-1, (a-1)(b-1)}$

$H_{02}: \beta_1 = \dots = \beta_b = 0; H_{02}$ é falsa se $F_b > F_{\alpha, b-1, (a-1)(b-1)}$

ANOVA - Modelo de regressão simples

Modelo $Y_i = \beta_0 + \beta_1 X_i + \epsilon_i, i = 1 \dots, n$

FV	SQ	gl	QM	F_{obs}
Regressão	$\sum_{i=1}^n (\hat{Y}_i - \overline{Y})^2$	1	$S_{reg}^2 = SQReg$	$\frac{S_{reg}^2}{S_{res}^2}$
Resíduo	$\sum_{i=1}^n (Y_i - \hat{Y})^2$	$n - 2$	$S_{res}^2 = \frac{SQRes}{n-2}$	
Total	$\sum_{i=1}^n (Y_i - \overline{Y})^2$	$n - 1$		

$SQReg = \hat{\beta}_1^2 \sum_{i=1}^n (X_i - \overline{X})^2; H_0: \beta_1 = 0; H_0$ é falsa se $F_{obs} > F_{\alpha, 1, n-2}$

$R^2 = \frac{SQReg}{SQT}; \hat{Y}_i = \hat{\beta}_0 + \hat{\beta}_1 X_i; \hat{\beta}_0 = \overline{Y} - \hat{\beta}_1 \overline{X}; \hat{\beta}_1 = \frac{\sum_{i=1}^n Y_i X_i - n \overline{Y} \overline{X}}{\sum_{i=1}^n (X_i - \overline{X})^2}$

IC: $\hat{\beta}_1 \pm t_{\alpha/2, n-2} S_{res} \sqrt{\frac{1}{\sum_{i=1}^n (X_i - \overline{X})^2}}; \hat{\beta}_0 \pm t_{\alpha/2, n-2} S_{res} \sqrt{\frac{\sum_{i=1}^n X_i^2}{n \sum_{i=1}^n (X_i - \overline{X})^2}};$

IC para média: $\hat{Y}_i \pm t_{\alpha/2, n-2} S_{res} \sqrt{\frac{1}{n} + \frac{(X_i - \overline{X})^2}{\sum_{i=1}^n (X_i - \overline{X})^2}};$

IC para futura obs.: $\hat{Y}_i \pm t_{\alpha/2, n-2} S_{res} \sqrt{1 + \frac{1}{n} + \frac{(X_i - \overline{X})^2}{\sum_{i=1}^n (X_i - \overline{X})^2}}$

ANOVA 2 fatores com réplica

Modelo $X_{ijk} = \mu + \alpha_i + \beta_j + \alpha \beta_{ij} + \epsilon_{ijk}, i = 1, \dots, a; j = 1, \dots, b; k = 1, \dots, n$

FV	SQ	gl	QM	F_{obs}
A	$\sum_{i=1}^a b n (\overline{X}_i - \overline{X})^2$	$a - 1$	$S_A^2 = \frac{SQA}{a-1}$	$F_a = \frac{S_A^2}{S_p^2}$
B	$\sum_{j=1}^b a n (\overline{X}_j - \overline{X})^2$	$b - 1$	$S_B^2 = \frac{SQB}{b-1}$	$F_b = \frac{S_B^2}{S_p^2}$
AB	$SQT - SQA - SQB - SQRes$	$(a-1)(b-1)$	$S_{AB}^2 = \frac{SQAB}{(a-1)(b-1)}$	$F_{ab} = \frac{S_{AB}^2}{S_p^2}$
Resíduos	$\sum_{i=1}^a \sum_{j=1}^b \sum_{k=1}^n (n-1) s_{ij}^2$	$ab(n-1)$	$S_r^2 = \frac{SQRes}{ab(n-1)}$	
Total	$\sum_{i=1}^a \sum_{j=1}^b \sum_{k=1}^n (X_{ijk} - \overline{X})^2$	$a \times b \times n - 1$		

$\overline{X}_{ij} = \sum_{k=1}^n \frac{X_{ijk}}{n}; \overline{X}_{i.} = \sum_{j=1}^b \frac{\overline{X}_{ij}}{b}; \overline{X}_{.j} = \sum_{i=1}^a \frac{\overline{X}_{ij}}{a}; \overline{X} = \frac{\sum_{i=1}^a \sum_{j=1}^b \overline{X}_{ij}}{ab}$

$H_{01}: \alpha_1 = \dots = \alpha_a = 0; H_{01}$ é falsa se $F_a > F_{\alpha, a-1, ab(n-1)}$

$H_{02}: \beta_1 = \dots = \beta_b = 0; H_{02}$ é falsa se $F_b > F_{\alpha, b-1, ab(n-1)}$

$H_{03}: \alpha \beta_{11} = \dots = \alpha \beta_{ab} = 0; H_{02}$ é falsa se $F_{ab} > F_{\alpha, (a-1)(b-1), ab(n-1)}$

ANOVA - Modelo de regressão com 2 v auxiliares

Modelo $Y_i = \beta_0 + \beta_1 X_{1i} + \beta_2 X_{2i} + \epsilon_i, i = 1 \dots, n$

FV	SQ	gl	QM	F_{obs}
Regressão	$\sum_{i=1}^n (\hat{Y}_i - \overline{Y})^2$	2	$S_{reg}^2 = SQReg/2$	$\frac{S_{reg}^2}{S_{res}^2}$
Resíduo	$\sum_{i=1}^n (Y_i - \hat{Y})^2$	$n - 3$	$S_{res}^2 = \frac{SQRes}{n-3}$	
Total	$\sum_{i=1}^n (Y_i - \overline{Y})^2$	$n - 1$		

$H_0: \beta_1 = \beta_2 = 0; H_0$ é falsa se $F_{obs} > F_{\alpha, 2, n-3}$

Teste de melhoria - Teste do F-parcial

$M_1: Y_i = \beta_0 + \beta_1 X_{1i} + \epsilon_i \rightarrow SQReg_1; H_0: \beta_1 = 0$ é falsa

$M_2: Y_i = \beta_0 + \beta_1 X_{1i} + \beta_2 X_{2i} + \epsilon_i \rightarrow SQReg_2; S_{res_2}^2; H_0: \beta_1 = \beta_2 = 0$ é falsa

$H_0: \beta_2 = 0 | \beta_1 \neq 0; H_0$ é falsa se $F_{parcial} = \frac{SQReg_2 - SQReg_1}{S_{res_2}^2} > F_{\alpha, 1, n-3}$

Teste de aderência H_0 : os dados seguem uma específica $f(X)$

H_0 é falsa se $\chi^2_{obs} = \sum_{i=1}^k \frac{(O_i - E_i)^2}{E_i} > \chi^2_{\alpha, k-1-p}, k, \#$ de classes

com $E_i > 5, \forall i, p, \#$ parâmetros estimados

Teste de associação H_0 : não existe associação entre linhas e colunas

H_0 é falsa se $\chi^2_{obs} = \sum_{i=1}^k \sum_{j=1}^c \frac{(O_{ij} - E_{ij})^2}{E_{ij}} > \chi^2_{\alpha, (k-1)(c-1)}, k, \#$ de linhas

$c, \#$ de colunas com $E_{ij} > 5, \forall i, j$