# Physics-Informed Calibration of Aeromagnetic Compensation in Magnetic Navigation Systems using Liquid Time-Constant Networks

### Favour Nerrise\*

Department of Electrical Engineering Stanford University, CA, USA fnerrise@stanford.edu Andrew (Sosa) Sosanya SandboxAQ Palo Alto, CA, USA andrew.sosanya@sandboxaq.com

Patrick Neary
SandboxAQ
Palo Alto, CA, USA
patrick.neary@sandboxaq.com

#### Abstract

Magnetic navigation (MagNav) is a rising alternative to the Global Positioning System (GPS) and has proven useful for aircraft navigation. Traditional aircraft navigation systems, while effective, face limitations in precision and reliability in certain environments and against attacks. Airborne MagNav leverages the Earth's magnetic field to provide accurate positional information. However, external magnetic fields induced by aircraft electronics and Earth's large-scale magnetic fields disrupt the weaker signal of interest. We introduce a physics-informed approach using Tolles-Lawson coefficients for compensation and Liquid Time-Constant Networks (LTCs) to remove complex, noisy signals derived from the aircraft's magnetic sources. Using real flight data with magnetometer measurements and aircraft measurements, we observe up to a 64% reduction in aeromagnetic compensation error (RMSE nT), outperforming conventional models. This significant improvement underscores the potential of a physics-informed, machine learning approach for extracting clean, reliable, and accurate magnetic signals for MagNav positional estimation.

#### 1 Introduction

In recent years, magnetic anomaly navigation (MagNav) has proven to be a viable fallback to the Global Positioning System (GPS) for aircraft navigation due to its reliability against jamming<sup>2</sup> or spoofing <sup>3</sup> attacks, independence from atmospheric weather conditions, and unsupervised position estimation [3]. Airborne MagNav estimates positioning by correlating aircraft magnetometer readings to anomaly maps of the Earth's crustal magnetic field [3]. Successful airborne MagNav studies have shown high accuracies in navigation estimation, with up to 10m distance root-mean-squared errors at low altitudes and tens of meters to kilometers at varying altitudes above ground level [4–6]. This is only slightly inferior to GPS estimation for aircraft navigation, which is accurate down to seven

<sup>\*</sup>F.N. is also an AI Ph.D. Resident at SandboxAQ, alternative email: favour.nerrise@sandboxaq.com.

<sup>&</sup>lt;sup>2</sup>GPS jamming disrupts a GPS receiver by transmitting powerful signals that block or interfere with the original GPS signal[1].

<sup>&</sup>lt;sup>3</sup>GPS spoofing manipulates existing GPS signals to mislead a receiver about its position, velocity, and timing[2].

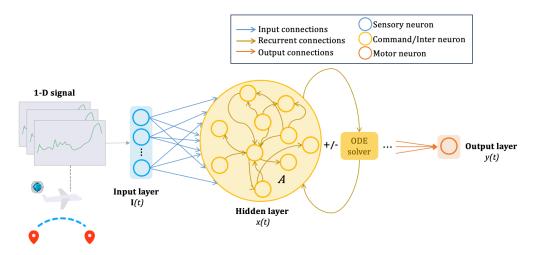


Figure 1: The architecture for the Liquid Time-Constant Network comprises the input, perception layer, a liquid layer (i.e., a time-continuous gating mechanism), and an output layer. Here, I(t) is the real input signal, and y(t) is the predicted, filtered signal.

meters ( $\sim 23$  feet), 95% of the time, anywhere on or near the Earth's surface [7]. However, GPS signals are increasingly unreliable due to their dependence on a network of vulnerable satellites. Additionally, GPS signals are prone to initialization delays and dropouts. MagNav signals, in contrast, constantly emit from the invisible Earth's geomagnetic field, are well-defined, and are mappable.

However, there are differences in MagNav estimation accuracies, which can be attributed to the altitude flown, map quality, and calibration of the platform's magnetic field. Additionally, magnetic measurements derived from scalar and vector magnetometers (magnetic sensors affixed to the aircraft) depend on a nonlinear combination of the Earth's magnetic field and the aircraft's magnetic field, which can cause a navigation estimate that drifts over time due to corrupted magnetic fields (namely, the permanent field, the induced field, and the eddy-current field, as defined by Tolles and Lawson [8]). Furthermore, time-varying magnetic fields from sources like electronic equipment, communication systems, and temperature-dependent magnetic properties of sensors cause deterministic and stochastic effects that violate static assumptions of the classical Tolles—Lawson (T-L) error sources used for predicting aircraft magnetic interference [9]. For a real-time application, a model continuously estimates and eliminates the unknown T-L coefficients of the corrupted magnetic fields.

In this work, we aim to reduce contamination fields and improve calibration accuracy through aeromagnetic compensation, i.e., eliminating interference related to the aircraft's magnetic field from the total magnetometer output signal to improve magnetometer measurement harmonization to a magnetic anomaly map. Traditional state space estimation models, like Kalman filters, have previously been applied to resolve this but are limited in handling the nonlinear nature of the underlying dynamical system and are highly sensitive to perturbations [3, 10–12]. Neural networks have also been used to improve the calibration of aeromagnetic compensation [13–17], but are typically traditional models that fail to leverage inherent physical laws of the system, are computationally expensive, and are not robust to high-dimensional, time-series data. We propose a two-step machine learning framework that: (1) uses a physics-informed neural network, a Liquid Time-Constant network, to capture complex, nonlinear dynamics of airborne MagNav and to detect the weak magnetic anomaly signal from a noisy environment; (2) derives the coefficients of known magnetic effects from the airplane that can be used to update a T-L model and improve calibration accuracy.

# 2 Methodology

#### 2.1 Liquid Time-Constant Networks

Liquid Time-Constant (LTC) networks are a promising variant of recurrent neural networks (RNNs) designed to capture nonlinear patterns of high-dimensional, sequential tasks [18]. While standard, discrete RNNs approximate continuous dynamics step-by-step via dependencies on the history of

their hidden states, LTCs approximate continuous dynamics using ordinary differential equations (ODEs) [19] with more elaborate temporal steps. Additionally, their timing behavior is adaptive to the input (how fast or slow they respond to some stimulus can depend on the specific input). These ODE-based neural networks, however, are slower in training and inference due to using advanced solvers. This lag intensifies with increasing data complexity, especially for tasks like autonomous driving, financial time series, and physics simulations. In this work, we leverage an LTC model enhanced by a closed-form continuous-depth solution (CfC) [20] that combines the rich modeling capabilities of ODE-based models without needing a solver, resulting in significantly faster training and inference speeds. This model has been applied to various sequence modeling problems like robot and drone navigation [21, 22], vision-based autonomous driving [20, 21], and forecasting sea ice concentration [23] and cardiac abnormality detection [24]. Given a 1-D, time-series input signal with m-features,  $\mathbf{I}(t)^{m\times 1}$ , at time-step t, a hidden state vector with D hidden units,  $\mathbf{x}^{(D\times 1)}(t)$ , and a time-constant parameter vector,  $w_{\tau}^{(D)}$ , the hidden state of an LTC network is determined by the solution to the following problem (see Fig. 1):

$$\frac{d\mathbf{x}}{dt} = w_{\tau} + f(\mathbf{x}, \mathbf{I}, \theta)\mathbf{x}(t) + Af(\mathbf{x}, \mathbf{I}, \theta)$$
(1)

where A is a bias vector, and f is a neural network parametrized by  $\theta$ .

#### 2.2 Neural Circuit Policies (NCPs)

A Neural Circuit Policy network [25] is a sparse recurrent neural network modeled after nervous system of the C. elegans nematode [26]. It has four recurrent connection types: sensory, inter-neurons, command, and motor neurons. Sensory neurons receive environmental observations (input, x), which are forwarded to inter-neurons. Command neurons, linked to inter-neurons, handle decision-making. Motor neurons, connected to command neurons, manage actuation (output, y). Synapses can be excitatory or inhibitory and affect neuron activation. Unlike traditional neural networks, each neuron's dynamics are governed by an ODE, which allows for complex dynamics. We train these networks using NCP wirings and the Proximal Policy Optimization (PPO) method [27].

## 2.3 Closed-form Continuous-time (CfC) Neural Networks

A CfC network is a recurrent neural network that resolves a bottleneck requiring a numerical ODE solver by approximating the closed-form solution of the differential equation. Accordingly, CfCs deliver higher efficiency and achieve adaptive, causal, and continuous-time attributes with faster training and inference time. The hidden state of the CfC model can be explicitly written as:

$$\mathbf{x}(t) = \underbrace{\sigma(-f(\mathbf{x}, \mathbf{I}; \theta_f)\mathbf{t})}_{\text{time-continuous gating}} \odot g(\mathbf{x}, \mathbf{I}; \theta_g) + \underbrace{\left[1 - \sigma(-[f(\mathbf{x}, \mathbf{I}; \theta_f)]\mathbf{t})\right]}_{\text{time-continuous gating}} \odot h(\mathbf{x}, \mathbf{I}; \theta_h)$$

$$(2)$$

where f, g, and h are NCP network heads and  $\odot$  is the Hadamard (element-wise) product. For time-variant datasets, t is set based on its timestamp or order, while for sequential applications where sample timing is irrelevant, t is sampled uniformly between two hyperparameters.

#### 2.4 Dataset & Pre-processing

We use the United States Air Force (USAF)-MIT Signal Enhancement for Magnetic Navigation Challenge dataset [28], which aims to identify optimal aeromagnetic compensation for airborne MagNav. This dataset includes time series from six flights and captures magnetic field data from five scalar and three vector magnetometers positioned differently within the aircraft (see Fig. 2b). Each flight has 65 features, with some segments having INS, avionics, electrical, and radar readings. Post T-L calibration, the scalar magnetometer at the aircraft's tail stinger, Mag 1, serves as our ground truth target signal,  $\hat{y}$ . Signals are sampled at 10 Hz. We apply T-L compensation to magnetometer data, subtract the International Geomagnetic Reference Field to degrade variations caused by the Earth's core field, and correct for diurnal effects.

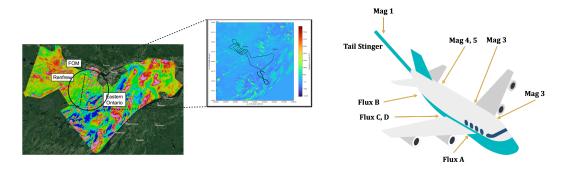


Figure 2: a) Flight trajectory on the magnetic anomaly of Renfrew, Canada, and Ontario, Canada, at 300m above the WGS84 ellipsoid (flight 1007). b) Locations of magnetometers positioned around the MagNav Challenge aircraft.

#### 2.5 Feature Selection

We standardize all features using *z*-score normalization to have zero mean and unit standard deviation. To gather more information from magnetometer measurements, we residualize magnetometers within the aircraft against the magnetometer outside the aircraft (Mag 1). To reduce overfitting and enhance the interpretability of salient features towards model performance, we apply three feature selection techniques: Spearman correlation [29], LASSO regularization [30], and XGBoost [31], to subselect the most important features from the dataset. Accordingly, we select the following features: magnetometer 4 & 5 measurements, aircraft positioning and orientation, INS velocities, altitude, and several electrical measurements (V\_BAT1, V\_BAT2, CUR\_ACLo, CUR\_FLAP, CUR\_TANK, CUR\_IHTR).

#### 2.6 Experiment Setup

We treat each flight as a sample to prevent overfitting due to looping flight segments within the same flight. We apply K-fold cross-validation [32] for resampling. We train all models on an NVIDIA Tesla T4 GPU using Python 3.10. We use PyTorch [33] to build the LTC module and conduct hyperparameter search, architecture search, and tuning using Optuna [34]. We use an LTC and CfC cell with NCP wirings (AutoNCP), 64 inter and command neurons, and one output neuron for each trial. We optimize the model using Adam (lr=1e-3), mean squared error (MSE) loss, and a dropout of 50%. We train for 300 epochs with a batch size of 64 samples. We use the Root Mean Square Error (RMSE) to measure model performance:

RMSE = 
$$\sqrt{\frac{1}{N} \sum_{i=1}^{N} (y_i - \hat{y}_i)^2}$$
 (3)

where  $y_i$  and  $\hat{y}_i$  are the truth and predicted signals, respectively.

# 3 Results

We conducted experiments on the Liquid Time-Constant (LTC) and Liquid Time-Constant-Closed-form Continuous model (LTC-CfC). We compared LTC models against three baseline models: Multi Perceptron (MLP), Convolutional Neural Network (CNN), and Long Short-Term Memory (LSTM) Network. We also compared the performance of our proposed approach against the T-L state estimation method for classical aerocompensation calibration.

As shown in Table 1, the LTC models show a significant increase in performance compared to standard non-ODE-based neural networks. The standard LTC demonstrates up to 58% deduction in compensation error [RMSE], and the LTC-CfC similarly shows a 64% reduction in compensation error compared to the T-L model, averaged across both test flights. Our method successfully detects weak anomaly fields with a significant accuracy threshold (see Fig. 3).

Model	Flt1003 [nT]	Flt1007 [nT]
T-L	58.85	45.13
LSTM	41.79	42.18
MLP	30.47	26.23
CNN	26.05	30.56
LTC	20.31	22.89
LTC-CfC	18.20	19.14

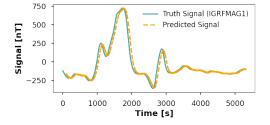


Table 1: Model comparison of aerocompensation calibration error (RMSE nT) for flights 1003 and 1007.

Figure 3: Truth signal (IGRF-corrected Mag 1) vs. predicted signal [nT] for a portion of flight 1007

#### 4 Conclusion

This paper presents a novel, physics-informed model that leverages nonlinear dynamics in airborne MagNav systems to enhance the calibration of aeromagnetic compensation. The pipeline consists of magnetic effects corrections, Liquid Time-Constant Networks enabled with ODE-solvers or closed-form solvers, and learned coefficients for updating state estimation models for real-time use. By incorporating physics-informed learning, our approach effectively separates weak magnetic anomaly fields from disruptive aircraft magnetic noise, enabling accurate navigation for airborne MagNav. Our experimental results outperform traditional state estimation techniques. We plan on leveraging additional physics-based features learned during training and conducting external validation on new datasets. We hope to see this work applied to real-time aircraft navigation systems in the future.

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