

OPEN Fast, vacancy-free climb of prismatic dislocation loops in bcc metals

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Vacancy-mediated climb models cannot account for the fast, direct coalescence of dislocation loops seen experimentally. An alternative mechanism, self climb, allows prismatic dislocation loops to move away from their glide surface via pipe diffusion around the loop perimeter, independent of any vacancy atmosphere. Despite the known importance of self climb, theoretical models require a typically unknown activation energy, hindering implementation in materials modeling. Here, extensive molecular statics calculations of pipe diffusion processes around irregular prismatic loops are used to map the energy landscape for self climb in iron and tungsten, finding a simple, material independent energy model after normalizing by the vacancy migration barrier. Kinetic Monte Carlo simulations yield a self climb activation energy of 2 (2.5) times the vacancy migration barrier for $1/2\langle 111 \rangle$ ($\langle 100 \rangle$) dislocation loops. Dislocation dynamics simulations allowing self climb and glide show quantitative agreement with transmission electron microscopy observations of climbing prismatic loops in iron and tungsten, confirming that this novel form of vacancy-free climb is many orders of magnitude faster than what is predicted by traditional climb models. Self climb significantly influences the coarsening rate of defect networks, with important implications for post-irradiation annealing.

Dislocation glide dominates plastic flow at low homologous temperatures, but confinement to a glide surface significantly restricts the evolution of a defect network¹. Dislocation climb, which requires concurrent mass transport, is typically much slower than glide but allows migration off the glide surface, giving rise to a wide range of important plasticity mechanisms including network coarsening^{2,3} and creep⁴. Climb is known^{5–9} to be particularly important in post-irradiation annealing, accelerating the coalescence of the many small self interstitial atom (SIA) and vacancy clusters produced in a cascade event, increasing the characteristic length scale of the dislocation network and transforming the mechanical response.

The most widely studied atomic mechanism for climb transports mass through a pre-existing vacancy atmosphere, here referred to as vacancy mediated climb (VMC), with dislocations acting as perfect sources and sinks for vacancies^{2–4}. By emitting and absorbing vacancies, dislocation segments can move off their glide plane; as the self stress of a dislocation loop is approximately proportional to the inverse of the loop radius¹, larger loops tend to grow at the expense of smaller loops whilst maintaining the equilibrium vacancy concentration, a feature that is clearly observed in some experiments7. As the vacancy current at a dislocation is proportional to the product of the vacancy concentration and diffusivity $c_V D_V \sim \exp(-\beta (E_f^V + E_m^V))$, the rate of VMC is controlled by the large activation energy $E_f^V + E_m^V$ for vacancy formation and migration³, meaning VMC mechanisms are only expected to be active at high homologous temperatures⁴.

However, it has long been recognized^{5–7,9,10} that prismatic loops can also migrate away from their glide cylin-

der, with no observable change in size, driving loop coalescence. The climb motion in this case is clearly not VMCas the loop area is conserved; furthermore, we confirm previous findings^{5,9,11} that the climb velocities are many orders of magnitude larger than velocities predicted by VMC models and active at much lower temperatures. An alternative 'self climb' model was proposed to account for these puzzling observations 5,10,12-14, where loops are able to migrate in their habit plane due to the diffusion of self interstitial atoms (SIA) around the loop perimeter,

¹CCFE, Culham Science Centre, Abingdon, Oxon, OX14 3DB, UK. ²Department of Materials Science, Faculty of Science and Engineering, Shimane University, 1060 Nishikawatsu, Matsue 690-8504, Japan. ³Research Center for Ultra-High Voltage Electron Microscopy, Osaka University, 7-1 Mihogaoka, Ibaraki, Osaka 567-0047, Japan. ⁴Institute of Multidisciplinary Research for Advanced Materials, Tohoku University, 2-2-1 Katahira, Aoba-ku, Sendai 980-8577, Japan. Correspondence and requests for materials should be addressed to T.D.S. (email: thomas.swinburne@ukaea.uk) in close analogy to the diffusion mechanism of large adatom islands 15 . Theoretical analyses $^{5,12-14}$ (see below) of self climb found a mobility law of

$$M_{\rm SC} = \frac{2\beta\nu a^5}{\pi R^3} e^{-\beta E_{\rm SC}},\tag{1}$$

where R is the loop radius, a is the lattice parameter, $\beta=1/k_{\rm B}T$, ν is an attempt frequency and $E_{\rm SC}$ is a characteristic activation energy. As no vacancy atmosphere is required, self climb is suspected to be much faster than VMC as a factor $c_{\rm V}=\exp(-\beta E_{\rm f}^V)$ is absent, but this cannot be confirmed without a quantitative calculation of $E_{\rm SC}$, the critical, rate controlling parameter in (1). In this paper, we use the results of over a hundred molecular statics barrier climbing calculations and kinetic Monte Carlo (KMC) simulations to explore the energy landscape for pipe diffusion around SIA loops. The pipe diffusion process in self climb effectively enables non-glide structural fluctuations of the loop, which enables thermally activated diffusive climb motion, with a characteristic activation energy $E_{\rm SC}$. Our main result is that the activation energy for self climb is given by

$$E_{SC} = \epsilon E_m^V, \tag{2}$$

where E_m^V is the *vacancy* migration barrier and $\epsilon=2$ or 2.5 for $\langle 111 \rangle$ or $\langle 100 \rangle$ loops. To complete the (1), ν is taken as the attempt frequency for vacancy diffusion 16,17 . We find that the self climb activation energy $E_{SC}=(2,2.5)E_m^V$ is much lower than the effective activation energy of $E_f^V+E_m^V\sim (3-5)E_m^V$ for VMC in bcc metals 18 , resulting in much larger self climb velocities. In fcc metals $E_f^V+E_m^V\sim (2-3)E_m^{V19}$, implying that self climb and VMC velocities may be of comparable magnitudes, a question we leave for a future investigation. Our observed activation energy is consistent with experimental estimates of E_{SC} that find $E_{SC}\sim (0.4-0.7)$ E_{f+Em} over a wide range of materials $^{5,12-14}$.

The fully parametrized mobility law is tested against direct *in situ* transmission electron microscopy (TEM) observations of SIA loops in iron at 500 °C, where isolated SIA loops are seen to execute unbiased self climb diffusion perpendicular to their Burgers vector, whilst adjacent SIA loops directly coalesce through self climb, driven by elastic interaction forces. We also analyze recently published observations of SIA loop coalescence in tungsten⁹. In all cases, we find the climb diffusivities and coalescence times measured experimentally are around six orders of magnitude faster than those predicted by the existing VMC models but in very good agreement with dislocation dynamics simulations that allow self climb and glide. The influence of self climb in bcc metals is further demonstrated through simulations of prismatic loop coarsening, which we compare to an analytical model for coarsening rates found from VMC simulations³.

Results

Energy landscape for pipe diffusion in SIA loops. As self climb is driven by pipe diffusion around the perimeter of SIA loops, we have simulated a large number (>100) of possible diffusion pathways for $1/2\langle111\rangle$ and $\langle100\rangle$ SIA loops in iron and tungsten (see methods). It was found that all relaxed pathways between metastable states could be approximated as $a/2\langle111\rangle$ jumps for $1/2\langle111\rangle$ loops, and $a/2\langle111\rangle$ or $a\langle100\rangle$ jumps for $\langle100\rangle$ loops. As shown in Fig. 1, after normalizing by the vacancy migration energy E_m^V for the interatomic potential, we find that the total change in energy ΔE and migration barrier E_m for a jumping atom can be accurately modeled simply by counting the number c of nearest SIA neighbors along the path, i.e. for each point on the path, $c = \sum_{j \neq i} \Theta(\sqrt{3} a/2 - |\mathbf{x}_i - \mathbf{x}_j|)$, where $\Theta(x)$ is the Heaviside step function. For SIAs in the interior of an $1/2\langle111\rangle$ loops c = 6, whilst for $\langle100\rangle$ loops c = 4; classifying the SIAs on a loop perimeter in this manner allowed us to produce the distribution of migration pathways shown in Fig. 1a,b,f,g. Collating the results of our NEB calculations revealed the approximate relationship

$$\Delta E \simeq \Delta c E_m^V, \quad E_m \simeq (\Delta c + \sigma) E_m^V,$$
 (3)

where Δc is the change in c between the initial and final configuration, $\sigma=1$ for jumps along $a/2\langle111\rangle$ (c.f. Fig. 1c,i) and $\sigma=2$ for jumps along $a/2\langle100\rangle$ (c.f. Fig. 1g). The remarkably simple relationship (3) can be rationalized by noting that the 'hopping' of a single SIA is akin to the vacancy migration process; in a first approximation, vacancy migration in the bulk is a hop of single atom, which requires 'breaking' a single nearest neighbors bond. A SIA on the perimeter of a prismatic loop has c additional bonds compared to an atom in the bulk, of which it must 'break' but one in order to jump along $a/2\langle111\rangle$ and two to jump along $a\langle100\rangle$, in close analogy to the vacancy migration mechanism. In contrast, the SIA migration barrier is typically much lower than E_m^V in bcc metals¹⁸ due to the extended strain field of SIA defects, meaning that no 'hopping' occurs under SIA migration²⁰. Generally, variations in the observed total energy change ΔE and migration barrier E_m were not observed to be greater than 15% from those predicted by (3), which typically overestimates E_m , meaning (3) will give an lower bound on the self climb mobility.

As self climb is known to play an important role in prismatic loop coalescence, we also determined the effect of a nearby loop's elastic field on the observed energy barriers by performing the same NEB calculations in the presence of another prismatic loop, rotating/inverting the loop of interest by a bcc symmetry operation (in O_h) to vary the elastic environment of the jumping atom. For loop separations of more than ~5a we found variations in the energy barrier of less than 5%. As such close proximity was needed to produce observable changes we expect the self-climb energy landscape to be essentially unaffected by any surrounding defect network, even line dislocations which are not elastically neutral. The goal of the NEB calculations is to parametrize KMC simulations; an alternative approach to the simple model (3) used here would be to correlate all observed migration pathways for a given material with some detailed structural signature for the jumping atom involving second and third nearest

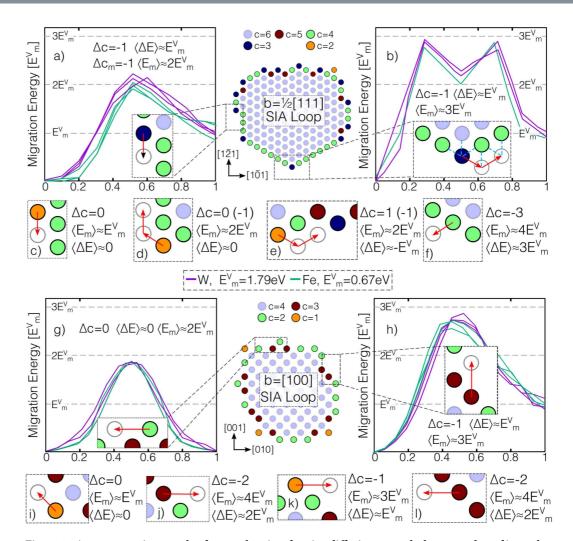


Figure 1. A representative sample of energy barriers for pipe diffusion around a large number of irregular 1/2(111) and (100) prismatic loops in iron and tungsten, two of which are shown. Defining a 'bond' as a nearest SIA neighbor, we find a clear correlation between the bond number and the expected migration barrier and total energy change, which can account for all observed pathways when normalized by the vacancy migration barrier (see main text for details).

neighbors, which could then be used to construct a large table of transition rates for use in KMC²¹. However, we believe our simple bond counting model (3), tested in iron and tungsten, provides a high degree of quantitative accuracy (given the expected tolerances of the interatomic potential) coupled with an attractive simplicity, resulting in a universal model for self climb in bcc metals and allowing the treatment of large, experimentally observable SIA loops.

Self climb mobility. As the presence of a realistic external stress field (due to a nearby dislocation loop) was found to have only a weak influence over the measured pipe diffusion migration barriers, we can calculate the self climb velocity $\mathbf{v}_{\rm cl}$ under a climb force $\mathbf{F}_{\rm cl}$ in the linear response regime $\mathbf{v}_{\rm cl} = M_{\rm SC}\mathbf{F}_{\rm cl}$, where the self climb mobility is given by the Einstein relation $M_{\rm SC} = \beta D_{\rm SC}$. We therefore only need to calculate the self climb diffusivity $D_{\rm SC}$ of an isolated loop under no applied stress, obviating the need to include computationally demanding long range elastic interactions in KMC²². In the presence of multiple migration pathways, the effective activation energy $E_{\rm SC}$ will reflect the rate limiting process for loop migration¹⁵; as shown in Fig. 2, our KMC simulations reveal (see methods) an effective activation energy $E_{\rm SC} = (2.0 \pm 0.07) E_{\rm M}^V$ for $1/2\langle 111\rangle$ SIA loops and $1/2\langle 111\rangle$ SIA loops, comparable to the energy barrier required for a lone SIA to traverse a corner or step on the loop perimeter (c.f. Fig. 1d,k). The larger activation energy for $1/2\langle 111\rangle$ self climb can be attributed to the larger energy barrier for SIA migration along $1/2\langle 111\rangle$ directions. We note that in both cases the self-climb activation energy is much lower than that required for the 'nucleation' of lone SIAs from flat low index directions ($1/2\langle 111\rangle$ for both SIA loops, c.f. Fig. 1f,l). Simulations where such nucleation processes are explicitly forbidden exhibit unchanged diffusivities, confirming that migrating SIAs are produced around corners or roughened structures on the loop perimeter, emphasizing the importance of considering 'non-perfect' defect structures when modeling self climb. We note that these imperfect defect structures could also be created through VMC. To derive an analytical expression for the self

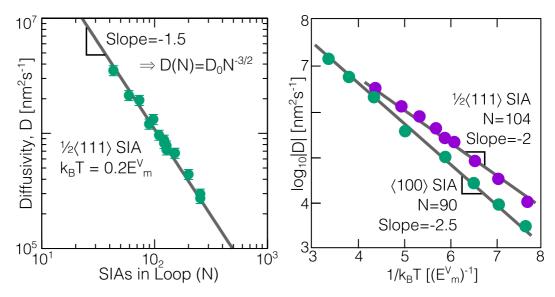


Figure 2. Results from KMC simulations of SIA loop self climb. Left: log-log plot showing the $D_{\rm SC} \propto N^{-3/2}$ relationship predicted by (4). Right: Arrhenius plots for $1/2\langle 111\rangle$ and $\langle 100\rangle$ SIA loops, giving clear activation energies of $2.0E_m^V$ and $2.5E_m^V$.

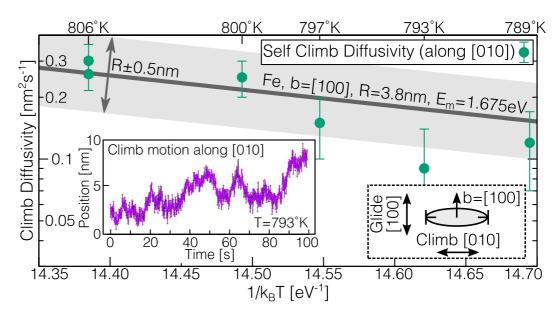


Figure 3. Self climb diffusivity of an $\langle 100 \rangle$ SIA loop in Fe. The trajectory (observed as a projection on (001) (inset) clearly shows a climb component along [010], perpendicular to the Burgers vector b = a[100]. The predicted self climb diffusivity (4), with vacancy attempt frequency taken from DFT calculations ¹⁶ shows good agreement.

climb diffusivity D_{SC} , consider an isolated loop of N SIAs with an approximately circular shape, such that $N \simeq \pi R^2/a^2$. The center of mass diffusivity is given by $D_{\text{SC}} = \sum_{ij} D_{ij} I N^2$, where $D_{ij} = \lim_{t \to \infty} \langle \Delta x_i \Delta x_j \rangle / 2t$. As only $N_p \simeq 2\pi R/a$ SIAs on the perimeter are able to move $(D_{ij} \neq 0)$, under the assumption of uncorrelated perimeter atoms we obtain

$$D_{SC} = \frac{N_p}{N^2} D_p = \frac{2a^5}{\pi R^3} \nu \exp(\beta E_{SC}),$$
 (4)

which with the Einstein relation $M_{\rm SC}=\beta D_{\rm SC}$ gives equation (1) for the self climb mobility. The predicted relationship $D_{\rm SC}\propto R^{-3}\sim N^{-3/2}$ is in agreement with our simulations (Fig. 2) and similar analysis of perimeter diffusion controlled transport of adatom islands^{15,23}.

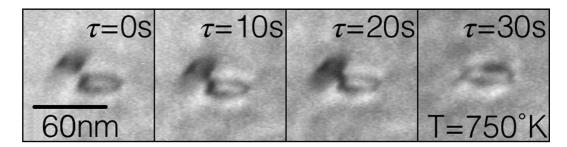


Figure 4. TEM observation of two $1/2\langle 111 \rangle$ prismatic loops in iron at 750 K, coalescing over a time period of 30 s. This processes corresponds to the first entry in Table 1.

	R ₁ [nm]	$R_2[\mathbf{nm}]$	d[nm]	T[K]	$ au_{\mathrm{exp}}[\mathbf{s}]$	$ au_{\mathrm{SC}}[\mathbf{s}]$	$ au_{ m VMC}[{ m s}]$
Fe	20	12	30	750	30.0	7.5	3.3×10^{7}
Fe	3.5	3.5	7	660	~0.8	1.8	2.7×10^{7}
Fe§	~5.	~5.	~10.	725	~6.	2.1	2.7×10^{7}
W [†]	20	20	100	1173	66.5	96.2	2.6×10^{7}
W [†]	100	500*	100	1273	7.	8.6	1.5×10^{5}

Table 1. Comparison of coalescence times of $1/2\langle 111\rangle$ SIA loops from TEM observations ($\tau_{\rm ex}$), DD simulations where loops can glide and self climb ($\tau_{\rm sc}$) and DD simulations where loops can glide and climb via VMC³ ($\tau_{\rm VMC}$). The self climb model is many orders of magnitude faster than VMC and retains accuracy over a wide range of loop sizes. Above: TEM observation of SIA loops in iron at 750 K, corresponding to the first entry in the above table. §Data taken from Dudarev et al.²⁴. †Data taken from Ferroni et al.⁴. *Pill shaped loop, length of ~50 nm, width ~20 nm.

Comparison to TEM observations of self climb. To validate our self-climb mobility (1) and diffusivity (4), transmission electron microscopy (TEM) was used to observe the dynamics of both isolated and interacting SIA loops in ultra-high purity α -Fe (RRR: 7900) and high-purity α -Fe (RRR: 2000, purity: 99.998 wt.%), respectively. An isolated b=a[100] SIA loop of radius $R\simeq 3.8\pm 0.3$ nm was observed freely diffusing both along and perpendicular to its Burgers vector of [100]. We identify the perpendicular motion along [010] as a one dimensional projection of self climb in (100) planes. Through analysis of the mean squared displacement along [010] (Fig. 3, inset) self climb diffusivities were extracted at five temperatures, from 793 K to 806 K, well below temperatures where vacancy-mediated climb is expected to be active. Figure 3 shows that equation (4), with parameters for a $\langle 100 \rangle$ SIA loop of radius 3.8 nm in iron, shows excellent agreement with the experimentally determined climb diffusivity, agreeing to within 10% apart from the measurement at 793 K. As a further validation of our model we implemented the self climb mobility law (1) in simple dislocation dynamics (DD) simulations that allow glide and self climb along with isotropic elastic interactions (see methods), in order to simulate a variety of loop coalescence processes seen under the TEM. A representative observation is show in Fig. 4. For comparison, we also replaced the self-climb mobility $M_{\rm scl}$ law by an approximate VMC mobility (Equation 10 in ref. 3)

$$M_{\text{VMC}} = \frac{2\pi\beta\nu e^{-\beta(E_{m}^{V} + E_{f}^{V})}}{b^{2} \ln(R/b)},$$
(5)

to give a measure of the expected coalescence times if VMC was the only active climb mechanism. Using the full-field elastic interaction energy given by Mura's formula¹, we investigated the various binary loop coalescence processes that were seen in our experiments and similar observations from other TEM studies in iron²⁴ and tungsten⁹. The DD simulations did not account for the presence of a free surface nor the surrounding defect network, but the shape and position of two loops, which were either circular or pill shaped (semicircles connected by two straight lines), were chosen to approximate as closely as possible those seen under the TEM. The results of these simulations are given in Table 1; despite the approximate treatment of our simulations, the calculated coalescence times are in fairly good agreement with experimental values for both iron and tungsten, whilst simulations with the VMC mobility (5) overestimate the observed coalescence times by around six orders of magnitude, highlighting both the quality of agreement with experiment and the speed of self climb compared to VMC. We emphasize that the observed non-glide motion therefore can only be accounted for by the self climb mechanisms investigated here. To further explore the influence of self climb in post-irradiation annealing, we performed similar glide/self climb DD simulations of SIA loop coarsening (see methods), using an approximate far field solution for the loop interaction, which we compare to an analytical model⁷ that has been shown to be in very good agreement with VMC-only enabled DD simulations of loop coarsening³. We used simulation parameters appropriate for 1/2(111) SIA loops in iron at 750 K in a simulation supercell of $200 \times 200 \times 200$ nm. An initial population of 80 loops were placed randomly in the supercell, with random radii between 1.5 nm and 3.5 nm, under the constraint that the initial average radius $\langle R(0) \rangle = 2.5$ nm. An ensemble of 150 simulations were performed until less than 4 loops remained in the supercell, though the ensemble average behavior could be considered converged after approximately 50

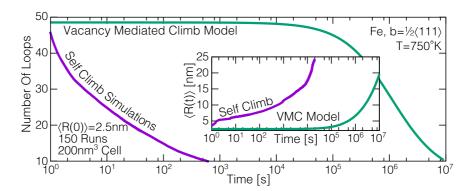


Figure 5. Self climb enabled dislocation dynamics simulations of SIA loop coarsening, using parameters appropriate for iron at 750 K. Our results are compared to an analytical model of VMC loop coarsening, which is in very good agreement with VMC enabled DD simulations³. We see that self climb coarsening rates are three to four orders of magnitude greater than those predicted by VMC.

simulations. In Fig. 5 we plot the ensemble average time evolution of the loop number N(t) and average loop radius $\langle R(t) \rangle$, along with the predictions of the analytical VMC model, $N(t) = \frac{N(0)}{1+\alpha t}$ and $\langle R(t) \rangle = \langle R(0) \rangle \sqrt{1+\alpha t}$, where $\alpha = \mu a^5 \beta \nu \exp(-\beta [E_m^V + E_f^V])/\langle R(0) \rangle^{23}$. It is clear that the self climb coarsening rates are around three to four orders of magnitude faster than those predicted by VMC, emphasizing the necessity of including the self climb mobility law (1) into simulations of post-irradiation annealing.

Discussion

We have derived and calculated a quantitative mobility law for self climb, by mapping out the energy landscape for pipe diffusion around a large number of randomly shaped prismatic dislocation loops in two different bcc metals which can then be explored in kinetic Monte Carlo simulations. Our results show that the activation energy for self climb is 2–2.5 times the vacancy migration barrier, which showed quantitative agreement with experimental observations of the same processes. Dislocation dynamics simulations, which account for self climb, show significantly accelerated prismatic loop coalescence rates at intermediate homologous temperatures, demonstrating that self climb is an essential component in models of microstructural evolution, even in regimes where vacancy-mediated climb can be neglected. Finally, we note that self climb activation energy $E_{\rm SC}$ is comparable to the inferred binding energy between dislocation loops and common impurities such as carbon or nitrogen (found experimentally as 1.2 eV for $1/2\langle111\rangle$ prismatic loops in iron²⁵ compared to $E_{\rm SC}=1.34\,{\rm eV}$), meaning that simulations which include impurity pinning effects should also account for self climb, as the timescales for the two processes are expected to be comparable. It is also possible that self climb could play a role in defect depinning process, a topic we leave for future study.

Methods

Atomistic calculations. The pipe diffusion barrier calculations used the LAMMPS molecular simulation package²⁶ with empirical potentials for iron by Gordon *et al.*²⁷ and for tungsten by Marinica *et al.*²⁸. Dislocation loops were created by inserting a random palette of SIAs on (111) or (100) planes into a perfect lattice before a structural relaxation. Away from a so called 'magic' number of SIAs, loops cannot form perfect hexagons or squares, resulting in a geometrically necessary roughening of the loop perimeter. Possible migration pathways were investigated by selecting at random SIAs on the perimeter of a palette, then translating the selected SIA by an $a/2\langle111\rangle$, $a\langle100\rangle$ or $a\langle1\bar{1}0\rangle$ lattice vector to another perimeter position before a further relaxation. As the SIA atoms are already in off-lattice positions, a lattice vector translation also finds an off lattice position. The nudged elastic band method²⁹ was then used to calculate the energy barrier between the two configurations, taking caution to choose an indexing protocol that minimizes the converged energy barrier, overcoming any ambiguity over identification of 'the' SIA atom in the relaxed structure of a dislocation core.

Kinetic Monte Carlo Simulations. We used the lattice KMC code KMCLIB²¹ to simulate two dimensional self climb diffusion with state-state energy differences and migration barriers determined by (3), using energy units such that $E_m^V = 1$, with a hexagonal or square lattice for $1/2\langle 111 \rangle$ or $\langle 100 \rangle$ loops. The simulations produce a set $\{t_n, \overline{x}_n\}$ of center of mass positions $\overline{x} = \sum_i x_i I N$. By taking the mean squared displacement at sequentially greater time delays a diffusivity was extracted using established methods³⁰.

Transmission Electron Microscopy Experiments. Thin foils with thickness less than 0.08 mm were pre-annealed at 773 K for 0.5 hours under a vacuum of 3×10^{-6} Pa (ultra-high purity α -Fe) and at 1073 K for 2 hours under a hydrogen atmosphere at 1 atm (high purity α -Fe) to reduce dislocation density and remove any residual stress before electro-polishing. In the TEM-visible regions, the residual-dislocation density was less than 10^9 m⁻², allowing the observation of individual loops with negligible effect from the stress field of residual dislocations. Loops were introduced through high-energy electron irradiation, using an ultra-high voltage TEM H-3000 by Hitachi, operated at an acceleration voltage of 2000 kV. The irradiation was performed with a beam

dose of $1 \times 10^{25} \, e/m^2$ at 290 K (ultra-high purity α -Fe) and $1 \times 10^{25} \, e/m^2$ at 150 K (high purity α -Fe), producing SIAs that agglomerated to form loops. Behavior of SIA loops in response to specimen heating were observed using a diffraction-contrast technique at an acceleration voltage of 200 kV to avoid additional knock-on displacement, recording at a frame rate of $30 \, s^{-1}$ with a Gatan 676 camera.

Dislocation Dynamics simulations. In our DD simulations, prismatic dislocation loops were allowed to glide along the direction of their Burgers vector \mathbf{b} and climb in two dimensions perpendicular to their Burgers vector. The shape of the dislocation loop was fixed to be constant throughout, allowing the total elastic energy of the system E_{elastic} , to be a function purely of the N loop positions $(\mathbf{x}_1, \mathbf{x}_2, \dots \mathbf{x}_N)$. In all our simulations the loops were assumed to have identical Burgers vectors $\mathbf{b}_i = \mathbf{b}$. The equation of motion for an individual loop i therefore read

$$\mathbf{v}_{i} = -(M_{\mathrm{scl}}(\mathbb{I} - \hat{\mathbf{b}} \otimes \hat{\mathbf{b}}) + M_{\mathrm{gl}}\hat{\mathbf{b}}) \cdot \nabla_{i} E_{\mathrm{elastic}}, \tag{6}$$

where $M_{\rm gl}$ is a glide mobility suitable for prismatic dislocation loops at high temperature^{31–33} and $M_{\rm scl}$ is the self climb mobility given in equation (1). For comparison, as described in the main text, we also performed identical simulations with $M_{\rm scl}$ replaced by the VMC law (5). As the glide mobility $M_{\rm gl}$ is much greater than the climb mobility $M_{\rm scl}$ we split the integration of (6), first allowing glide-only motion until a local steady state had been

reached, defined as when the total magnitude of the glide force, $\sqrt{\sum_i |\hat{\mathbf{b}} \cdot \nabla_i E_{\mathrm{elastic}}|^2}$, was less than 0.02 eV/Å. At this point loops were allowed to respond to their climb forces; the loop with the largest climb force magnitude $\mathbf{f}_{\mathrm{scl}}^{\mathrm{max}} = |(\mathbb{I} - \hat{\mathbf{b}} \otimes \hat{\mathbf{b}}) \cdot \nabla_i E_{\mathrm{elastic}}|$ was allowed to move a distance $\delta r = 1$ Å in the direction of the climb force, and the simulation time was updated by $\delta t_{\mathrm{scl}} = \delta r / (M_{\mathrm{SC}} f_{\mathrm{scl}}^{\mathrm{max}})$. The remaining loops all migrated in the direction of their climb force a distance $\delta r = \delta t_{\mathrm{scl}} M_{\mathrm{SC}} f_{\mathrm{scl}}^{\mathrm{max}}$.

For the binary loop coalescence simulations the elastic interaction energy was given by Mura's formula (equation 4–40 in ref. 1) for two loops with identical Burgers vectors **b**; the loops under study were either circular or pill shaped (i.e. two semicircles connected by parallel straight lines), and were chosen to approximate as closely as possible the shape and position of the coalescing loops seen under the TEM, though the effect of the free surface and the surrounding defect network is neglected.

For the simulations treating the coarsening of a distribution of dislocation loops, all loops were taken to be collinear and circular, with coalescence occurring instantaneously on contact, whereupon the larger loop was expanded to accommodate the area of the smaller loop. To speed up the simulations we used an analytical far field solution for the loop-loop interaction⁷ for two loops of radii R_1 , R_2 and positions \mathbf{x}_1 , \mathbf{x}_2

$$-\nabla E_{\text{elastic}}^{12} = \frac{\mu b^2 \pi^2 R_0^2 R_1^2}{4\pi (1-\nu) |\mathbf{d}|^4} (g(\theta) \hat{\mathbf{d}} - f(\theta) \hat{\mathbf{b}}), \tag{7}$$

where $\mathbf{d} = \mathbf{x}_1 - \mathbf{x}_2$, $\cos(\theta) = \hat{\mathbf{d}} \cdot \hat{\mathbf{b}}$, $f(\theta) = 3\cos(\theta)(3 - 30\cos^2(\theta) + 35\cos^4(\theta))$ and $g(\theta) = 3\sin(\theta)(1 - 10\cos^2(\theta) - 35\cos^4(\theta))$. As the difference in forces across the loop is greater than that given by the far field approximation, which assumes the loop radius is negligible compared to the loop separation, the true elastic force will be greater than that in our coarsening simulations as the loops approach each other, meaning our results can be considered to provide a lower bound on the coarsening times.

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Author Contributions

T.D.S. and S.L.D. conceived the initial molecular statics simulations. T.D.S. developed the simulation techniques, performed all simulations and the resultant analysis. K.A. conceived the experiments. M.I., K.M. and M.U. produced the high-purity ions for irradiating the samples. K.A., H.M. and H.Y. performed the TEM experiments. T.D.S. wrote the manuscript. All authors reviewed the manuscript.

Additional Information

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