Global Variables

```
In[145]:=
        prec = 100;
       Nmax = 100;
       x = 20.0;
       xmax = 20.0;
        xmin = -20.0;
       xsize = 100;
       dx = (xmax - xmin) / (xsize - 1);
       Xvector = N[Range[xmin, xmax, dx], prec];
                   L. Lintervalo de valores
       Nvector = Range[0, Nmax, 1];
                   intervalo de valores
        Wavefuntion_Wolfram_Mathematica_1
In[154]:=
       \label{lem:wavefunctionMathematical} \mbox{\tt WavefunctionMathematical[n\_, x\_, prec\_] :=} \\
          Module[{nPrec, xPrec, norm, H, wavefunction},
          módulo de código
           SetPrecision[n, prec];
           define precisão
           SetPrecision[x, prec];
           define precisão
           norm = (2^{(-0.5 * n)}) * (Gamma[n+1]^{(-0.5)}) * (Pi^{(-0.25)});
                                       função gama de Euler
                                                                 número pi
           H = HermiteH[n, x];
               polinômios de Hermite
           wavefunction = SetPrecision[norm * Exp[-0.5 * x^2] * H, prec];
                            define precisão
                                                 exponencial
           wavefunction];
```

Wavefuntion_Wolfram_Mathematica_2

```
In[155]:=
       WavefunctionMathematica2[n_, x_, prec_] :=
          Module[{wavefunction, xsize, i}, SetPrecision[x, prec];
          módulo de código
                                              define precisão
           wavefunction = Table[SetPrecision[0, prec], \{n + 1\}, \{Length[x]\}];
                           tabela define precisão
                                                                     comprimento
           wavefunction[1] = SetPrecision[Pi^{(-1/4)} Exp[-(x^2)/2], prec];
                              define precisão _número pi
                                                         exponencial
           wavefunction [ \hbox{\tt $2$} ] = SetPrecision [ \hbox{\tt $(2$} x wavefunction [ \hbox{\tt $1$}]) / Sqrt[2], prec];
                               define precisão
                                                                       raiz quadrada
           For [i = 3, i \le n + 1, i++, wavefunction[i]] = 2 \times (wavefunction[i - 1]] / Sqrt[2(i - 1)]) -
           para cada
                                                                                     raiz quadrada
                Sqrt[(i-2) / (i-1)] wavefunction[[i-2]];];
                raiz quadrada
           wavefunction[n + 1]];
       Wavefuntion_Wolfram_Mathematica_3
In[156]:=
       WavefunctionMathematica3[n_, x_, prec_] :=
          Module[{wavefunction, i}, SetPrecision[x, prec];
          módulo de código
                                       define precisão
           wavefunction = Table[SetPrecision[0, prec], {n + 1}, {Length[x]}];
                           tabela define precisão
           wavefunction[1] = SetPrecision[Pi^{(-1/4)} Exp[-(x^2)/2], prec];
                               define precisão  número pi  exponencial
           For [i = 1, i \le n, i++,
           para cada
            wavefunction[i + 1] =
              SetPrecision[2 x (wavefunction[i] / Sqrt[2 (i)]) -
                                                    raiz quadrada
                Sqrt[(i-1) / i] wavefunction[i-1], prec]];
                raiz quadrada
           wavefunction];
```

Tests

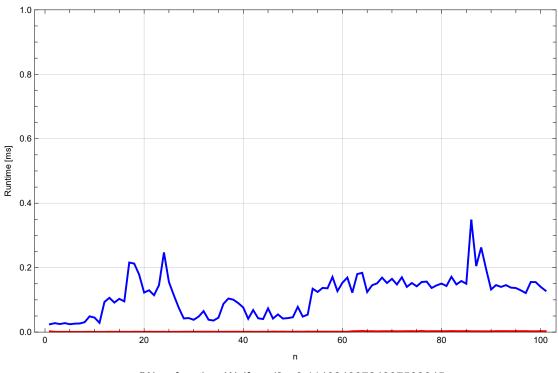
★ Single-Mode and Onedimensional speed test

```
In[157]:=
       (*To use timeit.repeat in the Python is a option too*)
       FastWaveSMODList = Normal[ExternalEvaluate["Python",
                           normal execução externa
            "from fast_wave.wavefunction import wavefunction_smod;import timeit;N_max
              = 100;x = 20.0; [(timeit.timeit(lambda : wavefunction_smod(n,
              x) , number=10000)/10000) *1000 for n in range(N max+1)];"]];
       WavefunctionWolframSMODList = {};
       For [i = 1, i \le (Nmax + 1), i++, AppendTo[WavefunctionWolframSMODList,]
       para cada
           RepeatedTiming[WavefunctionMathematica1[i - 1, x, prec]][1] * 1000];]
           cronometra repetidamente
       ListLinePlot[
       gráfico de linha de uma lista de valores
         {WavefunctionWolframSMODList, FastWaveSMODList},
        PlotStyle → {Blue, Red},
        estilo do gráfico azul
                            vermelho
        Frame → True,
        _quadro _verdadeiro
        FrameLabel → {"n", "Runtime [ms]"},
        legenda do quadro
        PlotLabel →
        etiqueta de gráfico
         Row[{Style["Wavefunction_Wolfram1 vs Wavefunction_Fast-Wave(smod)", Bold, 13],
         linha estilo
                                                                                     negrito
            "\n", Style["x: 20.0, to each value of n \n", 12]}],
                 estilo
        GridLines → Automatic,
        grade de linhas automático
        PlotLegends →
        legenda do gráfico
         Placed[{" avg[Wavefunction_Wolfram1] = " <> ToString[SetPrecision[Mean[
         situado
                                                          converte··· define precisão média
                 WavefunctionWolframSMODList], 20], TraditionalForm] <> " ms;",
                                                      forma tradicional
            " avg[Fast-Wave(smod)] = " <> ToString[
                                             converte em cadeia de caracteres
              SetPrecision[Mean[FastWaveSMODList], 20], TraditionalForm] <> " ms"}, Below],
                                                                                          abaixo
              define precisão média
                                                            forma tradicional
        ImageSize → Large ,
        _tamanho da ··· _grande
        PlotRange → {{Automatic, Automatic}, {0, 1.0}}
        Lintervalo do gráf··· Lautomático Lautomático
       ]
```

Functionality Test Passed: True

Wavefunction_Wolfram1 vs Wavefunction_Fast-Wave(smod)

x: 20.0, to each value of n



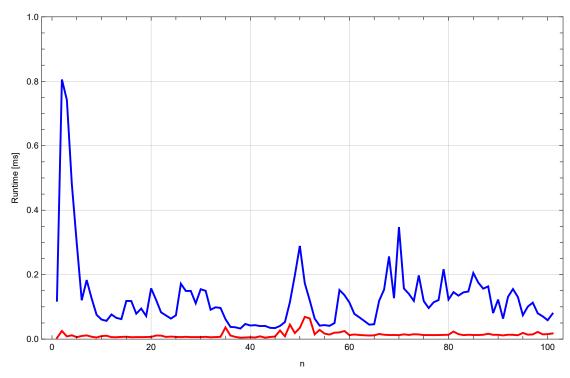
- avg[Wavefunction_Wolfram1] = 0.11408400724807588045 ms;
- avg[Fast-Wave(smod)] = 0.0017626952469846843274 ms

★ Single-Mode and Onedimensional speed test (less_fast)

```
In[@]:= FastWaveSMODList =
                                                       "from fast_wave.wavefunction
        Normal[ExternalEvaluate["Python",
       normal execução externa
             import wavefunction_smod;import timeit;N_max = 100;x =
             20.0;[(timeit.timeit(lambda : wavefunction_smod(n, x, more_fast=False)
                                                                                   falso
             , number=10000) /10000) *1000 for n in range(N_max+1)];"]];
     WavefunctionWolframSMODList = {};
     For [i = 1, i \le (Nmax + 1), i++, AppendTo[WavefunctionWolframSMODList,]
     para cada
         RepeatedTiming[WavefunctionMathematica1[i-1, x, prec]][1] * 1000];]
         cronometra repetidamente
     ListLinePlot[
     gráfico de linha de uma lista de valores
       {WavefunctionWolframSMODList, FastWaveSMODList},
      PlotStyle → {Blue, Red},
      estilo do gráfico azul vermelho
      Frame → True,
      quadro verdadeiro
      FrameLabel → {"n", "Runtime [ms]"},
      legenda do quadro
      PlotLabel →
      Letiqueta de gráfico
        Row[{Style["Wavefunction Wolfram1 vs Wavefunction Fast-Wave(smod; less fast)",
       linha estilo
           Bold, 13], "\n", Style["x: 20.0, to each value of n \n", 12]}],
      GridLines → Automatic,
      grade de linhas automático
      PlotLegends →
      Llegenda do gráfico
        Placed[{" avg[Wavefunction_Wolfram1] = " <> ToString[SetPrecision[Mean[
        situado
                                                        converte··· define precisão média
               WavefunctionWolframSMODList], 20], TraditionalForm] <> " ms;",
                                                    forma tradicional
          " avg[Fast-Wave(smod; less_fast)] = " <> ToString[
                                                       converte em cadeia de caracteres
             SetPrecision[Mean[FastWaveSMODList], 20], TraditionalForm] <> " ms"}, Below],
            define precisão _média
                                                          forma tradicional
                                                                                        abaixo
       ImageSize → Large ,
      tamanho da ··· grande
      PlotRange → {{Automatic, Automatic}, {0, 1.0}}
      intervalo do gráf··· automático automático
     1
     Functionality Test Passed: True
```

Out[0]=

Wavefunction_Wolfram1 vs Wavefunction_Fast-Wave(smod; less_fast) x: 20.0, to each value of n



- avg[Wavefunction_Wolfram1] = 0.12689482548779781879 ms;
- $avg[Fast-Wave(smod; less_fast)] = 0.013502909405886588667 ms$

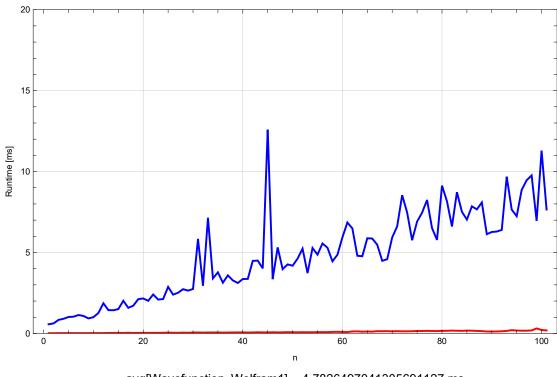
★ Single-Mode and Multidimensional speed test

```
In[161]:=
       FastWaveSMMDList =
          Normal[ExternalEvaluate["Python",
                                                          "from fast wave.wavefunction import
         normal execução externa
              wavefunction_smmd;import timeit;import numpy as np;N_max = 100;xmax =
               20.0;xmin=-20.0;xsize=100;X=np.linspace(xmin,xmax,xsize);[(timeit.timeit(
               lambda : wavefunction_smmd(n, X) ,
               number=10000) /10000) *1000 for n in range(N_max+1)];"]];
       WavefunctionWolframSMMDList = {};
       For[i = 1, i ≤ (Nmax + 1), i++, AppendTo[WavefunctionWolframSMMDList,
       para cada
           RepeatedTiming[WavefunctionMathematica1[i - 1, Xvector, prec]] [1] * 1000];]
           cronometra repetidamente
       ListLinePlot[
       gráfico de linha de uma lista de valores
         {WavefunctionWolframSMMDList, FastWaveSMMDList},
        PlotStyle → {Blue, Red},
        Lestilo do gráfico Lazul Vermelho
        Frame → True,
        Lquadro Lverdadeiro
        FrameLabel → {"n", "Runtime [ms]"},
        legenda do guadro
        PlotLabel →
        etiqueta de gráfico
          Row[{Style["Wavefunction_Wolfram1 vs Wavefunction_Fast-Wave(smmd)", Bold, 13],
         linha estilo
            "\n", Style["X: [(-20.0) \rightarrow 20.0 ; 100], to each value of n \n", 12]}],
                  estilo
        GridLines → Automatic,
        grade de linhas automático
        PlotLegends → Placed[{" avg[Wavefunction_Wolfram1] = " <> ToString[
        Legenda do gráfico situado
                                                                        converte em cadeia de caracteres
              SetPrecision[Mean[WavefunctionWolframSMMDList], 20], TraditionalForm] <> " ms",
              define precisão média
                                                                         forma tradicional
            " avg[Fast-Wave(smmd)] = " <> ToString[
                                             converte em cadeia de caracteres
              SetPrecision[Mean[FastWaveSMMDList], 20], TraditionalForm] <> " ms"}, Below],
                                                            forma tradicional
              define precisão média
                                                                                           abaixo
        ImageSize → Large , PlotRange → {{Automatic, Automatic}, {0, 20.0}}
        tamanho da ··· grande | intervalo do gráf··· | automático | automático
       ]
       Functionality Test Passed: True
```

Out[164]=

Wavefunction_Wolfram1 vs Wavefunction_Fast-Wave(smmd)

X: $[(-20.0) \rightarrow 20.0$; 100], to each value of n



- $avg[Wavefunction_Wolfram1] = 4.7826497041305691127 ms$
- avg[Fast-Wave(smmd)] = 0.091369714356479364570 ms

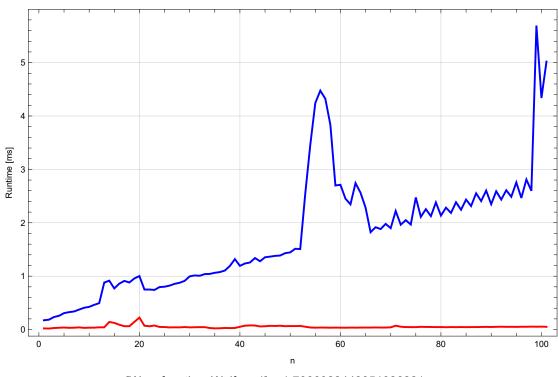
★ Single-Mode and Multidimensional speed test (less_fast)

```
In[@]:= FastWaveSMMDList =
                                                        "from fast_wave.wavefunction import
        Normal[ExternalEvaluate["Python",
        normal execução externa
             wavefunction_smmd;import timeit;import numpy as np;N_max = 100;xmax =
             20.0;xmin=-20.0;xsize=100;X=np.linspace(xmin,xmax,xsize);[(timeit.timeit(
             lambda : wavefunction_smmd(n, X, more_fast = False)
             , number=10000) /10000) *1000 for n in range(N_max+1)];"]];
     WavefunctionWolframSMMDList = {};
     For[i = 1, i ≤ (Nmax + 1), i++, AppendTo[WavefunctionWolframSMMDList,
     para cada
                                     adiciona a
         RepeatedTiming[WavefunctionMathematica1[i - 1, Xvector, prec]][1] * 1000];]
         cronometra repetidamente
     ListLinePlot[
     gráfico de linha de uma lista de valores
       {WavefunctionWolframSMMDList, FastWaveSMMDList},
      PlotStyle → {Blue, Red},
      Lestilo do gráfico Lazul Vermelho
       Frame → True,
      quadro verdadeiro
       FrameLabel → {"n", "Runtime [ms]"},
      Llegenda do quadro
       PlotLabel →
      Letiqueta de gráfico
        Row[{Style["Wavefunction Wolfram1 vs Wavefunction Fast-Wave(smmd; less fast)", Bold,
            13], "\n", Style["X: [(-20.0) \rightarrow 20.0 ; 100], to each value of n \n", 12]}],
                      estilo
       GridLines → Automatic,
      grade de linhas automático
       PlotLegends → Placed[{" avg[Wavefunction_Wolfram1] = " <> ToString[
      legenda do gráfico situado
                                                                     converte em cadeia de caracteres
             SetPrecision[Mean[WavefunctionWolframSMMDList], 20], TraditionalForm] <> " ms",
                                                                      forma tradicional
            define precisão média
          " avg[Fast-Wave(smmd; less_fast)] = " <> ToString[
                                                       converte em cadeia de caracteres
             SetPrecision[Mean[FastWaveSMMDList], 20], TraditionalForm] <> " ms"}, Below],
            define precisão média
                                                          forma tradicional
                                                                                        lahaixo
       ImageSize → Large ]
      tamanho da ··· grande
      Functionality Test Passed: True
```

Out[0]=

Wavefunction_Wolfram1 vs Wavefunction_Fast-Wave(smmd; less_fast)

X: $[(-20.0) \rightarrow 20.0$; 100], to each value of n



- avg[Wavefunction_Wolfram1] = 1.7666022448851326221 ms
- avg[Fast-Wave(smmd; less_fast)] = 0.051437425544533892097 ms

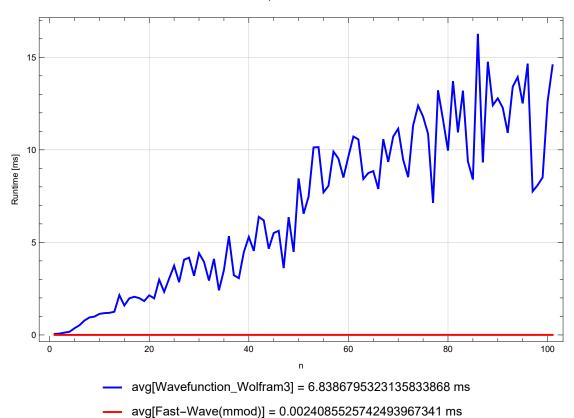
★ Multi-Mode and Onedimensional speed test

```
In[@]:= FastWaveMMODList = Normal[ExternalEvaluate["Python",
                         normal execução externa
          "from fast_wave.wavefunction import wavefunction_mmod;import timeit;N_max
             = 100;x = 20.0; [(timeit.timeit(lambda : wavefunction_mmod(n,
             x) , number=10000)/10000) *1000 for n in range(N max+1)];"]];
     WavefunctionWolframMMODList = {};
     For [i = 1, i \le (Nmax + 1), i++, AppendTo [WavefunctionWolframMMODList,]
         RepeatedTiming[WavefunctionMathematica3[i - 1, x, prec]] [1] * 1000];]
         cronometra repetidamente
     ListLinePlot[
     gráfico de linha de uma lista de valores
       {WavefunctionWolframMMODList, FastWaveMMODList},
      PlotStyle → {Blue, Red},
      estilo do gráfico azul vermelho
      Frame → True,
      _quadro _verdadeiro
      FrameLabel → {"n", "Runtime [ms]"},
      legenda do quadro
      PlotLabel →
      etiqueta de gráfico
        Row[{Style["Wavefunction_Wolfram3 vs Wavefunction_Fast-Wave(mmod)", Bold, 13],
       linha estilo
                                                                                   negrito
          "\n", Style["x: 20.0, to each value of n \n", 12]}],
                estilo
       GridLines → Automatic,
      grade de linhas automático
      PlotLegends → Placed[{" avg[Wavefunction_Wolfram3] = " <> ToString[
      legenda do gráfico situado
                                                                      converte em cadeia de caracteres
             SetPrecision[Mean[WavefunctionWolframMMODList], 20], TraditionalForm] <> " ms",
            define precisão _média
                                                                       forma tradicional
          " avg[Fast-Wave(mmod)] = " <> ToString[
                                           converte em cadeia de caracteres
             SetPrecision[Mean[FastWaveMMODList], 20], TraditionalForm] <> " ms"}, Below],
            define precisão média
                                                          forma tradicional
                                                                                         labaixo
       ImageSize → Large ]
      tamanho da ··· grande
     Functionality Test Passed: True
```

Out[0]=

Wavefunction_Wolfram3 vs Wavefunction_Fast-Wave(mmod)

x: 20.0, to each value of n



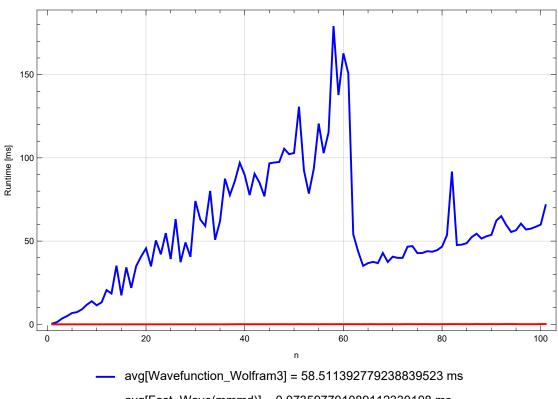
★ Multi-Mode and Multidimensional speed test

```
In[@]:= FastWaveMMMDList = Normal[ExternalEvaluate["Python",
                         normal execução externa
          "from fast_wave.wavefunction import wavefunction_mmmd;import
             timeit;import numpy as np;N_max = 100;xmax = 20.0;xmin =
             -20.0;xsize=100;X=np.linspace(xmin,xmax,xsize);[(timeit.timeit(lambda
             : wavefunction_mmmd(n, X) , number=10000)/10000)*1000
             for n in range(N_max+1)];"]];
     WavefunctionWolframMMMDList = {};
      For[i = 1, i ≤ (Nmax + 1), i++, AppendTo[WavefunctionWolframMMMDList,
     para cada
                                     adiciona a
         RepeatedTiming[WavefunctionMathematica3[i - 1, Xvector, prec]][1] * 1000];]
         cronometra repetidamente
     ListLinePlot[
     gráfico de linha de uma lista de valores
       {WavefunctionWolframMMMDList, FastWaveMMMDList},
      PlotStyle → {Blue, Red},
      Lestilo do gráfico Lazul Lvermelho
       Frame → True,
      quadro verdadeiro
       FrameLabel → {"n", "Runtime [ms]"},
      Llegenda do quadro
       PlotLabel →
      etiqueta de gráfico
        Row[{Style["Wavefunction Wolfram3 vs Wavefunction Fast-Wave(mmmd)", Bold, 13],
          "\n", Style["X: [(-20.0) \rightarrow 20.0 ; 100], to each value of n \n", 12]}],
       GridLines → Automatic,
      grade de linhas automático
       PlotLegends → Placed[{" avg[Wavefunction_Wolfram3] = " <> ToString[
      legenda do gráfico situado
                                                                      converte em cadeia de caracteres
             SetPrecision[Mean[WavefunctionWolframMMMDList], 20], TraditionalForm] <> " ms",
            define precisão média
                                                                      forma tradicional
           " avg[Fast-Wave(mmmd)] = " <> ToString[
                                           converte em cadeia de caracteres
             SetPrecision[Mean[FastWaveMMMDList], 20], TraditionalForm] <> " ms"}, Below],
             define precisão | média
                                                          forma tradicional
                                                                                         abaixo
       ImageSize → Large ]
      Ltamanho da ··· Lgrande
      Functionality Test Passed: True
```

Out[0]=

Wavefunction_Wolfram3 vs Wavefunction_Fast-Wave(mmmd)

X: [(-20.0) \rightarrow 20.0 ; 100], to each value of n



avg[Fast-Wave(mmmd)] = 0.073597701089112330108 ms