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Representation and Reasoning System

A Representation and Reasoning System (RRS) is made up of

- \bullet $\,$ $Formal\ language:$ specifies the legal sentences
- Semantics: specifies the meaning of the symbols
- \bullet $Reasoning\ theory\ or\ proof\ procedure:$ nondeterministic specification of how an answer can be produced

Implementation

An implementation of an RRS consists of

- Language parser: maps sentences of the language into data structures
- Reasoning procedure: implementation of reasoning theory and search strategy

The semantics aren't reflected in the implementation!

Using

- 1. Begin with a task domain
- 2. Distinguish those things you want to talk about (the ontology)
- 3. Choose symbols in the computer to denote objects and relations
- 4. Tell the system knowledge about the domain
- 5. Ask the system questions

Simplifying Assumptions of Inital RRS

An agent's knowledge can be usefully described in terms of *individuals* and *relations* among individuals. An agent's knowledge base consists of *definite* and *positive* statements. The environment is *static*. There are only a finite number of individuals of interest in the domain. Each individual can be given a unique name.

Syntax of Datalog

- Variable: starts with upper-case letter
- Constant: starts with lower-case letter or is a sequence of digits (numeral)
- Predicate symbol: starts with lower-case letter
- Term: is either a variable or a constant
- Atomic symbol: (atom) is of the form p or $p(t_1, \ldots, t_n)$ where p is a predicate symbol and t_i are terms
- Definite clause is either an atomic symbol (a fact) or of the form $a \leftarrow b_1 \lor \cdots \lor b_m$
- Query is of the form $?b_1 \lor \cdots \lor b_m$
- ullet Knowledge base is a set of definite clauses

Semantics: General Idea

A *semantics* specifies the meaning of sentences in the language. An *interpretation* specifies

- What objects (individuals) are in the world
- The correspondence between symbols in the computer and objects and relations in the world
 - Constants denote individuals
 - Predicate symbols denote relations

Formal Semantics

- An interpretation is a tiple $I = \{D, \phi, \pi\}$ where
- D, the domain, is a nonempty set
 - Elements of D are individuals
- ϕ is a mapping that assigns to each constant an element of D
 - Constant c denotes individual $\phi(c)$
- π is a mapping that assigns to each *n*-ary predicate symbol a relation: a function from D^n into $\{true, false\}$

Important Things to Note

- The domain *D* can contain real objects (e.g. a person, a room) and can't necessarily be stored in a computer
- $\pi(p)$ specifies whether the relation denoted by the *n*-ary predicate symbol p is true or false for each *n*-tuple of individuals
- If predicate symbol p has no arguments, then $\pi(p)$ is each true or false

Truth is an Interpretation

A constant c denotes in I the individual $\phi(c)$. Ground (variable-free) atom $p(t_1, \ldots, t_n)$ is

- True in interpretation I if $\pi(p)(t'_1,\ldots,t'_n)=true$ where t_i denotes t'_i in interpretation I
- False in interpretation I if $\pi(p)(t'_1,\ldots,t'_n) = false$

Ground clase $h \leftarrow b_1 \lor \cdots \lor b_m$ is false in interpretation I if h is false in I and each b_i is true in I, and if true in interpretation I otherwise.

Models and Logical Consequence

- A knowledge base KB, is true in interpration I if and only if every clause in KB is true in I
- A model of a set of clauses is an interpretaion in which all the clauses are true
- If KB is a set of clauses and g is a conjunction of atoms, g is a logical consequence of KB, written $KB \models g$ if g is true in every model of KB
- That is, $KB \vDash g$ if there is no interpretation in which KB is true and g is false

User's View of Semantics

- 1. Choose a task domain: intended interpretation
- 2. Associate constants with individuals you want to name
- 3. For each relation you want to represent, associate a predicate symbol in the language
- 4. Tell the system classes that are true in the intended interpretation: $axiomatising\ the\ domain$
- 5. Ask questions about the intended interpretation
- 6. If $KB \models g$ then g must be true in the intended interpretation

Computer's View of Semantics

- The computer doesn't have access to the intended interpretation
- All it knows is the knowledge base
- The computer can determine if a formula is a logic consequence of KB
- If $KB \models g$ then £g£ must be true in the intended interpretation
- if $KB \nvDash g$ then there is a model of KB in which g is false
 - This could be the intended interpretation

Proofs

- $\bullet\,$ A proof is a mechanically derivable demonstration that a formula logically follows from a knowledge base
- Given a proof proceduce $KB \vdash g$ means g can be derived from knowledge base KB
- Recall $KG \vDash g$ means g is true in all models of KB
- A proof procedure is *sound* if $KB \vdash g$ implies $KB \models g$
- A proof procedure is *complete* is $KB \vDash g$ implies $KB \vdash g$

Bottom-Up Ground Proof Procedure

One rule derivation, a generalised form of modus ponens:

If " $h \leftarrow b_1 \lor \cdots \lor b_m$ " is a caluse in the knowledge base, and each b_i has been derived, than h can be derived.

You are forward chaining on this clause

Soundness

If $KB \vdash g$ then $KB \models g$.

Suppose there is a g such that $KB \vdash g$ and $KB \nvDash g$.

Let h be the first atom added to C that's not true in every model of KB. Suppose h isn't true in model I of KB. There must be a clause in KB in the form

$$h \leftarrow b_1 \lor \dots \lor b_m$$

Each b_i is true in I. h is false in I. So this clause is false in I. Therefore I isn't a odel of KB.

Contradiction: thus no such g exists.

Fixed Point

The C generated at the end of the bottom-up algorithm is called a *fixed point*.

Let I be the interpretation in which every element of the fixed point is true and every other atom is false.

I is a model of KB.

Proof: suppose $h \to b_1 \lor \cdots \lor b_m$ in KB is false in I. Then h is false and each b_i is true in I. Thus h can be added to C. Contradiction to C being the fixed point.

I is called a Minimal Model.

Completeness

If $KB \vDash g$ then $KB \vdash g$.

Suppose $KB \vDash g$. Then g is true in all models of KB. Thus g is true in the minimal model. Thus g is generated by the bottom up algorithm. Thus $KB \vdash g$.