TRINITY COLLGE DUBLIN

School of Computer Science and Statistics

Extra Questions

ST3009: Statistical Methods for Computer Science

NOTE: There are many more example questions in the course textbook "A First Course in Probability" by Sheldon Ross.

- Question 1. (a) What is the number of ways that we can select 3 consonants from 7?
 - (b) What is the number of ways we can select 2 vowels from 4?
- (c) Out of 7 consonants and 4 vowels, how many ways can 3 consonants and 2 vowels be selected?
 - (d) How many ways can 3 consonants and 2 vowels (5 letters) be rearranged?

Question 2. In a group of 6 boys and 4 girls, four children are to be selected. In how many different ways can they be selected such that at least one boy should be there?

Question 3. A bag contains 1 red ball and 4 black balls.

- (a) In how many different ways can I draw 2 balls from the bag, i.e. one after another without replacement, where when counting all balls of the same colour are treated as being the same.
- (b) In how many different ways can I draw 2 balls from the bag when after drawing each ball I put it back into the bag.

Question 4. I toss a coin and if it comes up heads I roll two 4-sided die and otherwise two 6-sided die.

- (a) How many arrangements of heads/tails and die outcomes are possible (counting the 4 and 6 sided dice separately).
 - (b) Out of these arrangements, in how many do the dice rolls sum to 3?
 - (c) In how many do the dice rolls sum to 10?

Question 5. From a group of 5 women and 7 men:

- (a) A committee of 3 is to be formed. How many different committees are possible?
- (b) How many different committees consisting of 2 women and 3 men can be formed?
- (c) What if 2 of the men are feuding and refuse to serve on the committee together?

Question 6. (a) How many different 7-place license plates are possible if the first 2 places are for letters and the other 5 for numbers?

(b) And how many when no letter or number can be repeated in a single license plate.

Question 7. A deck of playing cards contains 52 cards consisting of four suits (hearts, spades, clubs or diamonds) and 13 ranks or values $(1,2,\ldots,10,\text{jack},\text{queen},\text{king})$.

- (a) You draw one card from the deck and then draw another (without replacement). How many ways could you draw a pair (two cards of the same rank) e.g. 4 of hearts and 4 of spades.
- (b) Suppose you now draw three cards. In how many ways can you draw a pair now (two cards of the same rank, the third of a different rank)

Question 8. I am stocking a fish tank. The fish shop has four types of sea creature: piranha, crocodile, tuna, catfish. Piranha's and crocodile's can share the tank with each other but not with tuna or catfish as they'll just eat these.

- (a) How many combinations of two sea creatures can I place in my tank?
- (b) How many combinations of three sea creatures?

Question 9. John, Jim, Jay, and Jack have formed a band consisting of 4 instruments.

- (a) If each of the boys can play all 4 instruments, how many different arrangements are possible?
- (b) What if John and Jim can play all 4 instruments, but Jay and Jack can each play only piano and drums (you can assume all four player have an instrument)?

Question 10. In how many ways can 3 novels, 2 mathematics books, and 1 chemistry book be arranged on a bookshelf if

- (a) the books can be arranged in any order?
- (b) the mathematics books must be together and the novels must be together?
- (c) the novels must be together, but the other books can be arranged in any order?