

**Search for supersymmetry using boosted Higgs bosons and
missing transverse momentum in proton-proton collisions
at 13 TeV**

by

Frank Jensen

M.S., University of Colorado Boulder, 2014

B.A., University of California Berkeley, 2008

A thesis submitted to the
Faculty of the Graduate School of the
University of Colorado in partial fulfillment
of the requirements for the degree of
Doctor of Philosophy
Department of Physics

2018

This thesis entitled:
Search for supersymmetry using boosted Higgs bosons and missing transverse momentum in
proton-proton collisions at 13 TeV
written by Frank Jensen
has been approved for the Department of Physics

Professor Kevin Stenson

Professor William Ford

Date _____

The final copy of this thesis has been examined by the signatories, and we find that both the content and the form meet acceptable presentation standards of scholarly work in the above mentioned discipline.

Jensen, Frank (Ph.D., Physics)

Search for supersymmetry using boosted Higgs bosons and missing transverse momentum in proton-proton collisions at 13 TeV

Thesis directed by Professor Kevin Stenson

A search for physics beyond the Standard Model in events with one or more high-momentum Higgs bosons decaying to pairs of b quarks in association with missing transverse momentum is presented. The data, corresponding to an integrated luminosity of 35.9 fb^{-1} , were collected with the CMS detector at the Large Hadron Collider in proton-proton collisions at the center-of-mass energy $\sqrt{s} = 13 \text{ TeV}$. The analysis utilizes a new b quark tagging technique based on jet substructure to identify jets from Higgs $\rightarrow b\bar{b}$ decays. Events are categorized by the number of $b\bar{b}$ -tagged jets, the mass of the jets, and the missing transverse momentum. No significant deviations from Standard Model expectations are observed. In the context of supersymmetry, limits on the cross sections of pair-produced gluinos are set, assuming that gluinos decay to quark pairs and a Higgs or Z boson, and the lightest supersymmetric particle. The decay chain proceeds through an intermediate particle assumed to be the second lightest in the theory. Assuming a large mass splitting between these two neutral particles, and 100% NLSP branching fraction to Higgs bosons, the lower limit on the gluino mass is found to be 2010 GeV.

Dedications

The taxpayers.

Contents

Chapter

1	Introduction	1
2	The Standard Model of Particle Physics	5
2.1	Introduction	5
2.2	Quantum Electrodynamics	6
2.3	Quantum Chromodynamics	7
2.3.1	Confinement, Hadrons, & the Quark Model	9
2.4	Electroweak Theory	11
2.4.1	The Higgs Mechanism	12
2.4.2	Quark Mixing: the CKM Matrix	16
2.4.3	Brief Electroweak Summary	16
2.5	Parameters of the Standard Model	17
2.6	Neutrino Mass	17
3	The Minimal Supersymmetric Model	19
4	The Large Hadron Collider	26
5	The CMS Detector	31
5.1	Silicon Tracker	32
5.1.1	Pixel Detector	35

5.1.2	Strips Detector	36
5.2	Electromagnetic Calorimeter	36
5.2.1	Preshower	37
5.3	Hadronic Calorimeter	38
5.4	Solenoidal Magnet	39
5.5	Muon System	40
5.5.1	Drift Tubes	41
5.5.2	Cathode Strip Chambers	41
5.5.3	Resistive Plate Chambers	43
5.6	Trigger System	43
6	Event Reconstruction	46
6.1	Basic Elements From the Detector	46
6.1.1	Tracks	46
6.1.2	ECAL & HCAL Clusters	48
6.1.3	Muon Tracks	48
6.2	Obtaining a Particle-level Description	48
6.3	Additional High-Level Objects	51
6.3.1	Jets	51
6.3.2	b-tagging of Jets	51
6.3.3	Invisible Particles $\rightarrow p_T^{\text{miss}}$	52
7	Search for supersymmetry using boosted Higgs bosons and missing transverse momentum in proton-proton collisions at 13 TeV	53
7.1	Motivation & Strategy	53
7.2	Baseline Selection and Object Definition	54
7.3	Dataset & Trigger	57
7.4	Event Simulation	59

7.4.1	Standard Model Processes	59
7.4.2	Signal Models	59
7.5	Event Binning & Background Estimation	61
7.5.1	Control Regions within Data	65
7.5.2	κ as a Correction to the Estimation	67
7.5.3	Sideband Yields & Predictions	77
7.6	Signal Systematic Uncertainties	77
7.7	Observed Yields in the Signal Regions	81
7.8	Exclusion Curves & Mass Limits	81
8	Conclusions	87
Bibliography		88
Appendix		
A	b \bar{b} -tagging of AK8 Jets	92
B	Reinterpretation	97
C	Determining b \bar{b} -tagging Scale Factors for W jets in t \bar{t} Events	102

Tables

Table

2.1	Summary of field content within the SM.	6
3.1	Summary of the additional particle content within the MSSM.	20
3.2	Mixing of the supersymmetric electroweak fields.	20
4.1	The stages of proton beam acceleration for the LHC at CERN.	27
6.1	Seeding requirements for each step in the iterative track reconstruction.	47
7.1	SM samples used in the analysis.	60
7.2	Summary of the control region scale-factors integrated over p_T^{miss}	69
7.3	Single lepton control region scale-factors in the anti-tag sideband region.	73
7.4	A summary of the background estimation corrections κ	73
7.5	Corrected yields in the signal regions.	75
7.6	Corrected yields in the sideband regions.	76
7.7	Sideband region yields, κ , and background predictions for the 6 signal bins.	77
7.8	Fit results for W-mass resolution in data and simulation.	81
7.9	Summary of signal shape and normalization uncertainties.	82
7.10	Yields and predicted background in the signal regions.	83
A.1	Data/MC scale factors for AK8 jet b \bar{b} -tagging.	96

B.1	Effective event weights for $b\bar{b}$ and mass tagging of AK8 jets.	98
B.2	Predicted yields in the 6 signal bins using reinterpretation prescription.	101
C.1	W jet $b\bar{b}$ mistag rates in data and simulation, inclusive in p_T	105
C.2	Summary of scale factors for $b\bar{b}$ -tagging W jets in $t\bar{t}$ events.	106

Figures

Figure

1.1	The particles in the Standard Model of particle physics.	2
2.1	Meson multiplets predicted by SU(3) flavor symmetry within the quark model.	10
2.2	Baryon multiplets predicted by SU(3) flavor symmetry within the quark model.	10
3.1	MSSM vertices coupling SM and supersymmetric particles.	23
3.2	Tree-level gluino pair-production mechanisms.	24
3.3	Previous results for searches of gluino-mediated supersymmetry.	25
4.1	The CERN accelerator complex.	27
4.2	An event recorded by the CMS experiment during a high pile-up fill in 2016.	29
4.3	The integrated luminosity of CMS as of September 2018.	30
5.1	A diagram of the CMS detector.	33
5.2	A diagram of the CMS detector in the $r\phi$ plane; particle signatures are shown.	33
5.3	A diagram of the CMS detector in the rz plane.	34
5.4	The CMS silicon tracker	35
5.5	The CMS electromagnetic calorimeter	37
5.6	The CMS hadron calorimeter	39
5.7	A simulation of the 4T CMS magnetic field.	40
5.8	The CMS muon drift tube detector.	42

5.9	The CMS muon cathode strip chambers.	44
5.10	The CMS muon resistive plate chamber.	44
7.1	Diagrams of the benchmark models used for motivation of the targeted signal.	55
7.2	Distributions of the $b\bar{b}$ -tagging discriminator and jet mass for AK8 jets.	58
7.3	Generator level distributions for the H bosons in the T5HH model.	62
7.4	Partitioning of the signal and sideband regions for event binning.	63
7.5	MC distributions of p_T^{miss} after baseline selection.	64
7.6	p_T^{miss} distributions and predictions in the signal regions using simulation only.	66
7.7	Comparisons of the predicted and observed yields within the data control regions . .	68
7.8	Signal and sideband yields in the single photon control region.	70
7.9	Signal and sideband yields in the single lepton control region.	71
7.10	Signal and sideband yields in the the low- $\Delta\phi$ control region.	72
7.11	Signal region p_T^{miss} distributions using scale-factor corrected simulation.	74
7.12	Sideband region p_T^{miss} distributions of data and scale-factor corrected simulation. .	78
7.13	Pruned jet mass in semi-leptonic $t\bar{t}$ events.	82
7.14	Observed yields in the signal regions.	83
7.15	The single event in the A_2 region.	84
7.16	Observed and expected limits on the gluino cross section.	86
A.1	ROC curve of the signal efficiency and mistag rate for the $b\bar{b}$ tagger.	93
A.2	$H \rightarrow b\bar{b}$ tagging efficiencies in signal events.	94
A.3	Signal efficiency to be in the single or double Higgs tag event category.	95
B.1	Efficiencies for an AK8 jet originating from H boson decay.	99
B.2	Efficiencies for an AK8 jet originating from Z boson decay.	100
B.3	Diagram for compiling the weights into each of the 6 analysis bins.	100
C.1	Diagram of a semileptonic $t\bar{t}$ event.	103

- C.2 AK8 jet mass and $b\bar{b}$ -tagging discriminator distributions in data and simulation. . . 104

Chapter 1

Introduction

The emerging picture of the last century is that the elements described by the Periodic Table are themselves not the most fundamental forms found in Nature. We have learned that these elements are made of atoms consisting of bound states of protons, neutrons, and electrons. We have discovered that these protons and neutrons themselves are made of more fundamental components called quarks and gluons. And so as the Periodic Table before it, the Standard Model of particle physics (SM) seen in Figure 1.1, has been developed to provide an organizing principle for what we currently understand to be the correct description for the strong and electroweak forces, describing the fundamental particles and forces that form the Universe (the SM does not address gravity). The discovery of the Higgs boson in 2012 [1] completed the search for all the fundamental particles addressed within the theory, a truly monumental achievement. As time goes on experimental verification only grows stronger.

But, there are many both experimental and theoretical indications that the SM is not the final story. Cosmological observations require the presence of a “dark matter” in the Universe, a ubiquitous substance thought to account for 85% of the total matter in the Universe. Although its influence has been observed in gravitational lensing phenomena and galaxy rotation curves, we do not yet have a particle description of its nature. One theoretical motivation that points toward the SM being a part of some grander theory is known as a “fine-tuning” problem. Because the Higgs boson is a scalar particle (the only such fundamental particle in the SM), its mass receives quantum mechanical corrections that are strongly dependent on the ultraviolet cutoff Λ_{UV} or other high mass

Standard Model of Elementary Particles

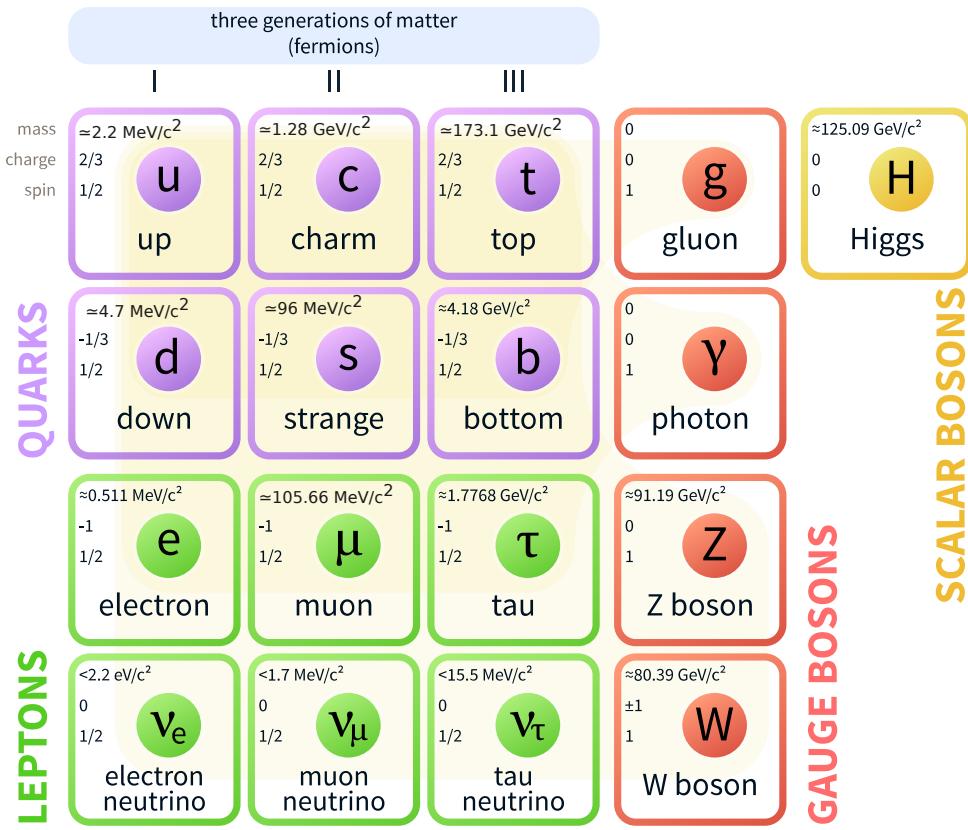


Figure 1.1: The particles in the Standard Model of particle physics. [2]

scales in the theory. As the most natural cutoff is likely at the Grand Unified Theory or Planck scale, we would expect the Higgs boson mass to be extremely large, many orders of magnitude larger than it has experimentally been determined to be. This implies that there is some sort of ‘unnatural’ collusion between the correction terms, which is somehow able to bring the mass to the electroweak scale (this is known as a *hierarchy problem*).

Supersymmetry (SUSY) is an elegant extension to the SM which is able to address many of these issues. In addition to the $SU(3) \times SU(2) \times U(1)$ symmetries of the SM, SUSY introduces space-time symmetries relating fermionic and bosonic degrees of freedom. The particle content within the simplest of such SUSY models, the Minimal Supersymmetric SM (MSSM), is over twice that of the SM as each particle requires a “superpartner” differing by $1/2$ unit of spin. The lightest neutral particle of the theory, expected to remain stable, is a popular candidate for particle dark matter. The addition of these superpartners to the theory yield quantum mechanical corrections to the Higgs mass that enter with the opposite sign and naturally are able to cancel the terms up to Λ_{UV} . An exact supersymmetry requires that these superpartners have identical mass to their SM counterpart. As we have not observed any such particles, it must be that the supersymmetry is broken, resulting in the partners acquiring large mass through some other means. These masses must be sufficiently large that small production cross sections at collider experiments have not allowed for their unambiguous detection. A major motivating force for the construction of the LHC is finding evidence of SUSY. The analysis presented in this thesis presents one such search, focusing in one small parameter space of the vast possibilities.

The thesis is outlined as follows: A description of the Standard Model (SM) of particle physics, the theory describing the known fundamental forces and particles, is presented in Chapter 2. A description of the Minimal Supersymmetric Standard Model (MSSM), one extension to the SM able to provide answers to many of our questions, is presented in Chapter 3. A description of the Large Hadron Collider (LHC), the facility that acts as our source of high-energy proton-proton collisions, is presented in Chapter 4. A description of the CMS particle detector, responsible for the detection of particles and reconstruction of the proton interactions, is presented in Chapter 5. A

description of how the data from the detector are reconstructed and identified as physical particles is presented in Chapter 6. The focus of the thesis, a description of how the physics data can be used to search for evidence of new particles such as those predicted by SUSY, is presented in Chapter 7. The conclusions are presented in Chapter 8. Appendix A presents a more detailed discussion of the $b\bar{b}$ -tagging algorithm used in this analysis. Appendix B provides tagging efficiencies for the reconstruction of Higgs and Z bosons relevant to the analysis. Appendix C presents a calculation of scale factors, correcting differences in simulation from data, for $b\bar{b}$ -tagging W boson jets — a topic partly independent from the rest of the thesis.

Chapter 2

The Standard Model of Particle Physics

2.1 Introduction

The Standard Model (SM) is a mathematical framework for the quantum mechanical description of matter and physical forces. It provides a description of the weak, strong, and electromagnetic interactions as mediated via “messenger” particles (gravity has so far eluded a quantum mechanical description). The particles constituting matter are all fermions and can be classified as *quarks* or *leptons* - quarks participate in the weak and strong force, leptons participate in the weak force; any charged particle experiences the electromagnetic force. *Gauge bosons* are the particles responsible for the force interactions. The Higgs field is important for the generation of particle mass. This particle content has been seen in Figure 1.1. We now turn to the field theory approach for these objects. This chapter is adapted from [3, 4, 5].

Matter particles are massive spin-1/2 fermions represented as solutions to the free-particle Dirac equation. The Lagrangian, and resulting equation of motion, are as follows:

$$\begin{aligned}\mathcal{L} &= i\bar{\psi}\gamma^\mu\partial_\mu\psi - m\bar{\psi}\psi, \text{ and} \\ i\gamma^\mu\partial_\mu\psi - m\psi &= 0,\end{aligned}\tag{2.1}$$

respectively. ψ is known as a Dirac fermion and has four degrees of representing the spin state of both a particle and anti-particle.

Particle interactions are generated by requiring the free-particle Lagrangian to be invariant under the action of different symmetry groups. Demanding local (gauge) invariance requires one

Table 2.1: Summary of field content within the SM.

Gauge Sector	Matter Fields	Gauge Fields
SU(3)	u, d, c, s, t, b	$G_\mu^{1\dots 8} \rightarrow g_\mu^{1\dots 8}$
SU(2) \times U(1)	$Q_L = \begin{pmatrix} u \\ d \end{pmatrix}_L, \begin{pmatrix} s \\ c \end{pmatrix}_L, \begin{pmatrix} t \\ b_L \end{pmatrix}_L$ $q = u, d, c, s, t, b$ $L_L = \begin{pmatrix} \nu_e \\ e^- \end{pmatrix}_L, \begin{pmatrix} \nu_\mu \\ \mu^- \end{pmatrix}_L, \begin{pmatrix} \nu_\tau \\ \tau^- \end{pmatrix}_L$ $\ell = (e, \mu, \tau)$	W_μ^{012}, B_μ^0 $W_\mu^0, B_\mu^0 \rightarrow Z_\mu^0, A_\mu^0$ $W_\mu^1, W_\mu^2 \rightarrow W_\mu^+, W_\mu^-$
Higgs Sector	$H = \begin{pmatrix} H^+ \\ H^0 \end{pmatrix} \rightarrow h^0$	

to introduce spin-1 vector fields to the Lagrangian that couple with the fermions. The vector fields are to be identified with the generators of the symmetry group and act as the mediator of the force via particle exchange. U(1) generates electromagnetism via interactions with photons. A combination of U(1) and SU(2) generates the electroweak theory, simultaneously describing the electromagnetic and weak nuclear force via interactions with W^\pm bosons, Z bosons and photons. SU(3) generates quantum chromodynamics, the theory of the strong nuclear force via interactions with gluons. Spin-1 gauge bosons are represented by solutions to the free particle Proca equations generated by the following Lagrangian, with equation of motion:

$$\mathcal{L} = -\frac{1}{16\pi} B^{\mu\nu} B_{\mu\nu} + \frac{1}{8\pi} m^2 B_\nu B^\nu, \text{ and} \quad (2.2)$$

$$\partial^\mu \partial_\mu \psi - m^2 \psi = 0,$$

where $B_{\mu\nu} \equiv \partial_\mu B_\nu - \partial_\nu B_\mu$ is known as the *energy-momentum tensor* representing the kinetic energy of the field. ($m = 0$ for the photon.)

The mathematical fields that are contained within the SM are seen in Table 2.1. This table will serve as a reference for the remainder of the chapter.

2.2 Quantum Electrodynamics

Quantum electrodynamics describes the interactions of particles with electric charge. Beginning with a free-particle Dirac fermion we see that the Lagrangian is invariant under the following

$U(1)$ transformation:

$$\psi(x) \xrightarrow{U(1)} e^{iq\alpha} \psi(x) \quad (2.3)$$

where q is the electric charge, and α is an arbitrary constant.

In light of this symmetry, Noether's theorem implies the existence of a conserved (electromagnetic) current $j^\mu = -e\bar{\psi}\gamma^\mu\psi$ ($\partial_\mu j^\mu = 0$). If we then allow the $U(1)$ transformation to be space-time dependent, that is $\alpha = \alpha(x)$, we must introduce a new spin-1 vector field A^μ in order for the derivative to transform such that the Lagrangian remains invariant. This new field is introduced by making a redefinition of the partial derivative, called the *covariant derivative*, and the following transformation property for the new field:

$$\begin{aligned} \partial_\mu &\rightarrow \partial_\mu - ieA_\mu \\ A_\mu &\xrightarrow{U(1)} A_\mu + \frac{1}{e}\partial_\mu\alpha \end{aligned} \quad (2.4)$$

We then make the substitution into the Lagrangian:

$$\mathcal{L}_{QED} = i\bar{\psi}\gamma^\mu\partial_\mu\psi - e\bar{\psi}\gamma^\mu\psi A_\mu - m\bar{\psi}\psi - \frac{1}{4}F_{\mu\nu}F^{\mu\nu} \quad (2.5)$$

, where $F_{\mu\nu} \equiv \partial_\mu A_\nu - \partial_\nu A_\mu$ is the field strength tensor.

We see that in order for the Lagrangian to remain invariant under this $U(1)$ transformation we introduced an additional term that links the (conserved) electromagnetic current with the spin-1 field: $e\bar{\psi}\gamma^\mu\psi A_\mu = j^\mu A_\mu$. This new field is to be identified with the photon, it acts as a mediator of the force between two particles with electric charge. A photon mass term of the form $\frac{1}{2}m^2 A^\mu A_\mu$ is forbidden as it is not invariant under the transformation rule; the photon remains massless.

2.3 Quantum Chromodynamics

Quantum chromodynamics describes the interactions of quarks due to the strong nuclear force. The theory is generated by demanding local invariance of the Lagrangian under an $SU(3)$ symmetry operating on *color triplets*. Eight new gauge fields must be introduced to give the proper

transformation rule of the covariant derivative. These new gauge fields become the gluons and act as the mediator of the strong force, mixing the color states within a quark.

Consider the following SU(3) transformation:

$$q \xrightarrow{\text{SU}(3)} e^{\frac{1}{2}ig_s\boldsymbol{\xi}(x)\cdot\boldsymbol{\lambda}} q \quad (2.6)$$

where g_s is the strong coupling constant, $\boldsymbol{\xi}$ is an 8-dimensional vector of arbitrary functions of spacetime, $\boldsymbol{\lambda}$ are the 8 3x3 Gell-Mann matrices, and q is a Dirac fermion (any of the 6 SM quarks). The SU(3) transformation acts on the **color** components of the quark.

SU(3) gauge invariance requires us to modify the definition of the partial derivative to include 8 spin-1 vector fields \mathbf{G}_μ :

$$\begin{aligned} \partial_\mu &\rightarrow \partial_\mu - ig_s \boldsymbol{\lambda} \cdot \mathbf{G}_\mu \\ G_\mu^k &\xrightarrow{\text{SU}(3)} G_\mu^k - \frac{1}{g_s} \partial_\mu \xi_k - f_{ijk} \xi_i G_\mu^j \end{aligned} \quad (2.7)$$

where f_{ijk} are known as the *structure constants* of SU(3) and arise from its non-Abelian nature; they satisfy $[\lambda_i, \lambda_j] = 2if_{ijk}\lambda_k$.

The complete QCD Lagrangian becomes:

$$\mathcal{L}_{\text{QCD}} = i\bar{q}\gamma^\mu \partial_\mu q - \frac{1}{2}(g_s\bar{q}\gamma^\mu \boldsymbol{\lambda} q) \cdot \mathbf{G}_\mu - m\bar{q}q - \frac{1}{4}\mathbf{G}^{\mu\nu} \cdot \mathbf{G}_{\mu\nu} \quad (2.8)$$

where $\mathbf{G}_i^{\mu\nu} \equiv \partial^\mu \mathbf{G}_i^\nu - \partial^\nu \mathbf{G}_i^\mu - g_s f_{ijk} \mathbf{G}_j^\mu \mathbf{G}_k^\nu$ is the field strength tensor for the gluon field i . We see the non-Abelian nature of SU(3) manifests itself as self-couplings within the gluon field, giving rise to interaction vertices with 3 or 4 gluons. The 8 conserved color currents, analogous to the electromagnetic current, are seen as interaction terms between two quarks and a gluon ($\frac{1}{2}g_s\bar{q}\gamma^\mu \boldsymbol{\lambda} q$) $\cdot \mathbf{G}_\mu = \mathbf{j}^\mu \cdot \mathbf{G}_\mu$.

To conserve color charge at the QCD vertices, gluons themselves must carry both color and anti-color. The color charge allows for self interactions of the gluons. The eight physical gluons are members of an SU(3) color/anticolor octet, with six of them represented as ladder operators and two as diagonal matrices. A gluon mass term of the form $\frac{1}{2}m^2 \mathbf{G}^\mu \cdot \mathbf{G}_\mu$ is forbidden as it is not invariant under the transformation rule; the gluons remain massless.

2.3.1 Confinement, Hadrons, & the Quark Model

Experimentally we have never detected a free quark. The physical manifestation of quark production results in a final state consisting of many lower energy particles collinear with the original quark. This “spray” of particles is known as a *jet*. This behavior is explained as arising from a phenomena known as *color confinement*: all objects with color charge are confined to colorless singlets. The origins of color confinement may be traced to the self interactions of the gluon fields causing the strong force between two quarks **increasing** as they separate. It eventually becomes energetically favorable to create quark-antiquark pairs from the vacuum, which can subsequently combine with other quarks to form the colorless objects (constituting the jets).

Hadrons are bound states of quarks, interacting via the strong force. Color confinement limits the possible combinations of quarks and antiquarks that can exist together in a bound state (antiquarks carry anticolor). Among states consisting of two quarks+antiquarks, the only possible color singlet wave function is a $q\bar{q}$ pair: $\psi = \frac{1}{\sqrt{3}}(r\bar{r} + g\bar{g} + b\bar{b})$ — these states are called *mesons*. For systems of three quarks+antiquarks, the only color singlet consists of three quarks (or antiquarks) qqq : $\psi = \frac{1}{\sqrt{6}}(rgb - rbg + gbr - grb + brg - bgr)$ — these states are called *baryons*.

The strength of the strong force between two quarks is independent of their flavor and therefore QCD possesses a symmetry under rotations in flavor-space. This would be an exact symmetry if it were not for the physical quark masses (Figure 1.1). To a crude approximation the u , d , and s quarks have the same mass: 2.2, 4.7, and 96 MeV (compared to the c with a mass of 1.28 GeV). The uds quarks can therefore be thought of as different states within a triplet. This is known as the *SU(3) flavor symmetry*. Within the symmetry, the $q\bar{q}$ meson states can be combined to form two nonets with angular momentum $l = 0$, and spins of $s = 0$ or $s = 1$. The $s = 0$ states are the lowest energy and provide a quark description of the kaons and pions. The qqq baryons can form flavor states consisting of a $j = 1/2$ octet and $j = 3/2$ decuplet. The $j = 1/2$ states are the lowest energy and include the proton and neutron. The multiplet structures for the mesons and baryons can be seen in Figures 2.1 and 2.2, respectively.

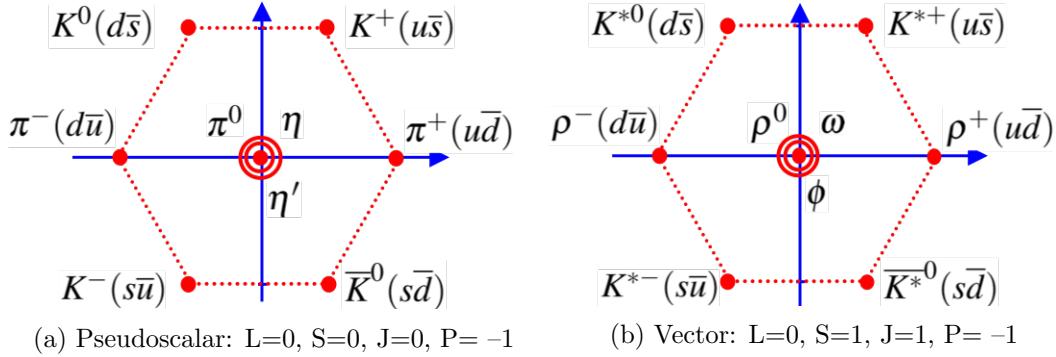


Figure 2.1: Meson multiplets predicted by SU(3) flavor symmetry within the quark model. [6]

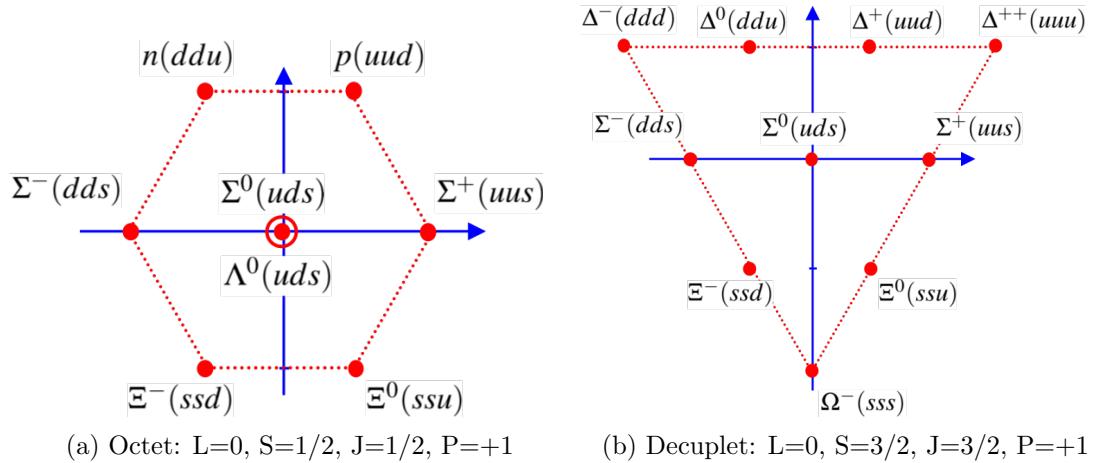


Figure 2.2: Baryon multiplets predicted by SU(3) flavor symmetry within the quark model. [6]

2.4 Electroweak Theory

The electroweak theory provides a unified and self-consistent description of both the electromagnetic and weak forces. The complete theory is generated by demanding local invariance of the Lagrangian under a combined $SU(2) \times U(1)$ symmetry. The $SU(2)$ invariance requires the addition of three new vector bosons, two of which are used to construct the physical W^\pm bosons responsible for the weak *charged current* interactions. An additional gauge boson is required for the $U(1)$ symmetry. A mixing between the remaining (neutral) $SU(2)$ gauge field and the $U(1)$ gauge field yield the Z boson and photon, responsible for weak *neutral current* and electromagnetic interactions, respectively.

Consider the following $U(1)$ transformation on a fermion ψ , and $SU(2)$ transformation on an *isospin doublet* Ψ :

$$\begin{aligned} \psi(x) &\xrightarrow{U(1)} e^{ig' \frac{Y}{2} \alpha(x)} \psi(x) \\ \Psi(x) &\xrightarrow{SU(2)} e^{ig_W \xi(x) \cdot \frac{1}{2} \boldsymbol{\sigma}} \Psi(x) \end{aligned} \quad (2.9)$$

where g' is the hypercharge coupling constant, Y is the hypercharge operator, g_W is the weak coupling constant, α and ξ are arbitrary functions of spacetime, and $\boldsymbol{\sigma}$ represents the three 2×2 Pauli spin matrices.

As usual, $SU(2)$ and $U(1)$ gauge-invariance requires us to modify the definition of the partial derivative to include three spin-1 vector fields \mathbf{W}^μ and a single spin-1 vector field \mathbf{B}^μ :

$$\begin{aligned} \partial_\mu &\rightarrow \partial_\mu - ig' \frac{Y}{2} \mathbf{B}_\mu - ig_W \frac{1}{2} \boldsymbol{\sigma} \cdot \mathbf{W}_\mu \\ \mathbf{B}_\mu &\xrightarrow{U(1)} \mathbf{B}_\mu - ig' \partial_\mu \alpha \\ \mathbf{W}_\mu^k &\xrightarrow{SU(2)} \mathbf{W}_\mu^k - g_W \partial_\mu \xi^k - g_W \epsilon_{ijk} \xi^i \mathbf{W}_\mu^j \end{aligned} \quad (2.10)$$

where ϵ_{ijk} is the totally antisymmetric Levi-Civita tensor (the structure constants of $SU(2)$).

The charged current interaction connects two elements within an isospin doublet Ψ ; by convention, the upper element has electric charge +1 relative to the lower element. There are doublets that connect the leptons with a corresponding neutrino (massless spin-1/2 particle), and there are

doublets that connect an 'up-type' quark (top entry of the doublet) to a 'down-type' quark (bottom entry):

$$\begin{pmatrix} \nu_e \\ e^- \end{pmatrix}, \begin{pmatrix} \nu_\mu \\ \mu^- \end{pmatrix}, \begin{pmatrix} \nu_\tau \\ \tau^- \end{pmatrix}, \begin{pmatrix} u \\ d' \end{pmatrix}, \begin{pmatrix} c \\ s' \end{pmatrix}, \begin{pmatrix} t \\ b' \end{pmatrix}$$

As Nature has it, the weak force is a *chiral* theory, which does not treat the left and right-chiral components of a Dirac fermion on equal footings. The projection operator $P_{R/L} = \frac{1}{2}(1 \pm \gamma^5)$ is used to define these left and right chiral states. All Dirac fermions can be decomposed as $\psi = \psi_L + \psi_R$ using these operators. In the Standard Model, only left-handed particle and right-handed antiparticle states enter into the isospin doublets participating in the electrically-charged weak interaction. This is summarized in Table 2.1.

Because of the SU(2) symmetry and doublet nature, we must introduce **two** fermions to the theory, where the left and right chiral components may transform differently under gauge interactions. Consider fields χ and τ ; the left handed components are members of an isospin doublet $\bar{\psi}_L = (\bar{\chi}_L, \bar{\tau}_L)$, and all components participate in the U(1) transformation. The complete electroweak Lagrangian becomes:

$$\begin{aligned} \mathcal{L}_{\text{EWK}} = & i\bar{\chi}\gamma^\mu\partial_\mu\chi - m\bar{\chi}\chi + i\bar{\tau}\gamma^\mu\partial_\mu\tau - m\bar{\tau}\tau - \frac{1}{4}B_{\mu\nu}B^{\mu\nu} - \frac{1}{4}\mathbf{W}_{\mu\nu}\cdot\mathbf{W}^{\mu\nu} \\ & - g'\bar{\chi}\gamma^\mu\frac{Y}{2}\chi B_\mu + g'\bar{\tau}\gamma^\mu\frac{Y}{2}\tau B_\mu - g_W\bar{\psi}_L\gamma^\mu\boldsymbol{\sigma}\psi_L \cdot \mathbf{W}_\mu \end{aligned} \quad (2.11)$$

Mass terms of the form $\frac{1}{2}m^2A^\mu A_\mu$ are forbidden as they are not invariant under the transformation rule; the **W** bosons remain massless.

2.4.1 The Higgs Mechanism

The gauge bosons responsible for the electroweak force have observationally been determined to have mass, which is a problem as the SU(2) gauge symmetry requires them to be massless. Surely there must be some mechanism that can be introduced to achieve this, while (at least initially) preserving the $SU(2)\times U(1)$ symmetry. The *Higgs field* is introduced to generate mass terms for

the electroweak gauge bosons. The Higgs mechanism proceeds by introducing a massive spin-0 complex scalar field with the following Lagrangian:

$$\mathcal{L} = \frac{1}{2}(\partial_\mu\phi^\dagger)(\partial^\mu\phi) - \frac{1}{2}\mu^2\phi^\dagger\phi + \lambda(\phi^\dagger\phi)^2, \quad (2.12)$$

where μ and λ are the strengths of the self-coupling terms.

Within the SM, the field is implemented as an isospin doublet consisting of electrically neutral and charged components:

$$\phi = \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix} = \begin{pmatrix} \phi_1 + i\phi_2 \\ \phi_3 + i\phi_4 \end{pmatrix}, \quad (2.13)$$

Solving for the minimum of the potential, it is found that the ground state of ϕ is non-zero and satisfies $\phi^\dagger\phi = \phi_1^2 + \phi_2^2 + \phi_3^2 + \phi_4^2 = -\mu^2/2\lambda = \frac{1}{2}v^2$. This is called *spontaneous symmetry breaking* — the Higgs field acquires a *vacuum expectation value* v . Perturbation theory of interactions represent particles as fluctuations about the ground state; we must express the fields in the same manner. Electric charge conservation requires that this vacuum expectation value lie entirely inside the neutral ϕ^0 . The ground state is expressed as:

$$\phi = \begin{pmatrix} 0 \\ v + h(x) \end{pmatrix}, \quad (2.14)$$

where $h(x)$ is identified as the Higgs boson.

If we substitute the ground-state expansion of ϕ to the Lagrangian of Equation 2.12, we obtain the following expression:

$$\mathcal{L} = \frac{1}{2}(\partial^\mu h)(\partial_\mu h) - \lambda v^2 h^2 - \lambda v h^3 - \frac{1}{4}\lambda h^4 + \lambda v^4, \quad (2.15)$$

where we see that we have generated a mass term $m_h = \sqrt{2\lambda}v$ for the Higgs boson. Additionally, there are now 3 and 4-point Higgs self-couplings.

2.4.1.1 Masses of the \mathbf{W}^\pm and \mathbf{Z} bosons

The kinetic energy term $\frac{1}{2}(\partial_\mu\phi^\dagger)(\partial^\mu\phi)$ for the Higgs field introduces a coupling with the \mathbf{W}^μ and \mathbf{B}^μ bosons when they are added to the covariant derivative:

$$\partial_\mu\phi = \left(\frac{1}{2}\partial_\mu + \frac{1}{2}ig_W\boldsymbol{\sigma} \cdot \mathbf{W} + ig'\frac{Y}{2}\mathbf{B}^\mu \right) \begin{pmatrix} 0 \\ v + h(x) \end{pmatrix} \quad (2.16)$$

After performing the matrix calculations, and lots of algebra, there are terms that are quadratic in the gauge fields:

$$\frac{1}{8}v^2g_W^2(W_\mu^1W_1^\mu + W_\mu^2W_2^\mu) + \frac{1}{8}v^2(g_WW_\mu^3 - g'B_\mu)(g_WW_3^\mu - g'B^\mu), \quad (2.17)$$

where we see we have generated mass terms for the W_1^μ and W_2^μ fields: $m_W = \frac{1}{2}vg_W$.

The W^1 and W^2 gauge fields correspond to the first two Pauli matrices; appropriate linear combinations of these two fields therefore define raising and lowering operators that transform elements within a doublet. The physical W^\pm bosons are the following linear combinations of the two gauge fields:

$$W_\mu^\pm = \frac{1}{\sqrt{2}}(W_\mu^1 \mp iW_\mu^2); \quad \text{with mass } \frac{1}{2}vg_W \quad (2.18)$$

The last term in the expansion introduces mixed couplings between the electrically neutral and massless W_3^μ and B^μ fields. The mixing can be represented via a non-diagonal mass matrix. Physical particles propagate as independent eigenstates of the free particle Hamiltonian and therefore we must find the basis in which this matrix is diagonal. Upon diagonalization, we find the states corresponding to these eigenvalues:

$$\begin{aligned} A_\mu &= \frac{1}{\sqrt{g_W^2+g'^2}}(g'W_\mu^3 + g_WB_\mu); \quad \text{with mass } 0 \\ Z_\mu &= \frac{1}{\sqrt{g_W^2+g'^2}}(g_WW_\mu^3 - g'B_\mu); \quad \text{with mass } \frac{1}{2}v\sqrt{g_W^2+g'^2} \end{aligned} \quad (2.19)$$

where A_μ corresponds to the photon of electromagnetism, and Z_μ the neutral gauge boson responsible for the weak neutral currents.

We have seen how the Higgs mechanism is able to generate mass terms for the gauge bosons in the electroweak theory.

2.4.1.2 Masses of the Fermions

It has not been mentioned that the fermion mass terms $-m\bar{\psi}\psi = -m(\bar{\psi}_R\psi_L + \bar{\psi}_L\psi_R)$ are in fact forbidden within the SM — the chiral nature of SU(2) treats the two chiral states differently and therefore this term is not invariant under the transformation rules. Masses for the fermions are created by introducing *Yukawa interactions* with the Higgs field. Consider the following terms, which are invariant under the $U(1) \times SU(2)$ transformation,:

$$\begin{aligned} \mathcal{L} &= -y[\bar{\psi}_L \phi \psi_R + h.c.] \\ &= -y \left[\begin{pmatrix} \bar{\nu}, \bar{\ell} \end{pmatrix}_L \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix} \ell_R + \bar{\ell}_R \begin{pmatrix} \phi^{+*}, \phi^{0*} \end{pmatrix} \begin{pmatrix} \nu \\ \ell \end{pmatrix}_L \right] \end{aligned} \quad (2.20)$$

where y is the *Yukawa coupling*, $\bar{\psi}_L$ is an isospin doublet of left-chiral fermions, and ψ_R is a right-chiral fermion.

After spontaneous symmetry breaking, this reduces to:

$$\begin{aligned} \mathcal{L} &= -\frac{1}{\sqrt{2}}yv(\bar{\ell}_L \ell_R + \bar{\ell}_R \ell_L) - \frac{1}{\sqrt{2}}yh(\bar{\ell}_L \ell_R + \bar{\ell}_R \ell_L) \\ &= -\frac{1}{\sqrt{2}}yv\bar{\ell}\ell - \frac{1}{\sqrt{2}}yh\bar{\ell}\ell \end{aligned} \quad (2.21)$$

and we see we have obtained a mass term for the fermion $m_\ell = \frac{1}{\sqrt{2}}yv$ and an interaction term $\frac{1}{\sqrt{2}}yh\bar{\ell}\ell$ between the fermion in the lower member of the isospin doublet and a single Higgs boson.

To generate a mass term for the upper component of the isospin doublet we need to follow the same prescription but with the *conjugate* Higgs field:

$$\phi_c = -i\sigma_2\phi^* = \begin{pmatrix} -\phi^{0*} \\ \phi^- \end{pmatrix} = \frac{1}{\sqrt{2}} \begin{pmatrix} -\phi_3 + i\phi_4 \\ \phi_1 - i\phi_2 \end{pmatrix}, \quad (2.22)$$

where the same story plays out.

2.4.2 Quark Mixing: the CKM Matrix

As seen at the beginning of this section, the charged weak current acts on isospin doublets connecting quarks of flavor eigenstates, labeled as u , d' , s' , c , b' , t . As Nature has it, these are not the same as the mass eigenstates of the free-particle Hamiltonian, labeled as u , d , s , c , b , t . This introduces mixing between these two bases and is represented by the *Cabibo-Kobayashi-Maskawa matrix*. The probability of a transition between two states is proportional to the square of a matrix element $|V|^2$ in the matrix. It is a unitary 3×3 matrix with 4 independent terms (3 amplitudes and 1 phase).

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix} \quad (2.23)$$

The best estimate of these parameters [7] are:

$$\begin{pmatrix} |V_{ud}| & |V_{us}| & |V_{ub}| \\ |V_{cd}| & |V_{cs}| & |V_{cb}| \\ |V_{td}| & |V_{ts}| & |V_{tb}| \end{pmatrix} \approx \begin{pmatrix} 0.974 & 0.225 & 0.004 \\ 0.224 & 0.974 & 0.042 \\ 0.009 & 0.041 & 0.999 \end{pmatrix} \quad (2.24)$$

2.4.3 Brief Electroweak Summary

We started with a theory of two fields each governed by the Dirac equation. We demanded that the theory be gauge-invariant under combined $U(1) \times SU(2)$ symmetry operations. The gauge bosons are required to be massless as their transformation rules do not allow their kinetic energy term to be invariant. The Higgs field was introduced, the action of the covariant derivative on the Higgs field generates an interaction term between the gauge bosons and the Higgs field. The Higgs field obtained a vacuum expectation value, and re-expressing the field about this ground state led us to mass terms for the gauge bosons. The physical W^\pm and Z bosons become mixtures of these states. Fermion mass terms are not initially allowed as the chiral $SU(2)$ symmetry treats the left and

right components differently and therefore they cannot remain invariant. Fermion mass terms are generated by introducing Yukawa interactions between the Higgs field and fermions, which generate appropriate mass terms after the Higgs field expansion about the ground state. In addition, under the charged-current interaction, quark flavor and mass eigenstates are not the same, this introduces the CKM matrix parametrizing the mixing.

2.5 Parameters of the Standard Model

There are 18 parameters that must be specified as an input to the SM — these must all be determined experimentally:

- 9 quark and lepton masses: $m_u, m_d, m_s, m_c, m_b, m_t, m_e, m_\mu, m_\tau$, with the values listed in Figure 1.1. (Alternatively these can be expressed as the 9 appropriate Yukawa couplings $y_f = \sqrt{2}m_f/v$)
- 4 parameters describing the mixing between quark mass and flavor eigenstates (CKM matrix, see Equations 2.23 and 2.24): often parametrized as λ, A, ρ, η
- 2 parameters for the Higgs field: mass and vacuum expectation value $m_H = 125$ GeV, $v = 246$ GeV
- 3 coupling constants for the relative strengths of the gauge group:

$$\begin{aligned}\alpha &\equiv e^2/4\pi, & \alpha(q^2 \approx 0) &= 1/137.0 \\ \alpha_s &\equiv g_s^2/4\pi, & \alpha_s(q^2 = m_Z^2 = (91 \text{ GeV})^2) &= 0.1184 \pm 0.0007 \\ G_F &\equiv \sqrt{2}g_W^2/8m_W^2, & G_F(q^2 \approx 0) &= 1.1663787 \times 10^{-5} \text{ GeV}^2\end{aligned}$$

2.6 Neutrino Mass

Within the 'canonical' SM the neutrinos are assumed to be massless spin-1/2 fermions. In the last decade, experiments have shown that neutrinos go through *flavor oscillations* wherein they

change flavor as they propagate through space. This flavor oscillation is dependent on **massive** neutrinos and can be described by a mixing among the mass and flavor eigenstates. The mixing is described by a 3x3 unitary matrix known as the *PMNS matrix* (analogous to the CKM matrix). One could consider giving the neutrinos a Yukawa coupling with the Higgs and give them a Dirac mass $-m\bar{\nu}\nu = -m(\bar{\nu}_R\nu_L + m\bar{\nu}_L\nu_R)$, but the non-observation of right-handed neutrinos does not allow that approach. The correct implementation of the neutrino mass is still an open question in the field. The currently known estimates for their masses are seen in Figure 1.1.

The neutrino mass sector possibly adds an additional 7 parameters [8] to the SM:

- 3 neutrino masses: $m_{\nu_1}, m_{\nu_2}, m_{\nu_3}$
- 4 parameters describing the mixing among the neutrino mass and flavor eigenstates (PMNS matrix): often parameterized as $\theta_{12}, \theta_{13}, \theta_{23}, \delta$.

Chapter 3

The Minimal Supersymmetric Model

In addition to the $SU(3) \times SU(2) \times U(1)$ symmetry imposed on the Lagrangian within the Standard Model, one can introduce additional *supersymmetries* to the theory. Supersymmetry transformations act on fields containing both fermionic and bosonic degrees of freedom, the Lagrangian being required to remain invariant under rotations between these two states. Many such extensions to the Standard Model exist, but the Minimal Supersymmetric Standard Model (MSSM) is the simplest of such cases as it only considers a single global transformation Q .

Within the MSSM, every SM particle has a *superpartner* that differs by 1/2 unit of spin but otherwise has identical properties. For example, the electron is paired with an electrically charged, massive, spin-0 scalar field, called a “selectron”. A striking prediction of the MSSM is more than a doubling of the known particle content of the Universe (there are more than one supersymmetric Higgs bosons in the MSSM). In addition to the single SM Higgs doublet, the MSSM requires another spin-0 Higgs isospin doublet, with opposite hypercharge. Each of these two spin-0 doublets has its own chiral superpartner. Table 3.1 lists the fields required within the MSSM (the sort of complement of Table 2.1). As the nature of the newly supersymmetric electroweak sector is unknown, the various components of the fields may mix. The charged components from the new $SU(2)$ fields and the Higgs are summarized in Table 3.2 (color charge prevents gluinos from mixing outside QCD). This chapter is adapted from [9].

Matter particles (both the left and right-chiral components separately) are placed in *chiral supermultiplets* consisting of a spin-1/2 Majorana fermion ψ and complex scalar field ϕ . In the

Table 3.1: Summary of the additional particle content within the MSSM.

SM Gauge Sector	sfermions	gauginos
SU(3)	$\tilde{u}, \tilde{d}, \tilde{c}, \tilde{s}, \tilde{t}, \tilde{b}$	$\tilde{g}_{1\ldots 8}$
SU(2) \times U(1)	$\tilde{Q}_L = \begin{pmatrix} \tilde{u} \\ \tilde{d} \end{pmatrix}_L, \begin{pmatrix} \tilde{s} \\ \tilde{c} \end{pmatrix}_L, \begin{pmatrix} \tilde{t} \\ \tilde{b} \end{pmatrix}_L$ $\tilde{q} = \tilde{u}, \tilde{d}, \tilde{c}, \tilde{s}, \tilde{t}, \tilde{b}$ $\tilde{L}_L = \begin{pmatrix} \tilde{\nu}_e \\ \tilde{e}^- \end{pmatrix}_L, \begin{pmatrix} \tilde{\nu}_\mu \\ \tilde{\mu}^- \end{pmatrix}_L, \begin{pmatrix} \tilde{\nu}_\tau \\ \tilde{\tau}^- \end{pmatrix}_L$ $\tilde{\ell} = (\tilde{e}, \tilde{\mu}, \tilde{\tau})$	$\widetilde{W}_{012}, \widetilde{B}_0$
Higgs Sector	spin-0 $H_u = \begin{pmatrix} H_u^+ \\ H_u^0 \end{pmatrix}, H_d = \begin{pmatrix} H_d^0 \\ H_d^- \end{pmatrix}$	spin-1/2 $\tilde{H}_u = \begin{pmatrix} \tilde{H}_u^+ \\ \tilde{H}_u^0 \end{pmatrix}, \tilde{H}_d = \begin{pmatrix} \tilde{H}_d^0 \\ \tilde{H}_d^- \end{pmatrix}$

Table 3.2: Mixing of the supersymmetric electroweak fields.

name	gauge states	mass eigenstates
neutralinos	$\tilde{H}_u^0 \leftrightarrow \tilde{H}_d^0 \leftrightarrow \widetilde{W}^0 \leftrightarrow \widetilde{B}^0$	$\tilde{\chi}_1^0, \tilde{\chi}_2^0, \tilde{\chi}_3^0, \tilde{\chi}_4^0$
charginos	$\tilde{H}_u^+ \leftrightarrow \tilde{H}_d^- \leftrightarrow \widetilde{W}^+ \leftrightarrow \widetilde{W}^-$	$\tilde{\chi}_1^\pm, \tilde{\chi}_2^\pm$
neutral Higgs	$H_u^0 \leftrightarrow H_d^0$	h^0, H^0, A^0
charged Higgs	$H_u^+ \leftrightarrow H_d^-$	H^\pm

massless and non-interacting case (i.e. just the two kinetic terms in the Lagrangian, known as the *Wess-Zumino model* [10]), the transformation laws of the fields can be deduced by demanding invariance of the (simple) Lagrangian under the supersymmetry transformation, and are:

$$\begin{aligned}\phi &\xrightarrow{\text{Q}} \phi + \epsilon\psi, \text{ and} \\ \psi &\xrightarrow{\text{Q}} \psi - i(\sigma^\mu\epsilon^\dagger)\partial_\mu\phi,\end{aligned}\tag{3.1}$$

where ϵ is a 2-component Weyl **spinor** parametrizing the transformation. For the duration of this chapter, all references to *auxiliary* fields will be omitted. Auxiliary fields are internal to the theory and must be introduced to allow the fields to satisfy their classical wave equations.

The requirement of renormalizability restricts the numbers of fields in any interaction involving ψ and ϕ . The most generic Lagrangian for a chiral supermultiplet is of the form:

$$\mathcal{L}_{chiral} = -D^\mu\phi^*D_\mu\phi - V(\phi, \phi^*) + i\psi^\dagger\bar{\sigma}^\mu D_\mu\psi - \frac{1}{2}(M\psi\psi + h.c.) - \frac{1}{2}(y\phi\psi\psi + h.c.),\tag{3.2}$$

where D^μ is the covariant derivative, $V(\phi, \phi^*)$ is a scalar potential for the theory, $\bar{\sigma}^0$ is the 2x2 identity matrix and $\bar{\sigma}^{123} \equiv -\sigma^{123}$, M is a (Majorana) mass term, $\psi\psi \equiv \epsilon^{ab}\psi_a\psi_b$, and y is a Yukawa coupling. The Yukawa coupling connects two SM fermions with the corresponding supersymmetric scalar field - a vertex diagram for this process is seen in Figure 3.1(a). The covariant derivative $D_\mu\phi = \partial_\mu\phi - igA_\mu^aT^a\phi$, when introduced in the kinetic term, creates two interactions between the SM gauge bosons and the new supersymmetric scalar field: $-ig[(\partial_\mu\phi)A_\mu^aT^a\phi + h.c.]$ and $g^2A^{a\mu}\phi^*t^aA_\mu^aT^a\phi$, seen in Figures 3.1(b, c), respectively.

Gauge bosons (before spontaneous symmetry breaking) are placed in *gauge supermultiplets* consisting of gauge bosons A_μ^a and spin-1/2 gauginos λ^a ; a is a label which runs over the SM gauge fields within the theory. Under the supersymmetry, fields can be found to transform as:

$$\begin{aligned}A_\mu^a &\xrightarrow{\text{Q}} A_\mu^a - \frac{1}{\sqrt{2}}(\epsilon^\dagger\bar{\sigma}_\mu\lambda + h.c) \\ \lambda_\alpha^a &\xrightarrow{\text{Q}} \lambda_\alpha + \frac{i}{2\sqrt{2}}(\sigma^\mu\bar{\sigma}^\nu\epsilon)F_{\mu\nu}^a\end{aligned}\tag{3.3}$$

where $F_{\mu\nu}^a$ is the regular field strength tensor for the gauge field A_μ^a . The SM symmetries (i.e. SU(3), SU(2), U(1)) transform the gauge supermultiplet in the following way:

$$\begin{aligned} A_\mu^a &\xrightarrow{\text{SM}} A_\mu^a + \partial_\mu \Lambda^a + g f^{ijk} A_\mu^b \Lambda^c \\ \lambda^a &\xrightarrow{\text{SM}} \lambda^a + g f^{abc} \lambda^b \Lambda^c \end{aligned} \quad (3.4)$$

where Λ^a is a parameter describing the transformation. (The transformation law for A^μ is the same as we have seen in Chapter 2.)

The Lagrangian for a free gauge multiplet consists simply of the kinetic terms for each field A_μ^a and λ^a :

$$\mathcal{L}_{gauge} = -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} + i \lambda^\dagger \bar{\sigma}^\mu \nabla^\mu \lambda^a \quad (3.5)$$

where f^{abc} are the structure constants of the gauge group. $\nabla \lambda^a = \partial_\mu \lambda^a + g f^{abc} A_\mu^b \lambda^c$ represents the covariant derivative acting on λ^a , creating an interaction term between a gauge boson and two gauginos: $i g \lambda^\dagger \bar{\sigma}^\mu f^{abc} A_\mu^b \lambda^c$, as seen in Figure 3.1(d).

The requirement of renormalization restricts the interactions between the gauge and chiral supermultiplets to be only of the form $-\sqrt{2}g(\phi^* T^a \psi \lambda^a + h.c.)$, involving a single spin-0, spin-1/2, and spin-1 particle; this vertex is seen in Figure 3.1(e).

Within a supersymmetric theory, the superpartners are required to have the same masses as their corresponding SM fields. If SUSY were exact, we would have expected to see evidence of sparticles over the years. There must be some mechanism that generates large mass for the sparticles such that their production is highly suppressed at our colliders. The remainder of this thesis presents a search for evidence of physics beyond the SM, such as the MSSM. Our motivation is taken from final state topologies arising from gluino pair production, as seen in Figure 3.2. The gluino is the spin-1/2 fermion that is the superpartner to the gluon, the mediator of the strong force.

Within the context of QCD the chiral supermultiplets consist of spin-1/2 quarks and spin-0 squarks. Searches for supersymmetric particles of QCD are partly motivated by the fact that most of their production mechanisms proceed through diagrams proportional to the strong coupling

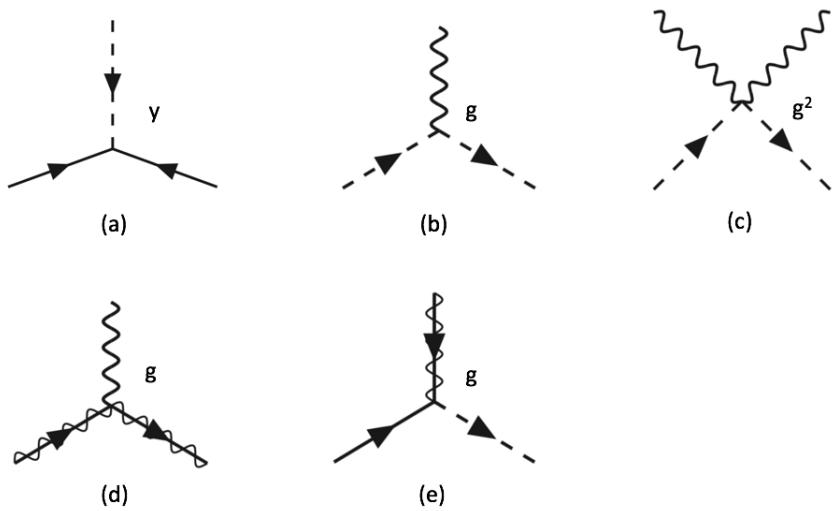


Figure 3.1: MSSM vertices coupling SM and supersymmetric particles. The dashed lines and solid lines represent spin-0 and spin-1/2 particles residing in a chiral multiplet, respectively. The lasagne lines and struck-through lasagne lines represent spin-1 and spin-1/2 particles residing in a gauge supermultiplet, respectively. y is a Yukawa coupling to be determined, g is the SM gauge coupling.

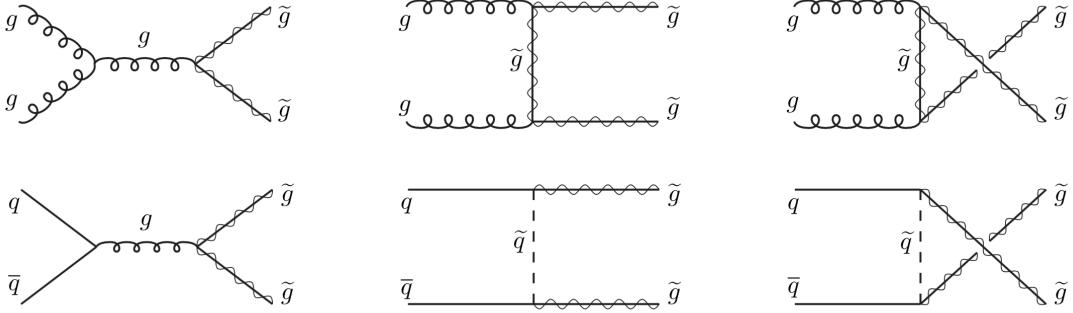


Figure 3.2: Tree-level gluino pair-production mechanisms.

constant g_s , which is largest among the three in the SM. The supersymmetric partners of QCD necessarily carry color charge, and therefore the QCD squarks and gluinos do not directly interact with other MSSM particles. There have been many searches for SUSY that provide lower limits on the mass of the gluino, such as [11, 12]. An example is seen in Figure 3.3, setting a lower bound at about 1.8 TeV, given assumptions about the decay (seen in the diagram below the plot). The blob in the diagrams below the limit plots indicates we are not interested in the particular production mechanism, but in the decay chain.

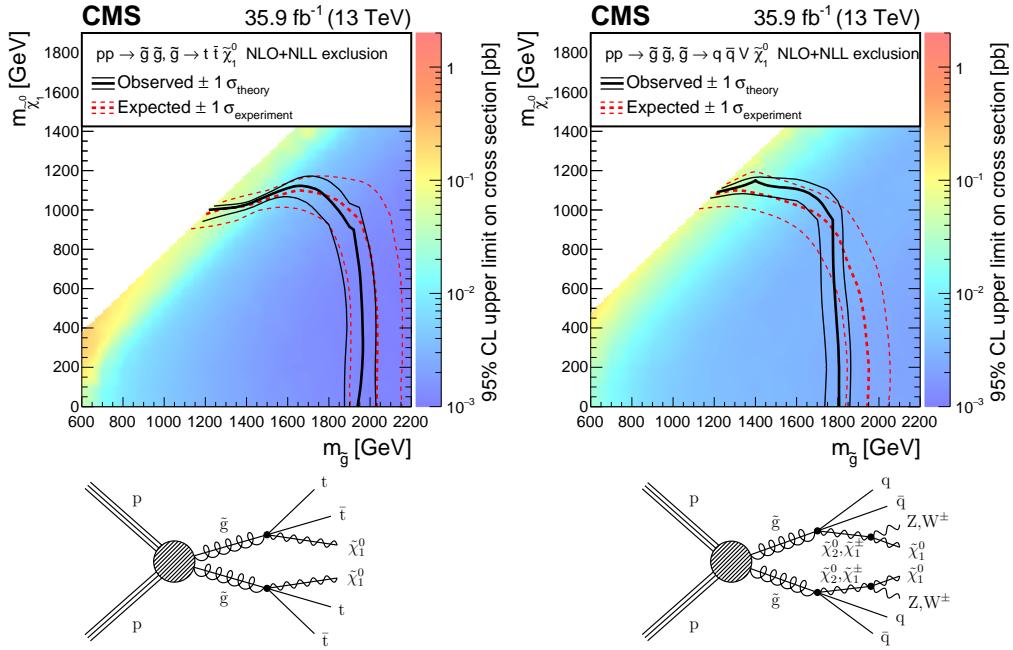


Figure 3.3: Previous results for searches of gluino-mediated supersymmetry for the T1tttt (left) and T1qqqqVV (right) models [11]. The x and y axes correspond to the mass of the gluino and LSP, respectively. The temperature corresponds to the upper limit which is set on the cross section at 95% confidence, for that mass point. Assuming the MSSM, the mass region excluded by the analysis lies to the lower-left of the central black curve. The exclusion expected assuming the background only hypothesis lies to the bottom-left of the central dashed-red line.

Chapter 4

The Large Hadron Collider

The Large Hadron Collider (LHC) [13] is a particle accelerator capable of creating the most energetic (man-made) collisions of particles to date . The LHC is housed within a tunnel 27 km in circumference and 100 m underground, at the European Organization for Nuclear Research (CERN) site near Geneva, Switzerland. Two beampipes, 5.6 cm in diameter, contain protons circulating in opposite directions around the LHC tunnel. Over 1200 superconducting dipole magnets, 15 m in length and providing a field strength up to 8.3 T, are placed along the beamline to guide the protons within the circular trajectory. Radio-frequency electric fields are used to accelerate the particles to nearly the speed of light.

Before the protons are stored in the LHC ring, they must first make their way through a number of stages which comprise the CERN accelerator complex. The proton source is a simple bottle of hydrogen gas. A large electric field is used to ionize the gas, and the protons are fed into a linear accelerator (Linac 2) which increases their energy to 50 MeV. These protons subsequently are fed through three synchrotrons: Proton Synchrotron Booster, Proton Synchrotron, and Super Proton Synchrotron, where the proton beam energy is increased to 1.5, 25, and 450 GeV, respectively. After the Super Proton Synchrotron, the beamlines of the LHC are filled and further accelerated, resulting in two counter-propagating beams of 6.5 TeV each. Figure 4.1 is a diagram of the entire CERN complex. As can be seen, the accelerator complex is rich with activity. Table 4.1 is a summary of the successive stages relevant in the beam development.

At four points around the ring, magnets are used to further confine and direct each of the

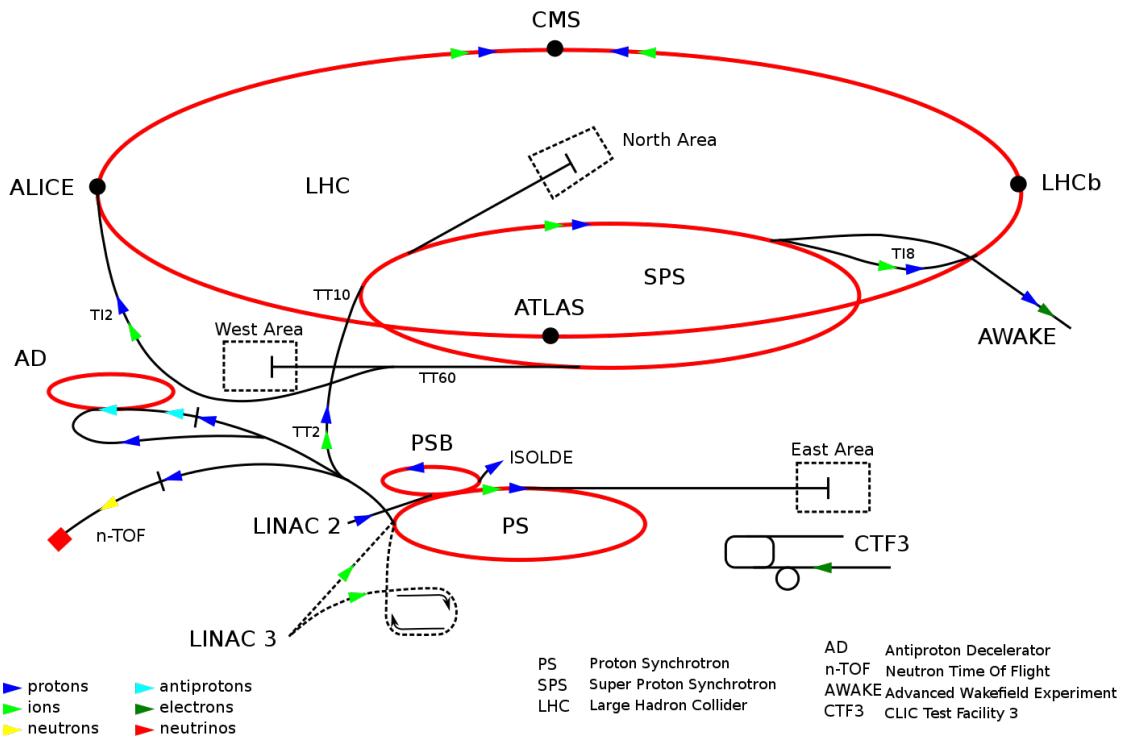


Figure 4.1: The CERN accelerator complex. [14]

Table 4.1: The stages of proton beam acceleration for the LHC at CERN.

stage	final energy
bottle of hydrogen gas	...
Linac 2	50 MeV
Proton Synchrotron Booster	1.5 GeV
Proton Synchrotron	25 GeV
Super Proton Synchrotron	450 GeV
LHC	6.5 TeV

two (counter-rotating) beams at one another. At each of these interaction points, there is a large detector placed to capture the remnants of the collisions. These detectors are named CMS, LHCb, ATLAS, and ALICE, and labeled as such in Figure 4.1. CMS and ATLAS are considered “general-purpose” detectors striving to surround the interaction region as much as possible, allowing the reconstruction of a wide variety of particles and the full event. The LHCb detector instruments the forward region that is specialized in reconstructing events containing b hadrons. The ALICE detector is specifically designed to record events from heavy-ion collisions.

A measure of the rate of particle collisions produced at a collider is given by the *instantaneous luminosity*. It relates the cross section probability (σ) for some interaction to occur with the expected numbers of events N of that type over some time period: $N = \sigma \int \mathcal{L}(t)$. It is an important parameter of an accelerator as it dictates how many proton interactions can be made within a given amount of time, dictating the total amount of data available. In general, the luminosity is dependent on the size and shape of each of the beams, the number of protons in each beam $n_{1,2}$, and how frequently they can be made to interact at the LHC. The instantaneous luminosity can be written as:

$$\mathcal{L} = f \frac{n_1 n_2}{4\pi \sigma_x \sigma_y} \quad (4.1)$$

where f is the collision frequency, and σ_x, σ_y are the effective transverse widths of the beams.

In the LHC, the protons within each beam are arranged in 2808 bunches about 30 cm long containing 10^{11} protons each (n_1, n_2) (arranged in this manner by the radiofrequency chambers). At each of the interaction points, the bunches are steered into one another every 25 ns ($f = 40\text{ MHz}$). Although there are many protons within each bunch, on average there are only about 25 proton-proton interactions per crossing that can be characterized by a large energy transfer between two partons (i.e. the constituents of the proton: quarks and gluons). Each of these interactions creates its own *vertex* from which tracks are found to emanate, indicating an interaction between two protons. The vertex with the largest outward momentum flux is known as the *primary vertex*, the

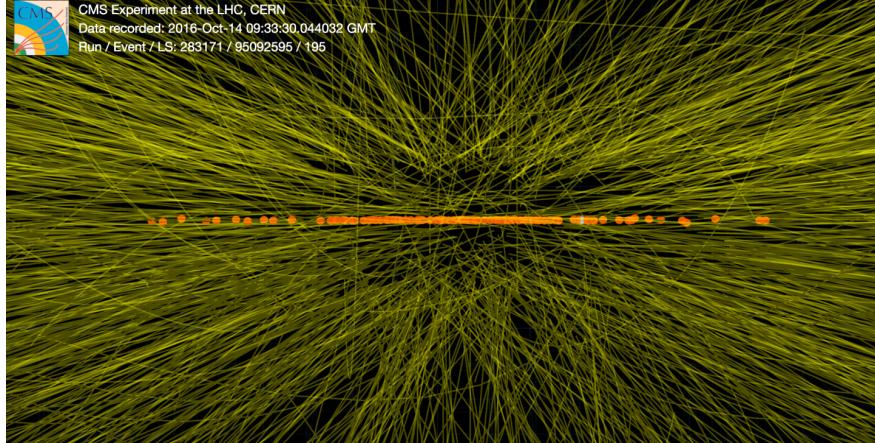


Figure 4.2: An event recorded by the CMS experiment during a high pile-up fill in 2016 [15]. The green lines represent tracks from charged particles. The orange dots represent primary vertices reconstructed from clustering of these tracks. Each dot represents the location of a proton-proton collision.

additional interactions are known as *pileup* and pose a formidable challenge in the reconstruction.

One of the long term goals for the LHC is to increase its instantaneous luminosity leading to a drastic increase in the number of these vertices which must be reconstructed. In Figure 4.2 we see the challenge we already face - an image of an event recorded in 2016. The green lines are tracks, and the orange dots are interaction vertices.

The LHC began taking data in 2009 with a total center-of-mass energy of 900 GeV. The center-of-mass energy of the beam collisions has been increasing over the years, with runs at 7, 8, and now 13 TeV. In coming years the machine is planning to deliver 14 TeV collisions, the design energy. The high performance of the LHC machine has allowed us to take over 150 fb^{-1} of data to date, the record for hadronic machines. Figure 4.3 shows the integrated luminosity collected by the CMS experiment over this time.

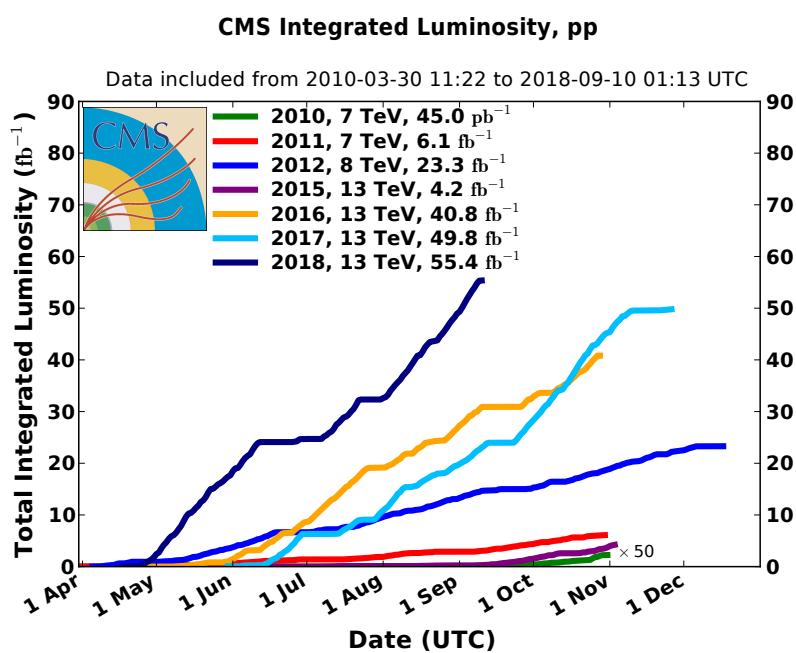


Figure 4.3: The integrated luminosity of CMS as of September 2018.

Chapter 5

The CMS Detector

The CMS experiment is (predominantly) interested in the dynamics of collisions with a very large energy transfer, unveiling quarks and gluons that are within the proton. Large energy transfers are necessary for the creation of massive particles such as the electroweak bosons, or potentially a new particle not within the SM. These collisions result in high-momentum particles produced in directions perpendicular to the beam line, where the components of the CMS detector are carefully arranged. By detecting the outgoing flux from these high-energy events, we are able to reconstruct the dynamics and quantum mechanical processes involved in the proton interactions.

The detector is composed of a modular design of subsystems allowing for measurements of a wide spectrum of particles. As seen in Figure 5.1, these detectors are placed around the interaction point to collect as many of the collision remnants as possible. In this figure, the beam line is seen as a small grey tube extending from the bottom right towards the top left. The interaction point is within the silicon trackers.

Each different system is capable of detecting specific types of particles. A silicon tracker allows for the reconstruction of charged particles traveling at least 50 cm (e.g. electrons e^\pm , charged pions π^\pm); electromagnetic calorimeters measure the energy of electrons and photons γ ; hadronic calorimeters measure the energy of charged and neutral hadrons (e.g. neutrons, π^0 , K_L^0); muon μ^\pm identification is made with gas detectors. The particle identification exploits the unique signature each of these particles leave in our detector. Figure 5.2 illustrates these signatures for some common SM particles.

Many of the particles produced in the interaction are unstable and decay before traveling any appreciable distance in the detector. These particles, such as top quarks, electroweak bosons, and many hadrons, must be reconstructed by the identification of their decay products. For instance, a Z boson may be reconstructed as a pair of oppositely charged muons μ^\pm .

This chapter will discuss the main elements of the CMS detector, beginning with the innermost (closest to the beam pipe) silicon tracker and concluding with the muon system. The detector can generically be divided into central *barrel* and forward *endcap* regions. The geometry either takes the form of concentric cylinders (in the barrel) or flat planes of detectors (in the endcaps). This is most apparent in Figure 5.3, where the beamline is seen as the thin cyan line at the bottom of the image. The origin is defined as the center of the detector. The radial coordinate r is the distance from the beam line, in the transverse plane. The z axis is the direction parallel to the beamline, counterclockwise when viewed from above. The coordinate $\eta \equiv -\tan(\ln \theta/2)$ is used to represent the polar angle above the beamline. The ϕ coordinate is the azimuth angle about the beamline, with $\phi = 0$ aligning with the x-axis pointing towards the center of the LHC ring. The y-axis points up.

5.1 Silicon Tracker

The silicon tracker is responsible for the reconstruction of charged particles (e.g. electrons, muons, kaons, pions, and protons). The particle trajectory is reconstructed using ionization deposits left in layers of thin silicon. The particle momentum is measured by the curvature of the trajectory caused by the magnetic field. The silicon tracker is divided into two major components. The pixel detector is at a closer proximity to the beam line and has finer spatial segmentation. The strips detector covers a much larger spatial volume and is responsible for the majority of the hits along a particle trajectory. [16, 17]. A diagram of the geometry and layers of the tracker is seen in Figure 5.4.

The tracker is built of modules consisting of a layer of sensitive silicon bonded to readout electronics. The silicon is arranged as a p-n junction, reversed-biased and fully-depleted. As a

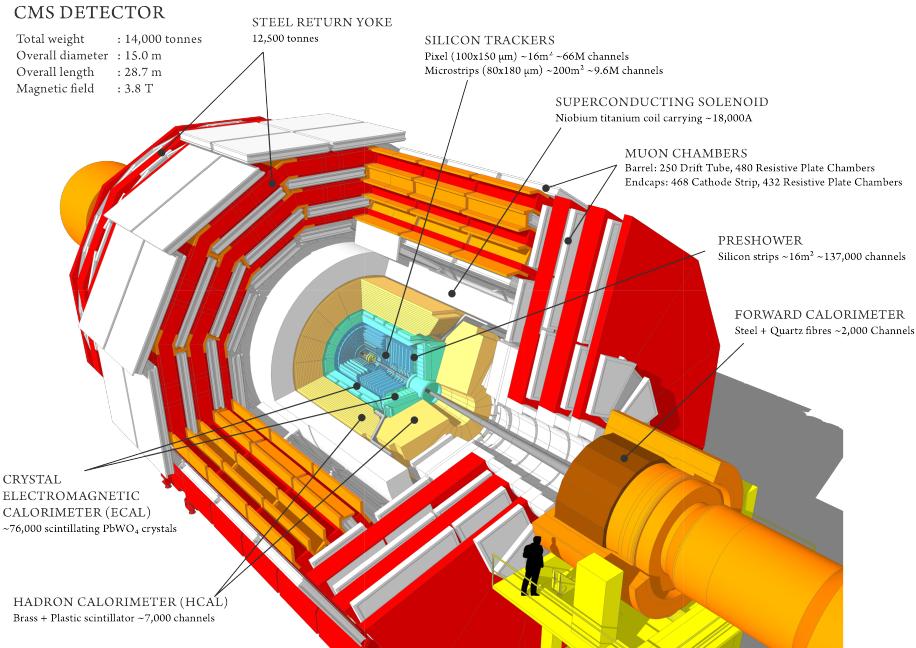


Figure 5.1: A diagram of the CMS detector. Specific detector subsystems are labeled.

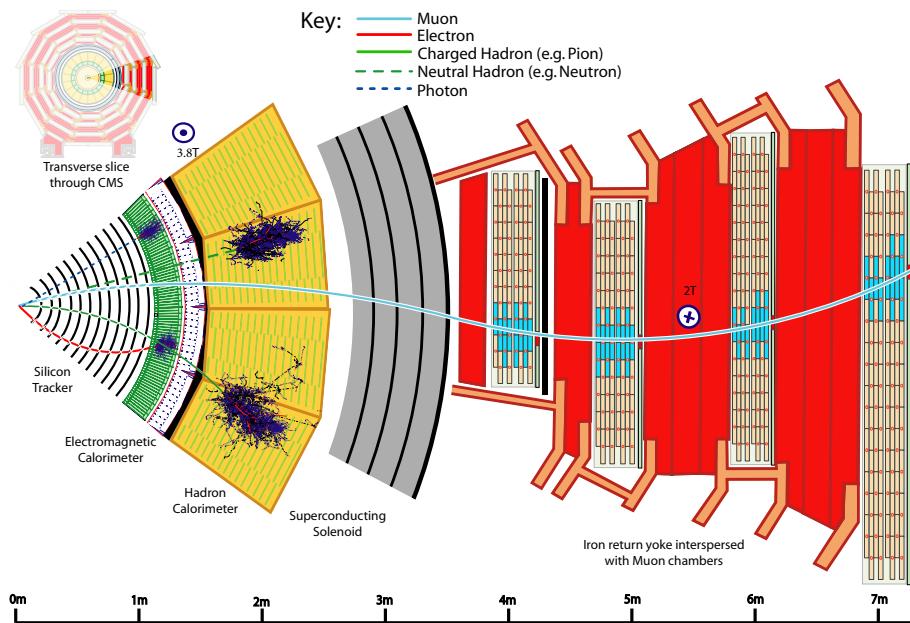


Figure 5.2: A diagram of the CMS detector in the $r-\phi$ plane; the beam axis is perpendicular to the page; SM particle signatures within the detector are shown.

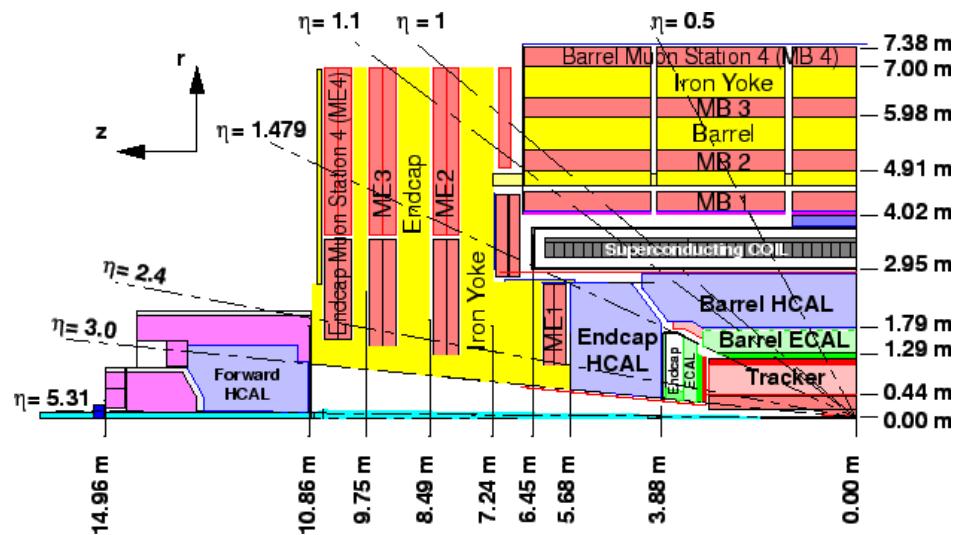


Figure 5.3: A diagram of the CMS detector in the r - z plane; the beampipe is the thin cyan sliver along the bottom. The detector subtends a large solid angle about the interaction region.

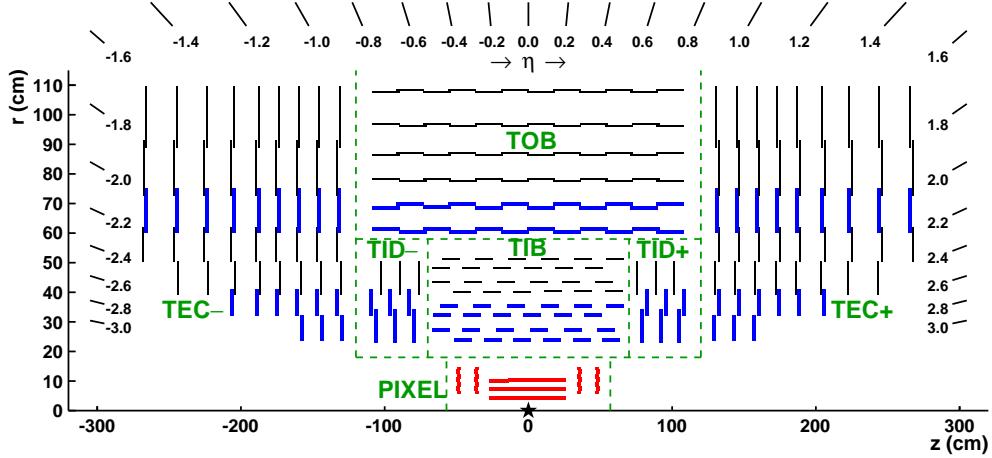


Figure 5.4: The CMS silicon tracker. The vertical and horizontal lines represent layers of silicon modules. Lines in blue represent layers with “stereo” hits, formed from two silicon layers.

charged particle travels through the material, it ionizes the silicon creating electron-hole pairs within the depletion zone. Electric fields accelerate the charge through the silicon to the readout electronics bonded to the back of the sensor. The readout chips amplify, digitize, and store the hit information before it is piped outside the detector. The silicon is very thin ($\sim 300 \mu\text{m}$); the tracker is constructed of as little material as possible so as not to perturb the trajectory of the particle.

5.1.1 Pixel Detector

The task of the pixel detector is to provide the spatial granularity required for precision track vertexing. The barrel region ($|\eta| < 1.5$) of the pixel detector consists of 3 concentric cylinders sitting at radii of 4.4, 7.3, and 10.2 cm from the beamline. The endcaps ($1.5 < |\eta| < 2.5$) consist of two discs on each side placed at $z = \pm 35.5, 48.5$ cm. A pixel module, used to form the detector layers, consists of 16 readout chips glued to a 2×6 cm mechanical support structure. Bump-bonded to the readout chips are the $285 \mu\text{m}$ thick silicon sensors. The readout chips and sensor are divided up into $100 \times 150 \mu\text{m}$ pixels which allow excellent hit resolution. The $100 \mu\text{m}$ lengths are oriented to give the most precise measurement of the ϕ coordinate of the track, as that is the direction of bending due to the magnetic field.

A new pixel detector was installed in 2016 to accommodate the ever-increasing instantaneous

luminosity provided by the LHC [18]. The increase in the luminosity results in many more additional proton-proton interactions per bunch crossing, called *pileup*. High pileup results in a very dense environment for track reconstruction to operate as all the individual hits in the detector layers must be disentangled correctly. To increase the performance, the new detector therefore included **4** layers in the barrel and **3** endcap discs on either end. The readout chip was upgraded to fully digital readout to give larger hit buffers to accommodate the increased hit rate.

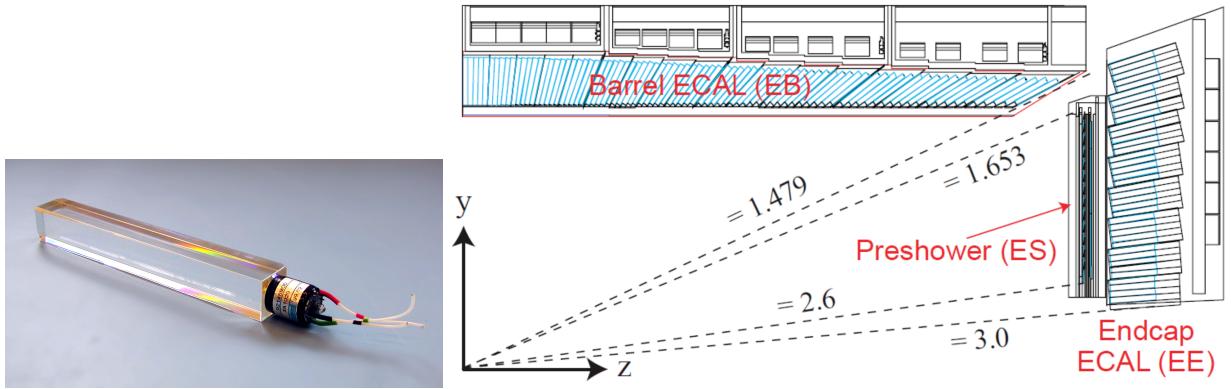
5.1.2 Strips Detector

The silicon strips detector sits immediately outside the pixel detector and provides additional hits along a particle’s trajectory. The barrel region ($|\eta| < 1.5$) provides 10 layers of sensor situated between 20 and 116 cm from the beamline. The endcap regions ($1.5 < |\eta| < 2.5$) have a total of 12 layers situated between 58 and 282 cm from the center of the detector, on each side. The silicon modules are partitioned in roughly 10 cm long strips which are oriented parallel to the beamline. The strip pitch varies from 80–180 μm . The silicon thickness ranges from 320–500 μm . Some of the layers, indicated in the blue lines in Figure 5.4, have two modules which are slightly rotated relative to each other to give a “stereo-hit”, providing a measurement of the z position.

5.2 Electromagnetic Calorimeter

The electromagnetic calorimeter is responsible for the reconstruction of electrons e^\pm and photons γ . The energy is measured by collecting the light generated by an electromagnetic shower as the particle is absorbed in the calorimeter [19, 20].

Electromagnetic showers are created when high energy photons and electrons enter the material comprising the ECAL. The cross section for interactions of these particles with the detector scales with the square of the atomic number, for this reason the material is made of clear PbWO₄ crystals. High energy photons predominantly lose energy by the creation of e^+e^- pairs via interactions with these crystals. High-energy electrons predominantly lose energy through photon radiation as they are scattered within the crystal (bremsstrahlung). An incident particle will there-



(a) A single PbWO_4 crystal attached to a photomultiplier tube. (b) Diagram of the ECAL layout, emphasizing the crystal orientation. A small gap in the η coverage is seen.

Figure 5.5: The CMS electromagnetic calorimeter.

fore cause a shower in the detector as this process evolves. Molecules embedded in the ECAL are activated by the shower and their subsequent decay results in the emission of scintillation light. The light is collected via avalanche photodiodes with a gain of 50 and vacuum phototriodes with a gain of 10 in the barrel and endcap, respectively. The signal is then further amplified and digitized.

The electromagnetic calorimeter is divided into barrel ($|\eta| < 1.5$) and endcap ($1.5 < |\eta| < 3$) regions comprising 75,848 crystals. The crystals measure $2.2 \times 2.2 \times 23 \text{ cm}^3$ in the barrel and $3 \times 3 \times 22 \text{ cm}$ in the endcaps; they are oriented radially outward from the interaction region and capture over 99% of the electromagnetic energy within the shower. A schematic of the detector is seen in Figure 5.5b. Additionally, the electromagnetic calorimeter serves as an absorber for the hadronic calorimeter, initiating a shower in approximately 1/3 of the hadrons that are headed into the HCAL.

5.2.1 Preshower

The Preshower is an additional detector which allows for greater spatial hit resolution of calorimeter clusters in the $1.7 < |\eta| < 2.6$ region. Placed in front of the crystal calorimeter, it consists of a lead absorber, followed by a plane of silicon-strip sensors, followed by another lead absorber, followed by an orthogonal plane of silicon strip sensors. The silicon is $320 \mu\text{m}$ thick and

measures $6.1 \times 6.1\text{cm}^2$ per sensor module. Measurements in the two orthogonal directions of each silicon layer are combined to provide precise shower shape measurements. The primary motivation for the detector was the reconstruction of high-momentum ($> 3\text{ GeV}$) neutral pions. Neutral pions have a 98.8% branching fraction to a photon pair and decay before exiting the beampipe. The relative angle at which the photons are emitted is inversely proportional the momentum of the parent, and eventually the photons are so aligned they can not be separately resolved within the ECAL crystals.

5.3 Hadronic Calorimeter

The hadronic calorimeter is responsible for the reconstruction of undecayed hadrons: pions π^\pm , protons p , neutrons n , and kaons K^\pm, K_L^0 . It is composed of 4 distinct components with some amount of overlap. It is divided into barrel ($|\eta| < 1.4$, HB), endcap ($1.3 < |\eta| < 3$, HE), forward ($3 < |\eta| < 5.2$, HF), and outer ($|\eta| < 1.2$, HO) regions [21]. A diagram of the HCAL geometry is seen in Figure 5.6.

In the HE and HB, a particle will interact with the brass absorber inducing a shower of secondary particles. These secondary particles in turn may interact with the brass, and so on creating a hadronic shower within the detector. Interspaced within the absorber are clear plastic scintillator which create flashes of light after de-excitation of the scintillating molecules embedded in the plastic. Wavelength shifting fibers are routed throughout the plastic to absorb the light, which is then piped to hybrid photodiodes. Light incident on the photodiodes liberates electrons via the photoelectric effect which are then accelerated onto the surface of a silicon diode, which further amplifies and digitizes the signal. The particle energy is therefore measured by collecting light generated by a hadronic shower as the particle is absorbed in the calorimeter.

Each of these detectors consists of 17 alternating layers of 5 cm thick brass and 1 cm thick scintillating plastic. The readouts of the optical fibers are summed into *towers* of size roughly 0.09×0.09 in $\eta - \phi$, this results in the η segmentation seen in Figure 5.6, labeled from 1 to 15 for HB and then 18-29 in HE. Depths of constant color represent the radial segmentation of the optically

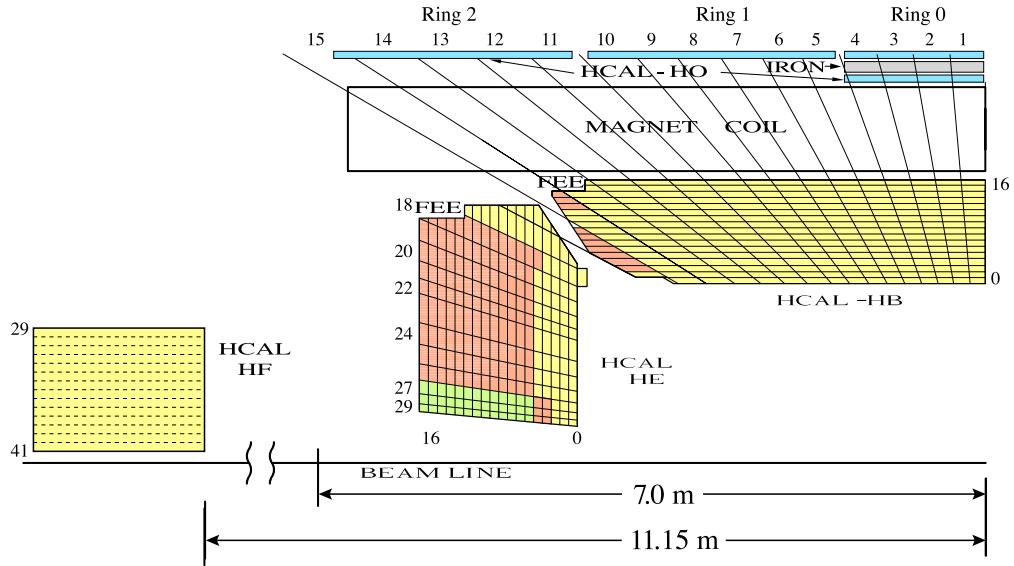


Figure 5.6: The CMS hadron calorimeter [22].

summed light within a tower. The HO sits **outside** the magnet in the barrel region $|\eta| < 1.2$ and collects additional energy not absorbed in the material in front of it with an additional layer of scintillator planes.

In addition to HB, HO, and HE, there is a steel calorimeter HF, which detects radiation in the very forward region $3 < |\eta| < 5.2$ on each side of the interaction point. This forward region has a very large radiation flux - the majority of the proton-proton interactions are “glancing blows” in which there is very little momentum transfer and the particles are deflected only slightly, directly into this region of the detector - this environment requires a different approach than in the rest of the HCAL. Each detector is comprised of 165cm thick steel interspersed with radiation-hard quartz fibers (parallel to the beamline) to collect light, which is read out by photomultipliers. The tower size in this detector is about 0.175×0.175 in $\eta - \phi$.

5.4 Solenoidal Magnet

The solenoidal magnet provides the magnetic field necessary to deflect charged particles within the tracker volume to allow for a measurement of the momentum. The tracker, ECAL, and HCAL all fit inside the magnet bore of diameter 6 m and length 12.5 m. It delivers a 3.8T solenoidal

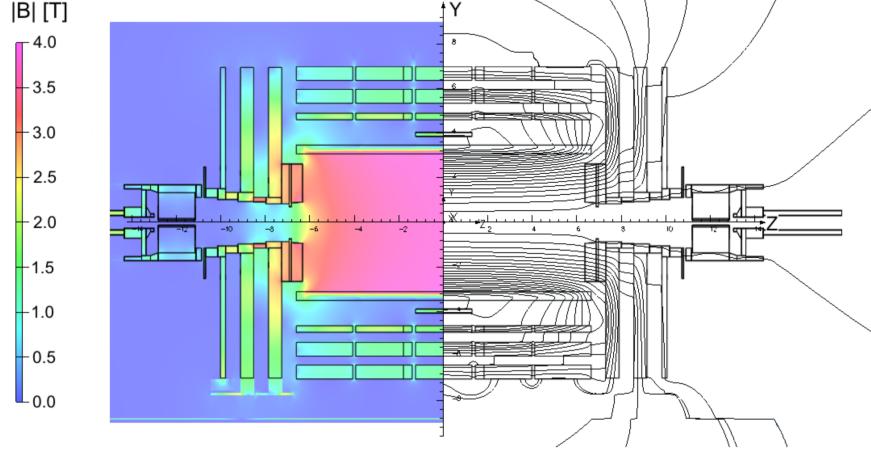


Figure 5.7: A simulation of the 4T CMS magnetic field. Note the uniformity within the tracker volume.

field (parallel to the beampipe) within the tracker volume. The field is produced by running current through coils of superconducting NbTi wires cooled to less than 5K. The magnetic field lines are returned via steel yokes sitting outside the magnet interspaced within the muon tracker volume. The field strength throughout the muon system is approximately 2 T [23]. A simulation of the magnetic field within the whole of CMS is seen in Figure 5.7 [24].

5.5 Muon System

The muon system is responsible for the reconstruction (and triggering) of muons μ^\pm . The muon trajectory is reconstructed using ionization deposits left in layers of gaseous detectors. The muon momentum is measured by the curvature of the trajectory caused by the magnetic field in the return yoke [25].

The muon system sits at the furthest distance from the beamline. Any particle that has made the journey to the muon system has traveled far and through many layers of detector material (e.g. Si, PbWO₄, Cu), Fe) before finally being detected. Many particles are unstable and decay before reaching the muon system; other particles are absorbed in either of the calorimeters. But the muon has a relatively large mass (compared to an electron) and is not very likely to initiate

electromagnetic showers in the ECAL. Nor does the muon interact strongly, and so there will be no hadron showers within the HCAL. Muons have a sufficiently long lifetime to make it to the outer detector. This combination yields a very pure sample of reconstructed muons.

There are three components of the muon system: The drift tubes (DT) are in the barrel ($|\eta| < 1.3$), the cathode strip chambers (CSC) are in the endcaps ($0.9 < |\eta| < 2.4$), and resistive plate chambers (RPC) are in both regions ($|\eta| < 1.6$). These detectors rely on different technology and have some amount of overlap with each other. All detectors participate in triggering and track reconstruction, but the DTs and CSCs provide greater position and momentum resolution, while the RPCs have excellent timing resolution allowing for more precise bunch crossing tagging.

5.5.1 Drift Tubes

The drift tubes are used for muon tracking in the barrel portion of the detector ($|\eta| < 1.3$). The basic element is a gas tube 4×1.3 cm in transverse size and 2-4 m long (depending on its position). High-voltage is applied to a wire strung the length of the cylinder and collects charge released when an incident muon ionizes an 85/15% Ar/CO₂ gas mixture [26].

The drift tubes are divided into four barrel regions (each called a station) at different radii within the magnetic return yoke. Each station contains 3 *superlayers*, where a superlayer is composed of four layers of stacked tubes, each layer staggered by one half width. For each station, two of the superlayers are oriented parallel to the beamline for $r - \phi$ measurements and one superlayer is perpendicular to the beamline to allow for measurements of the r-z position. An image of a DT station is seen in Figure 5.8.

5.5.2 Cathode Strip Chambers

The cathode strip chambers are used for muon tracking in the endcap portion of the detector ($0.9 < |\eta| < 2.4$). The system is divided up into 468 trapezoidal chambers arranged in 2 or 3 concentric rings on a disk. There are 4 discs on either side of the detector ($\pm z$). The geometry of the chambers on a disk are seen in Figure 5.9a (an example image of the hit occupancy of a disc

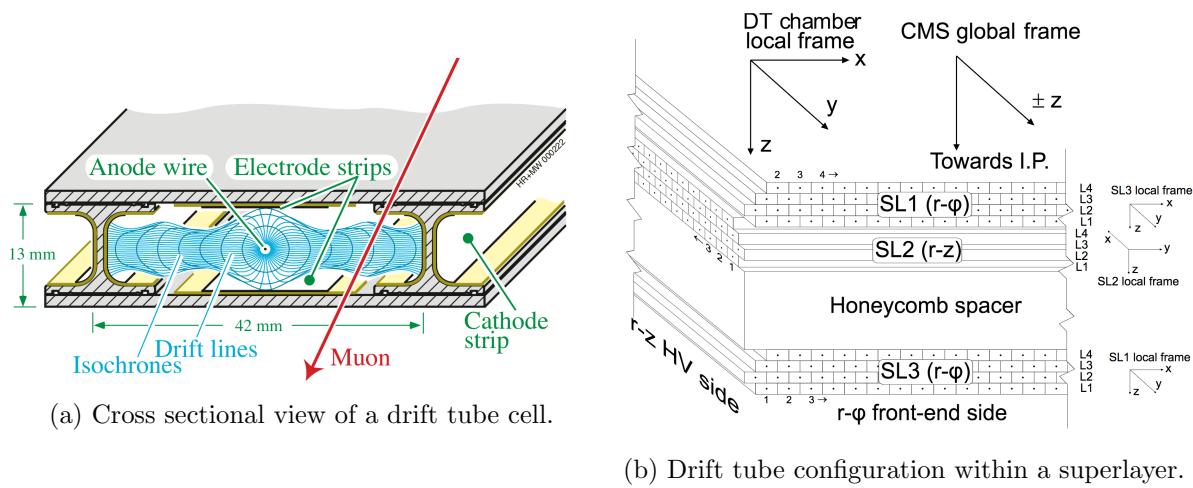


Figure 5.8: The CMS muon drift tube detector [27].

during cosmic ray runs). Each chamber (diagram in Figure 5.9b) consists of 6 layers of electrode planes separated by a gas layer of $\text{C}_2\text{H}_2\text{F}_4$ (freon) and C_4H_{10} (isobutane). Wires are strung in the ϕ direction (perpendicular to the z axis) and therefore make a measurement of the radial coordinate of the hit. The electron shower generates an image charge in cathode planes. For each layer, one of the planes is segmented into strips perpendicular to the wires, providing a good measure of the ϕ coordinate [28].

5.5.3 Resistive Plate Chambers

Resistive plate chambers cover the region $|\eta| < 1.6$ and are interspersed within CSC and DT and the magnetic return yoke [29]. They have an excellent timing resolution of about 3 ns which allows for fast muon triggering and identification of the different bunch crossings. Pattern matching across the hits in the different layers allows for estimates of the muon p_T to be used in further trigger processing. Hits created in the resistive plate chambers are additionally used for global fitting of the muon tracks.

The resistive plate chambers consist of an airtight system of two parallel high-resistivity planes separated by a 1 cm gas gap. The outside of each plate is coated to form an electrode for the high-voltage bias. On top of each electrode sits aluminum strips which are insulated from the electrode and serve as the readout. Electron showers created in the gas bulk induce an image charge on the strips which is then recorded. The gas mixture is 95/5% $\text{C}_2\text{H}_2\text{F}_4$ (freon) and C_4H_{10} (isobutane), with trace amounts of SF_6 . A diagram of an RPC chamber is seen in Figure 5.10.

5.6 Trigger System

While in operation mode, the LHC provides beam crossings at a rate of 40 MHz (25 ns per bunch crossing). This is a phenomenal rate which the CMS detector readout is not able to accommodate, nor does the experiment have access to the amount of storage space necessary to store all this information. Therefore, the CMS detector makes use of a trigger system to quickly determine if the event is ‘interesting’ and will be saved for storage — events which are not triggered

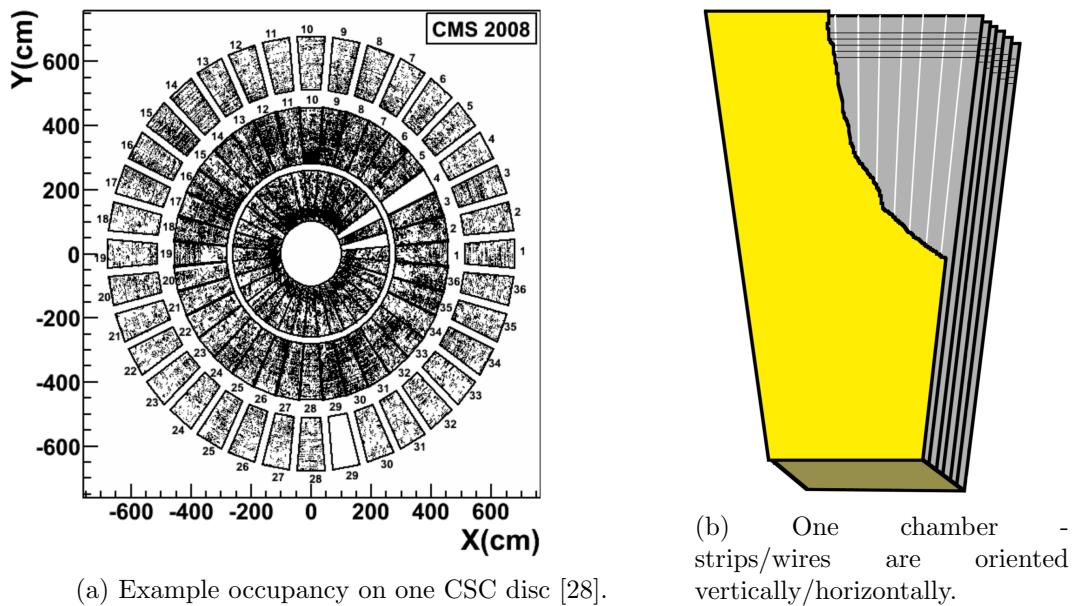


Figure 5.9: The CMS muon cathode strip chambers.

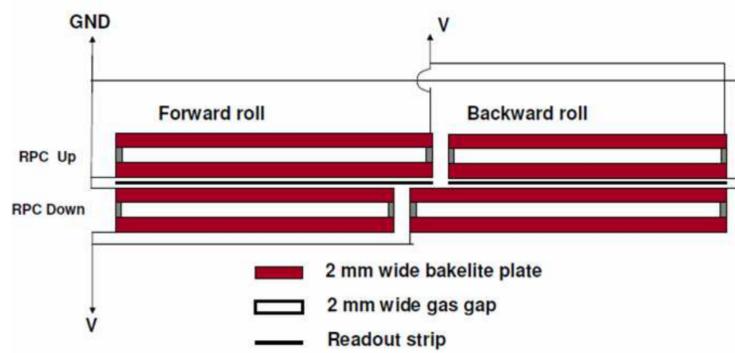


Figure 5.10: The CMS muon resistive plate chamber [29].

are lost forever. Examples of interesting events are those with high- p_T muons, or a large imbalance in the total momentum of the event [30].

The trigger consists of two stages known as the Level-1 (L1) and High-Level Trigger (HLT). L1 is a hardware based trigger that combines information from the calorimeters and muon systems to make a decision if the event will be passed to HLT for further processing. L1 is able to reduce the event rate from 40 MHz to 100 kHz and must make the decision within $4\ \mu s$. Primitive objects such as calorimeter energy deposits or muon track segments are first constructed locally within the detector before being combined to form the global decision at L1. If the decision is made at L1 that the event is of potential interest, it is passed to HLT. HLT is a software based trigger that makes use of more sophisticated reconstruction algorithms that can be tuned to select events of choice.

Chapter 6

Event Reconstruction

6.1 Basic Elements From the Detector

Depending on their nature, the particles emanating from the collision leave various forms of energy deposits in the different subdetectors. All these signals need to be aggregated and processed to allow for the reconstruction of what could be considered particle-level information. The first step in this process consists of building *Particle Flow elements* using information within each subdetector. There are four primary elements from the subdetectors: tracks from the tracker, calorimeter deposits in each of the ECAL and HCAL, and tracks from the muon detector. The elements are eventually combined via the *Particle Flow algorithm*, yielding reconstructed particles used for physics analysis.

Note that the definition of any object within the detector makes use of additional selection criteria, which are not generally discussed here. For instance, one may require that a track in the tracker have at least 3 hits in the pixel detector, or that a calorimeter hit be above some minimum threshold energy. The effects of these criteria are generally a balance between the particle reconstruction efficiency and misidentification rate (purity).

6.1.1 Tracks

Tracker hits are formed in the pixel and strips detectors by clustering any hits in neighboring elements of the detector plane. The cluster position is a weighted average of the individual channel positions. Charge sharing among detector channels allow for a finer spatial resolution in the position

measurement. Track reconstruction first begins by forming track seeds consisting of a small number of detector hits. These track seeds are then projected onto successive detector layers looking for additional hits. This follows the Kalman filtering procedure, in which track information is updated after the addition of each hit [31].

The track building procedure follows an iterative procedure, where the requirements on the quality of the track seed decrease as the iterations proceed. After a given iteration the hits used in building the tracks are removed from subsequent iterations. The first iterations begin with seeds consisting of 3 pixel hits and lead to high performance reconstruction of high p_T tracks emanating from the collision region. The iterations proceed until essentially only requiring hits in the outer tracker to reconstruct displaced tracks or tracks with missing hits. The iteration procedure provides a balance between reconstruction efficiency, purity, and computation economics. Table 6.1 lists these iterations, along with the requirements on the seeds and the type of tracks which are targeted.

Table 6.1: Seeding requirements for each step in the iterative track reconstruction [32].

Iteration	Name	Seeding	Targeted Tracks
1	InitialStep	pixel triplets	prompt, high p_T
2	DetachedTriplet	pixel triplets	from b hadron decays, $R \lesssim 5\text{ cm}$
3	LowPtTriplet	pixel triplets	prompt, low p_T
4	PixelPair	pixel pairs	recover high p_T
5	MixedTriplet	pixel+strip triplets	displaced, $R \lesssim 7\text{ cm}$
6	PixelLess	strip triplets/pairs	very displaced, $R \lesssim 25\text{ cm}$
7	TobTec	strip triplets/pairs	very displaced, $R \lesssim 60\text{ cm}$
8	JetCoreRegional	pixel+strip pairs	inside high p_T jets
9	MuonSeededInOut	muon-tagged tracks	muons
10	MuonSeededOutIn	muon detectors	muons

Electron tracking is performed with a modified Gaussian sum filter to account for the electron's energy loss in the detector. Electrons are very light and susceptible to emitting *bremsstrahlung* radiation, occurring when the electron scatters from nucleus within the tracker and emits a photon. This results in non-negligible energy loss and changes in direction as the electron traverses the detector. This results in very non-Gaussian energy loss mechanisms in which the Kalman filtering is non-optimal.

6.1.2 ECAL & HCAL Clusters

Superclusters in the ECAL are built by first identifying a crystal with the largest energy deposit, this is called a *seed*. The supercluster is then formed by aggregating any hits among the neighbors (8 or 4 for the ECAL or HCAL, respectively) of the hits already in the cluster. This process then proceeds building all the superclusters and consuming all the calorimeter hits. Within a given supercluster, N clusters are identified using an iterative algorithm assuming the observed hits arise from N Gaussian-distributed energy deposits; each of energy E, position in the $\eta - \phi$ plane $\vec{\mu}$, and width scale σ set by the crystal size. Clusters are built separately in the HCAL, ECAL, barrel, and endcaps.

6.1.3 Muon Tracks

The multiple detector layers within a single muon station allow for the reconstruction of local track segments. The segments are built with a fit using the hits within a station and can be used to perform a measurement of the momentum at that location. These segments can be calculated quickly allowing for triggering and bunch cross identification. The track segments are used as seeds for the track finding algorithm to construct the final muons. The hits in each the DT, CSC, and RPC subdetectors are used in the reconstruction of the final muons.

6.2 Obtaining a Particle-level Description

Once the elements have been built, the Particle Flow algorithm exploits the information from each of the detectors to form the best possible particle candidate [32]. As different varieties of particles have unique signatures in the detector, particle identification is aided by the particular combination of elements *linked* with one another. An illustrative example of these combinations are shown in Figure 5.2. Elements are linked when projections from one element to the other are spatially consistent. There are six primary links:

- Tracks formed in the tracker are linked to an ECAL or HCAL cluster if the projection of the

track, at a depth of the expected maximum of a shower in the ECAL or at one interaction length inside the HCAL, lies within the cluster area.

- ECAL and HCAL clusters are linked if the ECAL cluster falls within the envelope of the HCAL cluster; ECAL provides finer spatial resolution compared to the HCAL.
- If a Preshower cluster is within the envelope of an ECAL cluster the two are linked; Preshower has finer spatial granularity.
- A tracker track and a muon track are linked if their projections onto a common surface are spatially consistent.
- To collect bremsstrahlung radiation (photons) associated to an electron track, an ECAL cluster is linked to a track if projections tangent to the momentum at the tracker layers lies within the cluster volume. It is also possible a bremsstrahlung photon interacts with the tracker and converts into an e^+e^- pair, this pair may be identified as arising from photon conversion and then subsequently linked to the (primary) electron track.
- Tracks consistent with arising from a secondary vertex are linked to allow for reconstruction of nuclear interactions.

Particle Flow *blocks* are constructed by aggregating objects directly or indirectly linked with one another. The Particle Flow algorithm then processes each block in turn to create the final reconstructed particles. The algorithm builds the objects in the following order

- (1) **Muons:** There are three types of tracks that can be used for muon reconstruction:

- ***standalone*** muons are built from tracks reconstructed solely in the muon system.
- ***tracker*** muons are built from tracks reconstructed in the silicon tracker. They are tagged as such if the track projection is consistent with any track segments found in the muon system.

- *global* muons are reconstructed using the hits from both the silicon tracker and the muon stations. Global muons are reconstructed when a track in the tracker and a track in the muon system are compatible.

Any ECAL or HCAL clusters associated with the muon track are used as muon selection/definition criteria if those clusters are found to be consistent with the muon hypothesis.

(2) Electrons & Photons:

An electron is formed by combining a track from the silicon tracker with a cluster from the ECAL. Its energy assignment uses a combination of both elements. The momentum direction is made using the track, as it gives greater spatial resolution. A photon is defined as an ECAL cluster not associated with a track. Electrons and isolated photons are reconstructed within the same Particle Flow step to account for their common behavior in the tracker: photons often produce electron-pairs and electrons often radiate bremsstrahlung photons.

(3) Hadrons & Photons:

Hadrons & non-isolated photons result from hadronization/fragmentation of jets. ECAL clusters not associated to any tracks are assigned to be photons. Neutral hadrons (K_L^0 , neutrons) are reconstructed from HCAL clusters with no associated track; neutral hadrons leave a very small amount of energy in the ECAL. Charged hadrons (π^\pm , K^\pm , protons) are reconstructed using the remaining tracks and HCAL deposits.

(4) Nuclear Interactions:

A nuclear interaction may occur when a hadron from the pp collision interacts with the detector material causing a shower of (charged and neutral) secondary particles. The tracks from the shower may be linked through a common (secondary) vertex, in this case they will be replaced by a single charged hadron under the assumption of the pion mass.

6.3 Additional High-Level Objects

6.3.1 Jets

Bare quarks and gluons can never be observed in Nature due to a QCD phenomenon called *color confinement*. Therefore, quark and gluon production manifests as a “jet” of color-neutral particles emanating from the production point. These particles can be clustered together to reconstruct the original parton. The jets used in this analysis are made by clustering particles with the “anti- kt “ algorithm with cone sizes of $\Delta R = 0.4, 0.8$ [33], denoted as AK4 and AK8 jets, respectively. This algorithm produces nearly conical jets and is infrared and collinear safe. The AK4 jets subtend less solid angle and are used to capture the hadronisation of single quarks and gluons. AK8 jets subtend a larger solid angle and are used for reconstruction of boosted objects that decay to multiple jets.

6.3.2 b-tagging of Jets

Jets resulting from the production of b quarks (and to some extent c quarks) garner special attention in our experiment. As usual for quarks and gluons, the b-quark will quickly hadronize and form a b hadron. However, the lifetimes of b hadrons are such that it will generally travel hundreds of microns before decaying. Vertexing the tracks resulting from the decay will reveal the presence of a *secondary vertex*, which is spatially displaced from the primary vertex from which the other hadrons inside the jet originate. This secondary vertex allows a handle to identify jets as coming from b quark production. Other handles include the momenta and multiplicity of the other particles clustered into the jet.

In addition to tagging jets as originating from a single b quark, tagging of jets as originating from **two** b quarks is also possible [34].

6.3.3 Invisible Particles $\rightarrow p_T^{\text{miss}}$

Neutrinos are so weakly interacting that they leave no energy deposits in CMS and are not detected by our experiment. Although direct detection is not possible, we are able to infer their presence. The net momentum of the protons involved in the collisions is zero, but the individual partons (quarks and gluons) within the proton carry unknown fractions of this total (longitudinal) momentum. Only in the transverse direction may we require momentum conservation. We define this imbalance as:

$$p_T^{\text{miss}} \equiv \left| - \sum_i \vec{p}_T^i \right|, \quad \forall \text{ particles i.} \quad (6.1)$$

If all particles in the event are perfectly reconstructed, p_T^{miss} would equal zero. Large values indicate the presence of an undetected particle, such as a SM neutrino or something more exotic like the light supersymmetric neutralinos χ_0^0, χ_1^0 . This quantity is sometimes labeled as *MET*.

Chapter 7

Search for supersymmetry using boosted Higgs bosons and missing transverse momentum in proton-proton collisions at 13 TeV

7.1 Motivation & Strategy

If a more unifying theory than the SM exists it certainly has not been forthright in its manifestation. One possibility for the lack of discoveries of phenomena not explained within the SM is that there are indeed particles existing in Nature that have not been observed, but they have such a large mass that the energy of the proton-proton collisions provided by the LHC is insufficient to directly create them. The outcome of many searches for new particles is thus the setting of limits placed on the cross section of their production mechanism. As these cross sections are dependent on the particle mass, the limits can be interpreted as setting lower bounds on the mass of any new physics. If the particle were any lighter than this limit it would have been produced copiously enough for its unambiguous detection (see for example [11, 12]). As these particles become more massive more momentum is imparted upon the particles in the final state; any SM particles resulting from the decay of higher mass states will be produced with large momentum (this is called high boost). As a particle becomes more boosted its decay products are emitted at smaller angles, eventually collimating enough to be reconstructed as a single jet. If new physics exists with masses accessible at the LHC it is possible that there exists non-zero coupling with the electroweak H, Z, or W^\pm bosons. Observation of events containing high- p_T (>300 GeV) electroweak bosons are thus of considerable interest for finding new particles of large mass.

The Minimal Supersymmetric SM contains a discrete symmetry called R-parity in which all

SM and supersymmetric particles have charges -1 and $+1$, respectively [9]. One direct consequence of R-parity conservation is that the decay of a massive supersymmetric particle must include an odd number of supersymmetric particles in the final state. This decay cascade will continue until the final state consists of the lightest such particle in the theory, denoted the lightest supersymmetric particle (LSP). If the LSP is electrically neutral it may escape detection, creating an imbalance in the net momentum of the event (similar to a neutrino). Therefore, events with a large momentum imbalance are also interesting as potential signals for SUSY. For this thesis, we assume R-parity is conserved.

With this as a motivation, the authors ([35]) designed an analysis searching for physics beyond the SM in events with boosted H or Z bosons and a large transverse momentum imbalance of the event. We reconstruct the H and Z bosons in the $b\bar{b}$ decay mode, with 57% and 15% branching fractions, respectively. Although our analysis is sensitive to any new physics with this final state, we have adopted two benchmark models seen in Figure 7.1. These are known as the *T5HH* (left) and *T5ZH* (right) *SMS* models, respectively. The proton-proton interaction produces a pair of gluinos \tilde{g} that decay to a neutralino $\tilde{\chi}_2^0$ along with the emission of SM quarks. This neutralino $\tilde{\chi}_2^0$ further decays into a neutralino $\tilde{\chi}_1^0$ with the emission of a SM Higgs or Z boson. The blob in the figure indicates we are not interested in the particulars of the gluino production mechanism. SMS (simplified model spectrum) models serve to simplify the SUSY parameter space into particle masses, cross sections, and branching fractions [36]. In general, the diagrams begin with production of a pair of sparticles that subsequently cascade decay to final states consisting of stable SM particles and a pair of stable supersymmetric particles which are the lightest in the theory. We have seen two other examples of these diagrams previously in Figure 3.3.

7.2 Baseline Selection and Object Definition

The salient feature of our analysis is the presence of two high- p_T AK8 jets and large p_T^{miss} . Our most significant backgrounds are those which produce a large amount of p_T^{miss} ; these are divided into two categories depending on whether it comes from a “true” or “fake” source. True p_T^{miss} arises from

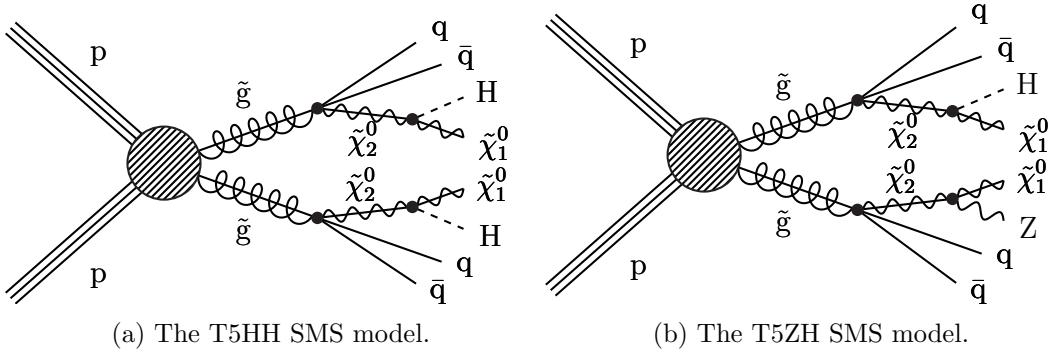


Figure 7.1: Diagrams of the benchmark models used for motivation of the targeted signal.

a neutrino or otherwise unobservable particle escaping our detector, i.e. a genuine imbalance in the detectable final-state momentum of the event. Fake p_T^{miss} arises from some sort of “imperfection” in our detector or reconstruction process, typically an under-measurement of the energy of a jet.

We approach our background as being constituted of three primary types. Two of them involve the production of neutrinos and the third is a result of jet resolution:

- $Z \rightarrow \nu\bar{\nu}$ in which the neutrinos from the Z decay results in true p_T^{miss} ('Z-invisible').
- $W \rightarrow \ell\nu$ in which the lepton ℓ is not properly identified, resulting in the event not being vetoed, and the associated neutrino from the leptonic decay creating true p_T^{miss} ('lost-lepton'). The W boson can be produced through the decay of a top quark, either in single-top or $t\bar{t}$ events; $t\bar{t}$ events generate two W bosons, in which the other may decay into an AK8 jet. A W boson may additionally be produced directly in association with other jets.
- Jet production via QCD in which the p_T of a jet is mis-measured, most commonly under-measured, creating a fake source of p_T^{miss} .

To mitigate these backgrounds, we establish a baseline selection choosing events with all-hadronic final states and missing transverse momentum (p_T^{miss}), as motivated by Figure 7.1. The baseline selection is as follows:

- ≥ 2 AK8 jets, with $p_T > 300 \text{ GeV}$ and $50 < \text{mass} < 250 \text{ GeV}$
- $p_T^{\text{miss}} > 300 \text{ GeV};$
- no isolated electrons with $p_T > 10 \text{ GeV}:$

Isolation requires the p_T sum of the particles within a cone of $\Delta R < 0.2$ to be less than 10% of the electron p_T . (See [37] for details about “mini-isolation”.)

- no isolated muons with $p_T > 10 \text{ GeV}:$

The energy fraction for the isolation requirement is relaxed to 20%.

- no isolated tracks:

To remove events with top or W production in which the W decays to a lepton. As an isolated track is defined by looser criteria than that of an electron or muon, this cut also serves to increase the efficiency of the isolated electron and muon vetoes. Leptonic tracks must satisfy $p_T > 5 \text{ GeV}$ and have 20% isolation. Hadronic tracks must satisfy $p_T > 10 \text{ GeV}$ and have 10% isolation.

- $\Delta\phi_{1,2,3,4} > 0.5, 0.5, 0.3, 0.3$; $\Delta\phi_i \equiv \Delta\phi(p_T^{\text{miss}}, \text{AK4 jet}_i)$

This cut requires that the difference in ϕ between the p_T^{miss} vector and each of the four highest- p_T jets is sufficiently large to remove events in which a jet has been under-measured giving rise to fake p_T^{miss} . If fewer than four AK4 jets are available the additional cuts are removed.

To tag jets from $H \rightarrow b\bar{b}$ decay, a dedicated machine learning algorithm has been developed by the CMS collaboration to discriminate these from those produced by QCD processes [34]. The algorithm makes use of the kinematics expected by having secondary vertices arising from the b-quark decays. Discriminating variables include the number, mass, energy, and position of the secondary vertices in the jets. Additional variables include the distance of closest approach between the vertices and tracks (when projected backwards); tracks arising from displaced vertices are not expected to project back to the primary interaction point. The distributions of this discriminator

for the two highest- p_T AK8 jets are seen in the upper left and right panels of Figure 7.2; signal-like events peak towards larger values. The stacked histogram and solid lines shows the distribution after baseline selection for simulated SM processes and two representative signal points, respectively. To $b\bar{b}$ tag the AK8 jets we choose the loose working-point (>0.3) corresponding to an efficiency of approximately 70 – 80% for $H \rightarrow b\bar{b}$ (see Figure B.1). Appendix A details the $b\bar{b}$ -tagger in more depth.

Additionally, to tag H or Z bosons, a requirement is made on the invariant mass of the jet. We use the mass of the so called “pruned” jet, which is a method involving removal of soft and wide-angle radiation inside the jet [38]. The pruning is very powerful for discriminating QCD jets from those produced by heavy particle decays. Our tagging requires the jet mass to fall within a window [85, 135 GeV] to be consistent with that of the H boson. The distributions of the jet mass are seen in the lower frames of Figure 7.2. The same identification criteria are applied to tag an AK8 jet as either an H or Z boson (there is no distinction made between the two).

7.3 Dataset & Trigger

We use a total of 35.9 fb^{-1} of data collected by the CMS experiment in 2016. Events are selected with the requirement of at least 100 GeV of p_T^{miss} calculated at the high-level trigger (`HLT_PFMET100_PFMHT100_IDTight`, HLT). To improve the trigger efficiency, the logical OR of similar triggers of thresholds 110 and 120 GeV are included.

The HLT is seeded at level-1 (L1) by the requirement of at least 100 GeV of missing transverse energy (`L1_ETM100`). Missing transverse energy is calculated by the vectorial sums of the regional energy deposits in the calorimeters (and rotation by 180°). This is additionally ORed with similar seeds of thresholds 90, 80, 70, 60, 50 GeV. Two additional ORed seeds require calorimeter jets with p_T of at least 60 GeV (`L1_ETM60_Jet60_dPhi_Min0p4`, `L1_DoubleJetC60_ETM60`).

The trigger efficiency is defined as $\epsilon = N_1/N_2$, where N_2 is the total number of events passing baseline selection and N_1 is the total number of events selected by the trigger and passing baseline selection. In order to calculate this efficiency, we need to form an additional (hopefully independent)

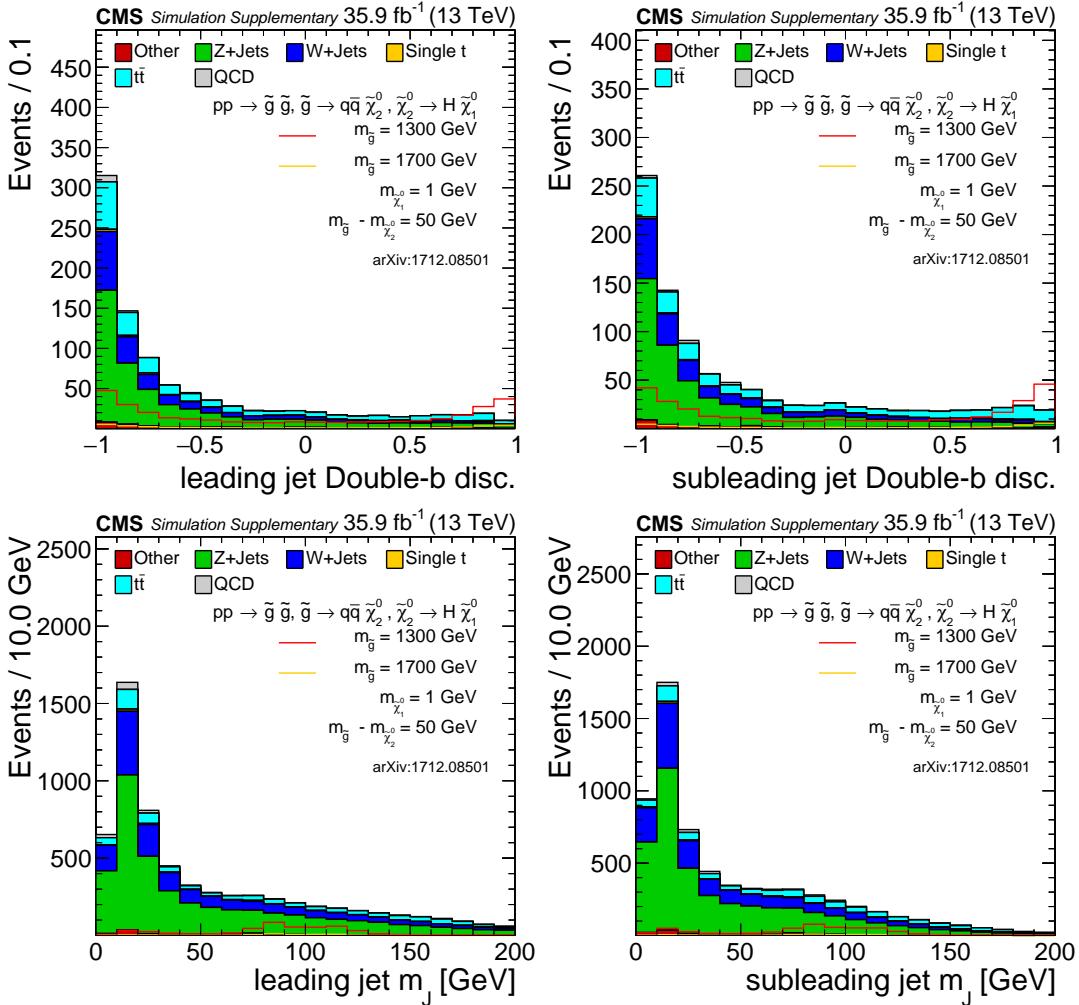


Figure 7.2: Distributions of the bb-tagging discriminator (top row) and jet mass (bottom row) for the highest (left column) and second highest (right column) p_T AK8 jets. In the signal models, the H bosons are allowed to decay inclusively.

dataset by selecting events via a *reference trigger*. Our reference trigger requires a single electron of $p_T > 27 \text{ GeV}$, in addition to the baseline selection we require these events to contain at least three AK4 jets and exactly one reconstructed electron of $p_T > 25 \text{ GeV}$. The signal region trigger is found to be greater than 98% for events with $p_T^{\text{miss}} > 250 \text{ GeV}$ and $H_T > 300 \text{ GeV}$ [11]. A correction for the trigger inefficiency is accounted for by introducing a systematic error of 2% to the final results.

7.4 Event Simulation

MadGraph@NLO2.2.2 [39] is a MC generator used to simulate the ‘hard’ interaction between the partons involved in the primary collision. Parton distribution functions, used to model the quark and gluon momentum distributions within the proton, are taken from NNPDF 3.0 [40]. Parton showering, which models quark and gluon evolution into hadrons, or final/initial state radiation, is performed with Pythia [41]. The final-state particles are traced through the detector using GEANT. This includes the effect of the magnetic field, interactions with both the inert and sensitive detector material, and additional particle decays [42]. These simulated data are processed in the same manner as those of the physical experiment.

7.4.1 Standard Model Processes

The SM samples that enter as the primary backgrounds are listed in Table 7.1 (see Section 7.5.1 for a discussion of the background). All samples are generated with a pileup distribution with an average of 25 interactions per bunch crossing and a 25 ns interval between bunches. For acceptable statistics over a wide range of parameter space, the samples are often binned in $H_T \equiv \sum_{\text{AK4 jets}} p_T$. As our event selection requires at least two AK8 jets with $p_T > 300 \text{ GeV}$ we roughly operate in the regime of $H_T > 600 \text{ GeV}$.

7.4.2 Signal Models

For commissioning of the analysis technique (as well as the limit-setting procedure, see Section 7.7) Monte Carlo samples with our final-state signal topology were generated, based on the

Table 7.1: SM samples used in the analysis. $H_T \equiv \sum_{AK4\text{jets}} p_T$ is the total hadronic energy in the event. σ is the cross section. $\int \mathcal{L} = N/\sigma$ is an alternative way to express the number of generated events.

process	final state	H_T (GeV)	σ (pb)	$\int \mathcal{L}$ (fb^{-1})
$t\bar{t}$	$t \rightarrow \ell\nu, \bar{t} \rightarrow 2q$	inclusive	182.72	283.90
$t\bar{t}$	$\bar{t} \rightarrow \ell\nu, t \rightarrow 2q$	inclusive	182.72	326.48
$t\bar{t}$	2ℓ	inclusive	88.34	346.25
$t\bar{t}$	inclusive	[600, 800]	2.734	5231.81
$t\bar{t}$	inclusive	[800, 1200]	1.121	9416.61
$t\bar{t}$	inclusive	[1200, 2500]	0.198	14819.34
$t\bar{t}$	inclusive	[2500, ∞]	0.002	221088.29
QCD	inclusive	[200, 300]	1735000	0.03
QCD	inclusive	[300, 500]	366800	0.16
QCD	inclusive	[500, 700]	29370	1.95
QCD	inclusive	[700, 1000]	6524	6.68
QCD	inclusive	[1000, 1500]	1064	12.62
QCD	inclusive	[1500, 2000]	121.5	32.63
QCD	inclusive	[2000, ∞]	25.42	239.30
Z+jets	$\nu\bar{\nu}$	[100, 200]	344.8	54.13
Z+jets	$\nu\bar{\nu}$	[200, 400]	95.53	208.46
Z+jets	$\nu\bar{\nu}$	[400, 600]	13.20	77.30
Z+jets	$\nu\bar{\nu}$	[600, 800]	3.148	1795.26
Z+jets	$\nu\bar{\nu}$	[800, 1200]	1.451	1486.09
Z+jets	$\nu\bar{\nu}$	[1200, 2500]	0.355	1029.81
Z+jets	$\nu\bar{\nu}$	[2500, ∞]	0.0085	47498.87
W+jets	$\ell\nu$	[100, 200]	1627.45	18.16
W+jets	$\ell\nu$	[200, 400]	435.24	45.88
W+jets	$\ell\nu$	[400, 600]	59.18	123.64
W+jets	$\ell\nu$	[600, 800]	14.58	221.32
W+jets	$\ell\nu$	[800, 1200]	6.66	1123.13
W+jets	$\ell\nu$	[1200, 2500]	1.608	153.44
W+jets	$\ell\nu$	[2500, ∞]	0.039	6497.28

processes in Figure 7.1. The signal sample follows the same processing chain as the SM samples. Samples are generated with a range of gluino \tilde{g} masses from 750 to 2200 GeV. The mass splitting between the gluino \tilde{g} and neutralino $\tilde{\chi}_2^0$ is chosen to be fixed at 50 GeV, resulting in low p_T SM quarks produced at the decay vertex. The mass of the neutralino $\tilde{\chi}_1^0$ (LSP) is fixed to 1 GeV.

The p_T distribution for the generated H bosons in these samples is seen in Figure 7.3 for a number of gluino \tilde{g} masses. Additionally, the angular separation $\Delta R \equiv \sqrt{\Delta\phi^2 + \Delta\eta^2}$ between the $b\bar{b}$ pair is shown. As the p_T of a parent boson increases, the $b\bar{b}$ pair from its decay tend to align, allowing complete reconstruction with a single AK8 jet. The distributions in Figure 7.3 motivate our use of two such high- p_T AK8 jets.

7.5 Event Binning & Background Estimation

The background estimation procedure makes use of what is known as an “ABCD” prediction in which the analysis phase space is divided into signal and sideband regions; scaling relations are applied to sideband yields to make predictions for the background in the signal regions. The events are categorized according to whether the two highest p_T AK8 jets are a) in the signal or sideband mass region and b) have or have not been $b\bar{b}$ tagged. A diagram of this partitioning is seen in Figure 7.4. An additional dimension is added by binning in p_T^{miss} : [300, 500 GeV], [500, 700 GeV], [700, ∞ GeV]. This additional binning, motivated by the p_T^{miss} distributions of Figure 7.5, allows us to maximize sensitivity for both low and high p_T^{miss} signal. This gives a total of $2 \times 3 = 6$ signal and $4 \times 3 = 12$ sideband bins. The two signal regions A_1 and A_2 contain events with exactly one and exactly two jets being consistent with H/Z boson decay, respectively.

Assuming that there is no correlation between the jet mass and the $b\bar{b}$ -tagging, one would expect that:

$$\frac{A_1}{B_1} = \frac{A_2}{B_2} = \frac{C}{D} \quad (7.1)$$

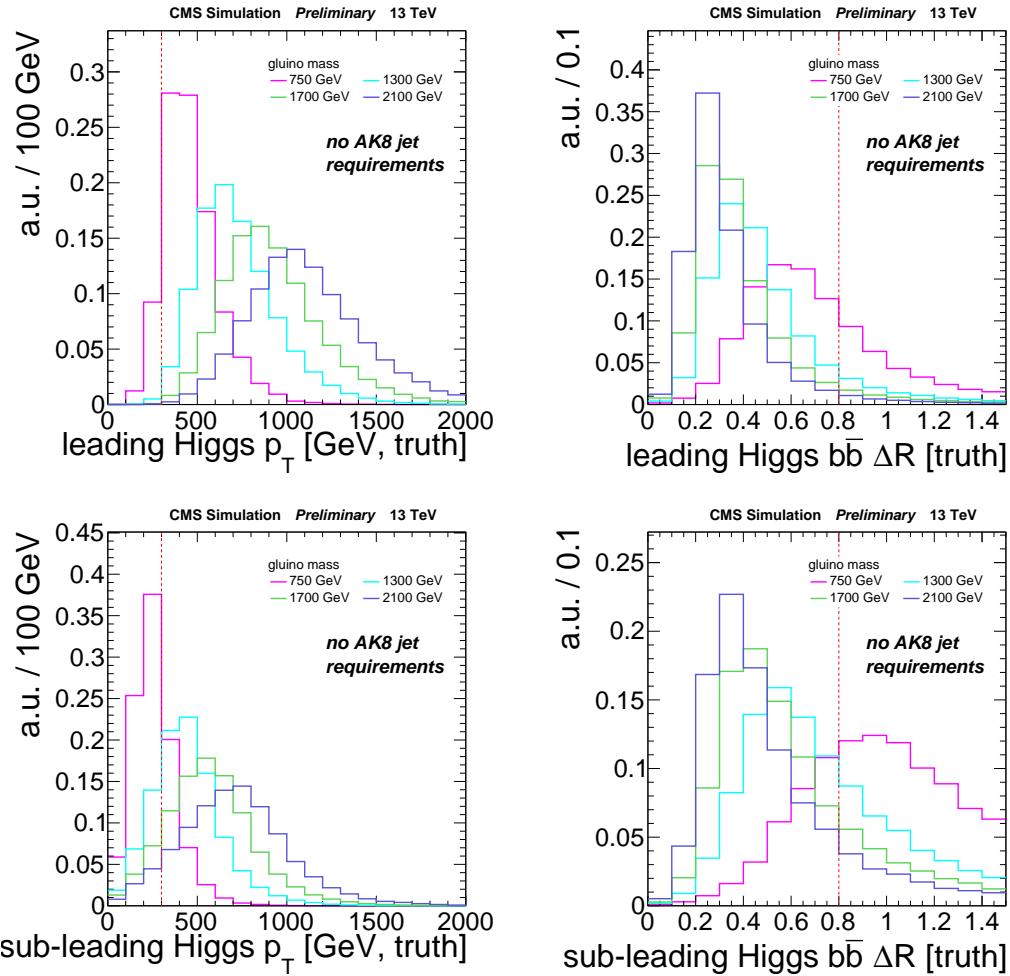


Figure 7.3: Generator level distributions for the leading (top row) and sub-leading (bottom row) H boson in the T5HH model. The left column shows the p_T distribution. The right column shows ΔR between the b-quark daughters; for large H p_T the daughters become collimated. [43]

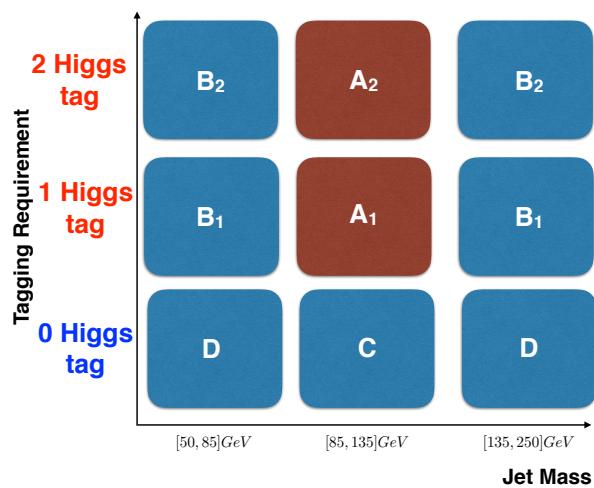


Figure 7.4: Partitioning of the signal and sideband regions for event binning. Additional binning in p_T^{miss} brings the total to $6 \times 3 = 18$.

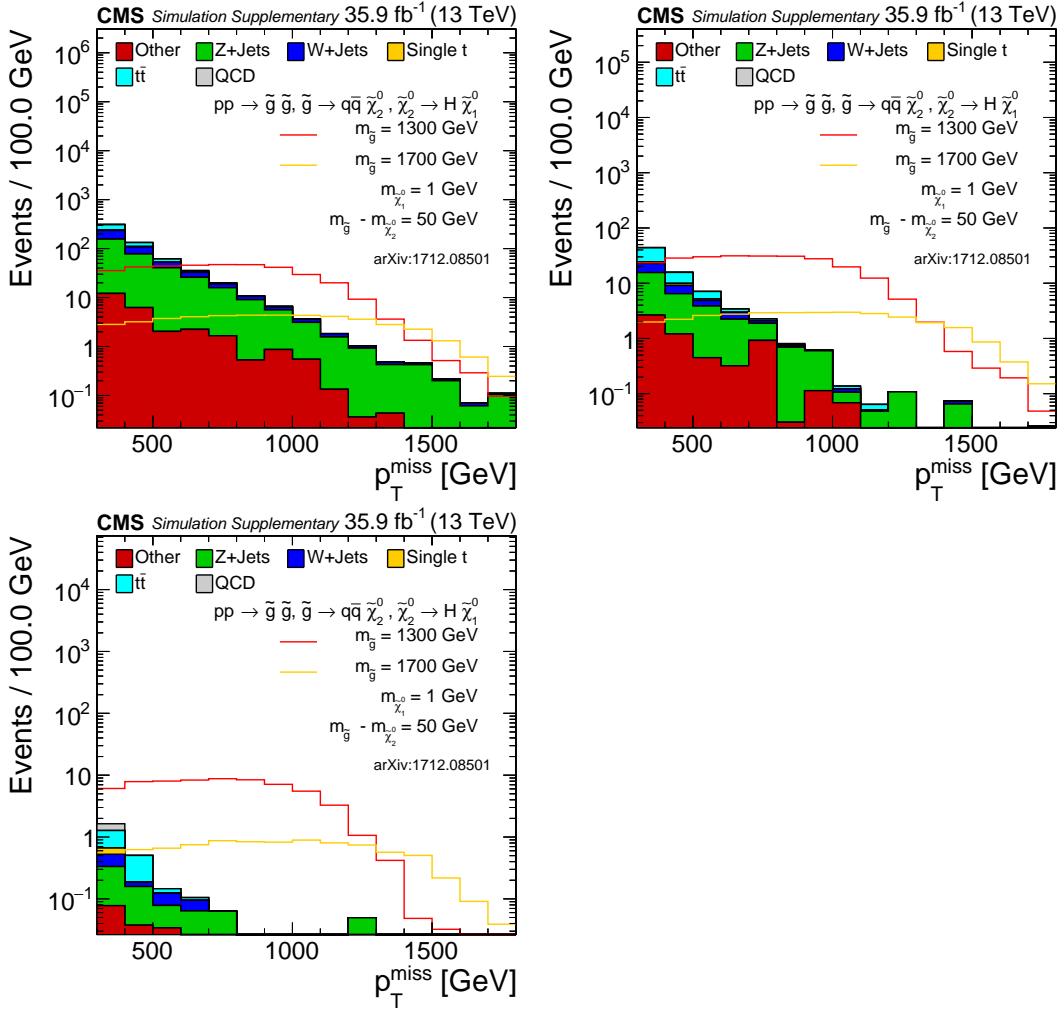


Figure 7.5: MC distributions of p_T^{miss} after baseline selection. Clockwise from top left: inclusive, the single H-tagged region A_1 , the double H-tagged region A_2 .

Rearranging this gives a prediction for the events in the signal regions

$$A_{1,2}^{\text{predicted}} = \left(B_{1,2} \cdot \frac{C}{D} \right)^{\text{observed}} \quad (7.2)$$

The expected p_T^{miss} distribution from simulation is seen in the stacked histograms of Figure 7.6.

The prediction using the ABCD method on the same simulated samples is seen in the red hash. The performance of the method within simulation can be determined by dividing the true content in the signal region with the prediction. This ratio, denoted κ , is seen in the bottom panel of Figure 7.6. $\kappa = 1$ represents perfect modeling. As will be discussed in Section 7.5.2, κ is used as a correction in the background estimation procedure.

7.5.1 Control Regions within Data

In order to study the expected backgrounds in data ($Z \rightarrow \nu\bar{\nu}$, $t\bar{t} \rightarrow \ell\nu qq'$, $W \rightarrow \ell\nu$, QCD), we define three control regions that are enhanced in processes representative of the background. The event selection is the same as applied to the nominal signal and sideband regions, but with some defining orthogonal condition:

- A control region with a single photon. When a Z boson has sufficiently large p_T such that its mass is negligible, it will be expected to have similar kinematics to the photon (the other massless, neutral, electroweak gauge boson). “Artificial” removal of the photon from the reconstruction (i.e. ignoring its calorimeter clusters) results in events similar to those of $Z \rightarrow \nu\bar{\nu}$ events.
- A control region with a single lepton. The topology of events from direct W or top quark production is the same regardless of whether the electron or muon is identified as such.
- A control region defined by the logical inversion of the low- $\Delta\phi$ cut. This explicitly selects events in which the AK4 jet momentum was likely under-measured, resulting in close alignment with the p_T^{miss} vector.

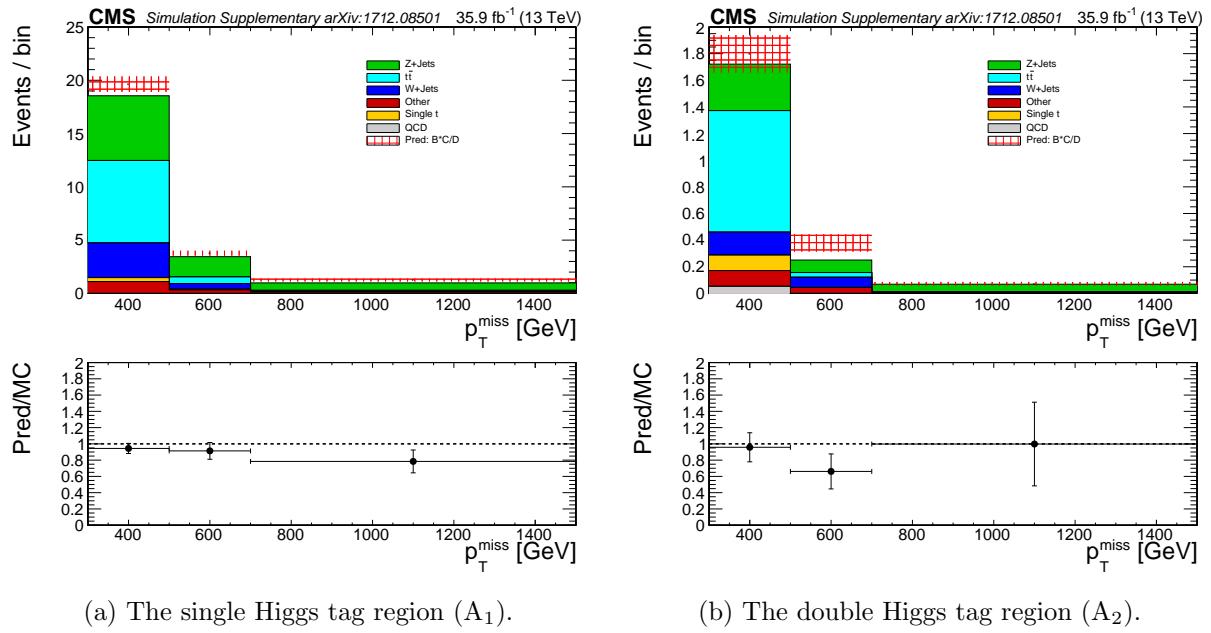


Figure 7.6: p_T^{miss} distributions and predictions in the signal regions using simulation only.

As they are orthogonal to the analysis region, we are able to test the validity of the background estimation technique independently **within** each of the three control regions. By comparing the prediction of the yields using the ABCD method with those observed, the validity of the technique can be verified for that particular background category. The comparisons for the single-photon, single-lepton and low- $\Delta\phi$ control regions can be seen in Figure 7.7. κ in the bottom panel is defined as the ratio of the true event yield to the prediction. $\kappa = 1$ represents the case in which the prediction perfectly matches the observation. These results are used for commissioning of the background estimation technique only.

7.5.2 κ as a Correction to the Estimation

A correction factor κ is applied to the prediction to account for the under-prediction of the background estimation procedure as observed in Figure 7.6. κ is obtained by dividing the yields for the signal region by that predicted:

$$\kappa \equiv A^{MC} / \left(B \cdot \frac{C}{D} \right)^{MC} \quad (7.3)$$

There are $2 \times 3 = 6$ values of κ , one for each signal bin. $\kappa = 1$ represents the case of a perfect prediction. The corrections are then applied as follows:

$$A_{1,2}^{\text{predicted}} = \kappa \cdot \left(B_{1,2} \cdot \frac{C}{D} \right)^{\text{observed}} \quad (7.4)$$

These values of κ are those that we have already seen in Figure 7.6.

The value of κ is dependent on the yields of each analysis bin and is therefore sensitive to the accuracy of the modeling in each of the 18 analysis bins. To improve the determination of κ , scale factors are derived using the data control regions to correct the normalization in each of these bins. Different scale factors are assigned separately to the Z-invisible, lost lepton, and QCD background samples. Rare processes (e.g. diboson production) are taken directly from MC.

First consider how the yield N predicted in an arbitrary bin (of 18) is the sum of the yields

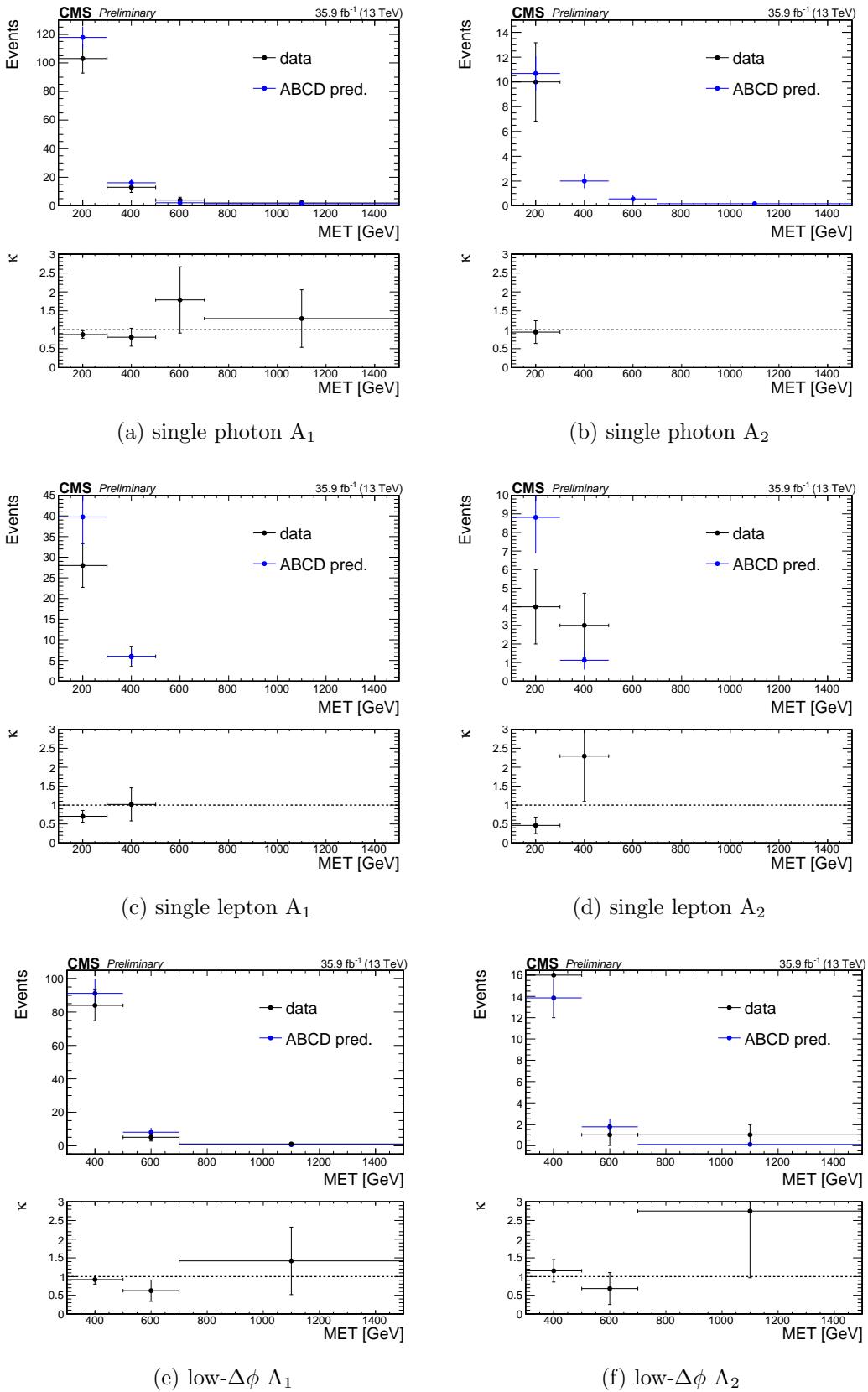


Figure 7.7: Comparisons of the predicted and observed yields within the data control regions. [43]

Table 7.2: Summary of the control region scale-factors integrated over p_T^{miss} .

Low $\Delta\phi$					
A_{SF}^{1H}	A_{SF}^{2H}	C_{SF}	B_{SF}^1	B_{SF}^2	D_{SF}
1.1 ± 0.33	0.85 ± 0.12	0.93 ± 0.1	0.88 ± 0.04	1.2 ± 0.16	0.71 ± 0.027
Single Lepton					
A_{SF}^{1H}	A_{SF}^{2H}	C_{SF}	B_{SF}^1	B_{SF}^2	D_{SF}
0.61 ± 0.04	0.59 ± 0.08	p_T^{miss} dependent	0.59 ± 0.016	0.71 ± 0.04	p_T^{miss} dependent
Photon					
A_{SF}^{1H}	A_{SF}^{2H}	C_{SF}	B_{SF}^1	B_{SF}^2	D_{SF}
0.61 ± 0.088	0.75 ± 0.29	0.5 ± 0.07	0.98 ± 0.094	2.58 ± 0.63	0.71 ± 0.035

in the different datasets ($t\bar{t}$ and $W \rightarrow \ell\nu$ are grouped as they together represent the lost-lepton background):

$$N^{MC} = N_{Z \rightarrow \nu\bar{\nu}}^{MC} + N_{tt, W \rightarrow \ell\nu}^{MC} + N_{QCD}^{MC} + N_{rare} \quad (7.5)$$

Scale factors are defined for this bin using the corresponding control regions in data and forming the ratio of events in simulation to that observed. They are then applied as follows:

$$N_{\text{corrected}}^{MC} = \left(\frac{N_{\text{single}-\gamma}^{\text{data}}}{N_{\text{single}-\gamma}^{MC}} \right) \cdot N_{Z \rightarrow \nu\bar{\nu}}^{MC} + \left(\frac{N_{\text{single}-\ell}^{\text{data}}}{N_{\text{single}-\ell}^{MC}} \right) \cdot N_{tt, W \rightarrow \ell\nu}^{MC} + \left(\frac{N_{\text{low}-\Delta\phi}^{\text{data}}}{N_{\text{low}-\Delta\phi}^{MC}} \right) \cdot N_{QCD}^{MC} + N_{rare} \quad (7.6)$$

The p_T^{miss} distribution within the control regions is shown in Figures 7.8, 7.9, and 7.10 for the single photon, single lepton, and low- $\Delta\phi$ control regions, respectively. The ratio in the bottom panel of each plot represents the scale factor for that p_T^{miss} bin. The dotted horizontal line shows the average scale factor inclusive in p_T^{miss} . These values are summarized in Table 7.2. The scale factors for the single-photon and low- $\Delta\phi$ control regions show no p_T^{miss} dependence and are determined inclusive for $p_T^{\text{miss}} > 300 \text{ GeV}$. Some of the scale factors in the single lepton region do show a p_T^{miss} dependence and are summarized in Table 7.3. In order to improve the statistical accuracy for the single lepton region, the low- $\Delta\phi$ requirement was removed.

The scale factors are then applied to the samples to give yields better representative of data. The p_T^{miss} distributions for the signal regions and expectations from the ABCD background

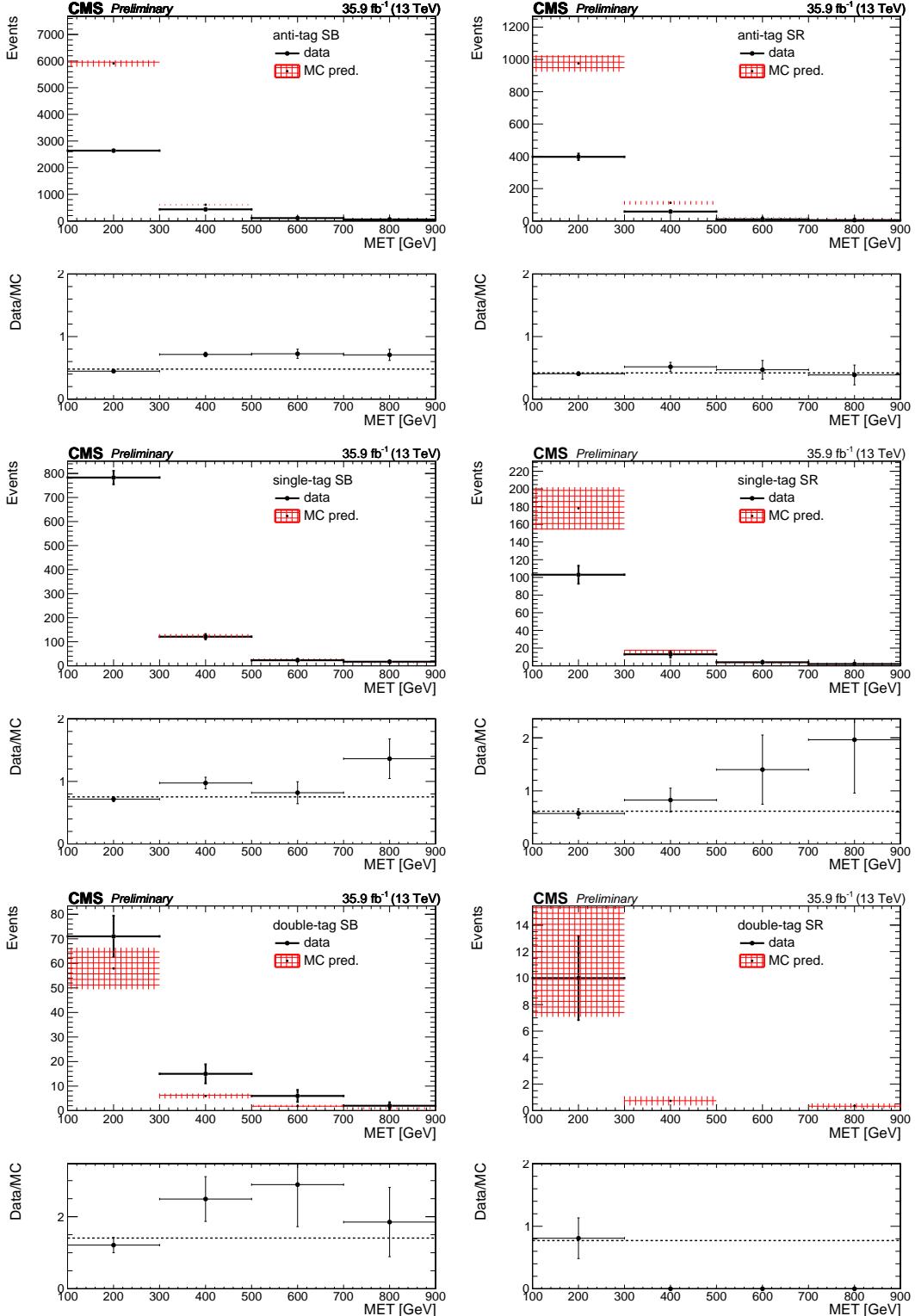


Figure 7.8: Signal and sideband yields in the single photon control region. The hashed red band denotes the prediction from simulation; the solid black points denote the observed yields in data. The Data/ ratio in the lower panel of each plot represents the scale factor for that bin. [43]

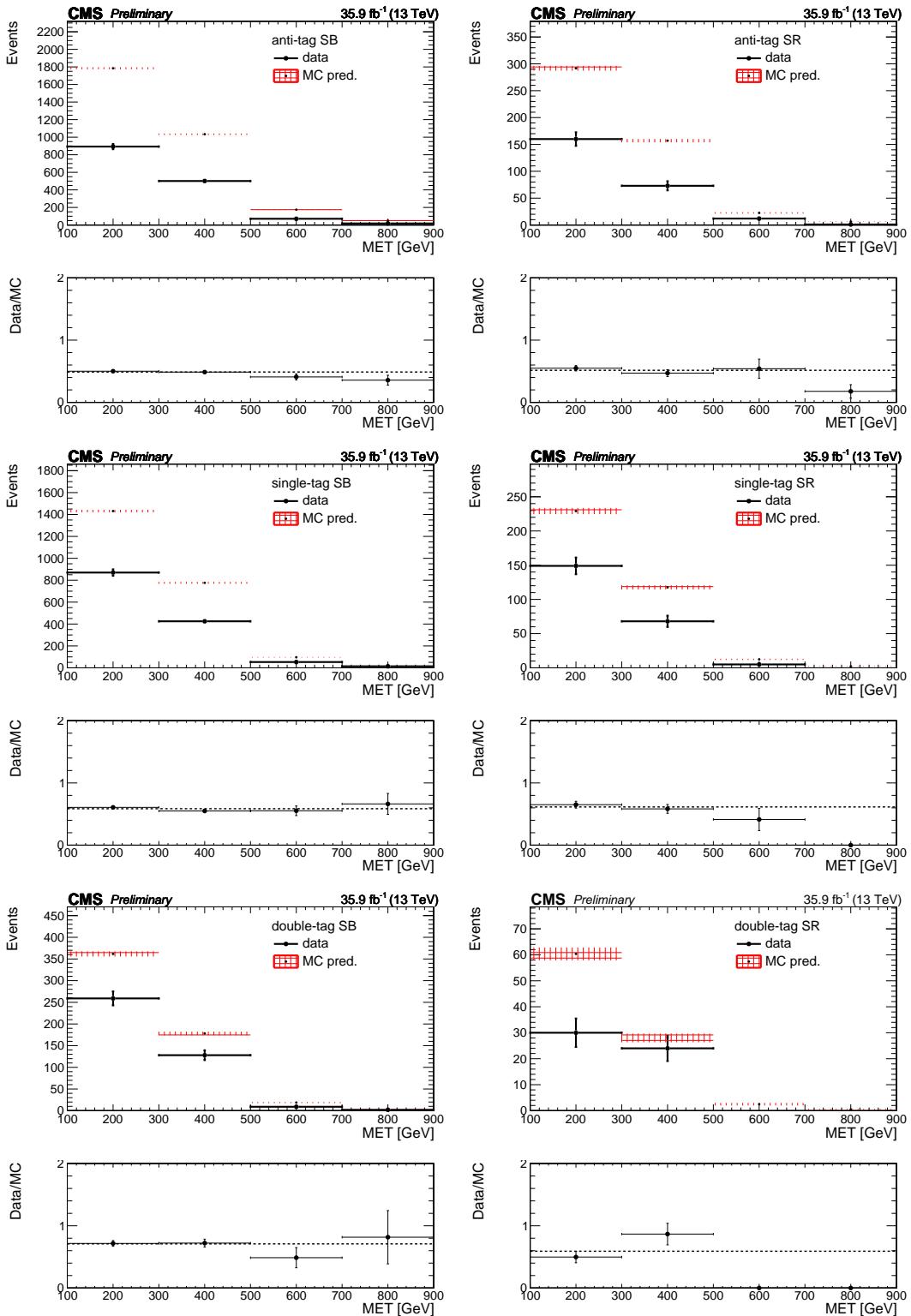


Figure 7.9: Signal and sideband yields in the single lepton control region. The hashed red band denotes the prediction from simulation; the solid black points denote the observed yields in data. The Data/ ratio in the lower panel of each plot represents the scale factor for that bin. The low- $\Delta\phi$ requirement has been removed to improve statistics. [43]

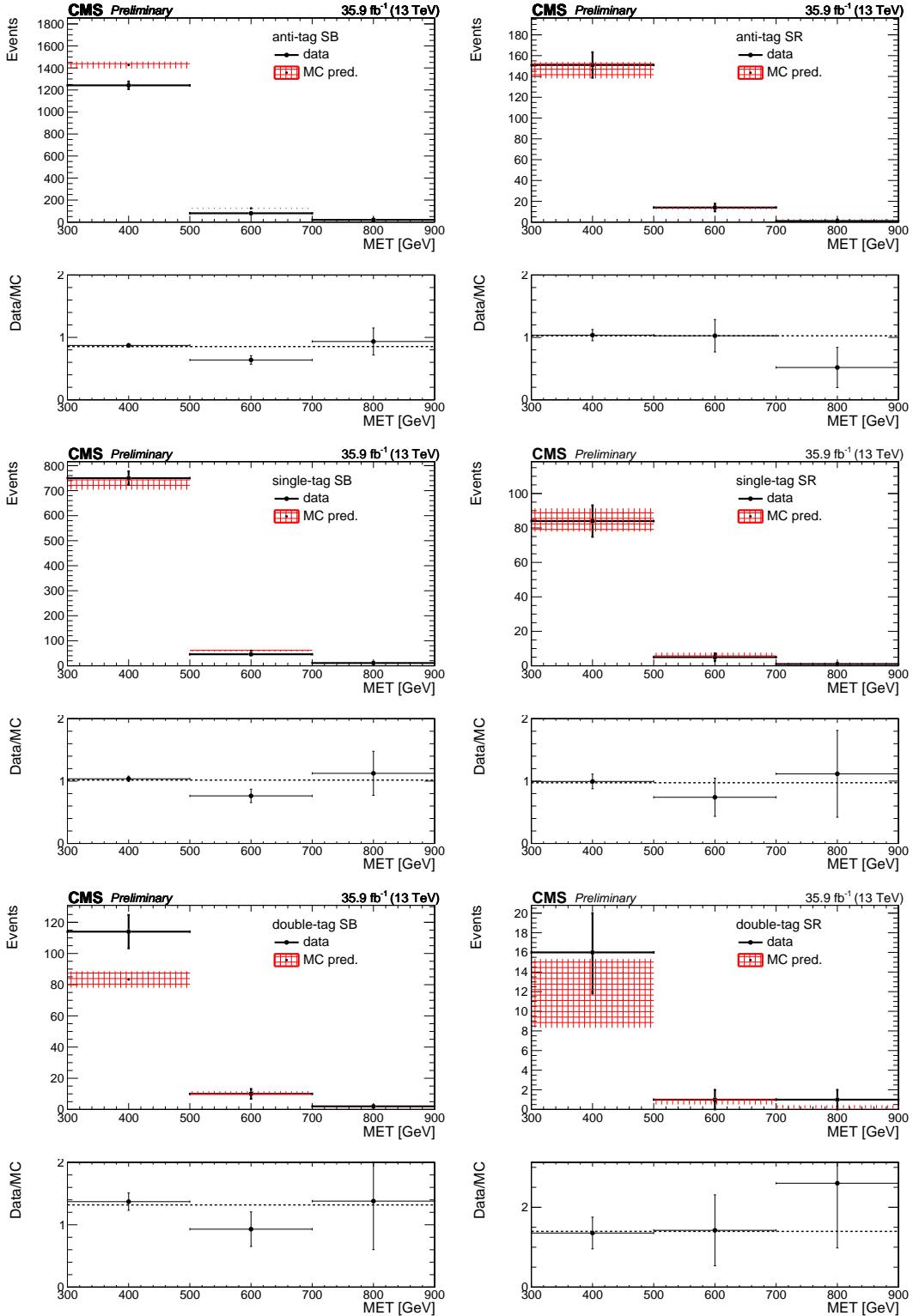


Figure 7.10: Signal and sideband yields in the the low- $\Delta\phi$ control region. The hashed red band denotes the prediction from simulation; the solid black points denote the observed yields in data. The Data/ ratio in the lower panel of each plot represents the scale factor for that bin. [43]

Table 7.3: Single lepton control region scale-factors in the anti-tag sideband region.

Single Lepton C_{SF}		
p_T^{miss} [300, 500]	[500, 700]	[700, ∞]
0.47 ± 0.05	0.54 ± 0.15	0.18 ± 0.1
Single Lepton D_{SF}		
0.49 ± 0.02	0.40 ± 0.05	0.35 ± 0.08

prediction are seen in Figure 7.11 (the data-corrected version of Figure 7.6). The improved value of κ is seen in the lower panel of each plot. The modified values of the yields in the signal region (seen in the calculation of κ) are seen in Tables 7.5 and 7.6. Since most of the scale factors are less than one the background decreases in Figure 7.11 relative to Figure 7.6 but still preserves the normalization so that κ is statistically compatible with unity. In order to obtain the best central value and error for κ , pseudo-experiments are performed allowing the yields in the ABCD regions to fluctuate according to Gaussian statistics. This procedure results in a distribution which is summarized in Table 7.4.

Table 7.4: A summary of the background estimation corrections κ .

	1-Higgs Tag	2-Higgs Tag
p_T^{miss}	κ	
[300, 500 GeV]	0.98 ± 0.11	0.73 ± 0.14
[500, 700 GeV]	0.86 ± 0.16	0.43 ± 0.12
[700, ∞ GeV]	0.86 ± 0.17	0.62 ± 0.30

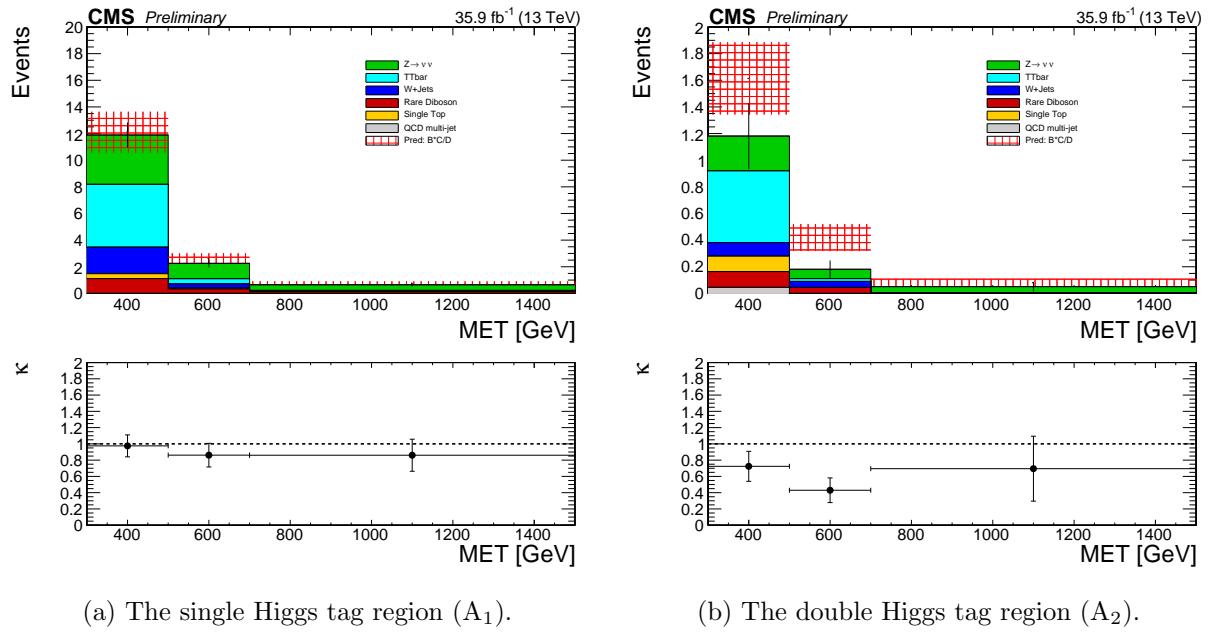


Figure 7.11: Signal region p_T^{miss} distributions using scale-factor corrected simulation. [43]

Table 7.5: Corrected yields in the signal regions. $\kappa = \text{AD} / \text{BC}$

p_T^{miss}	Z+Jets	W+Jets	TTbar	QCD	Rare	Total	Data
Region: A^{1H}							
[300, 500] GeV	3.76 ± 0.54	2.05 ± 0.30	4.87 ± 0.72	0 ± 0	1.48 ± 0.40	12.17 ± 1.03	15
[500, 700] GeV	1.18 ± 0.21	0.33 ± 0.08	0.40 ± 0.12	0 ± 0	0.39 ± 0.16	2.30 ± 0.29	2
> 700 GeV	0.43 ± 0.10	0.053 ± 0.025	0.046 ± 0.01	0 ± 0	0.13 ± 0.053	0.66 ± 0.12	1
Region: A^{2H}							
[300, 500] GeV	0.26 ± 0.12	0.11 ± 0.05	0.58 ± 0.21	0.045 ± 0.05	0.23 ± 0.12	1.24 ± 0.28	1
[500, 700] GeV	0.07 ± 0.045	0.049 ± 0.031	0.022 ± 0.0098	0 ± 0	0.045 ± 0.039	0.19 ± 0.068	0
> 700 GeV	0.044 ± 0.032	0.005 ± 0.005	0 ± 0	0 ± 0	0.002 ± 0.016	0.051 ± 0.036	0

Table 7.6: Corrected yields in the sideband regions. $\kappa = \text{AD} / \text{BC}$

p_T^{miss}	Z+Jets	W+Jets	TBar	QCD	Rare	Total	Data
Region: C							
[300, 500] GeV	17.66 ± 2.52	8.23 ± 1.44	3.87 ± 0.73	0.81 ± 0.49	2.78 ± 1.142	33.36 ± 3.24	44
[500, 700] GeV	5.20 ± 0.77	0.57 ± 0.27	0.22 ± 0.11	0 ± 0	0.63 ± 0.16	6.63 ± 0.84	12
> 700 GeV	2.48 ± 0.39	0.12 ± 0.12	0.028 ± 0.031	0 ± 0	0.14 ± 0.06	2.76 ± 0.41	4
Region: B^{1H}							
[300, 500] GeV	42.13 ± 4.17	15.61 ± 10.15	30.99 ± 20.15	1.57 ± 0.54	12.16 ± 1.37	102.47 ± 23.00	112
[500, 700] GeV	12.05 ± 1.28	2.74 ± 1.79	3.04 ± 2.00	0 ± 0	2.55 ± 0.43	20.37 ± 3.00	20
> 700 GeV	5.92 ± 0.69	0.67 ± 0.61	0.49 ± 0.46	0 ± 0	1.93 ± 0.72	9.01 ± 1.25	5
Region: B^{2H}							
[300, 500] GeV	5.51 ± 1.47	0.73 ± 0.44	4.46 ± 2.65	0.33 ± 0.23	2.06 ± 0.32	13.09 ± 3.09	13
[500, 700] GeV	1.80 ± 0.56	0.17 ± 0.11	0.59 ± 0.39	0 ± 0	0.62 ± 0.23	3.17 ± 0.73	1
> 700 GeV	0.67 ± 0.27	0.0084 ± 0.009	0.035 ± 0.031	0 ± 0	0.23 ± 0.073	0.94 ± 0.28	1
Region: D							
[300, 500] GeV	164.82 ± 8.31	61.24 ± 3.70	33.20 ± 2.16	8.50 ± 2.73	20.64 ± 1.78	288.41 ± 9.90	273
[500, 700] GeV	47.37 ± 2.52	6.36 ± 1.39	2.37 ± 0.55	0 ± 0	4.42 ± 1.46	60.51 ± 3.27	60
> 700 GeV	26.79 ± 1.50	0.99 ± 0.53	0.16 ± 0.086	0 ± 0	3.48 ± 1.01	31.42 ± 1.88	28

Table 7.7: Sideband region yields, κ , and background predictions for the 6 signal bins.

N_H	p_T^{miss} (GeV)	B	C	D	κ	$\kappa \cdot B \cdot C/D$
A_1	[300, 500 GeV]	112	44	273	0.98 ± 0.11	17.7 ± 3.8
A_1	[500, 700 GeV]	20	12	60	0.86 ± 0.16	3.4 ± 1.5
A_1	[700, ∞ GeV]	5	4	28	0.86 ± 0.17	0.61 ± 0.45
A_2	[300, 500 GeV]	13	44	273	0.73 ± 0.14	1.52 ± 0.57
A_2	[500, 700 GeV]	1	12	60	0.43 ± 0.12	0.09 ± 0.08
A_2	[700, ∞ GeV]	1	4	28	0.62 ± 0.30	$0.09^{+0.11}_{-0.09}$

7.5.3 Sideband Yields & Predictions

We have studied the background estimation technique in data control regions and found the predictions to be statistically consistent with the observed yields. We then calculated the correction to the ABCD prediction κ , using scale factors derived from control regions in data to best correct the normalization of the MC components. We can now use the observed yields in the sideband regions to form the background prediction via the ABCD method. Figure 7.12 shows the sideband yields in both data and the scale factor corrected MC. We see that the two agree within statistical errors. Table 7.7 tabulates the data yields alongside the full background prediction including κ .

7.6 Signal Systematic Uncertainties

We consider a variety of systematic uncertainties on the signal efficiency and distribution. Some are common to more inclusive SUSY analyses [44] and there are additional systematic uncertainties related to $b\bar{b}$ tagging efficiency and the effect of the pruned mass scale and resolution on the signal efficiency.

- **Luminosity:** The calculated uncertainty for the 2016 dataset is 2.5% [45].
- **Isolated Track Veto:** An uncertainty of 2% is assigned to the signal samples to account for any data/MC differences based on the study from the 2015 analysis [44].
- **Statistical Uncertainty:** The signal sample statistical uncertainty is generally 2-4%.
- **Trigger Efficiency:** The effect of the uncertainty on the signal yield is about 2%.

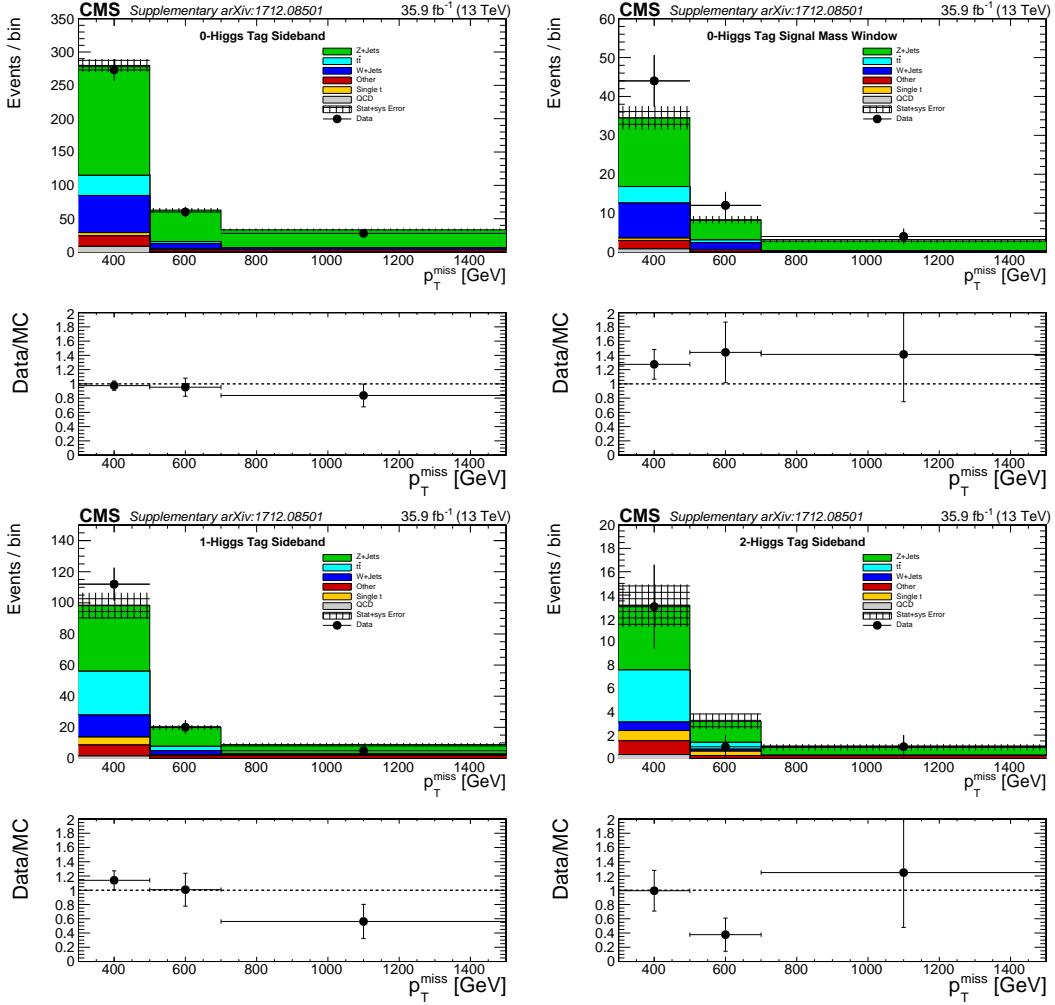


Figure 7.12: Sideband region p_T^{miss} distributions comparing data and scale-factor corrected simulation. The hatched black region denotes the prediction from simulation; the solid points denote the observed yields in data.

- **Pileup Reweighting:** MC production involves the simulation of the number of pileup interactions (vertices) in addition to the primary vertex. Corrections can be derived such that this distribution more closely resembles that as seen in data. The sensitivity of the various benchmark signal models to the pileup distribution was studied by comparing events with $n_{\text{vtx}} < 20$ (low PU) or $n_{\text{vtx}} \geq 20$ (high PU). As no difference was observed, pileup reweighting is not applied and no associated uncertainty is assessed.
- **Initial State Radiation:** Incoming partons have a non-negligible probability to radiate quarks or gluons before the 'hard' interaction occurs, this is known as initial state radiation. Corrections can be derived such that this distribution more closely resembles that as seen in data. These are derived using $t\bar{t}$ events, requiring two oppositely charged leptons and two b-tagged jets. Any **additional** jets in the event are likely to arise from initial-state radiation. The correction factors are 1.000, 0.920, 0.821, 0.715, 0.662, 0.561, 0.511 for $N_{\text{ISR}} = 0, 1, 2, 3, 4, 5, 6+$. The corrections are applied to the simulated signal samples with an additional normalization factor, typically about 1.15 (depending on the signal model), to ensure the overall cross section of the sample remains constant. The systematic uncertainty in these corrections is chosen to be half of the deviation from unity for each correction factor, with the largest effect at high p_T^{miss} .
- **Renormalization and Factorization Scales:** The renormalization scale μ_R in perturbative QCD is the energy scale one uses in the calculation of the running of the strong coupling constant. The factorization scale μ_F of the parton distribution functions characterize the energy scale of the interactions. These uncertainties are derived using the envelope of the weights by varying μ_R and μ_F by a factor of 2 [46, 47]. The effect on the yield is less than 0.1%.
- **Jet Energy Corrections:** The jet energy corrections are varied using the p_T -and η -dependent jet energy scale uncertainties from the official database. These variations are propagated into the various jet-dependent variables, including: H_T , MET, $\Delta\phi(\text{MET}, j_i)$.

The overall effect is less than 1%.

- **Jet Energy Resolution:** The jet momenta in the samples are smeared to match the jet energy resolution in data. The smearing factors are varied according to the uncertainties on the jet energy resolution measurements. These variations are propagated into the various jet-dependent variables, including: H_T , MET, $\Delta\phi(\text{MET}, j_i)$. The size of the effect is negligible.
- **Parton Distribution Functions:** The LHC4PDF prescription for the uncertainty on the total cross section is included as ± 1 sigma bands in the results plots. No additional uncertainty is considered for the uncertainty in the acceptance due to PDFs, as per SUSY group recommendation.

The above signal systematics are applied as an uncertainty on the signal normalization and are small in general. The main signal systematics come from the scale factors used to correct the data/MC differences seen in the AK8 jet double-b tagging efficiency, and from the uncertainty on the pruned mass resolution. The pruned mass scale factor is derived using W-jets in semi-leptonic $t\bar{t}$ and extrapolating to the Higgs mass. Both of these are accounted for by assigning a shape uncertainty within the signal and the sideband mass windows.

- A data/MC scale-factor is derived from double-muon tag data selected with HLT Trigger `HLT_BTagMu_AK8Jet300_Mu5_v` and muon enriched QCD Monte-Carlo. The scale factors have mainly a statistical error along with a smaller set of systematic errors due to shape systematics, Jet-Energy scale uncertainty, Pile-up corrections, uncertainty on the number of tracks, uncertainty of b-fragmentation and c-fragmentation, and the uncertainty on K_s and Λ fraction.
- The pruned mass scale-factor is derived by comparing the efficiency to select W-jets in data and within a mass window of [65, 85] GeV. The fit for the gaussian resolution of the W-mass peak is shown in Figure 7.13 and the fit results are shown in Table 7.8. The mass

Table 7.8: Fit results for W-mass resolution in data and simulation.

	Data	$t\bar{t}$
Mean	78.2 ± 0.46	78.4 ± 0.35
Sigma	10.10 ± 0.67	7.23 ± 0.48

scale between and data is consistent though predicts a narrower mass resolution compared to data. The jet mass in each event is smeared to mimic the pruned jet mass resolution in data and an uncertainty is assigned based on the ratio of efficiencies between the smeared and un-smeared cases [48].

The summary of the signal systematics and their effect on the signal yields is shown in Table 7.9. The dominant effect is from the mass resolution uncertainty.

7.7 Observed Yields in the Signal Regions

The observed yields, along with the background predictions, are seen in Table 7.10. Our signal region yields are consistent with the background expectation. Additionally, Table 7.10 shows the expected signal yields for two model points corresponding to gluino \tilde{g} masses of 2000 or 1800 GeV; the mass of the neutralino $\tilde{\chi}_1^0$ is fixed at 1 GeV; the mass splitting between the gluino \tilde{g} and neutralino $\tilde{\chi}_2^0$ is fixed at 50 GeV.

A visual representation of the single event in the double-H tagged signal bin is seen in Figure 7.15.

7.8 Exclusion Curves & Mass Limits

Interpreting our results in the context of the T5HH or T5ZH models, the absence of signal allows us to place upper limits on the cross section of gluino \tilde{g} pair production. For the statistical treatment, we use a profile-likelihood to combine the observed yields, expected background, and expected signal in all analysis bins to calculate a 95% upper limit on the signal cross section. The ABCD background estimation is explicitly coded in the likelihood, allowing the correlations in the

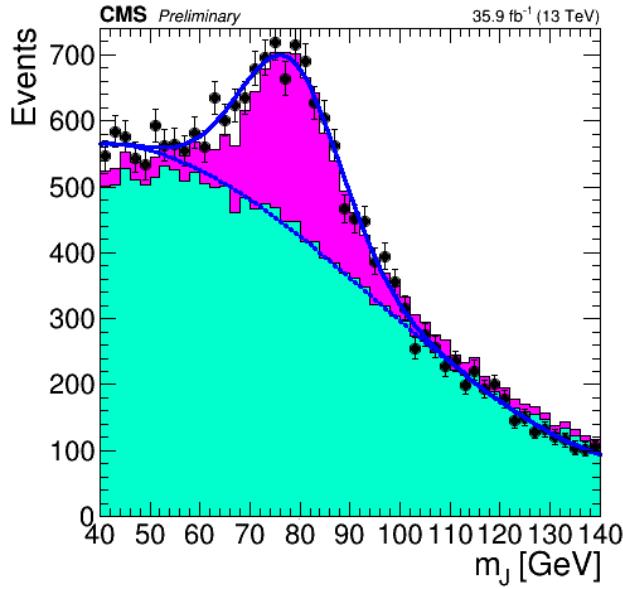


Figure 7.13: Pruned jet mass in semi-leptonic $t\bar{t}$ events. The mass peak for the W-jets is used to derive the mass resolution uncertainty. [43]

Unc. on Normalization	
Systematic	% Effect on yields
Luminosity	2.6%
Trigger Eff.	2.0%
Iso. Track Veto	2%
ISR modeling	0.01%
PDF Scale	0.1%
JEC	1%
JER	0.01%
Stat	1-4%
Shape Unc.	
Double-b SF	6%
Mass Resolution	1-15%

Table 7.9: Summary of signal shape and normalization uncertainties.

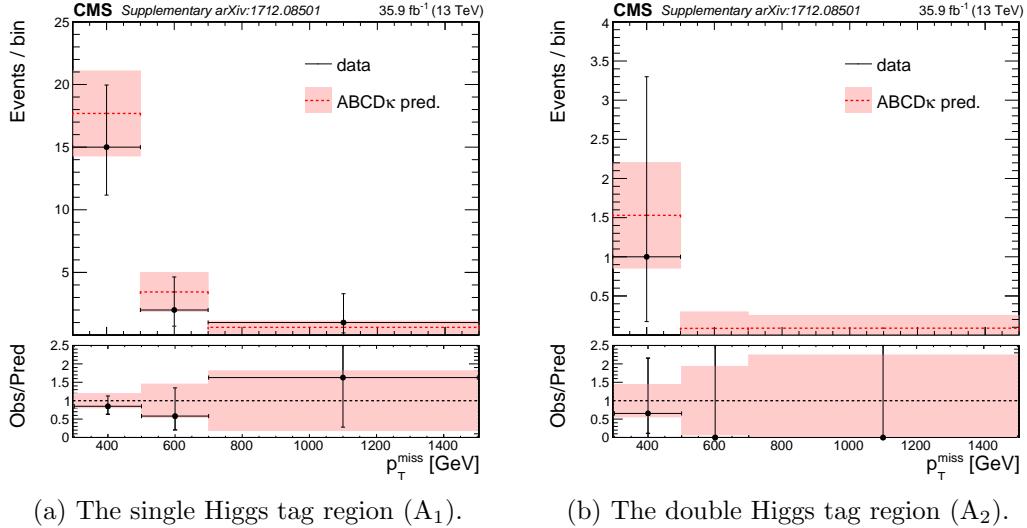


Figure 7.14: Observed yields in the signal regions.

Table 7.10: Yields and predicted background in the signal regions. Columns 2, 3, and 4 form the background prediction. Obs. represents the observed yields in data. The last two columns represent the expected yields from two model points (the gluino mass is in parenthesis).

p_T^{miss}	$B \cdot C/D$	κ	$\kappa \cdot B \cdot C/D$	Obs.	T5HH(2000)	T5HZ(1800)
1-Higgs Tag						
[300, 500 GeV]	18.05 ± 3.39	0.98 ± 0.11	17.68 ± 3.85	15	0.24	0.75
[500, 700 GeV]	4 ± 1.54	0.86 ± 0.16	3.44 ± 1.47	2	0.32	0.98
[700, ∞ GeV]	0.71 ± 0.50	0.86 ± 0.17	0.61 ± 0.45	1	2.13	4.34
2-Higgs Tag						
[300, 500 GeV]	2.09 ± 0.67	0.73 ± 0.14	1.52 ± 0.57	1	0.17	0.35
[500, 700 GeV]	0.2 ± 0.20	0.43 ± 0.12	$0.09^{+0.08}_{-0.08}$	0	0.23	0.44
[700, ∞ GeV]	0.14 ± 0.16	0.62 ± 0.30	$0.09^{+0.11}_{-0.09}$	0	1.36	1.98

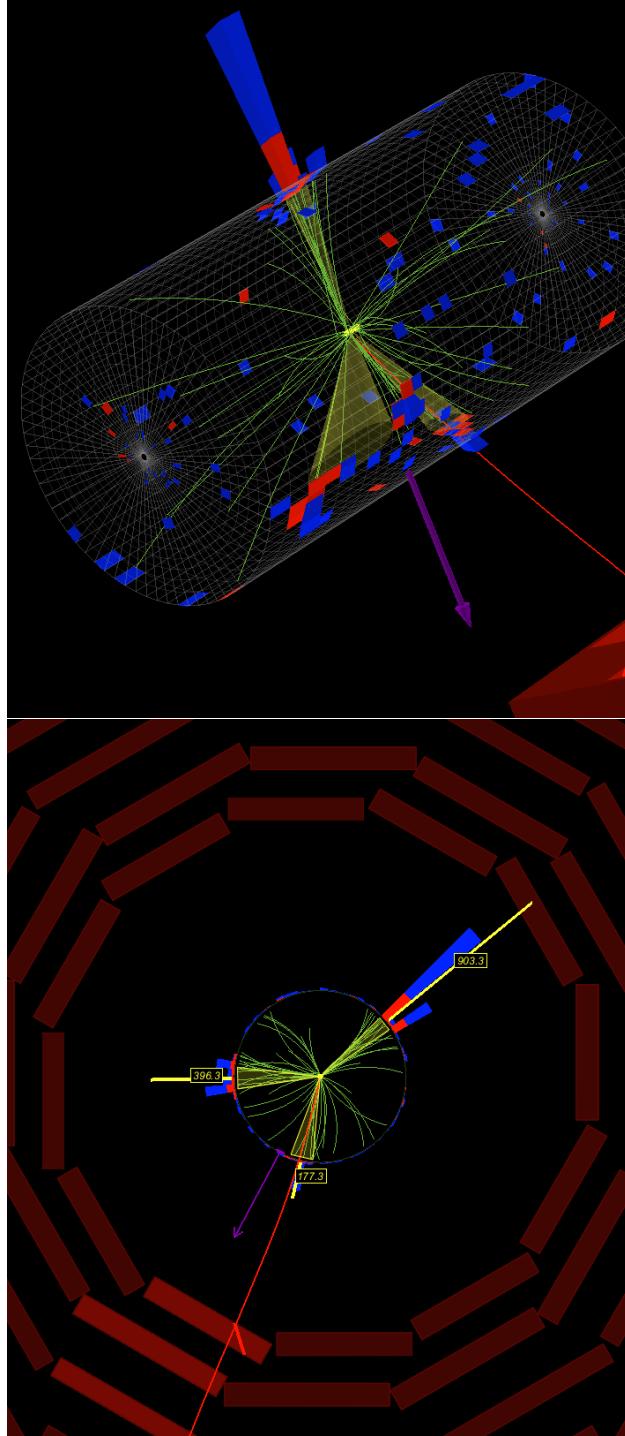


Figure 7.15: The single event in the A_2 region. The purple line represents $p_T^{miss} = 426 \text{ GeV}$. The three yellow cones represent the AK8 jets labeled with p_T . Note two additional objects not satisfying our object definition but still plotted in the representation: a) The additional low p_T and low mass jet likely from SM QCD and b) the $p_T = 18 \text{ GeV}$ muon (red line) that suffers from poor reconstruction properties.

estimations to be taken into account. The likelihood function can be expressed as:

$$\mathcal{L} = \prod_{i \in A, B, C, D} \text{Poisson}(n_i | bkg_i + r \cdot sig_i) \times \prod_j^{\text{nuisances}} \text{Constraints}(\theta_j, \hat{\theta}_j) \quad (7.7)$$

where the regions are modeled by Poisson distributions, n_i , bkg_i , and sig_i represent the yield, expected background, and expected signal in bin i. The constraints term encode the nuisance parameters θ_j : κ is modeled by a normal distribution, and the signal systematics are modeled as log-normal. The term $\hat{\theta}_j$ represents the profiled minimum of θ_j .

The expected and observed limits are then calculated based on approximations of the profile likelihood ratio using the CLs criterion [49] to place upper limits at the 95% confidence level on the production cross section, as seen in Figure 7.16. The branching fraction of the gluino to the NLSP and SM quarks, as seen in Figure 7.1, is assumed to be 100%. The allowed regions of phasespace lie below the red and blue lines. Calculations of the gluino pair production cross section [50], seen in the black line, allow us to exclude gluinos with mass lower than 2010 and 1825 GeV for the T5HH and T5ZH models, respectively. The weaker limit for the T5ZH model is due to the smaller branching fraction of the Z boson to b-quarks and our choice of signal mass window not being optimal for Z reconstruction.

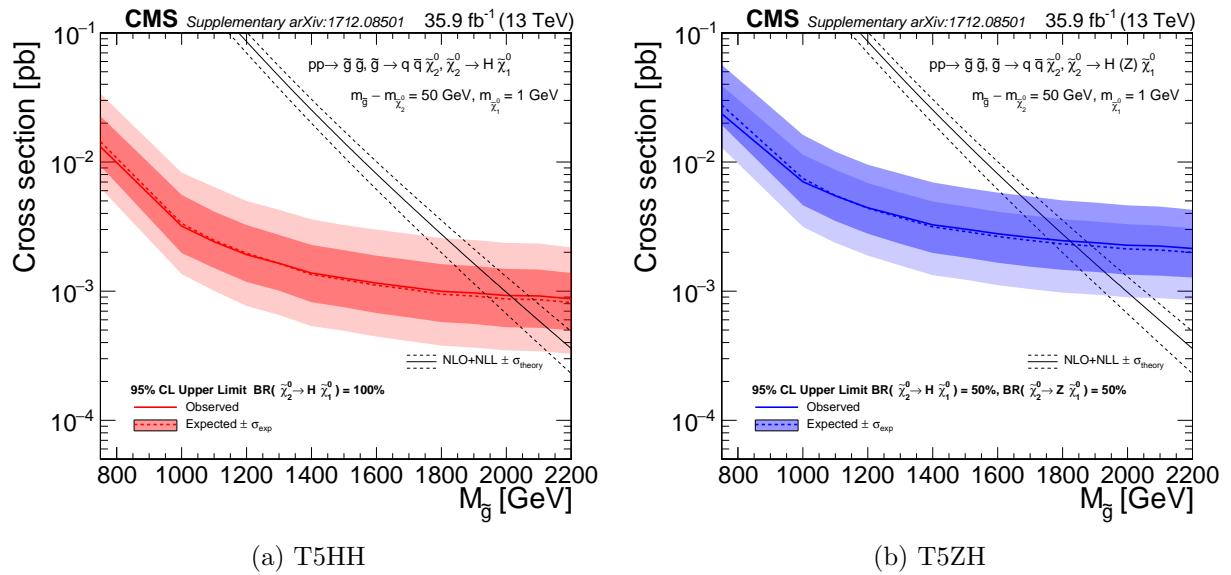


Figure 7.16: Observed and expected limits on the gluino cross section.

Chapter 8

Conclusions

This thesis presents a search for evidence of physics beyond the SM. The search targets events with two or more wide-angle jets (AK8) being consistent with boosted H or Z bosons decaying to $b\bar{b}$. The analysis makes use a dedicated heavy-flavor tagging algorithm used to identify large angle jets composed of two b quarks. We additionally require a large amount of p_T^{miss} potentially arising from a supersymmetric particle escaping detection. A data-driven method uses yields in 12 sideband bins to predict the background in 6 signal bins. Events are categorized according to the $b\bar{b}$ -tagging and masses of the highest two p_T AK8 jets, and the amount of p_T^{miss} . Backgrounds arise from QCD jet production, jets+ $Z \rightarrow \nu\bar{\nu}$, jets+ $W \rightarrow \ell\nu$, and $t\bar{t} \rightarrow qq'\ell\nu$, in which the leptons are not identified. These backgrounds are studied by defining control regions expected to be enhanced in each of these processes. In combination with simulation, these control regions are additionally used to derive corrections to the background prediction.

The observed yields in the signal bins are statistically compatible with the background expectation, and no excess of events is observed. A maximum-likelihood fit allows us to set limits on the cross section of gluino-pair production under the assumption of the T5ZH or T5HH decay models. Comparisons of our limits with the theoretical cross sections allow us to exclude gluinos with masses below 2010 and 1825 GeV at 95% confidence level for the T5HH and T5ZH models, respectively. These limits are made with the assumption that the NLSP mass is 50 GeV less than the gluino mass, and that the LSP has a mass of 1 GeV.

The work presented here has been published in Physical Review Letters in June 2018 [35].

Bibliography

- [1] CMS Collaboration, “Observation of a new boson at a mass of 125 GeV with the CMS experiment at the LHC,” *Phys. Lett. B*, vol. 716, pp. 30–61, September 2012. arXiv:1207.7235.
- [2] Wikipedia contributors, “Standard model — Wikipedia, the free encyclopedia.” , 2018. [Online; accessed 29-October-2018].
- [3] F. Halzen and A. D. Martin, *Quarks & Leptons*. Wiley, 1984.
- [4] M. Thomson, *Modern Particle Physics*. Cambridge, 6 ed., 2016.
- [5] D. J. Griffiths, *Introduction to Elementary Particles*. Wiley-VCH, 2 ed.
- [6] M. Thomson. <https://www.hep.phy.cam.ac.uk/~thomson/MPP/ModernParticlePhysics.html>.
- [7] Particle Data Group, 2018. <http://pdg.lbl.gov/2018/reviews/rpp2018-rev-ckm-matrix.pdf>.
- [8] Particle Data Group, 2018. <http://pdg.lbl.gov/2018/reviews/rpp2018-rev-neutrino-mixing.pdf>.
- [9] S. P. Martin, “A Supersymmetry Primer,” pp. 58–60, January 2016. arXiv:hep-ph/9709356v7.
- [10] J. Wess and B. Zumino, “Supergauge transformations in four dimensions,” , 1974. arXiv:0910.5530.
- [11] CMS Collaboration, “Search for supersymmetry in multijet events with missing transverse momentum in proton-proton collisions at 13 TeV,” *Phys. Rev. D*, vol. 96, p. 032003, 2017. arxiv:1704.07781.
- [12] CMS Collaboration, “Search for supersymmetry in the multijet and missing transverse momentum final state in pp collisions at 13 TeV,” *Phys. Lett. B*, vol. 758, p. 152, 2016. arXiv:1602.06581.
- [13] L. Evans and P. Bryant, “LHC Machine,” *JINST*, vol. 3, p. S08001, 2008. <http://cds.cern.ch/record/1129806/>.
- [14] Wikipedia contributors, “Large hadron collider — Wikipedia, the free encyclopedia.” , 2018. Online; accessed 29-October-2018.
- [15] “Collisions recorded by the CMS detector on 14 Oct 2016 during the high pile-up fill.” <https://cds.cern.ch/record/2231915>.

- [16] CMS Collaboration, “The CMS Tracker Project: Technical Design Report,” 1997. CERN-LHCC-98-006 ; CMS-TDR-5.
- [17] CMS Collaboration, “The CMS Tracker Project: Addendum to the Technical Design Report,” 2000. CERN-LHCC-2000-016 ; CMS-TDR-5-add-1.
- [18] D. A. Matzner Dominguez, D. Abbaneo, K. Arndt, N. Bacchetta, A. Ball, E. Bartz, W. Bertl, G. M. Bilei, G. Bolla, H. W. K. Cheung, *et al.*, “CMS Technical Design Report for the Pixel Detector Upgrade,” , September 2012. CERN-LHCC-2012-016 ; CMS-TDR-11.
- [19] CMS Collaboration, “The CMS Electromagnetic Calorimeter Project: Technical Design Report,” 1997. CERN-LHCC-97-033 ; CMS-TDR-4.
- [20] P. Bloch, R. Brown, P. Lecoq, and H. Rykaczewski, “The CMS Electromagnetic Calorimeter Project: Addendum to the Technical Design Report,” 2002. CERN-LHCC-2002-027 ; CMS-TDR-4-add-1.
- [21] CMS Collaboration, “The CMS Hadron Calorimeter Project: Technical Design Report,” 1997. CERN-LHCC-97-031 ; CMS-TDR-2.
- [22] CMS Collaboration, “Performance of the CMS Hadron Calorimeter with Cosmic Ray Muons and LHC Beam Data,” *JINST*, vol. 5, March 2010. arXiv:0911.4991.
- [23] CMS Collaboration, “The CMS Magnet Project: Technical Design Report,” 1997. CERN-LHCC-97-010 ; CMS-TDR-1.
- [24] CMS Collaboration, “Precise Mapping of the Magnetic Field in the CMS Barrel Yoke using Cosmic Rays,” . arXiv:0910.5530.
- [25] CMS Collaboration, “The CMS Muon Project: Technical Design Report,” 1997. CERN-LHCC-97-032 ; CMS-TDR-3.
- [26] CMS Collaboration, “Performance of the CMS Drift Tube Chambers with Cosmic Rays,” *JINST*, vol. 5, March 2010. arXiv:0911.4855.
- [27] CMS Collaboration, “The performance of the CMS muon detector in proton-proton collisions at $\sqrt{s} = 7$ TeV at the LHC,” *JINST*, vol. 8, November 2013. arXiv:1306.6905.
- [28] CMS Collaboration, “Performance of the CMS cathode strip chambers with Cosmic Rays,” *JINST*, vol. 5, March 2010. arXiv:0911.4992.
- [29] Costantini et al., “Uniformity and Stability of the CMS RPC Detector at the LHC,” *JINST*, vol. 8, 2013. arXiv:1209.1989.
- [30] CMS Collaboration, “The CMS trigger system,” *JINST*, vol. 12, p. 01020, 2017. arXiv:1609.02366.
- [31] CMS Collaboration, “Description and performance of track and primary-vertex reconstruction with the CMS tracker,” *JINST*, vol. 9, October 2014. arXiv:1405.6569.
- [32] CMS Collaboration, “Particle-flow reconstruction and global event description with the CMS detector,” *JINST*, vol. 12, p. 10003, 2017. arXiv:1706.04965.

- [33] M. Cacciari, G. P. Salam, and G. Soyez, “The anti-kt jet clustering algorithm,” *JHEP*, no. 04, p. 063, 2008. arXiv:0802.1189.
- [34] CMS Collaboration, “Identification of double-b quark jets in boosted event topologies,” 2016. CMS-PAS-BTV-15-002.
- [35] CMS Collaboration, “Search for physics beyond the standard model in events with high-momentum Higgs bosons and missing transverse momentum in proton-proton collisions at 13 TeV,” *Phys. Rev. Lett.*, vol. 120, p. 241801, 2018. arXiv:1712.08501.
- [36] Sabine Kraml, Suchita Kulkarni, Ursula Laa, Andre Lessa, Wolfgang Magerl, Doris Proschofsky-Spindler, Wolfgang Waltenberger, “SModelS: a tool for interpreting simplified-model results from the LHC and its application to supersymmetry,” *The European Physical Journal C*, May 2014. arXiv:1312.4175.
- [37] CMS Collaboration, “Search for supersymmetry in pp collisions at $\sqrt{s} = 13$ TeV in the single-lepton final state using the sum of masses of large-radius jets,” *JHEP*, August 2016. arXiv:1605.04608.
- [38] J. R. W. Stephen D. Ellis, Christopher K. Vermilion, “Recombination Algorithms and Jet Substructure: Pruning as a Tool for Heavy Particle Searches,” *Phys. Rev. D*, May 2010. arXiv:0912.0033.
- [39] J. Alwall, R. Frederix, S. Frixione, V. Hirschi, F. Maltoni, O. Mattelaer, H.-S. Shao, T. Stelzer, P. Torrielli, and M. Zaro, “The automated computation of tree-level and next-to-leading order differential cross sections, and their matching to parton shower simulations,” *JHEP*, vol. 07, p. 079, 2014. arXiv:1405.0301.
- [40] R. D. Ball et al., “Parton distributions for the LHC Run II,” *JHEP*, vol. 04, p. 040, 2015. arXiv:1410.8849.
- [41] T. Sjöstrand, S. Ask, J. R. Christiansen, R. Corke, N. Desai, P. Ilten, S. Mrenna, S. Prestel, C. O. Rasmussen, and P. Z. Skands, “An introduction to PYTHIA 8.2,” *Computer Physics Communications*, vol. 191, pp. 159–177, June 2015. arXiv:1410.3012.
- [42] S. Agostinelli et al., “GEANT4—a simulation toolkit,” *Nucl. Instrum. Meth. A*, vol. 506, p. 250, July 2003. [https://doi.org/10.1016/S0168-9002\(03\)01368-8](https://doi.org/10.1016/S0168-9002(03)01368-8).
- [43] W. Ford, J. Hirschauer, F. Jensen, M. Krohn, O. Long, R. Patel, K. Stenson, K. Ulmer, C. Vernieri, and A. Whitbeck, “Search for supersymmetry using boosted Higgses and missing transverse momentum in proton-proton collisions at 13 TeV,” , 2016. CMS AN-16-395.
- [44] CMS Collaboration, “Search for supersymmetry in multijet events with missing transverse momentum in proton-proton collisions at 13 TeV,” CMS AN-16-350.
- [45] “CMS Luminosity Measurements for the 2016 Data Taking Period,” Tech. Rep. CMS-PAS-LUM-17-001, CERN, Geneva, 2017.
- [46] M. Cacciari, S. Frixione, M. L. Mangano, P. Nason, and G. Ridolfi, “The $t\bar{t}$ cross-section at 1.8 TeV and 1.96 TeV: A Study of the systematics due to parton densities and scale dependence,” *JHEP*, vol. 4, no. 2004, p. 068, 2004. arXiv:hep-ph/0303085.

- [47] S. Catani, D. de Florian, M. Grazzini, and P. Nason, “Soft gluon resummation for Higgs boson production at hadron colliders,” *JHEP*, vol. 07, p. 028, 2003. arXiv:hep-ph/0306211.
- [48] I. Belotelov, I. Golutvin, D. Bourilkov, A. Lanyov, E. Rogalev, M. Savina, and S. Shmatov, “Identification and calibration of boosted hadronic W/Z bosons at 13 TeV,” CMS AN-16-215.
- [49] A. L. Read, “Presentation of search results: the cl s technique,” *Journal of Physics G: Nuclear and Particle Physics*, vol. 28, no. 10, p. 2693, 2002.
- [50] C. Borschensky, M. Krämer, A. Kulesza, M. Mangano, S. Padhi, T. Plehn, and X. Portell, “Squark and gluino production cross sections in pp collisions at $\sqrt{s} = 13, 14, 33$ and 100 TeV,” *Eur. Phys. J.*, vol. C74, no. 12, p. 3174, 2014. arXiv:1407.5066.
- [51] “Identification of double-b quark jets in boosted event topologies,” Tech. Rep. CMS-PAS-BTV-15-002, CERN, Geneva, 2016.
- [52] “Identification of b quark jets at the CMS Experiment in the LHC Run 2,” Tech. Rep. CMS-PAS-BTV-15-001, CERN, Geneva, 2016.
- [53] https://www-d0.fnal.gov/Run2Physics/top/top_public_web_pages/top_feynman_diagrams.html.
- [54] A. M. Sirunyan et al., “Identification of heavy-flavour jets with the CMS detector in pp collisions at 13 TeV,” *JINST*, vol. 13, p. P05011, 2018.
- [55] Jesse Thaler, Ken Van Tilburg, “Identifying Boosted Objects with N-subjettiness,” *JHEP*, March 2011. arXiv:1011.2268.
- [56] Jesse Thaler, Ken Van Tilburg, “Maximizing Boosted Top Identification by Minimizing N-subjettiness,” *JHEP*, February 2012. arXiv:1108.2701.

Appendix A

b \bar{b} -tagging of AK8 Jets

A novel approach has been studied to identify large-radius jets composed of two b quarks [51]. A dedicated multivariate (MVA) tagging algorithm is implemented to combine the information from secondary vertices, tracks, and subjet axes to optimize the discrimination between jets containing two b quarks and those containing a single parton. Input variables which do not depend on the momentum or mass of the parent are chosen to allow consistent performance over a wide range. Tracks with $p_T > 1 \text{ GeV}$ are associated to a jet if they are within a cone of $\Delta R < 0.8$ around the jet. A track is associated with a subjet if its distance of closest approach with the subjet axis is less than $700 \mu\text{m}$ and if its distance of closest approach with the primary vertex is less than 5 cm. The impact parameter significance with respect to the primary vertex is used to discriminate tracks from b decay with prompt tracks. Several input variables make use of the secondary vertices that are reconstructed using the Inclusive Vertex Finder [52], which identifies secondary vertices independently of the jet clustering. The list of final input variables to the MVA discriminant are detailed in [51]. Figure A.1 shows the discrimination between signal $H \rightarrow b\bar{b}$ and background jets based on the true number of b-hadrons.

The central and right plots of Figure A.2 show the signal efficiency for a $H \rightarrow b\bar{b}$ jet to pass the Double-b tag cut for the [85, 135 GeV] and [50, 250 GeV] mass windows, respectively. The efficiencies are computed by matching reconstructed jets to a generator-level Higgs or Z boson based on an angular requirement, $\Delta R < 0.8$, between the jet and the appropriate generated particle. Additionally, the reconstructed jet is required to have one or more generated b-hadrons associated

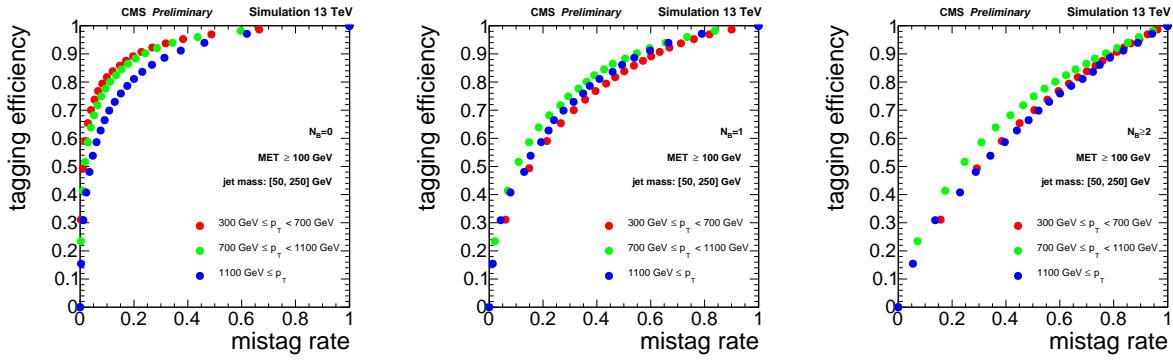


Figure A.1: ROC curve of the signal efficiency and mistag rate for the $b\bar{b}$ tagger. The mistag rate is calculated using all expected SM backgrounds.

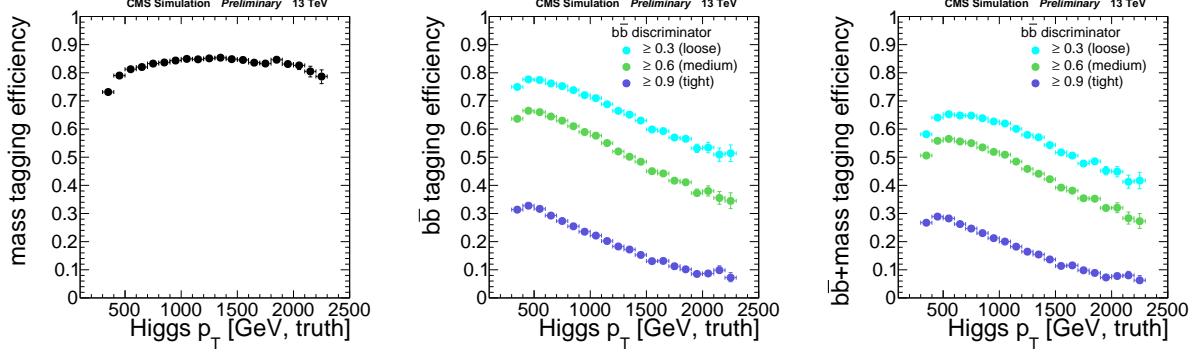


Figure A.2: The efficiency of a $H \rightarrow b\bar{b}$ jet to have mass [85, 135 GeV], as a function of the generator-level p_T (left). The efficiency of a $H \rightarrow b\bar{b}$ jet to pass the double-b tagging requirement, for three different working points (center). The efficiency of a $H \rightarrow b\bar{b}$ jet to pass both the tight mass and double-b tagging requirements (right).

with it (`jet.jetFlavourInfo().getbHadrons().size()`). The efficiency is above 80% for the Double-b discriminator alone, and drops to 65% when the pruned mass cut is applied. At high jet p_T there is an inefficiency in the double-b tag as tracks from the b quarks become more collimated. The QCD background consists of some mistagged light flavor jets and jets with true b-hadrons that can come from gluon splitting or flavor excitation. The $t\bar{t}$ background has both true heavy flavor jets and true p_T^{miss} , but a good number of the single b-hadron jets can be rejected with the Double-b tag requirement.

Figure A.3 shows the signal efficiency for $H(b\bar{b})H(b\bar{b})$ and $H(b\bar{b})Z(q\bar{q})$ signal models as a function of the double-b discriminator value. For the model with $H(b\bar{b})H(b\bar{b})$, the efficiency is plotted against the smaller of the double-b discriminators of the leading and sub-leading jet, since both are expected to have two b-quarks. For the model with $H(b\bar{b})Z(q\bar{q})$, only one jet is expected to have two b-quarks, so the efficiency is plotted against the larger double-b discriminator value between the leading and sub-leading jet. We use the loose working point of the double-b cut at 0.3 to consider a jet to be double tagged.

The efficiency of the double-b tagger is measured in a data sample consisting of high p_T jets enriched in $b\bar{b}$ from gluon-splitting. To select a boosted topology similar to the signal, the AK8 jet

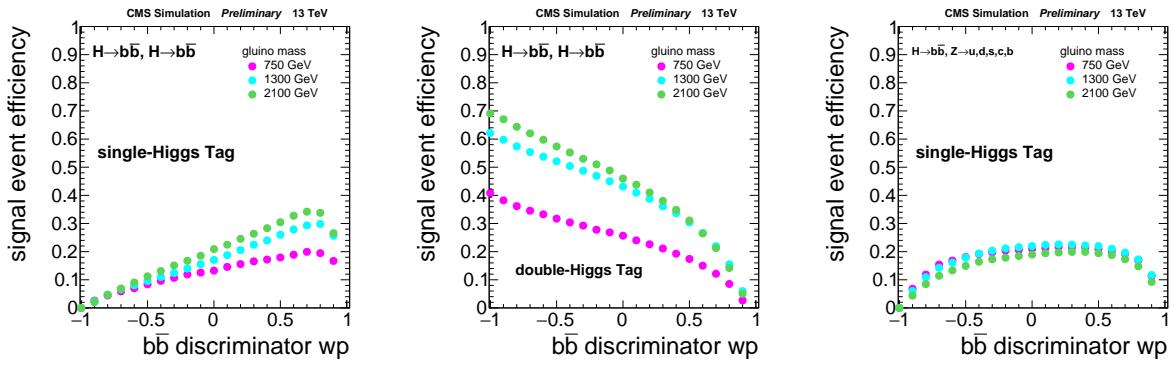


Figure A.3: Signal efficiency to be in the single or double Higgs tag event category, as a function of the double-b discriminator working-point. Efficiencies are relative to baseline selection. The left and center plots show the single and double Higgs tag efficiencies for the Higgs($b\bar{b}$)-Higgs($b\bar{b}$) MC. The right plot shows the single Higgs tag efficiency for the Z($q\bar{q}$)-Higgs($b\bar{b}$) MC. The curves for three representative gluino masses are shown here.

Table A.1: Data/MC scale factors for AK8 jet $b\bar{b}$ -tagging, for the loose working point $\mathcal{D}_{bb} > 0.3$.

p_T [GeV]	Signal SF
250-350	$0.94 + 0.03 - 0.02$
350-430	$1.00 + 0.04 - 0.03$
430-840	$1.01 + 0.02 - 0.04$

p_T is required to be above 300 GeV and the AK8 pruned mass is required to be above 50 GeV. The jet must also be matched to at least two muons with $p_T > 7\text{GeV}$ and within $\Delta R < 0.4$ of the sub-jet axis so that the jet can be “double-muon tagged”. The difference between data and MC is compared to give a data/MC scale factor which is fairly close to unity. The mis-tag rate is evaluated by comparing data and MC for top-quark jets faking H jets in $t\bar{t}$ production. The studies are based on single lepton $t\bar{t}$ events and the event selection requires one isolated muon with $p_t > 50\text{ GeV}$ and an AK4 jet in the same hemisphere. More details can be found in [51]. Table A.1 lists the data/MC scale-factors that correct for the efficiency difference between data and simulation based on the jet p_T . The final signal efficiency is scaled based on these scale-factors, and the double-b efficiency systematic of the signal is based on the uncertainty of these scale-factors. For p_T values above the limit of 840 GeV, the scale factor at this limit is used with twice the uncertainty for the signal systematic.

Appendix B

Reinterpretation

In Section 7.7, we presented our observed yields in the signal region and found they were consistent with the background expectations. Armed with this information, we were able to set upper limits on the cross sections of the T5HH and T5ZH SMS models (as a function of the gluino mass). As these two models are certainly not the only possibility for new physics to arise, it is important that we provide additional information necessary to cast other models within the context of our analysis. This information allows a model builder to make predictions of the yields for their models of similar construction. They can compare these yields to the ones we observed in our analysis and see if their model has potential for further investigation or would already be ruled out.

We present the efficiencies for mass-tagging and $b\bar{b}$ -tagging of Higgs and Z bosons reconstructed as AK8 jets. Tagging efficiencies for the five largest decay modes relevant to the analysis for the H boson are seen in Figure B.1. Tagging efficiencies for the hadronic decay modes of the Z boson are seen in Figure B.2. The lower mass tagging efficiency for the Z boson is due to the signal mass window [85, 135 GeV] not being optimal for the Z boson.

In the analysis, each event is categorized depending on the mass and $b\bar{b}$ -tagging of the two AK8 jets. Among these combinations, three are related to $b\bar{b}$ -tagging: they can both be tagged, one-and-only-one can be tagged, or neither of them can be tagged. There are two relevant combinations for the mass-tagging among the jets: they are both within the signal mass window [85, 135 GeV], or not. On an event-by-event basis, given the p_T of the Higgs or Z bosons from the model, we can use the provided efficiency maps to form event weights for each of the 6 analysis bins for the event.

Table B.1: Effective event weights for $b\bar{b}$ and mass tagging of AK8 jets.

2 bb-tagged	$W_{2b} = j_{0,bb} \cdot j_{1,bb}$
1 $b\bar{b}$ -tagged	$W_{1b} = j_{0,bb} \cdot (1 - j_{1,bb}) + (1 - j_{0,bb}) \cdot j_{1,bb}$
0 $b\bar{b}$ -tagged	$W_{0b} = (1 - j_{0,bb}) \cdot (1 - j_{1,bb})$
2 mass-tagged	$W_m = j_{0,m-sig} \cdot j_{1,m-sig}$
! (2 mass-tagged)	$W_{!m} = (j_{0,m-side} \cdot j_{1,m-sig}) + (j_{1,m-sig} \cdot j_{1,m-side}) + (j_{0,m-side} \cdot j_{1,m-side})$

As these weights are dependent on the decay mode of the boson, we additionally need to make sure to choose the correct map. The total expected yields in each bin are then obtained by summing these weights over the events in the sample.

For each event, we form “primitive weights”, which combine the status of the mass and $b\bar{b}$ -tagging, these are seen in Table B.1. $j_{0,bb}$ represents the probability that the leading AK8 jet is $b\bar{b}$ -tagged, $j_{0,m-sig}$ represents the probability that the leading AK8 jet falls within the signal mass window [85, 135 GeV], and $j_{0,m-side}$ represents the probability that the leading AK8 jet falls within the sideband mass window [50, 85]+[135, 250 GeV].

Now that these weights are formed we can combine them appropriately to make event weights for the individual analysis bins. The weights for a given bin are then summed over the total number of events in the sample. The weights for each analysis bin are shown in Figure B.3.

As a test of closure, the prescription is tested using the T5HH model with a gluino mass of 2200 GeV. The yields in each of the 6 analysis bins for this model point (inclusive in p_T^{miss}) are listed in Table B.2 under the heading “RECO truth”. As the efficiency maps are p_T dependent, we have the choice of using the momentum of the reconstructed or the generated bosons. The “RECO prediction” column in the table uses the reconstructed momentum as input, “GEN prediction” uses the generated momentum. The largest deficit is in the D region, with a difference of -36% from nominal. The greatest over-prediction is found in the B2 region, with a surplus of +8.2% events relative to nominal. The closure in the other bins fall somewhere in this range.

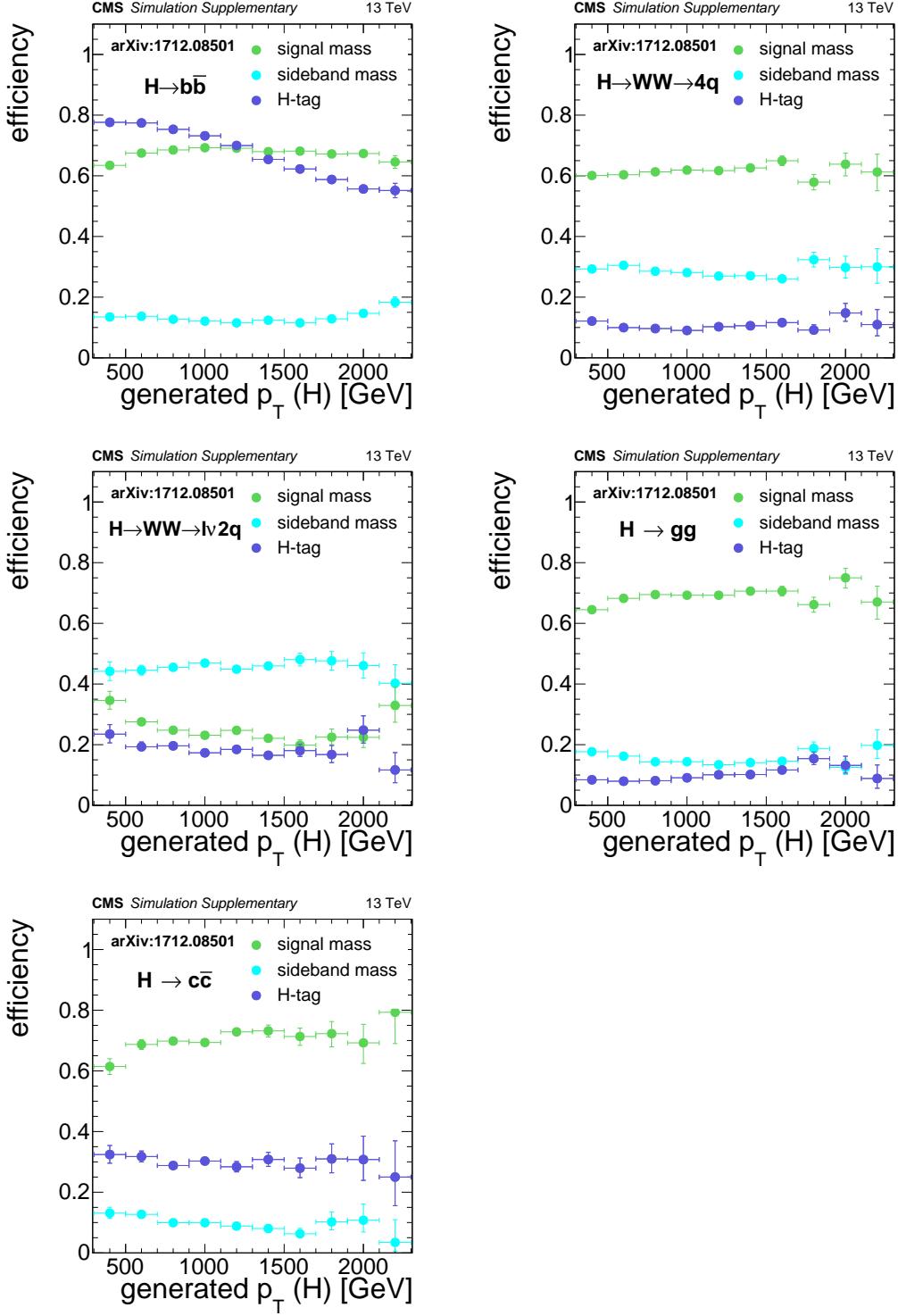


Figure B.1: Efficiencies for an AK8 jet originating from H boson decay, relative to baseline selection. "signal mass" represents the probability the jet will have mass [85, 135 GeV]. "sideband mass" represents the probability the jet will have mass [50, 85 GeV] or [135, 250 GeV]. "H-tag" represents the probability the jet have a double-b discriminator value greater than 0.3, for jets with mass [50, 250 GeV]. Efficiencies were derived using the T5ZH with a gluino mass of 2200 GeV.

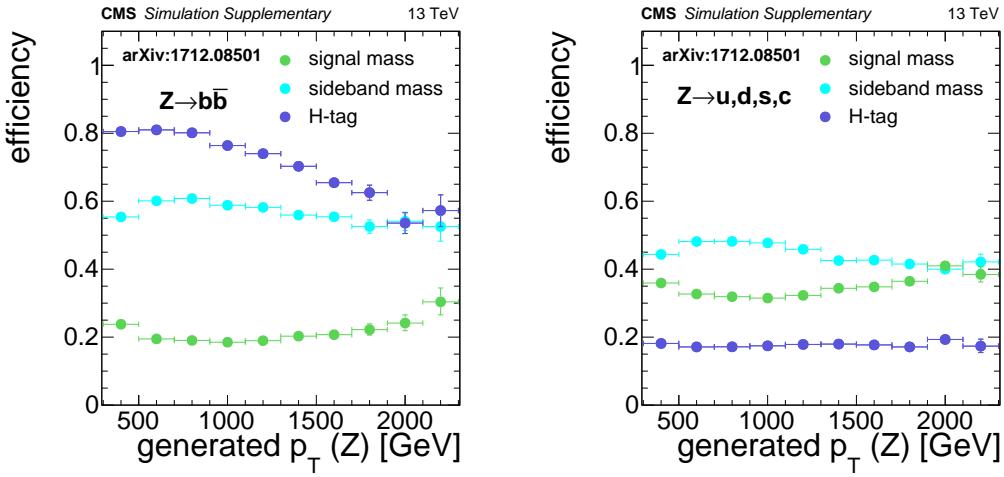


Figure B.2: Efficiencies for an AK8 jet originating from Z boson decay, relative to baseline selection. "signal mass" represents the probability the jet will have mass [85, 135 GeV]. "sideband mass" represents the probability the jet will have mass [50, 85 GeV] or [135, 250 GeV]. "H-tag" represents the probability the jet have a double-b discriminator value greater than 0.3, for jets with mass [50, 250 GeV]. Efficiencies were derived using the T5ZH with a gluino mass of 2200 GeV.

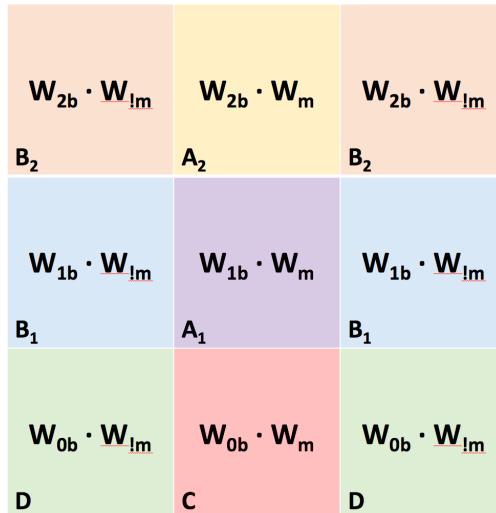


Figure B.3: Diagram for compiling the weights into each of the 6 analysis bins. (See Figure 7.4.)

Table B.2: Comparison of the event yields in the 6 analysis regions with those obtained via the prediction. The prediction was made using the T5HH signal MC with a gluino mass of 2200 GeV. Event yields are scaled to a luminosity of 35.9 fb^{-1} .

	RECO “truth”	RECO prediction	GEN prediction
Baseline	4.08	3.46 (-15%)	3.53 (-16%)
A1	1.21	1.18 (-2.3%)	1.26 (+3.6%)
A2	0.777	0.748 (-3.7%)	0.815 (+4.7%)
B1	0.802	0.703 (-12%)	0.664 (-21%)
B2	0.322	0.338 (+5.0%)	0.350 (+8.2%)
C	0.498	0.473 (-4.9%)	0.487 (-2.1%)
D	0.478	0.353 (-25%)	0.308 (-36%)

Appendix C

Determining $b\bar{b}$ -tagging Scale Factors for W jets in $t\bar{t}$ Events

At LHC energies, $t\bar{t}$ production has a large production cross section and often makes up a substantial component of the background for physics analyses. These events have a rich final state with two b jets from each of the top decays, and hadrons or leptons from the decay of each of the W bosons. Semileptonic $t\bar{t}$ events, illustrated in Figure C.1, are events in which one W decays to a lepton and neutrino, and the other decays hadronically. These events have a true source of missing energy (p_T^{miss}), and additionally can result in boosted W bosons.

Although W bosons do not decay to b-quarks (the top quark is too heavy), the $b\bar{b}$ -tagger, described in Section 7.2 has a non-zero probability to tag one of these jets as having decayed to a $b\bar{b}$ pair. This *mistag* rate can, in principle, be different in simulation compared to in data. Depending on the use, it may be necessary to apply *scale factors* to the simulation to correct for this difference. This appendix provides a description of how these scale factors and their uncertainties are determined.

To obtain a clean source of hadronically decaying W bosons, events are selected that are consistent with semileptonic $t\bar{t}$ events. The events are obtained from a data sample with a trigger requirement of at least one muon with $p_T > 50 \text{ GeV}$ and are reconstructed in the same manner as described in Chapter 6. In particular, jets are reconstructed with the anti- kt algorithm [33] operated with distance parameters of 0.4 (AK4 jets) and 0.8 (AK8 jets). The events are required to have a single muon with $p_T > 50 \text{ GeV}$ and $|\eta| < 2.1$ and be close ($\Delta\phi < 2\pi/3$) to a b-tagged AK4 jet, where the loose b-tagging working point of the CSV algorithm is used [54]. Away from

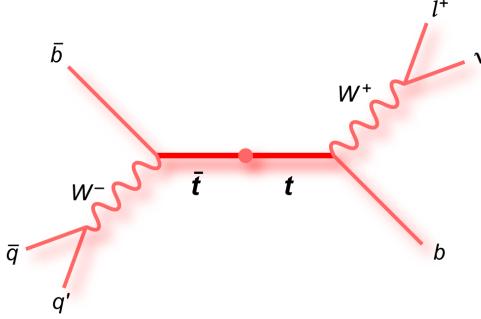


Figure C.1: Diagram of a semileptonic $t\bar{t}$ event; one W boson decays leptonically and one W boson decays hadronically [53].

this muon ($\Delta\phi > 2\pi/3$), we require at least one AK8 jet with $p_T > 250$ GeV and $|\eta| < 2.4$, intended to be the W jet. To increase the purity of the sample, three additional criteria are applied:

- The AK8 jet must be consistent with having a two-jet substructure. This requirement is made by defining a variable “ n -subjettiness” which parametrizes the degree to which an AK8 jet is consistent with having n subjets [55, 56]. The variable is calculated by forming a p_T weighted sum of the ΔR distance of every particle in the jet with its nearest subjet, for some fixed number of subjets: $\tau_N = \frac{1}{d_0} \sum_k p_{T,k} \min\{\Delta R_{1,k}, \Delta R_{2,k}, \dots, \Delta R_{N,k}\}$, where $d_0 = 0.8 \sum_k p_{T,k}$, is a normalization parameter. The ratio τ_2/τ_1 is formed to discriminate between jets with two subjets from those with one.
- The AK8 jet mass must be between 50 and 200 GeV. This is consistent with the W boson mass of 80.379 GeV, and tends to reject jets arising from QCD-only interactions, which tend to have lower mass.
- To minimize contamination from nearby objects, no AK4 jets are allowed within $\Delta R = \sqrt{(\Delta\phi)^2 + (\Delta\eta)^2} < 0.8$ of the selected AK8 jet.

Figure C.2 (left) shows the AK8 jet mass distribution from data and simulation after all selection criteria have been applied. The distribution peaks near the W boson mass (80.379 GeV) and is dominated by the desired signal. There is also a shoulder near the top quark mass (173.0 GeV), which arises from the merging of a W boson and a b quark into a single AK8 jet.

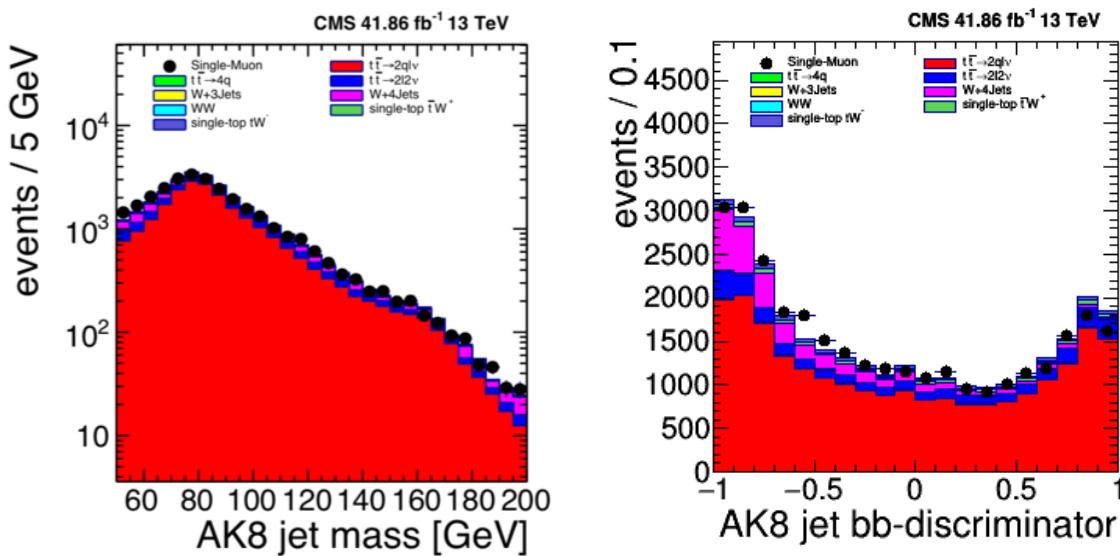


Figure C.2: AK8 jet mass and $b\bar{b}$ -tagging discriminator distributions from data and simulation. The simulation distributions are normalized by area to the data.

Table C.1: W jet $b\bar{b}$ mistag rates in data and simulation, inclusive in p_T . Statistical uncertainties only.

working point	data	MC
disc > 0.3	0.326 ± 0.003	0.340 ± 0.003
disc > 0.6	0.219 ± 0.003	0.236 ± 0.002
disc > 0.8	0.122 ± 0.002	0.138 ± 0.002
disc > 0.9	0.058 ± 0.001	0.067 ± 0.001

Figure C.2 (right) shows the distribution of the $b\bar{b}$ -tagging discriminator for data and simulation. The simulation contributions are divided into signal and background components, where the signal contributions are inclusive $t\bar{t}$ events and the background contributions are from events with direct W boson plus jets, WW, or single-top production. For a given working point (i.e. a fixed point along the x-axis), the mistag rate for the MC simulation is the ratio of the number of signal MC events above that point to the total number of signal MC events. The mistag rate for the data is calculated similarly except that the observed yields are corrected by subtracting the expected number of background events, estimated from the MC simulation:

$$\epsilon_{mc} = \frac{N_{b\bar{b}-tagged}^{sig,mc}}{N^{sig,mc}}, \quad \epsilon_{data} = \frac{N_{b\bar{b}-tagged}^{data} - N_{b\bar{b}-tagged}^{bkg,mc}}{N^{data} - N^{bkg,mc}}, \quad (C.1)$$

Following this prescription, we obtain the mistag rates in data and simulation seen in Table C.1. Four working points are defined ranging from disc>0.3 to disc>0.9. It is seen that the mistag rate in MC is higher for all working points than in data. This trend can be seen in the right-hand plot of Figure C.2 - the MC under-predicts the yields with low discriminator value, and over-predicts those with a large discriminator value.

The scale factors are then formed by taking the ratio of the mistag rate in data to that of simulation:

$$\text{scale factor} = \frac{\epsilon_{data}}{\epsilon_{mc}} \quad (C.2)$$

Table C.2 shows the scale factors, binned in jet p_T , for the four different working points. The uncertainties are the result of summing in quadrature the statistical and two additional systematic

Table C.2: Summary of scale factors for $b\bar{b}$ -tagging W jets in $t\bar{t}$ events.

working point	$250 < p_T < 350 \text{ GeV}$	$350 < p_T < 430 \text{ GeV}$	$p_T > 430 \text{ GeV}$
disc > 0.3	0.939 ± 0.026	1.007 ± 0.055	0.996 ± 0.079
disc > 0.6	0.922 ± 0.027	0.967 ± 0.057	0.902 ± 0.082
disc > 0.8	0.875 ± 0.030	0.939 ± 0.063	0.893 ± 0.090
disc > 0.9	0.855 ± 0.036		0.914 ± 0.068

uncertainties: The first systematic uncertainty originates from subtracting the background from the data using the MC. The uncertainty in the cross section of the background contributions is estimated to be 30%, which results in uncertainties of 2, 4, and 6% for the low, medium, and high p_T bins, respectively. The second systematic uncertainty arises from a known difference in the p_T spectra of top quarks between data and simulation [53]. We assess the systematic uncertainty by comparing results when the top quark p_T spectra is and is not reweighted to match the data. This results in 0, 1, and 2% uncertainties for the low, medium, and high p_T bins, respectively.