Esercizi da Matematica Blu

Esercizio guida da pagina 1657
$$f(x) = \frac{x^2 - z}{x + 1}$$
 in  $c = -z$ 

$$= \frac{2 \times (x + 1) - (x^{2} - 2) \cdot 1}{(x + 1)^{2}} = \frac{2 \times^{2} + 2 \times - x^{2} - 2}{(x + 1)^{2}}$$

$$= \frac{x^{2} + 2 \times - 2}{(x + 1)^{2}} \qquad \int (-2) = \frac{(-2)^{2} + 2(\cdot 2) - 2}{(\cdot 2 + 1)^{2}}$$

$$= \frac{4 + 4 - 2}{1} = 6$$

33) 
$$\int (x) = x^3 + 4x + 1 \quad \text{con } c = 1$$

$$\int (x) = 3x^2 + 4 \quad \int (c) = 3 + 4 = 4$$

$$\int_{0}^{1} f(x) = -\frac{5}{x} \qquad \text{Con } c = 2$$

$$\int_{0}^{1} f(x) = -5 \cdot x^{-1} = -5 \cdot (-1) \cdot x^{-2} = \frac{5}{x^{2}}$$

$$\int_{0}^{1} f(x) = -\frac{5}{2} \cdot x^{-2} = \frac{5}{4}$$

34) 
$$f(x) = 1 + \sqrt{x}$$
 in  $c = 4$   
 $1 + \sqrt{x} = 1 + x^{\frac{1}{2}} = 0$   $f'(x) = \frac{1}{2}x^{-\frac{1}{2}} = \frac{1}{2\sqrt{x}}$ 

$$f(x) = 2x^3 - x$$
 in  $c = 0$   
 $f'(x) = 6x^2 - 1$   $f(c) = -1$ 

35) 
$$\int = x^2 - 1$$
 in  $c = 3$   
 $\int \int = 2x$   $\int 3 = 6$ 

$$\int = \frac{x+3}{x-4} \qquad \text{in } c = -1$$

$$\int = \frac{x-4-x-3}{(x-4)^2} = \frac{-7}{(x-4)^2}$$

$$\int c = \frac{-7}{(-1-4)^2} = \frac{-7}{25} = \frac{7}{25}$$

$$\int f = \frac{x^2-1}{(x-4)^2} \qquad \text{in } c = 1$$

36) 
$$f = \frac{x^2 - 1}{2 - x}$$
 in  $c = 1$ 

$$\int_{-\infty}^{\infty} \frac{2 \times (2-x) - (x^{2}-1) \cdot (-1)}{(2-x)^{2}} = \frac{4x - 2x^{2} - (-x^{2}+1)}{(2-x)^{2}}$$

$$= \frac{4x - 2x^{2} + x^{2} + 1}{(2-x)^{2}} = \frac{-x^{2} + 4x + 1}{(2-x)^{2}} \qquad \int_{-\infty}^{\infty} c = \frac{1 + 4 + 1}{1} = 6$$

$$f = \frac{1}{2} x^2 - 2x$$
 in  $c = -3$ 

$$\int_{-3}^{1} x - 2 \qquad \int_{-3}^{1} -3 = -5$$

34) 
$$f = 2x-1$$
 in  $c = 6$   $f' = 2$ 

$$\int = \frac{3}{x-1}$$
 in  $C = 4$   $\frac{-3}{(x-1)^2}$   $\int 4 = -\frac{3}{93} = \frac{1}{3}$ 

38) 
$$f = \frac{1}{1-x^2} \int_{-1-x^2}^{1} f = \frac{-(-2x)}{(1-x^2)^2} = \frac{2x}{(1-x^2)^2} \int_{-2}^{2} f = \frac{-4}{9}$$

$$\int = \frac{1}{\sqrt{x-1}} \quad \text{in } c = 5$$

$$\int_{-\infty}^{\infty} \frac{1}{(x-1)^{\frac{1}{2}}} = (x-1)^{-\frac{1}{2}}$$

$$= \lambda \int (5) = \frac{1}{2\sqrt{(5-1)^3}} = \frac{1}{16}$$

$$\int = \frac{1}{\sqrt{x-1}} \quad \text{in } C = 5$$

$$\int = \frac{1}{(x-1)^{\frac{1}{2}}} = (x-1)^{-\frac{1}{2}}$$

$$\int = -\frac{1}{2} (x-1)^{-\frac{1}{2}} = -\frac{1}{2} (x-1)^{-\frac{1-2}{2}}$$

$$\int = -\frac{1}{2} (x-1)^{-\frac{3}{2}} = -\frac{1}{2} (x-1)^{\frac{3}{2}}$$

$$\int \int (x-1)^{\frac{1}{2}} = -\frac{1}{2} (x-1)^{\frac{3}{2}} = -\frac{1}{2} (x-1)^{\frac{3}{2}}$$

39) 
$$f = \frac{x-1}{x}$$
  $f' = \frac{x-x-1}{x^2} = -\frac{1}{x^2}$   
in  $c = \lambda = p$   $f(= -\frac{1}{4})$   
 $f = \frac{2-x^2}{1-x^2}$  in  $c = 0$   $f' = -\frac{2x(1-x^2)-(2-x^2)-2x}{(1-x^2)^2}$   
 $= \frac{-2x+2x^2+4x-2x^3}{(1-x^2)^2} = \frac{2x}{(1-x^2)^2}$   $f = 0 = 0$   
40)  $f = -\frac{1}{\sqrt{x}} = -\frac{1}{x^2}$   $f = 0 = 0$   
 $f' = \frac{1}{2} \cdot x^{-\frac{1}{2}-1} = \frac{1}{2} \cdot x^{-\frac{3}{2}} = \frac{1}{2\sqrt{x^3}}$   $f = 0 = 0$   
 $f' = -2x(x^2-2x+2) = (1-x^2)(2x-2)$ 

$$\int_{-2x}^{1} \frac{-2x(x^{2}-2x+2)-(4-x^{2})(2x-2)}{(x^{2}-2x+2)^{2}} \\
= \frac{-2x^{3}+4x^{2}-4x-8x+8+2x^{3}-2x^{2}}{(x^{2}-2x+2)^{2}} \\
= \frac{2x^{2}-12x+8}{(x^{2}-2x+2)^{2}} \qquad \int_{-2x^{2}-2(-2)+2}^{2} \frac{2(-2)^{2}-12(-2)+8}{((-2)^{2}-2(-2)+2)^{2}} \\
= \frac{8+24+8}{(4+4+7)^{2}} = \frac{40}{100} = \frac{20+0}{25} = \frac{2}{5}$$

41) 
$$f(x) = -2 \ln x$$
  $f' = -\frac{2}{x}$   $f(1) = -2$   
 $f = e^{x-1}$  inc = 1  $f' = e^{x-1}$ .  $1 = e^{x-1}$  tuncione composito  
 $f(x) = e^{x-1}$   $f' = \sec^{2}x$   $f'(0) = \frac{1}{2}$   
 $f(x) = 2^{-2x}$   $\frac{1}{2}$   $\frac{1}{2$ 

$$f = \frac{1}{2}x^2 - 4x \qquad f' = x - 4$$

50) 
$$f = \frac{z}{x}$$
 =  $z \cdot x^{-1} \Rightarrow f' = \frac{z}{x^2} \checkmark$ 

51) 
$$f = 4x-9$$
  $f' = 4\sqrt{52}$   $f' = (\frac{1}{2})^2 \cdot x^{-\frac{1}{2}} = \frac{1}{4\sqrt{x}}$ 

52)  $f = \frac{1}{2}\sqrt{x} = \frac{1}{2}x^{\frac{1}{2}}$   $f' = (\frac{1}{2})^2 \cdot x^{-\frac{1}{2}} = \frac{1}{4\sqrt{x}}$ 

53)  $f = 2x^3 - x = 6x^2 - 1$ 

54)  $f = \frac{1}{x^2 - 1}$   $\frac{d}{dx} \frac{1}{f} = -\frac{f'}{f^2}$ 

$$63) f = 2x^3 - x = 6x^2 - 1$$

54) 
$$f = \frac{1}{x^2 - 1}$$
  $\frac{d}{dx} \frac{1}{f} = -\frac{f'}{f^2}$ 

$$= b \quad \int_{-\infty}^{\infty} = -\frac{2x}{(x^2-1)^2} \quad \checkmark$$

55) 
$$f = -x^2 + 4x$$
  $f' = -2x + 4$ 

$$\frac{56}{f} = \frac{x+1}{x} f' = \frac{1(x) - (x+1) \cdot 1}{x^2} = \frac{x - x - 1}{x^2} = -\frac{1}{x^2} \sqrt{x^2}$$

57) 
$$f = \frac{1}{\sqrt{x+2}} = \frac{1}{(x+2)^{\frac{1}{2}}} = (x+2)^{\frac{1}{2}}$$

$$\int_{0}^{1} \int_{0}^{1} dx = -\frac{1}{2} (x+2)^{\frac{1}{2}} \int_{0}^{1} dx = -\frac{1}{2} (x+2)^{\frac{3}{2}} = -\frac{1}{2\sqrt{(x+2)}}$$

58) 
$$f(x) = Sen(-x)$$
 functione composta =  $-\frac{1}{2(x+2)\sqrt{x+2}}$ 

=0 
$$f' = \cos(-x) \cdot -1 = -\cos(-x) \sqrt{ }$$

59) 
$$f = -e^{i+x}$$
  $f' = -e^{i+x}$   $1 = -e^{i+x}$ 

59) 
$$f = -e^{itx}$$
  $f' = -e^{itx}$   $1 = -e^{itx}$   
60)  $f = \sqrt{3x} = (3x)^{\frac{1}{2}}$   $f' = \frac{1}{2}(3x)^{\frac{1}{2}-1}$  3

$$= \frac{(3x)^{\frac{-1}{2}}}{2} = \frac{3}{2\sqrt{3x}} \checkmark$$

$$61) f = 3 \ln x \qquad 3$$

(62) 
$$f = x^2 - 8x$$
  $f = 2x - 8$ 

61) 
$$f = 3 \ln x$$
  $\frac{3}{x} \sqrt{62}$   $f = x^2 - 8x$   $f' = 2x - 8 \sqrt{63}$   $f = 2\sqrt{x} = 2x^{\frac{1}{2}}$   $f' = x^{\frac{1}{2}} = \frac{1}{\sqrt{x}} \sqrt{x}$ 

64) 
$$f = \frac{1}{\sqrt{x} - 1} = \frac{1}{x^{\frac{1}{2}} - 1} = \frac{1}{-1} \cdot \frac{1}{x^{\frac{1}{2}}} = -\frac{1}{x^{\frac{1}{2}}}$$

$$f' = -\frac{1}{2} \cdot \frac{3}{x^{\frac{3}{2}}} = -\frac{1}{2\sqrt{x^{\frac{3}{2}}}}$$

65)  $f = \frac{1}{x^{\frac{1}{2}} - 2}$ 

$$f' = \frac{1}{2\sqrt{x}} \cdot \frac{1}{x^{\frac{1}{2}}} = \frac{1}{2\sqrt{x}}$$

66)  $f = \frac{x}{x - 5}$ 

$$f' = \frac{(x - 5) - x}{(x - 5)^{2}} = -\frac{5}{(x - 5)^{2}}$$

67)  $f = \frac{q - x}{(x - 5)^{2}}$ 

$$f' = -(x^{2} - 1) - (q - x) \cdot 2x$$

67) 
$$f = \frac{9-x}{x^2-1}$$
  $f' = -(x^2-1)-(9-x)\cdot 2x$   
=  $\frac{x^2+1-18x+2x^2}{(x^2-1)^2}$  =  $\frac{x^2-18x+1}{(x^2-1)^2}$