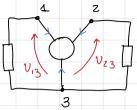


- (1) Solo N-1 Tensionie correnti Sono indipendenti.
- (2) Fissato un nodo, (ES: 3) le grandezte indip saranno V_{13} V_{23} V_{13} V_{23}



RELAZIONI CARATT

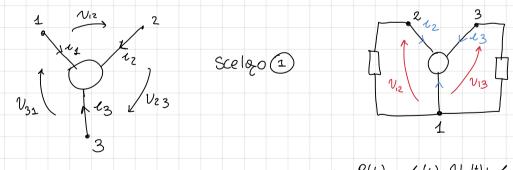
Possiamo esprimere le correnti con funz. di olue variabili:

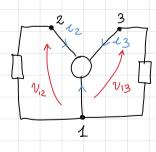
$$\begin{cases} L_{1} = g_{1}(V_{13}, V_{23}) \\ L_{2} = g_{2}(V_{13}, V_{23}) \\ CORRENTE \end{cases}$$

Ma abbiano auche

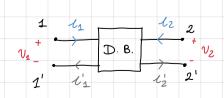
$$\begin{cases} V_4 = \mathcal{E}_1 (l_1, l_2) & \int l_2 = h_2 (l_1, V_2) & \int V_4 = h_1 (V_4, l_2) \\ V_2 = \mathcal{E}_2 (l_1, l_2) & \int V_2 = h_2 (l_1, V_2) & (l_2 = h_2 (V_1, l_2) \end{cases}$$

POTENZA ASSORBITA





=>
$$P(t) = L_2(t) \cdot V_{12}(t) + L_3 V_{13}(t)$$



CONDIZIONI DI PORTA $\begin{cases} \ell_1 = -\ell_1' \\ \ell_2 = -\ell_2' \end{cases}$

GENERATORI CONTROLLATI

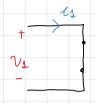
G.T. controllato in Teusione

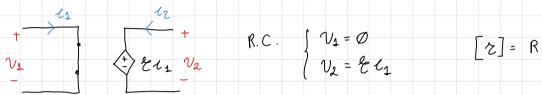


$$R.C. \qquad Sl_1 = 0 \qquad \forall v_2 = l \quad V_1$$

$$\left[\mathcal{A} \right] = \frac{V}{V}$$

controllato in CORRENTE

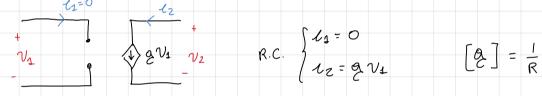




$$R.C. \int V_1 = \emptyset$$

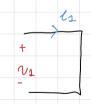
$$V_2 = & C_1$$

controllato in Teusione



$$\left[\begin{array}{c} Q \\ C \end{array} \right] = \frac{1}{R}$$

G.C. Controllato in CORRENTE

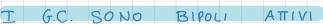


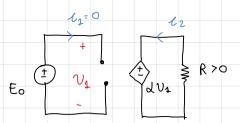
$$R.C \begin{cases} V_4 = 0 \\ V_2 = \beta V_4 \end{cases}$$

$$[\beta] = \frac{A}{A}$$

$$\begin{pmatrix} V_2 \\ \iota_z \end{pmatrix} = \begin{pmatrix} 0 & 0 \\ \beta & 0 \end{pmatrix} \begin{pmatrix} V_4 \\ \iota_z \end{pmatrix}$$

H ibrida





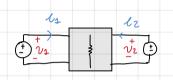
$$\begin{cases} \mathcal{L}_1 = 0 \\ \mathcal{V}_2 = \mathcal{L} \mathcal{V}_1 \end{cases} \longrightarrow \begin{pmatrix} \mathcal{L}_1 \\ \mathcal{V}_2 \end{pmatrix} = \begin{pmatrix} 0 & 0 \\ \mathcal{L} & 0 \end{pmatrix} \begin{pmatrix} \mathcal{V}_1 \\ \mathcal{L}_2 \end{pmatrix}$$

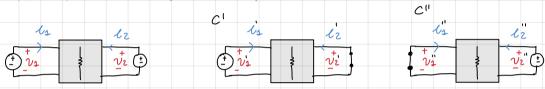
$$\max \begin{cases} V_2 = -L_2 R_2 & \text{no } L_2 = \frac{Vz}{-R} = \frac{Eo}{-R} \end{cases}$$

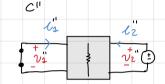
$$=0 P_{\alpha}(t) = V_{1} L_{1} + V_{2} L_{2} = E_{0} \cdot O + d E_{0} \cdot \frac{E_{0}}{-R} = d E_{0}^{2} \underbrace{\text{E}_{0}}_{-R} \underbrace{\text{D.B. ATIVO}}_{-R}$$

PROPRIETA' DI RECIPROCITA'

PRIMA FORMA (TENSIONE)







Sfrutto la cons. delle potenze virtuali
$$\geq \iota'(t) \cdot v'(t) = \mathcal{E} \iota''(t) \cdot v'(t) = 0$$

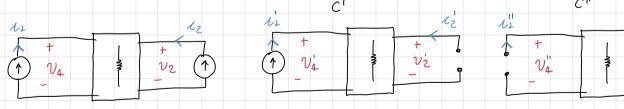
$$C' \int \frac{e}{\sum_{k} (a)} \frac{1}{k} v_{k}'' - \frac{1}{2} v_{1}'' - \frac{1}{2} v_{2}'' = 0 \qquad (1) \qquad # \sum_{k} \frac{1}{k} v_{k}'' = \sum_{k} \frac{1}{k} R_{k} v_{k}'' = \sum_{k} \frac{1}{k}$$

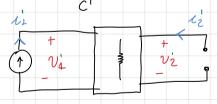
$$C'' \left(\sum_{k=1}^{6} \binom{0}{k} \binom{k}{k} - \binom{k}{1} \binom{k}{1} - \binom{k}{2} \binom{k}{2} - \binom{k}{2} \binom{k}{2} \binom{k}{2} - \binom{k}{2} \binom$$

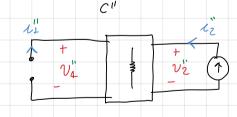
$$(1)$$
 - (2) - (2) - (2) - (2) (2) -

$$= 0 \qquad \frac{L_2}{V} = \frac{L_1}{V}$$

SECONDA FORMA





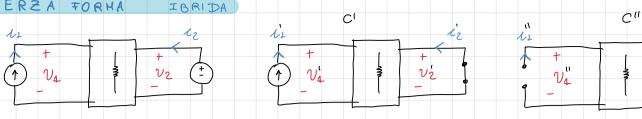


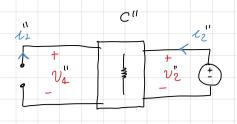
(1)
$$\begin{cases} \frac{e}{\sum v_{K}v_{K}^{"}} - c_{1}v_{1}^{"} - c_{2}v_{2}^{"} \\ \frac{e}{\sum c_{K}v_{K}} - c_{1}v_{2} - c_{2}v_{2}^{"} \end{cases}$$

$$l_1 = l_2 = I$$
 ~ 0

$$\frac{V_1''}{I} = \frac{V_2'}{I}$$







(1)
$$\begin{cases} \leq k_{K} v_{N}^{"} - k_{1} v_{1}^{"} - k_{2} v_{2}^{"} = 0 \end{cases}$$

$$(1) \begin{cases} \underbrace{\leq} \ \mathcal{L}_{K} \ \mathcal{V}_{N}^{"} - \mathcal{L}_{1}^{'} \ \mathcal{V}_{1}^{"} - \mathcal{L}_{2}^{'} \ \mathcal{V}_{2}^{"} = 0 \end{cases} \qquad \sim_{0} \quad - \mathcal{L}_{1}^{'} \ \mathcal{V}_{1}^{"} - \mathcal{L}_{2}^{'} \ \mathcal{V}_{2}^{"} = 0 \qquad con \quad \mathcal{L}_{1}^{'} = \mathbf{I} \quad , \quad \mathcal{V}_{2}^{"} = \mathbf{V}^{"}$$

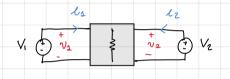
$$(2) \begin{cases} \underbrace{\leq} \ \mathcal{L}_{K}^{"} \ \mathcal{V}_{N}^{"} - \mathcal{L}_{1}^{'} \ \mathcal{V}_{2}^{'} - \mathcal{L}_{2}^{"} \ \mathcal{V}_{2}^{"} = 0 \end{cases} \qquad =_{0} \quad \underbrace{\mathcal{V}_{1}^{"}}_{\mathbf{I}} = \underbrace{\mathcal{L}_{2}^{'}}_{\mathbf{I}} \qquad con \quad \mathcal{L}_{1}^{'} = \mathbf{I} \quad , \quad \mathcal{V}_{2}^{"} = \mathbf{V}^{"}$$

$$\mathcal{L}_{1} V_{4} - \mathcal{L}_{2} V_{2} = 0 \quad \text{con } \mathcal{L}_{1} = I , V_{2} = V$$

$$= 6 \quad \frac{V_{1}''}{T} = 0 \quad \mathcal{L}_{2}$$

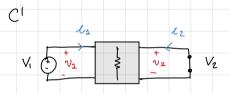
MATRICE DELLE CONDUTTANZE

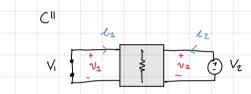
Controlliamo un D.B. in Tensione



se controllions in Tensione -0 le incognite sons le C:

$$\begin{cases} l_1 = l'_1 + l''_1 \\ l_2 = l'_2 + l''_2 \end{cases}$$





$$\begin{bmatrix}
\lambda'_{1} = \frac{V_{2}}{R_{11}} = G_{12}V_{1} & \lambda''_{1} = G_{12} & V_{2} \\
\lambda'_{2} = G_{21}V_{1} & \lambda''_{2} = G_{22} & V_{2}
\end{bmatrix}$$

$$\sim \circ \quad G = \begin{pmatrix} G_{11} & G_{12} \\
G_{21} & G_{22} \end{pmatrix}$$

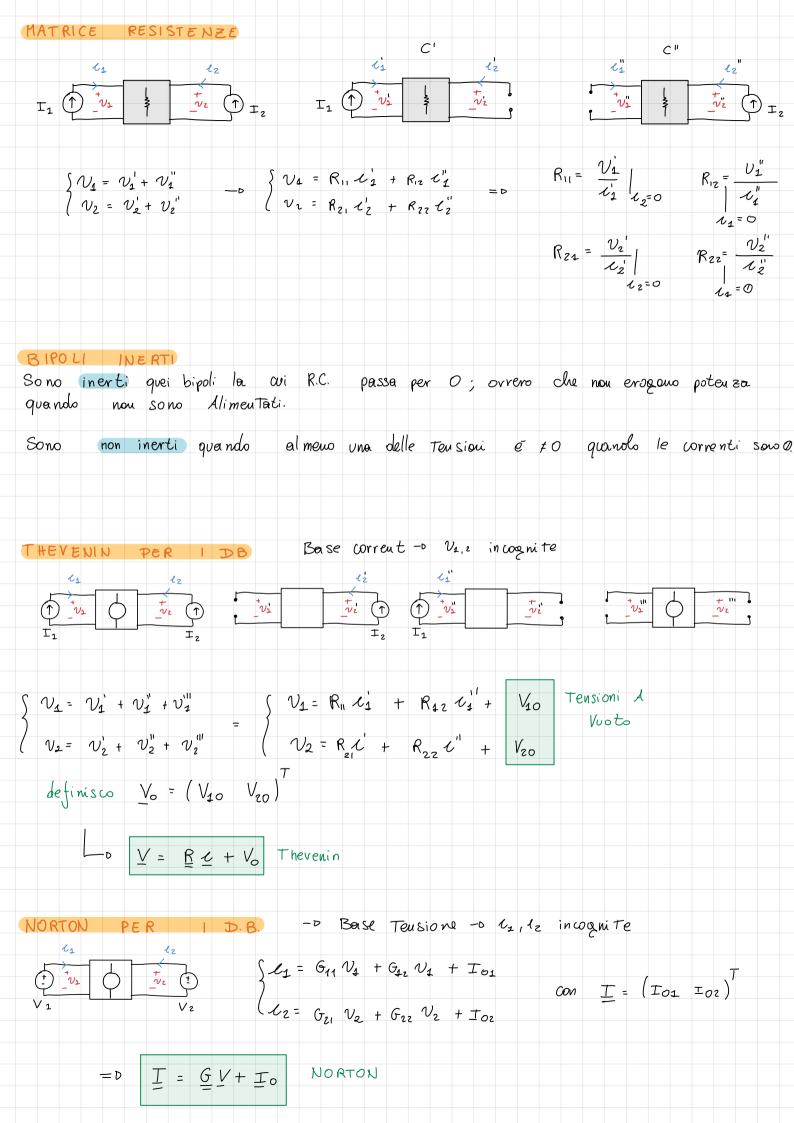
$$\sim 0 \quad \begin{pmatrix} \mathcal{L}_1 \\ \mathcal{L}_2 \end{pmatrix} = \begin{pmatrix} \mathcal{G}_{11} & \mathcal{G}_{12} \\ \mathcal{G}_{21} & \mathcal{G}_{22} \end{pmatrix} \begin{pmatrix} \mathcal{V}_1 \\ \mathcal{V}_2 \end{pmatrix} \qquad \mathcal{L}_{K} = \frac{\mathcal{V}_{K}}{R_{ij}} - 0 \quad \mathcal{G}_{ij} = \frac{\mathcal{L}_{K}}{\mathcal{V}_{K}}$$

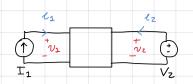
$$G = \begin{pmatrix} G_{11} = \frac{U_{1}}{v_{1}} |_{v_{2}=0} & G_{12} = \frac{U_{1}}{v_{2}} |_{v_{1}=0} \\ G_{21} = \frac{U_{2}}{v_{1}} |_{v_{2}=0} & G_{22} = \frac{U_{2}}{v_{2}} |_{v_{1}=0} \end{pmatrix}$$

POTENZA

$$\underline{\mathcal{L}} = (\mathcal{L}_1 \quad \mathcal{L}_2)^{\mathsf{T}} \qquad \underline{\mathcal{V}} = (\mathcal{V}_1 \quad \mathcal{V}_2)^{\mathsf{T}} \qquad -o \quad \underline{\mathcal{L}} = \underline{\mathcal{G}} \cdot \underline{\mathcal{V}}$$

$$P(t) = \underline{V}^{\mathsf{T}} \cdot \underline{c} = 0$$
 $P(t) = \underline{V}^{\mathsf{T}} \cdot \underline{G} \cdot \underline{V}$





$$\begin{cases} V_{1} = H_{1} (N_{1}, V_{2}) = H_{11} C_{1} + H_{12} V_{2} \\ V_{2} \end{cases}$$

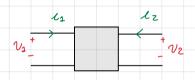
$$\begin{cases} V_{2} = H_{1} (N_{1}, V_{2}) = H_{21} C_{1} + H_{22} V_{2} \\ C_{2} = H_{2} (N_{1}, V_{2}) = H_{21} C_{1} + H_{22} V_{2} \end{cases}$$

$$H_{11} = \frac{V_1}{c_1} \Big|_{V_2 = 0}$$
 $H_{12} = \frac{V_1}{V_2} \Big|_{V_2 = 0}$

$$H_{12} = \frac{v_1}{v_2} \Big|_{v_2 = 0}$$

$$H_{24} = \frac{L_2}{L_1}\Big|_{L_2=0} \qquad H_{22} = \frac{L_2}{V_2}\Big|_{L_1=0}$$

$$H_{22} = \frac{\kappa_2}{\nu_2} \Big|_{\ell_1 = 0}$$



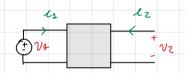
Ricariamo le grandezze della prima porta in funzione della se conolu-

$$\begin{cases} V_{4} = T_{11} V_{2} + T_{12} (-L_{2}) \\ L_{3} = T_{21} V_{2} + T_{22} (-L_{2}) \end{cases}$$

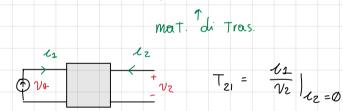
de finiti
$$V_0 = (V_1 \ \mathcal{L}_1)^T e \quad V_2 = (V_2 \ \mathcal{L}_2)^T \quad \sim o \quad V_0 = \begin{pmatrix} T_{11} & T_{12} \\ T_{21} & T_{22} \end{pmatrix} \cdot V_2$$

$$V_1 = (V_2 - L_2)^T$$

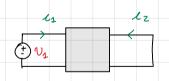
$$V_0 = \begin{pmatrix} T_{11} & T_{12} \\ T_{21} & T_{22} \end{pmatrix} \cdot V_2$$



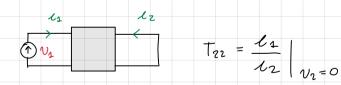
$$T_{11} = \frac{V_1}{V_2} \mid U_2 = 0$$



$$T_{21} = \frac{\ell_1}{v_2}\Big|_{\ell_2 = 0}$$



$$T_{12} = \frac{V_1}{-V_2} \Big|_{V_2=0}$$



$$T_{22} = \frac{l_4}{l_2} \Big|_{V_2 = 0}$$

ACCOPPIAMENTO MUTUO

$$\begin{cases}
\phi_1 = L_1 L_1 + M_{12} L_2 \\
\phi_2 = L_2 L_2 + M_{12} L_4
\end{cases}$$

ma
$$V = \frac{d\phi}{dt} = 0$$

ma
$$v = \frac{d\phi}{dt} = v$$
 $\begin{cases} v_1 = L_1 \dot{l}_1 + M \dot{l}_2 \\ v_2 = L_2 \dot{l}_2 + M \dot{l}_1 \end{cases}$

POTENZA DEL TRASFORM.

$$P^{\alpha}(t) = v_{1}(t) \cdot l_{2}(t) + v_{2}(t) l_{2}(t) = l_{1} l_{1} \frac{dl_{1}}{dt} + M l_{1} \frac{dl_{2}}{dt} + l_{2} l_{2} \frac{dl_{2}}{dt} + M l_{2} \frac{dl_{1}}{dt}$$

Siccome
$$\frac{d}{dt} \left[\frac{d\ell^2}{dt} \right] = 2\ell \frac{d\ell}{dt} - 0$$
 $P^a = \frac{d}{dt} \left[\frac{1}{2} L_1 L_1^2 \right] + M \left(L_1 \dot{l}_2 + L_2 \dot{l}_1 \right) + \frac{d}{dt} \left[\frac{1}{2} L_2 L_2^2 \right]$

$$-o \quad P^{\alpha} = \frac{d}{dt} \left(\frac{1}{2} L_1 L_1^2 \right) + M \frac{d}{dt} \left(L_1 L_2 \right) + \frac{d}{dt} \left[\frac{1}{2} L_2 L_2^2 \right]$$

Siccome
$$P = \frac{dW}{dt} R LAVORO$$
 $W = \int P dt$

$$= D \quad W = \frac{1}{2} L_1 L_1^2 + \left(H L_1 L_2 + \frac{1}{2} L_2 L_2^2 \right)$$
Energia

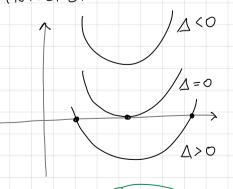
im magazz.

IL TRAS. E' UN BIPOLO PASSIVO -D Wa >0

$$\frac{1}{2} L_{1} L_{1}^{2} + M L_{1} L_{2} + \frac{1}{2} L_{2} L_{2}^{2} \ge 0 \quad -0 \quad \mathcal{L}_{2}^{2} \left[\frac{1}{2} L_{1} \left(\frac{L_{1}}{L_{1}} \right)^{2} + \frac{1}{2} L_{2} + M_{1} \frac{L_{1}}{L_{2}} \right] \ge 0$$

$$-0$$
 pongo $\frac{L_1}{L_2} = \chi -0$ $\frac{1}{2} L_1 \chi^2 + M \chi + \frac{1}{2} L_2 > 0$

ANALISI



$$\Delta = b^{2} - 4 \cdot 9 \cdot C = M^{2} - 4 \cdot \frac{1}{2} \cdot \frac{1}{2} \cdot L_{1} \cdot L_{2}$$

$$= M^{2} - L_{1} L_{2}$$

d prod

= D
$$K = \frac{\Delta}{\sqrt{L_1 L_2}}$$
 Coeff di Accoppiamento

TRASFORM IN ACCOPPIAMENTO PERFETTO

$$\int V_1 = L_1 i_1 + M i_2 = L_1 \left(i_1 + \frac{M}{L_1} i_2 \right)$$

 $\int V_2 = L_2 i_2 + M i_1 = M \left(i_1 + \frac{L_2}{M} i_2 \right)$

$$K = \frac{M^2}{L_1 L_2} = 1 = 0 \quad M^2 = L_1 L_2 \quad -0 \quad \frac{M}{L_1} = \frac{L_2}{M} = m$$

$$K = \frac{1}{L_1 L_2} = 1 \quad d = D \quad M = L_1 L_2 \quad -0 \quad \frac{PI}{L_1} = \frac{L_2}{M} = (m)$$

$$\begin{cases} V_{1} = L_{1}(i_{1} + ni_{2}) & (1) \\ V_{2} = H(L_{1} + ni_{2}) & (2) \end{cases} = 0 \qquad V_{1} = 0 \qquad V_{2} = 0 \qquad V_{1} = 0 \qquad V_{2} = 0 \qquad V_{2} = 0 \qquad V_{1} = 0 \qquad V_{2} = 0 \qquad V_{2} = 0 \qquad V_{3} = 0 \qquad V_{4} = 0 \qquad V_{5} =$$

$$\frac{V_1}{V_2} = \begin{pmatrix} 1 \\ M \end{pmatrix} \cdot \frac{l_1 + m l_2}{l_1 + m l_2}$$

$$Con n = \frac{L_1}{M}$$

$$- 0 \quad V_1 = n \quad V_2$$

$$L_1 = -\frac{1}{n} \quad L_2$$

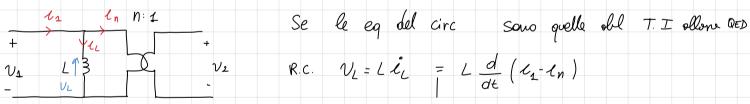
$$\frac{V_1}{V_2} = \frac{n_1}{n_2} - 0 \quad n_1 V_1 = n_2 V_2 \quad \text{se} \quad n_1 = 1 - 0 V_1 = n V_2$$

$$\left[\frac{\chi_1}{\chi_2} = -\frac{n_2}{n_1}\right] = 0 \qquad \chi_1 = -\frac{1}{n} \ell_2$$

CARATERISTICHE T. T.

$$\begin{cases} V_4 = n V_2 \\ V_2 = -n I_1 \end{cases} \quad \begin{cases} V_2 = \frac{1}{n} V_1 \\ V_4 = -\frac{1}{n} I_2 \end{cases}$$

CIRCUITO EQUIVALENTE



$$U_L = L - \ell_n$$

ma
$$l_n = -\frac{1}{n} l_2$$
 $\sim v_L = L \frac{d}{dt} \left(l_1 + \frac{1}{n} l_2 \right) = \left(\frac{L}{n} \right) i_2 + L i_1$

$$\frac{L_1}{M} = n - 0 \quad \frac{L_1}{n} = M \quad \infty \quad \sqrt{L} = H \dot{\ell}_2 + L \dot{\ell}_1 \qquad \epsilon_0 \quad Trasf (1)$$

$$V_1 = n V_2 - 0 \quad n V_2 = V_L \sim 0 \quad n V_2 = L \cdot l_L \sim 0 \quad V_2 = \frac{L}{n} \cdot l_1 + L \cdot l_2$$