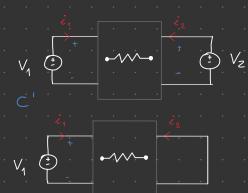
MATRICI DELLE CONDUTTANZE E RESISTENZE

MATRICE DELLE CONDUTANZE





$$\begin{cases} \dot{c}_1 = \dot{c}_1 + \dot{c}_1 \\ \dot{c}_2 = \dot{c}_2 + \dot{c}_2'' \end{cases}$$

$$i_1 = G_{11} \cdot V_1$$
 $i_1'' = G_{12} \cdot V_2$
 $i_2' = G_{21} \cdot V_1$ $i_2'' = G_{22} \cdot V_2$

$$\begin{cases} \lambda_1 = G_{11} \cdot V_1 + G_{12} \cdot V_2 \\ \lambda_2 = G_{21} \cdot V_1 + G_{22} \cdot V_2 \end{cases}$$

Siccome
$$V=Ri-0$$
 $\frac{1}{R}=\frac{\cancel{c}}{V}=0$ $G=\frac{\cancel{c}}{V}$

$$G_{11} = \frac{\dot{\mathcal{L}}_1}{V_1} \bigg|_{V_2 = \emptyset}$$

$$G_{12} = \frac{|\mathcal{L}_1|}{|V_2|}|_{V_1 = 0}$$

$$G_{21} = \frac{\overline{c_2}}{V_1} \bigg|_{V_2 = 0}$$

$$G_{22} = \frac{c^{11}}{V_2} \Big|_{V_1 = 0}$$





Definisco

$$\underline{\mathring{\mathcal{L}}} = (i_1, i_2)^{\mathsf{T}} \qquad \underline{V} = (v_1, v_2)^{\mathsf{T}}$$

$$Con \quad \underline{G} = \begin{pmatrix} G_{11} & G_{12} \\ G_{21} & G_{22} \end{pmatrix}$$

Simmetrica

G12 = G21 QED

Potenza Assorbita

Proprieta della Matrice delle conduttoure

•
$$G_{12} = G_{21}$$

$$\begin{pmatrix} \frac{\mathcal{L}_1}{V_2} \\ V_2 \end{pmatrix} = \begin{pmatrix} \frac{\mathcal{L}_2}{V_1} \\ V_1 \end{pmatrix} = D$$

•
$$|G_{21}| < G_{11}$$
 , $|G_{12}| \leq G_{22}$

$$-0 \qquad \left| \frac{iz}{V_1} \right| \leqslant \left| \frac{x_1}{V_1} \right|$$

MATRICE DELLE RESISTENZE

$$\begin{cases} V_1 = R_{11} \dot{i}_1 + R_{12} \dot{i}_2 \\ V_2 = R_{21} \dot{i}_1 + R_{22} \dot{i}_2 \end{cases}$$

$$Con \quad R = \begin{array}{c} R_{11} & R_{12} \\ R_{21} & R_{22} \end{array}$$

Resistenze proprie

MATRICI IBRIDE E DI TRASMISSION

MATRICE IBRIDA

DOPPI BIPOLI Resistivi: "AT

NoTa: Se ho due bipoli che hanno la stessa correute e Teusione sono sia in serie che in parallelo: sono in CASCATA

TRIPOLO

$$V_1 \quad V_2 \quad \begin{cases} R_C \quad V_2 \\ V_1 \quad V_2 \end{cases}$$

$$V_{1} = V_{2}$$

$$V_{1} = R_{11} \cdot \hat{\mathcal{L}}_{1} + R_{12} \hat{\mathcal{L}}_{2}$$

$$V_{2} = R_{21} \cdot \hat{\mathcal{L}}_{1} + R_{22} \cdot \hat{\mathcal{L}}_{2}$$

Deno Trovare

$$\mathcal{E}_{11} = \frac{\mathcal{V}_{1}}{i_{1}} = \frac{\dot{v}_{1}(R_{A}+R_{C})}{\dot{v}_{1}} = R_{A}+R_{C}$$

$$\mathcal{E}_{21} = \frac{\dot{v}_{2}}{i_{1}} = \frac{\dot{v}_{C}}{i_{1}} = \frac{i_{1}R_{C}}{i_{1}} = R_{C}$$

$$\mathcal{E}_{22} = \frac{V_2}{i_2''} = \frac{i_2'' (R_3 + R_c)}{i_2''}$$

$$= R_B + R_c$$

$$= \begin{bmatrix} (R_A + R_C) & R_C \\ R_C & (R_B + R_C) \end{bmatrix}$$

$$Z_{12} = \frac{V_1}{i_z''} = \frac{V_c''}{i_z''} = \frac{i_z'' Rc}{i_z''} = Rc$$
Verifica

Doppio Bipolo "ATC" Visto nella lez 23/22

Matrice conduttanze - Daratterizzazione su base Tensione

$$G_{11} = \frac{\dot{c}_{1}}{V_{1}}\Big|_{V_{2}=0} = \frac{\dot{c}_{1}}{V_{1}} = \frac{V_{1}(G_{1}+G_{1})}{V_{1}} = \frac{G_{1}}{V_{1}}$$

$$G_{12} = \frac{\dot{c}_{2}}{V_{1}}\Big|_{V_{2}=0} = \frac{-\dot{c}_{1}}{V_{1}} = \frac{-\dot{c}_{2}}{V_{1}} = -\dot{c}_{2}$$

$$G_{21} = \frac{i_1''}{V_2} = \frac{i_C'}{V_2''} = G_C$$

$$G_{21} = \frac{i_1'''}{V_2} = \frac{i_C''}{V_2''} = G_C$$

$$G_{21} = \frac{i_1'''}{V_2} = \frac{i_C''}{V_2''} = G_C$$

$$G_{21} = \frac{i_1'''}{V_2} = \frac{i_C''}{V_2''} = G_C$$

$$G_{22} = \frac{i_2'''}{V_2} = \frac{i_B - i_C}{V_2}$$

$$G_{21} = \frac{i_1'''}{V_2} = \frac{i_C''}{V_2''} = G_C$$

$$G_{21} = \frac{i_1'''}{V_2} = \frac{i_C''}{V_2''} = G_C$$

$$= D \qquad \stackrel{G}{\subseteq} \left[\begin{pmatrix} G_A + G_C \end{pmatrix} \quad \begin{pmatrix} -G_C \end{pmatrix} \\ \begin{pmatrix} -G_C \end{pmatrix} \quad \begin{pmatrix} G_B + G_C \end{pmatrix} \right]$$

Sintesi - PROGETIAZIONE

Abbienno
$$R = \begin{pmatrix} 20 & 6 \\ 6 & 18 \end{pmatrix}$$

$$\begin{cases} R_A + R_C = 20 & -D & R_A = 20 - 6 = 14 \\ R_C = 6 & R_C \\ R_B + R_C = 18 - D & R_B = 18 - 6 = 12 R_B \end{cases}$$

