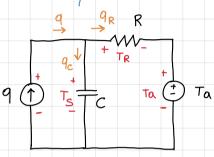


Questo è un semplice sistema dinamico di tipo termico: si compone di una stanza con delle pareti isolanti (coefficiente di isolamento dato dalla resistenza **R**) al cui interno è posto un radiatore avente un flusso q.

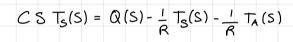
Possiamo modellare il sistema con un circuito equivalente, stando attenti a mettere la resistenza (delle pareti) schematicamente tra la temperatura esterna ed i componenti interni alla stanza.

Circuito equivalente



$$T_R = T_S - T_a = 0$$
 $C\frac{dT_S}{dt} = q - \frac{T_S - T_a}{R}$

Funzione di Trasferimento

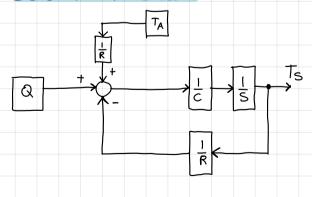


Unzione di Trasferimento

$$CST_{S}(S) = Q(S) - \frac{1}{R}T_{S}(S) - \frac{1}{R}T_{A}(S)$$
 $CST_{S}(S) = Q(S) - \frac{1}{R}T_{A}(S)$
 $CST_{S}(S) = Q(S) - \frac{1}{R}T_{A}(S)$

Voalio OUT:
$$T_S(S)$$
 IN: $Q(S)$ = D $T_S(S)$ = $Q(S)$ = $Q(S)$

Schemer a Blocchi



SPAZIO DI STATO
$$x_1 = T_S$$
 $v_{\frac{\pi}{2}}q$ $v_2 = T_A$

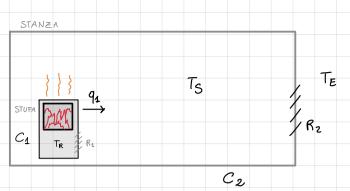
$$y = T_S$$

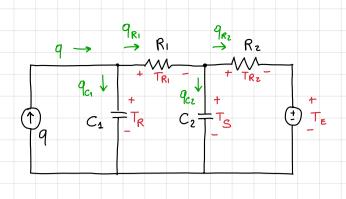
$$\begin{cases} \dot{x} = \frac{1}{C} \left[v_1 - \frac{1}{R} \left(x_1 - v_2 \right) \right] \\ y = x_1 \end{cases}$$

$$\begin{cases} \dot{x} = -\frac{1}{RC} \cdot x_1 + \left(\frac{1}{C} - \frac{1}{RC}\right) \cdot \left(\frac{U_1}{U_2}\right) \\ y = 1 \cdot x_1 \end{cases}$$



CIRCUITO EQUIVALENTE





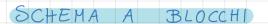
$$\begin{cases} C_{1} \frac{dT_{R}}{dt} = q_{C1} \\ C_{2} \frac{dT_{S}}{dt} = q_{C2} \\ C_{3} \frac{dT_{S}}{dt} = q_{C2} \end{cases} \qquad L_{KC}: q_{C_{1}} = q_{1} - q_{R_{1}} = 0 \qquad C_{4} \frac{dT_{R}}{dt} = q_{1} - q_{R_{1}} = q_{1} - T_{R_{1}} \\ C_{2} \frac{dT_{S}}{dt} = q_{C2} \qquad L_{KC}: q_{C_{2}} = q_{R_{1}} - q_{R_{2}} = 0 \qquad C_{2} \frac{dT_{S}}{dt} = q_{R_{1}} - q_{R_{2}} = T_{R_{1}} - T_{R_{2}} \\ T_{R_{1}} = q_{R_{1}} \cdot R_{1} = 0 \qquad q_{R_{1}} = T_{R_{1}} \\ T_{R_{2}} = q_{R_{2}} \cdot R_{2} = 0 \qquad q_{R_{2}} = T_{R_{2}} \\ T_{R_{2}} = q_{R_{2}} \cdot R_{2} = 0 \qquad q_{R_{2}} = T_{R_{2}} \\ T_{R_{2}} = q_{R_{2}} \cdot R_{2} = 0 \qquad q_{R_{2}} = T_{R_{2}} \\ T_{R_{2}} = q_{R_{2}} \cdot R_{2} = 0 \qquad q_{R_{2}} = T_{R_{2}} \\ T_{R_{2}} = q_{R_{2}} \cdot R_{2} = 0 \qquad q_{R_{2}} = T_{R_{2}} \\ T_{R_{2}} = q_{R_{2}} \cdot R_{2} = 0 \qquad q_{R_{2}} = T_{R_{2}} \\ T_{R_{2}} = q_{R_{2}} \cdot R_{2} = 0 \qquad q_{R_{2}} = T_{R_{2}} \\ T_{R_{2}} = q_{R_{2}} \cdot R_{2} = 0 \qquad q_{R_{2}} = T_{R_{2}} \\ T_{R_{2}} = q_{R_{2}} \cdot R_{2} = 0 \qquad q_{R_{2}} = T_{R_{2}} \\ T_{R_{2}} = q_{R_{2}} \cdot R_{2} = 0 \qquad q_{R_{2}} = T_{R_{2}} \\ T_{R_{2}} = q_{R_{2}} \cdot R_{2} = 0 \qquad q_{R_{2}} = T_{R_{2}} \\ T_{R_{2}} = q_{R_{2}} \cdot R_{2} = 0 \qquad q_{R_{2}} = T_{R_{2}} \\ T_{R_{2}} = q_{R_{2}} \cdot R_{2} = 0 \qquad q_{R_{2}} = T_{R_{2}} \\ T_{R_{2}} = q_{R_{2}} \cdot R_{2} = 0 \qquad q_{R_{2}} = T_{R_{2}} \\ T_{R_{2}} = q_{R_{2}} \cdot R_{2} = 0 \qquad q_{R_{2}} = T_{R_{2}} \\ T_{R_{2}} = q_{R_{2}} \cdot R_{2} = 0 \qquad q_{R_{2}} = T_{R_{2}} \\ T_{R_{2}} = q_{R_{2}} \cdot R_{2} = 0 \qquad q_{R_{2}} = T_{R_{2}} \\ T_{R_{2}} = q_{R_{2}} \cdot R_{2} = 0 \qquad q_{R_{2}} = T_{R_{2}} \\ T_{R_{2}} = q_{R_{2}} \cdot R_{2} = 0 \qquad q_{R_{2}} = T_{R_{2}} \\ T_{R_{2}} = q_{R_{2}} \cdot R_{2} = 0 \qquad q_{R_{2}} = T_{R_{2}} \\ T_{R_{2}} = q_{R_{2}} \cdot R_{2} = 0 \qquad q_{R_{2}} = T_{R_{2}} \\ T_{R_{2}} = q_{R_{2}} \cdot R_{2} = 0 \qquad q_{R_{2}} = T_{R_{2}} \\ T_{R_{2}} = q_{R_{2}} \cdot R_{2} = 0 \qquad q_{R_{2}} = T_{R_{2}} \\ T_{R_{2}} = q_{R_{2}} \cdot R_{2} = 0 \qquad q_{R_{2}} = T_{R_{2}} \\ T_{R_{2}} = q_{R_{2}} \cdot R_{2} = 0 \qquad q_{R_{2}} = T_{R_{2}} \\ T_{R_{2}} = q_{R_{2}} \cdot R_{2} = 0 \qquad q_{R_{2}} = T_{R_{2}} \\ T_{R_{2}} = q_{R_{2}} \cdot R_{2} = 0 \qquad q_{R_{2}} = T_{R_{2}} \\ T_{R_{2}} =$$

$$\begin{cases} C_4 \frac{dT_R}{dt} = Q - \frac{1}{R_1} \left(T_R - T_S \right) = Q - \frac{1}{R_1} T_R + \frac{1}{R_1} T_S \\ C_2 \frac{dT_S}{dt} = \frac{1}{R_1} \left(T_R - T_S \right) - \frac{1}{R_2} \left(T_S - T_E \right) = \frac{1}{R_1} T_R + \left(-\frac{1}{R_1} - \frac{1}{R_2} \right) T_S + \frac{1}{R_2} T_E \end{cases}$$

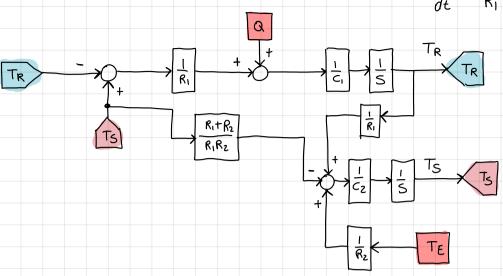
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$$\begin{pmatrix} \chi_1 \\ \chi_2 \end{pmatrix} = \begin{pmatrix} -\frac{1}{C_1 R_1} & \frac{1}{C_1 R_1} \\ \frac{1}{C_2 R_1} & -\frac{R_1 + R_2}{C_2 R_1 R_2} \end{pmatrix} \begin{pmatrix} \chi_1 \\ \chi_2 \end{pmatrix} + \begin{pmatrix} \frac{1}{C_1} & O \\ O & \frac{1}{C_2 K_2} \end{pmatrix} \begin{pmatrix} U_1 \\ U_2 \end{pmatrix}$$

$$y = (0 \quad 1) \begin{pmatrix} x_1 \\ x_2 \end{pmatrix} + \mathcal{O} \cdot \begin{pmatrix} U_1 \\ U_2 \end{pmatrix}$$



$$\begin{cases} C_4 \frac{dT_R}{dt} = q - \frac{1}{R_1} T_R + \frac{1}{R_1} T_S \\ C_2 \frac{dT_S}{dt} = \frac{1}{R_1} T_R + \left(-\frac{1}{R_1} - \frac{1}{R_2}\right) T_S + \frac{1}{R_2} T_E \end{cases}$$



Conducibilità termica	
sostanza	k(W/m°K)
argento	430
rame	390
alluminio	240
ferro	80
vetro	0,93
acqua	0,68
legno	0,2
aria secca	0,02
cemento	1,5
mattoni	0,35
muratura	0,7

FUNZIONE DI TRASFERIMENTO

$$\begin{cases} C_4 \frac{dT_R}{dt} = 9 - \frac{1}{R_1} T_R + \frac{1}{R_1} T_S \\ C_2 \frac{dT_S}{dt} = \frac{1}{R_1} T_R + \left(-\frac{1}{R_1} - \frac{1}{R_2}\right) T_S + \frac{1}{R_2} T_E \end{cases}$$

$$\begin{cases} SC_1 T_R = Q - \frac{1}{R_1} T_R + \frac{1}{R_1} T_S \\ SC_2 T_S = \frac{1}{R_1} T_R - \left(\frac{R_2 + R_1}{R_1 R_2}\right) T_S + \frac{1}{R_2} T_E \end{cases}$$

$$T_{S}\left(\frac{SC_{2}R_{1}R_{2}+R_{1}+R_{2}}{R_{1}R_{2}}\right) = \frac{RADIATORE}{R_{1}T_{R}} + \frac{1}{R_{2}}T_{E}$$

$$dalla (1): T_{R}\left(\frac{SC_{1}R_{1}+1}{R_{1}}\right) = Q + \frac{1}{R_{1}}TS = D T_{R} = \frac{R_{1}}{SC_{1}R_{1}+1}Q + \frac{STANZA}{SC_{1}R_{1}+1}TS$$

$$= D TS \left(\frac{SC_2R_1R_2 + R_1 + R_2}{R_1R_2} \right) = \frac{1}{R_2} TE + \frac{1}{SC_1R_1 + 1} Q + \frac{1}{SC_1R_1^2 + R_1} TS$$

$$T_{S}\left(\frac{SC_{2}R_{1}R_{2}+R_{1}+R_{2}}{R_{1}R_{2}}-\frac{1}{SC_{1}R_{1}^{2}+R_{1}}\right)=\frac{1}{SC_{1}R_{1}+1}Q+\frac{1}{R_{2}}T_{E}$$

$$-0 T_{S} \left(\frac{C_{1}C_{2}R_{1}R_{2}S + C_{1}R_{1}S + C_{1}R_{2}S + C_{2}R_{2} + 1}{C_{1}R_{1}R_{2}S + R_{2}} \right) = \frac{1}{SC_{1}R_{1} + 1} Q + \frac{1}{R_{2}}T_{E}$$