

CIRCUITO RC

R

Vin

$$V_{in}$$
 $V_{c}$ 
 $V_{c}$ 

$$\begin{cases} V_R = R \cdot L \\ L_c = C \dot{V}_C - 0 \quad \dot{V}_C = \frac{1}{C} L_C - 0 \quad V_C = \frac{1}{C} \int_{C} L_C dt \end{cases}$$

$$-0 V_{R} + V_{C} = V_{IN} - 0 RI(S) + \frac{1}{C} \cdot SI(S) - 160^{4} = V_{In}(S) - 0 V_{In}(S) = RI(S) + \frac{1}{CS}I(S) = I(S) + \frac{1}{CS}I(S) + \frac{$$

Siccome 
$$V_0(s) = \frac{1}{CS} I(s) = 0$$
  $G(s) = \frac{V_0(s)}{V_{in}(s)} = \frac{1}{CS} I(s)$ 

$$= \frac{1}{CS} I(s) = \frac{1}{CS$$

### SPAZIO DI STATO

# (1) Stabiliamo

in = 
$$U = V_{in}$$
  
 $OUt = y = V_{o}$   
Variabile di stato =  $X = V_{c} = V_{o}$ 

(2) Scrivo nella forma 
$$\begin{cases} \dot{x} = Ax + B \\ y = Cx + Dy \end{cases}$$

Dalle R.C.

$$\begin{bmatrix} c \frac{d}{dt} V_0 = \mathcal{U} & -o \hat{V}_0 = \frac{1}{C} \mathcal{U} = 0 & \hat{V}_0 = \frac{1}{RC} \left( V_{in} - V_0 \right) - o & \hat{V}_0 = -\frac{1}{RC} \left( V_{in} - V_0 \right) \\ \hat{\mathcal{X}} & V_0 = \mathcal{U} - o \hat{V}_0 = \frac{1}{C} \mathcal{U} = 0 & \hat{V}_0 = \frac{1}{RC} \left( V_{in} - V_0 \right) - o & \hat{V}_0 = -\frac{1}{RC} \left( V_{in} - V_0 \right) \\ \hat{\mathcal{X}} & V_0 = \mathcal{U} - o \hat{V}_0 = \frac{1}{C} \mathcal{U} = 0 & \hat{V}_0 = 0 & \mathcal{U} = \frac{1}{RC} \left( V_{in} - V_0 \right) - o & \hat{V}_0 = -\frac{1}{RC} \left( V_{in} - V_0 \right) \\ \hat{\mathcal{X}} & V_0 = \mathcal{U} - o \hat{V}_0 = \frac{1}{RC} \mathcal{U} = 0 & \hat{V}_0 = 0 & \mathcal{U} = \frac{1}{RC} \left( V_{in} - V_0 \right) - o & \hat{V}_0 = -\frac{1}{RC} \left( V_{in} - V_0 \right) \\ \hat{\mathcal{X}} & V_0 = \mathcal{U} - o \hat{V}_0 = \frac{1}{RC} \mathcal{U} = 0 & \hat{V}_0 = 0 & \mathcal{U} = \frac{1}{RC} \left( V_{in} - V_0 \right) \\ \hat{\mathcal{X}} & V_0 = \mathcal{U} - o \hat{V}_0 = \frac{1}{RC} \mathcal{U} = 0 & \hat{V}_0 = 0 & \mathcal{U} = \frac{1}{RC} \left( V_{in} - V_0 \right) \\ \hat{\mathcal{X}} & V_0 = 0 & \hat{V}_0 = 0 & \hat{V}_0 = 0 & \hat{V}_0 = 0 & \hat{V}_0 = 0 \\ \hat{V}_0 = 0 & \hat{V}_0 = 0 & \hat{V}_0 = 0 & \hat{V}_0 = 0 \\ \hat{V}_0 = 0 & \hat{V}_0 = 0 & \hat{V}_0 = 0 & \hat{V}_0 = 0 \\ \hat{V}_0 = 0 & \hat{V}_0 = 0 & \hat{V}_0 = 0 & \hat{V}_0 = 0 \\ \hat{V}_0 = 0 & \hat{V}_0 = 0 & \hat{V}_0 = 0 \\ \hat{V}_0 = 0 & \hat{V}_0 = 0 & \hat{V}_0 = 0 \\ \hat{V}_0 = 0 & \hat{V}_0 = 0 & \hat{V}_0 = 0 \\ \hat{V}_0 = 0 & \hat{V}_0 = 0 & \hat{V}_0 = 0 \\ \hat{V}_0 = 0 & \hat{V}_0 = 0 & \hat{V}_0 = 0 \\ \hat{V}_0 = 0$$

$$y = Siccome V_0 = x$$
,  $y = V_0 = 0$   $y = x$ 

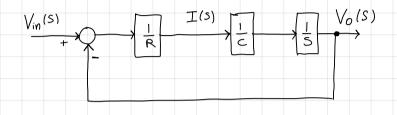
$$= 0 \int \dot{x} = -\frac{1}{Rc}x + \frac{1}{Rc}u$$

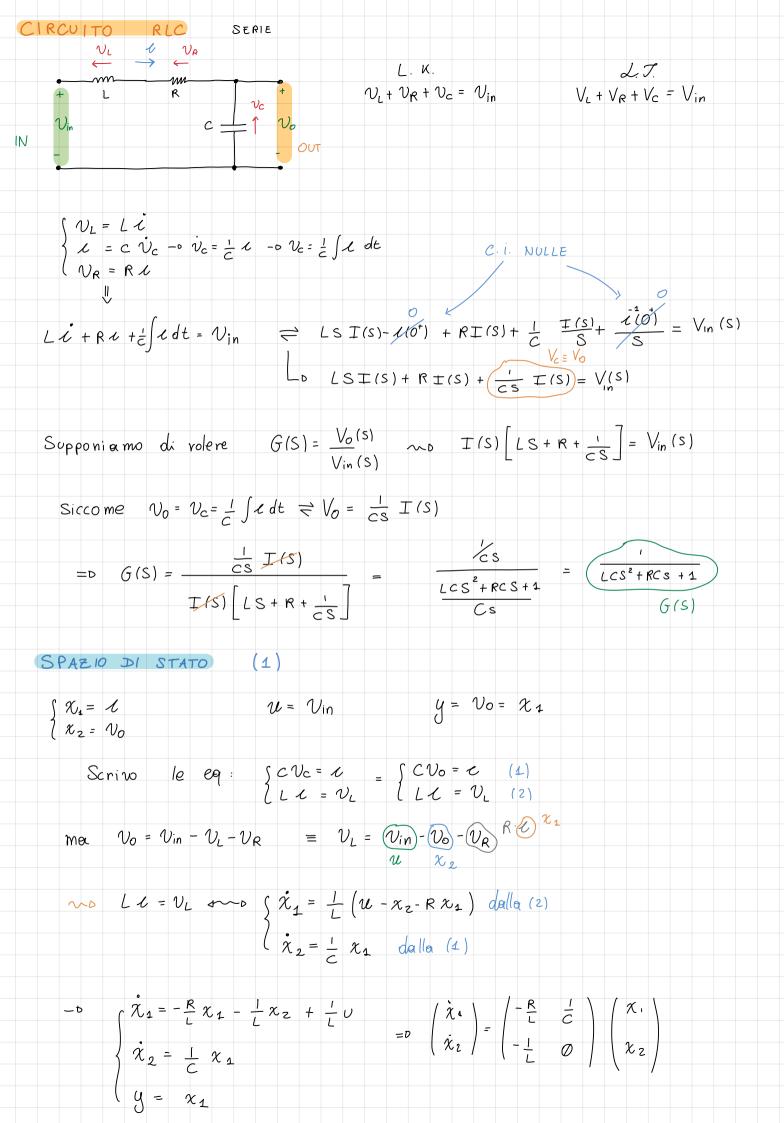
SCHEMA A BLOCCHI

dalle eq 
$$C \frac{dV_c}{dt} = C = C \frac{dV_o}{dt} = C = C S V_o(s) = I(s)$$

$$V_R = R \cdot \mathcal{L} - D \quad \mathcal{L} = \frac{V_R}{R} \quad \text{ma} \quad V_R = V_{\text{in}} - V_0 = D \quad \mathcal{L} = \frac{V_{\text{in}} - V_0}{R}$$

$$\Rightarrow I(S) = \frac{V_{\text{in}}(S) - V_0(S)}{R}$$



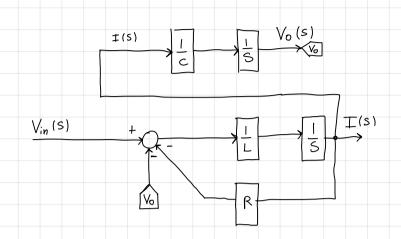


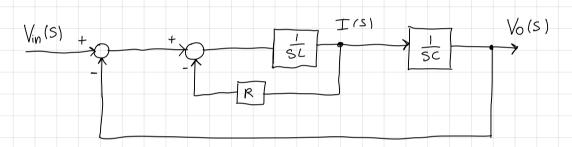
## SCHEMA A BLOCCHI

Dalle eq: 
$$\begin{cases} L \dot{i} = V_L \\ C \dot{V}_0 = L \\ V_R = R \cdot L \end{cases}$$

$$V_{L} = V_{in} - V_{O} - V_{R}$$

$$V_{R} = R \cdot L$$





Ricordia mo il sys in feedback: 
$$y = \frac{G}{1+G} \cdot R(s)$$

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$$=D \qquad V_{in} + \qquad I(S)$$

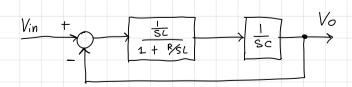
$$=D \qquad V_{in}(S) = \frac{1}{SL}$$

$$= \frac{1}{SL}$$

$$= \frac{1}{SL}$$

$$\frac{I(s)}{V_{in}(s)} = \frac{\frac{1}{sL}}{1 + \frac{R}{sL}}$$

-0 Posso scrivere lo schemo ounche cosi:



SPAZIO DI STATO (2)

(1) Equazione diff dalla funzione di trasferimento:

$$\frac{V_{o}(s)}{V_{in}(s)} = \frac{1}{LCs^{2} + RCs + 1} = D \qquad V_{in}(s) = LCs^{2}V_{o}(s) + RCSV_{o}(s) + V_{o}(s)$$

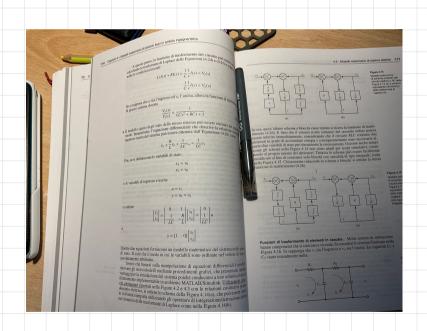
$$-D \qquad S^{2}V_{o}(s) + \frac{RS}{L}V_{o}(s) + \frac{1}{LC}V_{o}(s) = \frac{1}{LC}V_{in}(s)$$

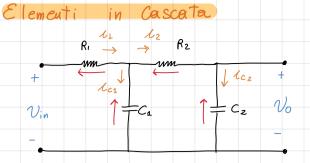
Siccome 
$$\mathcal{L}\left[\dot{f}(t)\right] = \frac{1}{5} \cdot F(S) = 0$$
  $v_0(t) + \frac{R}{L} \dot{v}_0(t) + \frac{1}{LC} v_0(t) = \frac{1}{LC} v_1(t)$ 

(2) Scelgo le entrate ed uscite e le Variabili di stato

Scelaro 
$$\begin{cases} x_1 = v_0 \\ x_2 = v_0 \end{cases}$$
  $\begin{cases} u = v_{in} \\ y = v_0 = x_1 \end{cases}$   $\begin{cases} x_n = A \times + B \cdot v \\ y = C \times + D \cdot v \end{cases}$ 

$$\begin{pmatrix} \dot{x}_1 \\ \dot{x}_2 \end{pmatrix} = \begin{pmatrix} \frac{1}{Lc} & \frac{R}{L} \\ & & \end{pmatrix} \begin{pmatrix} x_1 & v_0 \\ x_2 & \dot{v}_0 \end{pmatrix}$$





 $\Rightarrow V_{in}(s) =$ 

$$\begin{cases} \mathcal{N}_{C_1} = C_1 \mathcal{V}_{C_1} & \sim \circ & \mathcal{V}_{C_1} = \frac{1}{C_1} \int \mathcal{N}_{C_1} dt \\ \mathcal{N}_{C_2} = C_2 \mathcal{V}_{C_2} & \sim \circ & \mathcal{V}_{C_2} = \frac{1}{C_2} \int \iota_{C_2} dt \\ \end{cases}$$

$$\begin{cases} \mathcal{V}_1 = R_1 \mathcal{N}_1 \\ \mathcal{V}_2 = R_2 \mathcal{N}_2 \end{cases}$$

$$M_{1}: \begin{cases} V_{in} = V_{1} + V_{C_{1}} & -D & V_{C_{1}} = V_{in} - V_{1} \\ V_{2} = V_{2} & V_{2} = V_{2} \end{cases}$$

$$M_{2}: \begin{cases} V_{in} = V_{1} + V_{C_{1}} & -D & V_{C_{1}} = V_{in} - V_{1} \\ V_{in} - V_{1} = V_{2} + V_{C_{2}} & -D & V_{in} = V_{1} + V_{2} + V_{C_{2}} \end{cases}$$

$$V_{1} = R_{2}L_{1}$$
  $V_{2} = R_{2}L_{2}$ 
 $\uparrow$ 
 $V_{in} = V_{1} + V_{2} + V_{C2}$