

BPL_TEST2_Batch_calibration - demo

This notebook shows the possibilities for calibration of the model BPL_TEST2_Batch using `scipy.optimize.minimize()` routine. There are several different methods to choose between.

The text-book model of batch cultivation we simulate is the following where S is substrate, X is cell concentration, and V is volume of the broth

$$\frac{d(VS)}{dt} = -q_S(S) \cdot VX$$

$$\frac{d(VX)}{dt} = \mu(S) \cdot VX$$

and where specific cell growth rate μ and substrate uptake rate q_S are

$$\mu(S) = Y \cdot q_S(S)$$

$$q_S(S) = q_S^{max} \frac{S}{K_s + S}$$

where Y is the yield, q_S^{max} is the maximal specific substrate uptake rate and K_s is the corresponding saturation constant.

The parameter estimation is done with optimization methods that only require evaluation of the mismatch between simulation with given parameters and data. At start the allowed range for each parameter is given. The method used for optimization is SLQSP but can easily be changed [1].

In the near future the FMU may provide first derivative gradient information, that will make it possible to choose corresponding method of `minimize()` for improved performance. This possibility is related to the upgrade to the FMI-standard ver 3.0 for the Modelica compiler.

The Python package PyFMI [2] that is the base for FMU-explore has a simplified built-in functionality for parameter estimation that also use `scipy.optimize.minimize()`. However, there is estimated and the purpose seems to only address smaller examples. Therefore we here define a no possibility to include parameter changes to the compiled model that should not be Python function evaluation() that facilitate the formulation of the parameter estimation and bring flexibility to choice of optimization method.

In [1]:

```
run -i BPL_TEST2_Batch_explore.py
```

Windows - run FMU pre-compiled JModelica 2.14

Model for bioreactor has been setup. Key commands:

- `par()` - change of parameters and initial values
- `init()` - change initial values only
- `simu()` - simulate and plot
- `newplot()` - make a new plot
- `show()` - show plot from previous simulation
- `disp()` - display parameters and initial values from the last simulation
- `describe()` - describe culture, broth, parameters, variables with values / units

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Note that both `disp()` and `describe()` takes values from the last simulation

Brief information about a command by `help()`, eg `help(simu)`

Key system information is listed with the command `system_info()`

In [2]:

```
# Adjust the size of diagrams
plt.rcParams['figure.figsize'] = [15/2.54, 12/2.54]
```

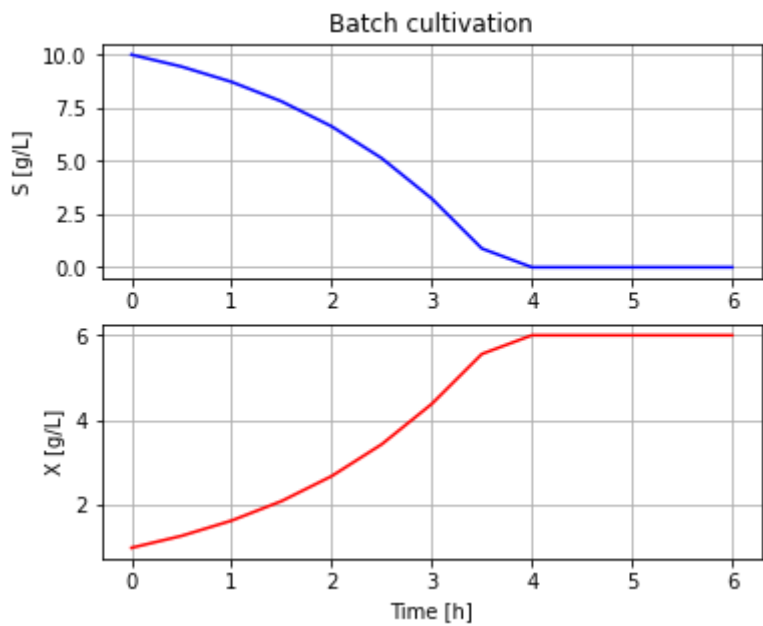
Generate data that later used for parameter estimation

In [3]:

```
import pandas as pd
```

In [4]:

```
# Data generated
par(Y=0.5, qSmax=1.0, Ks=0.1)
init(V_0=1.0, VS_0=10, VX_0=1.0)
newplot(plotType='Demo_1')
opts['ncp'] = 12
simu(6)
```



In [5]:

```
# Store data in a DataFrame for later use
data = pd.DataFrame(data={'time':sim_res['time'], 'X':sim_res['bioreactor.c[1]'], 'S':sim_res['S']})
```

Out[5]:

	time	X	S
0	0.0	1.000000	1.000000e+01
1	0.5	1.280773	9.438453e+00
2	1.0	1.640079	8.719842e+00
3	1.5	2.099615	7.800770e+00
4	2.0	2.686770	6.626459e+00
5	2.5	3.435479	5.129043e+00
6	3.0	4.385325	3.229350e+00

	time	X	S
7	3.5	5.559252	8.814967e-01
8	4.0	6.000000	1.048375e-08
9	4.5	6.000000	-1.936268e-10
10	5.0	6.000000	2.156125e-12
11	5.5	6.000000	9.975889e-14
12	6.0	6.000000	4.189854e-15

Alternatively we can choose to use data from an excel-file - do you prefer that?

Simulation with initial guess of parameters compared with data

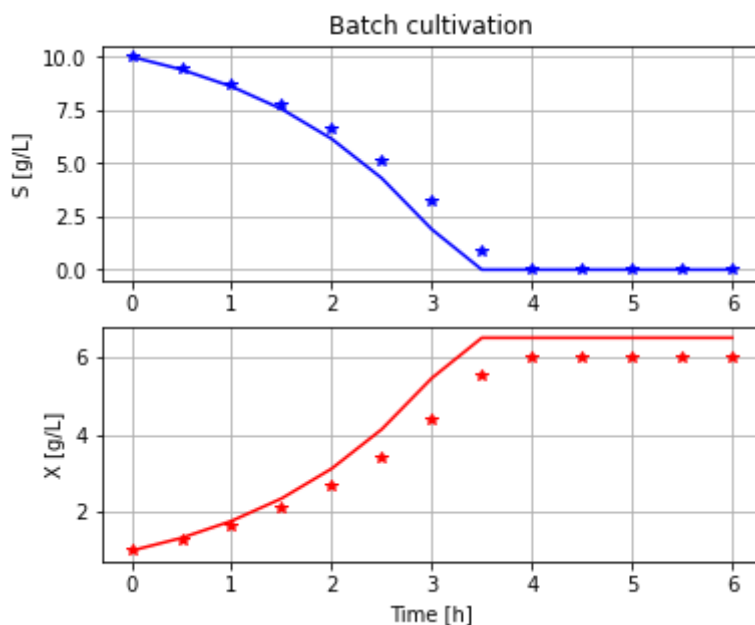
Here we define the parameters that should be estimated and specify allowed ranges. Nominal parameters are chosen as the mid-point of the allowed parameter range.

Simulation with these nominal parameter set and compare with data give an idea of how well the model fit data.

```
In [6]: # Parameters to be estimated using parDict names and their bounds
parEstim = ['Y', 'qSmax', 'Ks']
parBounds = [(0.4, 0.7), (0.8, 1.3), (0.05, 0.20)]
parEstim_0 = [np.mean(parBounds[k]) for k in range(len(parBounds))]
```

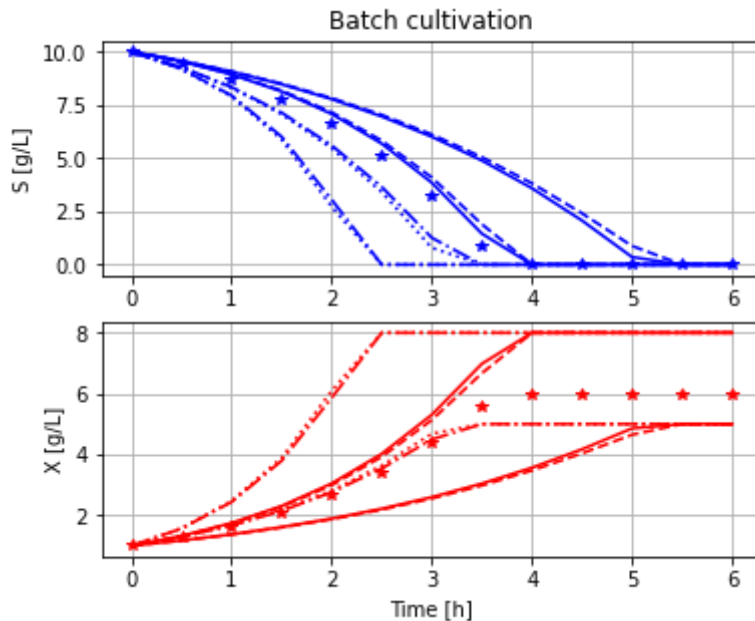
```
In [7]: # Simulation with nominal parameters
newplot(plotType='Demo_1')
par(Y=parEstim_0[0], qSmax=parEstim_0[1], Ks=parEstim_0[2])
simu(6)

# Show data
ax1.plot(data['time'], data['S'], 'b*')
ax2.plot(data['time'], data['X'], 'r*')
plt.show()
```



```
In [8]: # Simulation over the parameter ranges given
newplot(plotType='Demo_1')
for Y_value in parBounds [0]:
    for qSmax_value in parBounds[1]:
        for Ks_value in parBounds[2]:
            par(Y=Y_value, qSmax=qSmax_value, Ks=Ks_value)
            simu(6)

# Show data
ax1.plot(data['time'], data['S'],'b*')
ax2.plot(data['time'], data['X'],'r*')
plt.show()
```



Simulation over the different parameter combinations of the parameter bounds shows that data is "covered" and it should be possible to find a parameter combination that describes the data well.

Parameter estimation

Here we use the `scipy.optimize.minimize()` procedure which contains a family of different methods [1]. Since we have chosen to work with bounds on the parameters to be estimated there are only three methods to choose between. Here the method Sequential Least Squares Programming SLSQP is chosen.

```
In [9]: # For clarity of code here we import again
import scipy.optimize
```

```
In [10]: # Parameters to be estimated using parDict names and their bounds
extra_args = (parEstim, data, fmu_model, parDict, parLocation)
```

```
In [11]: # Modified evaluation function tailored for Python optimization algorithms
def evaluation(x, parEstim, data=data, fmu_model=fmu_model,
              parDict=parDict, parLocation=parLocation):
    """The parameter list is tailored for scipy optimization algorithms interface,
    where the first parameter x is an array with parameters that are tuned
```

```

        and evalauted."""

    # Load model
    global model
    if model is None:
        model = load_fmu(fmu_model)
    model.reset()

    # Change parameters and initial values from default
    for i, p in enumerate(parEstim): model.set(parLocation[p], x[i])
    for p in set(parDict)-set(parEstim): model.set(parLocation[p], parDict[p])

    # Simulation options
    opts = model.simulate_options()
    opts['ncp'] = 12
    opts['result_handling'] = 'memory'
    opts['silent_mode'] = True

    # Simulate
    sim_res = model.simulate(start_time=0.0, final_time=6.0, options=opts)

    # Calculate loss function V
    V={}
    V['X'] = np.linalg.norm(data['X'] - np.interp(data['time'], sim_res['time'], sim
    V['S'] = np.linalg.norm(data['S'] - np.interp(data['time'], sim_res['time'], sim

    return V['X'] + V['S']

```

In [12]: `import time`

In [13]: `# Run minimize()
start_time = time.time()
result = scipy.optimize.minimize(evaluation, x0=parEstim_0, args=extra_args,
 method='SLSQP', bounds=parBounds, options={"disp":T
print('CPU-time =', time.time()-start_time)`

```

Optimization terminated successfully    (Exit mode 0)
      Current function value: 0.0001843492608832435
      Iterations: 24
      Function evaluations: 127
      Gradient evaluations: 24
CPU-time = 0.37137293815612793

```

In [14]: `result`

```

Out[14]:
fun: 0.0001843492608832435
jac: array([ 2.03835198, -0.46493559, -1.85094705])
message: 'Optimization terminated successfully'
nfev: 127
nit: 24
njev: 24
status: 0
success: True
x: array([0.50000025, 1.00002488, 0.10014957])

```

The estimated parameters x are very close to the original values and no surprise.

Test of the three methods available that handle parameter bounds: TNC, L-BFGS-B and SLSQP. It turns out that SLSQP is by far the fastest. It is 3 times faster than L-BFGS-B which is faster than TNC. Can be that SLSQP is less robust though. The nit (number of iterations) does not differ that

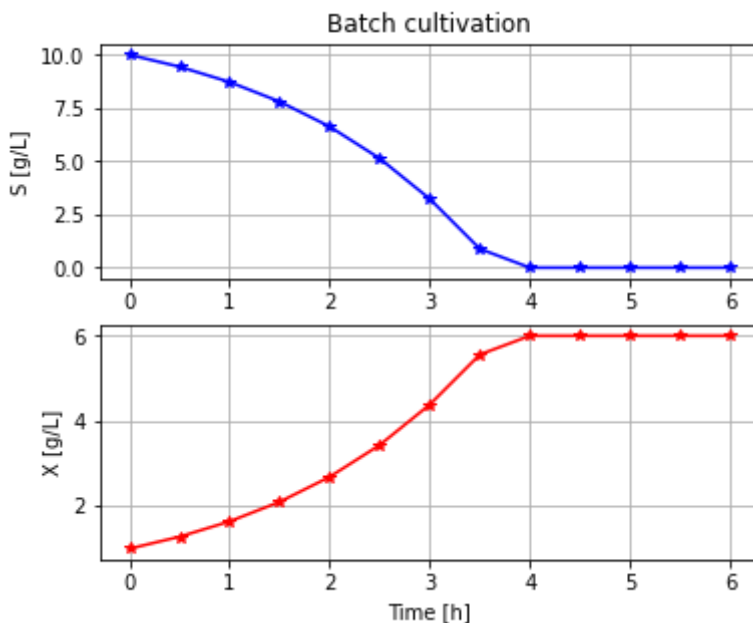
much though: 24 vs 30. The nfev (number of function evaluations) is perhaps more important 127 vs 256. A more precise timer function is likely timeit for this short times.

The Nelder-Mead algorithm has a good reputation to be very robust, but more slow, and with this method we cannot have bounds on the parameters.

Simulation with estimated parameters compared with data

```
In [15]: newplot(plotType='Demo_1')
par(Y=result.x[0], qSmax=result.x[1], Ks=result.x[2])
simu(6)

# Show data
ax1.plot(data['time'], data['S'],'b*')
ax2.plot(data['time'], data['X'],'r*')
plt.show()
```



Analysis of the loss function

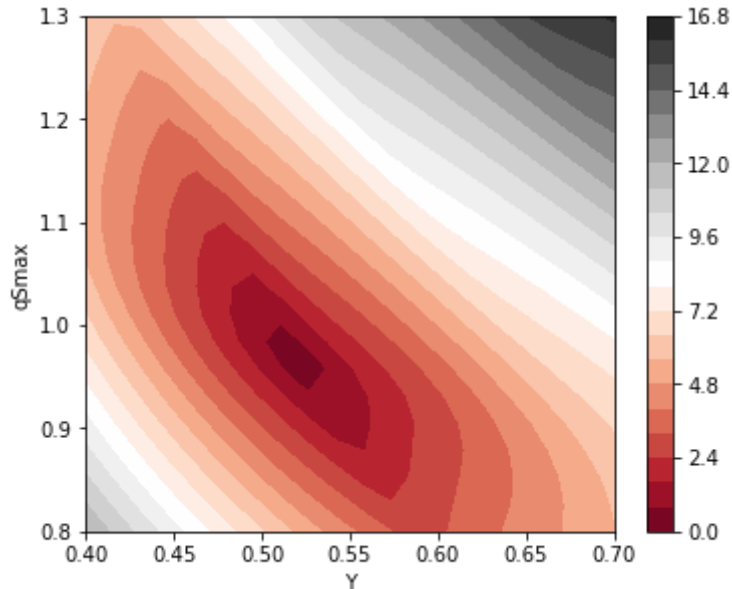
- Contour plot of simplified version $V(Y, qSmax)$
- One or several minima?
- Shape, elongated?
- Orthogonality of chosen parameters, compare with $V(Y, \mu_{max})$

```
In [16]: # Sweep through Y and qSmax variation and store the value of the loss-function for e
nY = 20
nqSmax = 20
V = np.zeros((nY, nqSmax))

Y = np.linspace(parBounds[0][0], parBounds[0][1], nY)
qSmax = np.linspace(parBounds[1][0], parBounds[1][1], nqSmax)

for j in range(nY):
    for k in range(nqSmax):
        V[j,k] = evaluation([Y[j], qSmax[k], 0.1], parEstim)
```

```
# Contour plot
plt.figure()
plt.subplot(1,1,1)
plt.contourf(Y, qSmax, V, 20, cmap='RdGy')
plt.colorbar()
plt.ylabel('qSmax')
plt.xlabel('Y')
plt.show()
```



We see

- Unique minima
- Narrow valley
- Valley about - 45 degree

Change variables to $\mu_{\max} = Y \cdot qS_{\max}$ vs qS_{\max}

Summary

A choice was made to work with allowed ranges of parameters to be estimated and a start value was defined as the center point in this parameter space.

An `evaluation()` function was created that define how the difference between simulation and data is measured. The function is rather transparent and easy to modify and you may want to change weight on the loss in S and X for instance. Here they have equal weight.

The FMU-explore workspace dictionaries `partDict[]` and `parLocation[]` are useful also here and simplify the code.

The call `optimize.minimize()` has several parameters and can easily be modified, for instance change of method.

The estimated parameters were close to perfect!

References

[1] Scipy Reference guide on optimize.minimize() [here](#)

[2] Andersson, C., Åkesson, J., Fuhrer C. : "PyFMI: A Python package for simulation of coupled dynamic models with the functional mock-up interface", Centre for Mathematical Sciences, Lund University, Report LUTFNA-5008, 2016.

Appendix

In [17]:

```
describe('parts')
```

```
['bioreactor', 'bioreactor.culture', 'liquidphase', 'MSL']
```

In [18]:

```
describe('MSL')
```

```
MSL: 3.2.2 build 3 - used components:
```

In [19]:

```
system_info()
```

```
System information
```

```
-OS: Windows
```

```
-Python: 3.9.5
```

```
-PyFMI: 2.9.5
```

```
-FMU by: JModelica.org
```

```
-FMI: 2.0
```

```
-Type: FMUModelCS2
```

```
-Name: BPL_TEST2.Batch
```

```
-Generated: 2022-09-13T11:19:04
```

```
-MSL: 3.2.2 build 3
```

```
-Description: Bioprocess Library version 2.1.0 beta
```

```
-Interaction: FMU-explore ver 0.9.3
```

In []: