$(n+1)C_{n+1}(X:Y) = \frac{1}{2}[X-Y,C_n(X:Y)]$