

# Computer Intensive Methods

## Presentation 1

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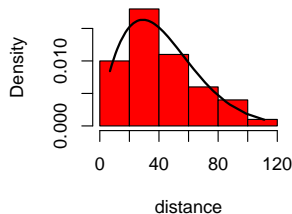
- Computing Odds Ratio

- Bootstrap Approach

## Appendix

# Exploration & Bootstrap Algorithm (Nonparametric)

**Histogram of distance**



- i Draw  $B = 5000, 50000, 100000$  from the data (stopping distance) with replacement
- ii Compute statistic of interest(maximum) from each bootstrap sample(bootstrap replicates)
- iii Approximate  $se(\hat{\theta})$  by the sample standard deviation of bootstrap replicates.

# Results, Problem & Remedies

## Results

Replicates	5000	50000	100000
SError	13.75	13.74	13.77

Table: Standard Error estimates

## Problems and Remedy

- ▶ Discrete not continuous distribution observed (see [Appendix graph](#))
- ▶ Poor approximation of the distribution of maximum ([Bickel, Gotze, and van Zwet \(1997\)](#))
- ▶ Remedy includes m out of n bootstrapp ([Bickel, Gotze, and van Zwet \(1997\)](#)) and Semiparametric bootstrapp ([Zelterman \(1993\)](#)).

# Bootstrap Algorithm (Parametric)

Candidate distributions based on extreme value theories include;

- i Gumbel
- ii Weibull
- iii Generalized extreme value distribution (GEV)

- i Draw  $B = 5000, 50000, 100000$  from a **distribution that best summarizes(weibull)** the data with parameters replaced with their plugin estimates
- ii Compute statistic of interest(maximum) from each bootstrap sample(bootstrap replicates)
- iii Approximate  $se(\hat{\theta})$  by the sample standard deviation of bootstrap replicates.

**Question of the best distribution to assume**

	Gumbel	Weibull	GEV
AIC	462.72	461.47	464.72

Table: AIC values of Candidate distributions

# Results & Comparison

## Results

Replicates	5000	50000	100000
SEerror	17.9	18.25	18.24

Table: Standard Error estimates

## Comparison & Discussions

- i Better approximation of the distribution of the maximum (See graph in appendix)
- ii Continuous and not discrete distribution observed.

# Bootstrap Algorithm (Non-Parametric) & Results

## Algorithm

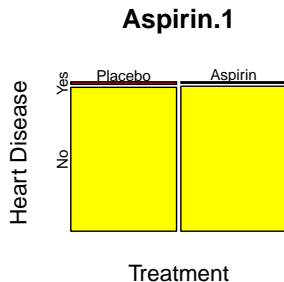
- i Draw  $B = 5000, 50000, 100000$  from the data (stopping distance) with replacement
- ii Compute probability of interest  $P(\text{distance} > 65\text{ft}) = \frac{\#(\text{distance} > 65)}{n}$  from each bootstrap sample (bootstrap replicates)
- iii Approximate  $P(\text{distance} > 65\text{ft})$  by the mean of bootstrap replicates.

## Results

Replicates	5000	50000	100000
Prob.	0.2	0.2	0.2

Table: Standard Error estimates

# Odds Ratio and Confidence Interval



## Results

- i Observation unit are
- ii Odds ratio is 1.83(1.44,2.33)
- iii The odds of.....



# Bootstrap Algorithm and Results

## Bootstrap t Algorithm

- i Draw  $B = 5000$  and  $50000$  bootstrap samples from the data and compute  $Z^* = \frac{\hat{\theta}^* - \hat{\theta}}{se(\hat{\theta}^*)}$ , where  $\hat{\theta}^*$  is the bootstrap log-odds and  $se(\hat{\theta}^*)$  is the corresponding bootstrap standard error.
- ii **Note that pairs are sampled**
- iii obtain quantiles of the replicate  $Z^*$
- iv Compute  $(\hat{\theta} + \hat{t}_{1-\alpha} se(\hat{\theta}), \hat{\theta} + \hat{t}_{\alpha} se(\hat{\theta}))$ , where  $\hat{\theta}$  is the estimated odds ratio and  $se(\hat{\theta})$  is the estimated standard error of the odds ratio.

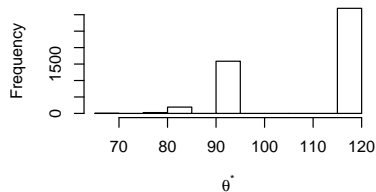
## Results

Replicates	5000	50000
Quantiles	-2.01, 1.99	-1.97, 1.93
CI	1.58, 2.07	1.59, 2.07

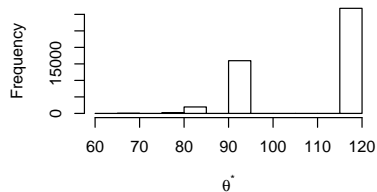
Table: Bootstrap Quantiles

# Distribution of Bootstrap Replicates (Non Parametric)

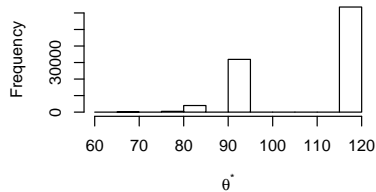
**5000 replicates**



**50000 replicates**

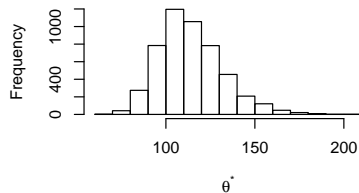


**1e+05 replicates**

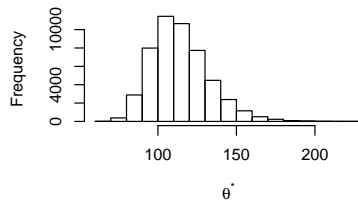


# Distribution of Bootstrap Replicates (Parametric)

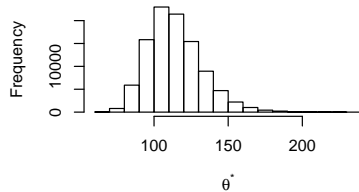
**5000 replicates**



**50000 replicates**

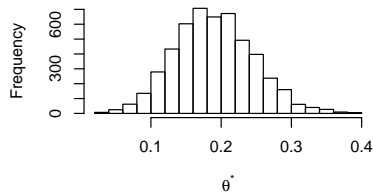


**1e+05 replicates**

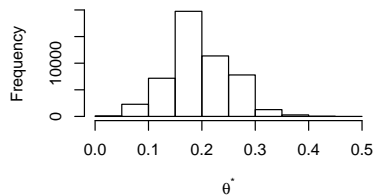


# Distribution of Bootstrap Replicates (Probability)

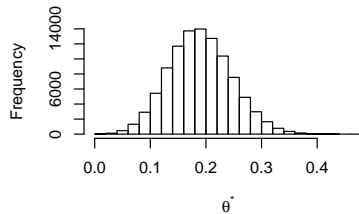
**5000 replicates**



**50000 replicates**



**1e+05 replicates**



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