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1 DNS study of turbulent pipe flow with imposed 2 radial rotation

3 Alessandro Ceci¹† and Sergio Pirozzoli ¹

4 ¹Dipartimento di Ingegneria Meccanica ed Aerospaziale, Sapienza University of Rome, Via Eudossiana
5 18, 00184 Rome, Italy

6 (Received xx; revised xx; accepted xx)

7 1. Introduction

8 2. The numerical dataset

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† Email address for correspondence: alessandro.ceci@uniroma1.it

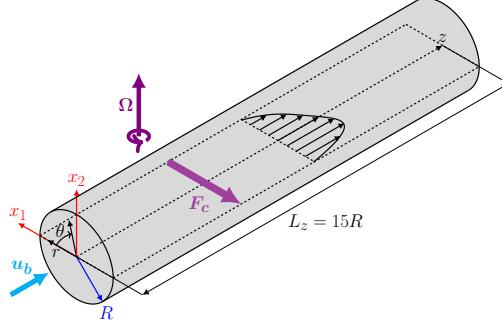


Figure 1: Definition of coordinate system for DNS of rotating pipe flow. z, r, θ are the axial, radial and azimuthal coordinates, respectively. R is the pipe radius, L_z the pipe length, and u_b is the bulk velocity. Ω is the angular velocity, and \mathbf{F}_c is the resultant mean Coriolis force. The Cartesian coordinates x_1, x_2 define positions in the cross-stream plane.

Re_b	Re_τ	N	$N_z \times N_r \times N_\theta$	$\lambda \times 10^{-2}$	Line
17000	508	0.0078125	$769 \times 97 \times 769$	2.862	—
17000	512	0.015625	$769 \times 97 \times 769$	2.942	—
17000	523	0.03125	$769 \times 97 \times 769$	3.030	—
17000	538	0.0625	$769 \times 97 \times 769$	3.212	—
17000	566	0.125	$769 \times 97 \times 769$	3.553	—
17000	610	0.25	$769 \times 97 \times 769$	4.120	—
17000	642	0.375	$769 \times 97 \times 769$	4.576	—
17000	669	0.5	$769 \times 97 \times 769$	4.962	—
17000	748	1.0	$769 \times 97 \times 769$	6.208	—
17000	856	2.0	$769 \times 97 \times 769$	8.117	—
44000	1405	0.5	$1793 \times 165 \times 1793$	3.262	-
82500	2379	0.5	$3073 \times 244 \times 3073$	2.662	-
133000	3634	0.5	$4609 \times 328 \times 4609$	2.389	-

Table 1: Flow parameters for DNS of rotating pipe flow. The bulk Reynolds number defined as $Re_b = 2Ru_b/\nu$, with R the pipe radius, u_b the bulk velocity and ν the fluid kinematic viscosity. $N = \Omega R/u_b$ is the rotation number and $N_\tau = \Omega R/u_\tau^*$ is the friction rotation number with the global friction velocity. N_z, N_r, N_θ are respectively the number of grid points in the axial, radial and azimuthal direction. The global friction factor is $\lambda = 8\tau_w^*/\rho u_b^2$, with τ_w^* the azimuthally averaged mean wall shear stress and ρ the fluid density. $Re_\tau = Ru_\tau^*/\nu$ is the friction Reynolds number, with $u_\tau^* = \sqrt{(\tau_w^*/\rho)}$ the mean friction velocity.

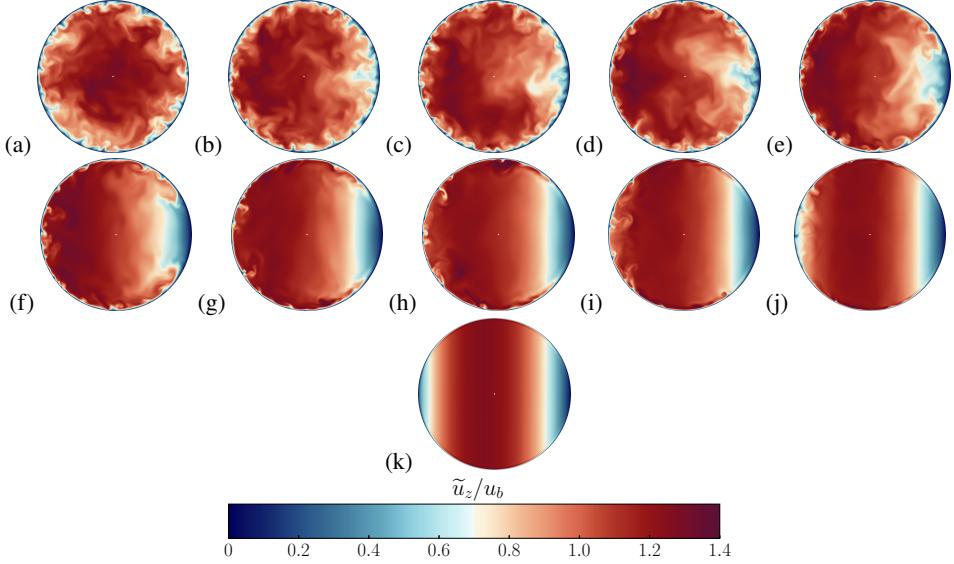


Figure 2: Instantaneous axial velocity contours at $Re_b = 17000$ in the cross-stream plane. Contour levels ranging from 0 to 1.4 are shown, in colour scale from blue to red. The pressure side of the pipe is on the left, and the suction side is on the right of each sub-panel. Various rotation numbers are considered: (a) $N = 0.0$, (b) $N = 0.0078125$, (c) $N = 0.015625$, (d) $N = 0.0315$, (e) $N = 0.0625$, (f) $N = 0.125$ (g) $N = 0.25$, (h) $N = 0.375$, (i) $N = 0.5$, (j) $N = 1.0$, (k) $N = 2.0$.

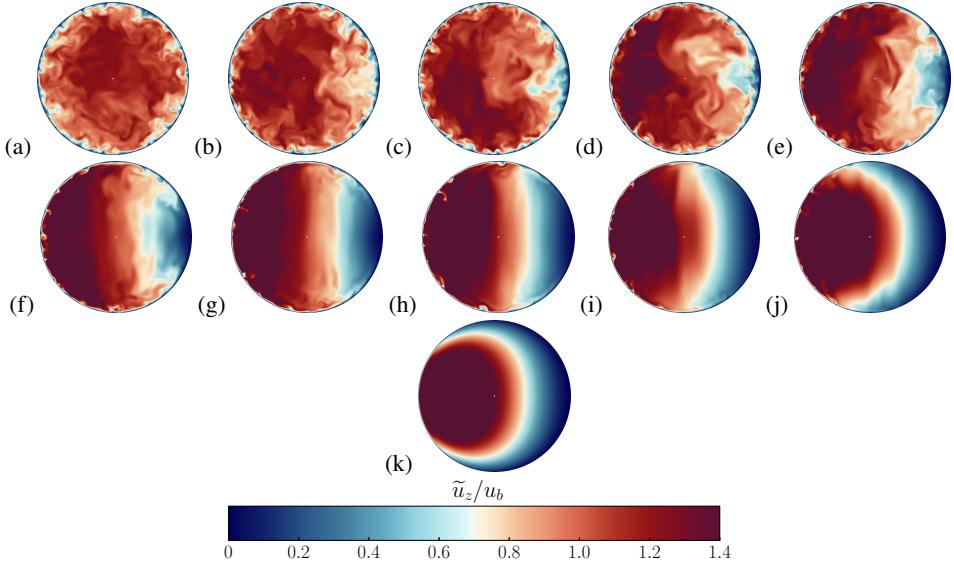


Figure 3: Instantaneous temperature contours at $Re_b = 17000$ in the cross-stream plane. Contour levels ranging from 0 to 1.4 are shown, in colour scale from blue to red. The pressure side of the pipe is on the left, and the suction side is on the right of each sub-panel. Various rotation numbers are considered: (a) $N = 0.0$, (b) $N = 0.0078125$, (c) $N = 0.015625$, (d) $N = 0.0315$, (e) $N = 0.0625$, (f) $N = 0.125$ (g) $N = 0.25$, (h) $N = 0.375$, (i) $N = 0.5$, (j) $N = 1.0$, (k) $N = 2.0$.

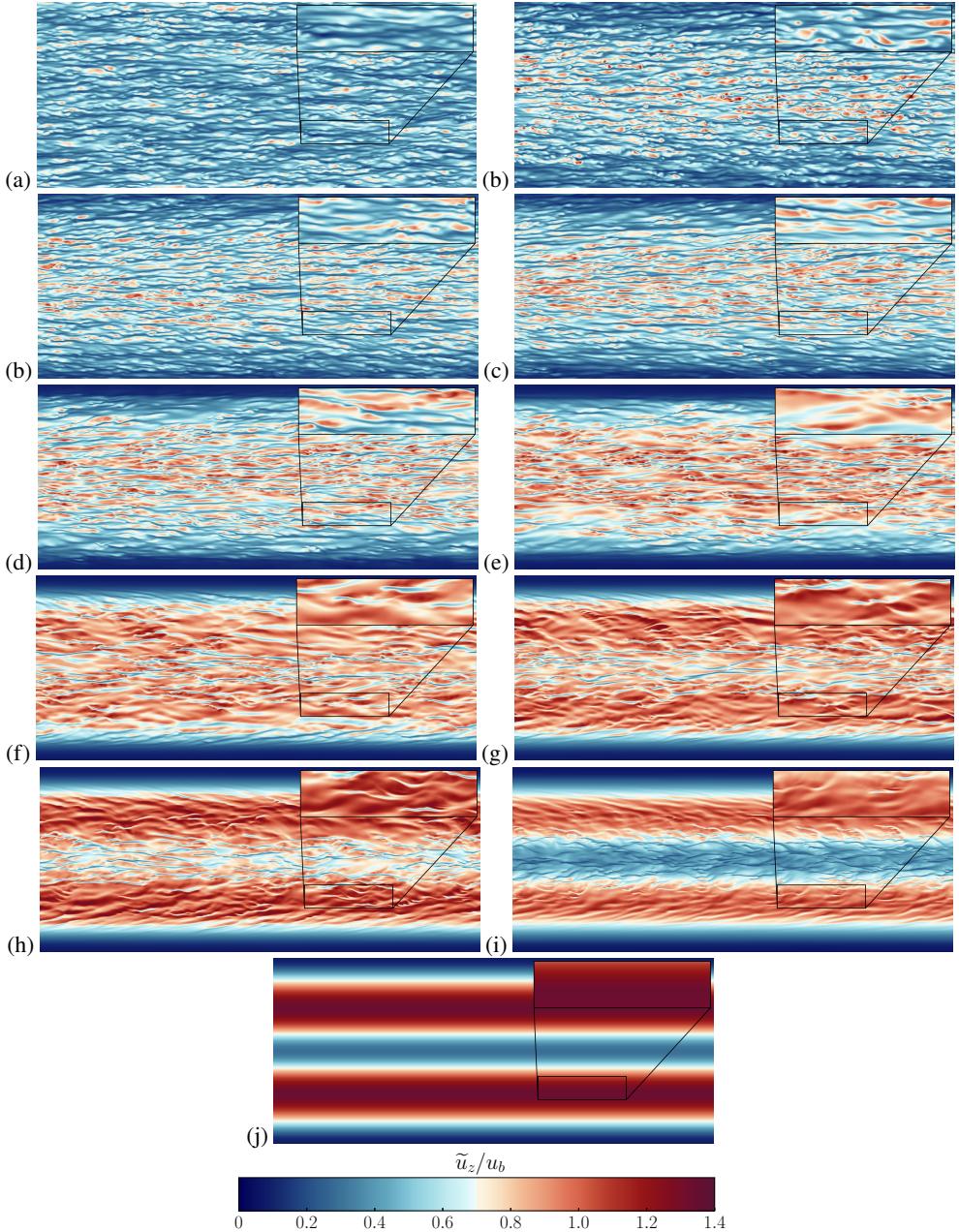


Figure 4: Instantaneous axial velocity (\tilde{u}_z/u_b) contours at $Re_b = 17000$ in an unrolled cylindrical shell at a distance $y^* = 15$ from the wall (evaluated in the non-rotating case).

Contour levels ranging from 0 to 1.4 are shown, in colour scale from blue to red. The insets in the top-right corner of each panel report magnified views of a small portion of the shell. Various rotation numbers are considered: (a) $N = 0.0$, (b) $N = 0.0078125$, (c) $N = 0.015625$, (d) $N = 0.0315$, (e) $N = 0.0625$, (f) $N = 0.125$, (g) $N = 0.1875$, (h) $N = 0.25$, (i) $N = 0.5$, (j) $N = 2.0$.

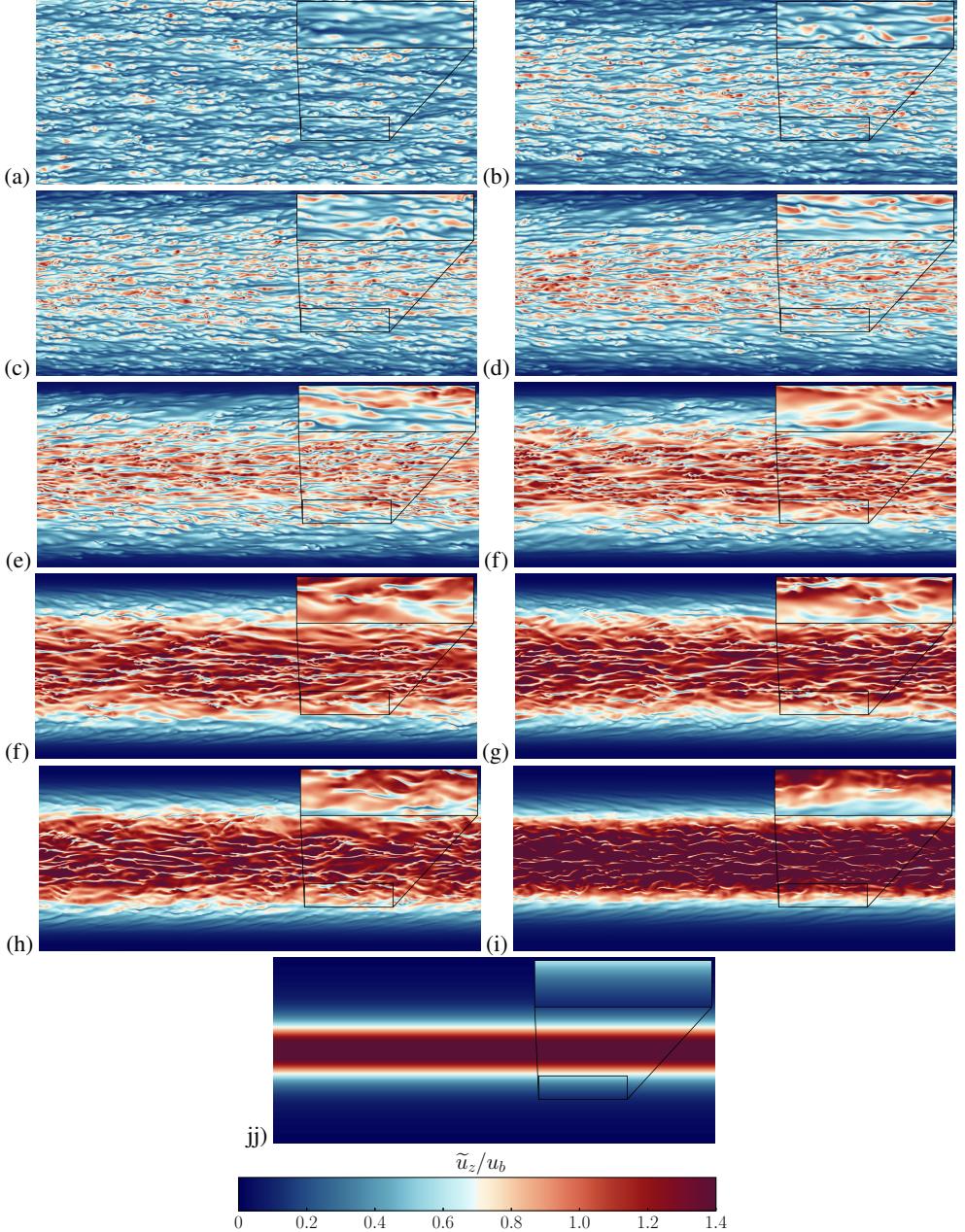


Figure 5: Instantaneous temperature (t_z/t_b) at $Re_b = 17000$ in an unrolled cylindrical shell at a distance $y^* = 15$ from the wall (evaluated in the non-rotating case). Contour levels ranging from 0 to 1.4 are shown, in colour scale from blue to red. The insets in the top-right corner of each panel report magnified views of a small portion of the shell.

Various rotation numbers are considered: (a) $N = 0.0$, (b) $N = 0.0078125$, (c) $N = 0.015625$, (d) $N = 0.0315$, (e) $N = 0.0625$, (f) $N = 0.125$, (g) $N = 0.1875$, (h) $N = 0.25$, (i) $N = 0.5$, (j) $N = 2.0$.

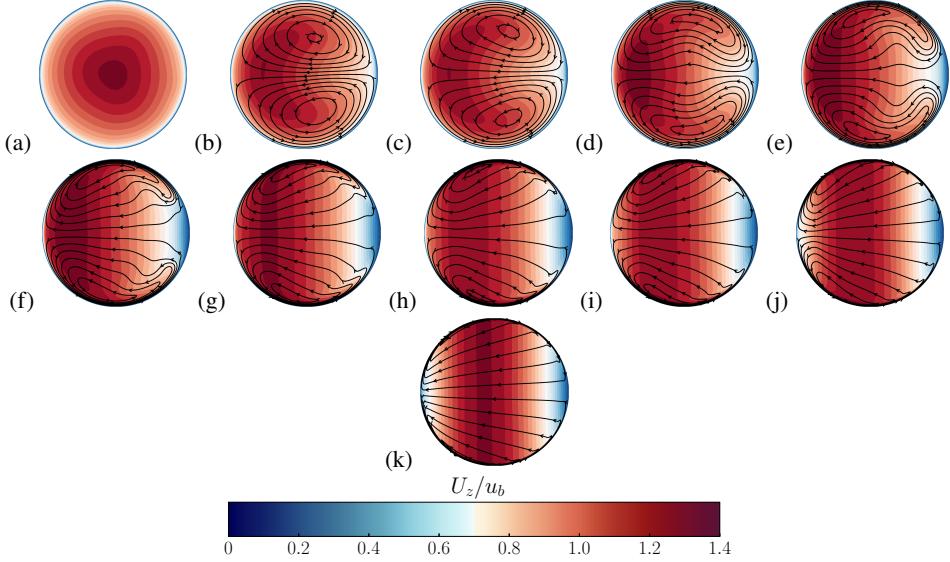


Figure 6: Mean axial velocity contours with superposed cross-flow streamlines, at $Re_b = 17000$. Twenty-four contour levels ranging from 0 to 1.4 are shown, in colour scale from blue to red. The pressure side of the pipe is on the left, and the suction side is on the right of each sub-panel. Various rotation numbers are considered: (a) $N = 0.0$, (b) $N = 0.0078125$, (c) $N = 0.015625$, (d) $N = 0.0315$, (e) $N = 0.0625$, (f) $N = 0.125$ (g) $N = 0.25$, (h) $N = 0.375$, (i) $N = 0.5$, (j) $N = 1.0$, (k) $N = 2.0$.

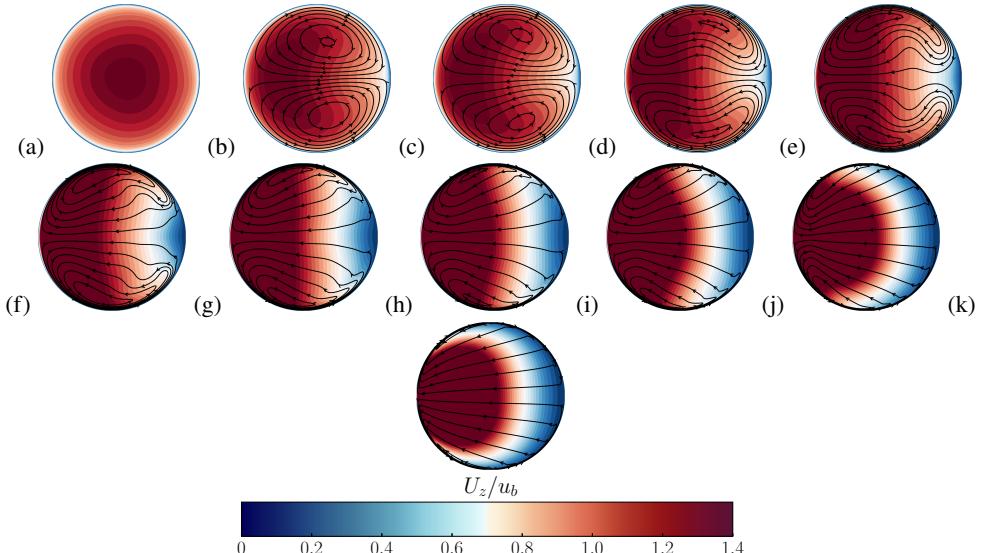


Figure 7: Mean temperature contours with superposed cross-flow streamlines, at $Re_b = 17000$. Twenty-four contour levels ranging from 0 to 1.4 are shown, in colour scale from blue to red. The pressure side of the pipe is on the left, and the suction side is on the right of each sub-panel. Various rotation numbers are considered: (a) $N = 0.0$, (b) $N = 0.0078125$, (c) $N = 0.015625$, (d) $N = 0.0315$, (e) $N = 0.0625$, (f) $N = 0.125$ (g) $N = 0.25$, (h) $N = 0.375$, (i) $N = 0.5$, (j) $N = 1.0$, (k) $N = 2.0$.

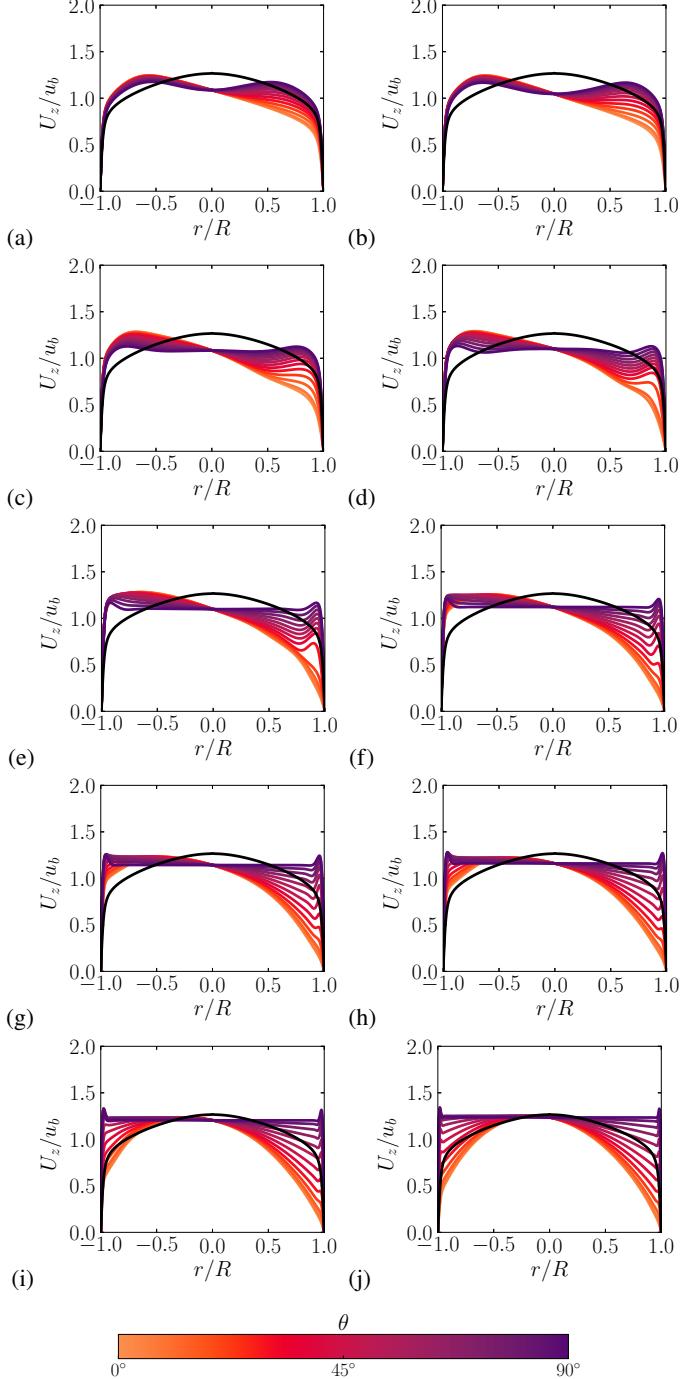


Figure 8: Radial profiles of outer-scaled axial velocity at various azimuthal positions, for flow cases at $Re_b = 17000$. Only the interval $\theta = [0^\circ, 90^\circ]$ is shown, at stations spaced 7.5° apart, with negative values of r signifying profiles taken at $\theta + 180^\circ$. (a) $N = 0.0078125$, (b) $N = 0.015625$, (c) $N = 0.0315$, (d) $N = 0.0625$, (e) $N = 0.125$ (f) $N = 0.25$, (g) $N = 0.375$, (h) $N = 0.5$, (i) $N = 1.0$, (j) $N = 2.0$. The black solid line denotes the mean axial velocity profile in the non-rotating case.

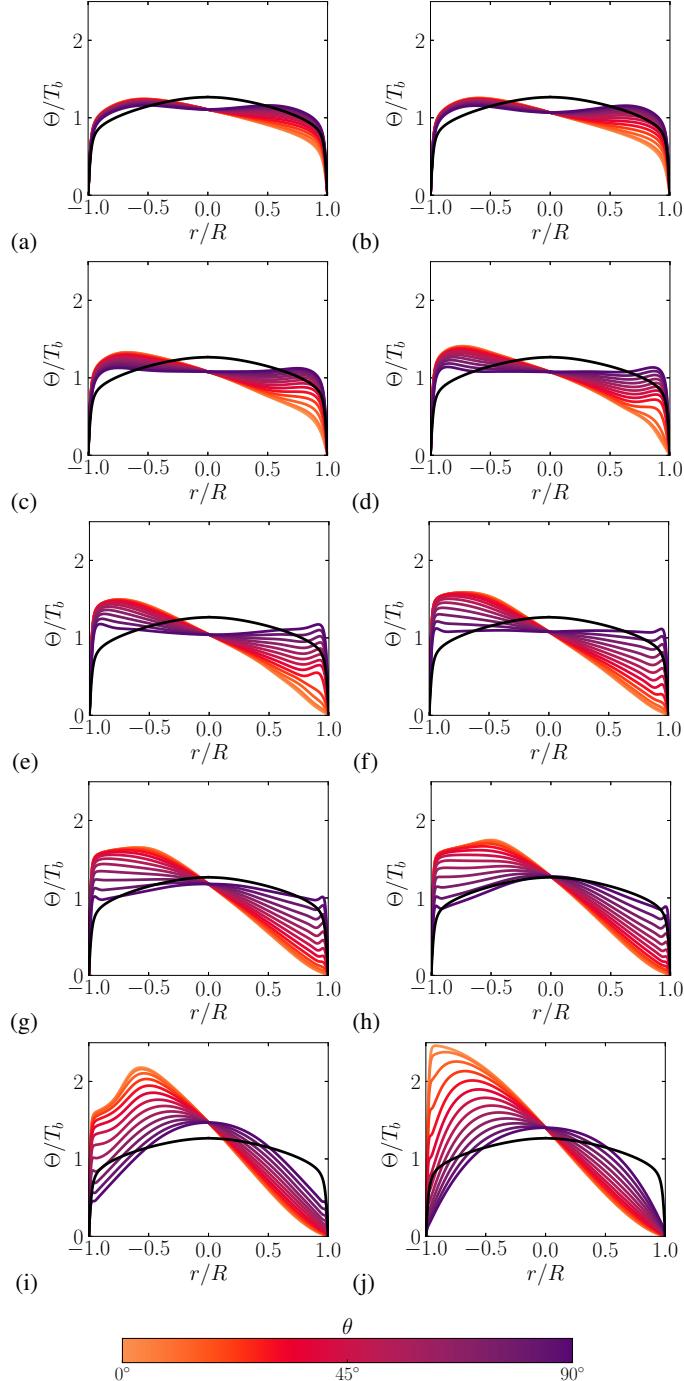


Figure 9: Radial profiles of outer-scaled temperature at various azimuthal positions, for flow cases at $Re_b = 17000$. Only the interval $\theta = [0^\circ, 90^\circ]$ is shown, at stations spaced 7.5° apart, with negative values of r signifying profiles taken at $\theta + 180^\circ$. (a) $N = 0.0078125$, (b) $N = 0.015625$, (c) $N = 0.0315$, (d) $N = 0.0625$, (e) $N = 0.125$ (f) $N = 0.25$, (g) $N = 0.375$, (h) $N = 0.5$, (i) $N = 1.0$, (j) $N = 2.0$. The black solid line denotes the mean axial velocity profile in the non-rotating case.

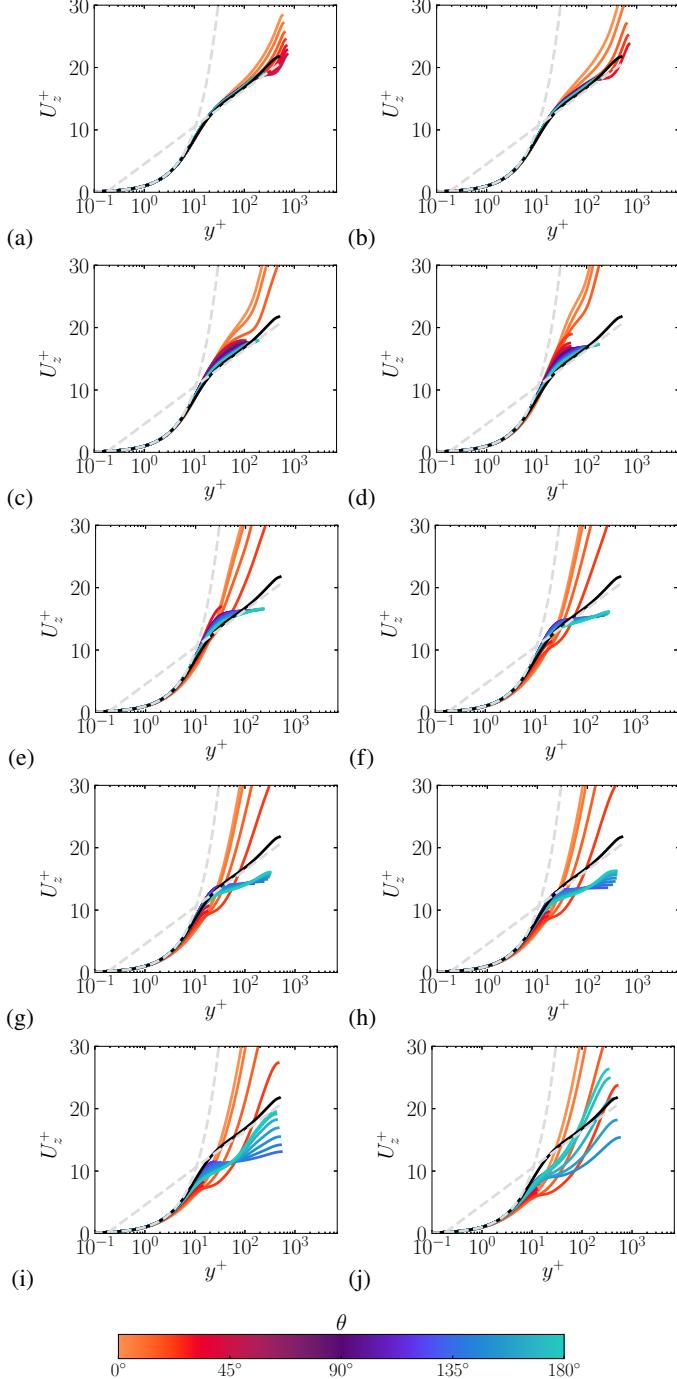


Figure 10: Wall-normal profiles of inner-scaled axial velocity, at various azimuthal positions spaced 7.5° apart, for flow cases at $Re_b = 17000$. Only the interval $\theta = [0^\circ, 180^\circ]$ is shown. (a) $N = 0.0078125$, (b) $N = 0.015625$, (c) $N = 0.0315$, (d) $N = 0.0625$, (e) $N = 0.125$ (f) $N = 0.25$, (g) $N = 0.375$, (h) $N = 0.5$, (i) $N = 1.0$, (j) $N = 2.0$. The black solid line denotes the mean axial velocity profile in the non-rotating case. The dashed gray lines depict the compound law-of-the wall $U^+ = \log y^+ / 0.387 + 4.53$.

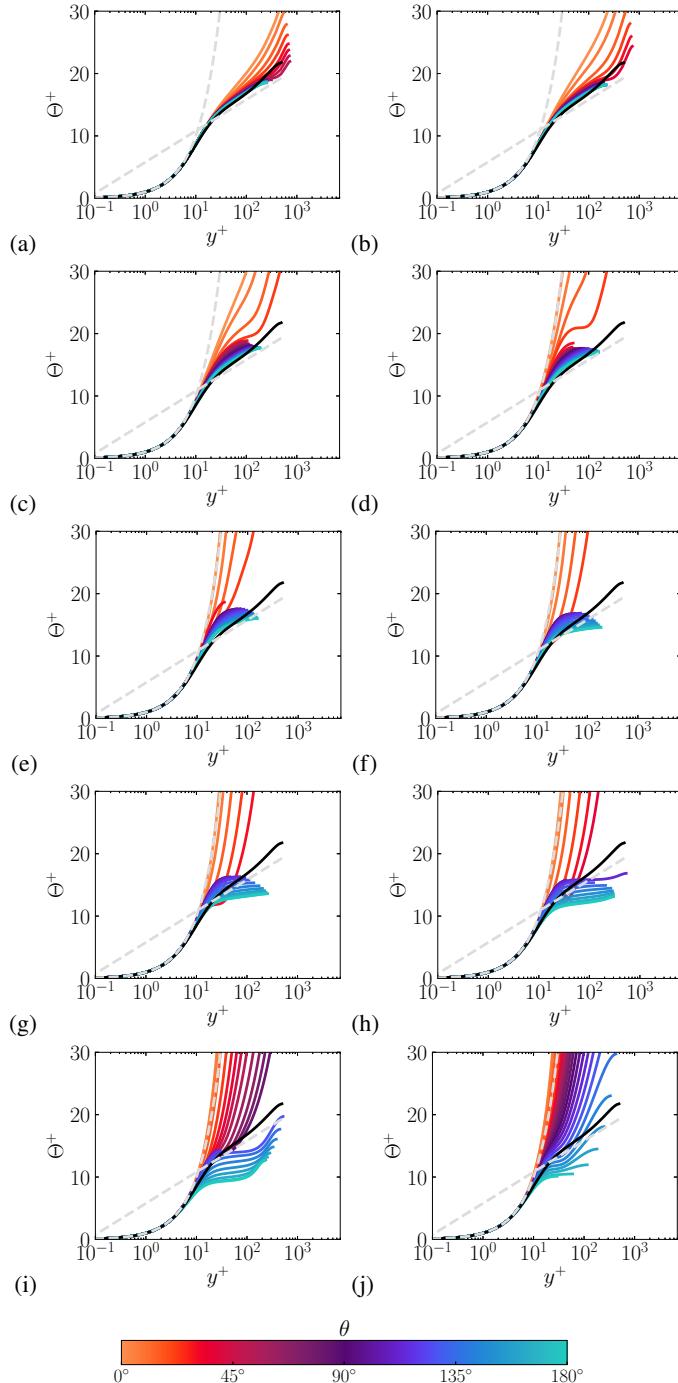


Figure 11: Wall-normal profiles of inner-scaled temperature, at various azimuthal positions spaced 7.5° apart, for flow cases at $Re_b = 17000$. Only the interval $\theta = [0^\circ, 180^\circ]$ is shown. (a) $N = 0.0078125$, (b) $N = 0.015625$, (c) $N = 0.0315$, (d) $N = 0.0625$, (e) $N = 0.125$ (f) $N = 0.25$, (g) $N = 0.375$, (h) $N = 0.5$, (i) $N = 1.0$, (j) $N = 2.0$. The black solid line denotes the mean temperature profile in the non-rotating case. The dashed gray lines depict the compound law-of-the wall $\theta^+ = y^+$, $\theta^+ = \log y^+ / 0.387 + 4.53$.

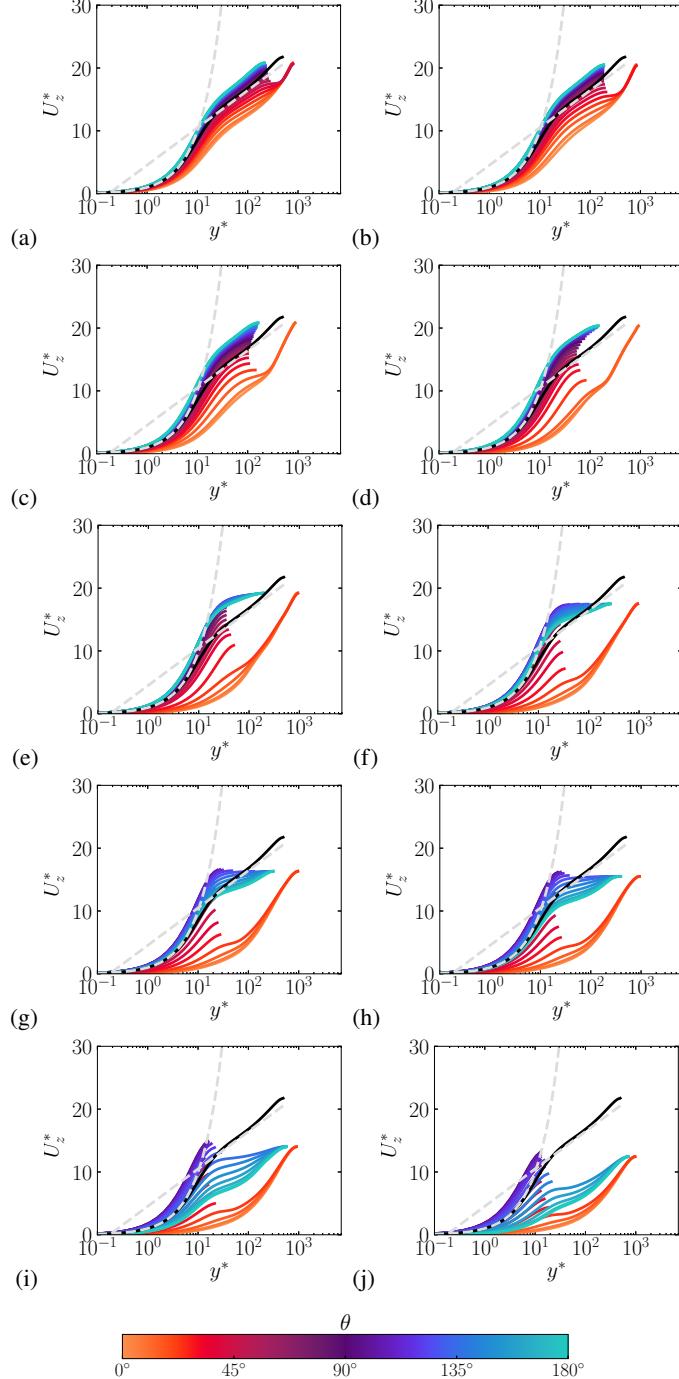


Figure 12: Wall-normal profiles of outer-scaled axial velocity, at various azimuthal positions spaced 7.5° apart, for flow cases at $Re_b = 17000$. Only the interval $\theta = [0^\circ, 180^\circ]$ is shown. (a) $N = 0.0078125$, (b) $N = 0.015625$, (c) $N = 0.0315$, (d) $N = 0.0625$, (e) $N = 0.125$ (f) $N = 0.25$, (g) $N = 0.375$, (h) $N = 0.5$, (i) $N = 1.0$, (j) $N = 2.0$. The black solid line denotes the mean axial velocity profile in the non-rotating case. The dashed gray lines depict the compound law-of-the wall $U^* = \log y^*/0.387 + 4.53$.

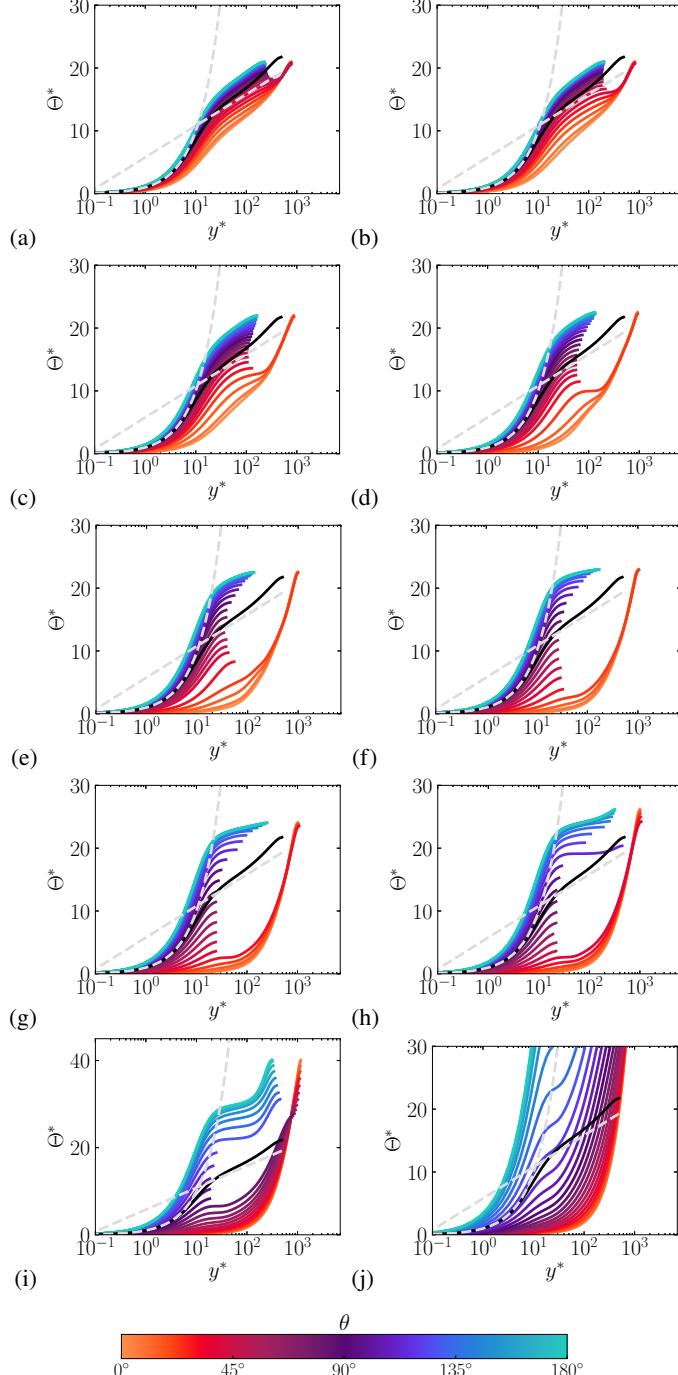


Figure 13: Wall-normal profiles of outer-scaled temperature, at various azimuthal positions spaced 7.5° apart, for flow cases at $Re_b = 17000$. Only the interval $\theta = [0^\circ, 180^\circ]$ is shown. (a) $N = 0.0078125$, (b) $N = 0.015625$, (c) $N = 0.0315$, (d) $N = 0.0625$, (e) $N = 0.125$ (f) $N = 0.25$, (g) $N = 0.375$, (h) $N = 0.5$, (i) $N = 1.0$, (j) $N = 2.0$. The black solid line denotes the mean temperature profile in the non-rotating case. The dashed gray lines depict the compound law-of-the wall $\theta^* = y^*$, $\theta^* = \log y^*/0.387 + 4.53$.

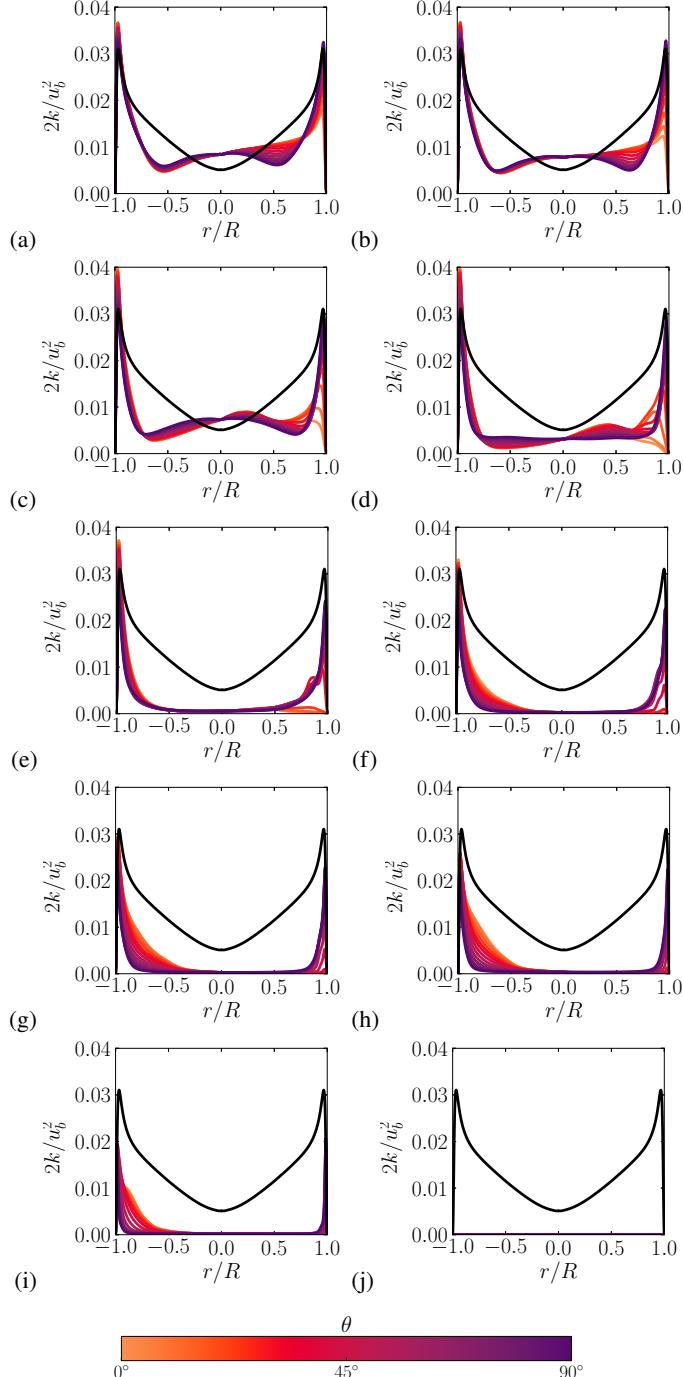


Figure 14: Radial profiles of outer-scaled turbulence kinetic energy at various azimuthal positions, for flow cases at $Re_b = 17000$. Only the interval $\theta = [0^\circ, 90^\circ]$ is shown, at stations spaced 7.5° apart, with negative values of r signifying profiles taken at $\theta + 180^\circ$.
 (a) $N = 0.0078125$, (b) $N = 0.015625$, (c) $N = 0.0315$, (d) $N = 0.0625$, (e) $N = 0.125$ (f) $N = 0.25$, (g) $N = 0.375$, (h) $N = 0.5$, (i) $N = 1.0$, (j) $N = 2.0$. The black solid line denotes the mean turbulence kinetic energy profile in the non-rotating case.

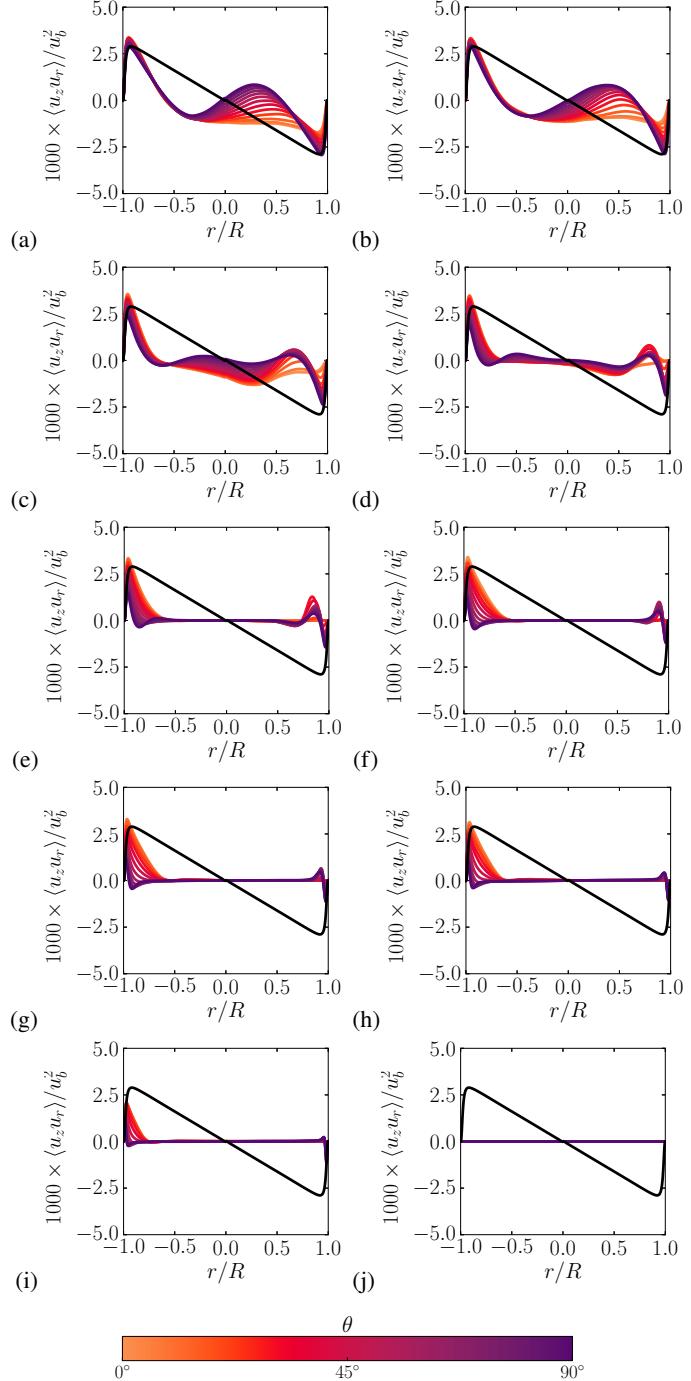


Figure 15: Radial profiles of outer-scaled Reynolds shear stress at various azimuthal positions, for flow cases at $Re_b = 17000$. Only the interval $\theta = [0^\circ, 90^\circ]$ is shown, at stations spaced 7.5° apart, with negative values of r signifying profiles taken at $\theta + 180^\circ$.
 (a) $N = 0.0078125$, (b) $N = 0.015625$, (c) $N = 0.0315$, (d) $N = 0.0625$, (e) $N = 0.125$ (f) $N = 0.25$, (g) $N = 0.375$, (h) $N = 0.5$, (i) $N = 1.0$, (j) $N = 2.0$. The black solid line denotes the Reynolds shear stress profile in the non-rotating case.

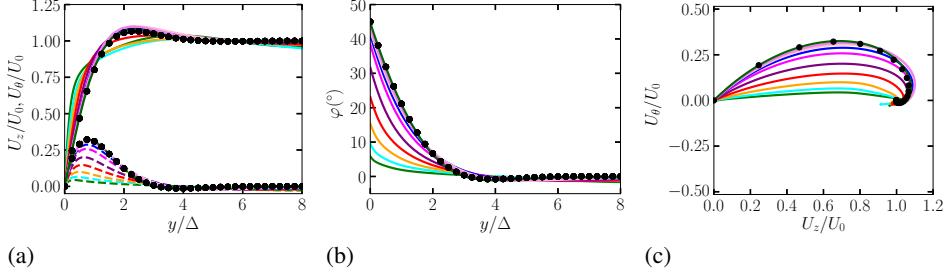


Figure 16: Profiles of mean axial (U_z) and azimuthal (U_θ) velocity (a), wall-parallel flow angle $\varphi = \tan^{-1}(U_\theta/U_z)$ (b) and hodograph diagram (c) at the polar coordinate $\theta = \pi/2$ (north pole of the pipe). Data are shown for $Re_b = 17000$, at various rotation numbers: (a) $N = 0.0078125$, (b) $N = 0.015625$, (c) $N = 0.0315$, (d) $N = 0.0625$, (e) $N = 0.125$ (f) $N = 0.25$, (g) $N = 0.375$, (h) $N = 0.5$, (i) $N = 1.0$, (j) $N = 2.0$. see table 1 for the color codes. The velocity profiles are scaled by the mean centreline axial velocity U_0 . The black circles denote the analytical solution for a laminar Ekman layer (?).

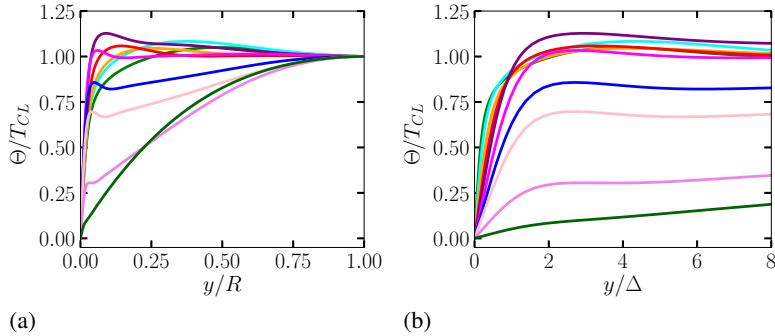


Figure 17: Profiles of the temperature Θ plotted at the poles of the pipe as a function of the radial coordinate normalised by the pipe radius (a) and the wall normal coordinate normalised by the local Ekman layer thickness (b). Data are shown for $Re_b = 17000$, at various rotation numbers: (a) $N = 0.0078125$, (b) $N = 0.015625$, (c) $N = 0.0315$, (d) $N = 0.0625$, (e) $N = 0.125$ (f) $N = 0.25$, (g) $N = 0.375$, (h) $N = 0.5$, (i) $N = 1.0$, (j) $N = 2.0$. see table 1 for the color codes. The temperature profiles are scaled by the temperature at the center of the pipe T_{CL} .

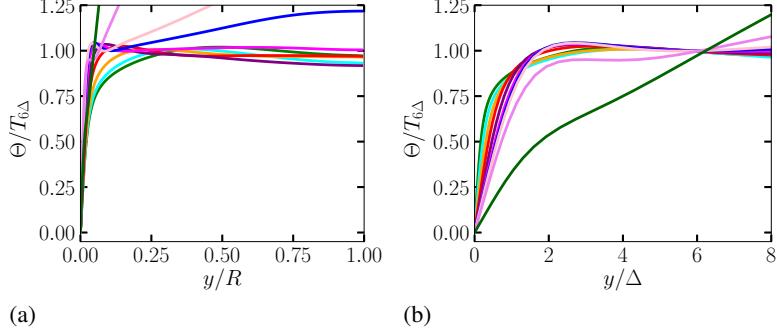


Figure 18: Profiles of the temperature Θ plotted at the poles of the pipe as a function of the radial coordinate normalised by the pipe radius (a) and the wall normal coordinate normalised by the local Ekman layer thickness (b). Data are shown for $Re_b = 17000$, at various rotation numbers: (a) $N = 0.0078125$, (b) $N = 0.015625$, (c) $N = 0.0315$, (d) $N = 0.0625$, (e) $N = 0.125$ (f) $N = 0.25$, (g) $N = 0.375$, (h) $N = 0.5$, (i) $N = 1.0$, (j) $N = 2.0$. see table 1 for the color codes. The temperature profiles are scaled by the temperature taken at the edge of the Ekman layer $T_{6\Delta}$.

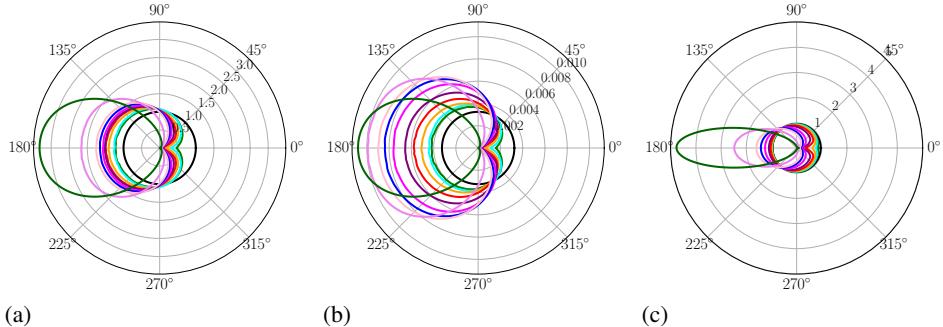


Figure 19: Polar distribution of the ratio of the local Stanton number and the global Stanton number (a), polar distribution of the local Stanton number (b) and polar distribution of the local Strong Reynolds Analogy factor (c), at $Re_b = 17000$. The color codes correspond to different values of N , as given in table 1, black denoting cases without rotation.

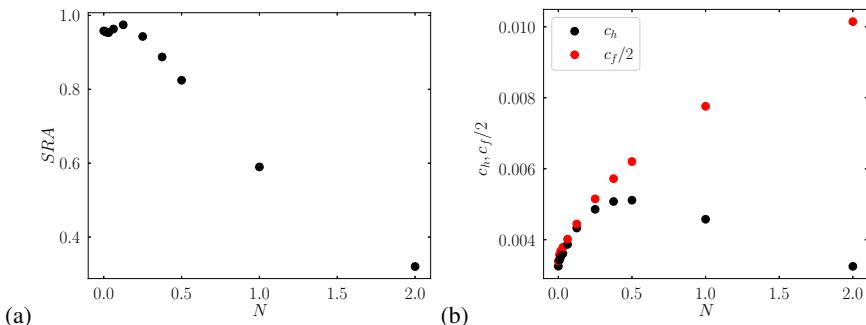


Figure 20: On the left the global Strong Reynolds Analogy factor as function of the rotation number N (a) and on the right the global Stanton number and friction coefficient as function of the rotation number (b).