

# Summary Tables of Sampling Distributions

Estimating $E(X) = \mu$ by $\bar{X} = \frac{\sum_{i=1}^n X_i}{n}$		
$X_i \sim i.i.d.N(\mu, \sigma^2)$		$X_i \sim i.i.d. (\mu, \sigma^2)$
for any $n$ , $\sigma^2$ known	for small $n$ , $\sigma^2$ unknown	for sufficiently large $n$
$\bar{X} \sim N(\mu, \frac{\sigma^2}{n})$  $\frac{\bar{X}-\mu}{\sqrt{\frac{\sigma^2}{n}}} \sim N(0, 1)$	$\bar{X} \sim t_{n-1}(\mu, \frac{s^2}{n})$  $\frac{\bar{X}-\mu}{\sqrt{\frac{s^2}{n}}} \sim t_{n-1}$	$\bar{X} \sim_{approx.} N(\mu, \frac{\sigma^2}{n})$ by CLT  $\frac{\bar{X}-\mu}{\sqrt{\frac{\sigma^2}{n}}} \sim_{approx.} N(0, 1)$ by CLT
Estimating $\pi$ by $P = \frac{\sum_{i=1}^n X_i}{n}$ where $\sum_{i=1}^n X_i \sim Bino(n, \pi)$		
for any $n$	for any $n$	for sufficiently large $n$
N/A	N/A	$P \sim_{approx.} N(\pi, \frac{\pi(1-\pi)}{n})$ by CLT  $\frac{P-\pi}{\sqrt{\frac{\pi(1-\pi)}{n}}} \sim_{approx.} N(0, 1)$ by CLT

Estimating $E(D) = \mu_D = \mu_X - \mu_Y$ by $\bar{D} = \frac{\sum_{i=1}^n D_i}{n}$ where $D_i = X_i - Y_i$ with a matched pair $X_i, Y_i$			
$D_i \sim i.i.d.N(\mu_D, \sigma_D^2)$			$D_i \sim i.i.d.(\mu_D, \sigma_D^2);$
for any $n, \sigma_D^2$ known	for small $n, \sigma_D^2$ unknown		for sufficiently large $n$
$\frac{\bar{D}-\mu_D}{\sqrt{\frac{\sigma_D^2}{n}}} \sim N(0, 1)$	$\frac{\bar{D}-\mu_D}{\sqrt{\frac{s_D^2}{n}}} \sim t_{n-1}, \quad (s_D^2 = \frac{\sum(D_i-\bar{D})^2}{n-1})$		$\frac{\bar{D}-\mu_D}{\sqrt{\frac{\sigma_D^2}{n}}} \sim_{approx.} N(0, 1)$ by CLT
Estimating $E(X - Y) = \mu_X - \mu_Y$ by $\bar{X} - \bar{Y}$ where $\bar{X} = \frac{\sum_{i=1}^{n_X} X_i}{n_X}, \bar{Y} = \frac{\sum_{i=1}^{n_Y} Y_i}{n_Y}, (X_i, Y_i \text{ indep.})$			
$X_i \sim i.i.d.N(\mu_X, \sigma_X^2); Y_i \sim i.i.d.N(\mu_Y, \sigma_Y^2)$			$X_i \sim i.i.d.(\mu_X, \sigma_X^2); Y_i \sim i.i.d.(\mu_Y, \sigma_Y^2);$
for any $n_X, n_Y, \sigma_X^2, \sigma_Y^2$ known	for small $n_X, n_Y, \sigma_X^2, \sigma_Y^2$ unknown		for sufficiently large $n_X, n_Y$
$\frac{(\bar{X}-\bar{Y})-(\mu_X-\mu_Y)}{\sqrt{\frac{\sigma_X^2}{n_X} + \frac{\sigma_Y^2}{n_Y}}} \sim N(0, 1)$	$\sigma_X^2 = \sigma_Y^2$	$\sigma_X^2 \neq \sigma_Y^2$	$\frac{(\bar{X}-\bar{Y})-(\mu_X-\mu_Y)}{\sqrt{\frac{\sigma_X^2}{n_X} + \frac{\sigma_Y^2}{n_Y}}} \sim_{approx.} N(0, 1)$ by CLT
	$\frac{(\bar{X}-\bar{Y})-(\mu_X-\mu_Y)}{s_p \sqrt{\frac{1}{n_X} + \frac{1}{n_Y}}} \sim t_{n_X+n_Y-2}$	$\frac{(\bar{X}-\bar{Y})-(\mu_X-\mu_Y)}{\sqrt{\frac{s_X^2}{n_X} + \frac{s_Y^2}{n_Y}}} \sim t_{df}$	
Estimating $\pi_X - \pi_Y$ by $P_X - P_Y$ where $P_X = \frac{\sum_{i=1}^{n_X} X_i}{n_X}, P_Y = \frac{\sum_{i=1}^{n_Y} Y_i}{n_Y}, \sum_{i=1}^{n_X} X_i \sim Bino(n_X, \pi_X); \sum_{i=1}^{n_Y} Y_i \sim Bino(n_Y, \pi_Y), (X_i, Y_i \text{ indep.})$			
for any $n_X, n_Y$	for any $n_X, n_Y$		for sufficiently large $n_X, n_Y$
N/A	N/A		$\frac{(P_X-P_Y)-(\pi_X-\pi_Y)}{\sqrt{\frac{\pi_X(1-\pi_X)}{n_X} + \frac{\pi_Y(1-\pi_Y)}{n_Y}}} \sim_{approx.} N(0, 1)$ by CLT