

Given  $P = \sum(0, 2, 4) + d\sum(3, 4)$

	4	2	1
0	0	0	0
2	0	1	0
3	0	1	1
4	1	0	0
5	1	0	1
6	1	1	0

→ For every min term that is matched we will put 1 in the map.

Step 1:

Group	min term	Variable
0	0 ✓	A B C
		0 0 0
1	2 ✓	0 1 0
	4 ✓	1 0 0
2	3 ✓	0 1 1
	5 ✓	1 0 1
	6 ✓	1 1 0

Step 2:

Group	matched pair	Variable
0	0, 2 ✓	A B C
		0 - 0
	0, 4 ✓	- 0 0
1	2, 3 ✓	0 1 -
		- 1 0
	4, 5 ✓	1 0 -
		- 1 0
	4, 6 ✓	1 - 0

Step 3:

Group	matched pair	Variable
0	0, 2, 4, 6	A B C
		- - 0
	0, 4, 2, 6	- - 0

Prime implicants table:

P I	0	2	4	6	min terms
$\bar{C}$	(X)	X		(X)	0, 2, 4, 6
$\bar{A}B$		X			2, 3
$A\bar{B}$			(X)		4, 5

⇒  $Y = \bar{C} + \bar{A}B$

b) K-Map

	0	1	1	0
A	1	1	X	1
B	X	1	1	1

⇒  $Y = \bar{C} + \bar{A}B$

→ The output of K-Map is same as the output of Tabulation Method.

1. Design a combinational circuit with three inputs:  $x, y, z$  and three outputs:  $A, B, C$ , such that,
- When the binary input  $xyz$  represents the decimal digits 1, 3, or 4, the binary output  $ABC$  should represent the decimal digit that is 3 greater than the input: that is 4, 6, or 7 respectively.
  - Similarly, when the binary input represents the digits 0 or 2, the binary output should represent the digit that is 2 greater than the input.
  - The remaining three, binary representations of the decimal digits 5, 6, and 7 never occur.

a) Start by drawing the truth table for the functions  $A, B$ , and  $C$ .

	x	y	z	A	B	C
0	0	0	0	0	0	0
1	0	0	1	1	0	0
2	0	1	0	1	1	0
3	0	1	1	1	1	1
4	1	0	0	1	0	1
5	1	0	1	d	d	d
6	1	1	0	d	d	d
7	1	1	1	d	d	d

b) Next, using K-Maps find all minimal forms of the three functions.

K-Maps for A, B, and C:

For A:  $A = yz + x\bar{y}$

For B:  $B = xz + y\bar{z}$

For C:  $C = x + y + z$

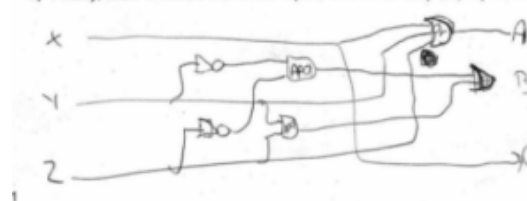
Minimal forms of the functions:

$f(A) = A$

$f(B) = B$

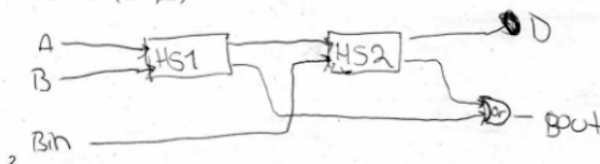
$f(C) = C$

c) Finally, draw a circuit with three inputs and three outputs, representing a minimal form of the functions.



3. Draw a full-subtractor using two half-subtractors, and one more simple gate only.

Hint:  $D = A - (B + \beta_{in})$



5. Draw a simple controlled D-Flip-Flop using two gates and inverters, and one D-Flip-Flop.



a	A	B	C	Y1	Y2	Y3
0	0	0	0	0	0	0
0	0	0	1	0	0	1
0	0	1	0	0	1	0
0	0	1	1	0	1	1
0	1	0	0	1	0	0
0	1	0	1	1	0	1
0	1	1	0	1	1	0
0	1	1	1	1	1	1
1	0	0	0	0	0	0
1	0	0	1	1	0	0
1	0	1	0	0	1	0
1	0	1	1	1	1	0
1	1	0	0	0	0	1
1	1	0	1	1	0	1
1	1	1	0	0	1	1
1	1	1	1	1	1	1

Using K-map for each output we will find function.

K-Map for  $Y_1$ :

BC	00	01	11	10
A=0	0	0	0	0
A=1	1	1	1	1

$Y_1 = \bar{A} + A = 1$

K-Map for  $Y_2$ :

BC	00	01	11	10
A=0	0	0	1	0
A=1	0	1	1	0

$Y_2 = B$

K-Map for  $Y_3$ :

BC	00	01	11	10
A=0	0	0	1	1
A=1	0	1	1	0

$Y_3 = \bar{A} + B$

