

**In-Video Quiz Questions for
Unit 8 Frequentist vs. Bayesian Inference**

(04:03) – slide 6, after “you might choose to do so and keep your money in your pocket.”

1. How many M&Ms would you like to buy?

5, 10, 15, or 20?

There is no correct answer here, but stop and think about the impact of your sample size, and make a decision.

(05:19) – slide 7, after “Remember that the significance level is also the probability of the type one error rate.”

2. What is a Type 1 error?

- (a) Failing to reject the null hypothesis when the null hypothesis is true.
- (b) Failing to reject the null hypothesis when the null hypothesis is false.
- (c) Rejecting the null hypothesis when the null hypothesis is true.
- (d) Rejecting the null hypothesis when the null hypothesis is false.

(08:08) – slide 9, after “So, therefore probability that the number of successes is greater than or equal to one, can be calculated 1 minus the probability of successes equaling zero.”

3. Assuming that 10% of M&Ms are yellow, which of the following is the correct calculation of the probability of obtaining at least one yellow M&M in a random sample of 5 M&Ms?

- (a) $(1 - 0.9)^5$
- (b) $1 - 0.9^5$
- (c) $1 - 0.1^5$
- (d) $1 - 0.9 \times 5$

(10:03) – slide 11, after “Remember that the significance level is also the probability of the type one error rate.”

4. Which of the following is the correct calculation of at least 2 successes in 10

trials? Check all that apply.

- (a) $P(K=2)+P(K=3)+\cdots+P(K=10)$
- (b) $P(K=3)+P(K=4)+\cdots+P(K=10)$
- (c) $1-[P(K=0)+P(K=1)+P(K=2)]$
- (d) $1-[P(K=0)+P(K=1)]$

(12:56) – slide 15, after “Given that the probability of success is 10% and we have a sample size of 20.”

5. Given that

H_0 : 10% yellow M&Ms

H_A : 20% yellow M&Ms

If in a random sample of 20 M&Ms there are 4 yellow M&Ms, what is the p-value?

Choose the **closest** answer.

- (a) 0.01
- (b) 0.09
- (c) 0.13
- (d) 0.59

(20:06) – slide 17, after “That is one success out of five trials, if the true probability of success was, instead of 10, 20%.”

6. What is the probability of 1 yellow M&M in a random sample of 5 M&Ms if 20% of the M&Ms are yellow? Choose the closest answer.

- (a) 0.0064
- (b) 0.41
- (c) 0.5
- (d) 0.67

(12:56) – slide 21, after “Our posterior probability for the hypothesis that percentage of yellow M&Ms is 10% was 0.44.”

7. If the posterior probability of the hypothesis that states that the population has 10% yellow M&Ms is 0.44, what is the posterior probability of the

hypothesis that states that the population has 20% yellow M&Ms?

- (a) -0.44
- (b) 0.44
- (c) 0.5
- (d) 0.56

(22:50) – slide 22, after “In this case remember we have said our sample size is ten and our number of successes is two.”

8. What is the probability of obtaining 2 yellow M&Ms in a random sample of 10 M&Ms if 10% of M&Ms are yellow?

- (a) 0.01
- (b) 0.09
- (c) 0.13
- (d) 0.59

(24:30) – slide 24, after “And once again, what changes are going to be the probability of the observed data given p is equal to 10 or 20%.”

9. What is the posterior probability of the hypothesis that states that 10% of M&Ms are yellow if the prior probability for this hypothesis is 0.5, and in the data we observed 3 yellow M&Ms in a random sample of 15 M&Ms?

- (a) 0.13
- (b) 0.25
- (c) 0.34
- (d) 0.5
- (e) 0.66

(26:30) – slide 24, after “Which yields a posterior probability of 29% roughly.”

10. Take a moment to think about how these probabilities were calculated, and if you're not sure, review earlier portions of the video and try calculating the probabilities yourself.

See below for calculations:

$$P(4 \text{ yellow M\&Ms in } 20 \mid p = 10\%) = \binom{20}{4} \times 0.1^4 \times 0.9^{16} \approx 0.09$$

In R: `dbinom(4, 20, 0.10)`

$$P(4 \text{ yellow M\&Ms in } 20 \mid p = 20\%) = \binom{20}{4} \times 0.2^4 \times 0.8^{16} \approx 0.22$$

In R: `dbinom(4, 20, 0.20)`

Answers:

2. c
3. b
4. a,d
5. c
6. b
7. d
8. a
9. c

Explanation: Prior: $P(10\% \text{ yellow}) = 0.5$

Data: $n = 15, k = 3$

$$P(\text{data} \mid p = 10\%) = P(K=3) = \binom{15}{3} \times 0.1^3 \times 0.9^{12} \approx 0.13$$

$$P(\text{data} \mid p = 20\%) = P(K=3) = \binom{15}{3} \times 0.2^3 \times 0.8^{12} \approx 0.25$$

$$\text{Posterior: } P(p = 10\% \mid \text{data}) = 0.13 \times 0.05 / (0.13 \times 0.5 + 0.25 \times 0.5) = 0.34$$