

Problem

Find the function $p(x)$, which maximizes the following functional

$$I(p) = \int_0^\infty e^{\frac{(x-4)^2 - (x+4)^2}{4}} \ln p(x) dx$$

Assuming that $p(x) > 0$ and $\int_0^\infty p(x) dx = 1$